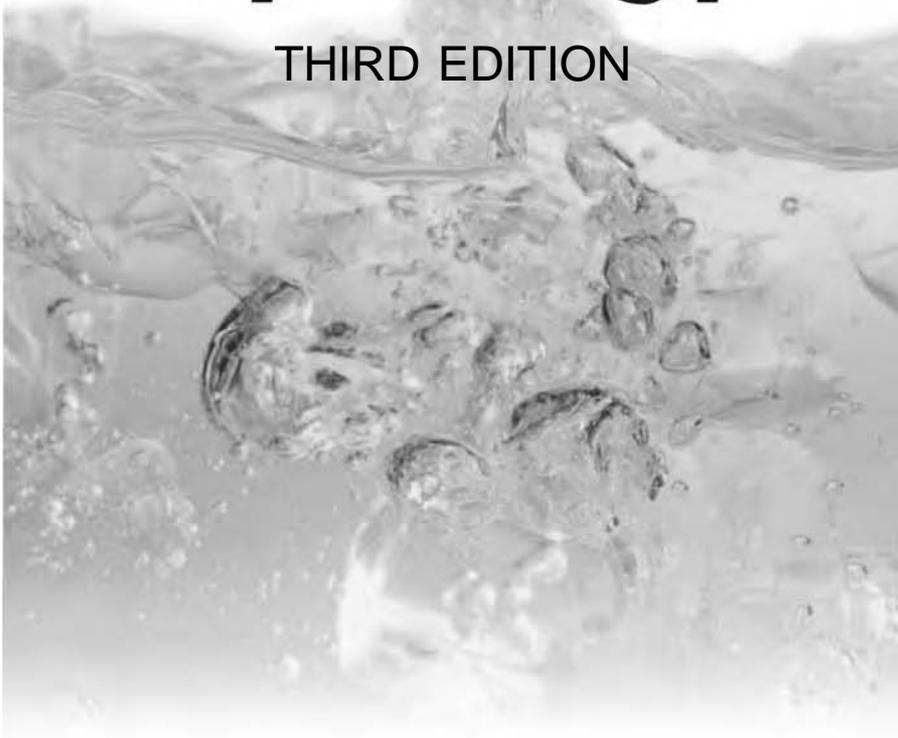# Engineering
Hydrology

THIRD EDITION

About the Author

Dr K Subramanya is a retired Professor of Civil Engineering at the Indian Institute of Technology, Kanpur. He obtained his bachelor's degree in Civil Engineering from Mysore University and a master's degree from the University of Madras. Further, he obtained another master's degree and Ph. D from the University of Alberta, Edmonton, Canada. He has taught at IIT Kanpur for over 30 years and has extensive teaching experience in the area of Hydrology and Water Resources Engineering. During his tenure at IIT Kanpur, Prof. Subramanya worked as Visiting Faculty at the Asian Institute of Technology, Bangkok, for a short while.

He has authored several successful books for McGraw-Hill Education (India). Besides the current book, his other books include *Flow in Open Channels* (2nd Ed., TMH, 1997), and *1000 Solved Problems in Fluid Mechanics* (TMH, 2005). Dr Subramanya has published over eighty technical papers in national and international journals. He has also presented numerous technical papers in conferences. He is a Fellow of the Institution of Engineers (India); Fellow of Indian Society for Hydraulics; Member of Indian Society of Technical Education and Member of Indian Water Resources Association.

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Engineering Hydrology

THIRD EDITION

K Subramanya

Former Professor of Civil Engineering
Indian Institute of Technology
Kanpur

Dedicated
to

My Mother

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Preface to the Third Edition

This is the third edition of the book, the first edition of which was published in 1984. While the second edition of the book is receiving very good response from students and teachers alike, a need was felt to update the book to accommodate changes in technology and practice. Towards this, the book was reviewed thoroughly with a view to enhance its usefulness as a textbook to meet the needs of the present day, as well as that of the near future, in the area of Engineering Hydrology.

Through careful pruning of the second edition and appropriate additions of new material, this edition attempts to make the book useful, catering to a wider range of interests by covering additional subject areas. While the book is essentially an undergraduate textbook in the subject area of Engineering Hydrology, in its present form it also serves as a useful reference book for post-graduate students and field engineers in the domain of Hydrology. The book also meets the need of students taking AMIE examinations. Candidates taking competitive examinations like Central Engineering Services examinations and Central Civil Services examinations will find this book very useful in their preparations related to the topic of hydrology. The book has a unique feature of being India centric; the applications, practices, examples and information about water resources are all aimed at familiarizing the reader to the present-day Indian water resources scene. As such, students and professionals in the related areas of Watershed development, Water Harvesting, Minor Irrigation, Forestry and Hydro-Geology would find this book a useful source material relating to technical issues dealing with water resources in general and hydrology in particular. NGOs working in the water sector would find this book useful in their training activities. The use of mathematics, statistics and probability concepts are kept at the minimal level necessary for understanding the subject matter and emphasis is placed on engineering applications of hydrology.

The significant additions in the present edition are the following:
- The **SCS–CN method of estimating Runoff volume**
- A new chapter entitled **Erosion and Reservoir Sedimentation**
- Thoroughly revised and rewritten section on **infiltration** with descriptions of various infiltration models
- Revised and enlarged section on **Yield of River Basins** to cover current Indian practice
- A new section dealing with **SCS–dimensionless unit hydrograph** and **SCS –Triangular unit hydrograph**
- Improvements to the chapter on Groundwater by including **sections on dug wells** and **recuperation tests of tube wells and dug wells**

- A new section dealing with various aspects of **recharge of groundwater**
- A section on **water harvesting**
- Improved coverage of **droughts**
- Revised information on **water resources of India**
- Additional **worked examples**, **revision questions**, **problems** and **objective questions**

The contents of the book cover essentially the entire subject areas normally covered in an undergraduate course in Engineering Hydrology. Each of the chapters covers not only the basic topics in detail but also includes some advanced topics at an introductory level. The book is designed as a textbook with clear explanations, illustrations and sufficient worked examples. As hydrology is best learned by solving problems, a vast number of them, amounting to more than **200 problems**, **with answers** are provided in the book. Additionally, the sets of **Revision questions** and **Objective questions** (with answers) provided at the end of each chapter help not only in the comprehension of the subject matter but also in preparing well for competitive examinations. Most of the problems can be solved by use of a spreadsheet (such as MS Excel) and this in fact can be made use of in designing interesting teaching and tutorial sessions.

The Online Learning Center of this book can be accessed at http://www.mhhe.com/subramanya/eh3e. The site contains a Solution Manual and PowerPoint Slides for **Instructors**; and Sample Question Papers with Solutions and Sample Case studies for **students**. I have received a large number of feedback, both formally and informally, towards the improvement of the book. The following reviewers of the typescript have provided valuable inputs for the contents of this edition.

Mohammed Jamil	*Department of Civil Engineering, Z H College of Engineering and Technology, Aligarh Muslim University, Aligarh*
Molly Kutty M V	*Department of Civil Engineering, Crescent Engineering College, Chennai*
Thiruvenkatasamy K	*Department of Civil Engineering, Bharath University, Chennai*
Jothi Prakash V	*Department of Civil Engineering, Indian Institute of Technology, Mumbai*
M R Y Putty	*National Institute of Engineering, Mysore*

I would also like to express my sincere thanks to all those who have directly or indirectly helped me in bringing out this revised edition. Comments and suggestions for further improvement of the book would be greatly appreciated. I can be contacted at the following e-mail address: *subramanyak1@gmail.com* .

K Subramanya
April 2008

Preface to the First Edition

Water is vital to life and development in all parts of the world. In Third World countries where the agricultural sector plays a key role in their economic growth, the management of water resources is an item of high priority in their developmental activities. The basic inputs in the evaluation of water resources are from hydrological parameters and the subject of hydrology forms the core in the evaluation and development of water resources. In the civil engineering curriculum, this subject occupies an important position.

During my long teaching experience, I have felt a strong need for a textbook oriented to the Indian environment and written in a simple and lucid style. The present book is a response to the same. This book is intended to serve as a text for a first course in engineering hydrology at the undergraduate level in the civil engineering discipline. Students specializing in various aspects of water-resources engineering, such as water-power engineering and agricultural engineering will find this book useful. This book also serves as a source of useful information to professional engineers working in the area of water-resources evaluation and development.

Engineering hydrology encompasses a wide spectrum of topics and a book like the present one meant for the first course must necessarily maintain a balance in the blend of topics. The subject matter has been developed in a logical and coherent manner and covers the prescribed syllabi of various Indian universities. The mathematical part is kept to the minimum and emphasis is placed on the applicability to field situations relevant to Indian conditions. SI units are used throughout the book.

Designed essentially for a one-semester course, the material in the book is presented in nine chapters. The hydrologic cycle and world-water balance are covered in Chap. 1. Aspects of precipitation, essentially rainfall, are dealt in sufficient detail in Chap. 2. Hydrologic abstractions including evapotranspiration and infiltration arc presented in Chap. 3. Streamflow-measurement techniques and assessment of surface-flow yield of a catchment form the subject matter of Chaps. 4 and 5 respectively. The characteristics of flood hydrographs and the unit hydrograph theory together with an introduction to instantaneous unit hydrograph are covered in sufficient detail with numerous worked examples in Chap. 6. Floods, a topic of considerable importance, constitute the subject matter of Chap. 7 and 8. While in Chap. 7 the flood-peak estimation and frequency studies are described in detail, Chap. 8 deals with the aspects of flood routing, flood control and forecasting. Basic information on the hydrological aspects of groundwater has been covered in Chap. 9.

Numerous worked examples, a set of problems and a set of objective type multiple-choice questions are provided at the end of each chapter to enable the student to gain good comprehension of the subject. Questions and problems included in the book are largely original and are designed to enhance the capabilities of comprehension, analysis and application of the student.

I am grateful to: UNESCO for permission to reproduce several figures from their publication, *Natural Resources of Humid Tropical Asia—Natural Resources Research XII,* ** UNESCO, 1974; the Director-General of Meteorology, India Meteorological Department, Government of India for permission to reproduce several maps; M/s Leupold and Stevens, Inc., Beaverton, Oregon, USA, for photographs of hydrometeorological instruments; M/s Alsthom-Atlantique, Neyrtec, Grenoble France, for photographs of several Neyrtec Instruments; M/s Lawrence and Mayo. (India) Pvt. Ltd., New Delhi for the photograph of a current meter.

Abbreviations

AET	Actual Evapotranspiration
AI	Aridity Index
AMC	Antecedent Moisture Condition
CBIP	Central Board of Irrigation and Power (India)
CGWB	Central Groundwater Board (India)
CN	Curve Number
CWC	Central Water Commission (India)
DAD	Maximum Depth-Area-Duration
DRH	Direct Runoff Hydrograph
DVC	Damodar Valley Corporation
ERH	Effective Rainfall Hyetograph
FAO	Food and Agriculture Organisation
FEM	Finite Element Method
FRL	Full Reservoir Level
GOI	Government of India
IMD	India Meteorological Department
IUH	Instantaneous Unit Hydrograph
KWM	Kentucky Watershed Model
MAI	Moisture Availability Index
MCM	Million Cubic Meter
MDDL	Minimum Drawdown Level
MOC	Method of Characteristics
MSL	Mean Sea Level
MUSLE	Modified Universal Soil Loss Equation
NBSS&LUP	National Bureau of Soil Survey and Land Use Planning
NCIWRD	National Commission for Integrated Water Resources Development (1999)
NRSA	National Remote Sensing Agency
PET	Potential Evapotranspiration
PI	Palmer Index
PMF	Probable Maximum Flood
PMP	Probable Maximum Precipitation
RBA	Rashtriya Barh Ayog (National Flood Commission)
RTWH	Roof Top Water Harvesting
SCS	US Soil Conservation Service
SDR	Sediment Delivery Ratio
SPF	Standard Project Flood

SPS	Standard Project Storm
SWM	Stanford Watershed Model
TMC	Thousand Million Cubic Feet
UH	Unit Hydrograph
UNESCO	United Nations Economic, Social and Cultural Organisation
USLE	Universal Soil Loss Equation
WMO	World Meteorological Organisation

Chapter
1

INTRODUCTION

1.1 INTRODUCTION

Hydrology means the science of water. It is the science that deals with the occurrence, circulation and distribution of water of the earth and earth's atmosphere. As a branch of earth science, it is concerned with the water in streams and lakes, rainfall and snow-fall, snow and ice on the land and water occurring below the earth's surface in the pores of the soil and rocks. In a general sense, hydrology is a very broad subject of an inter-disciplinary nature drawing support from allied sciences, such as meteorology, geology, statistics, chemistry, physics and fluid mechanics.

Hydrology is basically an applied science. To further emphasise the degree of applicability, the subject is sometimes classified as

1. **Scientific hydrology**—the study which is concerned chiefly with academic aspects.
2. **Engineering or applied hydrology**—a study concerned with engineering applications.

In a general sense engineering hydrology deals with (i) estimation of water resources, (ii) the study of processes such as precipitation, runoff, evapotranspiration and their interaction and (iii) the study of problems such as floods and droughts, and strategies to combat them.

This book is an elementary treatment of engineering hydrology with descriptions that aid in a qualitative appreciation and techniques which enable a quantitative evaluation of the hydrologic processes that are of importance to a civil engineer.

1.2 HYDROLOGIC CYCLE

Water occurs on the earth in all its three states, viz. liquid, solid and gaseous, and in various degrees of motion. Evaporation of water from water bodies such as oceans and lakes, formation and movement of clouds, rain and snowfall, streamflow and groundwater movement are some examples of the dynamic aspects of water. The various aspects of water related to the earth can be explained in terms of a cycle known as the *hydrologic cycle.*

Figure 1.1 is a schematic representation of the hydrologic cycle. A convenient starting point to describe the cycle is in the oceans. Water in the oceans evaporate due to the heat energy provided by solar radiation. The water vapour moves upwards and forms clouds. While much of the clouds condense and fall back to the oceans as rain, a part of the clouds is driven to the land areas by winds. There they condense and *precipitate* onto the land mass as rain, snow, hail, sleet, etc. A part of the precipitation
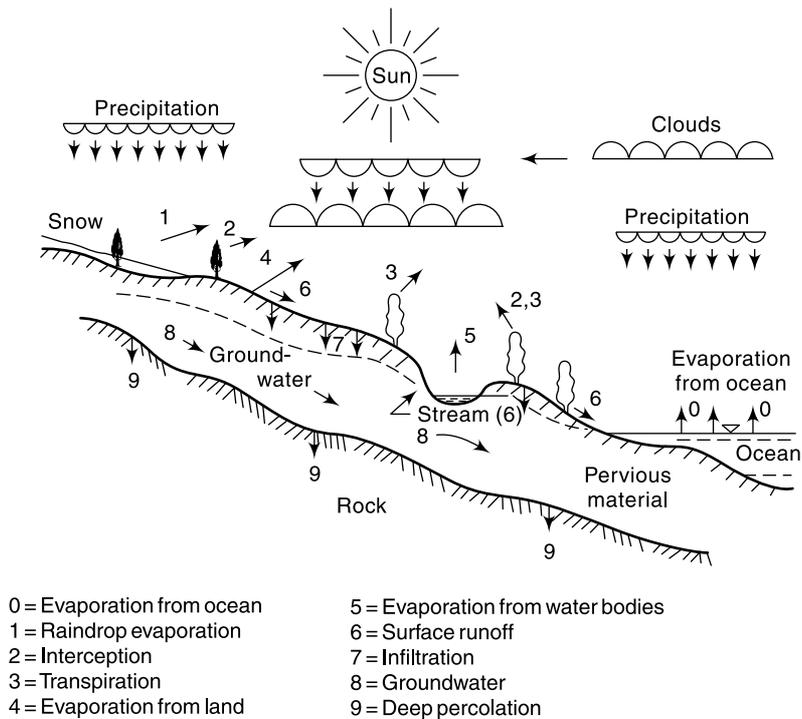
Fig. 1.1   The Hydrologic Cycle

may *evaporate* back to the atmosphere even while falling. Another part may be *intercepted* by vegetation, structures and other such surface modifications from which it may be either evaporated back to atmosphere or move down to the ground surface.

A portion of the water that reaches the ground enters the earth's surface through *infiltration,* enhance the moisture content of the soil and reach the groundwater body. Vegetation sends a portion of the water from under the ground surface back to the atmosphere through the process of *transpiration.* The precipitation reaching the ground surface after meeting the needs of infiltration and evaporation moves down the natural slope over the surface and through a network of gullies, streams and rivers to reach the ocean. The groundwater may come to the surface through springs and other outlets after spending a considerably longer time than the surface flow. The portion of the precipitation which by a variety of paths above and below the surface of the earth reaches the stream channel is called *runoff.* Once it enters a stream channel, runoff becomes *stream flow.*

The sequence of events as above is a simplistic picture of a very complex cycle that has been taking place since the formation of the earth. It is seen that the hydrologic cycle is a very vast and complicated cycle in which there are a large number of paths of varying time scales. Further, it is a continuous recirculating cycle in the sense that there is neither a beginning nor an end or a pause. Each path of the hydrologic cycle involves one or more of the following aspects: (i) transportation of water, (ii) temporary storage and (iii) change of state. For example, (a) the process of rainfall has the

change of state and transportation and (b) the groundwater path has storage and transportation aspects.

The main components of the hydrologic cycle can be broadly classified as *transportation (flow) components* and *storage components* as below:

Transportation components	Storage components
Precipitation	Storage on the land surface (Depression storage, Ponds, Lakes, Reservoirs, etc)
Evaporation	Soil moisture storage
Transpiration	Groundwater storage
Infiltration	
Runoff	

Schematically the interdependency of the transportation components can be represented as in Fig. 1.2. The quantities of water going through various individual paths of the hydrological cycle in a given system can be described by the continuity principle known as *water budget equation* or *hydrologic equation.*

It is important to note that the total water resources of the earth are constant and the sun is the source of energy for the hydrologic

Fig. 1.2 Transportation Components of the Hydrologic Cycle

cycle. A recognition of the various processes such as evaporation, precipitation and groundwater flow helps one to study the science of hydrology in a systematic way. Also, one realises that man can interfere with virtually any part of the hydrologic cycle, e.g. through artificial rain, evaporation suppression, change of vegetal cover and land use, extraction of groundwater, etc. Interference at one stage can cause serious repercussions at some other stage of the cycle.

The hydrological cycle has important influences in a variety of fields including agriculture, forestry, geography, economics, sociology and political scene. Engineering applications of the knowledge of the hydrologic cycle, and hence of the subjects of hydrology, are found in the design and operation of projects dealing with water supply, irrigation and drainage, water power, flood control, navigation, coastal works, salinity control and recreational uses of water.

1.3   WATER BUDGET EQUATION

Catchment Area

The area of land draining into a stream or a water course at a given location is known as *catchment area.* It is also called as *drainage area* or *drainage basin.* In USA, it is known as *watershed.* A catchment area is separated form its neighbouring areas by a

ridge called *divide* in USA and *watershed* in UK (Fig. 1.3). The areal extent of the catchment is obtained by tracing the ridge on a topographic map to delineate the catchment and measuring the area by a *planimeter*. It is obvious that for a river while mentioning the catchment area the station to which it pertains (Fig. 1.3) must also be mentioned. It is normal to assume the groundwater divide to coincide with the surface divide. Thus, the catchment area affords a logical and convenient unit to study various aspects relating to the hydrology and water resources of a region.

Fig. 1.3 Schematic Sketch of Catchment of River A at Station M

Further it is probably the singlemost important drainage characteristic used in hydrological analysis and design.

WATER BUDGET EQUATION

For a given problem area, say a catchment, in an interval of time Δt, the continuity equation for water in its various phases is written as

Mass inflow – mass outflow = change in mass storage

If the density of the inflow, outflow and storage volumes are the same

$$\Psi_i - \Psi_0 = \Delta S \qquad (1.1)$$

where Ψ_i = inflow volume of water into the problem area during the time period, Ψ_0 = outflow volume of water from the problem area during the time period, and ΔS = change in the storage of the water volume over and under the given area during the given period. In applying this continuity equation [Eq. (1.1)] to the paths of the hydrologic cycle involving change of state, the volumes considered are the equivalent volumes of water at a reference temperature. In hydrologic calculations, the volumes are often expressed as average depths over the catchment area. Thus, for example, if the annual stream flow from a 10 km^2 catchment is 10^7 m^3, it corresponds to a depth of

$\left(\dfrac{10^7}{10 \times 10^6} \right)$ = 1 m = 100 cm. Rainfall, evaporation and often runoff volumes are

expressed in units of depth over the catchment.

While realizing that all the terms in a hydrological water budget may not be known to the same degree of accuracy, an expression for the water budget of a catchment for a time interval Δt is written as

$$P - R - G - E - T = \Delta S \qquad (1.2\text{-a})$$

In this P = precipitation, R = surface runoff, G = net groundwater flow out of the catchment, E = evaporation, T = transpiration and ΔS = change in storage.

The storage S consists of three components as

$$S = S_s + S_{sm} + S_g$$

where S_s = surface water storage
          S_{sm} = water in storage as soil moisture and
          S_g = water in storage as groundwater.

Thus in Eq. (1.2-a) $\Delta S = \Delta S_s + \Delta S_{sm} + \Delta S_g$

All terms in Eq. (1.2-a) have the dimensions of volume. Note that all these terms can be expressed as depth over the catchment area (e.g. in centimetres), and in fact this is a very common unit.

In terms of rainfall–runoff relationship, Eq. (1.2-a) can be represented as

$$R = P - L \qquad\qquad (1.2\text{-}b)$$

where L = Losses = water not available to runoff due to infiltration (causing addition to soil moisture and groundwater storage), evaporation, transpiration and surface storage. Details of various components of the water budget equation are discussed in subsequent chapters. Note that in Eqs (1.2-a and b) the net import of water into the catchment, from sources outside the catchment, by action of man is assumed to be zero.

EXAMPLE 1.1 *A lake had a water surface elevation of 103.200 m above datum at the beginning of a certain month. In that month the lake received an average inflow of 6.0 m^3/s from surface runoff sources. In the same period the outflow from the lake had an average value of 6.5 m^3/s. Further, in that month, the lake received a rainfall of 145 mm and the evaporation from the lake surface was estimated as 6.10 cm. Write the water budget equation for the lake and calculate the water surface elevation of the lake at the end of the month. The average lake surface area can be taken as 5000 ha. Assume that there is no contribution to or from the groundwater storage.*

SOLUTION: In a time interval Δt the water budget for the lake can be written as
Input volume – output volume = change in storage of the lake

$$(\bar{I}\Delta t + PA) - (\bar{Q}\Delta t + EA) = \Delta S$$

where $\bar{I}$ = average rate of inflow of water into the lake, $\bar{Q}$ = average rate of outflow from the lake, P = precipitation, E = evaporation, A = average surface area of the lake and ΔS = change in storage volume of the lake.
Here $\Delta t = 1$ month $= 30 \times 24 \times 60 \times 60 = 2.592 \times 10^6$ s $= 2.592$ Ms
In one month:

$$\text{Inflow volume} = \bar{I}\Delta t = 6.0 \times 2.592 = 15.552 \text{ M m}^3$$

$$\text{Outflow volume} = \bar{Q}\Delta t = 6.5 \times 2.592 = 16.848 \text{ M m}^3$$

$$\text{Input due to precipitation} = PA = \frac{14.5 \times 5000 \times 100 \times 100}{100 \times 10^6} \text{ M m}^3 = 7.25 \text{ M m}^3$$

$$\text{Outflow due to evaporation} = EA = \frac{6.10}{100} \times \frac{5000 \times 100 \times 100}{10^6} = 3.05 \text{ M m}^3$$

Hence $\Delta S = 15.552 + 7.25 - 16.848 - 3.05 = 2.904 \text{ M m}^3$

Change in elevation $\Delta z = \dfrac{\Delta S}{A} = \dfrac{2.904 \times 10^6}{5000 \times 100 \times 100} = 0.058 \text{ m}$

New water surface elevation at the end of the month = 103.200 + 0.058
$$= 103.258 \text{ m above the datum.}$$

EXAMPLE 1.2 *A small catchment of area 150 ha received a rainfall of 10.5 cm in 90 minutes due to a storm. At the outlet of the catchment, the stream draining the catchment was dry before the storm and experienced a runoff lasting for 10 hours with an average discharge of 1.5 m^3/s. The stream was again dry after the runoff event. (a) What is the amount of water which was not available to runoff due to combined effect of infiltration, evaporation and transpiration? What is the ratio of runoff to precipitation?*

SOLUTION: The water budget equation for the catchment in a time Δt is

$$R = P - L \tag{1.2-b}$$

where L = Losses = water not available to runoff due to infiltration (causing addition to soil moisture and groundwater storage), evaporation, transpiration and surface storage. In the present case Δt = duration of the runoff = 10 hours.

    Note that the rainfall occurred in the first 90 minutes and the rest 8.5 hours the precipitation was zero.

(a) P = Input due to precipitation in 10 hours
      $= 150 \times 100 \times 100 \times (10.5/100) = 157{,}500$ m^3
    R = runoff volume = outflow volume at the catchment outlet in 10 hours
      $= 1.5 \times 10 \times 60 \times 60 = 54{,}000$ m^3
    Hence losses $L = 157{,}500 - 54{,}000 = 103{,}500$ m^3

(b)   Runoff/rainfall = $54{,}000/157{,}500 = 0.343$
    (This ratio is known as *runoff coefficient* and is discussed in Chapter 5)

1.4   WORLD WATER BALANCE

The total quantity of water in the world is estimated to be about 1386 million cubic kilometres (M km^3). About 96.5% of this water is contained in the oceans as saline water. Some of the water on the land amounting to about 1% of the total water is also saline. Thus only about 35.0 M km^3 of fresh water is available. Out of this about 10.6 M km^3 is both liquid and fresh and the remaining 24.4 M km^3 is contained in frozen state as ice in the polar regions and on mountain tops and glaciers. An estimated distribution of water on the earth is given in Table 1.1.

Table 1.1   Estimated World Water Quantities

Item	Area (M km^2)	Volume (M km^3)	Percent total water	Percent fresh water
1. Oceans	361.3	1338.0	96.5	—
2. Groundwater				
(a) fresh	134.8	10.530	0.76	30.1
(b) saline	134.8	12.870	0.93	—
3. Soil moisture	82.0	0.0165	0.0012	0.05
4. Polar ice	16.0	24.0235	1.7	68.6
5. Other ice and snow	0.3	0.3406	0.025	1.0
6. Lakes				
(a) fresh	1.2	0.0910	0.007	0.26
(b) saline	0.8	0.0854	0.006	—
7. Marshes	2.7	0.01147	0.0008	0.03
8. Rivers	148.8	0.00212	0.0002	0.006
9. Biological water	510.0	0.00112	0.0001	0.003
10. Atmospheric water	510.0	0.01290	0.001	0.04
Total: (a) All kinds of water	510.0	1386.0	100.0	
(b) Fresh water	148.8	35.0	2.5	100.0

Table from WORLD WATER BALANCE AND WATER RESOURCES OF THE EARTH, © UNESCO, 1975. Reproduced by the permission of UNESCO.

The global annual water balance is shown in Table 1.2.

Table 1.2 Global Annual Water Balance

Item	Ocean	Land
1. Area (M km^2)	361.30	148.8
2. Precipitation (km^3/year)	458,000	119,000
(mm/year)	1270	800
3. Evaporation (km^3/year)	505,000	72,000
(mm/year)	1400	484
4. Runoff to ocean		
(i) Rivers (km^3/year)		44,700
(ii) Groundwater (km^3/year)		2,200
Total Runoff (km^3/year)		47,000
(mm/year)		316

It is seen from Table 1.2 that the annual evaporation from the world's oceans and inland areas are 0.505 and 0.072 M km^3 respectively. Thus, over the oceans about 9% more water evaporates than that falls back as precipitation. Correspondingly, there will be excess precipitation over evaporation on the land mass. The differential, which is estimated to be about 0.047 M km^3 is the runoff from land mass to oceans and groundwater outflow to oceans. It is interesting to know that less than 4% of this total river flow is used for irrigation and the rest flows down to sea.

These estimates are only approximate and the results from different studies vary; the chief cause being the difficulty in obtaining adequate and reliable data on a global scale.

The volume in various phases of the hydrologic cycle (Table 1.1) as also the rate of flow in that phase (Table 1.2) do vary considerably. The average duration of a particle of water to pass through a phase of the hydrologic cycle is known as the *residence time* of that phase. It could be calculated by dividing the volume of water in the phase by the average flow rate in that phase. For example, by assuming that all the surface runoff to the oceans comes from the rivers,

From Table 1.1, the volume of
water in the rivers of the world   = 0.00212 M km^3
From Table 1.2, the average flow rate
of water in global rivers   = 44700 km^3/year
Hence residence time of global rivers, T_r = 2120/44700 = 0.0474 year = 17.3 days.

Similarly, the residence time for other phases of the hydrological cycle can be calculated (Prob. 1.6). It will be found that the value of T_r varies from phase to phase. In a general sense the shorter the residence time the greater is the difficulty in predicting the behaviour of that phase of the hydrologic cycle.

Annual water balance studies of the sub-areas of the world indicate interesting facts. The water balance of the continental land mass is shown in Table 1.3(a). It is interesting to see from this table that Africa, in spite of its equatorial forest zones, is

the driest continent in the world with only 20% of the precipitation going as runoff. On the other hand, North America and Europe emerge as continents with highest runoff. Extending this type of analysis to a smaller land mass, viz. the Indian subcontinent, the long term average runoff for India is found to be 46%.

Table 1.3(a)   Water Balance of Continents[2] mm/year

Continent	Area (M km^2)	Precipitation	Total runoff	Runoff as % of precipitation	Evaporation
Africa	30.3	686	139	20	547
Asia	45.0	726	293	40	433
Australia	8.7	736	226	30	510
Europe	9.8	734	319	43	415
N. America	20.7	670	287	43	383
S. America	17.8	1648	583	35	1065

Water balance studies on the oceans indicate that there is considerable transfer of water between the oceans and the evaporation and precipitation values vary from one ocean to another (Table 1.3(b)).

Table 1.3(b)   Water Balance of Oceans[2] mm/year

Ocean	Area (M km^2)	Precipitation	Inflow from adjacent continents	Evaporation	Water exchange with other oceans
Atlantic	107	780	200	1040	−60
Arctic	12	240	230	120	350
Indian	75	1010	70	1380	−300
Pacific	167	1210	60	1140	130

Each year the rivers of the world discharge about 44,700 km^3 of water into the oceans. This amounts to an annual average flow of 1.417 Mm^3/s. The world's largest river, the Amazon, has an annual average discharge of 200,000 m^3/s, i.e. one-seventh of the world's annual average value. India's largest river, the Brahmaputra, and the second largest, the Ganga, flow into the Bay of Bengal with a mean annual average discharges of 16,200 m^3/s and 15,600 m^3/s respectively.

1.5   HISTORY OF HYDROLOGY

Water is the prime requirement for the existence of life and thus it has been man's endeavour from time immemorial to utilise the available water resources. History has instances of civilizations that flourished with the availability of dependable water supplies and then collapsed when the water supply failed. Numerous references exist in Vedic literature to groundwater availability and its utility. During 3000 BC groundwater development through wells was known to the people of the Indus Valley civilizations as revealed by archaeological excavations at Mohenjodaro. Quotations in ancient Hindu scriptures indicate the existence of the knowledge of the hydrologic cycle even as far back as the Vedic period. The first description of the raingauge and its use is contained

in the *Arthashastra* by Chanakya (300 BC). Varahamihira's (AD 505–587) *Brihatsamhita* contains descriptions of the raingauge, wind vane and prediction procedures for rainfall. Egyptians knew the importance of the stage measurement of rivers and records of the stages of the Nile dating back to 1800 BC have been located. The knowledge of the hydrologic cycle came to be known to Europe much later, around AD 1500.

Chow[1] classifies the history of hydrology into eight periods as:

1. Period of speculation—prior to AD 1400
2. Period of observation—1400–1600
3. Period of measurement—1600–1700
4. Period of experimentation—1700–1800
5. Period of modernization—1800–1900
6. Period of empiricism—1900–1930
7. Period of rationalization—1930–1950
8. Period of theorization—1950–to–date

Most of the present-day science of hydrology has been developed since 1930, thus giving hydrology the status of a young science. The worldwide activities in water-resources development since the last few decades by both developed and developing countries aided by rapid advances in instrumentation for data acquisition and in the computer facilities for data analysis have contributed towards the rapid growth rate of this young science.

1.6 APPLICATIONS IN ENGINEERING

Hydrology finds its greatest application in the design and operation of water-resources engineering projects, such as those for (i) irrigation, (ii) water supply, (iii) flood control, (iv) water power, and (v) navigation. In all these projects hydrological investigations for the proper assessment of the following factors are necessary:

1. The capacity of storage structures such as reservoirs.
2. The magnitude of flood flows to enable safe disposal of the excess flow.
3. The minimum flow and quantity of flow available at various seasons.
4. The interaction of the flood wave and hydraulic structures, such as levees, reservoirs, barrages and bridges.

The hydrological study of a project should necessarily precede structural and other detailed design studies. It involves the collection of relevant data and analysis of the data by applying the principles and theories of hydrology to seek solutions to practical problems.

Many important projects in the past have failed due to improper assessment of the hydrological factors. Some typical failures of hydraulic structures are: (i) overtopping and consequent failure of an earthen dam due to an inadequate spillway capacity, (ii) failure of bridges and culverts due to excess flood flow and (iii) inability of a large reservoir to fill up with water due to overestimation of the stream flow. Such failure, often called *hydrologic failures* underscore the uncertainty aspect inherent in hydrological studies.

Various phases of the hydrological cycle, such as rainfall, runoff, evaporation and transpiration are all nonuniformly distributed both in time and space. Further, practically all hydrologic phenomena are complex and at the present level of knowledge, they can at best be interpreted with the aid of probability concepts. Hydrological events are treated as random processes and the historical data relating to the event are analysed by statistical methods to obtain information on probabilities of occurrence of various events. The probability analysis of hydrologic data is an important component of present-day hydrological studies and enables the engineer to take suitable design decisions consistent with economic and other criteria to be taken in a given project.

1.7   SOURCES OF DATA

Depending upon the problem at hand, a hydrologist would require data relating to the various relevant phases of the hydrological cycle playing on the problem catchment. The data normally required in the studies are:
- Weather records—temperature, humidity and wind velocity
- Precipitation data
- Stream flow records
- Evaporation and evapotranspiration data
- Infiltration characteristics of the study area
- Soils of the area
- Land use and land cover
- Groundwater characteristics
- Physical and geological characteristics of the area
- Water quality data

In India, hydro-meteorological data are collected by the India Meteorological Department (IMD) and by some state government agencies. The Central Water Commission (CWC) monitors flow in major rivers of the country. Stream flow data of various rivers and streams are usually available from the State Water Resources/Irrigation Department. Groundwater data will normally be available with Central Groundwater Board (CGWB) and state Government groundwater development agencies. Data relating evapotranspiration and infiltration characteristics of soils will be available with State Government organizations such as Department of Agriculture, Department of Watershed development and Irrigation department. The physical features of the study area have to be obtained from a study of topographical maps available with the Survey of India. The information relating to geological characteristics of the basin under study will be available with the Geological Survey of India and the state Geology Directorate. Information relating to soils at an area are available from relevant maps of National Bureau of Soil Survey and Land Use Planning (NBSS&LUP), 1996. Further additional or specific data can be obtained from the state Agriculture Department and the state Watershed Development Department. Land use and land cover data would generally be available from state Remote sensing Agencies. Specific details will have to be derived through interpretation of multi-spectral multi-season satellite images available from National Remote Sensing Agency (NRSA) of Government of India. Central and State Pollution Control Boards, CWC and CGWB collect water quality data.

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3. UNESCO, "World Water Balance and Water Resources of the Earth", *Studies and Reports in Hydrology,* 25, UNESCO, Paris, France, 1978.
4. Van der Leeden, *Water Resources of the World,* Water Information Center, Port Washington, N.Y., USA, 1975.

REVISION QUESTIONS

1.1 Describe the Hydrologic cycle. Explain briefly the man's interference in various parts of this cycle.
1.2 Discuss the hydrological water budget with the aid of examples.
1.3 What are the significant features of global water balance studies?
1.4 List the major activities in which hydrological studies are important.
1.5 Describe briefly the sources of hydrological data in India.

PROBLEMS

1.1 Two and half centimetres of rain per day over an area of 200 km^2 is equivalent to average rate of input of how many cubic metres per second of water to that area?

1.2 A catchment area of 140 km^2 received 120 cm of rainfall in a year. At the outlet of the catchment the flow in the stream draining the catchment was found to have an average rate of 2.0 m^3/s for 3 months, 3.0 m^3/s for 6 months and 5.0 m^3/s for 3 months. (i) What is the runoff coefficient of the catchment? (ii) If the afforestation of the catchment reduces the runoff coefficient to 0.50, what is the increase in the abstraction from precipitation due to infiltration, evaporation and transpiration, for the same annual rainfall of 120 cm?

1.3 Estimate the constant rate of withdrawal from a 1375 ha reservoir in a month of 30 days during which the reservoir level dropped by 0.75 m in spite of an average inflow into the reservoir of 0.5 Mm^3/day. During the month the average seepage loss from the reservoir was 2.5 cm, total precipitation on the reservoir was 18.5 cm and the total evaporation was 9.5 cm.

1.4 A river reach had a flood wave passing through it. At a given instant the storage of water in the reach was estimated as 15.5 ha.m. What would be the storage in the reach after an interval of 3 hours if the average inflow and outflow during the time period are 14.2 m^3/s and 10.6 m^3/s respectively?

1.5 A catchment has four sub-areas. The annual precipitation and evaporation from each of the sub-areas are given below.
Assume that there is no change in the groundwater storage on an annual basis and calculate for the whole catchment the values of annual average (i) precipitation, and (ii) evaporation. What are the annual runoff coefficients for the sub-areas and for the total catchment taken as a whole?

Sub-area	Area Mm^2	Annual precipitation mm	Annual evaporation mm
A	10.7	1030	530
B	3.0	830	438
C	8.2	900	430
D	17.0	1300	600

1.6 Estimate the residence time of
   (a) Global atmospheric moisture.
   (b) Global groundwater by assuming that only the fresh groundwater runs off to the oceans.
   (c) Ocean water.

───────────┤ OBJECTIVE QUESTIONS ├───────────

1.1 The percentage of earth covered by oceans is about
   (a) 31%   (b) 51%   (c) 71%   (d) 97%
1.2 The percentage of total quantity of water in the world that is saline is about
   (a) 71%   (b) 33%   (c) 67%   (d) 97%
1.3 The percentage of total quantity of fresh water in the world available in the liquid form
   is about
   (a) 30%   (b) 70%   (c) 11%   (d) 51%
1.4 If the average annual rainfall and evaporation over land masses and oceans of the earth
   are considered it would be found that
   (a) over the land mass the annual evaporation is the same as the annual precipitation
   (b) about 9% more water evaporates from the oceans than what falls back on them as
       precipitation
   (c) over the ocean about 19% more rain falls than what is evaporated
   (d) over the oceans about 19% more water evaporates than what falls back on them as
       precipitation.
1.5 Considering the ratio of annual precipitation to runoff $= r_0$ for all the continents on the
   earth,
   (a) Asia has the largest value of the ratio r_0.
   (b) Europe has the smallest value of r_0.
   (c) Africa has the smallest value of r_0.
   (d) Australia has the smallest value of r_0.
1.6 In the hydrological cycle the average residence time of water in the global
   (a) atmospheric moisture is larger than that in the global rivers
   (b) oceans is smaller than that of the global groundwater
   (c) rivers is larger than that of the global groundwater
   (d) oceans is larger than that of the global groundwater.
1.7 A watershed has an area of 300 ha. Due to a 10 cm rainfall event over the watershed a
   stream flow is generated and at the outlet of the watershed it lasts for 10 hours. Assum-
   ing a runoff/rainfall ratio of 0.20 for this event, the average stream flow rate at the outlet
   in this period of 10 hours is
   (a) 1.33 m^3/s   (b) 16.7 m^3/s   (c) 100 m^3/minute   (d) 60,000 m^3/h
1.8 Rainfall of intensity of 20 mm/h occurred over a watershed of area 100 ha for a duration
   of 6 h. measured direct runoff volume in the stream draining the watershed was found to
   be 30,000 m^3. The precipitation not available to runoff in this case is
   (a) 9 cm   (b) 3 cm   (c) 17.5 mm   (d) 5 mm
1.9 A catchment of area 120 km^2 has three distinct zones as below:

Zone	Area (km^2)	Annual runoff (cm)
A	61	52
B	39	42
C	20	32

The annual runoff from the catchment, is
   (a) 126.0 cm   (b) 42.0 cm   (c) 45.4 cm   (d) 47.3 cm

Chapter
2

PRECIPITATION

2.1 INTRODUCTION

The term *precipitation* denotes all forms of water that reach the earth from the atmosphere. The usual forms are rainfall, snowfall, hail, frost and dew. Of all these, only the first two contribute significant amounts of water. Rainfall being the predominant form of precipitation causing stream flow, especially the flood flow in a majority of rivers in India, unless otherwise stated the term *rainfall* is used in this book synonymously with precipitation. The magnitude of precipitation varies with time and space. Differences in the magnitude of rainfall in various parts of a country at a given time and variations of rainfall at a place in various seasons of the year are obvious and need no elaboration. It is this variation that is responsible for many hydrological problems, such as floods and droughts. The study of precipitation forms a major portion of the subject of hydrometeorology. In this chapter, a brief introduction is given to familiarize the engineer with important aspects of rainfall, and, in particular, with the collection and analysis of rainfall data.

For precipitation to form: (i) the atmosphere must have moisture, (ii) there must be sufficient nuclei present to aid condensation, (iii) weather conditions must be good for condensation of water vapour to take place, and (iv) the products of condensation must reach the earth. Under proper weather conditions, the water vapour condenses over nuclei to form tiny water droplets of sizes less than 0.1 mm in diameter. The nuclei are usually salt particles or products of combustion and are normally available in plenty. Wind speed facilitates the movement of clouds while its turbulence retains the water droplets in suspension. Water droplets in a cloud are somewhat similar to the particles in a colloidal suspension. Precipitation results when water droplets come together and coalesce to form larger drops that can drop down. A considerable part of this precipitation gets evaporated back to the atmosphere. The net precipitation at a place and its form depend upon a number of meteorological factors, such as the weather elements like wind, temperature, humidity and pressure in the volume region enclosing the clouds and the ground surface at the given place.

2.2 FORMS OF PRECIPITATION

Some of the common forms of precipitation are: rain, snow, drizzle, glaze, sleet and hail.

RAIN   It is the principal form of precipitation in India. The term *rainfall* is used to describe precipitations in the form of water drops of sizes larger than 0.5 mm. The maximum size of a raindrop is about 6 mm. Any drop larger in size than this tends to

break up into drops of smaller sizes during its fall from the clouds. On the basis of its intensity, rainfall is classified as:

Type	Intensity
1. Light rain	trace to 2.5 mm/h
2. Moderate rain	2.5 mm/h to 7.5 mm/h
3. Heavy rain	> 7.5 mm/h

SNOW   *Snow* is another important form of precipitation. Snow consists of ice crystals which usually combine to form flakes. When fresh, snow has an initial density varying from 0.06 to 0.15 g/cm^3 and it is usual to assume an average density of 0.1 g/cm^3. In India, snow occurs only in the Himalayan regions.

DRIZZLE   A fine sprinkle of numerous water droplets of size less than 0.5 mm and intensity less than 1 mm/h is known as drizzle. In this the drops are so small that they appear to float in the air.

GLAZE   When rain or drizzle comes in contact with cold ground at around 0º C, the water drops freeze to form an ice coating called *glaze* or *freezing rain.*

SLEET   It is frozen raindrops of transparent grains which form when rain falls through air at subfreezing temperature. In Britain, *sleet* denotes precipitation of snow and rain simultaneously.

HAIL   It is a showery precipitation in the form of irregular pellets or lumps of ice of size more than 8 mm. Hails occur in violent thunderstorms in which vertical currents are very strong.

2.3   WEATHER SYSTEMS FOR PRECIPITATION

For the formation of clouds and subsequent precipitation, it is necessary that the moist air masses cool to form condensation. This is normally accomplished by adiabatic cooling of moist air through a process of being lifted to higher altitudes. Some of the terms and processes connected with the weather systems associated with precipitation are given below.

FRONT   A *front* is the interface between two distinct air masses. Under certain favourable conditions when a warm air mass and cold air mass meet, the warmer air mass is lifted over the colder one with the formation of a front. The ascending warmer air cools adiabatically with the consequent formation of clouds and precipitation.

CYCLONE   A *cyclone* is a large low pressure region with circular wind motion. Two types of cyclones are recognised: tropical cyclones and extratropical cyclones.

Tropical cyclone: A tropical cyclone, also called *cyclone* in India, *hurricane* in USA and *typhoon* in South-East Asia, is a wind system with an intensely strong depression with MSL pressures sometimes below 915 mbars The normal areal extent of a cyclone is about 100–200 km in diameter. The isobars are closely spaced and the winds are anticlockwise in the northern hemisphere. The centre of the storm, called the *eye,* which may extend to about 10–50 km in diameter, will be relatively quiet. However, right outside the eye, very strong winds/reaching to as much as 200 kmph

exist. The wind speed gradually decreases towards the outer edge. The pressure also increases outwards (Fig. 2.1). The rainfall will normally be heavy in the entire area occupied by the cyclone.
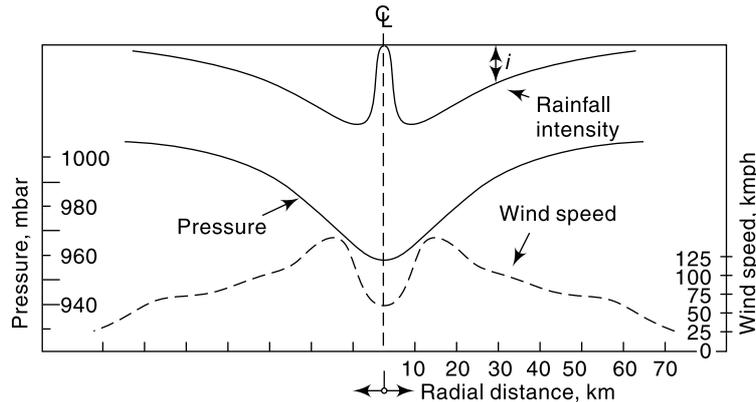
Fig. 2.1 Schematic Section of a Tropical Cyclone

During summer months, tropical cyclones originate in the open ocean at around 5–10° latitude and move at speeds of about 10–30 kmph to higher latitudes in an irregular path. They derive their energy from the latent heat of condensation of ocean water vapour and increase in size as they move on oceans. When they move on land the source of energy is cut off and the cyclone dissipates its energy very fast. Hence, the intensity of the storm decreases rapidly. Tropical cyclones cause heavy damage to life and property on their land path and intense rainfall and heavy floods in streams are its usual consequences. Tropical cyclones give moderate to excessive precipitation over very large areas, of the order of 10^3 km^2, for several days.

Extratropical Cyclone: These are cyclones formed in locations outside the tropical zone. Associated with a frontal system, they possess a strong counter-clockwise wind circulation in the northern hemisphere. The magnitude of precipitation and wind velocities are relatively lower than those of a tropical cyclone. However, the duration of precipitation is usually longer and the areal extent also is larger.

ANTICYCLONES   These are regions of high pressure, usually of large areal extent. The weather is usually calm at the centre. Anticyclones cause clockwise wind circulations in the northern hemisphere. Winds are of moderate speed, and at the outer edges, cloudy and precipitation conditions exist.

CONVECTIVE PRECIPITATION   In this type of precipitation a packet of air which is warmer than the surrounding air due to localised heating rises because of its lesser density. Air from cooler surroundings flows to take up its place thus setting up a convective cell. The warm air continues to rise, undergoes cooling and results in precipitation. Depending upon the moisture, thermal and other conditions light showers to thunderstorms can be expected in convective precipitation. Usually the areal extent of such rains is small, being limited to a diameter of about 10 km.

OROGRAPHIC PRECIPITATION   The moist air masses may get lifted-up to higher altitudes due to the presence of mountain barriers and consequently undergo cooling,

condensation and precipitation. Such a precipitation is known as *Orographic precipitation.* Thus in mountain ranges, the windward slopes have heavy precipitation and the leeward slopes light rainfall.

2.4 CHARACTERISTICS OF PRECIPITATION IN INDIA

From the point of view of climate the Indian subcontinent can be considered to have two major seasons and two transitional periods as:

- South-west monsoon (June–September)
- Transition-I, post-monsoon (October–November)
- Winter season (December–February)
- Transition-II, Summer, (March–May)

The chief precipitation characteristics of these seasons are given below.

SOUTH-WEST MONSOON (JUNE–SEPTEMBER)

The south-west monsoon (popularly known as *monsoon*) is the principal rainy season of India when over 75% of the annual rainfall is received over a major portion of the country. Excepting the south-eastern part of the peninsula and Jammu and Kashmir, for the rest of the country the south-west monsoon is the principal source of rain with July as the month which has maximum rain. The monsoon originates in the Indian ocean and heralds its appearance in the southern part of Kerala by the end of May. The onset of monsoon is accompanied by high south-westerly winds at speeds of 30–70 kmph and low-pressure regions at the advancing edge. The monsoon winds advance across the country in two branches: (i) the Arabian sea branch, and (ii) the Bay of Bengal branch. The former sets in at the extreme southern part of Kerala and the latter at Assam, almost simultaneously in the first week of June. The Bay branch first covers the north-eastern regions of the country and turns westwards to advance into Bihar and UP. The Arabian sea branch moves northwards over Karnataka, Maharashtra and Gujarat. Both the branches reach Delhi around the same time by about the fourth week of June. A low-pressure region known as *monsoon trough* is formed between the two branches. The trough extends from the Bay of Bengal to Rajasthan and the precipitation pattern over the country is generally determined by its position. The monsoon winds increase from June to July and begin to weaken in September. The withdrawal of the monsoon, marked by a substantial rainfall activity starts in September in the northern part of the country. The onset and withdrawal of the monsoon at various parts of the country are shown in Fig. 2.2(a) and Fig. 2.2(b).

The monsoon is not a period of continuous rainfall. The weather is generally cloudy with frequent spells of rainfall. Heavy rainfall activity in various parts of the country owing to the passage of low pressure regions is common. Depressions formed in the Bay of Bengal at a frequency of 2–3 per month move along the trough causing excessive precipitation of about 100–200 mm per day. Breaks of about a week in which the rainfall activity is the least is another feature of the monsoon. The south-west monsoon rainfall over the country is indicated in Fig. 2.3. As seen from this figure, the heavy rainfall areas are Assam and the north-eastern region with 200–400 cm, west coast and western ghats with 200–300 cm, West Bengal with 120–160 cm, UP, Haryana and the Punjab with 100–120 cm. The long term average monsoon rainfall over the country is estimated as 95.0 cm.
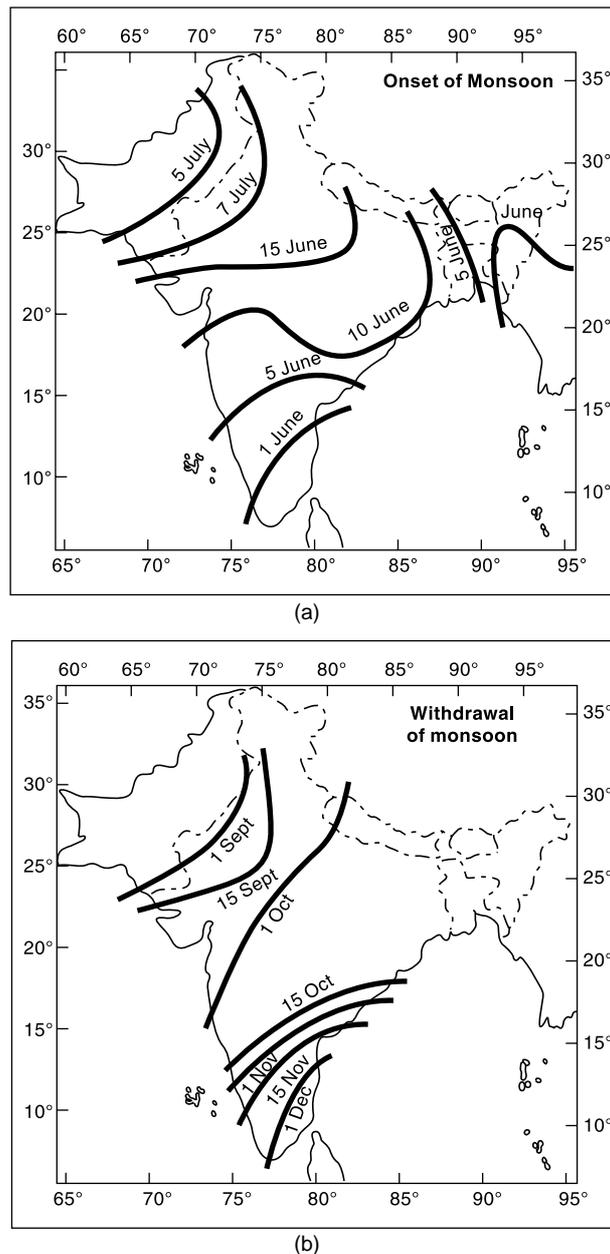
Fig. 2.2   (a) Normal Dates of Onset of Monsoon, (b) Normal Dates of With-
drawal of Monsoon
(Reproduced from *Natural Resources of Humid Tropical Asia – Natural
Resources Research, XII.* © UNESCO, 1974, with permission of
UNESCO)

The territorial waters of India extend into the sea to a distance of 200 nautical miles measured from the appro-
priate baseline
   Responsibility for the correctness of the internal details on the map rests with the publisher.
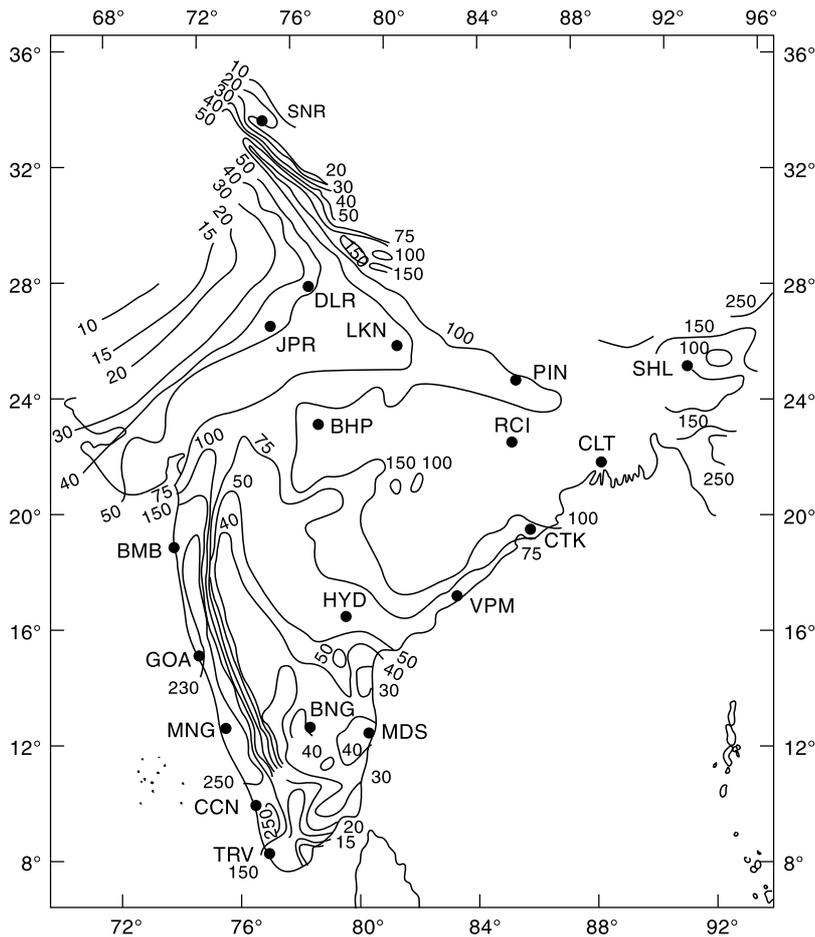
Fig. 2.3 Southwest Monsoon Rainfall (cm) over India and Neighbourhood
(Reproduced with permission from India Meteorological Department)

Based upon Survey of India map with the permission of the Surveyor General of India © Government of India Copyright 1984

The territorial waters of India extend into the sea to a distance of 200 nautical miles measured from the appropriate baseline

Responsibility for the correctness of the internal details on the map rests with the publisher.

POST-MONSOON (OCTOBER–NOVEMBER)

As the south-west monsoon retreats, low-pressure areas form in the Bay of Bengal and a north-easterly flow of air that picks up moisture in the Bay of Bengal is formed. This air mass strikes the east coast of the southern peninsula (Tamil Nadu) and causes rainfall. Also, in this period, especially in November, severe tropical cyclones form in the Bay of Bengal and the Arabian sea. The cyclones formed in the Bay of Bengal are about twice as many as in the Arabian sea. These cyclones strike the coastal areas and cause intense rainfall and heavy damage to life and property.

WINTER SEASON (DECEMBER–FEBRUARY)

By about mid-December, disturbances of extra tropical origin travel eastwards across Afghanistan and Pakistan. Known as *western disturbances,* they cause moderate to

heavy rain and snowfall (about 25 cm) in the Himalayas, and, Jammu and Kashmir. Some light rainfall also occurs in the northern plains. Low-pressure areas in the Bay of Bengal formed in these months cause 10–12 cm of rainfall in the southern parts of Tamil Nadu.

SUMMER (PRE-MONSOON) (MARCH-MAY)

There is very little rainfall in India in this season. Convective cells cause some thunderstorms mainly in Kerala, West Bengal and Assam. Some cyclone activity, dominantly on the east coast, also occurs.

ANNUAL RAINFALL

The annual rainfall over the country is shown in Fig. 2.4. Considerable areal variation exists for the annual rainfall in India with high rainfall of the magnitude of 200 cm in
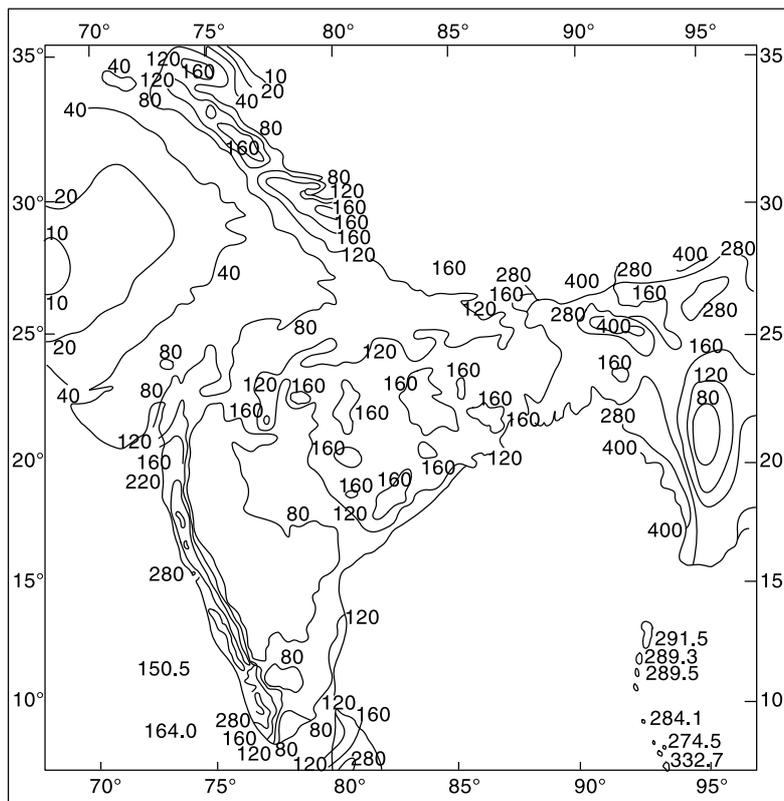
Fig. 2.4 Annual Rainfall (cm) over India and Neighbourhood
(Reproduced from *Natural Resources of Humid Tropical Asia – Natural Resources Research, XII.* © UNESCO, 1974, with permission of UNESCO)

Assam and north-eastern parts and the western ghats, and scanty rainfall in eastern Rajasthan and parts of Gujarat, Maharashtra and Karnataka. The average annual rainfall for the entire country is estimated as 117 cm.

It is well-known that there is considerable variation of annual rainfall in time at a place. The coefficient of variation,

$$C_v = \frac{100 \times \text{standard deviation}}{\text{mean}}$$

of the annual rainfall varies between 15 and 70, from place to place with an average value of about 30. Variability is least in regions of high rainfall and largest in regions of scanty rainfall. Gujarat, Haryana, Punjab and Rajasthan have large variability of rainfall.

Some of the interesting statistics relating to the variability of the seasonal and annual rainfall of India are as follows:

- A few heavy spells of rain contribute nearly 90% of total rainfall.
- While the average annual rainfall of the country is 117 cm, average annual rainfall varies from 10 cm in the western desert to 1100 cm in the North East region.
- More than 50% rain occurs within 15 days and less than 100 hours in a year.
- More than 80% of seasonal rainfall is produced in 10–20% rain events each lasting 1–3 days.

2.5 MEASUREMENT OF PRECIPITATION

A. RAINFALL

Precipitation is expressed in terms of the depth to which rainfall water would stand on an area if all the rain were collected on it. Thus 1 cm of rainfall over a catchment area of 1 km^2 represents a volume of water equal to 10^4 m^3. In the case of snowfall, an equivalent depth of water is used as the depth of precipitation. The precipitation is collected and measured in a *raingauge.* Terms such as *pluviometer, ombrometer* and *hyetometer* are also sometimes used to designate a raingauge.

A raingauge essentially consists of a cylindrical-vessel assembly kept in the open to collect rain. The rainfall catch of the raingauge is affected by its exposure conditions. To enable the catch of raingauge to accurately represent the rainfall in the area surrounding the raingauge standard settings are adopted. For siting a raingauge the following considerations are important:

- The ground must be level and in the open and the instrument must present a horizontal catch surface.
- The gauge must be set as near the ground as possible to reduce wind effects but it must be sufficiently high to prevent splashing, flooding, etc.
- The instrument must be surrounded by an open fenced area of at least 5.5 m × 5.5 m. No object should be nearer to the instrument than 30 m or twice the height of the obstruction.

Raingauges can be broadly classified into two categories as (i) nonrecording raingauges and (ii) recording gauges.

NONRECORDING GAUGES

The nonrecording gauge extensively used in India is the *Symons' gauge.* It essentially consists of a circular collecting area of 12.7 cm (5.0 inch) diameter connected to a

funnel. The rim of the collector is set in a horizontal plane at a height of 30.5 cm above the ground level. The funnel discharges the rainfall catch into a receiving vessel. The funnel and receiving vessel are housed in a metallic container. Figure 2.5 shows the details of the installation. Water contained in the receiving vessel is measured by a suitably graduated measuring glass, with an accuracy up to 0.1 mm.

Recently, the India Meteorological Department (IMD) has changed over to the use of fibreglass reinforced polyester

Fig. 2.5 Nonrecording Raingauge (Symons' Gauge)

raingauges, which is an improvement over the *Symons' gauge.* These come in different combinations of collector and bottle. The collector is in two sizes having areas of 200 and 100 cm^2 respectively. Indian standard (IS: 5225–1969) gives details of these new raingauges.

For uniformity, the rainfall is measured every day at 8.30 AM (IST) and is recorded as the rainfall of that day. The receiving bottle normally does not hold more than 10 cm of rain and as such in the case of heavy rainfall the measurements must be done more frequently and entered. However, the last reading must be taken at 8.30 AM and the sum of the previous readings in the past 24 hours entered as total of that day. Proper care, maintenance and inspection of raingauges, especially during dry weather to keep the instrument free from dust and dirt is very necessary. The details of installation of nonrecording raingauges and measurement of rain are specified in Indian Standard (IS: 4986–1968).

This raingauge can also be used to measure snowfall. When snow is expected, the funnel and receiving bottle are removed and the snow is allowed to collect in the outer metal container. The snow is then melted and the depth of resulting water measured. Antifreeze agents are sometimes used to facilitate melting of snow. In areas where considerable snowfall is expected, special snowgauges with shields (for minimizing the wind effect) and storage pipes (to collect snow over longer durations) are used.

Recording Gauges

Recording gauges produce a continuous plot of rainfall against time and provide valuable data of intensity and duration of rainfall for hydrological analysis of storms. The following are some of the commonly used recording raingauges.

Tipping-Bucket Type   This is a 30.5 cm size raingauge adopted for use by the US Weather Bureau. The catch from the funnel falls onto one of a pair of small buckets. These buckets are so balanced that when 0.25 mm of rainfall collects in one bucket, it tips and brings the other one in position. The water from the tipped bucket is col-

lected in a storage can. The tipping actuates an electrically driven pen to trace a record on clockwork-driven chart. The water collected in the storage can is measured at regular intervals to provide the total rainfall and also serve as a check. It may be noted that the record from the tipping bucket gives data on the intensity of rainfall. Further, the instrument is ideally suited for digitalizing of the output signal.
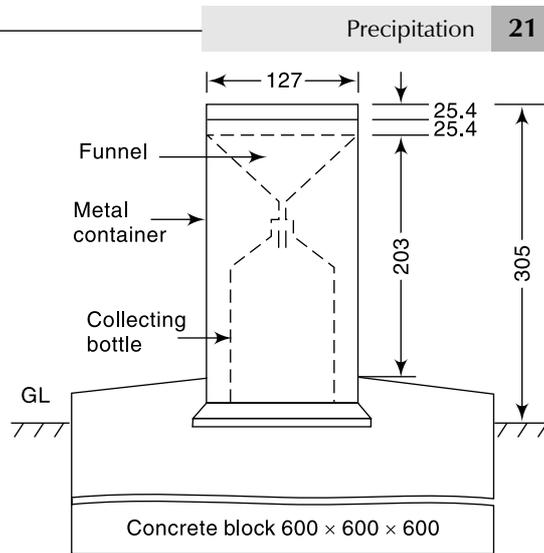
WEIGHING-BUCKET TYPE   In this raingauge the catch from the funnel empties into a bucket mounted on a weighing scale. The weight of the bucket and its contents are recorded on a clock-work-driven chart. The clockwork mechanism has the capacity to run for as long as one week. This instrument gives a plot of the accumulated rainfall against the elapsed time, i.e. the mass curve of rainfall. In some instruments of this type the recording unit is so constructed that the pen reverses its direction at every preset value, say 7.5 cm (3 in.) so that a continuous plot of storm is obtained.

NATURAL-SYPHON TYPE   This type of recording raingauge is also known as *float-type gauge.* Here the rainfall collected by a funnel-shaped collector is led into a float chamber causing a float to rise. As the float rises, a pen attached to the float through a lever system records the elevation of the float on a rotating drum driven by a clock-work mechanism. A syphon arrangement empties the float chamber when the float has reached a pre-set maximum level. This type of raingauge is adopted as the standard recording-type raingauge in India and its details are described in Indian Standard (IS: 5235–1969).

A typical chart from this type of raingauge is shown in Fig. 2.6. This chart shows a rainfall of 53.8 mm in 30 h. The vertical lines in the pen-trace correspond to the sudden emptying of the float chamber by syphon action which resets the pen to zero level. It is obvious that the natural syphon-type recording raingauge gives a plot of the mass curve of rainfall.
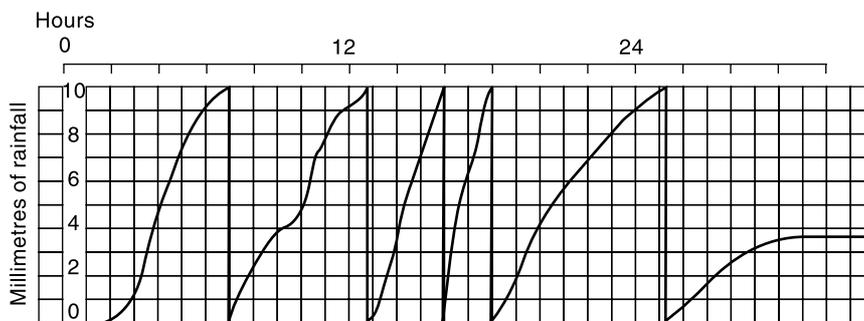
Fig. 2.6   Recording from a Natural Syphon-type Gauge (Schematic)

TELEMETERING RAINGAUGES

These raingauges are of the recording type and contain electronic units to transmit the data on rainfall to a base station both at regular intervals and on interrogation. The tipping-bucket type raingauge, being ideally suited, is usually adopted for this purpose. Any of the other types of recording raingauges can also be used equally effectively. Telemetering gauges are of utmost use in gathering rainfall data from mountainous and generally inaccessible places.

Radar Measurement of Rainfall

The meteorological radar is a powerful instrument for measuring the areal extent, location and movement of rain storms. Further, the amounts of rainfall over large areas can be determined through the radar with a good degree of accuracy.

The radar emits a regular succession of pulses of electromagnetic radiation in a narrow beam. When raindrops intercept a radar beam, it has been shown that

$$P_r = \frac{CZ}{r^2} \tag{2.1}$$

where P_r = average echopower, Z = radar-echo factor, r = distance to target volume and C = a constant. Generally the factor Z is related to the intensity of rainfall as

$$Z = aI^b \tag{2.2}$$

where a and b are coefficients and I = intensity of rainfall in mm/h. The values a and b for a given radar station have to be determined by calibration with the help of recording raingauges. A typical equation for Z is

$$Z = 200 \ I^{1.60}$$

Meteorological radars operate with wavelengths ranging from 3 to 10 cm, the common values being 5 and 10 cm. For observing details of heavy flood-producing rains, a 10-cm radar is used while for light rain and snow a 5-cm radar is used. The hydrological range of the radar is about 200 km. Thus a radar can be considered to be a remote-sensing super gauge covering an areal extent of as much as 100,000 km^2. Radar measurement is continuous in time and space. Present-day developments in the field include (i) On-line processing of radar data on a computer and (ii) Doppler-type radars for measuring the velocity and distribution of raindrops.

B. Snowfall

Snowfall as a form of precipitation differs from rainfall in that it may accumulate over a surface for some time before it melts and causes runoff. Further, evaporation from the surface of accumulated snow surface is a factor to be considered in analysis dealing with snow. Water equivalent of snowfall is included in the total precipitation amounts of a station to prepare seasonal and annual precipitation records.

Depth of Snowfall   Depth of snowfall is an important indicator for many engineering applications and in hydrology it is useful for seasonal precipitation and long-term runoff forecasts. A graduated stick or staff is used to measure the depth of snow at a selected place. Average of several measurements in an area is taken as the depth of snow in a snowfall event. *Snow stakes* are permanent graduated posts used to measure total depth of accumulated snow at a place.

Snow boards are 40 cm side square boards used to collect snow samples. These boards are placed horizontally on a previous accumulation of snow and after a snowfall event the snow samples are cut off from the board and depth of snow and water equivalent of snow are derived and recorded.

Water Equivalent of Snow   Water equivalent of snow is the depth of water that would result in melting of a unit of snow. This parameter is important in assessing the seasonal water resources of a catchment as well as in estimates of stream flow and floods due to melting of snow.

The amount of water present in a known depth of snow could be estimated if the information about the density of snow is available. The density of snow, however, varies quite considerably. Freshly fallen snow may have a density in the range of 0.07 to 0.15 with an average value of about 0.10. The accumulated snow however causes compaction and in regions of high accumulation densities as high as 0.4 to 0.6 is not uncommon. Where specific data is not available, it is usual to assume the density of fresh snow as 0.10.

Water equivalent of snow is obtained in two ways:

Snow Gauges Like rain gauges, *snow gauges* are receptacles to catch precipitation as it falls in a specified sampling area. Here, a large cylindrical receiver 203 mm in diameter is used to collect the snow as it falls. The height of the cylinder depends upon the snow storage needed at the spot as a consequence of accessibility etc. and may range from 60 cm to several metres. The receiver is mounted on a tower to keep the rim of the gauge above the anticipated maximum depth of accumulated snow in the area. The top of the cylinder is usually a funnel like fulcrum of cone with side slopes not less than 1 H: 6 V, to minimize deposits of ice on the exterior of the gauge. Also, a windshield is provided at the top. Melting agents or heating systems are sometimes provided in the remote snow gauges to reduce the size of the containers. The snow collected in the cylinder is brought in to a warm room and the snow melted by adding a pre-measured quantity of hot water. Through weighing or by volume measurements, the water equivalent of snow is ascertained and recorded.

Snow Tubes Water equivalent of accumulated snow is measured by means of *snow tubes* which are essentially a set of telescopic metal tubes. While a tube size of 40 mm diameter is in normal use, higher sizes up to 90 mm diameter are also in use. The main tube is provided with a cutter edge for easy penetration as well as to enable extracting of core sample. Additional lengths of tube can be attached to the main tube depending upon the depth of snow.

To extract a sample, the tube is driven into the snow deposit till it reaches the bottom of the deposit and then twisted and turned to cut a core. The core is extracted carefully and studied for its physical properties and then melted to obtain water equivalent of the snow core. Obviously, a large number of samples are needed to obtain representative values for a large area deposit. Usually, the sampling is done along an established route with specified locations called *snow course.*

2.6 RAINGAUGE NETWORK

Since the catching area of a raingauge is very small compared to the areal extent of a storm, it is obvious that to get a representative picture of a storm over a catchment the number of raingauges should be as large as possible, i.e. the catchment area per gauge should be small. On the other hand, economic considerations to a large extent and other considerations, such as topography, accessibility, etc. to some extent restrict the number of gauges to be maintained. Hence one aims at an optimum density of gauges from which reasonably accurate information about the storms can be obtained. Towards this the World Meteorological Organisation (WMO) recommends the following densities.

- In flat regions of temperate, Mediterranean and tropical zones
  Ideal—1 station for 600–900 km^2
  Acceptable—1 station for 900–3000 km^2

- In mountainous regions of temperate, Mediterranean and topical zones
   Ideal—1 station for 100–250 km^2
   Acceptable—1 station for 25–1000 km^2
- In arid and polar zones: 1 station for 1500–10,000 km^2 depending on the feasibility.

Ten per cent of raingauge stations should be equipped with self-recording gauges to know the intensities of rainfall.

From practical considerations of Indian conditions, the Indian Standard (IS: 4987–1968) recommends the following densities as sufficient.

- In plains: 1 station per 520 km^2;
- In regions of average elevation 1000 m: 1 station per 260–390 km^2; and
- In predominantly hilly areas with heavy rainfall: 1 station per 130 km^2.

ADEQUACY OF RAINGAUGE STATIONS

If there are already some raingauge stations in a catchment, the optimal number of stations that should exist to have an assigned percentage of error in the estimation of mean rainfall is obtained by statistical analysis as

$$N = \left(\frac{C_v}{\varepsilon} \right)^2 \tag{2.3}$$

where N = optimal number of stations, ε = allowable degree of error in the estimate of the mean rainfall and C_v = coefficient of variation of the rainfall values at the existing m stations (in per cent). If there are m stations in the catchment each recording rainfall values $P_1, P_2, \ldots, P_i, \ldots P_m$ in a known time, the coefficient of variation C_v is calculated as:

$$C_v = \frac{100 \times \sigma_{m-1}}{\bar{P}}$$

where $\sigma_{m-1} = \sqrt{\left[\dfrac{\sum_{1}^{m}(P_i - \bar{P})^2}{m-1} \right]}$ = standard deviation

P_i = precipitation magnitude in the ith station

$\bar{P} = \dfrac{1}{m}\left(\sum_{1}^{m} P_i \right)$ = mean precipitation

In calculating N from Eq. (2.3) it is usual to take $\varepsilon = 10\%$. It is seen that if the value of ε is small, the number of raingauge stations will be more.

According to WMO recommendations, at least 10% of the total raingauges should be of self-recording type.

EXAMPLE 2.1 *A catchment has six raingauge stations. In a year, the annual rainfall recorded by the gauges are as follows:*

Station	A	B	C	D	E	F
Rainfall (cm)	82.6	102.9	180.3	110.3	98.8	136.7

For a 10% error in the estimation of the mean rainfall, calculate the optimum number of stations in the catchment.

SOLUTION: For this data,

$$m = 6 \qquad \overline{P} = 118.6 \qquad \sigma_{m-1} = 35.04 \qquad \varepsilon = 10$$

$$C_v = \frac{100 \times 35.04}{118.6} = 29.54$$

$$N = \left(\frac{29.54}{10}\right)^2 = 8.7, \text{ say 9 stations}$$

The optimal number of stations for the catchment is 9. Hence three more additional stations are needed.

2.7 PREPARATION OF DATA

Before using the rainfall records of a station, it is necessary to first check the data for continuity and consistency. The continuity of a record may be broken with missing data due to many reasons such as damage or fault in a raingauge during a period. The missing data can be estimated by using the data of the neighbouring stations. In these calculations the *normal rainfall* is used as a standard of comparison. The normal rainfall is the average value of rainfall at a particular date, month or year over a specified 30-year period. The 30-year normals are recomputed every decade. Thus the term *normal annual percipitation* at station A means the average annual precipitation at A based on a specified 30-years of record.

ESTIMATION OF MISSING DATA

Given the annual precipitation values, P_1 P_2, P_3, ... P_m at neighbouring M stations 1,2, 3, ..., M respectively, it is required to find the missing annual precipitation P_x at a station X not included in the above M stations. Further, the normal annual precipitations N_1 N_2, ..., N_i ... at each of the above $(M + 1)$ stations including station X are known.

If the normal annual precipitations at various stations are within about 10% of the normal annual precipitation at station X, then a simple arithmetic average procedure is followed to estimate P_x. Thus

$$P_x = \frac{1}{M} [P_1 + P_2 + ... + P_m] \tag{2.4}$$

If the normal precipitations vary considerably, then P_x is estimated by weighing the precipitation at the various stations by the ratios of normal annual precipitations. This method, known as the *normal ratio method,* gives P_x as

$$P_x = \frac{N_x}{M} \left[\frac{P_1}{N_1} + \frac{P_2}{N_2} + ... + \frac{P_m}{N_m} \right] \tag{2.5}$$

EXAMPLE 2.2 *The normal annual rainfall at stations A, B, C, and D in a basin are 80.97, 67.59, 76.28 and 92.01 cm respectively. In the year 1975, the station D was inoperative and the stations A, B and C recorded annual precipitations of 91.11, 72.23 and 79.89 cm respectively. Estimate the rainfall at station D in that year.*

SOLUTION: As the normal rainfall values vary more than 10%, the normal ratio method is adopted. Using Eq. (2.5),

$$P_D = \frac{92.01}{3} \times \left(\frac{91.11}{80.79} + \frac{72.23}{67.59} + \frac{79.89}{76.28} \right) = 99.48 \text{ cm}$$

TEST FOR CONSISTENCY OF RECORD

If the conditions relevant to the recording of a raingauge station have undergone a significant change during the period of record, inconsistency would arise in the rainfall data of that station. This inconsistency would be felt from the time the significant change took place. Some of the common causes for inconsistency of record are: (i) shifting of a raingauge station to a new location, (ii) the neighbourhood of the station undergoing a marked change, (iii) change in the ecosystem due to calamities, such as forest fires, land slides, and (iv) occurrence of observational error from a certain date. The checking for inconsistency of a record is done by the *double-mass curve technique.* This technique is based on the principle that when each recorded data comes from the same parent population, they are consistent.

A group of 5 to 10 base stations in the neighbourhood of the problem station X is selected. The data of the annual (or monthly or seasonal mean) rainfall of the station X and also the average rainfall of the group of base stations covering a long period is arranged in the reverse chronological order (i.e. the latest record as the first entry and the oldest record as the last entry in the list). The accumulated precipitation of the station X (i.e. ΣP_x) and the accumulated values of the average of the group of base stations (i.e. ΣP_{av}) are calculated starting from the latest record. Values of ΣP_x are plotted against ΣP_{av} for various consecutive time periods (Fig. 2.7). A decided break in the slope of the resulting plot indicates a change in the precipitation regime of station X. The precipitation values at station X beyond the period of change of regime (point 63 in Fig. 2.7) is corrected by using the relation

$$P_{cx} = P_x \frac{M_e}{M_a} \tag{2.6}$$

where P_{cx} = corrected precipitation at any time period t_1 at station X
          P_x = original recorded precipitation at time period t_1 at station X
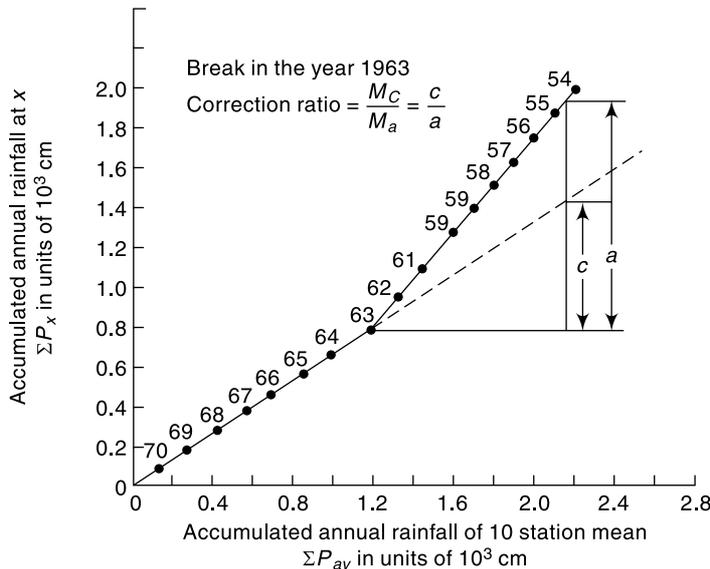
Fig. 2.7   Double-mass Curve

M_c = corrected slope of the double-mass curve

M_a = original slope of the double-mass curve

In this way the older records are brought to the new regime of the station. It is apparent that the more homogeneous the base station records are, the more accurate will be the corrected values at station X. A change in the slope is normally taken as significant only where it persists for more than five years. The double-mass curve is also helpful in checking systematic arithmetical errors in transferring rainfall data from one record to another.

EXAMPLE 2.3 *Annual rainfall data for station M as well as the average annual rainfall values for a group of ten neighbouring stations located in a meteorologically homogeneous region are given below.*

Year	Annual Rainfall of Station M (mm)	Average Annual Rainfall of the group (mm)	Year	Annual Rainfall of Station M (mm)	Average Annual Rainfall of the group (mm)
1950	676	780	1965	1244	1400
1951	578	660	1966	999	1140
1952	95	110	1967	573	650
1953	462	520	1968	596	646
1954	472	540	1969	375	350
1955	699	800	1970	635	590
1956	479	540	1971	497	490
1957	431	490	1972	386	400
1958	493	560	1973	438	390
1959	503	575	1974	568	570
1960	415	480	1975	356	377
1961	531	600	1976	685	653
1962	504	580	1977	825	787
1963	828	950	1978	426	410
1964	679	770	1979	612	588

Test the consistency of the annual rainfall data of station M and correct the record if there is any discrepancy. Estimate the mean annual precipitation at station M.

SOLUTION: The data is sorted in descending order of the year, starting from the latest year 1979. Cumulative values of station M rainfall (ΣP_m) and the ten station average rainfall values (ΣP_{av}) are calculated as shown in Table 2.1. The data is then plotted with ΣP_m on the Y-axis and ΣP_{av} on the X-axis to obtain a double mass curve plot (Fig. 2.8). The value of the year corresponding to the plotted points is also noted on the plot. It is seen that the data plots as two straight lines with a break of grade at the year 1969. This represents a change in the regime of the station M after the year 1968. The slope of the best straight line for the period 1979–1969 is $M_c = 1.0295$ and the slope of the best straight line for the period 1968–1950 is $M_a = 0.8779$.

The correction ratio to bring the old records (1950–1968) to the current (post 1968) regime is $= M_c/M_a = 1.0295/0.8779 = 1.173$. Each of the pre 1969 annual rainfall value is
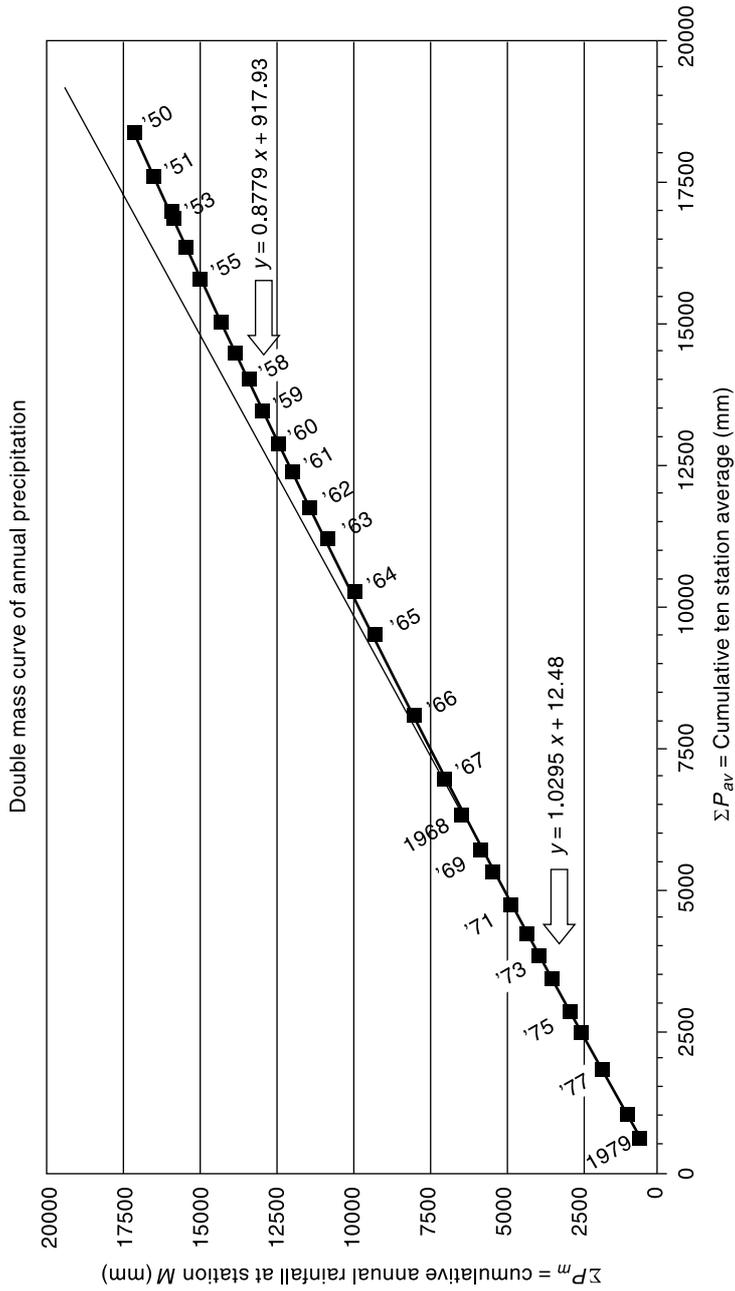
Fig. 2.8 Double Mass Curve of Annual Rainfall at Station *M*

multiplied by the correction ratio of 1.173 to get the adjusted value. The adjusted values at station M are shown in Col. 5 of Table. The finalized values of P_m (rounded off to nearest mm) for all the 30 years of record are shown in Col. 7.

The mean annual precipitation at station M (based on the corrected time series) = $(19004/30) = 633.5$ mm

Table 2.1   Calculation of Double Mass Curve of Example 2.3

1	2	3	4	5	6	7
Year	P_m (mm)	ΣP_m (mm)	P_{av} (mm)	P_{av} (mm)	Adjusted values of P_m (mm)	Finalised values of P_m (mm)
1979	612	612	588	588		612
1978	426	1038	410	998		426
1977	825	1863	787	1785		825
1976	685	2548	653	2438		685
1975	356	2904	377	2815		356
1974	568	3472	570	3385		568
1973	438	3910	390	3775		438
1972	386	4296	400	4175		386
1971	497	4793	490	4665		497
1970	635	5428	590	5255		635
1969	375	5803	350	5605		375
1968	596	6399	646	6251	698.92	699
1967	573	6972	650	6901	671.95	672
1966	999	7971	1140	8041	1171.51	1172
1965	1244	9215	1400	9441	1458.82	1459
1964	679	9894	770	10211	796.25	796
1963	828	10722	950	11161	970.98	971
1962	504	11226	5801	11741	591.03	591
1961	531	11757	600	12341	622.70	623
1960	415	12172	480	12821	486.66	487
1959	503	12675	575	13396	589.86	590
1958	493	13168	560	13956	578.13	578
1957	431	13599	490	14446	505.43	505
1956	479	14078	540	14986	561.72	562
1955	699	14777	800	15786	819.71	820
1954	472	15249	540	16326	553.51	554
1953	462	15711	520	16846	541.78	542
1952	95	15806	110	16956	111.41	111
1951	578	16384	660	17616	677.81	678
1950	676	17060	780	18396	792.73	193

Total of P_m = 19004 mm
Mean of P_m = 633.5 mm

2.8   PRESENTATION OF RAINFALL DATA

A few commonly used methods of presentation of rainfall data which have been found to be useful in interpretation and analysis of such data are given as follows:

MASS CURVE OF RAINFALL

The mass curve of rainfall is a plot of the accumulated precipitation against time, plotted in chronological order. Records of float type and weighing bucket type gauges are of this form. A typical mass curve of rainfall at a station during a storm is shown in Fig. 2.9. Mass curves of rainfall are very useful in extracting the information on the duration and magnitude of a storm. Also, intensities at various time intervals in a storm can be obtained by the slope of the curve. For nonrecording raingauges, mass curves are prepared from a knowledge of the approximate beginning and end of a storm and by using the mass curves of adjacent recording gauge stations as a guide.
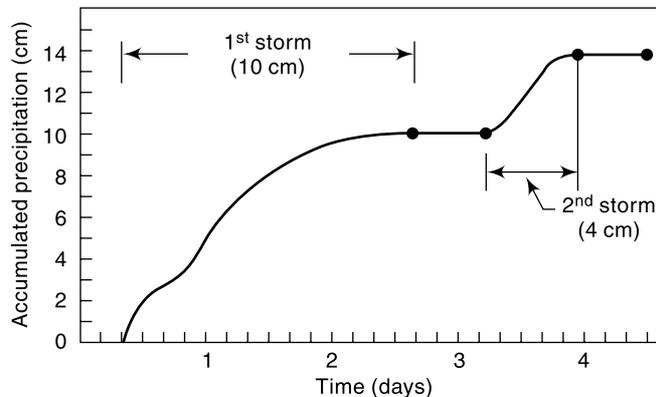
Fig. 2.9   Mass Curve of Rainfall

HYETOGRAPH

A hyetograph is a plot of the intensity of rainfall against the time interval. The hyetograph is derived from the mass curve and is usually represented as a bar chart (Fig. 2.10). It is a very convenient way of representing the characteristics of a storm and is particularly important in the development of design
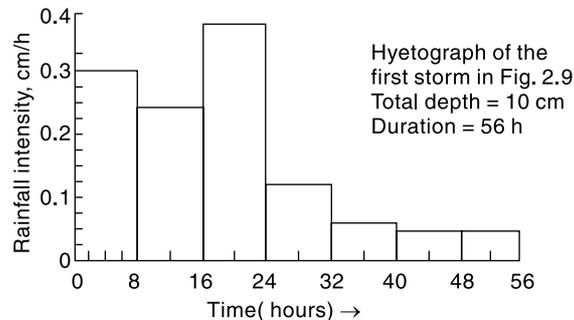
Fig. 2.10   Hyetograph of a Storm

storms to predict extreme floods. The area under a hyetograph represents the total precipitation received in the period. The time interval used depends on the purpose, in urban-drainage problems small durations are used while in flood-flow computations in larger catchments the intervals are of about 6 h.

POINT RAINFALL

Point rainfall, also known as *station rainfall* refers to the rainfall data of a station. Depending upon the need, data can be listed as daily, weekly, monthly, seasonal or annual values for various periods. Graphically these data are represented as plots of

magnitude *vs* chronological time in the form of a bar diagram. Such a plot, however, is not convenient for discerning a trend in the rainfall as there will be considerable variations in the rainfall values leading to rapid changes in the plot. The trend is often discerned by the method of *moving averages*, also known as *moving means*.

Moving average   Moving average is a technique for smoothening out the high frequency fluctuations of a time series and to enable the trend, if any, to be noticed. The basic principle is that a window of time range *m* years is selected. Starting from the first set of *m* years of data, the average of the data for *m* years is calculated and placed in the middle year of the range *m*. The window is next moved sequentially one time unit (year) at a time and the mean of the *m* terms in the window is determined at each window location. The value of *m* can be 3 or more years; usually an odd value. Generally, the larger the size of the range *m*, the greater is the smoothening. There are many ways of averaging (and consequently the plotting position of the mean) and the method described above is called Central Simple Moving Average. Example 2.4 describes the application of the method of moving averages.

EXAMPLE 2.4   *Annual rainfall values recorded at station M for the period 1950 to 1979 is given in Example 2.3. Represent this data as a bar diagram with time in chronological order. (i) Identify those years in which the annual rainfall is (a) less than 20% of the mean, and (b) more than the mean. (ii) Plot the three-year moving mean of the annual rainfall time series.*

SOLUTION: (i) Figure 2.11 shows the bar chart with height of the column representing the annual rainfall depth and the position of the column representing the year of occurrence. The time is arranged in chronological order.

The mean of the annual rainfall time series is 568.7 mm. As such, 20% less than the mean = 426.5 mm. Lines representing these values are shown in Fig. 2.11 as horizontal lines. It can be seen that in 6 years, viz. 1952, 1960, 1969, 1972, 1975 and 1978, the
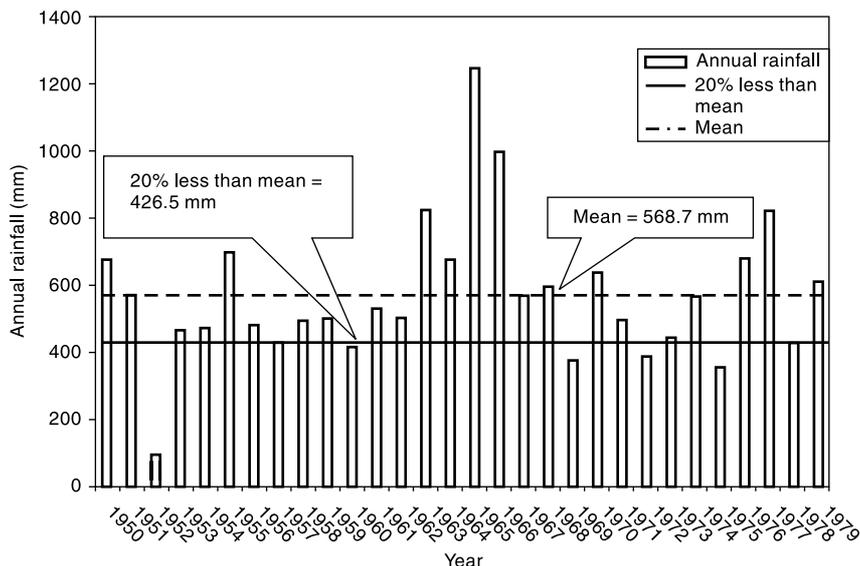
Fig. 2.11   Bar Chart of Annual Rainfall at Station *M*

annual rainfall values are less than 426.5 mm. In thirteen years, viz. 1950, 1951, 1955, 1963, 1964, 1965, 1966, 1967, 1968, 1970, 1976, 1977 and 1978, the annual rainfall was more than the mean.

(ii) Moving mean calculations are shown in Table 2.2. Three-year moving mean curve is shown plotted in Fig. 2.12 with the moving mean value as the ordinate and the time in chronological order as abscissa. Note that the curve starts from 1951 and ends in the year 1978. No apparent trend is indicated in this plot.

Table 2.2   Computation of Three-year Moving Mean

1	2	3	4
Year	Annual Rainfall (mm) P_i	Three consecutive year total for moving mean $(P_{i-1} + P_i + P_{i+1})$	3-year moving mean (Col. 3/3)*
1950	676		
1951	578	676 + 578 + 95 = 1349	449.7
1952	95	578 + 95 + 462 = 1135	378.3
1953	462	95 + 462 + 472 = 1029	343.0
1954	472	462 + 472 + 699 = 1633	544.3
1955	699	472 + 699 + 479 = 1650	550.0
1956	479	699 + 479 + 431 = 1609	536.3
1957	431	479 + 431 + 493 = 1403	467.7
1958	493	431 + 493 + 503 = 1427	475.7
1959	503	493 + 503 + 415 = 1411	470.3
1960	415	503 + 415 + 531 = 1449	483.0
1961	531	415 + 531 + 504 = 1450	483.3
1962	504	531 + 504 + 828 = 1863	621.0
1963	828	504 + 828 + 679 = 2011	670.3
1964	679	828 + 679 + 1244 = 2751	917.0
1965	1244	679 + 1244 + 999 = 2922	974.0
1966	999	1244 + 999 + 573 = 2816	938.7
1967	573	999 + 573 + 596 = 2168	722.7
1968	596	573 + 596 + 375 = 1544	514.7
1969	375	596 + 375 + 635 = 1606	535.3
1970	635	375 + 635 + 497 = 1507	502.3
1971	497	635 + 497 + 386 = 1518	506.0
1972	386	497 + 386 + 438 = 1321	440.3
1973	438	386 + 438 + 568 = 1392	464.0
1974	568	438 + 568 + 356 = 1362	454.0
1975	356	568 + 356 + 685 = 1609	536.3
1976	685	356 + 685 + 825 = 1866	622.0
1977	825	685 + 825 + 426 = 1936	645.3
1978	426	825 + 426 + 162 = 1863	621.0
1979	612		

*The moving mean is recorded at the mid span of 3 years.

2.9   MEAN PRECIPITATION OVER AN AREA

As indicated earlier, raingauges represent only point sampling of the areal
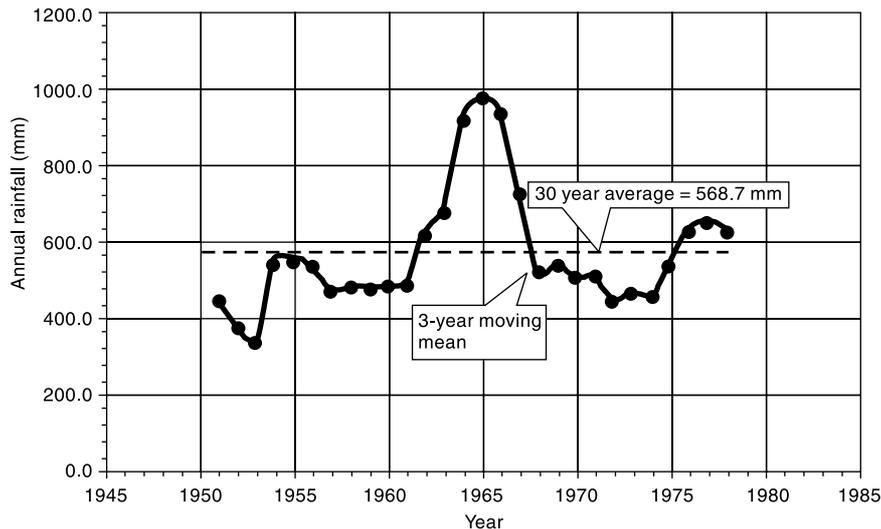
Fig. 2.12   Three-year Moving Mean

distribution of a storm. In practice, however, hydrological analysis requires a knowledge of the rainfall over an area, such as over a catchment.

To convert the point rainfall values at various stations into an average value over a catchment the following three methods are in use: (i) Arithmetical-mean method, (ii) Thiessen-polygon method, and (iii) Isohyetal method.

ARITHMETICAL-MEAN METHOD

When the rainfall measured at various stations in a catchment show little variation, the average precipitation over the catchment area is taken as the arithmetic mean of the station values. Thus if $P_1, P_2, \ldots, P_i, \ldots P_n$ are the rainfall values in a given period in N stations within a catchment, then the value of the mean precipitation $\bar{P}$ over the catchment by the arithmetic-mean method is

$$\bar{P} = \frac{P_1 + P_2 + \ldots + P_i + \ldots + P_n}{N} = \frac{1}{N} \sum_{i=1}^{N} P_i \qquad (2.7)$$

In practice, this method is used very rarely.

THIESSEN-MEAN METHOD

In this method the rainfall recorded at each station is given a weightage on the basis of an area closest to the station. The procedure of determining the weighing area is as follows: Consider a catchment area as in Fig. 2.13 containing three raingauge stations. There are three stations outside the catchment but in its neighbourhood. The catchment area is drawn to scale and the positions of the six stations marked on it. Stations 1 to 6 are joined to form a network of triangles. Perpendicular bisectors for each of the sides of the triangle are drawn. These bisectors form a polygon around each station. The boundary of the catchment, if it cuts the bisectors is taken as the outer limit of the polygon. Thus for station 1, the bounding polygon is *abcd*. For station 2, *kade* is taken as the bounding polygon. These bounding polygons are called *Thiessen polygons*. The areas of these six Thiessen polygons are determined either with a planimeter or

A = total catchment area

Station	Bounded by	Area	Weightage
1	abcd	A_1	A_1/A
2	kade	A_2	A_2/A
3	edcgf	A_3	A_3/A
4	fgh	A_4	A_4/A
5	hgcbj	A_5	A_5/A
6	jbak	A_6	A_6/A
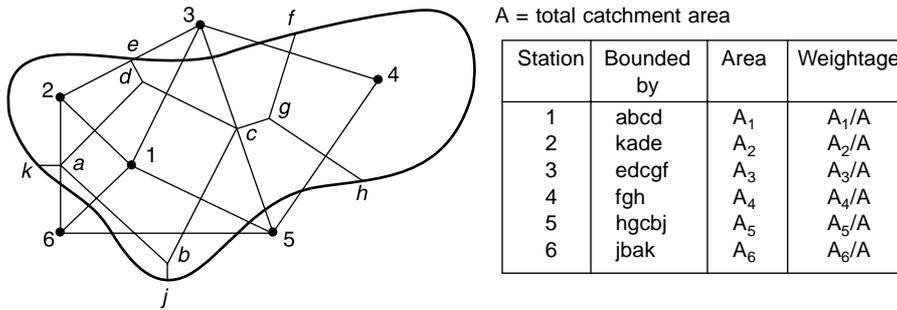
Fig. 2.13 Thiessen Polygons

by using an overlay grid. If P_1 P_2,... , P_6 are the rainfall magnitudes recorded by the stations 1, 2,…, 6 respectively, and A_1, A_2,…, A_6 are the respective areas of the Thiessen polygons, then the average rainfall over the catchment $\overline{P}$ is given by

$$\overline{P} = \frac{P_1 A_1 + P_2 A_2 + \ldots + P_6 A_6}{(A_1 + A_2 + \ldots + A_6)}$$

Thus in general for M stations,

$$\overline{P} = \frac{\sum_{i=1}^{M} P_i A_i}{A} = \sum_{i=1}^{M} P_i \frac{A_i}{A} \tag{2.8}$$

The ratio $\dfrac{A_i}{A}$ is called the *weightage factor* for each station.

The Thiessen-polygon method of calculating the average percipitation over an area is superior to the arithmetic-average method as some weightage is given to the various stations on a rational basis. Further, the raingauge stations outside the catchment are also used effectively. Once the weightage factors are determined, the calculation of $\overline{P}$ is relatively easy for a fixed network of stations.

ISOHYETAL METHOD

An *isohyet* is a line joining points of equal rainfall magnitude. In the isohyetal method, the catchment area is drawn to scale and the raingauge stations are marked. The recorded values for which areal average $\overline{P}$ is to be determined are then marked on the plot at appropriate stations. Neighbouring stations outside the catchment are also considered. The isohyets of various values are then drawn by considering point rain-
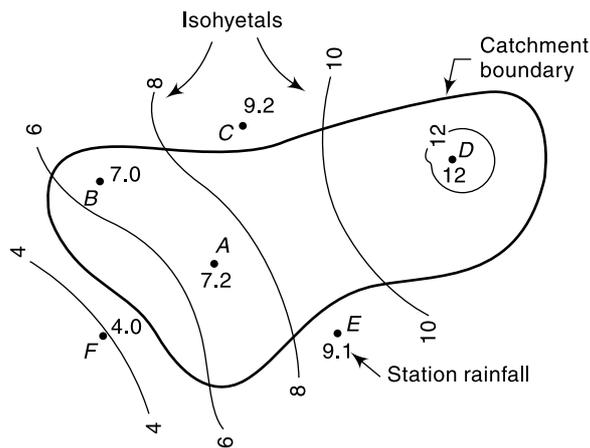
Fig. 2.14 Isohyetals of a Storm

falls as guides and interpolating between them by the eye (Fig. 2.14). The procedure is similar to the drawing of elevation contours based on spot levels.

The area between two adjacent isohyets are then determined with a planimeter. If the isohyets go out of catchment, the catchment boundary is used as the bounding line. The average value of the rainfall indicated by two isohyets is assumed to be acting over the inter-isohyet area. Thus P_1, P_2, …, P_n are the values of isohyets and if a_1, a_2, …, a_{n-1} are the inter-isohyet areas respectively, then the mean precipitation over the catchment of area A is given by

$$\bar{P} = \frac{a_1\left(\dfrac{P_1 + P_2}{2}\right) + a_2\left(\dfrac{P_2 + P_3}{2}\right) + \ldots + a_{n-1}\left(\dfrac{P_{n-1} + P_n}{2}\right)}{A} \qquad (2.9)$$

The isohyet method is superior to the other two methods especially when the stations are large in number.

EXAMPLE 2.5 *In a catchment area, approximated by a circle of diameter 100 km, four rainfall stations are situated inside the catchment and one station is outside in its neighbourhood. The coordinates of the centre of the catchment and of the five stations are given below. Also given are the annual precipitation recorded by the five stations in 1980. Determine the average annual precipitation by the Thiessen-mean method.*

Centre: (100, 100)   Diameter: 100 km.
Distance are in km

Station	1	2	3	4	5
Coordinates	(30, 80)	(70, 100)	(100, 140)	(130, 100)	(100, 70)
Precipitation (cm)	85.0	135.2	95.3	146.4	102.2

SOLUTION: The catchment area is drawn to scale and the stations are marked on it (Fig. 2.15). The stations are joined to form a set of triangles and the perpendicular bisector of each side is then drawn. The Thiessen-polygon area enclosing each station is then identified. It may be noted that station 1 in this problem does not have any area of influence in the catchment. The areas of various Thiessen polygons are determined either by a planimeter or by placing an overlay grid.
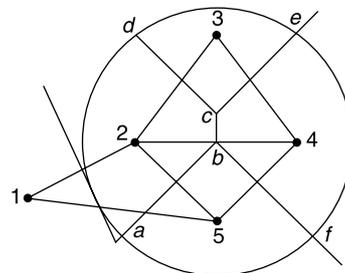
Fig. 2.15 Thiessen Polygons – Example 2.5

Station	Boundary of area	Area (km²)	Fraction of total area	Rainfall	Weighted P (cm) (col. 4 × col. 5)
1	—	—	—	85.0	—
2	abcd	2141	0.2726	135.2	36.86
3	dce	1609	0.2049	95.3	19.53
4	ecbf	2141	0.2726	146.4	39.91
5	fba	1963	0.2499	102.2	25.54
Total		7854	1.000		121. 84

Mean precipitation = 121.84 cm.

EXAMPLE 2.6   *The isohyets due to a storm in a catchment were drawn (Fig. 2.14) and the area of the catchment bounded by isohyets were tabulated as below.*

Isohyets (cm)	Area (km²)
Station–12.0	30
12.0–10.0	140
10.0–8.0	80
8.0–6.0	180
6.0–4.0	20

Estimate the mean precipitation due to the storm.

SOLUTION: For the first area consisting of a station surrounded by a closed isohyet, a precipitation value of 12.0 cm is taken. For all other areas, the mean of two bounding isohyets are taken.

Isohytes	Average value of P (cm)	Area (km²)	Fraction of total area (col. 3/450)	Weighted P (cm) (col. 2 × col. 4)
1	2	3	4	5
12.0	12.0	30	0.0667	0.800
12.0–10.0	11.0	140	0.3111	3.422
10.0–8.0	9.0	80	0.1778	1.600
8.0–6.0	7.0	180	0.4000	2.800
6.0–4.0	5.0	20	0.0444	0.222
Total		450	1.0000	8.844

Mean precipitation $\bar{P}$ = 8.84 cm

2.10   DEPTH-AREA-DURATION RELATIONSHIPS

The areal distribution characteristics of a storm of given duration is reflected in its depth-area relationship. A few aspects of the interdependency of depth, area and duration of storms are discussed below.

DEPTH-AREA RELATION

For a rainfall of a given duration, the average depth decreases with the area in an exponential fashion given by

$$\bar{P} = P_0 \exp(-KA^n) \tag{2.10}$$

where $\bar{P}$ = average depth in cm over an area A km², P_0 = highest amount of rainfall in cm at the storm centre and K and n are constants for a given region. On the basis of 42 severemost storms in north India, Dhar and Bhattacharya[3] (1975) have obtained the following values for K and n for storms of different duration:

Duration	K	n
1 day	0.0008526	0.6614
2 days	0.0009877	0.6306
3 days	0.001745	0.5961

Since it is very unlikely that the storm centre coincides over a raingauge station, the exact determination of P_0 is not possible. Hence in the analysis of large area storms the highest station rainfall is taken as the average depth over an area of 25 km^2.

Equation (2.10) is useful in extrapolating an existing storm data over an area.

MAXIMUM DEPTH-AREA-DURATION CURVES

In many hydrological studies involving estimation of severe floods, it is necessary to have information on the maximum amount of rainfall of various durations occurring over various sizes of areas. The development of relationship, between maximum depth-area-duration for a region is known as DAD analysis and forms an important aspect of hydro-meteorological study. References 2 and 9 can be consulted for details on DAD analysis. A brief description of the analysis is given below.

First, the severemost rainstorms that have occurred in the region under question are considered. Isohyetal maps and mass curves of the storm are compiled. A depth-area curve of a given duration of the storm is prepared. Then from a study of the mass curve of rainfall, various durations and the maximum depth of rainfall in these durations are noted. The maximum depth-area curve for a given duration D is prepared by assuming the area distribution of rainfall for smaller duration to be similar to the total storm. The procedure is then repeated for different storms and the envelope curve of maximum depth-area for duration D is obtained. A similar procedure for various values of D results in a family of envelope curves of maximum depth *vs* area, with duration as the third parameter (Fig. 2.16). These curves are called *DAD curves*.

Figure 2.16 shows typical DAD curves for a catchment. In this the average depth denotes the depth averaged over the area under consideration. It may be seen that the maximum depth for a given storm decreases with the area; for a given area the maximum depth increases with the duration.
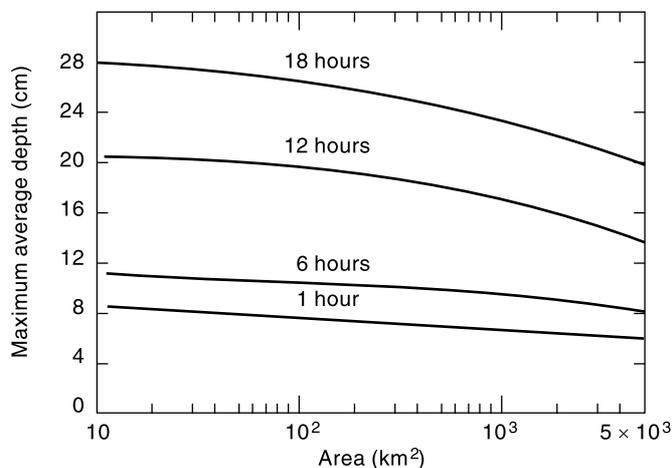
Fig. 2.16 Typical DAD Curves

Preparation of DAD curves involves considerable computational effort and requires meteorological and topographical information of the region. Detailed data on severemost storms in the past are needed. DAD curves are essential to develop design

storms for use in computing the design flood in the hydrological design of major structures such as dams.

Table 2.3 Maximum (Observed) Rain Depths (cm) over Plains of North India[4, 5]

Duration	Area in km² × 10⁴								
	.026	0.13	0.26	1.3	2.6	5.2	7.8	10.5	13.0
1 day	81.0*	76.5*	71.1	47.2*	37.1 *	26.4	20.3†	18.0†	16.0†
2 days	102.9*	97.5*	93.2*	73.4*	58.7*	42.4*	35.6†	31.5†	27.9†
3 days	121.9†	110.7†	103.l†	79.2†	67.1†	54.6†	48.3†	42.7†	38.9†

Note: *—Storm of 17–18 September 1880 over north-west U.P.
　　　†—Storm of 28–30 July 1927 over north Gujarat.

Maximum rain depths observed over the plains of north India are indicated in Table 2.3. These were due to two storms, which are perhaps the few severe most recorded rainstorms over the world.

2.11   FREQUENCY OF POINT RAINFALL

In many hydraulic-engineering applications such as those concerned with floods, the probability of occurrence of a particular extreme rainfall, e.g. a 24-h maximum rainfall, will be of importance. Such information is obtained by the frequency analysis of the point-rainfall data. The rainfall at a place is a random hydrologic process and a sequence of rainfall data at a place when arranged in chronological order constitute a time series. One of the commonly used data series is the annual series composed of annual values such as annual rainfall. If the extreme values of a specified event occurring in each year is listed, it also constitutes an annual series. Thus for example, one may list the maximum 24-h rainfall occurring in a year at a station to prepare an annual series of 24-h maximum rainfall values. The probability of occurrence of an event in this series is studied by frequency analysis of this annual data series. A brief description of the terminology and a simple method of predicting the frequency of an event is described in this section and for details the reader is referred to standard works on probability and statistical methods. The analysis of annual series, even though described with rainfall as a reference is equally applicable to any other random hydrological process, e.g. stream flow.

First, it is necessary to correctly understand the terminology used in frequency analysis. The probability of occurrence of an event of a random variable (e.g. rainfall) whose magnitude is equal to or in excess of a specified magnitude X is denoted by P. The *recurrence interval* (also known as *return period*) is defined as

$$T = 1/P \qquad\qquad (2.11)$$

This represents the average interval between the occurrence of a rainfall of magnitude equal to or greater than X. Thus if it is stated that the return period of rainfall of 20 cm in 24 h is 10 years at a certain station A, it implies that on an average rainfall magnitudes equal to or greater than 20 cm in 24 h occur once in 10 years, i.e. in a long period of say 100 years, 10 such events can be expected. However, it does not mean that every 10 years one such event is likely, i.e. periodicity is not implied. The probability of a rainfall of 20 cm in 24 h occurring in anyone year at station A is $1/T = 1/10 = 0.l$.

If the probability of an event occurring is P, the probability of the event *not occurring in a given year* is $q = (1 - P)$. The binomial distribution can be used to find the probability of occurrence of the event r times in n successive years. Thus

$$P_{r, n} = {}^nC_r P_r q^{n-r} = \frac{n!}{(n-r)!\, r!} P^r q^{n-r} \tag{2.12}$$

where $P_{r, n}$ = probability of a random hydrologic event (rainfall) of given magnitude and exceedence probability P occurring r times in n successive years. Thus, for example,

(a) The probability of an event of exceedence probability P occurring 2 times in n successive years is

$$P_{2, n} = \frac{n!}{(n-2)!\, 2!} P^2 q^{n-2}$$

(b) The probability of the event not occurring at all in n successive years is

$$P_{0, n} = q^n = (1 - P)^n$$

(c) The probability of the event occurring at least once in n successive years

$$P_1 = 1 - q^n = 1 - (1 - P)^n \tag{2.13}$$

EXAMPLE 2.7 *Analysis of data on maximum one-day rainfall depth at Madras indicated that a depth of 280 mm had a return period of 50 years. Determine the probability of a one-day rainfall depth equal to or greater than 280 mm at Madras occurring (a) once in 20 successive years, (b) two times in 15 successive years, and (c) at least once in 20 successive years.*

SOLUTION: Here $P = \dfrac{1}{50} = 0.02$

By using Eq. (2.12):

(a) $n = 20$, $r = 1$

$$P_{1, 20} = \frac{20!}{19!1!} \times 0.02 \times (0.98)^{19} = 20 \times 0.02 \times 0.68123 = 0.272$$

(b) $n = 15$, $r = 2$

$$P_{2, 15} = \frac{15!}{13!2!} \times (0.02)^2 \times (0.98)^{13} = 15 \times \frac{14}{2} \times 0.0004 \times 0.769 = 0.323$$

(c) By Eq. (2.13)

$$P_1 = 1 - (1 - 0.02)^{20} = 0.332$$

PLOTTING POSITION

The purpose of the frequency analysis of an annual series is to obtain a relation between the magnitude of the event and its probability of exceedence. The probability analysis may be made either by empirical or by analytical methods.

A simple empirical technique is to arrange the given annual extreme series in descending order of magnitude and to assign an order number m. Thus for the first entry $m = 1$, for the second entry $m = 2$, and so on, till the last event for which $m = N =$ Number of years of record. The probability P of an event equalled to or exceeded is given by the *Weibull formula*

$$P = \left(\frac{m}{N + 1} \right) \tag{2.14}$$

The recurrence interval $T = 1/P = (N + 1)/m$.

Equation (2.14) is an empirical for-
mula and there are several other such
empirical formulae available to calcu-
late *P* (Table 2.4). The exceedence
probability of the event obtained by the
use of an empirical formula, such as
Eq. (2.14) is called *plotting position.*
Equation (2.14) is the most popular
plotting position formula and hence
only this formula is used in further sec-
tions of this book.

Table 2.4   Plotting Position Formulae

Method	*P*
California	m/N
Hazen	$(m - 0.5)/N$
Weibull	$m/(N + 1)$
Chegodayev	$(m - 0.3)/(N + 0.4)$
Blom	$(m - 0.44)/(N + 0.12)$
Gringorten	$(m - 3/8)/(N + 1/4)$

Having calculated *P* (and hence *T*) for all the events in the series, the variation of
the rainfall magnitude is plotted against the corresponding *T* on a semi-log paper
(Fig. 2.17) or log-log paper. By suitable extrapolation of this plot, the rainfall magnitude
of specific duration for any recurrence interval can be estimated.
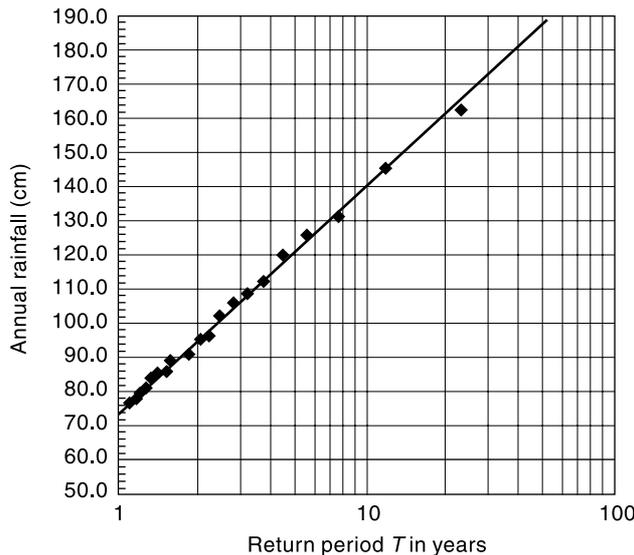
Fig. 2.17   Return Periods of Annual Rainfall at Station *A*

This simple empirical procedure can give good results for small extrapolations and
the errors increase with the amount of extrapolation. For accurate work, various ana-
lytical calculation procedures using frequency factors are available. Gumbel's extreme
value distribution and Log Pearson Type III method are two commonly used analyti-
cal methods and are described in Chap. 7 of this book.

If *P* is the probability of exceedence of a variable having a magnitude *M*, a com-
mon practice is to designate the magnitude *M* as having $(100\,P)$ percent dependability.
For example, 75% dependable annual rainfall at a station means the value of annual
rainfall at the station that can be expected to be equalled to or exceeded 75% times,
(i.e., on an average 30 times out of 40 years). Thus 75% dependable annual rainfall
means the value of rainfall in the annual rainfall time series that has $P = 0.75$, i.e.,
$T = 1/P = 1.333$ years.

EXAMPLE 2.8 *The record of annual rainfall at Station A covering a period of 22 years is given below. (a) Estimate the annual rainfall with return periods of 10 years and 50 years. (b) What would be the probability of an annual rainfall of magnitude equal to or exceeding 100 cm occurring at Station A? (b) What is the 75% dependable annual rainfall at station A?*

Year	Annual rainfall (cm)	Year	Annual rainfall (cm)
1960	130.0	1971	90.0
1961	84.0	1972	102.0
1962	76.0	1973	108.0
1963	89.0	1974	60.0
1964	112.0	1975	75.0
1965	96.0	1976	120.0
1966	80.0	1977	160.0
1967	125.0	1978	85.0
1968	143.0	1979	106.0
1969	89.0	1980	83.0
1970	78.0	1981	95.0

SOLUTION: The data are arranged in descending order and the rank number assigned to the recorded events. The probability P of the event being equalled to or exceeded is calculated by using Weibull formula (Eq. 2.14). Calculations are shown in Table 2.5. It may be noted that when two or more events have the same magnitude (as for $m = 13$ and 14 in Table 2.5) the probability P is calculated for the largest m value of the set. The return period T is calculated as $T = 1/P$.

Table 2.5 Calculation of Return Periods

$N = 22$ years

m	Annual Rainfall (cm)	Probability $= m/(N+1)$	Return Period $T = 1/P$ (years)	m	Annual Rainfall (cm)	Probability $P = m/(N+1)$	Return Period $T = 1/P$ (Years)
1	160.0	0.043	23.000	12	90.0	0.522	1.917
2	143.0	0.087	11.500	13	89.0	0.565	
3	130.0	0.130	7.667	14	89.0	0.609	1.643
4	125.0	0.174	5.750	15	85.0	0.652	1.533
5	120.0	0.217	4.600	16	84.0	0.696	1.438
6	112.0	0.261	3.833	17	83.0	0.739	1.353
7	108.0	0.304	3.286	18	80.0	0.783	1.278
8	106.0	0.348	2.875	19	78.0	0.826	1.211
9	102.0	0.391	2.556	20	76.0	0.870	1.150
10	96.0	0.435	2.300	21	75.0	0.913	1.095
11	95.0	0.478	2.091	22	60.0	0.957	1.045

A graph is plotted between the annual rainfall magnitude as the ordinate (on arithmetic scale) and the return period T as the abscissa (on logarithmic scale), (Fig. 2.17). It can be

seen that excepting the point with the lowest T, a straight line could represent the trend of the rest of data.

   (a)   (i) For $T = 10$ years, the corresponding rainfall magnitude is obtained by interpolation between two appropriate successive values in Table 2.5, viz. those having $T = 11.5$ and 7.667 years respectively, as 137.9 cm

        (ii) for $T = 50$ years the corresponding rainfall magnitude, by extrapolation of the best fit straight line, is 180.0 cm

   (b) Return period of an annual rainfall of magnitude equal to or exceeding 100 cm, by interpolation, is 2.4 years. As such the exceedence probability $P = \dfrac{1}{2.4} = 0.417$

   (c) 75% dependable annual rainfall at Station A = Annual rainfall with probability $P = 0.75$, i.e. $T = 1/0.75 = 1.33$ years. By interpolation between two successive values in Table 2.7 having $T = 1.28$ and 1.35 respectively, the 75% dependable annual rainfall at Station A is 82.3 cm.

2.12   MAXIMUM INTENSITY-DURATION-FREQUENCY RELATIONSHIP

MAXIMUM INTENSITY-DURATION RELATIONSHIP

In any storm, the actual intensity as reflected by the slope of the mass curve of rainfall varies over a wide range during the course of the rainfall. If the mass curve is considered divided into N segments of time interval Δt such that the total duration of the storm $D = N \Delta t$, then the intensity of the storm for various sub-durations $t_j = (1. \Delta t)$, $(2. \Delta t)$, $(3. \Delta t)$,…$(j. \Delta t)$… and $(N. \Delta t)$ could be calculated. It will be found that for each duration (say t_j), the intensity will have a maximum value and this could be analysed to obtain a relationship for the variation of the maximum intensity with duration for the storm. This process is basic to the development of maximum intensity duration frequency relationship for the station discussed later on.

   Briefly, the procedure for analysis of a mass curve of rainfall for developing maximum intensity-duration relationship of the storm is as follows.

- Select a convenient time step Δt such that duration of the storm $D = N. \Delta t$.
- For each duration (say $t_j = j.\Delta t$) the mass curve of rainfall is considered to be divided into consecutive segments of duration t_j. For each segment the incremental rainfall d_j in duration t_j is noted and intensity $I_j = d_j/t_j$ obtained.
- Maximum value of the intensity (I_{mj}) for the chosen t_j is noted.
- The procedure is repeated for all values of $j = 1$ to N to obtain a data set of I_{mj} as a function of duration t_j. Plot the maximum intensity I_m as function of duration t.
- It is common to express the variation of I_m with t as

$$I_m = \frac{c}{(t+a)^b}$$

where a, b and c are coefficients obtained through regression analysis.
Example 2.9 describes the procedure in detail.

MAXIMUM DEPTH-DURATION RELATIONSHIP

Instead of the maximum intensity I_m in a duration t, the product $(I_m. t) = d_m$ = maximum depth of precipitation in the duration t could be used to relate it to the duration.

Such a relationship is known as the maximum depth-duration relationship of the storm. The procedure of developing this relationship is essentially same as that for maximum intensity-duration relationship described earlier.

Example 2.9 describes the procedure in detail

MAXIMUM INTENSITY-DURATION-FREQUENCY RELATIONSHIP

If the rainfall data from a self-recording raingauge is available for a long period, the frequency of occurrence of maximum intensity occurring over a specified duration can be determined. A knowledge of maximum intensity of rainfall of specified return period and of duration equal to the critical time of concentration is of considerable practical importance in evaluating peak flows related to hydraulic structures.

Briefly, the procedure to calculate the intensity-duration-frequency relationship for a given station is as follows.

- M numbers of significant and heavy storms in a particular year Y_1 are selected for analysis. Each of these storms are analysed for maximum intensity duration relationship as described in Sec. 2.12.1
- This gives the set of maximum intensity I_m as a function of duration for the year Y_1.
- The procedure is repeated for all the N years of record to obtain the maximum intensity $I_m (D_j)_k$ for all $j = 1$ to M and $k = 1$ to N.
- Each record of $I_m (D_j)_k$ for $k = 1$ to N constitutes a time series which can be analysed to obtain frequencies of occurrence of various $I_m (D_j)$ values. Thus there will be M time series generated.
- The results are plotted as maximum intensity *vs* return period with the *Duration* as the third parameter (Fig. 2.18). Alternatively, maximum intensity *vs* duration with frequency as the third variable can also be adopted (Fig. 2.19).
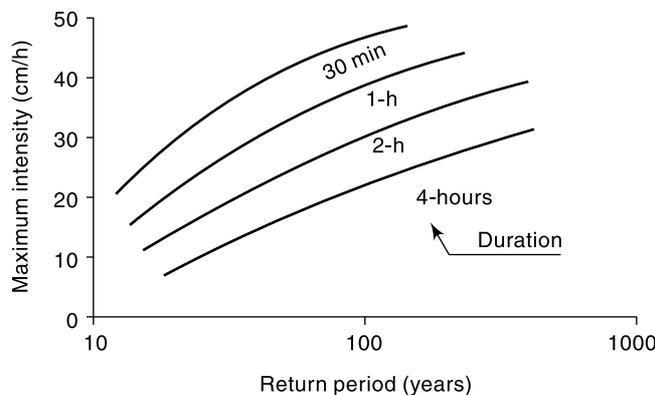
Fig. 2.18   Maximum Intensity-Return Period-Duration Curves

Analytically, these relationships are commonly expressed in a condensed form by general form

$$i = \frac{KT^x}{(D+a)^n} \tag{2.15}$$

where i = maximum intensity (cm/h), T = return period (years), D = duration (hours)
K, x, a and n are coefficients for the area represented by the station.
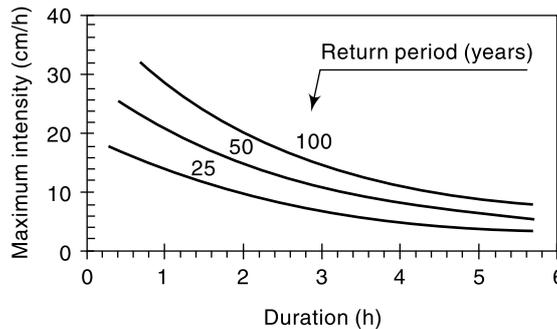
Fig. 2.19 Maximum Intensity-Duration-Frequency Curves

Sometimes, instead of maximum intensity, maximum depth is used as a parameter and the results are represented as a plot of maximum depth *vs* duration with return period as the third variable (Fig. 2.20).

[*Note:* While maximum intensity is expressed as a function of duration and return period, it is customary to refer this function as intensity-duration-frequency relationship. Similarly, in the

Fig. 2.20 Maximum Depth-Duration-Frequency Curves

depth-duration-frequency relationship deals with maximum depth in a given duration.]

Rambabu et al. (1979)[10] have analysed the self-recording rain gauge rainfall records of 42 stations in the country and have obtained the values of coefficients K, x, a, and n of Eq. 2.15. Some typical values of the coefficients for a few places in India are given in Table 2.6.

Table 2.6 Typical values of Coefficients K, x, a and n in Eq. (2.15)

[Ref. 10]

Zone	Place	K	x	a	n
Northern Zone	Allahabad	4.911	0.1667	0.25	0.6293
	Amritsar	14.41	0.1304	1.40	1.2963
	Dehradun	6.00	0.22	0.50	0.8000
	Jodhpur	4.098	0.1677	0.50	1.0369
	Srinagar	1.503	0.2730	0.25	1.0636
	Average for the zone	5.914	0.1623	0.50	1.0127
Central Zone	Bhopal	6.9296	0.1892	0.50	0.8767
	Nagpur	11.45	0.1560	1.25	1.0324
	Raipur	4.683	0. 1389	0.15	0.9284
	Average for the zone	7.4645	0.1712	0.75	0.9599
Western Zone	Aurangabad	6.081	0.1459	0.50	1.0923
	Bhuj	3.823	0.1919	0.25	0.9902

(Contd.)

(*Contd.*)

	Veraval	7.787	0.2087	0.50	0.8908
	Average for the zone	3.974	0.1647	0.15	0.7327
Eastern Zone	Agarthala	8.097	0.1177	0.50	0.8191
	Kolkata (Dumdum)	5.940	0.1150	0.15	0.9241
	Gauhati	7.206	0.1157	0.75	0.9401
	Jarsuguda	8.596	0.1392	0.75	0.8740
	Average for the zone	6.933	0.1353	0.50	0.8801
Southern Zone	Bangalore	6.275	0.1262	0.50	1.1280
	Hyderabad	5.250	0.1354	0.50	1.0295
	Chennai	6.126	0.1664	0.50	0.8027
	Trivandrum	6.762	0.1536	0.50	0.8158
	Average for the zone	6.311	0.1523	0.50	0.9465

Extreme point rainfall values of different durations and for different return periods have been evaluated by IMD and the *iso-pluvial* (lines connecting equal depths of rainfall) maps covering the entire country have been prepared. These are available for rainfall durations of 15 min, 30 min, 45 min, 1 h, 3 h, 6 h, 9 h, 15 h and 24 h for return periods of 2, 5, 10, 25, 50 and 100 years. A typical 50 year–24 h maximum rainfall map of the southern peninsula is given in Fig. 2.21. The 50 year-l h maximum rainfall
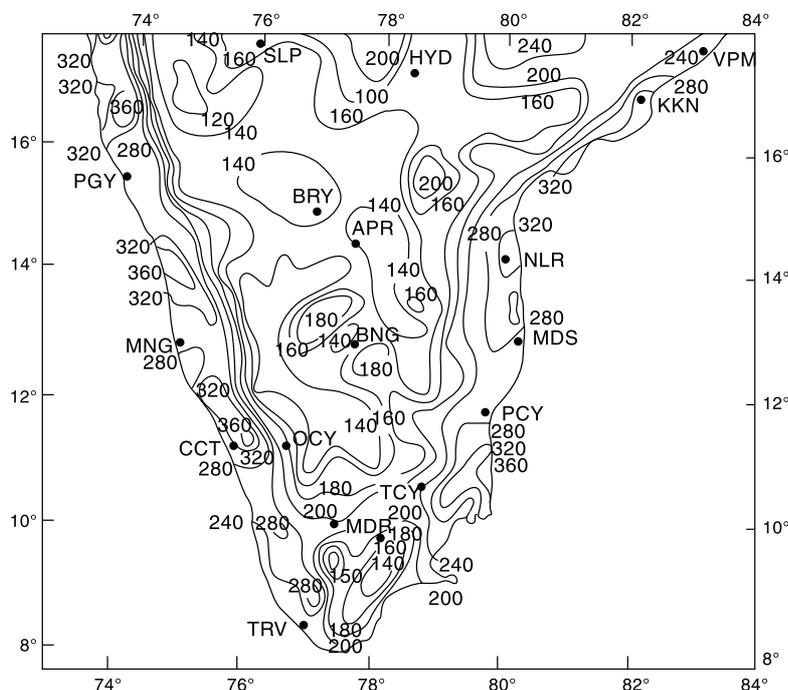
Fig. 2.21 Isopluvial Map of 50 yr-24 h Maximum Rainfall (mm)
(Reproduced with permission from India Meteorological Department)

depths over India and the neighbourhood are shown in Fig. 2.22. Isopluvial maps of the maximum rainfall of various durations and of 50-year return periods covering the entire country are available in Ref. 1.
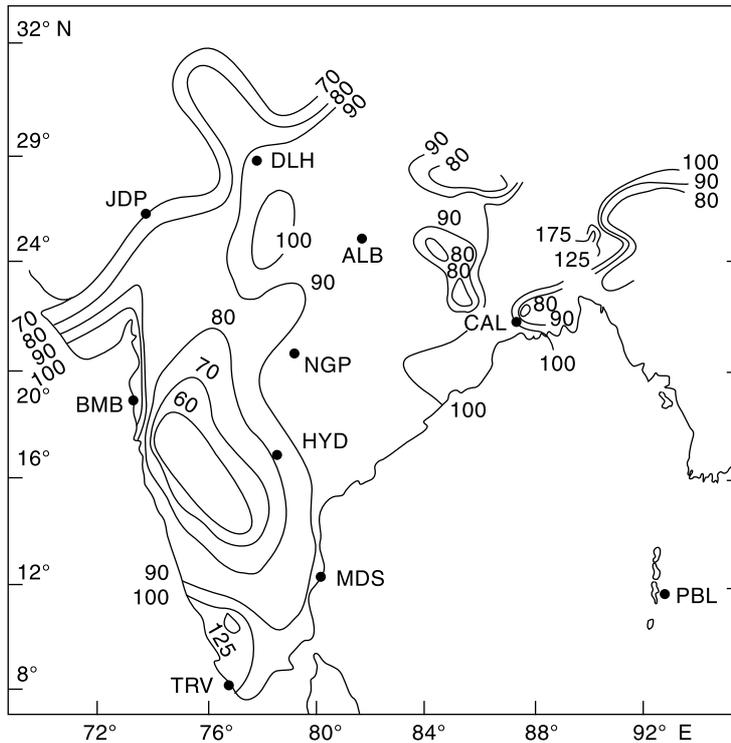
Fig. 2.22 Isopluvial Map of 50 yr-l h Maximum Rainfall (mm)
(Reproduced from *Natural Resources of Humid Tropical Asia—Natural Resources Research,* XII. © UNESCO, 1974, with permission of UNESCO)

Based upon Survey of India map with the permission of the Surveyor General of India © Government of India Copyright 1984

The territorial waters of India extend into the sea to a distance of 200 nautical miles measured from the appropriate baseline

Responsibility for the correctness of the internal details on the map rests with the publisher.

EXAMPLE 2.9 *The mass curve of rainfall in a storm of total duration 270 minutes is given below. (a) Draw the hyetograph of the storm at 30 minutes time step. (b) Plot the maximum intensity-duration curve for this storm. (c) Plot the maximum depth-duration curve for the storm.*

Times since Start in Minutes	0	30	60	90	120	150	180	210	240	270
Cumulative Rainfall (mm)	0	6	18	21	36	43	49	52	53	54

SOLUTION: (a) Hyetograph: The intensity of rainfall at various time durations is calculated as shown below:

Time since Start (min)	30	60	90	120	150	180	210	240	270
Cumulative Rainfall (mm)	6.0	18.0	21.0	36.0	43.0	49.0	52.0	53.0	54.0
Incremental depth of rainfall in the interval (mm)	6.0	12.0	3.0	15.0	7.0	6.0	3.0	1.0	1.0
Intensity (mm/h)	12.0	24.0	6.0	30.0	14.0	12.0	6.0	2.0	2.0

The hyetograph of the storm is shown in Fig. 2.23
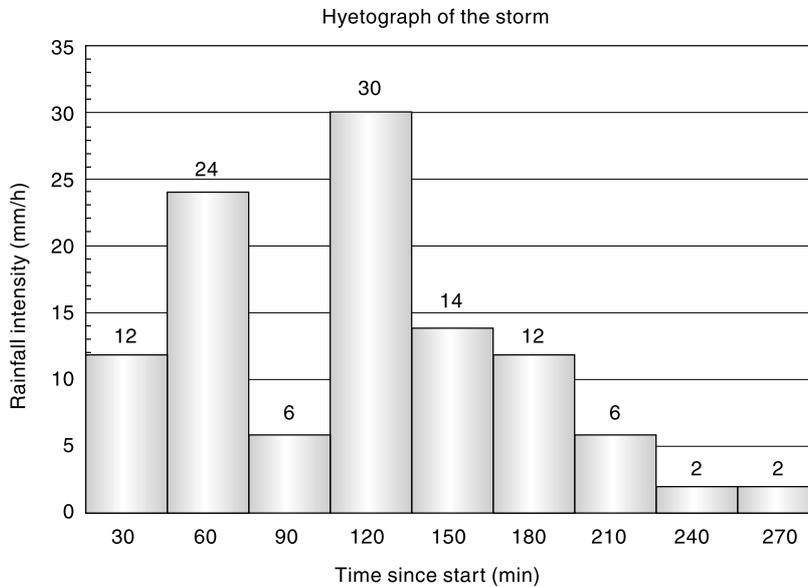
Fig. 2.23 Hyetograph of the Storm—Example 2.9

(b) Various durations Δt = 30, 60, 90 … 240, 270 minutes are chosen. For each duration Δt a series of running totals of rainfall depth is obtained by starting from various points of the mass curve. This can be done systematically as shown in Table 2.7(a & b). By inspection the maximum depth for each t_j is identified and corresponding maximum intensity is calculated. In Table 2.7(a) the maximum depth is marked by bold letter and maximum intensity corresponding to a specified duration is shown in Row No. 3 of Table 2.7(b). The data obtained from the above analysis is plotted as maximum depth *vs* duration and maximum intensity *vs* duration as shown in Fig. 2.24.

2.13 PROBABLE MAXIMUM PRECIPITATION (PMP)

In the design of major hydraulic structures such as spillways in large dams, the hydrologist and hydraulic engineer would like to keep the failure probability as low as possible, i.e. virtually zero. This is because the failure of such a major structure will cause very heavy damages to life, property, economy and national morale. In the design and analysis of such structures, the maximum possible precipitation that can reasonably be expected at a given location is used. This stems from the recognition that there is a physical upper limit to the amount of precipitation that can fall over a specified area in a given time.

Table 2.7(a) Maximum Intensity-Duration Relation

Time (min.)	Cumulative Rainfall (mm)	Incremental depth of rainfall (mm) in various durations								
		Durations(min)								
		30	60	90	120	150	180	210	240	270
0	0									
30	6	6								
60	18	12	18							
90	21	3	15	21						
120	36	**15**	18	**30**	36					
150	43	7	**22**	25	**37**	43				
180	49	6	13	28	31	**43**	49			
210	52	3	9	16	31	34	46	**52**		
240	53	1	4	10	17	32	35	47	**53**	
270	54	1	2	5	11	18	33	36	48	**54**

Table 2.7(b) Maximum Intensity-Maximum Depth-Duration Relation

Maximum Intensity (mm/h)	30.0	22.0	20.0	18.5	17.2	16.3	14.9	13.3	12.0
Duration in min.	30	60	90	120	150	180	210	240	270
Maximum Depth (mm)	15.0	22.0	30.0	37.0	43.0	49.0	52.0	53.0	54.0
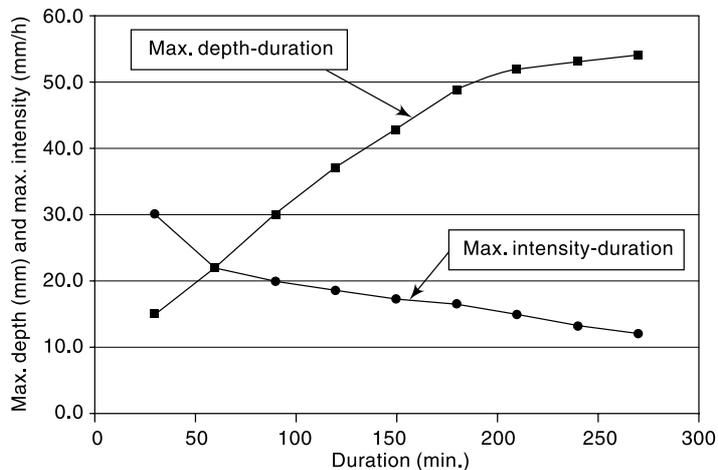
Fig. 2.24 Maximum Intensity-Duration and Maximum Depth-Duration Curves for the Storm of Example 2.9

The probable maximum precipitation (PMP) is defined as the greatest or extreme rainfall for a given duration that is physically possible over a station or basin. From the operational point of view, PMP can be defined as that rainfall over a basin which

would produce a flood flow with virtually no risk of being exceeded. The development of PMP for a given region is an involved procedure and requires the knowledge of an experienced hydrometeorologist. Basically two approaches are used (i) Meteorological methods and (ii) the statistical study of rainfall data. Details of meteorological methods that use storm models are available in published literature.[8]

Statistical studies indicate that PMP can be estimated as

$$\text{PMP} = \bar{P} + K\sigma \qquad (2.16)$$

where $\bar{P}$ = mean of annual maximum rainfall series, σ = standard deviation of the series and K = a frequency factor which depends upon the statistical distribution of the series, number of years of record and the return period. The value of K is usually in the neighbourhood of 15. Generalised charts for one-day PMP prepared on the basis of the statistical analysis of 60 to 70 years of rainfall data in the North-Indian plain area (Lat. 20° N to 32° N, Long. 68° E to 89° E) are available in Refs 4 and 5. It is found that PMP estimates for North-Indian plains vary from 37 to 100 cm for one-day rainfall. Maps depicting isolines of 1-day PMP over different parts of India are available in the PMP atlas published by the Indian Institute of Tropical Meteorology.[6]

WORLD'S GREATEST OBSERVED RAINFALL

Based upon the rainfall records available all over the world, a list of world's greatest recorded rainfalls of various duration can be assembled. When this data is plotted on a log-log paper, an enveloping straight line drawn to the plotted points obeys the equation.

$$P_m = 42.16\ D^{0.475} \qquad (2.17)$$

where P_m = extreme rainfall depth in cm and D = duration in hours. The values obtained from this Eq. (2.17) are of use in PMP estimations.

2.14 RAINFALL DATA IN INDIA

Rainfall measurement in India began in the eighteenth century. The first recorded data were obtained at Calcutta (1784) and it was followed by observations at Madras (1792), Bombay (1823) and Simla (1840). The India Meteorological Department (IMD) was established in 1875 and the rainfall resolution of the Government of India in 1930 empowered IMD to have overall technical control of rainfall registration in the country. According to this resolution, which is still the basis, the recording, collection and publication of rainfall data is the responsibility of the state government whereas the technical control is under IMD. The state government have the obligation to supply daily, monthly and annual rainfall data to IMD for compilation of its two important annual publications entitled *Daily Rainfall of India* and *Monthly Rainfall of India.*

India has a network of observatories and rain gauges maintained by IMD. Currently (2005), IMD has 701 hydrometeorological observatories and 201 agrometeorological observatories. In addition there are 8579 rain gauge stations out of which 3540 stations report their data to IMD. A fair amount of these gauges are of self-recording type and IMD operates nearly 400 self-recording rain gauges.

A set of 21 snow gauges, 10 ordinary rain gauges and 6 seasonal snow poles form part of glaciological observatories of the country.

In addition to the above, a large number of rain gauges are maintained by different governmental agencies such as Railways, State departments of Agriculture, Forestry and Irrigation and also by private agencies like coffee and tea plantations. Data from these stations though recorded regularly are not published and as such are not easily available for hydrological studies.

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REVISION QUESTIONS

2.1 Describe the different methods of recording of rainfall.

2.2 Discuss the current practice and status of rainfall recording in India.

2.3 Describe the salient characteristics of precipitation on India.

2.4 Explain the different methods of determining the average rainfall over a catchment due to a storm. Discuss the relative merits and demerits of the various methods.

2.5 Explain a procedure for checking a rainfall data for consistency.

2.6 Explain a procedure for supplementing the missing rainfall data.

2.7 Explain briefly the following relationships relating to the precipitation over a basin:
  (a) Depth-Area Relationship
  (b) Maximum Depth-Area-Duration Curves
  (c) Intensity Duration Frequency Relationship.

2.8 What is meant by Probable Maximum Precipitation (PMP) over a basin? Explain how PMP is estimated.

2.9 Consider the statement: The 50 year-24 hour maximum rainfall at Bangalore is 160 mm. What do you understand by this statement?

PROBLEMS

2.1 A catchment area has seven raingauge stations. In a year the annual rainfall recorded by the gauges are as follows:

Station	P	Q	R	S	T	U	V
Rainfall (cm)	130.0	142.1	118.2	108.5	165.2	102.1	146.9

For a 5% error in the estimation of the mean rainfall, calculate the minimum number of additional stations required to be established in the catchment.

2.2 The normal annual precipitation of five raingauge stations P, Q, R, S and T are respectively 125, 102, 76, 113 and 137 cm. During a particular storm the precipitation recorded by stations P, Q, R, and S are 13.2, 9.2, 6.8 and 10.2 cm respectively. The instrument at station T was inoperative during that storm. Estimate the rainfall at station T during that storm.

2.3 Test the consistency of the 22 years of data of the annual precipitation measured at station A. Rainfall data for station A as well as the average annual rainfall measured at a group of eight neighbouring stations located in a meteorologically homogeneous region are given as follows.

Year	Annual Rainfall of Station A (mm)	Average Annual Rainfall of 8 Station groups (mm)	Year	Annual Rainfall of Station A (mm)	Average Annual Rainfall of 8 Station groups (mm)
1946	177	143	1957	158	164
1947	144	132	1958	145	155
1948	178	146	1959	132	143
1949	162	147	1960	95	115
1950	194	161	1961	148	135
1951	168	155	1962	142	163
1952	196	152	1963	140	135
1953	144	117	1964	130	143
1954	160	128	1965	137	130
1955	196	193	1966	130	146
1956	141	156	1967	163	161

(a) In what year is a change in regime indicated?

(b) Adjust the recorded data at station A and determine the mean annual precipitation.

2.4 In a storm of 210 minutes duration, the incremental rainfall at various time intervals is given below.

Time since start of the storm (minutes)	30	60	90	120	150	180	210
Incremental rainfall in the time interval (cm)	1.75	2.25	6.00	4.50	2.50	1.50	0.75

(a) Obtain the ordinates of the hyetograph and represent the hyetograph as a bar chart with time in chronological order in the x-axis.

(b) Obtain the ordinates of the mass curve of rainfall for this storm and plot the same. What is the average intensity of storm over the duration of the storm?

2.5 Assuming the density of water as 998 kg/m^3, determine the internal diameter of a tubular snow sample such that 0.1 N of snow in the sample represents 10 mm of water equivalent.

2.6 Represent the annual rainfall data of station A given below as a bar chart with time in chronological order. If the annual rainfall less than 75% of long term mean is taken to signify meteorological drought, identify the drought years and suitably display the same in the bar chart.

Year	1961	1962	1963	1964	1965	1966	1967	1968	1969	1970
Annual rain (mm)	760	750	427	380	480	620	550	640	624	500
Year	1971	1972	1973	1974	1975	1976	1977	1978	1979	1980
Annual rain (mm)	400	356	700	580	520	102	525	900	600	400

2.7 For a drainage basin of 600 km^2, isohyetals drawn for a storm gave the following data:

Isohyetals (interval) (cm)	15–12	12–9	9–6	6–3	3–1
Inter-isohyetal area (km^2)	92	128	120	175	85

Estimate the average depth of precipitation over the catchment.

2.8 There are 10 raingauge stations available to calculate the rainfall characteristics of a catchment whose shape can be approximately described by straight lines joining the following coordinates (distances in kilometres):
(30, 0), (80, 10), (110, 30), (140, 90), (130, 115), (40, 110), (15, 60). Coordinates of the raingauge stations and the annual rainfall recorded in them in the year 1981 are given below.

Station	1	2	3	4	5
Co-ordinates	(0, 40)	(50, 0)	(140, 30)	(140, 80)	(90, 140)
Annual Rainfall (cm)	132	136	93	81	85
Station	**6**	**7**	**8**	**9**	**10**
Co-ordinates	(0, 80)	(40, 50)	(90, 30)	(90, 90)	(40, 80)
Annual Rainfall (cm)	124	156	128	102	128

Determine the average annual rainfall over the catchment.

2.9 Figure 2.25 shows a catchment with seven raingauge stations inside it and three stations outside. The rainfall recorded by each of these stations are indicated in the figure. Draw the figure to an enlarged scale and calculate the mean precipitation by (a) Thiessen-mean method, (b) Isohyetal method and by (c) Arithmetic-mean method.

2.10 Annual rainfall at a point M is needed. At five points surrounding the point M the values of recorded rainfall together with the coordinates of these stations with respect to a set of axes at point M are given below. Estimate the annual rainfall at point M by using the USNWS method.

Station	Rainfall P (cm)	Coordinates of station (in units)	
		X	**Y**
A	102	2.0	1.0
B	120	2.0	2.0
C	126	3.0	1.0
D	108	1.5	1.0
E	131	4.5	1.5
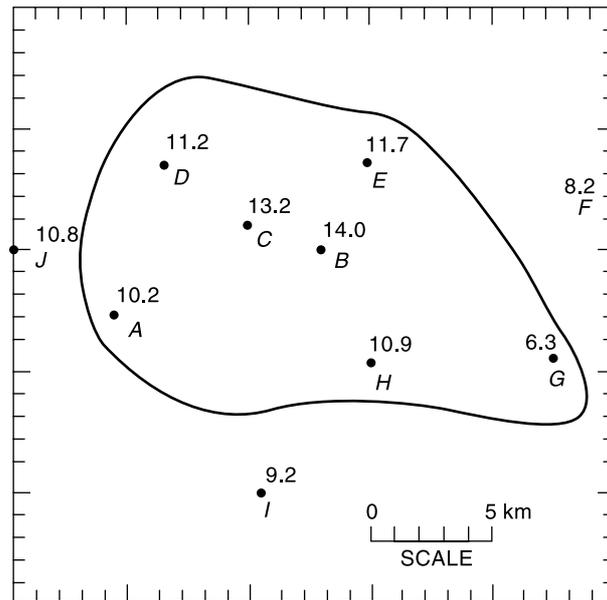
Fig. 2.25 Problem 2.9

> **Hint:** In the US National Weather Service (USNWS) method the weightage to the stations are inversely proportional to the square of the distance of the station from the station M. If the co-ordinate of any station is (x, y) then $D^2 = x^2 + y^2$ and weightage $W = 1/D^2$. Then rainfall at $M = P_m = \dfrac{\Sigma PW}{\Sigma W}$.

2.11 Estimate from depth-area curve, the average depth of precipitation that may be expected over an area of 2400 Sq. km due to the storm of 27th September 1978 which lasted for 24 hours. Assume the storm centre to be located at the centre of the area. The isohyetal map for the storm gave the areas enclosed between different isohyetes as follows:

Isohyet (mm)	21	20	19	18	17	16	15	14	13	12
Enclosed area (km²)	543	1345	2030	2545	2955	3280	3535	3710	3880	3915

2.12 Following are the data of a storm as recorded in a self-recording rain gauge at a station:

Time from the beginning of storm (minutes)	10	20	30	40	50	60	70	80	90
Cumulative rainfall (mm)	19	41	48	68	91	124	152	160	166

(a) Plot the hyetograph of the storm.
(b) Plot the maximum intensity-duration curve of the storm.

2.13 Prepare the Maximum depth-duration curve for the 90 minute storm given below:

Time (minutes)	0	10	20	30	40	50	60	70	80	90
Cumulative rainfall (mm)	0	8	15	25	30	46	55	60	64	67

2.14 The mass curve of rainfall in a storm of total duration 90 minutes is given below. (a) Draw the hyetograph of the storm at 10 minutes time step. (b) Plot the Maximum intensity-duration curve for this storm. (c) Plot the Maximum depth-duration curve for the storm.

Time (Minutes)	0	10	20	30	40	50	60	70	80	90
Cumulative rainfall (mm)	0	2.1	6.3	14.5	21.7	27.9	33.0	35.1	36.2	37.0

2.15 The record of annual rainfall at a place is available for 25 years. Plot the curve of recurrence interval *vs* annual rainfall magnitude and by suitable interpolation estimate the magnitude of rainfall at the station that would correspond to a recurrence interval of (a) 50 years and (b) 100 years.

Year	Annual Rainfall (cm)	Year	Annual Rainfall (cm)
1950	113.0	1963	68.6
1951	94.5	1964	82.5
1952	76.0	1965	90.7
1953	87.5	1966	99.8
1954	92.7	1967	74.4
1955	71.3	1968	66.6
1956	77.3	1969	65.0
1957	85.1	1970	91.0
1958	122.8	1971	106.8
1959	69.4	1972	102.2
1960	81.0	1973	87.0
1961	94.5	1974	84.0
1962	86.3		

2.16 The annual rainfall values at a station *P* for a period of 20 years are as follows:

Year	Annual Rainfall (cm)	Year	Annual Rainfall (cm)
1975	120.0	1985	101.0
1976	84.0	1986	109.0
1977	68.0	1987	106.0
1978	92.0	1988	115.0
1979	102.0	1989	95.0
1980	92.0	1990	90.0
1981	95.0	1991	70.0
1982	88.0	1992	89.0
1983	76.0	1993	80.0
1984	84.0	1994	90.0

Determine
(a) The value of annual rainfall at *P* with a recurrence interval of 15 years.
(b) The probability of occurrence of an annual rainfall of magnitude 100 cm at station *P*.
(c) 75% dependable annual rainfall at the station.
[**Hint:** If an event (rainfall magnitude in the present case) occurs more than once, the rank *m* = number of times the event is equalled + number of times it is exceeded.]

2.17 Plot the three-year and the five-year moving means for the data of Problem 2.15. Comment on the effect of increase in the period of the moving mean. Is there any apparent trend in the data?

2.18 On the basis of isopluvial maps the 50 year-24 hour maximum rainfall at Bangalore is found to be 16.0 cm. Determine the probability of a 24 h rainfall of magnitude 16.0 cm occurring at Bangalore:

(a) Once in ten successive years.

(b) Twice in ten successive years.

(c) At least once in ten successive years.

2.19 A one-day rainfall of 20.0 cm at a place X was found to have a period of 100 years. Calculate the probability that a one-day rainfall of magnitude equal to or larger than 20.0 cm:

(a) Will not occur at station X during the next 50 years.

(b) Will occur in the next year.

2.20 When long records are not available, records at two or more stations are combined to get one long record for the purposes of recurrence interval calculation. This method is known as *Station-year method*.

The number of times a storm of intensity 6 cm/h was equalled or exceeded in three different rain gauge stations in a region were 4, 2 and 5 for periods of records of 36, 25 and 48 years. Find the recurrence interval of the 6 cm/h storm in that area by the *station–year method*.

2.21 Annual precipitation values at a place having 70 years of record can be tabulated as follows:

Range (cm)	Number of years
< 60.0	6
60.0–79.9	6
80.0–99.9	22
100.0–119.9	25
120.0–139.9	8
> 140.0	3

Calculate the probability of having:

(a) an annual rainfall equal to or larger than 120 cm,

(b) two successive years in which the annual rainfall is equal to or greater than 140 cm,

(c) an annual rainfall less than 60 cm.

──────────────── OBJECTIVE QUESTIONS ────────────────

2.1 A tropical cyclone is a

(a) low-pressure zone that occurs in the northern hemisphere only

(b) high-pressure zone with high winds

(c) zone of low pressure with clockwise winds in the northern hemisphere

(d) zone of low pressure with anticlockwise winds in the northern hemisphere.

2.2 A tropical cyclone in the northern hemisphere is a zone of

(a) low pressure with clockwise wind

(b) low pressure with anticlockwise wind

(c) high pressure with clockwise wind

(d) high pressure with anticlockwise wind.

2.3 Orographic precipitation occurs due to air masses being lifted to higher altitudes by
 (a) the density difference of air masses
 (b) a frontal action
 (c) the presence of mountain barriers
 (d) extratropical cyclones.

2.4 The average annual rainfall over the whole of India is estimated as
 (a) 189 cm   (b) 319 cm   (c) 89 cm   (d) 117 cm.

2.5 Variability of annual rainfall in India is
 (a) least in regions of scanty rainfall   (b) largest in regions of high rainfall
 (c) least in regions of high rainfall   (d) largest in coastal areas.

2.6 The standard Symons' type raingauge has a collecting area of diameter
 (a) 12.7 cm   (b) 10 cm   (c) 5.08 cm   (d) 25.4 cm.

2.7 The standard recording raingauge adopted in India is of
 (a) weighing bucket type   (b) natural siphon type
 (c) tipping bucket type   (d) telemetry type

2.8 The following recording raingauges does not produce the mass curve of precipitation as record:
 (a) Symons' raingauge   (b) tipping-bucket type gauge
 (c) weighing-bucket type gauge   (d) natural siphon gauge.

2.9 When specific information about the density of snowfall is not available, the water equivalent of snowfall is taken as
 (a) 50%   (b) 30%   (c) 10%   (d) 90%

2.10 The normal annual rainfall at stations A, B and C situated in meteorologically homogeneous region are 175 cm, 180 cm and 150 cm respectively. In the year 2000, station B was inoperative and stations A and C recorded annual precipitations of 150 cm and 135 cm respectively. The annual rainfall at station B in that year could be estimated to be nearly
 (a) 150 cm   (b) 143 cm   (c) 158 cm   (d) 168 cm

2.11 The monthly rainfall at a place A during September 1982 was recorded as 55 mm above normal. Here the term *normal* means
 (a) the rainfall in the same month in the previous year
 (b) the rainfall was normally expected based on previous month's data
 (c) the average rainfall computed from past 12 months' record
 (d) The average monthly rainfall for September computed from a specific 30 years of past record.

2.12 The Double mass curve technique is adopted to
 (a) check the consistency of raingauge records
 (b) to find the average rainfall over a number of years
 (c) to find the number of rainguages required
 (d) to estimate the missing rainfall data

2.13 The mass curve of rainfall of a storm is a plot of
 (a) rainfall depths for various equal durations plotted in decreasing order
 (b) rainfall intensity *vs* time in chronological order
 (c) accumulated rainfall intensity *vs* time
 (d) accumulated precipitation *vs* time in chronological order.

2.14 A plot between rainfall intensity *vs* time is called as
 (a) hydrograph   (b) mass curve   (c) hyetograph   (d) isohyet

2.15 A hyetograph is a plot of
 (a) Cumulative rainfall *vs* time   (b) rainfall intensity *vs* time
 (c) rainfall depth *vs* duration   (d) discharge *vs* time

2.16 The Thiessen polygon is
  (a) a polygon obtained by joining adjoining raingauge stations
  (b) a representative area used for weighing the observed station precipitation
  (c) an area used in the construction of depth-area curves
  (d) the descriptive term for the shape of a hydrograph.

2.17 An isohyet is a line joining points having
  (a) equal evaporation value   (b) equal barometric pressure
  (c) equal height above the MSL   (d) equal rainfall depth in a given duration.

2.18 By DAD analysis the maximum average depth over an area of 10^4 km^2 due to one-day storm is found to be 47 cm. For the same area the maximum average depth for a three day storm can be expected to be
  (a) < 47 cm   (b) > 47 cm   (c) $= 47$ cm
  (d) inadequate information to conclude.

2.19 Depth-Area-Duration curves of precipitation are drawn as
  (a) minimizing envelopes through the appropriate data points
  (b) maximising envelopes through the appropriate data point
  (c) best fit mean curves through the appropriate data points
  (d) best fit straight lines through the appropriate data points

2.20 Depth-Area-Duration curves of precipitation at a station would normally be
  (a) curves, concave upwards, with duration increasing outward
  (b) curves, concave downwards, with duration increasing outward
  (c) curves, concave upwards, with duration decreasing outward
  (d) curves, concave downwards, with duration decreasing outward

2.21 A study of the isopluvial maps revealed that at Calcutta a maximum rainfall depth of 200 mm in 12 h has a return period of 50 years. The probability of a 12 h rainfall equal to or greater than 200 mm occurring at Calcutta at least once in 30 years is
  (a) 0.45   (b) 0.60   (c) 0.56   (d) 1.0

2.22 A 6-h rainfall of 6 cm at a place A was found to have a return period of 40 years. The probability that at A a 6-h rainfall of this or larger magnitude will occur at least once in 20 successive years is
  (a) 0.397   (b) 0.603   (c) 0.309   (d) 0.025

2.23 The probability of a 10 cm rain in 1 hour occurring at a station B is found to be 1/60. What is the probability that a 1 hour rain of magnitude 10 cm or larger will occur in station B once in 30 successive years is
  (a) 0.396   (b) 0.307   (c) 0.604   (d) 0.500

2.24 A one day rainfall of 18 hours at Station C was found to have a return period of 50 years. The probability that a one-day rainfall of this or larger magnitude will not occur at station C during next 50 years is
  (a) 0.636   (b) 0.020   (c) 0.364   (d) 0.371

2.25 If the maximum depth of a 50 years-15 h-rainfall depth at Bhubaneshwar is 260 mm, the 50 year-3 h-maximum rainfall depth at the same place is
  (a) < 260 mm   (b) > 260 mm   (c) $= 260$ mm
  (d) inadequate date to conclude anything.

2.26 The probable maximum depth of precipitation over a catchment is given by the relation PMP =
  (a) $\bar{P} + KA^n$ (b) $\bar{P} + K\sigma$ (c) $\bar{P} \exp(-K A^n)$ (d) $m\bar{P}$

ABSTRACTIONS FROM PRECIPITATION

3.1 INTRODUCTION

In Engineering Hydrology runoff due to a storm event is often the major subject of study. All abstractions from precipitation, viz. those due to evaporation, transpiration, infiltration, surface detention and storage, are considered as losses in the production of runoff. Chief components of abstractions from precipitation, knowledge of which are necessary in the analysis of various hydrologic situations, are described in this chapter.

Evaporation from water bodies and soil masses together with transpiration from vegetation is termed as *evapotranspiration*. Various aspects of evaporation from water bodies and evapotranspiration from a basin are discussed in detail in Secs 3.2 through 3.11. Interception and depression storages, which act as 'losses' in the production of runoff, are discussed in Secs 3.12 and 3.13. Infiltration process, which is a major abstraction from precipitation and an important process in groundwater recharge and in increasing soil moisture storage, is described in detail in Secs 3.14 through 3.19.

A: EVAPORATION

3.2 EVAPORATION PROCESS

Evaporation is the process in which a liquid changes to the gaseous state at the free surface, below the boiling point through the transfer of heat energy. Consider a body of water in a pond. The molecules of water are in constant motion with a wide range of instantaneous velocities. An addition of heat causes this range and average speed to increase. When some molecules possess sufficient kinetic energy, they may cross over the water surface. Similarly, the atmosphere in the immediate neighbourhood of the water surface contains water molecules within the water vapour in motion and some of them may penetrate the water surface. The net escape of water molecules from the liquid state to the gaseous state constitutes evaporation. Evaporation is a cooling process in that the latent heat of vaporization (at about 585 cal/g of evaporated water) must be provided by the water body. The rate of evaporation is dependent on (i) the vapour pressures at the water surface and air above, (ii) air and water temperatures, (iii) wind speed, (iv) atmospheric pressure, (v) quality of water, and (vi) size of the water body.

VAPOUR PRESSURE

The rate of evaporation is proportional to the difference between the saturation vapour pressure at the water temperature, e_w and the actual vapour pressure in the air, e_a. Thus

$$E_L = C(e_w - e_a) \qquad (3.1)$$

where E_L = rate of evaporation (mm/day) and C = a constant; e_w and e_a are in mm of mercury. Equation (3.1) is known as *Dalton's law of evaporation* after John Dalton (1802) who first recognised this law. Evaporation continues till $e_w = e_a$. If $e_w > e_a$ condensation takes place.

TEMPERATURE   Other factors remaining the same, the rate of evaporation increases with an increase in the water temperature. Regarding air temperature, although there is a general increase in the evaporation rate with increasing temperature, a high correlation between evaporation rate and air temperature does not exist. Thus for the same mean monthly temperature it is possible to have evaporation to different degrees in a lake in different months.

WIND   Wind aids in removing the evaporated water vapour from the zone of evaporation and consequently creates greater scope for evaporation. However, if the wind velocity is large enough to remove all the evaporated water vapour, any further increase in wind velocity does not influence the evaporation. Thus the rate of evaporation increases with the wind speed up to a critical speed beyond which any further increase in the wind speed has no influence on the evaporation rate. This critical wind-speed value is a function of the size of the water surface. For large water bodies high-speed turbulent winds are needed to cause maximum rate of evaporation.

ATMOSPHERIC PRESSURE   Other factors remaining same, a decrease in the barometric pressure, as in high altitudes, increases evaporation.

SOLUBLE SALTS   When a solute is dissolved in water, the vapour pressure of the solution is less than that of pure water and hence causes reduction in the rate of evaporation. The percent reduction in evaporation approximately corresponds to the percentage increase in the specific gravity. Thus, for example, under identical conditions evaporation from sea water is about 2–3% less than that from fresh water.

HEAT STORAGE IN WATER BODIES   Deep water bodies have more heat storage than shallow ones. A deep lake may store radiation energy received in summer and release it in winter causing less evaporation in summer and more evaporation in winter compared to a shallow lake exposed to a similar situation. However, the effect of heat storage is essentially to change the seasonal evaporation rates and the annual evaporation rate is seldom affected.

3.3   EVAPORIMETERS

Estimation of evaporation is of utmost importance in many hydrologic problems associated with planning and operation of reservoirs and irrigation systems. In arid zones, this estimation is particularly important to conserve the scarce water resources. However, the exact measurement of evaporation from a large body of water is indeed one of the most difficult tasks.

The amount of water evaporated from a water surface is estimated by the following methods: (i) using evaporimeter data, (ii) empirical evaporation equations, and (iii) analytical methods.

TYPES OF EVAPORIMETERS

Evaporimeters are water-containing pans which are exposed to the atmosphere and the loss of water by evaporation measured in them at regular intervals. Meteorological

data, such as humidity, wind movement, air and water temperatures and precipitation are also noted along with evaporation measurement.

Many types of evaporimeters are in use and a few commonly used pans are described here.

CLASS A EVAPORATION PAN   It is a standard pan of 1210 mm diameter and 255 mm depth used by the US Weather Bureau and is known as Class A Land Pan. The depth of water is maintained between 18 cm and 20 cm (Fig. 3.1). The pan is normally made of unpainted galvanised iron sheet. Monel metal is used where

Fig. 3.1   U.S. Class *A* Evaporation Pan

corrosion is a problem. The pan is placed on a wooden platform of 15 cm height above the ground to allow free circulation of air below the pan. Evaporation measurements are made by measuring the depth of water with a hook gauge in a stilling well.

ISI STANDARD PAN   This pan evaporimeter specified by IS: 5973–1970, also known as modified Class A Pan, consists of a pan 1220 mm in diameter with 255 mm of depth. The pan is made of copper sheet of 0.9 mm thickness, tinned inside and painted white outside (Fig. 3.2). A fixed point gauge indicates the level of water. A calibrated cylindrical measure is used to add or remove water maintaining the water level in the pan to a fixed mark. The top of the pan is covered fully with a hexagonal wire netting of galvanized iron to protect the water in the pan from birds. Further, the presence of a wire mesh makes the water temperature more uniform during day and night. The evaporation from this pan is found to be less by about 14% compared to that from unscreened pan. The pan is placed over a square wooden platform of 1225 mm width and 100 mm height to enable circulation of air underneath the pan.
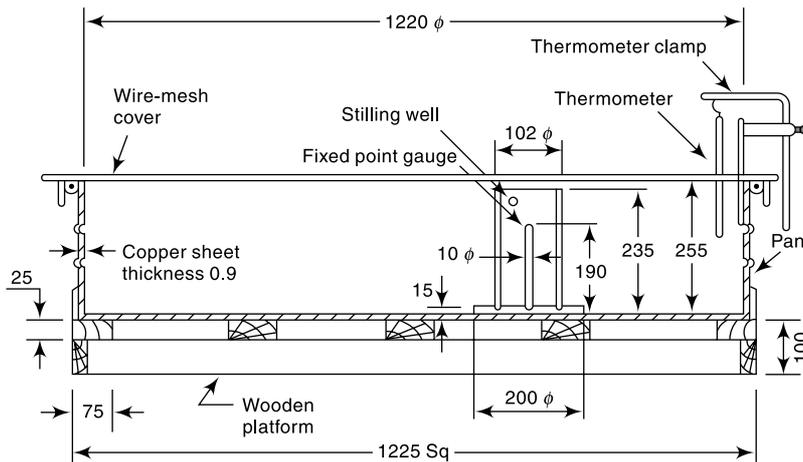
Fig. 3.2   ISI Evaporation Pan

COLORADO SUNKEN PAN
This pan, 920 mm square and 460 mm deep is made up of unpainted galvanised iron sheet and buried into the ground within 100 mm of the top (Fig. 3.3). The chief advantage of the sunken pan is that radiation and aerodynamic characteristics are similar to those of a lake. However, it has the following disadvantages: (i) difficult to detect leaks, (ii) extra care is needed to keep the surrounding area free from tall grass, dust, etc., and (iii) expensive to instal.
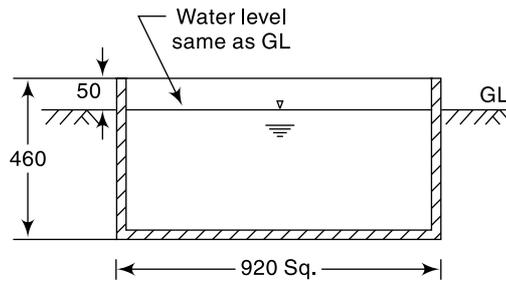
Fig. 3.3 Colorado Sunken Evaporation Pan

US GEOLOGICAL SURVEY FLOATING PAN   With a view to simulate the characteristics of a large body of water, this square pan (900 mm side and 450 mm depth) supported by drum floats in the middle of a raft (4.25 m × 4.87 m) is set afloat in a lake. The water level in the pan is kept at the same level as the lake leaving a rim of 75 mm. Diagonal baffles provided in the pan reduce the surging in the pan due to wave action. Its high cost of installation and maintenance together with the difficulty involved in performing measurements are its main disadvantages.

PAN COEFFICIENT C_P Evaporation pans are not exact models of large reservoirs and have the following principal drawbacks:

1. They differ in the heat-storing capacity and heat transfer from the sides and bottom. The sunken pan and floating pan aim to reduce this deficiency. As a result of this factor the evaporation from a pan depends to a certain extent on its size. While a pan of 3 m diameter is known to give a value which is about the same as from a neighbouring large lake, a pan of size 1.0 m diameter indicates about 20% excess evaporation than that of the 3 m diameter pan.
2. The height of the rim in an evaporation pan affects the wind action over the surface. Also, it casts a shadow of variable magnitude over the water surface.
3. The heat-transfer characteristics of the pan material is different from that of the reservoir.

In view of the above, the evaporation observed from a pan has to be corrected to get the evaporation from a lake under similar climatic and exposure conditions. Thus a coefficient is introduced as

$$\text{Lake evaporation} = C_p \times \text{pan evaporation}$$

in which C_p = pan coefficient. The values of C_p in use for different pans are given in Table 3.l.

Table 3.1 Values of Pan Coefficient C_p

S.No.	Types of pan	Average value	Range
1.	Class A Land Pan	0.70	0.60–0.80
2.	ISI Pan (modified Class A)	0.80	0.65–1.10
3.	Colorado Sunken Pan	0.78	0.75–0.86
4.	USGS Floating Pan	0.80	0.70–0.82

EVAPORATION STATIONS   It is usual to instal evaporation pans in such locations where other meteorological data are also simultaneously collected. The WMO recommends the minimum network of evaporimeter stations as below:

1. Arid zones—One station for every 30,000 km^2,
2. Humid temperate climates—One station for every 50,000 km^2, and
3. Cold regions—One station for every 100,000 km^2.

Currently, about 220 pan-evaporimeter stations are being maintained by India Meteorological Department.

A typical hydrometeorological station contains the following: Ordinary raingauge; Recording raingauge; Stevenson Box with maximum and minimum thermometer and dry and wet bulb thermometers; wind anemometer, wind direction indicator, sunshine recorder, thermohydrograph and pan evaporimeter.

3.4   EMPIRICAL EVAPORATION EQUATIONS

A large number of empirical equations are available to estimate lake evaporation using commonly available meteorological data. Most formulae are based on the Dalton-type equation and can be expressed in the general form

$$E_L = Kf(u)(e_w - e_a) \tag{3.2}$$

where E_L = lake evaporation in mm/day, e_w = saturated vapour pressure at the water-surface temperature in mm of mercury, e_a = actual vapour pressure of over-lying air at a specified height in mm of mercury, $f(u)$ = wind-speed correction function and K = a coefficient. The term e_a is measured at the same height at which wind speed is measured. Two commonly used empirical evaporation formulae are:

MEYER'S FORMULA (1915)

$$E_L = K_M(e_w - e_a)\left(1 + \frac{u_9}{16}\right) \tag{3.3}$$

in which E_L, e_w, e_a are as defined in Eq. (3.2), u_9 = monthly mean wind velocity in km/h at about 9 m above ground and K_M = coefficient accounting for various other factors with a value of 0.36 for large deep waters and 0.50 for small, shallow waters.

ROHWER'S FORMULA (1931)   Rohwer's formula considers a correction for the effect of pressure in addition to the wind-speed effect and is given by

$$E_L = 0.771(1.465 - 0.000732\, p_a)(0.44 + 0.0733\, u_0)\,(e_w - e_a) \tag{3.4}$$

in which E_L, e_w, and e_a are as defined earlier in Eq. (3.2),

p_a = mean barometric reading in mm of mercury

u_0 = mean wind velocity in km/h at ground level, which can be taken to be the velocity at 0.6 m height above ground.

These empirical formulae are simple to use and permit the use of standard meteorological data. However, in view of the various limitations of the formulae, they can at best be expected to give an approximate magnitude of the evaporation. References 2 and 3 list several other popular empirical formulae.

In using the empirical equations, the saturated vapour pressure at a given temperature (e_w) is found from a table of e_w *vs* temperature in °C, such as Table 3.3. Often, the wind-velocity data would be available at an elevation other than that needed in the particular equation. However, it is known that in the lower part of the atmosphere, up

to a height of about 500 m above the ground level, the wind velocity can be assumed to follow the 1/7 power law as

$$u_h = Ch^{1/7} \tag{3.5}$$

where u_h = wind velocity at a height h above the ground and C = constant. This equation can be used to determine the velocity at any desired level if u_h is known.

EXAMPLE 3.1

(a) A reservoir with a surface area of 250 hectares had the following average values of climate parameters during a week: Water temperature = 20°C, Relative humidity = 40%, Wind velocity at 1.0 m above ground surface = 16 km/h. Estimate the average daily evaporation from the lake by using Meyer's formula.

(b) An ISI Standard evaporation pan at the site indicated a pan coefficient of 0.80 on the basis of calibration against controlled water budgeting method. If this pan indicated an evaporation of 72 mm in the week under question, (i) estimate the accuracy if Meyer's method relative to the pan evaporation measurements. (ii) Also, estimate the volume of water evaporated from the lake in that week.

SOLUTION:

(a) From Table 3.3

e_w = 17.54 mm of Hg e_a = 0.4 × 17.54 = 7.02 mm of Hg

u_9 = wind velocity at a height of 9.0 m above ground = $u_1 \times (9)^{1/7}$ = 21.9 km/h

By Meyer's Formula [Eq. (3.3)],

$$E_L = 0.36\,(17.54 - 7.02)\left(1 + \frac{21.9}{16}\right) = 8.97 \text{ mm/day}$$

(b) (i) Daily evaporation as per Pan evaporimeter = $\left(\dfrac{72.00}{7}\right) \times 0.8 = 8.23$ mm

Error by Meyer's formula = (8.23 − 8.97) = −0.74 mm. Hence, Meyer's method overestimates the evaporation relative to the Pan.

Percentage over estimation by Meyer's formula = (0.74/8.23) × 100 = 9%

(ii) Considering the Pan measurements as the basis, volume of water evaporated from the lake in 7 days = $7 \times (8.23/1000) \times 250 \times 10^4 = 144{,}025$ m^3

[The lake area is assumed to be constant at 250 ha throughout the week.]

3.5 ANALYTICAL METHODS OF EVAPORATION ESTIMATION

The analytical methods for the determination of lake evaporation can be broadly classified into three categories as:

1. Water-budget method,   2. Energy-balance method, and

3. Mass-transfer method.

WATER-BUDGET METHOD

The water-budget method is the simplest of the three analytical methods and is also the least reliable. It involves writing the hydrological continuity equation for the lake and determining the evaporation from a knowledge or estimation of other variables. Thus considering the daily average values for a lake, the continuity equation is written as

$$P + V_{is} + V_{ig} = V_{os} + V_{og} + E_L + \Delta S + T_L \tag{3.6}$$

where P = daily precipitation

V_{is} = daily surface inflow into the lake
V_{ig} = daily groundwater inflow
V_{os} = daily surface outflow from the lake
V_{og} = daily seepage outflow
E_L = daily lake evaporation
ΔS = increase in lake storage in a day
T_L = daily transpiration loss

All quantities are in units of volume (m^3) or depth (mm) over a reference area. Equation (3.6) can be written as

$$E_L = P + (V_{is} - V_{os}) + (V_{ig} - V_{og}) - T_L - \Delta S \tag{3.7}$$

In this the terms P, V_{is}, V_{os} and ΔS can be measured. However, it is not possible to measure V_{ig}. V_{og} and T_L and therefore these quantities can only be estimated. Transpiration losses can be considered to be insignificant in some reservoirs. If the unit of time is kept large, say weeks or months, better accuracy in the estimate of E_L is possible. In view of the various uncertainties in the estimated values and the possibilities of errors in measured variables, the water-budget method cannot be expected to give very accurate results. However, controlled studies such as at Lake Hefner in USA (1952) have given fairly accurate results by this method.

ENERGY-BUDGET METHOD

The energy-budget method is an application of the law of conservation of energy. The energy available for evaporation is determined by considering the incoming energy, outgoing energy and energy stored in the water body over a known time interval.

Considering the water body as in Fig. 3.4, the energy balance to the evaporating surface in a period of one day is give by

$$H_n = H_a + H_e + H_g + H_s + H_i \tag{3.8}$$

where H_n = net heat energy received by the water surface
             = $H_c(1 - r) - H_b$
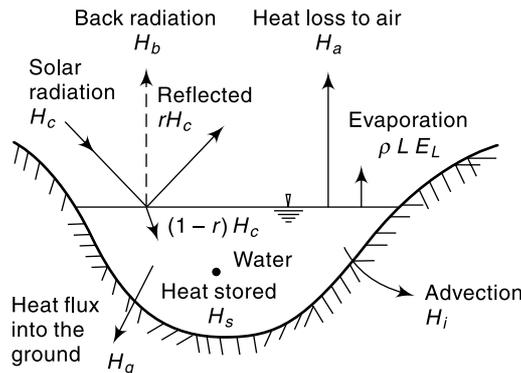
Fig. 3.4   Energy Balance in a Water Body

in which $H_c(1 - r)$ = incoming solar radiation into a surface of reflection
                         coefficient (albedo) r

H_b = back radiation (long wave) from water body

H_a = sensible heat transfer from water surface to air

H_e = heat energy used up in evaporation

    = $\rho L E_L$, where ρ = density of water, L = latent heat of evaporation and E_L = evaporation in mm

H_g = heat flux into the ground

H_s = heat stored in water body

H_i = net heat conducted out of the system by water flow (advected energy)

All the energy terms are in calories per square mm per day. If the time periods are short, the terms H_s and H_i can be neglected as negligibly small. All the terms except H_a can either be measured or evaluated indirectly. The sensible heat term H_a which cannot be readily measured is estimated using *Bowen's ratio* β given by the expression

$$\beta = \frac{H_a}{\rho L E_L} = 6.1 \times 10^{-4} \times p_a \frac{T_w - T_a}{e_w - e_a} \tag{3.9}$$

where p_a = atmospheric pressure in mm of mercury, e_w = saturated vapour pressure in mm of mercury, e_a = actual vapour pressure of air in mm of mercury, T_w = temperature of water surface in °C and T_a = temperature of air in °C. From Eqs (3.8) and (3.9) E_L can be evaluated as

$$E_L = \frac{H_n - H_g - H_s - H_i}{\rho L (1 + \beta)} \tag{3.10}$$

Estimation of evaporation in a lake by the energy balance method has been found to give satisfactory results, with errors of the order of 5% when applied to periods less than a week. Further details of the energy-budget method are available in Refs 2, 3 and 5.

MASS-TRANSFER METHOD

This method is based on theories of turbulent mass transfer in boundary layer to calculate the mass water vapour transfer from the surface to the surrounding atmosphere. However, the details of the method are beyond the scope of this book and can be found in published literature[2, 5]. With the use of quantities measured by sophisticated (and expensive) instrumentation, this method can give satisfactory results.

3.6 RESERVOIR EVAPORATION AND METHODS FOR ITS REDUCTION

Any of the methods mentioned above may be used for the estimation of reservoir evaporation. Although analytical methods provide better results, they involve parameters that are difficult to assess or expensive to obtain. Empirical equations can at best give approximate values of the correct order of magnitude. Therefore, the pan measurements find general acceptance for practical application. Mean monthly and annual evaporation data collected by IMD are very valuable in field estimations. The water volume lost due to evaporation from a reservoir in a month is calculated as

$$V_E = A \, E_{pm} \, C_p \tag{3.11}$$

where V_E = volume of water lost in evaporation in a month (m³)

        A = average reservoir area during the month (m²)

E_{pm} = pan evaporation loss in metres in a month (m)

= E_L in mm/day × No. of days in the month × 10^{-3}

C_p = relevant pan coefficient

Evaporation from a water surface is a continuous process. Typically under Indian conditions, evaporation loss from a water body is about 160 cm in a year with enhanced values in arid regions. The quantity of stored water lost by evaporation in a year is indeed considerable as the surface area of many natural and man-made lakes in the country are very large. While a small sized tank (lake) may have a surface area of about 20 ha large reservoirs such as Narmada Sagar have surface area of about 90,000 ha. Table 3.2 (a) indicates surface areas and capacities of some large Indian reservoirs.

Table 3.2(a)   Surface Areas and Capacities of Some Indian Reservoirs

Sl. No	Reservoir	River	State	Surface area at MRL in km^2	Gross capacity of the reservoir in Mm^3
1.	Narmada Sagar	Narmada	Madhya Pradesh	914	12,230
2.	Nagarjuna Sagar	Krishna	Andhra Pradesh	285	11,315
3.	Sardar Sarovar	Narmada	Gujarat	370	9510
4.	Bhakra	Sutlej	Punjab	169	9868
5.	Hirakud	Mahanadi	Orissa	725	8141
6.	Gandhi Sagar	Chambal	Madhya Pradesh	660	7746
7.	Tungabhadra	Tungabhadra	Karnataka	378	4040
8.	Shivaji Sagar	Koyna	Maharashtra	115	2780
9.	Kadana	Mahi	Gujarat	172	1714
10.	Panchet	Damodar	Jharkhand	153	1497

Using evaporation data from 29 major and medium reservoirs in the country, the National Commission for integrated water resources development (1999)[8] has estimated the national water loss due to evaporation at various time horizons as below:

Table 3.2(b)   Water Loss due to Evaporation (Volume in km^3)

Sl. No.	Particular	1997	2010	2025	2050
1.	Live Capacity–Major storage	173.7	211.4	249.2	381.5
2.	Live Capacity–Minor storage	34.7	42.3	49.8	76.3
3.	Evaporation for Major storage Reservoirs @ 15% of live capacity	26.1	31.7	37.4	57.2
4.	Evaporation for Minor storage Reservoirs @ 25% of live capacity	8.7	10.6	12.5	19.1
5.	**Total Evaporation loss**	**35**	**42**	**50**	**76**

Roughly, a quantity equivalent to entire live capacity of minor storages is lost annually by evaporation. As the construction of various reservoirs as a part of water resources developmental effort involve considerable inputs of money, which is a scarce resource, evaporation from such water bodies signifies an economic loss. In semi-arid zones where water is scarce, the importance of conservation of water through reduction of evaporation is obvious.

Methods to Reduce Evaporation Losses

Various methods available for reduction of evaporation losses can be considered in three categories:

(i) Reduction of Surface Area   Since the volume of water lost by evaporation is directly proportional to the surface area of the water body, the reduction of surface area wherever feasible reduces evaporation losses. Measures like having deep reservoirs in place of wider ones and elimination of shallow areas can be considered under this category.

(ii) Mechanical Covers   Permanent roofs over the reservoir, temporary roofs and floating roofs such as rafts and light-weight floating particles can be adopted wherever feasible. Obviously these measures are limited to very small water bodies such as ponds, etc.

(iii) Chemical Films   This method consists of applying a thin chemical film on the water surface to reduce evaporation. Currently this is the only feasible method available for reduction of evaporation of reservoirs up to moderate size.

Certain chemicals such as *cetyl alcohol* (hexadecanol) and *stearyl alcohol* (octadecanol) form monomolecular layers on a water surface. These layers act as evaporation inhibitors by preventing the water molecules to escape past them. The thin film formed has the following desirable features:

1. The film is strong and flexible and does not break easily due to wave action.
2. If punctured due to the impact of raindrops or by birds, insects, etc., the film closes back soon after.
3. It is pervious to oxygen and carbon dioxide; the water quality is therefore not affected by its presence.
4. It is colourless, odourless and nontoxic.

Cetyl alcohol is found to be the most suitable chemical for use as an evaporation inhibitor. It is a white, waxy, crystalline solid and is available as lumps, flakes or powder. It can be applied to the water surface in the form of powder, emulsion or solution in mineral turpentine. Roughly about 3.5 N/hectare/day of cetyl alcohol is needed for effective action. The chemical is periodically replenished to make up the losses due to oxidation, wind sweep of the layer to the shore and its removal by birds and insects. Evaporation reduction can be achieved to a maximum if a film pressure of 4×10^{-2} N/m is maintained.

Controlled experiments with evaporation pans have indicated an evaporation reduction of about 60% through use of cetyl alcohol. Under field conditions, the reported values of evaporation reduction range from 20 to 50%. It appears that a reduction of 20–30% can be achieved easily in small size lakes (≤ 1000 hectares) through the use of these monomolecular layers. The adverse effect of heavy wind appears to be the only major impediment affecting the efficiency of these chemical films.

B: Evapotranspiration

3.7 TRANSPIRATION

Transpiration is the process by which water leaves the body of a living plant and reaches the atmosphere as water vapour. The water is taken up by the plant-root system

and escapes through the leaves. The important factors affecting transpiration are: atmospheric vapour pressure, temperature, wind, light intensity and characteristics of the plant, such as the root and leaf systems. For a given plant, factors that affect the free-water evaporation also affect transpiration. However, a major difference exists between transpiration and evaporation. Transpiration is essentially confined to daylight hours and the rate of transpiration depends upon the growth periods of the plant. Evaporation, on the other hand, continues all through the day and night although the rates are different.

3.8   EVAPOTRANSPIRATION

While transpiration takes place, the land area in which plants stand also lose moisture by the evaporation of water from soil and water bodies. In hydrology and irrigation practice, it is found that evaporation and transpiration processes can be considered advantageously under one head as evapotranspiration. The term *consumptive use* is also used to denote this loss by evapotranspiration. For a given set of atmospheric conditions, evapotranspiration obviously depends on the availability of water. If sufficient moisture is always available to completely meet the needs of vegetation fully covering the area, the resulting evapotranspiration is called *potential evapotranspiration* (PET). Potential evapotranspiration no longer critically depends on the soil and plant factors but depends essentially on the climatic factors. The real evapotranspiration occurring in a specific situation is called *actual evapotranspiration* (AET).

It is necessary to introduce at this stage two terms: *field capacity* and *permanent wilting point*. Field capacity is the maximum quantity of water that the soil can retain against the force of gravity. Any higher moisture input to a soil at field capacity simply drains away. Permanent wilting point is the moisture content of a soil at which the moisture is no longer available in sufficient quantity to sustain the plants. At this stage, even though the soil contains some moisture, it will be so held by the soil grains that the roots of the plants are not able to extract it in sufficient quantities to sustain the plants and consequently the plants wilt. The field capacity and permanent wilting point depend upon the soil characteristics. The difference between these two moisture contents is called *available water*, the moisture available for plant growth.

If the water supply to the plant is adequate, soil moisture will be at the field capacity and AET will be equal to PET. If the water supply is less than PET, the soil dries out and the ratio AET/PET would then be less than unity. The decrease of the ratio AET/PET with available moisture depends upon the type of soil and rate of drying. Generally, for clayey soils, AET/PET = 1.0 for nearly 50% drop in the available moisture. As can be expected, when the soil moisture reaches the permanent wilting point, the AET reduces to zero (Fig. 3.5). For a catchment in a given period of time, the hydrologic budget can be written as

$$P - R_s - G_o - E_{act} = \Delta S \qquad (3.12)$$

where P = precipitation, R_s = surface runoff, G_o = subsurface outflow, E_{act} = actual evapotranspiration (AET) and ΔS = change in the moisture storage. This water budgeting can be used to calculate E_{act} by knowing or estimating other elements of Eq. (3.12). Generally, the sum of R_s and G_o can be taken as the stream flow at the basin outlet without much error. Method of estimating AET is given in Sec. 3.11.
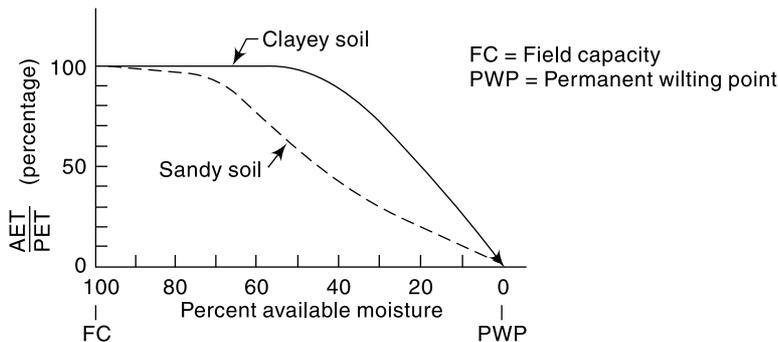
Fig. 3.5 Variation of AET

Except in a few specialized studies, all applied studies in hydrology use PET (not AET) as a basic parameter in various estimations related to water utilizations connected with evapotranspiration process. It is generally agreed that PET is a good approximation for lake evaporation. As such, where pan evaporation data is not available, PET can be used to estimate lake evaporation.

3.9   MEASUREMENT OF EVAPOTRANSPIRATION

The measurement of evapotranspiration for a given vegetation type can be carried out in two ways: either by using lysimeters or by the use of field plots.

LYSIMETERS

A lysimeter is a special watertight tank containing a block of soil and set in a field of growing plants. The plants grown in the lysimeter are the same as in the surrounding field. Evapotranspiration is estimated in terms of the amount of water required to maintain constant moisture conditions within the tank measured either volumetric ally or gravimetrically through an arrangement made in the lysimeter. Lysimeters should be designed to accurately reproduce the soil conditions, moisture content, type and size of the vegetation of the surrounding area. They should be so buried that the soil is at the same level inside and outside the container. Lysimeter studies are time-consuming and expensive.

FIELD PLOTS

In special plots all the elements of the water budget in a known interval of time are measured and the evapotranspiration determined as

Evapotranspiration = [precipitation + irrigation input – runoff
– increase in soil storage groundwater loss]

Measurements are usually confined to precipitation, irrigation input, surface runoff and soil moisture. Groundwater loss due to deep percolation is difficult to measure and can be minimised by keeping the moisture condition of the plot at the field capacity. This method provides fairly reliable results.

3.10   EVAPOTRANSPIRATION EQUATIONS

The lack of reliable field data and the difficulties of obtaining reliable evapotranspiration data have given rise to a number of methods to predict PET by using climatological

data. Large number of formulae are available: they range from purely empirical ones to those backed by theoretical concepts. Two useful equations are given below.

PENMAN'S EQUATION

Penman's equation is based on sound theoretical reasoning and is obtained by a combination of the energy-balance and mass-transfer approach. Penman's equation, incorporating some of the modifications suggested by other investigators is

$$\text{PET} = \frac{AH_n + E_a\gamma}{A + \gamma} \tag{3.13}$$

where   PET = daily potential evapotranspiration in mm per day
   A = slope of the saturation vapour pressure vs temperature curve at the mean air temperature, in mm of mercury per °C (Table 3.3)
   H_n = net radiation in mm of evaporable water per day
   E_a = parameter including wind velocity and saturation deficit
   γ = psychrometric constant = 0.49 mm of mercury/°C

The net radiation is the same as used in the energy budget [Eq. (3.8)] and is estimated by the following equation:

$$H_n = H_a (1 - r)\left(a + b\frac{n}{N}\right) - \sigma\, T_a^4 (0.56 - 0.092 \sqrt{e_a}\,)\left(0.10 + 0.90\frac{n}{N}\right) \tag{3.14}$$

where H_a = incident solar radiation outside the atmosphere on a horizontal surface, expressed in mm of evaporable water per day (it is a function of the latitude and period of the year as indicated in Table 3.4)
   a = a constant depending upon the latitude ϕ and is given by $a = 0.29 \cos \phi$
   b = a constant with an average value of 0.52
   n = actual duration of bright sunshine in hours
   N = maximum possible hours of bright sunshine (it is a function of latitude as indicated in Table 3.5)
   r = reflection coefficient (albedo). Usual ranges of values of r are given below.

Surface	Range of r values
Close ground corps	0.15–0.25
Bare lands	0.05–0.45
Water surface	0.05
Snow	0.45–0.95

σ = Stefan-Boltzman constant = 2.01×10^{-9} mm/day
T_a = mean air temperature in degrees kelvin = 273 + °C
e_a = actual mean vapour pressure in the air in mm of mercury

The parameter E_a is estimated as

$$E_a = 0.35\left(1 + \frac{u_2}{160}\right)(e_w - e_a) \tag{3.15}$$

in which
   u_2 = mean wind speed at 2 m above ground in km/day
   e_w = saturation vapour pressure at mean air temperature in mm of mercury (Table 3.3)
   e_a = actual vapour pressure, defined earlier

For the computation of PET, data on n, e_a, u_2, mean air temperature and nature of surface (i.e. value of r) are needed. These can be obtained from actual observations or through available meteorological data of the region. Equations (3.13), (3.14) and (3.15) together with Tables 3.3, 3.4, and 3.5 enable the daily PET to be calculated. It may be noted that Penman's equation can be used to calculate evaporation from a water surface by using $r = 0.05$. Penman's equation is widely used in India, the UK, Australia and in some parts of USA. Further details about this equation are available elsewhere[2,5,7].

EXAMPLE 3.2 *Calculate the potential evapotranspiration from an area near New Delhi in the month of November by Penman's fomula. The following data are available:*

Latitude	:	28°4′N
Elevation	:	230 m (above sea level)

Table 3.3 Saturation Vapour Pressure of Water

Temperature (°C)	Saturation vapour pressure e_w (mm of Hg)	A (mm/°C)
0	4.58	0.30
5.0	6.54	0.45
7.5	7.78	0.54
10.0	9.21	0.60
12.5	10.87	0.71
15.0	12.79	0.80
17.5	15.00	0.95
20.0	17.54	1.05
22.5	20.44	1.24
25.0	23.76	1.40
27.5	27.54	1.61
30.0	31.82	1.85
32.5	36.68	2.07
35.0	42.81	2.35
37.5	48.36	2.62
40.0	55.32	2.95
45.0	71.20	3.66

$e_w = 4.584 \exp\left(\dfrac{17.27t}{237.3+t}\right)$ mm of Hg, where t = temperature in °C.

Table 3.4 Mean Monthly Solar Radiation at Top of Atmosphere, H_a in mm of Evaporable Water/Day

North latitude	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
0°	14.5	15.0	15.2	14.7	13.9	13.4	13.5	14.2	14.9	15.0	14.6	14.3
10°	12.8	13.9	14.8	15.2	15.0	14.8	14.8	15.0	14.9	14.1	13.1	12.4
20°	10.8	12.3	13.9	15.2	15.7	15.8	15.7	15.3	14.4	12.9	11.2	10.3
30°	8.5	10.5	12.7	14.8	16.0	16.5	16.2	15.3	13.5	11.3	9.1	7.9
40°	6.0	8.3	11.0	13.9	15.9	16.7	16.3	14.8	12.2	9.3	6.7	5.4
50°	3.6	5.9	9.1	12.7	15.4	16.7	16.1	13.9	10.5	7.1	4.3	3.0

Table 3.5   Mean Monthly Values of Possible Sunshine Hours, N

North latitude	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
0°	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1
10°	11.6	11.8	12.1	12.4	12.6	12.7	12.6	12.4	12.9	11.9	11.7	11.5
20°	11.1	11.5	12.0	12.6	13.1	13.3	13.2	12.8	12.3	11.7	11.2	10.9
30°	10.4	11.1	12.0	12.9	13.7	14.1	13.9	13.2	12.4	11.5	10.6	10.2
40°	9.6	10.7	11.9	13.2	14.4	15.0	14.7	13.8	12.5	11.2	10.0	9.4
50°	8.6	10.1	11.8	13.8	15.4	16.4	16.0	14.5	12.7	10.8	9.1	8.1

Mean monthly temperature	:	*19° C*
Mean relative humidity	:	*75%*
Mean observed sunshine hours	:	*9 h*
Wind velocity at 2 m height	:	*85 km/day*
Nature of surface cover	:	*Close-ground green crop*

SOLUTION: From Table 3.3,

$$A = 1.00 \text{ mm/°C} \qquad e_w = 16.50 \text{ mm of Hg}$$

From Table 3.4

$$H_a = 9.506 \text{ mm of water/day}$$

From Table 3.5

$$N = 10.716 \text{ h} \qquad n/N = 9/10.716 = 0.84$$

From given data

$$e_a = 16.50 \times 0.75 = 12.38 \text{ mm of Hg}$$
$$a = 0.29 \cos 28° \, 4' = 0.2559$$
$$b = 0.52$$
$$\sigma = 2.01 \times 10^{-9} \text{ mm/day}$$
$$T_a = 273 + 19 = 292 \text{ K}$$
$$\sigma T_a^4 = 14.613$$
$$r = \text{albedo fer close-ground green crop is taken as } 0.25$$

From Eq. (3.14),

$$H_n = 9.506 \times (1 - 0.25) \times (0.2559 + (0.52 \times 0.84))$$
$$- 14.613 \times (0.56 - 0.092 \sqrt{12.38}\,) \times (0.10 + (0.9 \times 0.84))$$
$$= 4.936 - 2.946 = 1.990 \text{ mm of water/day}$$

From Eq. (3.15),

$$E_a = 0.35 \times \left(1 + \frac{85}{160}\right) \times (16.50 - 12.38) = 2.208 \text{ mm/day}$$

From Eq. (3.13), noting the value of $\gamma = 0.49$.

$$\text{PET} = \frac{(1 \times 1.990) + (2.208 \times 0.49)}{(1.00 + 0.49)} = 2.06 \text{ mm/day}$$

EXAMPLE 3.3   *Using the data of Example 3.2, estimate the daily evaporation from a lake situated in that place.*

SOLUTION: For estimating the daily evaporation from a lake, Penman's equation is used with the albedo $r = 0.05$.

Hence

$$H_n = 4.936 \times \frac{(1.0 - 0.05)}{(1.0 - 0.25)} - 2.946 = 6.252 - 2.946 = 3.306 \text{ mm of water/day}$$
$$E_a = 2.208 \text{ mm/day}$$

From Eq. (3.13),

$$PET = \text{Lake evaporation}$$
$$= \frac{(1.0 \times 3.306) + (2.208 \times 0.49)}{(1.0 - 0.49)} = 2.95 \text{ mm/day}$$

REFERENCE CROP EVAPOTRANSPIRATION (ET_O)   In irrigation practice, the PET is extensively used in calculation of crop-water requirements. For purposes of standardization, FAO recommends[3] a *reference crop evapotranspiration* or *reference evapotranspiration* denoted as ET_o. The reference surface is a hypothetical grass reference crop with an assumed crop height of 0.12 m, a defined fixed surface resistance of 70 s m^{-1} and an albedo of 0.23. The reference surface closely resembles an extensive surface of green, well-watered grass of uniform height, actively growing and completely shading the ground. The defined fixed surface resistance 70 s m^{-1} implies a moderately dry soil surface resulting from about a weekly irrigation frequency. The FAO recommends a method called *FAO Penman-Monteith method* to estimate ET_o by using radiation, air temperature, air humidity and wind speed data. Details of *FAO Penman-Monteith method* are available in Ref. 3.

The potential evapotranspiration of any other crop (ET) is calculated by multiplying the reference crop evapotranspiration by a coefficient K, the value of which changes with stage of the crop. Thus

$$ET = K(ET_o) \qquad (3.16)$$

The value of K varies from 0.5 to 1.3. Table 3.7 gives average values of K for some selected crops.

EMPIRICAL FORMULAE

A large number of empirical formulae are available for estimation of PET based on climatological data. These are not universally applicable to all climatic areas. They should be used with caution in areas different from those for which they were derived.

BLANEY-CRIDDLE FORMULA

This purely empirical formula based on data from arid western United States. This formula assumes that the PET is related to hours of sunshine and temperature, which are taken as measures of solar radiation at an area. The potential evapotranspiration in a crop-growing season is given by

$$E_T = 2.54 \ KF$$

and
$$F = \Sigma P_h \bar{T}_f / 100 \qquad (3.17)$$

where E_T = PET in a crop season in cm

   K = an empirical coefficient, depends on the type of the crop and stage of growth

   F = sum of monthly consumptive use factors for the period

   P_h = monthly percent of annual day-time hours, depends on the latitude of the place (Table 3.6)

and $\bar{T}_f$ = mean monthly temperature in °F

Values of K depend on the month and locality. Average value for the season for selected crops is given in Table 3.7. The Blaney-Criddle formula is largely used by irrigation engineers to calculate the water requirements of crops, which is taken as the difference between PET and effective precipitation. Blaney-Morin equation is another empirical formula similar to Eq. (3.17) but with an additional correction for humidity.

Table 3.6 Monthly Daytime Hours Percentages, P_h, for use in Blaney-Criddle Formula (Eq. 3.17)

North latitude (deg)	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
0	8.50	7.66	8.49	8.21	8.50	8.22	8.50	8.49	8.21	8.50	8.22	8.50
10	8.13	7.47	8.45	8.37	8.81	8.60	8.86	8.71	8.25	8.34	7.91	8.10
15	7.94	7.36	8.43	8.44	8.98	8.80	9.05	8.83	8.28	8.26	7.75	7.88
20	7.74	7.25	8.41	8.52	9.15	9.00	9.25	8.96	8.30	8.18	7.58	7.66
25	7.53	7.14	8.39	8.61	9.33	9.23	9.45	9.09	8.32	8.09	7.40	7.42
30	7.30	7.03	8.38	8.72	9.53	9.49	9.67	9.22	8.33	7.99	7.19	7.15
35	7.05	6.88	8.35	8.83	9.76	9.77	9.93	9.37	8.36	7.87	6.97	6.86
40	6.76	6.72	8.33	8.95	10.02	10.08	10.22	9.54	8.39	7.75	6.72	6.52

Table 3.7 Values of K for Selected Crops

Crop	Average value of K	Range of monthly values
Rice	1.10	0.85–1.30
Wheat	0.65	0.50–0.75
Maize	0.65	0.50–0.80
Sugarcane	0.90	0.75–1.00
Cotton	0.65	0.50–0.90
Potatoes	0.70	0.65–0.75
Natural Vegetation:		
(a) Very dense	1.30	
(b) Dense	1.20	
(c) Medium	1.00	
(d) Light	0.80	

EXAMPLE 3.4 *Estimate the PET of an area for the season November to February in which wheat is grown. The area is in North India at a latitude of 30° N with mean monthly temperatures as below:*

Month	Nov.	Dec.	Jan.	Feb.
Temp. (°C)	16.5	13.0	11.0	14.5

Use the Blaney-Criddle formula.

SOLUTION: From Table 3.7, for wheat $K = 0.65$. Values of P_h for 30° N is read from Table 3.6, the temperatures are converted to Fahrenheit and the calculations are performed in the following table.

Month	$\bar{T}_f$	P_h	$P_h\bar{T}_f/100$
Nov.	61.7	7.19	4.44
Dec.	55.4	7.15	3.96
Jan.	51.8	7.30	3.78
Feb.	58.1	7.03	4.08
		$\Sigma P_h \bar{T}_f /100 =$	16.26

By Eq. (3.17),

$$E_T = 2.54 \times 16.26 \times 0.65 = 26.85 \text{ cm.}$$

THORNTHWAITE FORMULA This formula was developed from data of eastern USA and uses only the mean monthly temperature together with an adjustment for day-lengths. The PET is given by this formula as

$$E_T = 1.6 \, L_a \left(\frac{10 \, \overline{T}}{I_t} \right)^a \qquad (3.18)$$

where E_T = monthly PET in cm

L_a = adjustment for the number of hours of daylight and days in the month, related to the latitude of the place (Table 3.8)

$\overline{T}$ = mean monthly air temperature °C

I_t = the total of 12 monthly values of heat index = $\sum\limits_{1}^{12} i$, where $i = (\overline{T}/5)^{1.514}$

a = an empirical constant

$= 6.75 \times 10^{-7} I_t^3 - 7.71 \times 10^{-5} I_t^2 + 1.792 \times 10^{-2} I_t + 0.49239$

Table 3.8 Adjustment Factor L_a for Use in Thornthwaite Formula (Eq. 3.18)

North latitude (deg)	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
0	1.04	0.94	1.04	1.01	1.04	1.01	1.04	1.04	1.01	1.04	1.01	1.04
10	1.00	0.91	1.03	1.03	1.08	1.06	1.08	1.07	1.02	1.02	0.98	0.99
15	0.97	0.91	1.03	1.04	1.11	1.08	1.12	1.08	1.02	1.01	0.95	0.97
20	0.95	0.90	1.03	1.05	1.13	1.11	1.14	1.11	1.02	1.00	0.93	0.94
25	0.93	0.89	1.03	1.06	1.15	1.14	1.17	1.12	1.02	0.99	0.91	0.91
30	0.90	0.87	1.03	1.08	1.18	1.17	1.20	1.14	1.03	0.98	0.89	0.88
40	0.84	0.83	1.03	1.11	1.24	1.25	1.27	1.18	1.04	0.96	0.83	0.81

3.11 POTENTIAL EVAPOTRANSPIRATION OVER INDIA

Using Penman's equation and the available climatological data, PET estimate[5] for the country has been made. The mean annual PET (in cm) over various parts of the country is shown in the form of *isopleths*—the lines on a map through places having equal depths of evapotranspiration [Fig. 3.6(a)]. It is seen that the annual PET ranges from 140 to 180 cm over most parts of the country. The annual PET is highest at Rajkot, Gujarat with a value of 214.5 cm. Extreme south-east of Tamil Nadu also show high average values greater than 180 cm. The highest PET for southern peninsula is at Tiruchirapalli, Tamil Nadu with a value of 209 cm. The variation of monthly PET at some stations located in different climatic zones in the country is shown in Fig. 3.6(b). Valuable PET data relevant to various parts of the country are available in Refs 4 and 7.

3.12 ACTUAL EVAPOTRANSPIRATION (AET)

AET for hydrological and irrigation applications can be obtained through a process water budgeting and accounting for soil-plant-atmosphere interactions. A simple procedure due to *Doorenbos* and *Pruit* is as follows:
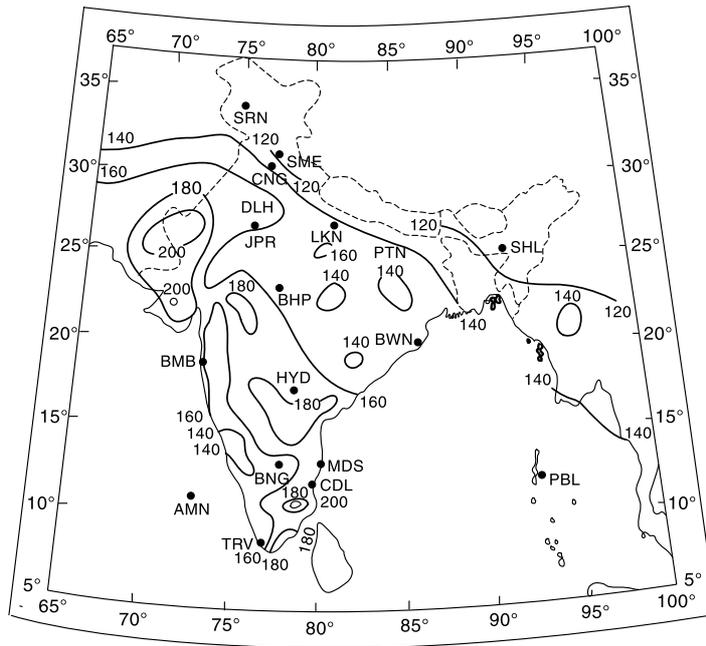
Fig. 3.6(a)   Annual PET (cm) over India
(*Source: Scientific: Report No.* 136, IMD, 1971, © Government of India Copyright)

Based upon survey of India map with the permission of the Surveyor General of India, © Government of India Copyright 1984

The territorial waters of India extend into the sea to a distance of 200 nautical miles measured from the appropriate baseline

Responsibility for the correctness of internal details on the map rests with the publisher.
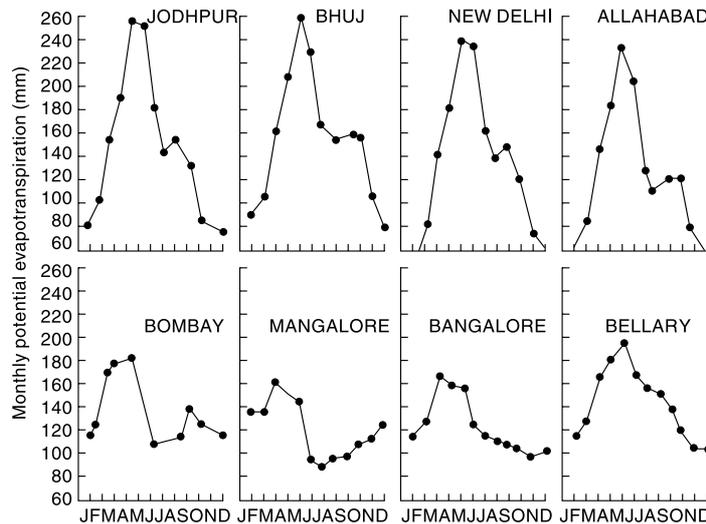
Fig. 3.6(b)   Monthly Variation of PET (mm)
(*Source: Scientific Report No.* 136, India Meteorological Department, 1971, © Government of India Copyright)

1. Using available meteorological data the reference crop evapotranspiration (ET_o) is calculated.
2. The crop coefficient K for the given crop (and stage of growth) is obtained from published tables such as Table 3.7. The potential crop evapotrans-piration ET_c is calculated using Eq. 3.16 as $ET_c = K(ET_o)$.
3. The actual evapotranspiration (ET_a) at any time t at the farm having the given crop is calculated as below:
   - If $AASW \geq (1 - p) \, MASW$
     $$ET_a = ET_o \qquad \text{(known as } potential \ condition) \qquad \text{(3.19-a)}$$
   - If $AASW < (1 - p) \, MASW$
     $$ET_a = \left[\frac{AASW}{(1 - p) \, MASW} \right] ET_c \qquad \text{(3.19-b)}$$

where $MASW$ = total available soil water over the root depth
          $AASW$ = actual available soil-water at time t over the root depth
             p = soil-water depletion factor for a given crop and soil complex. (Values of p ranges from about 0.1 for sandy soils to about 0.5 for clayey soils)

[Note the equivalence of terms used earlier as $PET = ET_o$ and $AET = ET_a$]

EXAMPLE 3.5 *A recently irrigated field plot has on Day 1 the total available soil moisture at its maximum value of 10 cm. If the reference crop evapotranspiration is 5.0 mm/day, calculate the actual evapotranspiration on Day 1, Day 6 and Day 7. Assume soil-water depletion factor p = 0.20 and crop factor K = 0.8.*

SOLUTION: *Here* ET_o = 5.0 mm and $MASW$ = 100 mm
             $(1 - p) \, MASW = (1 - 0.2) \times 100 = 80.0$ and $ET_c = 0.9 \times 5.0 = 4.5$ mm/day
Day 1: $AASW$ = 100 mm > $(1 - p) \, MASW$
             Hence potential condition exists and $ET_a = ET_c = 4.5$ mm/day
This rate will continue till a depletion of $(100 - 80) = 20$ mm takes place in the soil. This will take $20/4.5 = 4.44$ days. Thus **Day 5** also will have $ET_a = ET_c = 4.5$ mm/day
Day 6:   At the beginning of Day 6, $AASW = (100 - 4.5 \times 5) = 77.5$ mm
             Since $AASW < (1 - p) \, MASW$,
             $$ET_a = \left[\frac{77.5}{80.0} \right] \times 4.5 = 4.36 \text{ mm}$$
Day 7:   At the beginning of Day 7, $AASW = (77.5 - 4.36) = 73.14$ mm
             Since $AASW < (1 - p) \, MASW$
             $$ET_a = \left[\frac{73.14}{80.0} \right] \times 4.5 = 4.11 \text{ mm.}$$
             $AASW$ at the end of Day 7 = $73.14 - 4.11 = 69.03$ mm.

C: INITIAL LOSS

In the precipitation reaching the surface of a catchment the major abstraction is from the infiltration process. However, two other processes, though small in magnitude, operate to reduce the water volume available for runoff and thus act as abstractions. These are (i) the *interception process*, and (ii) the *depression storage* and together they are called the *initial loss*. This abstraction represents the quantity of storage that must be satisfied before overland runoff begins. The following two sections deal with these two processes briefly.

3.13   INTERCEPTION

When it rains over a catchment, not all the precipitation falls directly onto the ground. Before it reaches the ground, a part of it may be caught by the vegetation and subsequently evaporated. The volume of water so caught is called *interception*. The intercepted precipitation may follow one of the three possible routes:

1. It may be retained by the vegetation as surface storage and returned to the atmosphere by evaporation; a process termed *interception loss;*
2. It can drip off the plant leaves to join the ground surface or the surface flow; this is known as *throughfall*; and
3. The rainwater may run along the leaves and branches and down the stem to reach the ground surface. This part is called *stemflow.*

    Interception loss is solely due to evaporation and does not include transpiration, throughfall or stemflow.

    The amount of water intercepted in a given area is extremely difficult to measure. It depends on the species composition of vegetation, its density and also on the storm characteristics. It is estimated that of the total rainfall in an area during a plant-growing season the interception loss is about 10 to 20%. Interception is satisfied during the first part of a storm and if an area

Fig. 3.7   Typical Interception Loss Curve

experiences a large number of small storms, the annual interception loss due to forests in such cases will be high, amounting to greater than 25% of the annual precipitation. Quantitatively, the variation of interception loss with the rainfall magnitude per storm for small storms is as shown in Fig. 3.7. It is seen that the interception loss is large for a small rainfall and levels off to a constant value for larger storms. For a given storm, the interception loss is estimated as

$$I_i = S_i + K_i Et \tag{3.18}$$

where I_i = interception loss in mm, S_i = interception storage whose value varies from 0.25 to 1.25 mm depending on the nature of vegetation, K_i = ratio of vegetal surface area to its projected area, E = evaporation rate in mm/h during the precipitation and t = duration of rainfall in hours.

    It is found that coniferous trees have more interception loss than deciduous ones. Also, dense grasses have nearly same interception losses as full-grown trees and can account for nearly 20% of the total rainfall in the season. Agricultural crops in their growing season also contribute high interception losses. In view of these the interception process has a very significant impact on the ecology of the area related to silvicultural aspects, in *in situ* water harvesting and in the water balance of a region. However, in hydrological studies dealing with floods interception loss is rarely significant and is not separately considered. The common practice is to allow a lump sum value as the initial loss to be deducted from the initial period of the storm.

3.14   DEPRESSION STORAGE

When the precipitation of a storm reaches the ground, it must first fill up all depressions

before it can flow over the surface. The volume of water trapped in these depressions is called *depression storage.* This amount is eventually lost to runoff through processes of infiltration and evaporation and thus form a part of the initial loss. Depression storage depends on a vast number of factors the chief of which are: (i) the type of soil, (ii) the condition of the surface reflecting the amount and nature of depression, (iii) the slope of the catchment, and (iv) the antecedent precipitation, as a measure of the soil moisture. Obviously, general expressions for quantitative estimation of this loss are not available. Qualitatively, it has been found that antecedent precipitation has a very pronounced effect on decreasing the loss to runoff in a storm due to depression. Values of 0.50 cm in sand, 0.4 cm in loam and 0.25 cm in clay can be taken as representatives for depression-storage loss during intensive storms.

<center>D: INFILTRATION</center>

3.15 INFILTRATION

Infiltration is the flow of water into the ground through the soil surface. The distribution of soil moisture within the soil profile during the infiltration process is illustrated in Fig. 3.8. When water is applied at the surface of a soil, four moisture zones in the soil, as indicated in Fig. 3.8 can be identified.

Zone 1: At the top, a thin layer of *saturated zone* is created.

Zone 2: Beneath zone 1, there is a *transition zone*.

Zone 3: Next lower zone is the *trans-mission zone* where the downward motion of the moisture takes place. The moisture content in this zone is above field capacity but below saturation. Further, it is characterized by unsaturated flow and fairly uniform moisture content.

Fig. 3.8   Distribution of Soil Moisture in the Infiltration Process

Zone 4: The last zone is the *wetting zone*. The soil moisture in this zone will be at or near field capacity and the moisture content decreases with the depth. The boundary of the wetting zone is the wetting front where a sharp discontinuity exists between the newly wet soil and original moisture content of the soil. Depending upon the amount of infiltration and physical properties of the soil, the wetting front can extend from a few centimetres to metres.

The infiltration process can be easily understood through a simple analogy. Consider a small container covered with wire gauze as in Fig. 3.9. If water is

Fig. 3.9   An Analogy for Infiltration

poured into the container a part of it will go into the container and a part overflows. Further, the container can hold only a fixed quantity and when it is full no more flow into the container can take place. While this analogy is highly simplified, it underscores two important aspects; viz. (i) the maximum rate at which the ground can absorb water, the *infiltration capacity* and (ii) the volume of water that the ground can hold, the *field capacity.* Since the infiltered water may contribute to the ground water discharge in addition to increasing the soil moisture, the process can be schematically modelled as in Fig. 3.10(a) and (b) wherein two situations, viz. low intensity rainfall and high intensity rainfall are considered.
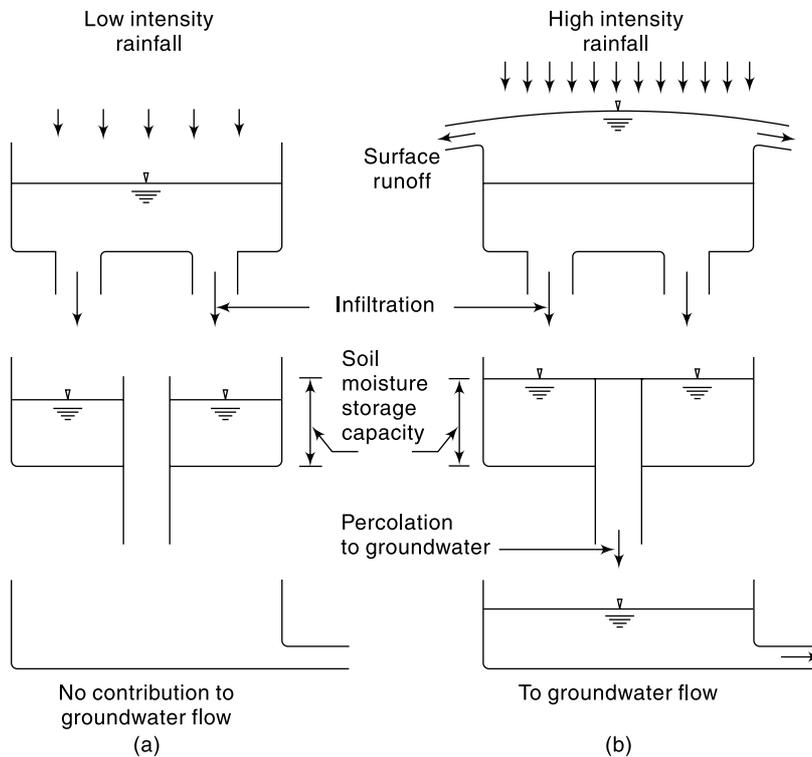
Fig. 3.10   An Infiltration Model

3.16   INFILTRATION CAPACITY

The maximum rate at which a given soil at a given time can absorb water is defined as the *infiltration capacity.* It is designated as f_p and is expressed in units of cm/h. The actual rate of infiltration f can be expressed as

$$f = f_p \text{ when } i \geq f_p$$

and $$f = i \text{ when } i < f_p \tag{3.20}$$

where i = intensity of rainfall. The infiltration capacity of a soil is high at the beginning of a storm and has an exponential decay as the time elapses.

The typical variation of the infiltration capacity f_p of a soil with time is shown in Fig. 3.11. The infiltration capacity of an area is dependent on a large number of factors, chief of them are:

- Characteristics of the soil (Texture, porosity and hydraulic conductivity)
- Condition of the soil surface   • Current moisture content
- Vegetative cover and   • Soil temperature

A few important factors affecting f_p are described below:

CHARACTERISTICS OF SOIL   The type of soil, viz. sand, silt or clay, its texture, structure, permeability and underdrainage are the important characteristics under this category. A loose, permeable, sandy soil will have a larger infiltration capacity than a tight, clayey soil. A soil with good underdrainage, i.e. the facility to transmit the infiltered water downward to a groundwater storage would obviously have a higher infiltration capacity. When the soils occur in layers, the transmission capacity of the layers determines the overall infiltration rate. Also, a dry soil can absorb more water than one whose pores are already

Fig. 3.11   Variation of Infiltration Capacity

full (Fig. 3.11). The land use has a significant influence on f_p. For example, a forest soil rich in organic matter will have a much higher value of f_p under identical conditions than the same soil in an urban area where it is subjected to compaction.

SURFACE OF ENTRY   At the soil surface, the impact of raindrops causes the fines in the soil to be displaced and these in turn can clog the pore spaces in the upper layers of the soil. This is an important factor affecting the infiltration capacity. Thus a surface covered with grass and other vegetation which can reduce this process has a pronounced influence on the value of f_p.

FLUID CHARACTERISTICS   Water infiltrating into the soil will have many impurities, both in solution and in suspension. The turbidity of the water, especially the clay and colloid content is an important factor and such suspended particles block the fine pores in the soil and reduce its infiltration capacity. The temperature of the water is a factor in the sense that it affects the viscosity of the water by which in turn affects the infiltration rate. Contamination of the water by dissolved salts can affect the soil structure and in turn affect the infiltration rate.

3.17   MEASUREMENT OF INFILTRATION

Infiltration characteristics of a soil at a given location can be estimated by
- Using flooding type infiltrometers
- Measurement of subsidence of free water in a large basin or pond
- Rainfall simulator
- Hydrograph analysis

FLOODING-TYPE INFILTROMETER

Flooding-type infiltrometers are experimental devices used to obtain data relating to variation of infiltration capacity with time. Two types of flooding type infiltrometers are in common use. They are (a) Tube-type (or Simple) infiltrometer and (b) Double-ring infiltrometer.

SIMPLE (TUBE TYPE) INFILTROMETER This is a simple instrument consisting essentially of a metal cylinder, 30 cm diameter and 60 cm long, open at both ends. The cylinder is driven into the ground to a depth of 50 cm (Fig. 3.12(a)). Water is poured into the top part to a depth of 5 cm and a pointer is set to mark the water level. As infiltration proceeds, the volume is made up by adding water from a burette to keep the water level at the tip of the pointer. Knowing the volume of water added during different time intervals, the plot of the infiltration capacity *vs* time is obtained. The experiments are continued till a uniform rate of infiltration is obtained and this may take 2–3 hours. The surface of the soil is usually protected by a perforated disc to prevent formation of turbidity and its settling on the soil surface.

(a) Simple (tube-type) infiltrometer   (b) Double-ring infiltrometer
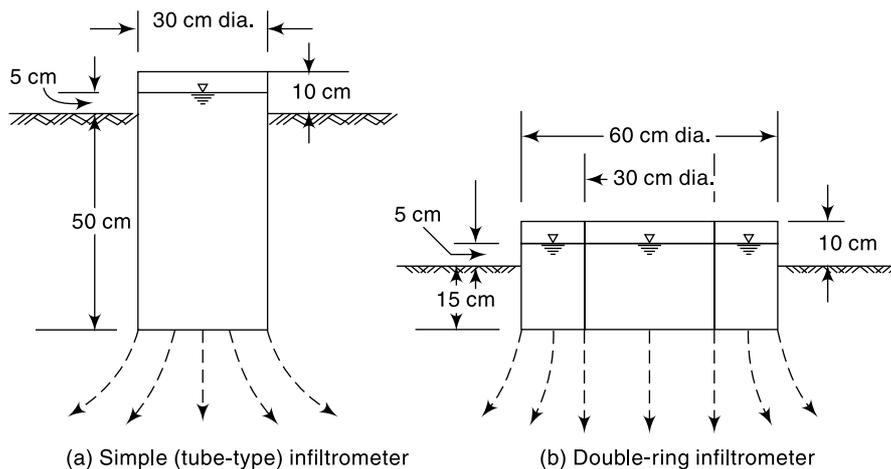
Fig. 3.12 Flooding Type Infiltrometers

A major objection to the simple infiltrometer as above is that the infiltered water spreads at the outlet from the tube (as shown by dotted lines in Fig. 3.12(a)) and as such the tube area is not representative of the area in which infiltration is taking place.

DOUBLE-RING INFILTROMETER This most commonly used infiltrometer is designed to overcome the basic objection of the tube infiltrometer, viz. the tube area is not representative of the infiltrating area. In this, two sets of concentrating rings with diameters of 30 cm and 60 cm and of a minimum length of 25 cm, as shown in Fig. 3.12(b), are used. The two rings are inserted into the ground and water is applied into both the rings to maintain a constant depth of about 5.0 cm. The outer ring provides water jacket to the infiltering water from the inner ring and hence prevents the spreading out of the infiltering water of the inner ring. The water depths in the inner and outer rings are kept the same during the observation period. The measurement of

the water volume is done on the inner ring only. The experiment is carried out till a constant infiltration rate is obtained. A perforated disc to prevent formation of turbidity and settling of fines on the soil surface is provided on the surface of the soil in the inner ring as well as in the annular space.

As the flooding-type infiltrometer measures the infiltration characteristics at a spot only, a large number of pre-planned experiments are necessary to obtain representative infiltration characteristics for an entire watershed. Some of the chief disadvantages of flooding-type infiltrometers are:

1. the raindrop impact effect is not simulated;
2. the driving of the tube or rings disturbs the soil structure; and
3. the results of the infiltrometers depend to some extent on their size with the larger meters giving less rates than the smaller ones; this is due to the border effect.

RAINFALL SIMULATOR

In this a small plot of land, of about 2 m × 4 m size, is provided with a series of nozzles on the longer side with arrangements to collect and measure the surface runoff rate. The specially designed nozzles produce raindrops falling from a height of 2 m and are capable of producing various intensities of rainfall. Experiments are conducted under controlled conditions with various combinations of intensities and durations and the surface runoff rates and volumes are measured in each case. Using the water budget equation involving the volume of rainfall, infiltration and runoff, the infiltration rate and its variation with time are estimated. If the rainfall intensity is higher than the infiltration rate, infiltration capacity values are obtained.

Rainfall simulator type infiltrometers give lower values than flooding type infiltrometers. This is due to effect of the rainfall impact and turbidity of the surface water present in the former.

HYDROGRAPH ANALYSIS

Reasonable estimation of the infiltration capacity of a small watershed can be obtained by analyzing measured runoff hydrographs and corresponding rainfall records. If sufficiently good rainfall records and runoff hydrographs corresponding to isolated storms in a small watershed with fairly homogeneous soils are available, water budget equation can be applied to estimate the abstraction by infiltration. In this the evapotranspiration losses are estimated by knowing the land cover/use of the watershed.

3.18 MODELING INFILTRATION CAPACITY

Figure 3.13 shows a typical variation of infiltration capacity f_p with time.
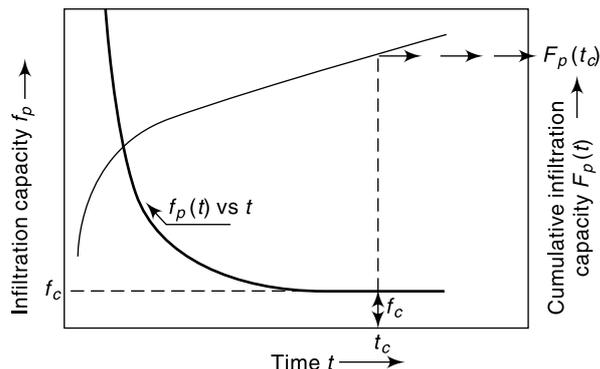
Fig. 3.13 Curves of Infiltration Capacity and Cumulative Infiltration Capacity

Cumulative infiltration capacity $F_p(t)$ is defined as the accumulation of infiltration volume over a time period since the start of the process and is given by

$$F_p = \int_0^t f_p(t)\, dt \qquad\qquad (3.21\text{-a})$$

Thus the curve $F_p(t)$ vs time in Fig. (3.13) is the mass curve of infiltration. It may be noted that from Eq. (3.21-a) it follow that

$$f_p(t) = \frac{dF_p(t)}{dt} \qquad\qquad (3.21\text{-b})$$

Many equations have been proposed to express the curves $f_p(t)$ or $F_p(t)$ for use in hydrological analysis. In this section four such equations will be described.

[**Note:** Practically all the infiltration equations relate infiltration capacity $f_p(t)$ or cumulative infiltration capacity $F_p(t)$ with time and other parameters. As such many authors find it convenient to drop the suffix p while denoting capacity. Thus f_p is denoted as f and F_p as F.]

HORTON'S EQUATION (1933) Horton expressed the decay of infiltration capacity with time as an exponential decay given by

$$f_p = f_c + (f_0 - f_c)\, e^{-K_h t} \qquad \text{for } 0 \geq t \leq t_c \qquad\qquad (3.22)$$

where f_p = infiltration capacity at any time t from the start of the rainfall
        f_0 = initial infiltration capacity at $t = 0$
        f_c = final steady state infiltration capacity occurring at $t = t_c$. Also, f_c is sometimes known as *constant rate* or *ultimate infiltration capacity.*
       K_h = Horton's decay coefficient which depends upon soil characteristics and vegetation cover.

The difficulty of determining the variation of the three parameters f_0, f_c and k_h with soil characteristics and antecedent moisture conditions preclude the general use of Eq. (3.22).

PHILIP'S EQUATION (1957) Philip's two term model relates $F_p(t)$ as

$$F_p = s t^{1/2} + Kt \qquad\qquad (3.23)$$

where s = a function of soil suction potential and called as *sorptivity*
      K = Darcy's hydraulic conductivity

By Eq. (3.21-b) infiltration capacity could be expressed as

$$f_p = \frac{1}{2} s t^{-1/2} + K \qquad\qquad (3.24)$$

KOSTIAKOV EQUATION (1932) Kostiakov model expresses cumulative infiltration capacity as

$$F_p = a t^b \qquad\qquad (3.25)$$

where a and b are local parameters with $a > 0$ and $0 < b < 1$.

The infiltration capacity would now b e expressed by Eq. (3.21-b) as

$$f_p = (ab)\, t^{(b-1)} \qquad\qquad (3.26)$$

GREEN−AMPT EQUATION (1911) Green and Ampt proposed a model for infiltration capacity based on Darcy's law as

$$f_p = K\left(1 + \frac{\eta S_c}{F_p}\right) \qquad\qquad (3.27)$$

where η = porosity of the soil
S_c = capillary suction at the wetting front and
K = Darcy's hydraulic conductivity.
Eq. (3.27) could be considered as

$$f_p = m + \frac{n}{F_p} \tag{3.28}$$

where m and n are Green–Ampt parameters of infiltration model.

ESTIMATION OF PARAMETERS OF INFILTRATION MODELS

Data from infiltrometer experiments can be processed to generate data sets f_p and F_p values for various time t values. The following procedures are convenient to evaluate the parameters of the infiltration models.

HORTON'S MODEL   Value of f_c in a test is obtained from inspection of the data. Equation (3.22) is rearranged to read as

$$(f_p - f_c) = (f_0 - f_c)\, e^{-K_h t} \tag{3.22-a}$$

Taking logarithms $\ln(f_p - f_c) = \ln(f_o - f_c) - K_h t$
Plot $\ln(f_p - f_c)$ against t and fit the best straight line through the plotted points. The intercept gives $\ln(f_0 - f_c)$ and the slope of the straight line is K_h.

PHILIP'S MODEL   Use the expression for f_p as

$$f_p = \frac{1}{2}\, s t^{-1/2} + K \tag{3.24}$$

Plot the observed values of f_p against $t^{-0.5}$ on an arithmetic graph paper. The best fitting straight line through the plotted points gives K as the intercept and $(s/2)$ as the slope of the line. While fitting Philip's model it is necessary to note that K is positive and to achieve this it may be necessary to neglect a few data points at the initial stages (viz. at small values of t) of the infiltration experiment. K will be of the order of magnitude of the asymptotic value of f_p.

KOSTIAKOV MODEL   Kostiakov model relates F_p to t as

$$F_p = a t^b \tag{3.25}$$

Taking logarithms of both sides of Eq. (3.25),

$$\ln(F_p) = \ln a + b \ln(t)$$

The data is plotted as $\ln(F_p)$ *vs* $\ln(t)$ on an arithmetic graph paper and the best fit straight through the plotted points gives $\ln a$ as intercept and the slope is b. Note that b is a positive quantity such that $0 < b < 1$.

GREEN–AMPT MODEL   Green–Ampt equation is considered in the form $f_p = m + \frac{n}{F_p}$. Values of f_p are plotted against $(1/F_p)$ on a simple arithmetic graph paper and the best fit straight line is drawn through the plotted points. The intercept and the slope of the line are the coefficients m and n respectively. Sometimes values of f_p and corresponding F_p at very low values of t may have to be omitted to get best fitting straight line with reasonably good correlation coefficient.

[**Note:** 1. Procedure for calculation of the best fit straight line relating the dependent variable Y and independent variable X by the least-square error method is described in Section 4.9, Chapter 4.

2. Use of spread sheets (for eg., MS Excel) greatly simplifies these procedures and the best values of parameters can be obtained by fitting regression equations. Further, various plots and the coefficient of correlation, etc. can be calculated with ease.]

EXAMPLE 3.6 *Infiltration capacity data obtained in a flooding type infiltration test is given below:*

Time since start (minutes)	5	10	15	25	45	60	75	90	110	130
Cumulative infiltration depth (cm)	1.75	3.00	3.95	5.50	7.25	8.30	9.30	10.20	11.28	12.36

(a) For this data plot the curves of (i) infiltration capacity vs time, (ii) infiltration capacity vs cumulative infiltration, and (iii) cumulative infiltration vs time.

(b) Obtain the best values of the parameters in Horton's infiltration capacity equation to represent this data set.

SOLUTION: Incremental infiltration values and corresponding infiltration intensities f_p at various data observation times are calculated as shown in the following Table. Also other data required for various plots are calculated as shown in Table 3.9.

Table 3.9 Calculations for Example 3.6

Time in Minutes	Cum. Depth (cm)	Incremental Depth in the interval (cm)	Infiltration rate, f_p(cm/h)	$Ln(f_p - f_c)$	Time in hours
0					
5	1.75	1.75	21.00	2.877	0.083
10	3.00	1.25	15.00	2.465	0.167
15	3.95	0.95	11.40	2.099	0.250
25	5.50	1.55	9.30	1.802	0.417
45.	7.25	1.75	5.25	0.698	0.750
60	8.30	1.05	4.20	−0.041	1.000
75	9.30	1.00	4.00	−0.274	1.250
90	10.20	0.90	3.60	−1.022	1.500
110	11.28	1.08	3.24		1.833
130	12.36	1.08	3.24		2.167

(a) Plots of f_p vs time and F_p vs time are shown in Fig. 3.14. Best fitting curve for plotted points are also shown in the Fig. 3.14-a.

Plot of f_p vs F_p is shown in Fig. 3.14-b.

(b) By observation from Table 3.9, $f_c = 3.24$ cm/h

$Ln(f_p - f_c)$ is plotted against time t as shown in Fig. 3.14-c. The best fit line through the plotted points is drawn and its equation is obtained as
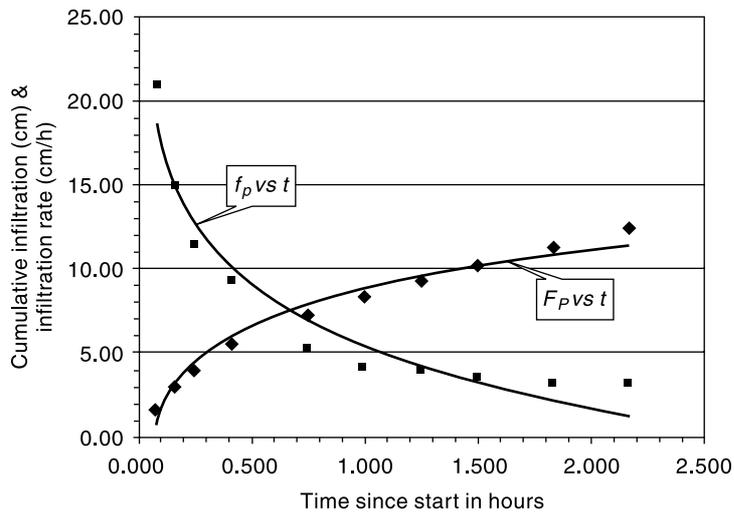
Fig. 3.14 (a)   Plot of F_p vs Time and f_p vs Time
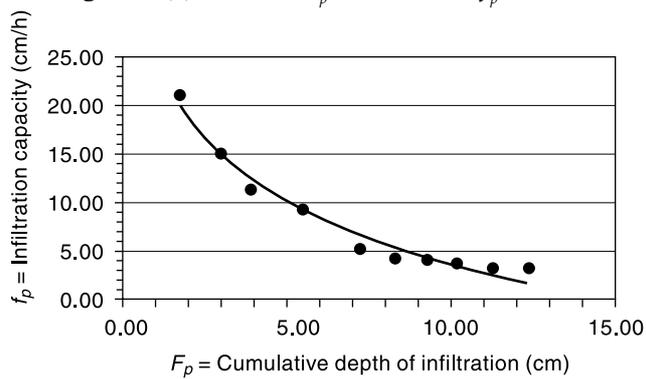
Fig. 3.14 (b)   Plot of f_p vs F_p
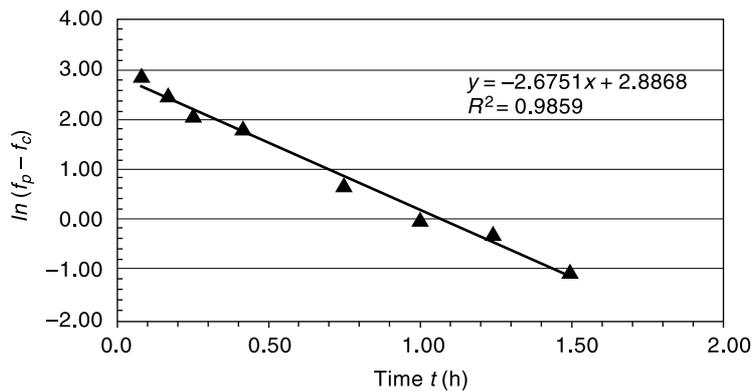
Fig. 3.14 (c)   Horton's Equation. Plot of $\ln(f_p - f_c)$ vs Time

$\ln(f_p - f_c) = 2.8868 - 2.6751\ t$
$-K_h$ = slope of the best fit line = -2.6751, thus $K_h = 2.6751$ h^{-1}
$\ln(f_0 - f_c)$ = intercept = 2.8868, thus $f_0 - f_c = 17.94$ and $f_0 = 21.18$ cm/h

EXAMPLE 3.7   *Values of infiltration capacities at various times obtained from an infiltration test are given below. Determine the parameters of (i) Green–Ampt equation, (ii) Philip's equation, and (iii) Kostiakov's equation that best fits this data.*

Time since start (minutes)	5	10	15	20	25	30	60	90	120	150
Cumulative infiltration depth (cm)	1.0	1.8	2.5	3.1	3.6	4.0	6.1	8.1	9.9	11.6

SOLUTION: Incremental infiltration depth values and corresponding infiltration intensities f_p at various data observation times are calculated as shown in Table 3.10. Also, various parameters needed for plotting different infiltration models are calculated as shown in Table 3.10. The units used are f_p in cm/h, F_p in cm and t in hours.

Table 3.10   Calculations Relating to Example 3.7

1	2	3	4	5	6	7	8	9
Time (min)	F_p (cm)	Incremental depth of infiltration (cm)	f_p (cm/h)	t in hours	$t^{-0.5}$	$1/F_p$	Ln F_p	Ln t
5	1.0	1.0	12.0	0.083	3.464	1.000	0.000	−2.485
10	1.8	0.8	9.6	0.167	2.449	0.556	0.588	−1.792
15	2.5	0.7	8.4	0.250	2.000	0.400	0.916	−1.386
20	3.1	0.6	7.2	0.333	1.732	0.323	1.131	−1.099
25	3.6	0.5	6.0	0.417	1.549	0.278	1.281	−0.875
30	4.0	0.4	4.8	0.500	1.414	0.250	1.386	−0.693
60	6.1	2.1	4.2	1.000	1.000	0.164	1.808	0.000
90	8.1	2.0	4.0	1.500	0.816	0.123	2.092	0.405
120	9.9	1.8	3.6	2.000	0.707	0.101	2.293	0.693
150	11.6	1.7	3.4	2.500	0.632	0.086	2.451	0.916

Green–Ampt Equation: $f_p = m + \dfrac{n}{F_p}$ (3.28)

Values of f_p (col. 4) are plotted against $1/F_p$ (col. 7) on an arithmetic graph paper (Fig. 3.15-a). The best fit straight line through the plotted points is obtained as

$f_p = 10.042 \left(\dfrac{1}{F_p} \right)$
  + 3.0256.
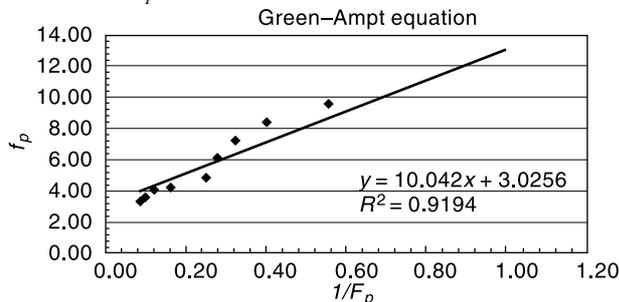
Fig. 3.15 (a)   Fitting of Green–Ampt Equation

(Graph labeled "Green–Ampt equation", y-axis f_p from 0.00 to 14.00, x-axis $1/F_p$ from 0.00 to 1.20, with fitted line $y = 10.042x + 3.0256$, $R^2 = 0.9194$)

The coefficients of the Green–Ampt equations are $m = 3.0256$ and $n = 10.042$

Philip's Equation: The expression $f_p(t) = \dfrac{1}{2} st^{-1/2} + K$ (Eq. 3.24) is used. Values of f_p (Col. 4) are plotted against $t^{-0.5}$ (col. 6) on an arithmetic graph paper (Fig. 15-b). The best fit straight line through the plotted points is obtained as

$f_p = 3.2287\ t^{-0.5} + 1.23$

The coefficients of Philip's equation are $s = 2 \times 3.2287 = 6.4574$ and $K = 1.23$

Fig. 3.15 (b) Fitting of Philip's Equation

Kostiakov's Equation:
$F_p(t) = at^b$

Eq. (3.25)

Taking logarithms of both sides of the equation (3.25)

$\ln(F_p) = \ln a + b \ln(t).$

The data set is plotted as $\ln(F_p)$ *vs* $\ln(t)$ on an arithmetic graph paper (Fig. 3.15-c) and the best fit straight line through the plotted points is obtained as
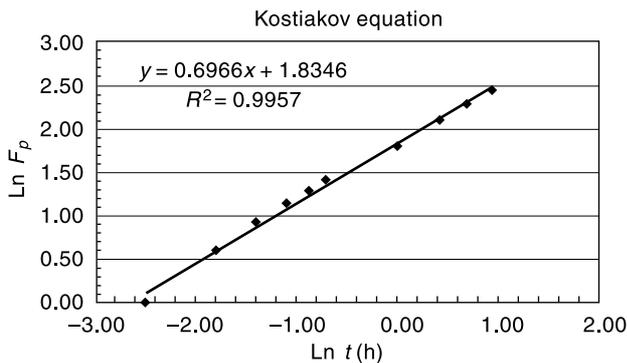
Fig. 3.15 (c) Fitting of Kostiakov Equation

$\ln(F_p) = 1.8346 + 0.6966\ \text{in}(t).$

The coefficients of Kostiakov equation are $b = 0.6966$ and $\ln a = 1.8346$ and hence $a = 6.2626$. Best fitting Kostiakov equation for the data is

$F_p = 6.2626\ t^{0.6966}$

EXAMPLE 3.8 *The infiltration capacity in a basin is represented by Horton's equation as*

$$f_p = 3.0 + e^{-2t}$$

where f_p is in cm/h and t is in hours. Assuming the infiltration to take place at capacity rates in a storm of 60 minutes duration, estimate the depth of infiltration in (i) the first 30 minutes and (ii) the second 30 minutes of the storm.

SOLUTION:

$$F_p = \int_0^t f_p\, dt \quad \text{and} \quad f_p = 3.0 + e^{-2t}$$

(i) In the first 0.5 hour

$$F_{p1} = \int_0^{0.5} (3.0 + e^{-2t})\, dt = \left[3.0t - \frac{1}{2}e^{-2t} \right]_0^{0.5}$$

$$= [(3.0 \times 0.5) - (1/2)(e^{-(2 \times 0.5)}] - [-(1/2)] = (1.5 - 0.184) + 0.5$$

$$= 1.816 \text{ cm}$$

(ii) In the second 0.5 hour

$$F_{p2} = \int_{0.50}^{1.0} (3.0 + e^{-2t})\, dt = \left[3.0t - \frac{1}{2}e^{-2t} \right]_{0.5}^{1.0}$$

$$= [(3.0 \times 1.0) - (1/2)(e^{-2})] - [(3.0 \times 0.5) - (1/2)(e^{-(2 \times 0.5)})]$$

$$= (3.0 - 0.0677) - (1.5 - 0.184) = 1.616 \text{ cm}$$

EXAMPLE 3.9 *The infiltration capacity of soil in a small watershed was found to be 6 cm/h before a rainfall event. It was found to be 1.2 cm/h at the end of 8 hours of storm. If the total infiltration during the 8 hours period of storm was 15 cm, estimate the value of the decay coefficient K_h in Horton's infiltration capacity equation.*

SOLUTION: Horton's equation is $\quad f_p = f_c + (f_0 - f_c)\, e^{-K_h t}$

and $\qquad\qquad F_p = \int_0^t f_p(t)\, dt = f_c t + (f_0 - f_c)\int_0^t e^{-K_h t}\, dt$

As $t \to \infty$, $\int_0^\infty e^{-K_h t}\, dt \to \dfrac{1}{K_h}$. Hence for large t values

$$F_p = f_c t + \frac{(f_0 - f_c)}{K_h}$$

Here F_p = 15.0 cm, f_0 = 6.0 cm, f_c = 1.2 cm and t = 8 hours.

$$15.0 = (1.2 \times 8) + (6.0 - 1.2)/K_h$$

$$K_h = 4.8/5.4 = 0.888 \text{ h}^{-1}$$

3.19 CLASSIFICATION OF INFILTRATION CAPACITIES

For purposes of runoff volume classification in small watersheds, one of the widely used methods is the *SCS–CN* method described in detail in Chapter 5. In this method, the soils are considered divided into four groups known as hydrologic soil groups. The steady state infiltration capacity, being one of the main parameters in this soil classification, is divided into four infiltration classes as mentioned below.

Table 3.11 Classification of Infiltration Capacities

Infiltration Class	Infiltration Capacity (mm/h)	Remarks
Very Low	< 2.5	Highly clayey soils
Low	2.5 to 25.0	Shallow soils, Clay soils, Soils low in organic matter
Medium	12.5 to 25.0	Sandy loam, Silt
High	>25.0	Deep sands, well drained aggregated soils

3.20 INFILTRATION INDICES

In hydrological calculations involving floods it is found convenient to use a constant value of infiltration rate for the duration of the storm. The defined average infiltration rate is called *infiltration index* and two types of indices are in common use.

φ-INDEX

The φ-index is the average rainfall above which the rainfall volume is equal to the runoff volume. The φ-index is derived from the rainfall hyetograph with the knowledge of the resulting runoff volume. The initial loss is also considered as infiltration. The φ value is found by treating it as a constant infiltration capacity. If the rainfall intensity is less than φ, then the infiltration rate is equal to the rain-fall intensity; however, if the rainfall

Fig. 3.16 φ-Index

intensity is larger than φ the difference between the rainfall and infiltration in an inter-val of time represents the runoff volume as shown in Fig. 3.16. The amount of rainfall in excess of the index is called *rainfall excess.* In connection with runoff and flood studies it is also known as *effective rainfall*, (details in Sec. 6.5, Chapter 6). The φ-index thus accounts for the total abstraction and enables magnitudes to be estimated for a given rainfall hyetograph. A detailed procedure for calculating φ-index for a given storm hyetograph and resulting runoff volume is as follows.
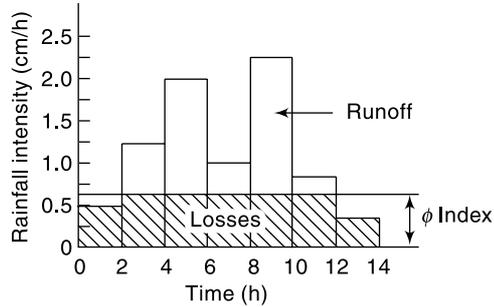
PROCEDURE FOR CALCULATION OF φ-INDEX   Consider a rainfall hyetograph of event duration D hours and having N pulses of time interval Δt such that

$$N \cdot \Delta t = D. \qquad \text{(In Fig. 3.16, } N = 7)$$

Let I_i be the intensity of rainfall in ith pulse and R_d = total direct runoff.

$$\text{Total Rainfall } P = \sum_{1}^{N} I_i \cdot \Delta t$$

If φ is φ-index,   then $P - \varphi \cdot t_e = R_d$
where t_e = duration of rainfall excess.

   If the rainfall hyetograph and total runoff depth R_d are given, the φ-index of the storm can be determined by trial and error procedure as given below.

1. Assume that out of given N pulses, M number of pulses have rainfall excess. (Note that $M \le N$). Select M number of pulses in decreasing order of rainfall intensity I_i.
2. Find the value of φ that satisfies the relation

$$R_d = \sum_{1}^{M} (I_i - \varphi) \Delta t$$

3. Using the value of φ of Step 2, find the number of pulses (M_c) which give rain-fall excess. (Thus M_c = number of pulses with rainfall intensity $I_i \ge \varphi$).
4. If $M_c = M$, then φ of Step 2 is the correct value of φ-index. If not, repeat the procedure Step 1 onwards with new value of M. Result of Step 3 can be used as guidance to the next trial.

Example 3.10 illustrates this procedure in detail.

EXAMPLE 3.10 *A storm with 10 cm of precipitation produced a direct runoff of 5.8 cm. The duration of the rainfall was 16 hours and its time distribution is given below. Estimate the φ-index of the storm.*

Time from start (h)	0	2	4	6	8	10	12	14	16
Cumulative rainfall (cm)	0	0.4	1.3	2.8	5.1	6.9	8.5	9.5	10.0

SOLUTION: Pulses of uniform time duration $\Delta t = 2$ h are considered. The pulses are numbered sequentially and intensity of rainfall in each pulse is calculated as shown below.

Table 3.12 Calculations for Example 3.10

Pulse number	**1**	**2**	**3**	**4**	**5**	**6**	**7**	**8**
Time from start of rain (h)	2	4	6	8	10	12	14	16
Cumulative rainfall (cm)	0.4	1.3	2.8	5.1	6.9	8.5	9.5	10.0
Incremental rain (cm)	0.40	0.90	1.50	2.30	1.80	1.60	1.00	0.50
Intensity of rain (I_i) in cm/h.	0.20	0.45	0.75	1.15	0.90	0.80	0.50	0.25

Here duration of rainfall $D = 16$ h, $\Delta t = 2$ h and $N = 8$.

Trial 1:

Assume $M = 8$, $\Delta t = 2$ h and hence $t_e = M \cdot \Delta t = 16$ hours.
Since $M = N$, all the pulses are included.

$$\text{Runoff } R_d = 5.8 \text{ cm} = \sum_1^8 (I_i - \varphi)\Delta t = \sum_1^8 I_i \times \Delta t - \varphi (8 \times 2)$$

$$5.8 = \{(0.20 \times 2) + (0.45 \times 2) + (0.75 \times 2) + (1.15 \times 2) + (0.90 \times 2) + (0.80 \times 2)$$
$$+ (0.50 \times 2) + (0.25 \times 2)\} - 16 \, \varphi = 10.0 - 14 \, \varphi$$
$$\varphi = 4.2/14 = 0.263 \text{ cm/h}$$
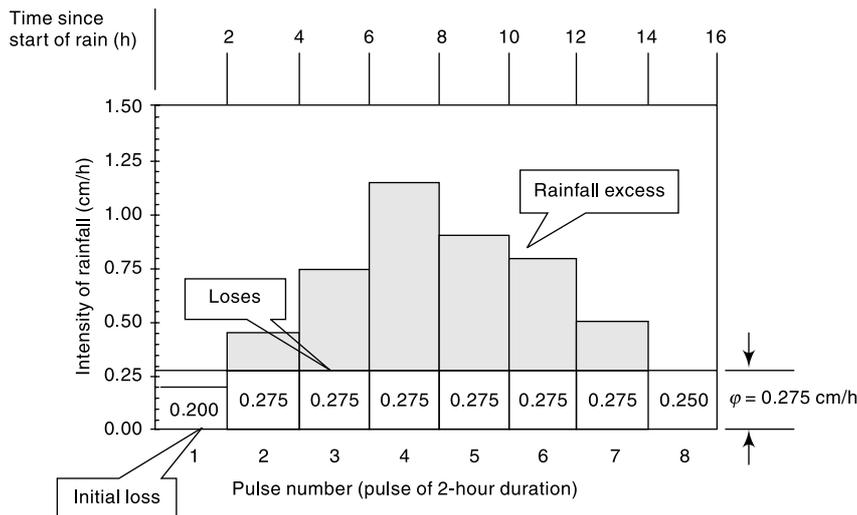
Fig. 3.17 Hyetograph and Rainfall Excess of the Storm – Example 3.10

By inspection of row 5 of Table 3.12, M_c = number of pulses having $I_i \geq \varphi$, that is $I_i \geq 0.263$ cm/h is 6.

Thus $M_c = 6 \neq M$. Hence assumed M is **not** correct. Try a new value of $M < 8$ in the next trial.

Trial 2:

Assume $M = 7$, $\Delta t = 2$ h and hence $t_e = M \cdot \Delta t = 14$ hours.

Select these 7 pulses in decreasing order of I_i. Pulse 1 is omitted.

Runoff $R_d = 5.8$ cm $= \sum_1^7 (I_i - \varphi) \, \Delta t = \sum_1^7 (I_i \cdot \Delta t - \varphi \,(7 \times 2)$

$$5.8 = \{(0.45 \times 2) + (0.75 \times 2) + (1.15 \times 2) + (0.90 \times 2)$$
$$+ (0.80 \times 2) + (0.50 \times 2) + (0.25 \times 2)\} - 14 \; \varphi = 9.6 - 14 \; \varphi$$
$$\varphi = 3.8/14 = 0.271 \text{ cm/h}$$

By inspection of row 5 of Table 3.12, M_c = number of pulses having $I_i \geq \varphi$, that is $I_i \geq 0.271$ cm/h is 6.

Thus $M_c = 6 \neq M$. Hence assumed M is **not** O.K. Try a new value of $M < 7$ in the next trial.

Trial 3:

Assume $M = 6 \cdot \Delta t = 2$ h and hence $t_e = M \cdot \Delta t = 12$ hours.

Select these 6 pulses in decreasing order of I_i. Pulse 1 and 8 are omitted.

Runoff $R_d = 5.8$ cm $= a$

$$5.8 = \{(0.45 \times 2) + (0.75 \times 2) + (1.15 \times 2) + (0.90 \times 2) + (0.80 \times 2)$$
$$+ (0.50 \times 2)\} - 12 \; \varphi = 9.1 - 12 \; \varphi$$
$$\varphi = 3.3/12 = 0.275 \text{ cm/h}$$

By inspection of row 5 of Table 3. 12, M_c = number of pulses having $I_i \geq \varphi$, that is $I_i \geq 0.275$ cm/h is 6.

Thus $M_c = 6 = M$. Hence assumed M is OK.

The φ-index of the storm is 0.275 cm/h and the duration of rainfall excess $= t_e = 12$ hours. The hyetograph of the storm, losses, the rainfall excess and the duration of rainfall excess are shown in Fig. 3.17.

W-INDEX

In an attempt to refine the φ-index the initial losses are separated from the total abstractions and an average value of infiltration rate, called W-index, is defined as

$$W = \frac{P - R - I_a}{t_e} \qquad (3.29)$$

where
P = total storm precipitation (cm)

R = total storm runoff (cm)

I_a = Initial losses (cm)

t_e = duration of the rainfall excess, i.e. the total time in which the rainfall intensity is greater than W (in hours) and

W = defined average rate of infiltration (cm).

Since I_a rates are difficult to obtain, the accurate estimation of W-index is rather difficult.

The minimum value of the W-index obtained under very wet soil conditions, representing the constant minimum rate of infiltration of the catchment, is known as W_{min}. It is to be noted that both the φ-index and W-index vary from storm to storm.

COMPUTATION OF W-INDEX To compute W-index from a given storm hyetograph with known values of I_a and runoff R, the following procedure is followed:

(i) Deduct the initial loss I_a from the storm hyetograph pulses starting from the first pulse

(ii) Use the resulting hyetograph pulse diagram and follow the procedure indicated in Sec. 3.19.1.

Thus the procedure is exactly same as in the determination of φ-index except for the fact that the storm hyetograph is appropriately modified by deducting I_a.

φ-INDEX FOR PRACTICAL USE   The φ-index for a catchment, during a storm, depends in general upon the soil type, vegetal cover, initial moisture condition, storm duration and intensity. To obtain complete information on the interrelationship between these factors, a detailed expensive study of the catchment is necessary. As such, for practical use in the estimation of flood magnitudes due to critical storms a simplified relationship for φ-index is adopted. As the maximum flood peaks are invariably produced due to long storms and usually in the wet season, the initial losses are assumed to be negligibly small. Further, only the soil type and rainfall are found to be critical in the estimate of the φ-index for maximum flood producing storms.

On the basis of rainfall and runoff correlations, CWC[1] has found the following relationships for the estimation of φ-index for flood producing storms and soil conditions prevalent in India

$$R = \alpha I^{1.2} \tag{3.30}$$

$$\varphi = \frac{I - R}{24} \tag{3.31}$$

where R = runoff in cm from a 24-h rainfall of intensity I cm/h and α = a coefficient which depends upon the soil type as indicated in Table 3.13. In estimating the maximum floods for design purposes, in the absence of any other data, a φ-index value of 0.10 cm/h can be assumed.

Table 3.13   Variation of Coefficient α in Eq. 3.30

Sl. No.	Type of Soil	Coefficient α
1.	Sandy soils and sandy loam	0.17 to 0.25
2.	Coastal alluvium and silty loam	0.25 to 0.34
3.	Red soils, clayey loam, grey and brown alluvium	0.42
4.	Black–cotton and clayey soils	0.42 to 0.46
5.	Hilly soils	0.46 to 0.50

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---| REVISION QUESTIONS |---

3.1 Discuss briefly the various abstractions from precipitation.

3.2 Explain briefly the evaporation process.

3.3 Discuss the factors that affect the evaporation from a water body.

3.4 Describe a commonly used evaporimeter.

3.5 Explain the energy budget method of estimating evaporation from a lake.

3.6 Discuss the importance of evaporation control of reservoirs and possible methods of achieving the same.

3.7 Describe the factors affecting evapotranspiration process.

3.8 List the various data needed to use Penman's equation for estimating the potential evapotranspiration from a given area.

3.9 Describe briefly (a) Reference crop evapotranspiration and (b) Actual evapotrans-piration.

3.10 Explain briefly the infiltration process and the resulting soil moisture zones in the soil.

3.11 Discuss the factors affecting the infiltration capacity of an area.

3.12 Describe the commonly used procedures for determining the infiltration characteristics of a plot of land. Explain clearly the relative advantages and disadvantages of the enumerated methods.

3.13 Describe various models adopted to represent the variation of infiltration capacity with time.

3.14 Explain a procedure for fitting Horton's infiltration equation for experimental data from a given plot.

3.15 Distinguish between
  (a) Infiltration capacity and infiltration rate (b) Actual and potential evapotranspiration
  (c) Field capacity and permanent wilting point (d) Depression storage and interception

---| PROBLEMS |---

3.1 Calculate the evaporation rate from an open water source, if the net radiation is 300 W/m^2 and the air temperature is 30° C. Assume value of zero for sensible heat, ground heat flux, heat stored in water body and advected energy. The density of water at 30° C = 996 kg/m^3.
[**Hint:** Calculate latent heat of vapourisation L by the formula:
$L = 2501 – 2.37\ T$ (kJ/kg), where T = temperature in °C.]

3.2 A class A pan was set up adjacent to a lake. The depth of water in the pan at the beginning of a certain week was 195 mm. In that week there was a rainfall of 45 mm and 15 mm of water was removed from the pan to keep the water level within the specified depth range. If the depth of the water in the pan at the end of the week was 190 mm calculate the pan evaporation. Using a suitable pan coefficient estimate the lake evaporation in that week.

3.3 A reservoir has an average area of 50 km^2 over an year. The normal annual rainfall at the place is 120 cm and the class A pan evaporation is 240 cm. Assuming the land flooded by the reservoir has a runoff coefficient of 0.4, estimate the net annual increase or decrease in the streamflow as a result of the reservoir.

3.4 At a reservoir in the neighbourhood of Delhi the following climatic data were observed. Estimate the mean monthly and annual evaporation from the reservoir using Meyer's formula.

Month	Temp. (°C)	Relative humidity (%)	Wind velocity at 2 m above GL (km/h)
Jan	12.5	85	4.0
Feb	15.8	82	5.0
Mar	20.7	71	5.0

<div align="right">(<i>Contd.</i>)</div>

(*Contd.*)

Apr	27.0	48	5.0
May	31.0	41	7.8
Jun	33.5	52	10.0
Jul	30.6	78	8.0
Aug	29.0	86	5.5
Sep	28.2	82	5.0
Oct	28.8	75	4.0
Nov	18.9	77	3.6
Dec	13.7	73	4.0

3.5 For the lake in Prob. 3.4, estimate the evaporation in the month of June by (a) Penman formula and (b) Thornthwaite equation by assuming that the lake evaporation is the same as PET, given latitude = 28° N and elevation = 230 m above MSL. Mean observed sunshine = 9 h/day.

3.6 A reservoir had an average surface area of 20 km^2 during June 1982. In that month the mean rate of inflow = 10 m^3/s, outflow = 15 m^3/s, monthly rainfall = 10 cm and change in storage = 16 million m^3. Assuming the seepage losses to be 1.8 cm, estimate the evaporation in that month.

3.7 For an area in South India (latitude = 12° N), the mean monthly temperatures are given.

Month	June	July	Aug	Sep	Oct
Temp (°C)	31.5	31.0	30.0	29.0	28.0

Calculate the seasonal consumptive use of water for the rice crop in the season June 16 to October 15, by using the Blaney–Criddle formula.

3.8 A catchment area near Mysore is at latitude 12° 18′ N and at an elevation of 770 m. The mean monthly temperatures are given below.

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
Mean monthly temp. (°C)	22.5	24.5	27.0	28.0	27.0	25.0	23.5	24.0	24.0	24.5	23.0	22.5

Calculate the monthly and annual PET for this catchment using the Thornthwaite formula.

3.9 A wheat field has maximum available moisture of 12 cm. If the reference evapotranspiration is 6.0 mm/day, estimate the actual evapotranspiration on Day 2, Day 7 and Day 9 after irrigation. Assume soil-water depletion factor $p = 0.20$ and crop factor $K = 0.65$.

3.10 Results of an infiltrometer test on a soil are given below. Determine the Horton's infiltration capacity equation for this soil.

Time since start in (h)	0.25	0.50	0.75	1.00	1.25	1.50	1.75	2.0
Infiltration capacity in cm/h	5.6	3.20	2.10	1.50	1.20	1.10	1.0	1.0

3.11 Results of an infiltrometer test on a soil are given below. Determine the best values of the parameters of Horton's infiltration capacity equation for this soil.

Time since start in minutes	5	10	15	20	30	40	60	80	100
Cumulative infiltration in mm	21.5	37.7	52.2	65.8	78.4	89.5	101.8	112.6	123.3

3.12 Results of an infiltrometer test on a soil are as follows:

Time since start in minutes	5	10	15	20	30	40	60	120	150
Cumulative infiltration in mm	1.00	1.80	2.50	3.10	4.20	5.10	6.60	11.00	12.90

Determine the parameters of (i) Kostiakov's equation, (ii) Green–Ampt equation, and (iii) Philips equation

3.13 Determine the best values of the parameters of Horton's infiltration capacity equation for the following data pertaining to infiltration tests on a soil using double ring infiltrometer.

Time since start in minutes	5	10	15	25	40	60	75	90	110	130
Cumulative infiltration in mm	21.0	36.0	47.6	56.9	63.8	69.8	74.8	79.3	87.0	92.0

3.14 For the infiltration data set given below, establish (a) Kostiakov's equation, (b) Philips equation, and (c) Green–Ampt equation.

Time since start in minutes	10	20	30	50	80	120	160	200	280	360
Cumulative Infiltration in mm	9.8	18.0	25.0	38.0	55.0	76.0	94.0	110.0	137.0	163.0

3.15 Following table gives the values of a field study of infiltration using flooding type infiltrometer. (a) For this data plot the curves of (i) infiltration capacity f_p (mm/h) vs time (h) on a log–log paper and obtain the equation of the best fit line, and (ii) Cumulative infiltration (mm) F_p vs time (h) on a semi-log paper and obtain the equation of the best fit line. (b) Establish Horton's infiltration capacity equation for this soil.

Time since start in minutes	2	10	30	60	90	120	240	360
Cumulative Infiltration in cm	7.0	20.0	33.5	37.8	39.5	41.0	43.0	45.0

3.16 The infiltration capacity of a catchment is represented by Horton's equation as

$$f_p = 0.5 + 1.2e^{-0.5t}$$

where f_p is in cm/h and t is in hours. Assuming the infiltration to take place at capacity rates in a storm of 4 hours duration, estimate the average rate of infiltration for the duration of the storm.

3.17 The infiltration process at capacity rates in a soil is described by Kostiakov's equation as $F_p = 3.0\, t^{0.7}$ where F_p is cumulative infiltration in cm and t is time in hours. Estimate the infiltration capacity at (i) 2.0 h and (ii) 3.0 h from the start of infiltration.

3.18 The mass curve of an isolated storm in a 500 ha watershed is as follows:

Time from start (h)	0	2	4	6	8	10	12	14	16	18
Cumulative rainfall (cm)	0	0.8	2.6	2.8	4.1	7.3	10.8	11.8	12.4	12.6

If the direct runoff produced by the storm is measured at the outlet of the watershed as 0.340 Mm^3, estimate the φ-index of the storm and duration of rainfall excess.

3.19 The mass curve of an isolated storm over a watershed is given below.

Time from start (h)	0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0
Cummulative rainfall (cm)	0	0.25	0.50	1.10	1.60	2.60	3.50	5.70	6.50	7.30	7.70

If the storm produced a direct runoff of 3.5 cm at the outlet of the watershed, estimate the φ-index of the storm and duration of rainfall excess.

3.20 In a 140-min storm the following rates of rainfall were observed in successive 20-min intervals: 6.0, 6.0, 18.0, 13.0, 2.0, 2.0 and 12.0 mm/h. Assuming the φ-index value as 3.0 mm/h and an initial loss of 0.8 mm, determine the total rainfall, net runoff and W-index for the storm.

3.21 The mass curve of rainfall of duration 100 min is given below. If the catchment had an initial loss of 0.6 cm and a φ-index of 0.6 cm/h, calculate the total surface runoff from the catchment.

Time from start of rainfall (min)	0	20	40	60	80	100
Cummulative rainfall (cm)	0	0.5	1.2	2.6	3.3	3.5

3.22 An isolated 3-h storm occurred over a basin in the following fashion:

% of catchment area	φ–index (cm/h)	Rainfall (cm)		
		1st hour	2nd hour	3rd hour
20	1.00	0.8	2.3	1.5
30	0.75	0.7	2.1	1.0
50	0.50	1.0	2.5	0.8

Estimate the runoff from the catchment due to the storm.

OBJECTIVE QUESTIONS

3.1 If e_w and e_a are the saturated vapour pressures of the water surface and air respectively, the Dalton's law for evaporation E_L in unit time is given by $E_L =$
    (a) $(e_w - e_a)$ (b) $K e_w e_a$ (c) $K(e_w - e_a)$ (d) $K(e_w + e_a)$

3.2 The average pan coefficient for the standard US Weather Bureau class A pan is
    (a) 0.85   (b) 0.70   (c) 0.90   (d) 0.20

3.3 A canal is 80 km long and has an average surface width of 15 m. If the evaporation measured in a class A pan is 0.5 cm/day, the volume of water evaporated in a month of 30 days is (in m^3)
    (a) 12600   (b) 18000   (c) 180000   (d) 126000

3.4 The ISI standard pan evaporimeter is the
    (a) same as the US class A pan
    (b) has an average pan coefficient value of 0.60

    (c) has less evaporation than a US class A pan

    (d) has more evaporation than a US class A pan.

3.5 The chemical that is found to be most suitable as water evaporation inhibitor is

    (a) ethyl alcohol   (b) methyl alcohol

    (c) cetyl alcohol   (d) butyl alcohol.

3.6 Wind speed is measured with

    (a) a wind vane   (b) a heliometer

    (c) Stevenson box   (d) anemometer

3.7 If the wind velocity at a height of 2 m above ground is 5.0 kmph, its value at a height of 9 m above ground can be expected to be in km/h about

    (a) 9.0   (b) 6.2   (c) 2.3   (d) 10.6

3.8 Evapotranspiration is confined

    (a) to daylight hours   (b) night-time only

    (c) land surfaces only   (d) none of these.

3.9 Lysimeter is used to measure

    (a) infiltration   (b) evaporation   (c) evapotranspiration   (d) vapour pressure.

3.10 The highest value of annual evapotranspiration in India is at Rajkot, Gujarat. Here the annual PET is about

    (a) 150 cm   (b) 150 mm   (c) 210 cm   (d) 310 cm.

3.11 Interception losses

    (a) include evaporation, through flow and stemflow

    (b) consists of only evaporation loss

    (c) includes evaporation and transpiration losses

    (d) consists of only stemflow.

3.12 The infiltration capacity of a soil was measured under fairly identical general conditions by a flooding type infiltrometer as f_f and by a rainfall simulator as f_r. One can expect

    (a) $f_f = f_r$ (b) $f_f > f_r$ (c) $f_f < f_r$ (d) no fixed pattern.

3.13 A watershed 600 ha in area experienced a rainfall of uniform intensity 2.0 cm/h for duration of 8 hours. If the resulting surface runoff is measured as 0.6 Mm^3, the average infiltration capacity during the storm is

    (a) 1.5 cm/h   (b) 0.75 cm/h   (c) 1.0 cm/h   (d) 2.0 cm/h

3.14 In a small catchment the infiltration rate was observed to be 10 cm/h at the beginning of the rain and it decreased exponentially to an equilibrium value of 1.0 cm/h at the end of 9 hours of rain. If a total of 18 cm of water infiltered during 9 hours interval, the value of the decay constant K_h in Horton's infiltration equation in (h^{-1}) units is

    (a) 0.1   (b) 0.5   (c) 1.0   (d) 2.0

3.15 In Horton's infiltration equation fitted to data from a soil, the initial infiltration capacity is 10 mm/h, final infiltration capacity is 5 mm/h and the exponential decay constant is 0.5 h^{-1}. Assuming the infiltration takes place at capacity rates, the total infiltration depth for a uniform storm of duration 8 hours is

    (a) 40 mm   (b) 60 mm   (c) 80 mm   (d) 90 mm

3.16 The rainfall on five successive days on a catchment was 2, 6, 9, 5 and 3 cm. If the φ-index for the storm can be assumed to be 3 cm/day, the total direct runoff from the catchment is

    (a) 20 cm   (b) 11 cm   (c) 10 cm   (d) 22 cm

3.17 A 6-h storm had 6 cm of rainfall and the resulting runoff was 3.0 cm. If the φ-index remains at the same value the runoff due to 12 cm of rainfall in 9 h in the catchment is

    (a) 9.0 cm   (b) 4.5 cm   (c) 6.0 cm   (d) 7.5 cm

3.18 For a basin, in a given period Δt, there is no change in the groundwater and soil water status. If P = precipitation, R = total runoff, E = Evapotranspiration and ΔS = increase in the surface water storage in the basin, the hydrological water budget equation states

    (a) $P = R - E \pm \Delta S$ (b) $R = P + E - \Delta S$ (c) $P = R + E + \Delta S$ (d) None of these

Chapter
4

STREAMFLOW
MEASUREMENT

4.1 INTRODUCTION

Streamflow representing the runoff phase of the hydrologic cycle is the most important basic data for hydrologic studies. It was seen in the previous chapters that precipitation, evaporation and evapotranspiration are all difficult to measure exactly and the presently adopted methods have severe limitations. In contrast the measurement of streamflow is amenable to fairly accurate assessment. Interestingly, streamflow is the only part of the hydrologic cycle that can be measured accurately.

A stream can be defined as a flow channel into which the surface runoff from a specified basin drains. Generally, there is considerable exchange of water between a stream and the underground water. Streamflow is measured in units of discharge (m^3/s) occurring at a specified time and constitutes historical data. The measurement of discharge in a stream forms an important branch of *Hydrometry*, the science and practice of water measurement. This chapter deals with only the salient streamflow measurement techniques to provide an appreciation of this important aspect of engineering hydrology. Excellent treatises[1, 2, 4, 5] and a bibliography[6] are available on the theory and practice of streamflow measurement and these are recommended for further details.

Streamflow measurement techniques can be broadly classified into two cate-gories as (i) direct determination and (ii) indirect determination. Under each category there are a host of methods, the important ones are listed below:
1. Direct determination of stream discharge:
    (a) Area-velocity methods,   (b) Dilution techniques,
    (c) Electromagnetic method, and   (d) Ultrasonic method.
2. Indirect determination of streamflow:
    (a) Hydraulic structures, such as weirs, flumes and gated structures, and
    (b) Slope-area method.

Barring a few exceptional cases, continuous measurement of stream discharge is very difficult. As a rule, direct measurement of discharge is a very time-consuming and costly procedure. Hence, a two step procedure is followed. First, the discharge in a given stream is related to the elevation of the water surface (Stage) through a series of careful measurements. In the next step the stage of the stream is observed routinely in a relatively inexpensive manner and the discharge is estimated by using the previously determined stage–discharge relationship. The observation of the stage is easy, inexpensive, and if desired, continuous readings can also be obtained. This method of discharge determination of streams is adopted universally.

4.2 MEASUREMENT OF STAGE

The stage of a river is defined as its water-surface elevation measured above a datum. This datum can be the mean-sea level (MSL) or any arbitrary datum connected independently to the MSL.

MANUAL GAUGES

STAFF GAUGE The simplest of stage measurements are made by noting the elevation of the water surface in contact with a fixed graduated staff. The staff is made of a durable material with a low coefficient of expansion with respect to both temperature and moisture. It is fixed rigidly to a structure, such as an abutment, pier, wall, etc. The staff may be vertical or inclined with clearly and accurately graduated permanent markings. The markings are distinctive, easy to read from a distance and are similar to those on a surveying staff. Sometimes, it may not be possible to read the entire range of water-surface elevations of a stream by a single gauge and in such cases the gauge is built in sections at different locations. Such gauges are called *sectional gauges* (Fig. 4.1). When installing sectional gauges, care must be taken to provide an overlap between various gauges and to refer all the sections to the same common datum.

(a) Vertical staff gauge   (b) Sectional staff gauge
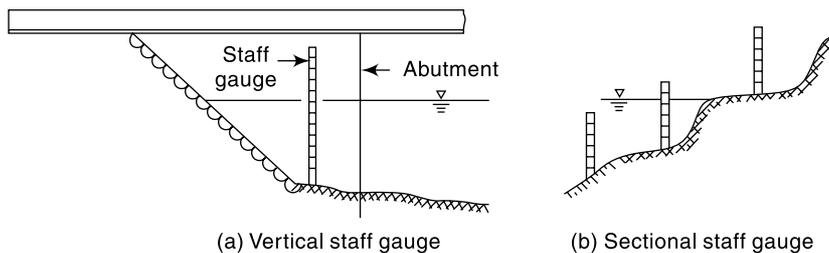
Fig. 4.1   Staff Gauge

WIRE GAUGE It is a gauge used to measure the water-surface elevation from above the surface such as from a bridge or similar structure. In this a weight is lowered by a reel to touch the water surface. A mechanical counter measures the rotation of the wheel which is proportional to the length of the wire paid out. The operating range of this kind of gauge is about 25 m.

AUTOMATIC STAGE RECORDERS

The staff gauge and wire gauge described earlier are manual gauges. While they are simple and inexpensive, they have to be read at frequent intervals to define the variation of stage with time accurately. Automatic stage recorders overcome this basic objection of manual staff gauges and find considerable use in stream-flow measurement practice. Two typical automatic stage recorders are described below.

FLOAT-GAUGE RECORDER The Float-operated stage recorder is the most common type of automatic stage recorder in use. In this, a float operating in a stilling well is balanced by means of a counterweight over the pulley of a recorder. Displacement of the float due to the rising or lowering of the water-surface elevation causes an angular displacement of the pulley and hence of the input shaft of the recorder.

Mechanical linkages convert this angular displacement to the linear displacement of a pen to record over a drum driven by clockwork. The pen traverse is continuous with automatic reversing when it reaches the full width of the chart. A clockwork mechanism runs the recorder for a day, week or fortnight and provides a continuous plot of stage *vs* time. A good instrument will have a large-size float and least fric-

Fig. 4.2 Stilling well Installation

tion. Improvements over this basic analogue model consists of models that give digital signals recorded on a storage device or transmit directly onto a central data-processing centre.

To protect the float from debris and to reduce the water surface wave effects on the recording, *stilling wells* are provided in all float-type stage recorder installations. Figure 4.2 shows a typical stilling well installation. Note the intake pipes that communicate with the river and flushing arrangement to flush these intake pipes off the sediment and debris occasionally. The water-stage recorder has to be located above the highest water level expected in the stream to prevent it from getting inundated during floods. Further, the instrument must be properly housed in a suitable enclosure to protect it from weather elements and vandalism. On account of these, the water-stage-recorder installations prove to be costly in most instances. A water-depth recorder is shown in Fig. 4.3.
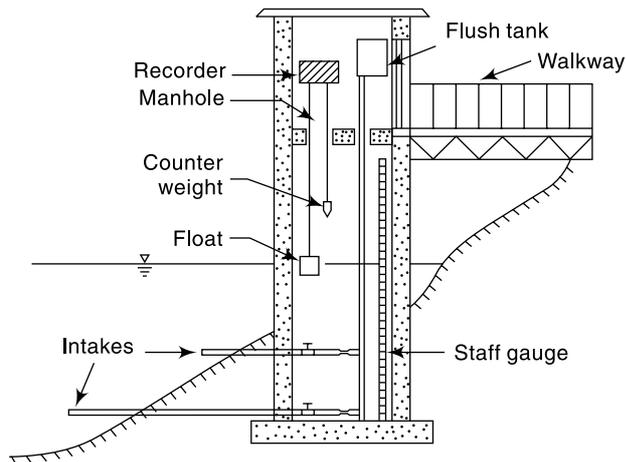
Fig. 4.3 Water-depth recorder— Stevens Type F recorder (*Courtesy*: Leupold and Stevens, Inc. Beaverton, Oregon, USA)

BUBBLE GAUGE   In this gauge compressed air or gas is made to bleed out at a very small rate through an outlet placed at the bottom of the river [Figs. 4.4, 4.5 and 4.6]. A pressure gauge measures the gas pressure which in turn is equal to the water column above the outlet. A small change in the water-surface elevation is felt as a change in pressure from the present value at the pressure gauge and this in turn is adjusted by a servo-mechanism to bring the gas to bleed at the original rate under the new head. The pressure gauge reads the new water depth which is transmitted to a recorder.

The bubble gauge has certain specific advantages over a float operated water stage recorder and these can be listed as under:

Instrument room

$p = \gamma H$

Gas circuit

H

Pressure point

Reference level

1 High pressure bottle
2 Gas adjustment unit
3 To pressure point
4 Mercury monometer
5 Recorder
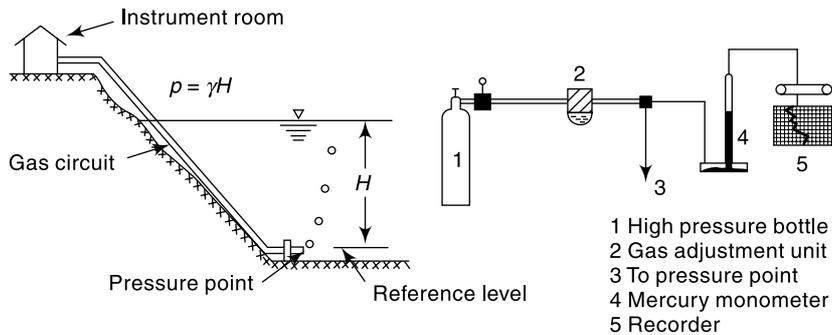
Fig. 4.4 Bubble Gauge

Fig. 4.5 Bubble Gauge Installation —
Telemnip
(*Courtesy* : Neyrtec, Grenoble, France)
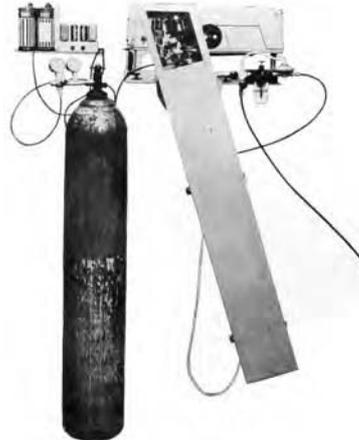
Fig. 4.6 Bubble Gauge — Stevens
Manometer Servo
(*Courtesy* : Leupold and Stevens, Inc.
Beaverton, Oregon, USA)

1. there is no need for costly stilling wells;
2. a large change in the stage, as much as 30 m, can be measured;
3. the recorder assembly can be quite far away from the sensing point; and
4. due to constant bleeding action there is less likelihood of the inlet getting blocked or choked.

STAGE DATA

The stage data is often presented in the form of a plot of stage against chrono-logical time (Fig. 4.7) known as *stage hydrograph*. In addition to its use in the determination of stream discharge, stage data itself is of importance in design of hydraulic structures, flood warning and flood-protection works. Reliable long-term stage data corresponding
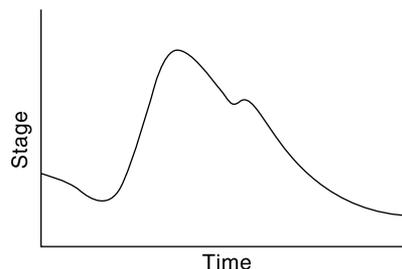
Fig. 4.7 Stage Hydrograph

to peak floods can be analysed statistically to estimate the design peak river stages foruse in the design of hydraulic structures, such as bridges, weirs, etc. Historic flood stages are invaluable in the indirect estimation of corresponding flood discharges. In view of these multifarious uses, the river stage forms an important hydrologic parameter chosen for regular observation and recording.

4.3   MEASUREMENT OF VELOCITY

The measurement of velocity is an important aspect of many direct stream flow measurement techniques. A mechanical device, called *current meter,* consisting essentially of a rotating element is probably the most commonly used instrument for accurate determination of the stream-velocity field. Approximate stream velocities can be determined by *floats.*

CURRENT METERS

The most commonly used instrument in hydrometry to measure the velocity at a point in the flow cross-section is the current meter. It consists essentially of a rotating element which rotates due to the reaction of the stream current with an angular velocity proportional to the stream velocity. Historically, Robert Hooke (1663) invented a propeller-type current meter to measure the distance traversed by a ship. The present-day cup-type instrument and the electrical make-and-break mechanism were invented by Henry in 1868. There are two main types of current meters.

1. Vertical-axis meters, and
2. Horizontal-axis meters.

VERTICAL-AXIS METERS   These instruments consist of a series of conical cups mounted around a vertical axis [Figs. 4.8 and 4.9]. The cups rotate in a horizontal plane and a cam attached to the vertical axial spindle records generated signals proportional to the revolutions of the cup assembly. The Price current meter and Gurley current meter are typical instruments under this category. The normal range of velocities is from 0.15 to 4.0 m/s. The accuracy of these instruments is about 1.50% at the threshold value and improves to about 0.30% at speeds in excess of 1.0 m/s. Vertical-axis instruments have the disadvantage that they cannot be used in situations where there are appreciable vertical components of velocities. For example, the instrument shows a positive velocity when it is lifted vertically in still water.
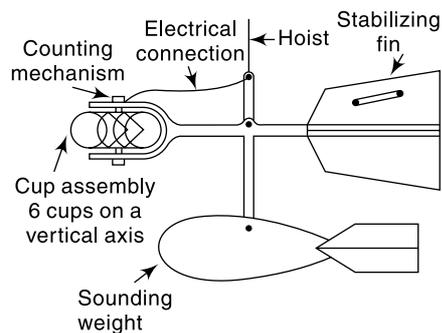
Fig. 4.8   Vertical-axis Current Meter
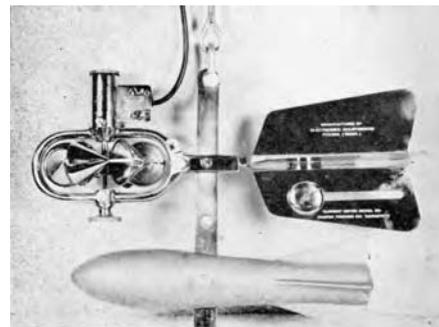
Fig. 4.9 Cup-type Current Meter with Sounding Weight— 'Lynx' Type
(*Courtesy*: Lawrence and Mayo (India) New Delhi)

HORIZONTAL-AXIS METERS These meters consist of a propeller mounted at the end of horizontal shaft as shown in Fig. 4.10 and Fig. 4.11. These come in a wide variety of size with propeller diameters in the range 6 to 12 cm, and can register velocities in the range of 0.15 to 4.0 m/s. Ott, Neyrtec [Fig. 4.12] and Watt-type meters are typical instruments under this kind. These meters are fairly rugged and are not affected by oblique flows of as much as 15°. The accuracy of the instrument is about 1% at the threshold value and is about 0.25% at a velocity of 0.3 m/s and above.

A current meter is so designed that its rotation speed varies linearly with the stream velocity v at the location of the instrument. A typical relationship is

$$v = aN_s + b \qquad (4.1)$$

where v = stream velocity at the instrument location in m/s, N_s = revolutions per second of the meter and a, b = constants of the meter. Typical values of a and b for a standard size 12.5 cm diameter Price meter (cup-type) is $a = 0.65$ and $b = 0.03$. Smaller meters of 5 cm diameter cup assembly called *pigmy meters* run faster and are useful in measuring small velocities. The values of the meter constants for them are of the order of $a = 0.30$ and $b = 0.003$. Further, each instrument has a

Fig. 4.10 Propeller-type Current Meter — Neyrtec Type with Sounding Weight
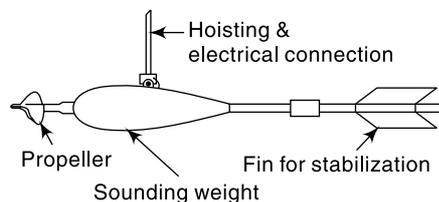
Fig. 4.11 Horizontal-axis Current Meter

threshold velocity below which Eq. (4.1) is not applicable. The instruments have a provision to count the number of revolutions in a known interval of time. This is usually accomplished by the making and breaking of an electric circuit either mechanically or electro-magnetically at each revolution of the shaft. In older model instruments the breaking of the circuit would be counted through an audible sharp signal ("tick") heard on a headphone. The revolutions per second is calculated by counting the number of such signals in a known interval of time, usually about 100 s. Present-day models employ electro-magnetic counters with digital or analogue displays.

CALIBRATION

The relation between the stream velocity and revolutions per second of the meter as in Eq. (4.1) is called the *calibration equation*. The calibration equation is unique to each instrument and is determined by towing the instrument in a special tank. A *towing tank* is a long channel containing still water with arrangements for moving a carriage

Fig. 4.12(a) Neyrtec Type Current Meter for use in Wading (*Courtesy:* Neyrtec, Grenoble, France)

Fig. 4.12(b) Neyrtec Type Meter in a Cableway

longitudinally over its surface at constant speed. The instrument to be calibrated is mounted on the carriage with the rotating element immersed to a specified depth in the water body in the tank. The carriage is then towed at a predetermined constant speed (v) and the corresponding average value of revolutions per second (N_s) of the instruments determined. This experiment is repeated over the complete range of velocities and a best-fit linear relation in the form of Eq. (4.1) obtained. The instruments are designed for rugged use and hence the calibration once done lasts for quite some time. However, from the point of view of accuracy it is advisable to check the instrument calibration once in a while and whenever there is a suspicion that the instrument is damaged due to bad handling or accident. In India excellent towing-tank facilities for calibration of current meters exist at the Central Water and Power Research Station, Pune and the Indian Institute of Technology, Madras.

FIELD USE

The velocity distribution in a stream across a vertical section is logarithmic in nature. In a rough turbulent flow the velocity distribution is given by

$$v = 5.75 \, v_* \, \log_{10}\left(\frac{30 \, y}{k_s}\right) \tag{4.2}$$

where v = velocity at a point y above the bed, v_* = shear velocity and k_s = equivalent sand-grain roughness. To accurately determine the average velocity in a vertical section, one has to measure the velocity at a large number of points on the vertical. As it is time-consuming, certain simplified procedures have been evolved.

- In shallow streams of depth up to about 3.0 m, the velocity measured at 0.6 times the depth of flow below the water surface is taken as the average velocity $\overline{v}$ in the vertical,

$$\bar{v} = v_{0.6} \tag{4.3}$$

This procedure is known as the single-point observation method.

- In moderately deep streams the velocity is observed at two points;
  (i) at 0.2 times the depth of flow below the free surface ($v_{0.2}$) and (ii) at 0.8 times the depth of flow below the free surface ($v_{0.8}$). The average velocity in the vertical $\bar{v}$ is taken as

$$\bar{v} = \frac{v_{0.2} + v_{0.8}}{2} \tag{4.4}$$

- In rivers having flood flows, only the surface velocity (v_s) is measured within a depth of about 0.5 m below the surface. The average velocity $\bar{v}$ is obtained by using a reduction factor K as

$$\bar{v} = Kv_s \tag{4.5}$$

The value of K is obtained from observations at lower stages and lie in the range of 0.85 to 0.95.

In small streams of shallow depth the current meter is held at the requisite depth below the surface in a vertical by an observer who stands in the water. The arrangement, called *wading* is quite fast but is obviously applicable only to small streams.

In rivers flowing in narrow gorges in well-defined channels a cableway is stretched from bank to bank well above the flood level. A carriage moving over the cableway is used as the observation platform.

Bridges, while hydraulically not the best locations, are advantageous from the point of view of accessibility and transportation. Hence, railway and road bridges are frequently employed as gauging stations. The velocity measurement is performed on the downstream portion of the bridge to minimize the instrument damage due to drift and knock against the bridge piers.

For wide rivers, boats are the most satisfactory aids in current meter measurement. A cross-sectional line is marked by distinctive land markings and buoys. The position of the boat is determined by using two theodolites on the bank through an intersection method. Use of total station simplifies the work considerably.

SOUNDING WEIGHTS

Current meters are weighted down by lead weights called *sounding weights* to enable them to be positioned in a stable manner at the required location in flowing water. These weights are of streamlined shape with a fin in the rear (Fig. 4.8) and are connected to the current meter by a hangar bar and pin assembly. Sounding weights come in different sizes and the minimum weight is estimated as

$$W = 50\ \bar{v}\ d \tag{4.6}$$

where W = minimum weight in N, $\bar{v}$ = average stream velocity in the vertical in m/s and d = depth of flow at the vertical in metres.

VELOCITY MEASUREMENT BY FLOATS

A floating object on the surface of a stream when timed can yield the surface velocity by the relation

$$v_s = \frac{S}{t} \tag{4.7}$$

where S = distance travelled in time $t.$ This method of measuring velocities while primitive still finds applications in special circumstances, such as: (i) a small stream in flood, (ii) small stream with a rapidly changing water surface, and (iii) preliminary or exploratory surveys. While any floating object can be used, normally specially made leakproof and easily identifiable floats are used (Fig.
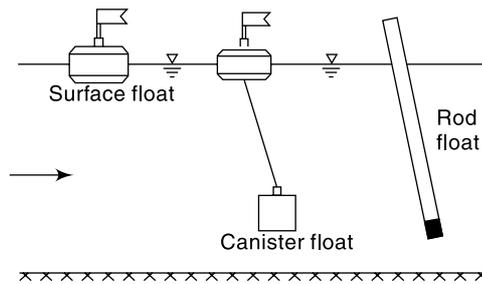
Fig. 4.13   Floats

4.13). A simple float moving on stream surface is called *surface float.* It is easy to use and the mean velocity is obtained by multiplying the observed surface velocity by a reduction coefficient as in Eq. (4.5). However, surface floats are affected by surface winds. To get the average velocity in the vertical directly, special floats in which part of the body is under water are used. *Rod float* (Fig. 4.13), in which a cylindrical rod is weighed so that it can float vertically, belongs to this category.

In using floats to observe the stream velocity a large number of easily identifiable floats are released at fairly uniform spacings on the width of the stream at an upstream section. Two sections on a fairly straight reach are selected and the time to cross this reach by each float is noted and the surface velocity calculated.

4.4   AREA-VELOCITY METHOD

This method of discharge measurement consists essentially of measuring the area of cross-section of the river at a selected section called the *gauging site* and measuring the velocity of flow through the cross-sectional area. The gauging site must be selected with care to assure that the stage-discharge curve is reasonably constant over a long period of about a few years. Towards this the following criteria are adopted.

- The stream should have a well-defined cross-section which does not change in various seasons.
- It should be easily accessible all through the year.
- The site should be in a straight, stable reach.
- The gauging site should be free from backwater effects in the channel.

At the selected site the section line is marked off by permanent survey markings and the cross-section determined. Towards this the depth at various locations are measured by sounding rods or sounding weights. When the stream depth is large or when quick and accurate depth measurements are needed, an electroacoustic instrument called *echo-depth recorder* is used. In this a high frequency sound wave is sent down by a transducer kept immersed at the water surface and the echo reflected by the bed is also picked up by the same transducer. By comparing the time interval between the transmission of the signal and the receipt of its echo, the distance to the bed is obtained and is indicated or recorded in the instrument. Echo-depth recorders are particularly advantageous in high-velocity streams, deep streams and in streams with soft or mobile beds.

For purposes of discharge estimation, the cross-section is considered to be divided into a large number of subsections by verticals (Fig. 4.14). The average velocity in these subsections are measured by current meters or floats. It is quite obvious that the
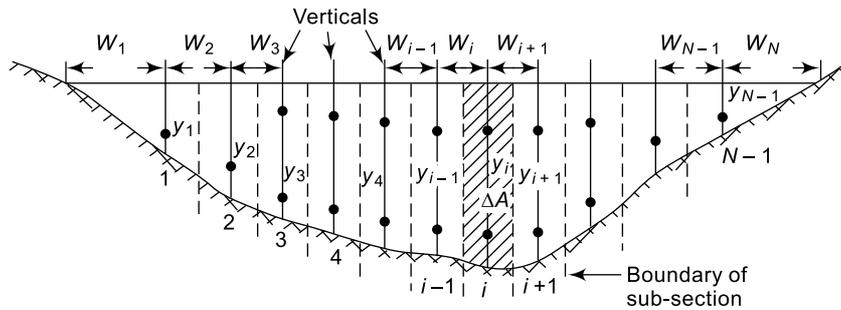
Fig. 4.14 Stream Section for Area-velocity Method

accuracy of discharge estimation increases with the number of subsections used. However, the larger the number of segments, the larger is the effort, time and expenditure involved. The following are some of the guidelines to select the number of segments.

- The segment width should not be greater than 1/15 to 1/20 of the width of the river.
- The discharge in each segment should be less than 10% of the total discharge.
- The difference of velocities in adjacent segments should not be more than 20%.

It should be noted that in natural rivers the verticals for velocity measurement are not necessarily equally spaced. The area-velocity method as above using the current meter is often called as the *standard current meter method.*

CALCULATION OF DISCHARGE

Figure 4.14 shows the cross section of a river in which $N-1$ verticals are drawn. The velocity averaged over the vertical at each section is known. Considering the total area to be divided into $N-1$ segments, the total discharge is calculated by the *method of mid-sections* as follows.

$$Q = \sum_{i=1}^{N-1} \Delta Q_i \tag{4.8}$$

where ΔQ_i = discharge in the ith segment

$$= (\text{depth at the }i\text{th segment}) \times \left(\frac{1}{2} \text{ width to the left} \right.$$

$$\left. + \frac{1}{2} \text{ width to right} \right) \times (\text{average velocity at the }i\text{th vertical})$$

$$\Delta Q_i = y_i \times \left(\frac{W_i}{2} + \frac{W_{i+1}}{2} \right) \times v_i \qquad \text{for } i = 2 \text{ to } (N-2) \tag{4.9}$$

For the first and last sections, the segments are taken to have triangular areas and area calculated as

$$\Delta A_1 = W_1 \cdot y_1$$

where $$\overline{W}_1 = \frac{\left(W_1 + \dfrac{W_2}{2} \right)^2}{2\,W_1} \qquad \text{and} \qquad \Delta A_N = \overline{W}_{N-1} \cdot y_{N-1}$$

$$\text{where} \qquad \overline{W}_{N-1} = \frac{\left(W_N + \dfrac{W_{N-1}}{2}\right)^2}{2\,W_N}$$

to get

$$\Delta Q_1 = \overline{v}_1 \cdot \Delta A_1 \text{ and } \Delta Q_{N-1} = \overline{v}_{N-1}\ \Delta A_{N-1} \tag{4.10}$$

EXAMPLE 4.1 *The data pertaining to a stream-gauging operation at a gauging site are given below.*

The rating equation of the current meter is v = 0.51 N_s + 0.03 m/s where N_s = revolutions per second. Calculate the discharge in the stream.

Distance from left water edge (m)	0	1.0	3.0	5.0	7.0	9.0	11.0	12.0
Depth (m)	0	1.1	2.0	2.5	2.0	1.7	1.0	0
Revolutions of a current meter kept at 0.6 depth	0	39	58	112	90	45	30	0
Duration of observation (s)	0	100	100	150	150	100	100	0

SOLUTION: The calculations are performed in a tabular form.
For the first and last sections,

$$\text{Average width,} \qquad \overline{W} = \frac{\left(1 + \dfrac{2}{2}\right)^2}{2 \times 1} = 2.0 \text{ m}$$

For the rest of the segments,

$$\overline{W} = \left(\frac{2}{2} + \frac{2}{2}\right) = 2.0 \text{ m}$$

Since the velocity is measured at 0.6 depth, the measured velocity is the average velocity at that vertical ($\overline{v}$).

The calculation of discharge by the mid-section method is shown in tabular form below:

Distance from left water edge (m)	Average width $\overline{W}$ (m)	Depth y (m)	N_s = Rev./second	Velocity $\overline{v}$ (m/s)	Segmental discharge ΔQ_i (m³/s)
0	0	0			0.0000
1	2	1.10	0.390	0.2289	0.5036
3	2	2.00	0.580	0.3258	1.3032
5	2	2.50	0.747	0.4110	2..0549
7	2	2.00	0.600	0.3360	1.3440
9	2	1.70	0.450	0.2595	0.8823
11	2	1.00	0.300	0.1830	0.3660
12	0	0.00			0.0000
				Sum =	**6.45393**

Discharge in the stream = 6.454 m³/s

MOVING-BOAT METHOD

Discharge measurement of large alluvial rivers, such as the Ganga, by the standard current meter method is very time-consuming even when the flow is low or moderate. When the river is in spate, it is almost impossible to use the standard current meter technique due to the difficulty of keeping the boat stationary on the fast-moving surface of the stream for observation purposes. It is in such circumstance that the moving-boat techniques prove very helpful.

Fig. 4.15 Moving-boat Method

In this method a special propeller-type current meter which is free to move about a vertical axis is towed in a boat at a velocity v_b at right angles to the stream flow. If the flow velocity is v_f the meter will align itself in the direction of the resultant velocity v_R making an angle θ with the direction of the boat (Fig. 4.15). Further, the meter will register the velocity v_R. If v_b is normal to v_f,

$$v_b = v_R \cos \theta \quad \text{and} \quad v_f = v_R \sin \theta$$

If the time of transit between two verticals is Δt, then the width between the two verticals (Fig. 4.15) is

$$W = v_b \Delta t$$

The flow in the sub-area between two verticals i and $i + 1$ where the depths are y_i and y_{i+1} respectively, by assuming the current meter to measure the average velocity in the vertical, is

$$\Delta Q_i = \left(\frac{y_i + y_{i+1}}{2} \right) W_{i+1} v_f$$

i.e.
$$\Delta Q_i = \left(\frac{y_i + y_{i+1}}{2} \right) v_R^2 \sin \theta \cdot \cos \theta \cdot \Delta t \tag{4.11}$$

Thus by measuring the depths y_i, velocity v_R and θ in a reach and the time taken to cross the reach Δt, the discharge in the sub-area can be determined. The summation of the partial discharges ΔQ_i over the whole width of the stream gives the stream discharge

$$Q = \Sigma \Delta Q_i \tag{4.12}$$

In field application a good stretch of the river with no shoals, islands, bars, etc. is selected. The cross-sectional line is defined by permanent landmarks so that the boat can be aligned along this line. A motor boat with different sizes of outboard motors for use in different river stages is selected. A special current meter of the propeller-type, in which the velocity and inclination of the meter to the boat direction θ in the horizontal plane can be measured, is selected. The current meter is usually immersed at a depth of 0.5 m from the water surface to record surface velocities. To mark the various vertical sections and know the depths at these points, an echo-depth recorder is used.

In a typical run, the boat is started from the water edge and aligned to go across the cross-sectional line. When the boat is in sufficient depth of water, the instruments are lowered. The echo-depth recorder and current meter are commissioned. A button on
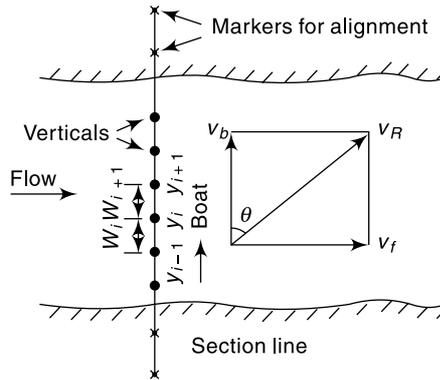
the signal processor when pressed marks a distinctive mark line on the depth vs time chart of the echo-depth recorder. Further, it gives simultaneously a sharp audio signal to enable the measuring party to take simultaneous readings of the velocity v_R and the inclination θ. A large number of such measurements are taken during the traverse of the boat to the other bank of the river. The operation is repeated in the return journey of the boat. It is important that the boat is kept aligned along the cross-sectional line and this requires considerable skill on the part of the pilot. Typically, a river of about 2 km stretch takes about 15 min for one crossing. A number of crossings are made to get the average value of the discharge.

The surface velocities are converted to average velocities across the vertical by applying a coefficient [Eq. (4.5)]. The depths y_i and time intervals Δt are read from the echo-depth recorder chart. The discharge is calculated by Eqs. (4.11) and (4.12). In practical use additional coefficients may be needed to account for deviations from the ideal case and these depend upon the actual field conditions.

4.5   DILUTION TECHNIQUE OF STREAMFLOW MEASUREMENT

The *dilution method* of flow measurement, also known as the *chemical method* depends upon the continuity principle applied to a tracer which is allowed to mix completely with the flow.

Consider a tracer which does not react with the fluid or boundary. Let C_0 be the small initial concentration of the tracer in the streamflow. At Section 1 a small quantity (volume $\forall_1$)" of high concentra-tion C_1 of this tracer is added as shown in Fig. 4.16. Let Section 2 be sufficiently far away on the downstream of Section 1 so that the tracer mixes thoroughly with the fluid due to the turbulent mixing process while passing through the reach. The concentration profile taken at Section 2 is schematically shown in Fig. 4.16. The concentration will

Fig. 4.16   Sudden-injection Method

have a base value of C_0, increases from time t_1 to a peak value and gradually reaches the base value of C_0 at time t_2. The stream flow is assumed to be steady. By continuity of the tracer material

$$M_1 = \text{mass of tracer added at Section 1} = \forall_1 C_1$$

$$= \int_{t_1}^{t_2} Q(C_2 - C_0)\, dt + \frac{\forall_1}{t_2 - t_1} \int_{t_1}^{t_2} (C_2 - C_0)\, dt$$

Neglecting the second term on the right-hand side as insignificantly small,

$$Q = \frac{\forall_1 C_1}{\int_{t_1}^{t_2} (C_2 - C_0)\, dt} \tag{4.13}$$

Thus the discharge Q in the stream can be estimated if for a known M_1 the variation of C_2 with time at Section 2 and C_0 are determined. This method is known as *sudden injection* or *gulp* or *integration method*.

Another way of using the dilution principle is to inject the tracer of concentration C_1 at a constant rate Q_t at Section 1. At Section 2, the concentration gradually rises from the background value of C_0 at time t_1 to a constant value C_2 as shown in Fig. 4.17. At the steady state, the continuity equation for the tracer is

$$Q_t C_1 + Q C_0 = (Q + Q_t) C_2$$

i.e.,
$$Q = \frac{Q_t(C_1 - C_2)}{(C_2 - C_0)} \quad (4.14)$$

This technique in which Q is estimated by knowing C_1, C_2, C_0 and Q_t is known as *constant rate injection method* or *plateau gauging*.

It is necessary to emphasise here that the dilution method of gauging is based on the assumption of steady flow. If the flow is unsteady and the flow rate changes appreciably during gauging, there will be a change in the storage volume in the reach

Fig. 4.17 Constant Rate Injection Method

and the steady-state continuity equation used to develop Eqs. (4.13) and (4.14) is not valid. Systematic errors can be expected in such cases.

TRACERS

The tracer used should have ideally the following properties
1. It should not be absorbed by the sediment, channel boundary and vegetation. It should not chemically react with any of the above surfaces and also should not be lost by evaporation.
2. It should be non-toxic.
3. It should be capable of being detected in a distinctive manner in small concentrations.
4. It should not be very expensive.

The tracers used are of three main types
1. Chemicals (common salt and sodium dichromate are typical)
2. Fluorescent dyes (Rhodamine-WT and Sulpho-Rhodamine B Extra are typical)
3. Radioactive materials (such as Bromine-82, Sodium-24 and Iodine-132).

Common salt can be detected with an error of $\pm 1\%$ up to a concentration of 10 ppm. Sodium dichromate can be detected up to 0.2 ppm concentrations. Fluorescent dyes have the advantage that they can be detected at levels of tens of nanograms per litre (~ 1 in 10^{11}) and hence require very small amounts of solution for injections. Radioactive tracers are detectable up to accuracies of tens of picocuries per litre (~ 1 in 10^{14}) and therefore permit large-scale dilutions. However, they involve the use of very sophisticated instruments and handling by trained personnel only. The availability of detection instrumentation, environmental effects of the tracer and overall cost of the operation are chief factors that decide the tracer to be used.

LENGTH OF REACH   The length of the reach between the dosing section and sampling section should be adequate to have complete mixing of the tracer with the flow. This length depends upon the geometric dimensions of the channel cross-section, discharge and turbulence levels. An empirical formula suggested by Rimmar (1960) for estimation of mixing length for point injection of a tracer in a straight reach is

$$L = \frac{0.13 \, B^2 \, C(0.7 \, C + 2\sqrt{g})}{gd} \qquad (4.15)$$

where L = mixing length (m), B = average width of the stream (m), d = average depth of the stream (m), C = Chezy coefficient of roughness and g = acceleration due to gravity. The value of L varies from about 1 km for a mountain stream carrying a discharge of about 1.0 m^3/s to about 100 km for river in a plain with a discharge of about 300 m^3/s. The mixing length becomes very large for large rivers and is one of the major constraints of the dilution method. Artificial mixing of the tracer at the dosing station may prove beneficial for small streams in reducing the mixing length of the reach.

USE   The dilution method has the major advantage that the discharge is estimated directly in an absolute way. It is a particularly attractive method for small turbulent streams, such as those in mountainous areas. Where suitable, it can be used as an occasional method for checking the calibration, stage-discharge curves, etc. obtained by other methods.

EXAMPLE 4.2   *A 25 g/l solution of a flourescent tracer was discharged into a stream at a constant rate of 10 cm^3/s. The background concentration of the dye in the stream water was found to be zero. At a downstream section sufficiently far away, the dye was found to reach an equilibrium concentration of 5 parts per billion. Estimate the stream discharge.*

SOLUTION: By Eq. (4.14) for the constant-rate injection method,

$$Q = \frac{Q_t (C_1 - C_2)}{C_2 - C_0}$$

$Q_t = 10 \text{ cm}^3/\text{s} = 10 \times 10^{-6} \text{ m}^3/\text{s}$

$C_1 = 0.025, \, C_2 = 5 \times 10^{-9}, \, C_0 = 0$

$$Q = \frac{10 \times 10^{-6}}{5 \times 10^{-9}} (0.025 - 5 \times 10^{-9}) = 50 \text{ m}^3/\text{s}$$

4.6   ELECTROMAGNETIC METHOD

The electromagnetic method is based on the Faraday's principle that an emf is induced in the conductor (water in the present case) when it cuts a normal magnetic field. Large coils buried at the bottom of the channel carry a current I to produce a controlled vertical magnetic field (Fig. 4.18). Electrodes provided at the sides of the channel section measure the small voltage produced due to flow of water in the channel. It has been found that the signal output E will be of the order of millivolts and is related to the discharge Q as

$$Q = K_1 \left(\frac{Ed}{I} + K_2 \right)^n \qquad (4.16)$$

where d = depth of flow, I = current in the coil, and n, K_1 and K_2 are system constants.

C = Conductivity sensor
V = Voltage probe
N = Noise cancellation probe
B = Bed conductivity probe
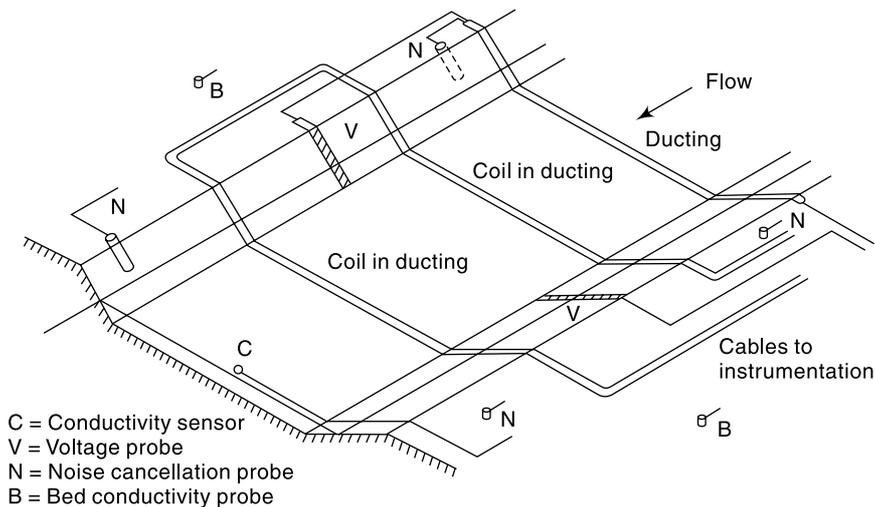
Fig. 4.18 Electromagnetic Method

The method involves sophisticated and expensive instrumentation and has been successfully tried in a number of installations. The fact that this kind of set-up gives the total discharge when once it has been calibrated, makes it specially suited for field situations where the cross-sectional properties can change with time due to weed growth, sedimentation, etc. Another specific application is in tidal channels where the flow undergoes rapid changes both in magnitude as well as in direction. Present, day commercially available electromagnetic flowmeters can measure the discharge to an accuracy of ±3%, the maximum channel width that can be accommodated being 100 m. The minimum detectable velocity is 0.005 m/s.

4.7 ULTRASONIC METHOD

This is essentially an area-velocity method with the average velocity being measured by using ultrasonic signals. The method was first reported by Swengel (1955), since then it has been perfected and complete systems are available commercially.

Consider a channel carrying a flow with two transducers A and B fixed at the same level h above the bed and on either side of the channel (Fig. 4.19). These transducers can receive as well as send ultrasonic signals. Let A send an ultrasonic signal to be received at B after an elapse time t_1 Similarly, let B send a signal to be received at A after an elapse time t_2. If C = velocity of sound in water,

$$t_1 = L/(C + v_p) \tag{4.17}$$

where L = length of path from A to B and v_p = component of the flow velocity in the sound path = $v \cos \theta$. Similarly, from Fig. 4.19 it is easy to see that

$$t_2 = \frac{L}{(C - v_p)} \tag{4.18}$$

Thus
$$\frac{1}{t_1} - \frac{1}{t_2} = \frac{2 v_p}{L} = \frac{2 v \cos \theta}{L}$$
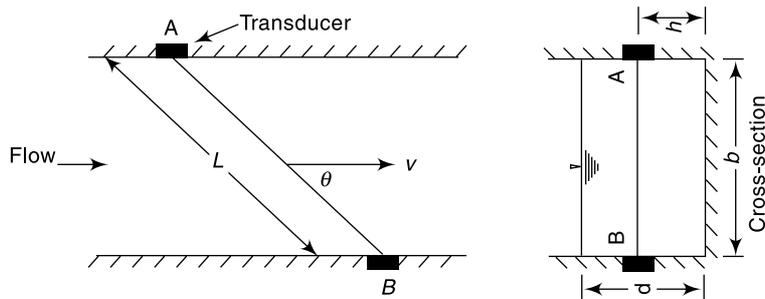
Fig. 4.19 Ultrasonic Method

or
$$v = \frac{L}{2 \cos \theta} \left(\frac{1}{t_1} - \frac{1}{t_2} \right)$$
(4.19)

Thus for a given L and θ, by knowing t_1 and t_2, the average velocity along the path AB, i.e., v can be determined. It may be noted that v is the average velocity at a height h above the bed and is not the average velocity V for the whole cross-section. However, for a given channel cross-section v can be related to V and by calibration a relation between v/V and h can be obtained. For a given set-up, as the area of cross-section is fixed, the discharge is obtained as a product of area and mean velocity V. Estimation of discharge by using one signal path as above is called *single-path gauging*. Alternatively, for a given depth of flow, multiple single paths can be used to obtain v for different h values. Mean velocity of flow through the cross-section is obtained by averaging these v values. This techniques is known as *multi-path gauging*.

Ultrasonic flowmeters using the above principal have frequencies of the order of 500 kHz. Sophisticated electronics are involved to transmit, detect and evaluate the mean velocity of flow along the path. In a given installation a calibration (usually performed by the current-meter method) is needed to determine the system constants. Currently available commercial systems have accuracies of about 2% for the single-path method and 1% for the multipath method. The systems are currently available for rivers up to 500 m width.

The specific advantages of the ultrasonic system of river gauging are
1. It is rapid and gives high accuracy.
2. It is suitable for automatic recording of data.
3. It can handle rapid changes in the magnitude and direction of flow, as in tidal rivers.
4. The cost of installation is independent of the size of rivers.

The accuracy of this method is limited by the factors that affect the signal velo-city and averaging of flow velocity, such as (i) unstable cross-section, (ii) fluctuating weed growth, (iii) high loads of suspended solids, (iv) air entrainment, and (v) salinity and temperature changes.

4.8 INDIRECT METHODS

Under this category are included those methods which make use of the relationship between the flow discharge and the depths at specified locations. The field measurement is restricted to the measurements of these depths only.

Two broad classifications of these indirect methods are

1. Flow measuring structures, and   2. Slope area method.

FLOW-MEASURING STRUCTURES

Use of structures like notches, weirs, flumes and sluice gates for flow measurement in hydraulic laboratories is well known. These conventional structures are used in field conditions also but their use is limited by the ranges of head, debris or sediment load of the stream and the back-water effects produced by the installations. To overcome many of these limitations a wide variety of flow measuring structures with specific advantages are in use.

The basic principle governing the use of a weir, flume or similar flow-measuring structure is that these structures produce a unique *control section* in the flow. At these structures, the discharge Q is a function of the water-surface elevation measured at a specified upstream location,

$$Q = f(H) \tag{4.20}$$

where H = water surface elevation measured from a specified datum. Thus, for example, for weirs, Eq. (4.20) takes the form

$$Q = KH^n \tag{4.21}$$

where H = head over the weir and K, n = system constants. Equation (4.20) is applicable so long as the downstream water level is below a certain limiting water level known as the *modular limit*. Such flows which are independent of the downstream water level are known as *free flows*. If the tail water conditions do affect the flow, then the flow is known as *drowned* or *submerged flow*. Discharges under drowned, condition are obtained by applying a reduction factor to the free flow discharges. For example, the submerged flow over a weir [Fig. 4.20(b)] is estimated by the Villemonte formula,

$$Q_s = Q_1 \left[1 - \left(\frac{H_2}{H_1} \right)^n \right]^{0.385} \tag{4.22}$$

where Q_s = submerged discharge, Q_1 = free flow discharge under head H_1, H_1 = upstream water surface elevation measured above the weir crest, H_2 = downstream water surface elevation measured above the weir crest, n = exponent of head in the free flow head discharge relationship [Eq. (4.21)]. For a rectangular weir $n = 1.5$.
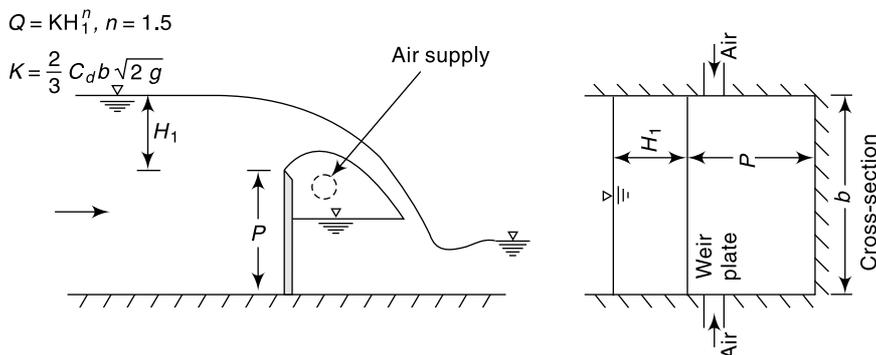
Fig. 4.20(a)   Flow over a Weir: (a) Free Flow

The various flow measuring structures can be broadly considered under three categories:

Fig. 4.20(b) Submerged Flow

THIN-PLATE STRUCTURES are usually made from a vertically set metal plate. The V-notch, rectangular full width and contracted notches are typical examples under this category.
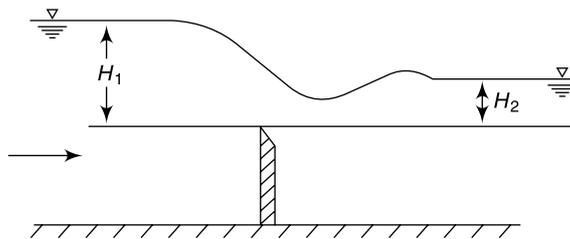
LONG-BASE WEIRS also known as *broad-crested weirs* are made of concrete or masonry and are used for large discharge values.

FLUMES are made of concrete, masonry or metal sheets depending on their use and location. They depend primarily on the width constriction to produce a control section.

Details of the discharge characteristics of flow-measuring structures are available in Refs. 1, 2 and 7.

SLOPE-AREA METHOD

The resistance equation for uniform flow in an open channel, e.g. Manning's formula can be used to relate the depths at either ends of a reach to the discharge. Figure 4.21 shows the longitudinal section of the flow in a river between two sections, 1 and 2. Knowing the water-surface

Fig. 4.21 Slope-area Method

elevations at the two sections, it is required to estimate the discharge. Applying the energy equation to Sections 1 and 2,

$$Z_1 + y_1 + \frac{V_1^2}{2g} = Z_2 + y_2 + \frac{V_2^2}{2g} + h_L$$

where h_L = head loss in the reach. The head loss h_L can be considered to be made up of two parts (i) frictional loss h_f and (ii) eddy loss h_e. Denoting $Z + y = h =$ water-surface elevation above the datum,

$$h_1 + \frac{V_1^2}{2g} = h_2 + \frac{V_2^2}{2g} + h_e + h_f$$

or
$$h_f = (h_1 - h_2) + \left(\frac{V_1^2}{2g} - \frac{V_2^2}{2g}\right) - h_e \qquad (4.23)$$

If L = length of the reach, by Manning's formula for uniform flow,

$$\frac{h_f}{L} = S_f = \text{energy slope} = \frac{Q^2}{K^2}$$

where K = conveyance of the channel = $\frac{1}{n} AR^{2/3}$

In nonuniform flow an average conveyance is used to estimate the average energy slope and

$$\frac{h_f}{L} = \bar{S}_f = \frac{Q^2}{K^2} \tag{4.24}$$

where $K = \sqrt{K_1 K_2}$; $K_1 = \frac{1}{n_1} A_1 R_1^{2/3}$ and $K_2 = \frac{1}{n_2} A_2 R_2^{2/3}$

n = Manning's roughness coefficient

The eddy loss h_e is estimated as

$$h_e = K_e \left| \frac{V_1^2}{2g} - \frac{V_2^2}{2g} \right| \tag{4.25}$$

where K_e = eddy-loss coefficient having values as below.

Cross-section characteristic of the reach	Value of K	
	Expansion	**Contraction**
Uniform	0	0
Gradual transition	0.3	0.1
Abrupt transition	0.8	0.6

Equation (4.23), (4.24) and (4.25) together with the continuity equation $Q = A_1 V_1 = A_2 V_2$ enable the discharge Q to be estimated for known values of h, channel cross-sectional properties and n.

The discharge is calculated by a trial and error procedure using the following sequence of calculations

1. Assume $V_1 = V_2$. This leads to $V_1^2/2g = V_2^2/2g$ and by Eq. (4.23)
   $h_f = h_1 - h_2 = F =$ fall in the water Surface between Sections 1 and 2
2. Using Eq. (4.24) calculate discharge Q
3. Compute $V_1 = Q/A_1$ and $V_2 = Q/A_2$. Calculate velocity heads and eddy-loss h_e
4. Now calculate a refined value of h_f by Eq. (4.23) and go to step (2). Repeat the calculations till two successive calculations give values of discharge (or h_f) differing by a negligible margin.

This method of estimating the discharge is known as the *slope-area method*. It is a very versatile indirect method of discharge estimation and requires (i) the selection of a reach in which cross-sectional properties including bed elevations are known at its ends, (ii) the value of Manning's n and (iii) water-surface elevations at the two end sections.

EXAMPLE 4.3 *During a flood flow the depth of water in a 10 m wide rectangular channel was found to be 3.0 m and 2.9 m at two sections 200 m apart. The drop in the water-surface elevation was found to be 0.12 m. Assuming Manning's coefficient to be 0.025, estimate the flood discharge through the channel.*

SOLUTION: Using suffixes 1 and 2 to denote the upstream and downstream sections respectively, the cross-sectional properties are calculated as follows:

Section 1	Section 2
$y_1 = 3.0$ m	$y_2 = 2.90$ m
$A_1 = 30$ m^2	$A_2 = 29$ m^2
$P_1 = 16$ m	$P_2 = 15.8$ m
$R_1 = 1.875$ m	$R_2 = 1.835$ m
$K_I = \dfrac{1}{0.025} \times 30 \times (1.875)^{2/3}$	$K_2 = \dfrac{1}{0.025} \times 29 \times (1.835)^{2/3}$
$= 1824.7$	$= 1738.9$

Average K for the reach $= \sqrt{K_1 K_2} = 1781.3$
To start with $h_f =$ fall $= 0.12$ m is assumed.
Eddy loss $h_e = 0$
The calculations are shown in Table 4.1.

$$\bar{S}_f = h_f/L = h_f/200 \qquad Q = K\sqrt{\bar{S}_f} = 1781.3\sqrt{\bar{S}_f}$$

$$\frac{V_1^2}{2g} = \left(\frac{Q}{30}\right)^2 /19.62, \frac{V_2^2}{2g} = \left(\frac{Q}{29}\right)^2 /19.62$$

$$h_f = (h_1 - h_2) + \left(\frac{V_1^2}{2g} - \frac{V_2^2}{2g}\right)$$

$$h_f = \text{fall} + \left(\frac{V_1^2}{2g} - \frac{V_2^2}{2g}\right) = 0.12 + \left(\frac{V_1^2}{2g} - \frac{V_2^2}{2g}\right) \qquad \text{(E–1)}$$

Table 4.1   Calculations for Example 4.3

Trial	h_f (trial)	S_f (units of 10^{-4})	Q (m^3/s)	$V_1^2/2g$ (m)	$V_2^2/2g$ (m)	h_f by Eq. (E–1) (m)
1	0.1200	6.000	43.63	0.1078	0.1154	0.1124
2	0.1124	5.622	42.24	0.1010	0.1081	0.1129
3	0.1129	5.646	42.32	0.1014	0.1081	0.1129

(The last column is h_f by Eq. (E–1) and its value is adopted for the next trial.)
The discharge in the channel is 42.32 m^3/s.

FLOOD DISCHARGE BY SLOPE-AREA METHOD   The slope-area method is of particular use in estimating the flood discharges in a river by past records of stages at different sections. Floods leave traces of peak elevations called high-water marks in their wake. Floating vegetative matter, such as grass, straw and seeds are left stranded at high water levels when the flood subsides and form excellent marks. Other high-water marks include silt lines on river banks, trace of erosion on the banks called *wash lines* and silt or stain lines on buildings. In connection with the estimation of very high

floods, interviews with senior citizens living in the area, who can recollect from memory certain salient flood marks are valuable. Old records in archives often provide valuable information on flood marks and dates of occurrence of those floods. Various such information relating to a particular flood are cross-checked for consistency and only reliable data are retained. The slope-area method is then used to estimate the magnitude of the flood.

The selection of the reach is probably the most important aspect of the slope-area method. The following criteria can be listed towards this:

- The quality of high-water marks must be good.
- The reach should be straight and uniform as far as possible. Gradually contracting sections are preferred to an expanding reach.
- The recorded fall in the water-surface elevation should be larger than the velocity head. It is preferable if the fall is greater than 0.15 m.
- The longer the reach, the greater is the accuracy in the estimated discharge. A length greater than 75 times the mean depth provides an estimate of the reach length required.

The Manning's roughness coefficient n for use in the computation of discharge is obtained from standard tables[7]. Sometimes a relation between n and the stage is prepared from measured discharges at a neighbouring gauging station and an appropriate value of n selected from it, with extrapolation if necessary.

4.9   STAGE-DISCHARGE RELATIONSHIP

As indicated earlier the measurement of discharge by the direct method involves a two step procedure; the development of the stage-discharge relationship which forms the first step is of utmost importance. Once the stage-discharge $(G - Q)$ relationship is established, the subsequent procedure consists of measuring the stage (G) and reading the discharge (Q) from the $(G - Q)$ relationship. This second part is a routine operation. Thus the aim of all current-meter and other direct-discharge measurements is to prepare a stage-discharge relationship for the given channel gauging section. The stage-discharge relationship is also known as the *rating curve.*

The measured value of discharges when plotted against the corresponding stages gives relationship that represents the integrated effect of a wide range of channel and flow parameters. The combined effect of these parameters is termed *control.* If the $(G - Q)$ relationship for a gauging section is constant and does not change with time, the control is said to be *permanent.* If it changes with time, it is called *shifting control*.

PERMANENT CONTROL

A majority of streams and rivers, especially nonalluvial rivers exhibit permanent control. For such a case, the relationship between the stage and the discharge is a single-valued relation which is expressed as

$$Q = C_r (G - a)^\beta \tag{4.26}$$

in which Q = stream discharge, G = gauge height (stage), a = a constant which represent the gauge reading corresponding to zero discharge, C_r and β are rating curve constants. This relationship can be expressed graphically by plotting the observed relative stage $(G - a)$ against the corresponding discharge values in an arithmetic or logarithmic plot [Fig. 4.22(a) and (b)]. Logarithmic plotting is advantageous as Eq. (4.26) plots as a
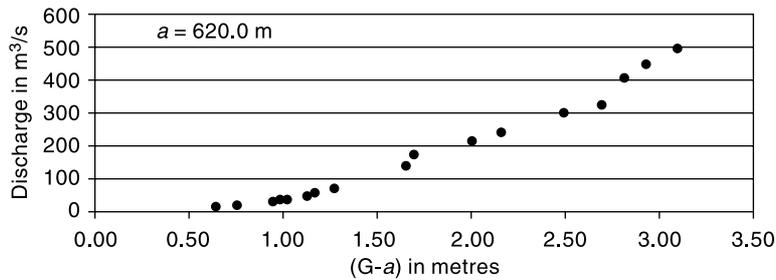
Fig. 4.22(a)   Stage-Discharge Curve: Arithmetic Plot
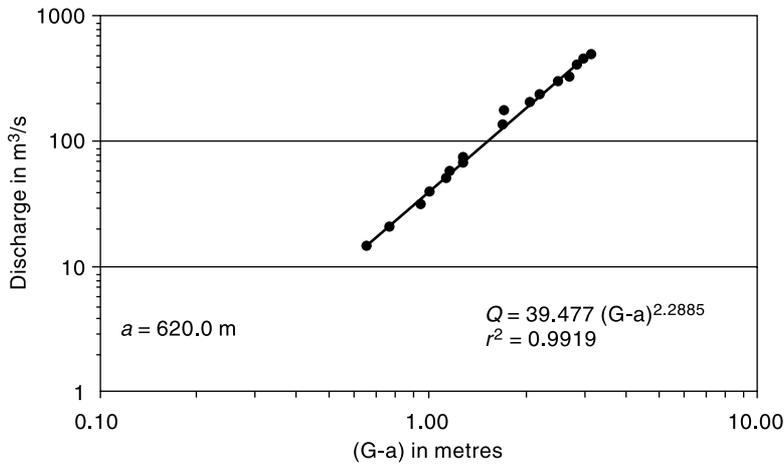
Fig. 4.22(b)   Stage-Discharge Curve: Logarithmic Plot

straight line in logarithmic coordinates. In Fig. 4.22(b) the straight line is drawn to best represent the data plotted as Q vs $(G - a)$. Coefficients C_r and β need not be the same for the full range of stages.

The best values of C_r and β in Eq. (4.26) for a given range of stage are obtained by the least-square-error method. Thus by taking logarithms,

$$\log Q = \beta \log (G - a) + \log C_r \tag{4.27}$$

or $$Y = \beta X + b \tag{4.27a}$$

in which the dependent variable $Y = \log Q$, independent variable $X = \log (G - a)$ and $b = \log C_r$. For the best-fit straight line of N observations of X and Y, by regressing $X = \log (G - a)$ on $Y = \log Q$

$$\beta = \frac{N\,(\Sigma XY) - (\Sigma X)(\Sigma Y)}{N\,(\Sigma X^2) - (\Sigma X)^2} \tag{4.28a}$$

and $$b = \frac{\Sigma Y - \beta(\Sigma X)}{N} \tag{4.28b}$$

Pearson product moment correlation coefficient

$$r = \frac{N\,(\Sigma XY) - (\Sigma X)(\Sigma Y)}{\sqrt{[N\,(\Sigma X^2) - (\Sigma X)^2][N\,(\Sigma Y^2) - (\Sigma Y)^2]}} \tag{4.29}$$

Here r reflects the extent of linear relationship between the two data sets.

For a perfect correlation $r = 1.0$. If r is between 0.6 and 1.0 it is generally taken as a good correlation. It should be noted that in the present case, as the discharge Q increases with $(G - a)$ the variables Y and X are positively correlated and hence r is positive. Equation (4.26), viz.

$$Q = C_r(G - a)^\beta$$

is called the *rating equation* of the stream and can be used for estimating the discharge Q of the stream for a given gauge reading G within range of data used in its derivation.

STAGE FOR ZERO DISCHARGE, a In Eq. (4.26) the constant a representing the stage (gauge height) for zero discharge in the stream is a hypothetical parameter and cannot be measured in the field. As such, its determination poses some difficulties. The following alternative methods are available for its determination:

1. Plot Q vs G on an arithmetic graph paper and draw a best-fit curve. By extrapolating the curve by eye judgment find a as the value of G corresponding to $Q = 0$. Using the value of a, plot log Q vs log $(G - a)$ and verify whether the data plots as a straight line. If not, select another value in the neighbourhood of previously assumed value and by trial and error find an acceptable value of a which gives a straight line plot of log Q vs log $(G - a)$.

2. A graphical method due to Running[8] is as follows. The Q vs G data are plotted to an arithmetic scale and a smooth curve through the plotted points are drawn. Three points A, B and C on the curve are selected such that their discharges are in geometric progression (Fig. 4.23), i.e.

Fig. 4.23 Running's Method for Estimation of the Constant a

$$\frac{Q_A}{Q_B} = \frac{Q_B}{Q_C}$$

At A and B vertical lines are drawn and then horizontal lines are drawn at B and C to get D and E as intersection points with the verticals. Two straight lines ED and BA are drawn to intersect at F. The ordinate at F is the required value of a, the gauge height corresponding to zero discharge. This method assumes the lower part of the stage-discharge curve to be a parabola.

3. Plot Q vs G to an arithmetic scale and draw a smooth good-fitting curve by eye-judgement. Select three discharges Q_1, Q_2 and Q_3 such that $Q_1/Q_2 = Q_2/Q_3$ and note from the curve the corresponding values of gauge readings G_1, G_2 and G_3. From Eq. (4.26)

$$(G_1 - a)/(G_2 - a) = (G_2 - a)/(G_3 - a)$$

i.e.

$$a = \frac{G_1 G_3 - G_2^2}{(G_1 + G_3) - 2G_2} \tag{4.30}$$

4. A number of optimization procedures are available to estimate the best value of *a*. A trial-and-error search for *a* which gives the best value of the correlation coefficient is one of them.

EXAMPLE 4.4 *Following are the data of gauge and discharge collected at a particular section of the river by stream gauging operation. (a) Develop a gauge-discharge relationship for this stream at this section for use in estimating the discharge for a known gauge reading. What is the coefficient of correlation of the derived relationship? Use a value of a = 7.50 m for the gauge reading corresponding to zero discharge. (b) Estimate the discharge corresponding to a gauge reading of 10.5 m at this gauging section.*

Gauge reading (m)	Discharge (m^3/s)	Gauge reading (m)	Discharge (m^3/s)
7.65	15	8.48	170
7.70	30	8.98	400
7.77	57	9.30	600
7.80	39	9.50	800
7.90	60	10.50	1500
7.91	100	11.10	2000
8.08	150	11.70	2400

SOLUTION: (a) The gauge–discharge equation is $Q = C_r(G - a)^\beta$
Taking the logarithms $\log Q = \beta \log (G - a) + \log C_r$
or $Y = \beta X + b$
where $Y = \log Q$ and $X = \log (G - a)$.
Values of X, Y and XY are calculated for all the data as shown in Table 4.2.

Table 4.2 Calculations for Example 4.4

$a = 7.5$ m $N = 14$

Stage (G) (metres)	(G – a) (m)	Discharge (Q)(m^3/s)	log (G – a) = X	log Q = Y	XY	X^2	Y^2
7.65	0.15	15	–0.824	1.176	–0.969	0.679	1.383
7.70	0.20	30	–0.699	1.477	–1.032	0.489	2.182
7.77	0.27	57	–0.569	1.756	–0.998	0.323	3.083
7.80	0.30	39	–0.523	1.591	–0.832	0.273	2.531
7.90	0.40	60	–0.398	1. 778	–0.708	0.158	3.162
7.91	0.41	100	–0.387	2.000	–0.774	0.150	4.000
8.08	0.58	150	–0.237	2.176	–0.515	0.056	4.735
8.48	0.98	170	–0.009	2.230	–0.020	0.000	4.975
8.98	1.48	400	0.170	2.602	0.443	0.029	6.771
9.30	1.80	600	0.255	2.778	0.709	0.065	7.718
9.50	2.00	800	0.301	2.903	0.874	0.091	8.428
10.50	3.00	1500	0.477	3.176	1.515	0.228	10.088
11.10	3.60	2000	0.556	3.301	1.836	0.309	10.897
11.70	4.20	2400	0.623	3.380	2.107	0.388	11.426
		Sum	**–1.262**	**32.325**	**1.636**	**3.239**	**81.379**

From the above table:

$\Sigma X = -1.262$	$\Sigma Y = 32.325$	$\Sigma XY = 1.636$
$\Sigma X^2 = 3.239$	$\Sigma Y^2 = 81.379$	
$(\Sigma X)^2 = 1.5926$	$(\Sigma Y)^2 = 1044.906$	$N = 14$

By using Eq. (4.28a)

$$\beta = \frac{N(\Sigma XY) - (\Sigma X)(\Sigma Y)}{N(\Sigma X^2) - (\Sigma X)^2} = \frac{(14 \times 1.636) - (-1.262)(32.325)}{(14 \times 3.239) - (-1.262)^2} = 1.4558$$

By Eq. (4.28b)

$$b = \frac{\Sigma Y - \beta(\Sigma X)}{N} = \frac{(32.325) - 1.4558 \times (-1.262)}{14} = 2.440$$

Hence $\quad C_r = 275.52$

The required gauge–discharge relationship is therefore

$$Q = 275.52 \, (G - a)^{1.456}$$

By Eq. 4.29 coefficient of correlation

$$r = \frac{N(\Sigma XY) - (\Sigma X)(\Sigma Y)}{\sqrt{[N(\Sigma X^2) - (\Sigma X)^2][N(\Sigma Y^2) - (\Sigma Y)^2]}}$$

$$= \frac{(14 \times 1.636) - (-1.262)(32.325)}{\sqrt{[(14 \times 3.239) - (1.5926)][(14 \times 81.379) - (1044.906)]}} = 0.9913$$

As the value of r is nearer to unity the correlation is very good.

The variation of discharge (Q) with relative stage ($G - a$) is shown in Fig. 4.24(a)—arithmetic plot and in Fig. 4.24(b)—logarithmic plot.

(b) when $G = 10.05$: as $a = 7.5$ m

$$G = 275.52 \, (10.05 - 7.50)^{1.456} = 1076 \text{ m}^3/\text{s}$$
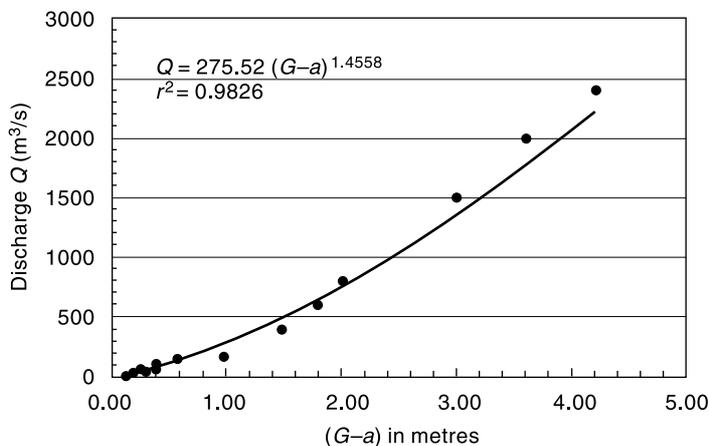
Fig. 4.24(a)   Stage-discharge Relation (Arithmetic Plot)—Example 4.4

SHIFTING CONTROL

The control that exists at a gauging section giving rise to a unique stage-discharge relationship can change due to: (i) changing characteristics caused by weed growth,
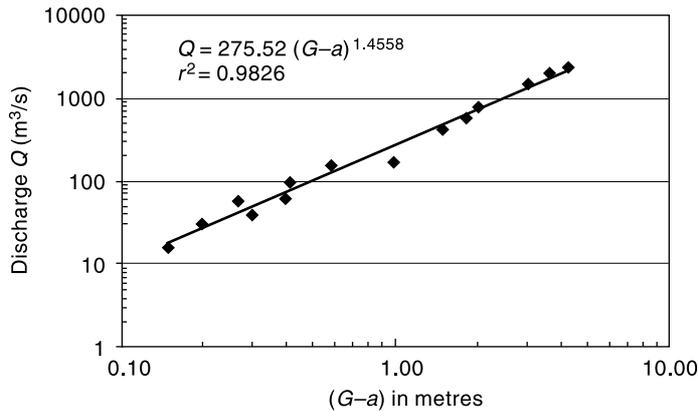
Fig. 4.24(b) Stage-discharge Relationship (Logarithmic Plot) — Example 4.4

dredging or channel encroachment, (ii) aggradation or degradation phenomenon in an alluvial channel, (iii) variable backwater effects affecting the gauging section and (iv) unsteady flow effects of a rapidly changing stage. There are no permanent corrective measure to tackle the shifting controls due to causes (i) and (ii) listed above. The only recourse in such cases is to have frequent current-meter gaugings and to update the rating curves. Shifting controls due to causes (iii) and (iv) are described below.

BACKWATER EFFECT If the shifting control is due to variable backwater curves, the same stage will indicate different discharges depending upon the backwater effect. To remedy this situation another gauge, called the *secondary gauge* or *auxiliary gauge* is installed some distance downstream of the gauging section and readings of both gauges are taken. The difference between the main gauge and the secondary gauge gives the *fall* (F) of the water surface in the reach. Now, for a given main-stage reading, the discharge under variable backwater condition is a function of the fall F, i.e.

$$Q = f(G, F)$$

Schematically, this functional relationship is shown in Fig. 4.25. Instead of having a three-parameter plot, the observed data is normalized with respect to a constant fall value. Let F_0 be a normalizing value of the fall taken to be constant at all stages and F the actual fall at a given stage when the actual discharge is Q. These two fall values are related as

$$\frac{Q}{Q_0} = \left(\frac{F}{F_0}\right)^m \qquad (4.31)$$

in which Q_0 = normalized discharge at the given stage when the fall is equal to F_0 and m = an
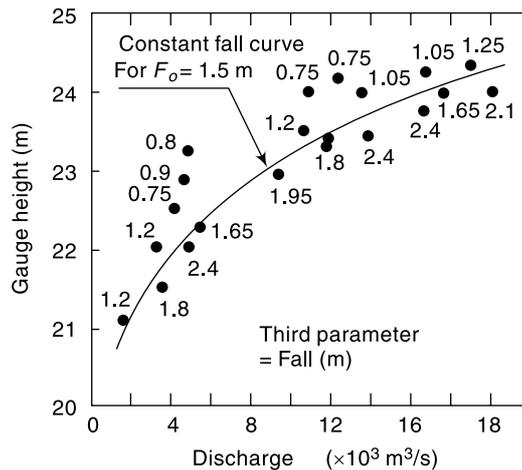
Fig. 4.25 Backwater Effect on a Rating Curve — Normalised Curve

exponent with a value close to 0.5. From the observed data, a convenient value of F_0 is selected. An approximate Q_0 vs G curve for a constant F_0 called *constant fall curve* is drawn. For each observed data, Q/Q_0 and F/F_0 values are calculated and plotted as Q/Q_0 vs F/F_0 (Fig. 4.26). This is called the *adjustment curve*. Both the constant fall curve and the adjustment curve are refined, by trial and error to get the best-fit curves. When finalized, these two curves provide the stage-discharge information for gauging purposes. For example, if the ob-

Fig. 4.26 Backwater Effect on a Rating Curve — Adjustment Curve

served stage is G_1 and fall F_1, first by using the adjustment curve the value of Q_1/Q_0 is read for a known value of F_1/F_0. Using the constant fall-rating curve, Q_0 is read for the given stage G_1 and the actual discharge calculated as $(Q_1/Q_0) \times Q_0$.

UNSTEADY-FLOW EFFECT   When a flood wave passes a gauging station in the advancing portion of the wave the approach velocities are larger than in the steady flow at corresponding stage. Thus for the same stage, more-discharge than in a steady uniform flow occurs. In the retreating phase of the flood wave the converse situation occurs with reduced approach velocities giving lower discharges than in an equivalent steady flow case. Thus the stage-discharge relationship for an unsteady flow will not be a single-valued relationship as in steady flow but it will be a looped curve as in Fig. 4.27. It may be noted that at the same stage, more discharge passes through the river during rising stages than in falling ones. Since the conditions for each flood may be different, different floods may give different loops.
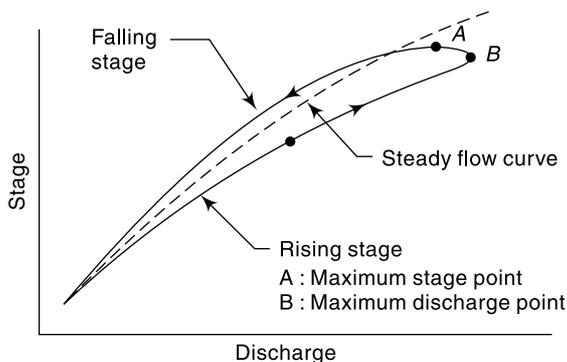
Fig. 4.27 Loop Rating Curve

If Q_n is the normal discharge at a given stage under steady uniform flow and Q_M is the measured (actual) unsteady flow the two are related as[7]

$$\frac{Q_M}{Q_n} = \sqrt{1 + \frac{1}{V_w S_0}\frac{dh}{dt}} \tag{4.32}$$

where S_0 = channel slope = water surface slope at uniform flow, dh/dt = rate of change of stage and V_w = velocity of the flood wave. For natural channels, V_w is usually

assumed equal to 1.4 V, where V = average velocity for a given stage estimated by applying Manning's formula and the energy slope S_f. Also, the energy slope is used in place of S_0 in the denominator of Eq. (4.32). If enough field data about the flood magnitude and dh/dt are available, the term $(1/V_w S_0)$ can be calculated and plotted against the stage for use in Eq. (4.32). For estimating the actual discharge at an observed stage, Q_M/Q_n is calculated by using the observed data of dh/dt. Here Q_n is the discharge corresponding to the observed stage relationship for steady flow in the channel reach.

EXAMPLE 4.5 *An auxiliary gauge was used downstream of a main gauge in a river to provide corrections to the gauge-discharge relationship due to backwater effects. The following data were noted at a certain main gauge reading.*

Main gauge (m above datum)	Auxiliary gauge (m above datum)	Discharge (m³/s)
86.00	85.50	275
86.00	84 80	600

If the main gauge reading is still 86.00 m and the auxiliary gauge reads 85.30 m, estimate the discharge in the river.

SOLUTION: Fall (F) = main gauge reading – auxiliary gauge reading.

When $\quad\quad F_1 = (86.00 - 85.50) = 0.50$ m $\quad\quad Q_1 = 275$ m³/s

$\quad\quad\quad\quad F_2 = (86.00 - 84.80) = 1.20$ m $\quad\quad Q_2 = 600$ m³/s

By Eq. (4.31) $\quad (Q_1/Q_2) = (F_1/F_2)^m \quad$ or $\quad (275/600) = (0.50/1.20)^m$

Hence $\quad\quad m = 0.891$

When the auxiliary gauge reads 85.30 m, at a main gauge reading of 86.00 m,

$\quad\quad$ Fall $F = (86.00 - 85.30) = 0.70$ m and

$\quad\quad Q = Q_2 (F/F_2)^m = 600 (0.70/1.20)^{0.891} = 371$ m³/s

4.10   EXTRAPOLATION OF RATING CURVE

Most hydrological designs consider extreme flood flows. As an example, in the design of hydraulic structures, such as barrages, dams and bridges one needs maximum flood discharges as well as maximum flood levels. While the design flood discharge magnitude can be estimated from other considerations, the stage-discharge relationship at the project site will have to be used to predict the stage corresponding to design-flood discharges. Rarely will the available stage-discharge data include the design-flood range and hence the need for extrapolation of the rating curve.

Before attempting extrapolation, it is necessary to examine the site and collect relevant data on changes in the river cross-section due to flood plains, roughness and backwater effects. The reliability of the extrapolated value depends on the stability of the gauging section control. A stable control at all stages leads to reliable results. Extrapolation of the rating curve in an alluvial river subjected to aggradation and degradation is unreliable and the results should always be confirmed by alternate methods. There are many techniques of extending the rating curve and two well-known methods are described here.

CONVEYANCE METHOD

The conveyance of a channel in nonuniform flow is defined by the relation

$$Q = K\sqrt{S_f} \qquad (4.33)$$

where Q = discharge in the channel, S_f = slope of the energy line and K = conveyance. If Manning's formula is used,

$$K = \frac{1}{n} AR^{2/3} \qquad (4.34)$$

where n = Manning's roughness, A = area of cross-section and, R = hydraulic radius. Since A and R are functions of the stage, the values of K for various values of stage are calculated by using Eq. (4.34) and plotted against the stage. The range of the stage should include values beyond the level up to which extrapolation is desired. Then a smooth curve is fitted to the plotted points as shown in Fig. 4.28(a). Using the available discharge and stage data, values of S_f are calculated by using Eq. (4.33) as $S_f = Q^2/K^2$ and are plotted against the stage. A smooth curve is fitted through the plotted points as shown in Fig. 4.28(b). This curve is then extrapolated keeping in mind that S_f approaches a constant value at high stages.
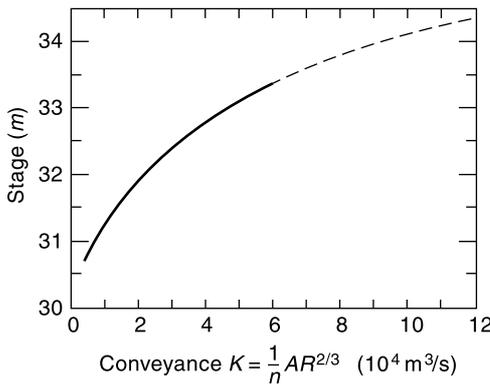
Fig. 4.28(a)　Conveyance Method of Rating Curve Extension: K vs Stage
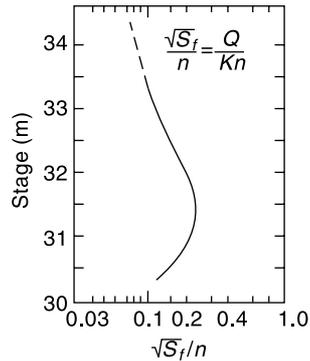
Fig. 4.28(b)　Conveyance Method of Rating Curve Extension: S_f vs Stage

Using the conveyance and slope curves, the discharge at any stage is calculated as $Q = K\sqrt{S_f}$ and a stage-discharge curve covering the desired range of extrapolation is constructed. With this extrapolated-rating curve, the stage corresponding to a design-flood discharge can be obtained.

LOGARITHMIC-PLOT METHOD

In this technique the stage-discharge relationship given by Eq. (4.26) is made use of. The stage is plotted against the discharge on a log–log paper. A best-fit linear relationship is obtained for data points lying in the high-stage range and the line is extended to cover the range of extrapolation. Alternatively, coefficients of Eq. (4.26) are obtained by the least-square-error method by regressing X on Y in Eq. (4.27a). For this Eq. (4.27a) is written as

$$X = \alpha Y + C \tag{4.35}$$

where the dependent variable $X = \log(G - a)$ and $Y = \log Q$. The coefficients α and C are obtained as,

$$\alpha = \frac{N(\Sigma XY) - (\Sigma Y)(\Sigma X)}{N(\Sigma Y^2) - (\Sigma Y)^2} \tag{4.35a}$$

and

$$C = \frac{(\Sigma X) - \alpha(\Sigma Y)}{N} \tag{4.35b}$$

The relationship governing the stage and discharge is now

$$(G - a) = C_1 Q^\alpha \tag{4.36}$$

where $C_1 = $ antilog C.

By the use of Eq. (4.36) the value of the stage corresponding to a design flood discharge is estimated.

EXAMPLE 4.6 *For the stage-discharge data of Example 4.4, fit a regression equation for use in estimation of stage for a known value of discharge. Use a value of 7.50 m as the gauge reading corresponding to zero discharge. Determine the stage for a discharge of 3500 m^3/s.*

SOLUTION: The regression equation is $X = \alpha Y + C$ (Eq. 4.35)
where $X = \log(G - a)$ and $Y = \log Q$. The value of α is given by Eq. (4.35a) as

$$\alpha = \frac{N(\Sigma XY) - (\Sigma Y)(\Sigma X)}{N(\Sigma Y^2) - (\Sigma Y)^2}$$

Values of X, Y and XY are the same as calculated for the data in Table 4.3. Thus

$\Sigma X = -1.262$ $\Sigma Y = 32.325$ $\Sigma XY = 1.636$
$\Sigma X^2 = 3.239$ $\Sigma Y^2 = 81.379$
$(\Sigma X)^2 = 1.5926$ $(\Sigma Y)^2 = 1044.906$ $N = 14$

Substituting these values in Eq. (4.35)

$$\alpha = \frac{(14 \times 1.636) - (32.325)(-1.262)}{(14 \times 81.379) - (1044.906)} = 0.675$$

The coefficient C is given by Eq. (4.35b) as

$$C = \frac{(\Sigma X) - \alpha(\Sigma Y)}{N} = \frac{(-1.262) - 0.675(32.325)}{14} = -1.6486$$

$C_1 = $ antilog $C = 0.02246$ leading to the gage-discharge equation as

$$(G - a) = 0.02246 \, Q^{0.675}$$

The variation of relative stage $(G - a)$ with discharge (Q) is shown in Fig. 4.29(a)—arithmetic plot and in Fig. 4.29(b)—logarithmic plot.
(b) When $Q = 3500$ m^3/s and given that $a = 7.50$ m

$$(G - 7.50) = 0.02246 \, (3500)^{0.675} = 5.540 \text{ m}$$
$$G = 13.04 \text{ m}$$

4.11 HYDROMETRY STATIONS

As the measurement of discharge is of paramount importance in applied hydrologic studies, considerable expenditure and effort are being expended in every country to collect and store this valuable historic data. The WMO recommendations for the minimum number of hydrometry stations in various geographical regions are given in Table 4.3.
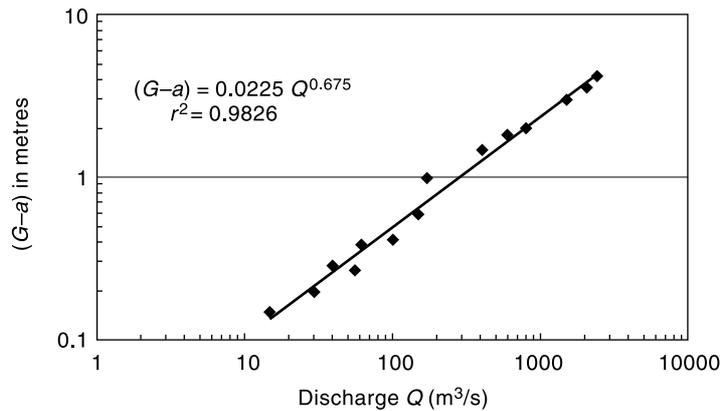
Fig. 4.29(a) Discharge-stage Relationship: Example 4.6 (Logarithmic Plot)
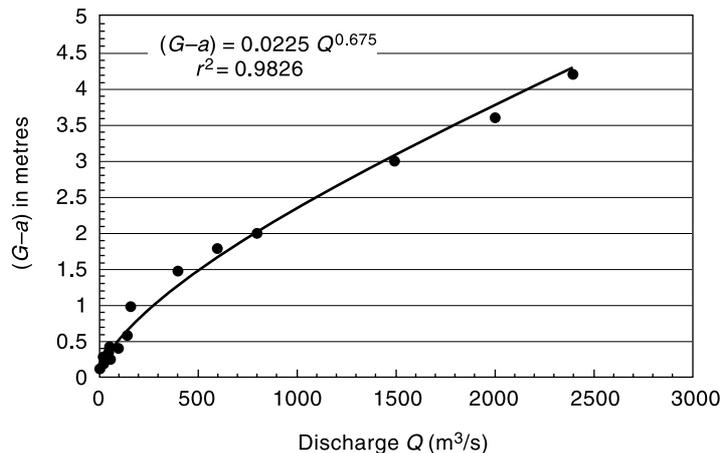
Fig. 4.29(b) Discharge-stage Relationship: Example 4.6 (Arithmetic Plot)

Table 4.3 WMO Criteria for Hydrometry Station Density

S. No.	Region	Minimum density (km²/station)	Tolerable density under difficult conditions (km²/station)
1.	Flat region of temperate, mediterranean and tropical zones	1,000 – 2,500	3,000 – 10,000
2.	Mountainous regions of temperate mediterranean and tropical zones	300 – 1,000	1,000 – 5,000
3.	Arid and polar zones	5,000 – 20,000	

Hydrometry stations must be sited in adequate number in the catchment area of all major streams so that the water potential of an area can be assessed as accurately as possible.

As a part of hydrological observation activities CWC operates a vast network of 877 hydrological observation stations on various state and interstate rivers for collection of gauge, discharge, silt and water quality data which are stored after analysis in central data bank. In addition to observation of river flow, CWC is also monitoring water quality, covering all the major river basins of India. The distribution of various kinds of CWC hydrological observation stations is as follows:

Type of Station	Number
Gauge observation only	236
Gauge—Discharge	281
Gauge—Discharge and Silt	41
Gauge—Discharge and water quality	80
Gauge—Discharge, water quality and Silt	239

In a few gauging stations on major rivers, moving boat method facilities exist. Reports containing the gauge, discharge, sediment and water quality data are brought out by CWC every year as *Year books*. In addition to the above, the state governments maintain nearly 800 gauging stations. Further, in most of the states institutional arrangements exist for collection, processing and analysis of hydrometric and hydrometeorological data and publication of the same.

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REVISION QUESTIONS

4.1 Explain the various commonly used methods of measurement of stage of a river. Indicate for each method its specific advantage and the conditions under which one would use it.
4.2 What factors should be considered in selecting a site for a stream gauging station?
4.3 Explain the salient features of a current meter. Describe briefly the procedure of using a current meter for measuring velocity in a stream.
4.4 List the qualities of a good tracer for use in dilution technique of flow measurement.
4.5 Explain briefly the dilution method of flow measurement.
4.6 Explain the streamflow measurement by area-velocity method.
4.7 Describe briefly the moving boat method of stream flow measurement.
4.8 Describe the slope-area method of measurement of flood discharge in a stream.
4.9 Explain the procedure for obtaining the stage-discharge relationship of a stream by using the stage-discharge data from a site with permanent control.

4.10 Describe briefly:
  (a) Backwater effect on a rating curve.
  (b) Unsteady flow effect on a rating curve
4.11 Describe a procedure for extrapolating a rating curve of a stream.
4.12 Discuss the advantages and disadvantages of the following relative to the flow measurement by using current meters:
  (a) Electromagnetic method   (b) Ultrasound method
4.13 Explain briefly the important aspects relating to the following instruments
  (a) Float-gauge recorder   (b) Bubble gauge
  (c) Echo-depth recorder   (d) Current meter

PROBLEMS

4.1 The following data were collected during a stream-gauging operation in a river. Compute the discharge.

Distance from left water edge (m)	Depth (m)	Velocity (m/s)	
		at 0.2 d	at 0.8 d
0.0	0.0	0.0	0.0
1.5	1.3	0.6	0.4
3.0	2.5	0.9	0.6
4.5	1.7	0.7	0.5
6.0	1.0	0.6	0.4
7.5	0.4	0.4	0.3
9.0	0.0	0.0	0.0

4.2 The velocity distribution in a stream is usually approximated as $v/v_a = (y/a)^m$, where v and v_a are velocities at heights y and a above the bed respectively and m is a coefficient with a value between 1/5 to 1/8. (i) Obtain an expression for $v/\bar{v}$, where $\bar{v}$ is the mean velocity in terms of the depth of flow. (ii) If $m = 1/6$ show that (a) the measured velocity is equal to the mean velocity if the velocity is measured at 0.6 depth from the water surface and (b) $\bar{v} = \frac{1}{2}(v_{0.2} + v_{0.82})$, where $v_{0.2}$ and $v_{0.82}$ are the velocities measured at 0.2 and 0.82 depths below the water surface respectively.

4.3 The following are the data obtained in a stream-gauging operation. A current meter with a calibration equation $V = (0.32N + 0.032)$ m/s, where N = revolutions per second was used to measure the velocity at 0.6 depth. Using the mid-section method, calculate the discharge in the stream.

Distance from right bank (m)	0	2	4	6	9	12	15	18	20	22	23	24
Depth (m)	0	0.50	1.10	1.95	2.25	1.85	1.75	1.65	1.50	1.25	0.75	0
Number of revolutions	0	80	83	131	139	121	114	109	92	85	70	0
Observation Time (s)	0	180	120	120	120	120	120	120	120	120	150	0

4.4 In the moving-boat method of discharge measurement the magnitude (V_R) and direction (θ) of the velocity of the stream relative to the moving boat are measured. The depth of the stream is also simultaneously recorded. Estimate the discharge in a river that gave the following moving-boat data. Assume the mean velocity in a vertical to be 0.95 times the surface velocity measured by the instrument.

Section	V_R (m/s)	θ (degrees)	Depth (m)	Remark
0	—	—	—	Right bank.
1	1.75	55	1.8	
2	1.84	57	2.5	
3	2.00	60	3.5	θ is the angle made by V_R
4	2.28	64	3.8	with the boat direction
5	2.30	65	4.0	
6	2.20	63	3.8	The various sections are
7	2.00	60	3.0	spaced at a constant
8	1.84	57	2.5	distance of 75 m apart
9	1.70	54	2.0	
10	—	—	—	Left bank

4.5 The dilution method with the sudden-injection procedure was used to measure the discharge of a stream. The data of concentration measurements are given below. A fluorescent dye weighing 300 N used as a tracer was suddenly injected at station A at 07 h.

Time (h)	07	08	09	10	11	12	13	14	15	16	17	18
Concentration at station B in parts per 10^9 by weight	0	0	3.0	10.5	18.0	18.0	12.0	9.0	6.0	4.5	1.5	0

Estimate the stream discharge.

4.6 A 500 g/l solution of sodium dichromate was used as chemical tracer. It was dosed at a constant rate of 4 l/s and at a downstream section. The equilibrium concentration was, measured as 4 parts per million (ppm). Estimate the discharge in the stream.

4.7 A 200 g/l solution of common salt was discharged into a stream at a constant rate of 25 l/s. The background concentration of the salt in the stream water was found to be 10 ppm. At a downstream section where the solution was believed to have been completely mixed, the salt concentration was found to reach an equilibrium value of 45 ppm. Estimate the discharge in the stream.

4.8 It is proposed to adopt the dilution method of stream gauging for a river whose hydraulic properties at average flow are as follows: width = 45 m, depth = 2.0 m, discharge = 85 m³/s, Chezy coefficient = 20 to 30. Determine the safe mixing length that has to be adopted for this stream.

4.9 During a high flow water-surface elevations of a small stream were noted at two sections A and B, 10 km apart. These elevations and other salient hydraulic properties are given below.

Section	Water-surface elevation (m)	Area of cross-section (m²)	Hydraulic radius (m)	Remarks
A	104.771	73.293	2.733	A is upsteam of B
B	104.500	93.375	3.089	$n = 0.020$

The eddy loss coefficients of 0.3 for gradual expansion and 0.1 for gradual contraction are appropriate. Estimate the discharge in the stream.

4.10 A small stream has a trapezoidal cross section with base width of 12 m and side slope 2 horizontal: 1 vertical in a reach of 8 km. During a flood the high water levels record at the ends of the reach are as follows.

Section	Elevation of bed (m)	Water surface elevation (m)	Remarks
Upstream	100.20	102.70	Manning's $n = 0.030$
Downstream	98.60	101.30	

Estimate the discharge in the stream.

4.11 The stage-discharge data of a river are given below. Establish the stage-discharge relationship to predict the discharge for a given stage. Assume the value of stage for zero discharge as 35.00 m. (2) What is the correlation coefficient of the relationship established above? (3) Estimate the discharge corresponding to stage values of 42.50 m and 48.50 m respectively.

Stage (m)	Discharge (m³/s)	Stage (m)	Discharge (m³/s)
35.91	89	39.07	469
36.90	230	41.00	798
37.92	360	43.53	2800
44.40	3800	48.02	5900
45.40	4560	49.05	6800
46.43	5305	49.55	6900
		49.68	6950

4.12 Downstream of a main gauging station, an auxiliary gauge was installed and the following readings were obtained.

Main gauge (m)	Auxiliary gauge (m)	Discharge (m³/s)
121.00	120.50	300
121.00	119.50	580

What discharge is indicated when the main gauge reading is 121.00 m and the auxiliary gauge reads 120.10 m.

4.13 The following are the coordinates of a smooth curve drawn to best represent the stage-discharge data of a river.

Stage (m)	20.80	21.42	21.95	23.37	23.00	23.52	23.90
Discharge (m³/s)	100	200	300	400	600	800	1000

Determine the stage corresponding to zero discharge.

4.14 The stage discharge data of a river are given below. Establish a stage-discharge relationship to predict the stage for a known discharge. Assume the stage value for zero discharge as 20.50 m. Determine the stage of the river corresponding to a discharge of 2600 m³/s.

Stage (m)	Discharge (m³/s)	Stage (m)	Discharge (m³/s)
21.95	100	24.05	780
22.45	220	24.55	1010
22.80	295	24.85	1220
23.00	400	25.40	1300
23.40	490	25.15	1420
23.75	500	25.55	1550
23.65	640	25.90	1760

(**Hint:** Use Eq. 4.35)

4.15 During a flood the water surface at a section in a river was found to increase at a rate of 11.2 cm/h. The slope of the river is 1/3600 and the normal discharge for the river stage read from a steady-flow rating curve was 160 m^3/s . If the velocity of the flood wave can be assumed as 2.0 m/s, determine the actual discharge.

──────────┤ OBJECTIVE QUESTIONS ├──────────

4.1 The science and practice of water flow measurement is known as
   (a) Hypsometry   (b) Hydro-meteorology
   (c) Fluvimetry   (d) Hydrometry
4.2 The following is *not* a direct stream flow determination technique
   (a) Dilution method   (b) Ultrasonic method
   (c) Area-velocity method   (d) Slope-area method
4.3 A stilling well is required when the stage measurement is made by employing a
   (a) bubble gauge   (b) float gauge recorder
   (c) vertical staff gauge   (d) inclined staff gauge
4.4 In a river carrying a discharge of 142 m^3/s, the stage at a station *A* was 3.6 m and the water surface slope was 1 in 6000. If during a flood the stage at *A* was 3.6 m and the water surface slope was 1/3000, the flood discharge (in m^3/s) was approximately
   (a) 100   (b) 284   (c) 71   (d) 200
4.5 In a triangular channel the top width and depth of flow were 2.0 m and 0.9 m respectively. Velocity measurements on the centre line at 18 cm and 72 cm below water surface indicated velocities of 0.60 m/s and 0.40 m/s respectively. The discharge in the channel (in m^3/s) is
   (a) 0.90   (b) 1.80   (c) 0.45   (d) none of these.
4.6 In the moving-boat method of stream-flow measurement, the essential measurements are:
   (a) the velocity recorded by the current meter, the depths and the speed of the boat.
   (b) the velocity and direction of the current meter, the depths and the time interval between depth readings
   (c) the depth, time interval between readings, speed of the boat and velocity of the stream
   (d) the velocity and direction of the current meter and the speed of the boat.
4.7 Which of the following instruments in *not* connected with stream flow measurement
   (a) hygrometer   (b) Echo-depth recorder
   (c) Electro-magnetic flow meter   (d) Sounding weight
4.8 The surface velocity at any vertical section of a stream is
   (a) not of any use in stream flow measurement
   (b) smaller than the mean velocity in that vertical
   (c) larger than the mean velocity in that vertical section
   (d) equal to the velocity in that vertical at 0.6 times the depth.
4.9 If a gauging section is having shifting control due to backwater effects, then
   (a) a loop rating curve results
   (b) the section is useless for stream-gauging purposes
   (c) the discharge is determined by area-velocity methods
   (d) a secondary gauge downstream of the section is needed.
4.10 The stage discharge relation in a river during the passage of a flood wave is measured. If Q_R = discharge at a stage when the water surface was rising and Q_F = discharge at the same stage when the water surface was falling, then
   (a) $Q_F = Q_R$ (b) $Q_R > Q_F$
   (c) $Q_R < Q_F$ (d) Q_R/Q_F = constant at all stages

4.11 A large irrigation canal can be approximated as a wide rectangular channel and Manning's formula is applicable to describe the flow in it. If the gauge (G) is related to discharge (Q) as

$$Q = C_r(G - a)^\beta$$

where a = gauge height at zero discharge, the value of β is
 (a) 1.67   (b) 1.50   (c) 2.50   (d) 0.67

4.12 The dilution method of stream gauging is ideally suited for measuring discharges in
 (a) a large alluvial river
 (b) flood flow in a mountain stream
 (c) steady flow in a small turbulent stream
 (d) a stretch of a river having heavy industrial pollution loads.

4.13 A 400 g/l solution of common salt was discharged into a stream at a constant rate of 45 l/s. At a downstream section where the salt solution is known to have completely mixed with the stream flow the equilibrium concentration was read as 120 ppm. If a background concentration of 20 ppm is applicable, the discharge in the stream can be estimated to be, in m^3/s, as
 (a) 150   (b) 180   (c) 117   (d) 889

4.14 In the gulp method of stream gauging by dilution technique, 60 litres of chemical X with concentration of 250 g/litre is introduced suddenly in to the stream at a section. At a downstream monitoring section the concentration profile of chemical X that crossed the section was found to be a triangle with a base of 10 hours and a peak of 0.10 ppm. The discharge in the stream can be estimated to be about
 (a) 83 m^3/s   (b) 180 m^3/s   (c) 15000 m^3/s   (d) 833 m^3/s

4.15 The slope-area method is extensively used in
 (a) development of rating curve
 (b) estimation of flood discharge based on high-water marks
 (c) cases where shifting control exists.
 (d) cases where backwater effect is present.

4.16 For a given stream the rating curve applicable to a section is available. To determine the discharge in this stream, the following-data are needed
 (a) current meter readings at various verticals at the section
 (b) slope of the water surface at the section
 (c) stage at the section
 (d) surface velocity at various sections.

4.17 During a flood in a wide rectangular channel it is found that at a section the depth of flow increases by 50% and at this depth the water-surface slope is half its original value in a given interval of time. This marks an approximate change in the discharge of
 (a) –33%   (b) +39%   (c) +20%   (d) no change.

4.18 In a river the discharge was 173 m^3/s, the water surface slope was 1 in 6000 and the stage at the station X was 10.00 m. If during a flood, the stage at station X was 10.00 and the water surface slope was 1/2000, the flood discharge was approximately
 (a) 100 m^3/s   (b) 519 m^3/s   (c) 300 m^3/s   (d) 371 m^3/s

4.19 During a flood, the water surface at a section was found to decrease at a rate of 10 cm/h. The slope of the river is 1/3600. Assuming the velocity of the flood wave as 2 m/s, the actual discharge in the stream can be estimated as
 (a) 2.5% larger than the normal discharge
 (b) 5% smaller than the normal discharge
 (c) 2.5% smaller than the normal discharge
 (d) Same as the normal discharge
 where normal discharge is the discharge at a given stage under steady, uniform flow.

Chapter
5

RUNOFF

5.1 INTRODUCTION

Runoff means the draining or flowing off of precipitation from a catchment area through a surface channel. It thus represents the output from the catchment in a given unit of time.

Consider a catchment area receiving precipitation. For a given precipitation, the evapotranspiration, initial loss, infiltration and detention storage requirements will have to be first satisfied before the commencement of runoff. When these are satisfied, the excess precipitation moves over the land surfaces to reach smaller channels. This portion of the runoff is called *overland flow* and involves building up of a storage over the surface and draining off of the same. Usually the lengths and depths of overland flow are small and the flow is in the laminar regime. Flows from several small channels join bigger channels and flows from these in turn combine to form a larger stream, and so on, till the flow reaches the catchment outlet. The flow in this mode, where it travels all the time over the surface as overland flow and through the channels as open-channel flow and reaches the catchment outlet is called *surface runoff.*

A part of the precipitation that infilters moves laterally through upper crusts of the soil and returns to the surface at some location away from the point of entry into the soil. This component of runoff is known variously as *interflow, through flow, storm seepage, subsurface storm flow* or *quick return flow* (Fig. 5.1). The amount of interflow
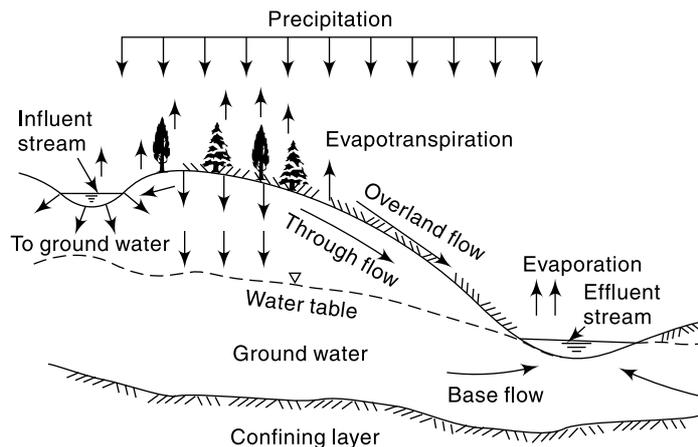
Fig. 5.1 Different routes of runoff

depends on the geological conditions of the catchment. A fairly pervious soil overlying a hard impermeable surface is conducive to large interflows. Depending upon the time delay between the infiltration and the outflow, the interflow is sometimes classified into *prompt interflow,* i.e. the interflow with the least time lag and *delayed interflow.*

Another route for the infiltered water is to undergo deep percolation and reach the groundwater storage in the soil. The groundwater follows a complicated and long path of travel and ultimately reaches the surface. The time lag, i.e. the difference in time between the entry into the soil and outflows from it is very large, being of the order of months and years. This part of runoff is called *groundwater runoff* or *groundwater flow.* Groundwater flow provides the dry-weather flow in perennial streams.

Based on the time delay between the precipitation and the runoff, the runoff is classified into two categories; as

1. Direct runoff, and   2. Base flow.

These are discussed below.

DIRECT RUNOFF

It is that part of the runoff which enters the stream immediately after the rainfall. It includes surface runoff, prompt interflow and rainfall on the surface of the stream. In the case of snow-melt, the resulting flow entering the stream is also a direct runoff. Sometimes terms such as *direct storm runoff* and *storm runoff* are used to designate direct runoff. Direct runoff hydrographs are studied in detail in Chapter 6.

BASE FLOW

The delayed flow that reaches a stream essentially as groundwater flow is called *base flow.* Many times delayed interflow is also included under this category. In the annual hydrograph of a perennial stream (Fig. 5.2) the base flow is easily recognized as the slowly decreasing flow of the stream in rainless periods. Aspects relating to the identification of base flow in a hydrograph are discussed in Chapter 6.

NATURAL FLOW

Runoff representing the response of a catchment to precipitation reflects the integrated effects of a wide range of catchment, climate and rainfall characteristics. True runoff is therefore stream flow in its natural condition, i.e. without human intervention. Such a stream flow unaffected by works of man, such as reservoirs and diversion structures on a stream, is called *natural flow* or *virgin flow.* When there exists storage or diversion works on a stream, the flow on the downstream channel is affected by the operational and hydraulic characteristics of these structures and hence does not represent the true runoff, unless corrected for the diversion of flow and return flow.

The natural flow (virgin flow) volume in time Δt at the terminal point of a catchment is expressed by water balance equation as

$$R_N = (R_o - V_r) + V_d + E + E_X + \Delta S \tag{5.1}$$

where R_N = Natural flow volume in time Δt
    R_o = Observed flow volume in time Δt at the terminal site
    V_r = Volume of return flow from irrigation, domestic water supply and industrial use
    V_d = Volume diverted out of the stream for irrigation, domestic water supply and industrial use

E = net evaporation losses from reservoirs on the stream

E_X = Net export of water from the basin

ΔS = Change in the storage volumes of water storage bodies on the stream

In hydrological studies, one develops relations for natural flows. However, natural flows have to be derived based on observed flows and data on abstractions from the stream. In practice, however, the observed stream flow at a site includes return flow and is influenced by upstream abstractions. As such, natural flows have to be derived based on observed flows and data on abstractions from the stream. Always, it is the natural flow that is used in all hydrological correlations. Example 5.1 explains these aspects clearly.

EXAMPLE 5.1 *The following table gives values of measured discharges at a stream–gauging site in a year. Upstream of the gauging site a weir built across the stream diverts 3.0 Mm³ and 0.50 Mm³ of water per month for irrigation and for use in an industry respectively. The return flows from the irrigation is estimated as 0.8 Mm³ and from the industry at 0.30 Mm³ reaching the stream upstream of the gauging site. Estimate the natural flow. If the catchment area is 180 km² and the average annual rainfall is 185 cm, determine the runoff-rainfall ratio.*

Month	1	2	3	4	5	6	7	8	9	10	11	12
Gauged flow (Mm³)	2.0	1.5	0.8	0.6	2.1	8.0	18.0	22.0	14.0	9.0	7.0	3.0

SOLUTION: In a month the natural flow volume R_N is obtained from Eq. (5.1) as

$$R_N = (R_o - V_r) + V_d + E + E_X + \Delta S$$

Here E, E_X and ΔS are assumed to be insignificant and of zero value.

V_r = Volume of return flow from irrigation, domestic water supply and industrial use = 0.80 + 0.30 = 1.10 Mm³

V_d = Volume diverted out of the stream for irrigation, domestic water supply and industrial use = 3.0 + 0.5 = 3.5 Mm³

The calculations are shown in the following Table:

Month	1	2	3	4	5	6	7	8	9	10	11	12
R_o(Mm³)	2.0	1.5	0.8	0.6	2.1	8.0	18.0	22.0	14.0	9.0	7.0	3.0
V_d(Mm³)	3.5	3.5	3.5	3.5	3.5	3.5	3.5	3.5	3.5	3.5	3.5	3.5
V_r(Mm³)	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1	1.1
R_N(Mm³)	4.4	3.9	3.2	3.0	4.5	10.4	20.4	24.4	16.4	11.4	9.4	5.4

Total R_N = 116.8 Mm³

Annual natural flow volume = Annual runoff volume = 116.8 Mm³

Area of the catchment = 180 km² = 1.80×10^8

Annual runoff depth = $\dfrac{1.168 \times 10^8}{1.80 \times 10^8}$ = 0.649 m = 64.9 cm

Annual rainfall = 185 cm   (Runoff/Rainfall) = 64.9/185 = 0.35

5.2   HYDROGRAPH

A plot of the discharge in a stream plotted against time chronologically is called a *hydrograph*. Depending upon the unit of time involved, we have

- Annual hydrographs showing the variation of daily or weekly or 10 daily mean flows over a year.
- Monthly hydrographs showing the variation of daily mean flows over a month.
- Seasonal hydrographs depicting the variation of the discharge in a particular season such as the monsoon season or dry season.
- Flood hydrographs or hydrographs due to a storm representing stream flow due to a storm over a catchment.

Each of these types have particular applications. Annual and seasonal hydrographs are of use in (i) calculating the surface water potential of stream, (ii) reservoir studies, and (iii) drought studies. Flood hydrographs are essential in analysing stream characteristics associated with floods. This chapter is concerned with the estimation and use of long-term runoffs. The study of storm hydrograph forms the subject matter of the next chapter.

Water Year

In annual runoff studies it is advantageous to consider a water year beginning from the time when the precipitation exceeds the average evapotranspiration losses. In India, June 1st is the beginning of a water year which ends on May 31st of the following calendar year. In a water year a complete cycle of climatic changes is expected and hence the water budget will have the least amount of carryover.

5.3   RUNOFF CHARACTERISTICS OF STREAMS

A study of the annual hydrographs of streams enables one to classify streams into three classes as (i) perennial, (ii) intermittent and (iii) ephemeral.

A perennial stream is one which always carries some flow (Fig. 5.2). There is considerable amount of groundwater flow throughout the year. Even during the dry seasons the water table will be above the bed of the stream.
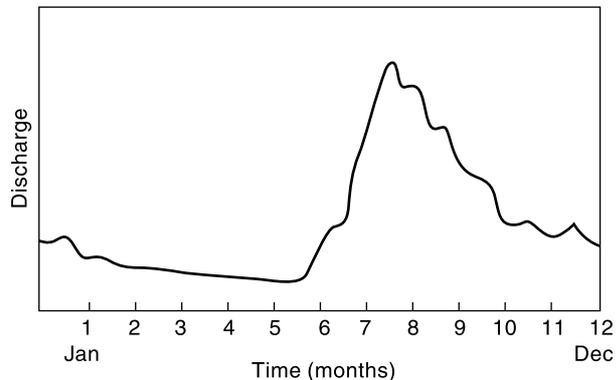
Fig. 5.2   Perennial stream

An intermittent stream has limited contribution from the groundwater. During the wet season the water table is above the stream bed and there is a contribution of the base flow to the stream flow. However, during dry seasons the water table drops to a level lower than that of the stream bed and the stream dries up. Excepting for an occasional storm which can produce a short-duration flow, the stream remains dry for the most part of the dry months (Fig. 5.3).

An ephemeral stream is one which does not have any base-flow contribution. The annual hydrograph of such a river shows series of short-duration spikes marking flash flows in response to storms (Fig. 5.4). The stream becomes dry soon after the end of
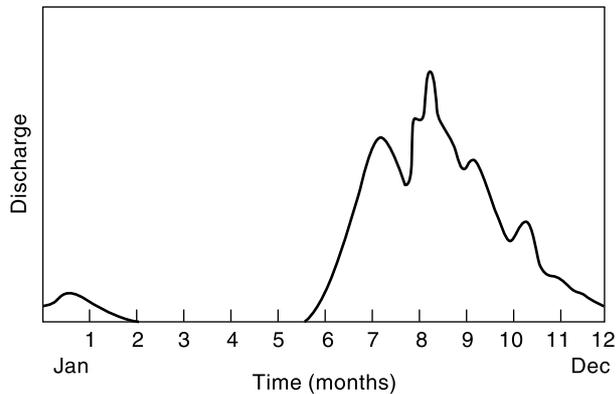
Fig. 5.3 Intermittent stream

the storm flow. Typically an ephemeral stream does not have any well-defined, channel. Most of the rivers in arid zones are of the ephemeral kind.

The flow characteristics of a stream depend upon:

Fig. 5.4 Ephemeral stream

- The rainfall characteristics, such as magnitude intensity, distribution according to time and space, and its variability.
- Catchment characteristics such as soil, land use/cover, slope, geology, shape and drainage density.
- Climatic factors which influence evapotranspiration.

The interrelationship of these factors is extremely complex. However, at the risk of oversimplification, the following points can be noted.

- The seasonal variation of rainfall is clearly reflected in the runoff. High stream discharges occur during the monsoon months and low flow which is essentially due to the base flow is maintained during the rest of the year.
- The shape of the stream hydrograph and hence the peak flow is essentially controlled by the storm and the physical characteristics of the basin. Evapotranspiration plays a minor role in this.
- The annual runoff volume of a stream is mainly controlled by the amount of rainfall and evapotranspiration. The geology of the basin is significant to the extent of deep percolation losses. The land use/cover play an important role in creating infiltration and evapotranspiration opportunities and retarding of runoff.
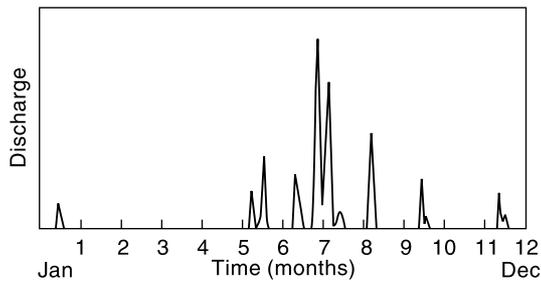
5.4   RUNOFF VOLUME

YIELD

The total quantity of surface water that can be expected in a given period from a stream at the outlet of its catchment is known as *yield* of the catchment in that period.

Depending upon the period chosen we have annual yield and seasonal yield signifying yield of the catchment in an year and in a specified season respectively. Unless otherwise qualified the term yield is usually used to represent annual yield. The term *yield* is used mostly by the irrigation engineering professionals in India.

The annual yield from a catchment is the end product of various processes such as precipitation, infiltration and evapotranspiration operating on the catchment. Due to the inherent nature of the various parameters involved in the processes, the yield is a random variable. A list of values of annual yield in a number of years constitutes an annual time series which can be analyzed by methods indicated in Chapter 2 (Sec. 2.11) to assign probabilities of occurrences of various events. A common practice is to assign a dependability value (say 75% dependable yield) to the yield. Thus, 75% dependable annual yield is the value that can be expected to be equalled to or exceeded 75% times (i.e. on an average 15 times in a span of 20 years). Similarly, 50% dependable yield is the annual yield value that is likely to be equalled or exceeded 50% of times (i.e. on an average 10 times in 20 years).

It should be remembered that the yield of a stream is always related to the natural flow in the river. However, when water is diverted from a stream for use in activities such as irrigation, domestic water supply and industries, the non-consumptive part of the diverted water returns back to the hydrologic system of the basin. Such additional flow, known as *return flow*, is available for the suitable use and as such is added to the natural flow to estimate the yield. (Details pertaining to the return flow are available in Sec. 5.9). The annual yield of a basin at a site is thus taken as the annual natural water flow in the river at the site plus the return flow to the stream from different uses upstream of the site.

The yield of a catchment Y in a period Δt could be expressed by water balance equation (Eq. 5.1) as

$$Y = R_N + V_r = R_o + A_b + \Delta S \tag{5.1a}$$

where R_N = Natural flow in time Δt

V_r = Volume of return flow from irrigation, domestic water supply and industrial use

R_o = Observed runoff volume at the terminal gauging station of the basin in time Δt.

A_b = Abstraction in time, Δt for irrigation, water supply and industrial use and inclusive of evaporation losses in surface water bodies on the stream.

ΔS = Change in the storage volumes of water storage bodies on the stream.

The calculation of natural runoff volume (and hence yield), is of fundamental importance in all surface water resources development studies. The most desirable basis for assessing the yield characteristics of a catchment is to analyze the actual flow records of the stream draining the catchment. However, in general, observed discharge data of sufficient length is unlikely to be available for many catchments. As such, other alternate methods such as the *empirical equations* and *watershed simulations* (described in Secs 5.4.3 to 5.4.5) are often adopted.

It should be noted that the observed stream flow at a site includes return flow. For small catchments and for catchments where water resources developments are at a small scale, the return flow is likely to be a negligibly small part of the runoff. In the further parts of this chapter the term annual (or seasonal) runoff volume R and the term annual (or seasonal) yield are used synonymously with the implied assumption

that the return flow is negligibly small. It is emphasized that when return flow is not negligible, it is the natural flow volume that is to be used in hydrological correlations with rainfall.

RAINFALL–RUNOFF CORRELATION

The relationship between rainfall in a period and the corresponding runoff is quite complex and is influenced by a host of factors relating to the catchment and climate. Further, there is the problem of paucity of data which forces one to adopt simple correlations for adequate estimation of runoff. One of the most common methods is to correlate seasonal or annual measured runoff values *(R)* with corresponding rainfall *(P)* values. A commonly adopted method is to fit a linear regression line between R and P and to accept the result if the correlation coefficient is nearer unity. The equation of the straight-line regression between runoff R and rainfall P is

$$R = aP + b \qquad (5.2)$$

and the values of the coefficient a and b are given by

$$a = \frac{N(\Sigma PR) - (\Sigma P)(\Sigma R)}{N(\Sigma P^2) - (\Sigma P)^2} \qquad (5.3a)$$

and
$$b = \frac{\Sigma R - a(\Sigma P)}{N} \qquad (5.3b)$$

in which N = number of observation sets R and P. The coefficient of correlation r can be calculated as

$$r = \frac{N(\Sigma PR) - (\Sigma P)(\Sigma R)}{\sqrt{[N(\Sigma P^2) - (\Sigma P)^2][N(\Sigma R^2) - (\Sigma R)^2]}} \qquad (5.4)$$

The value of r lies between 0 and 1 as R can have only positive correlation with P. The value of $0.6 < r < 1.0$ indicates good correlation. Further, it should be noted that $R \geq 0$.

For large catchments, sometimes it is found advantageous to have exponential relationship as

$$R = \beta P^m \qquad (5.5)$$

where β and m are constants, instead of the linear relationship given by Eq. (5.2). In that case Eq. (5.5) is reduced to linear form by logarithmic transformation as

$$\ln R = m \ln P + \ln \beta \qquad (5.6)$$

and the coefficients m and $\ln \beta$ are determined by using methods indicated earlier.

Since rainfall records of longer periods than that of runoff data are normally available for a catchment, the regression equation [Eq. (5.2) or (5.5)] can be used to generate synthetic runoff data by using rainfall data. While this may be adequate for preliminary studies, for accurate results sophisticated methods are adopted for synthetic generation of runoff data. Many improvements of the above basic rainfall-runoff correlation by considering additional parameters such as soil moisture and antecedent rainfall have been attempted. Antecedent rainfall influences the initial soil moisture and hence the infiltration rate at the start of the storm. For calculation of the annual runoff from the annual rainfall a commonly used antecedent precipitation index P_a is given by

$$P_a = aP_i + bP_{i-1} + cP_{i-2} \qquad (5.7)$$

where P_i, p_{i-1} and P_{i-2} are the annual precipitation in the ith, $(i-1)^{th}$ and $(i-2)^{th}$ year and i = current year, a, b and c are the coefficients with their sum equal to unity. The coefficients are found by trial and error to produce best results. There are many other types of antecedent precipitation indices in use to account for antecedent soil moisture condition. For example, in $SCS-CN$ method (Sec. 5.4.5) the sum of past five-day rainfall is taken as the index of antecedent moisture condition.

EXAMPLE 5.2 *Annual rainfall and runoff values (in cm) of a catchment spanning a period of 21 years are given below. Analyze the data to (a) estimate the 75% and 50% dependable annual yield of the catchment and (b) to develop a linear correlation equation to estimate annual runoff volume for a given annual rainfall value.*

Year	Annual rainfall (cm)	Annual runoff (cm)	Year	Annual rainfall (cm)	Annual runoff (cm)
1975	118	54	1986	75	17
1976	98	45	1987	107	32
1977	112	51	1988	75	15
1978	97	41	1989	93	28
1979	84	21	1990	129	48
1980	91	32	1991	153	76
1981	138	66	1992	92	27
1982	89	25	1993	84	18
1983	104	42	1994	121	52
1984	80	11	1995	95	26
1985	97	32			

SOLUTION: (*a*) The annual runoff values are arranged in descending order of magnitude and a rank (*m*) is assigned for each value starting from the highest value (Table 5.1).

The exceedence probability p is calculated for each runoff value as $p = \dfrac{m}{N+1}$. In this m = rank number and N = number of data sets. (Note that in Table 5.1 three items have the same value of $R = 32$ cm and for this set p is calculated for the item having the highest value of m, i.e $m = 12$). For estimating 75% dependable yield, the value of $p = 0.75$ is read from Table 5.1 by linear interpolation between items having $p = 0.773$ and $p = 0.727$. By this method, the 75% dependable yield for the given annual yield time series is found to be $R_{75} = 23.0$ cm.

Similarly, the 50% dependable yield is obtained by linear interpolation between items having $p = 0.545$ and $p = 0.409$ as $R_{50} = 34.0$ cm.

(*b*) The correlation equation is written as $R = aP + b$

The coefficients of the best fit straight line for the data are obtained by the least square error method as mentioned in Table 5.1.

From the Table 5.1,

$$\Sigma P = 2132 \qquad \Sigma R = 759 \qquad \Sigma PR = 83838$$
$$\Sigma P^2 = 224992 \qquad \Sigma R^2 = 33413$$
$$(\Sigma P)^2 = 4545424 \qquad (\Sigma R)^2 = 576081 \qquad N = 21$$

By using Eq. (5.3-a)

$$a = \frac{N(\Sigma PR) - (\Sigma P)(\Sigma R)}{N(\Sigma P^2) - (\Sigma R)^2} = \frac{(21 \times 83838) - (2132)(759)}{(21 \times 224992) - (2132)^2} = 0.7938$$

Table 5.1 Calculations for Example 5.2

1	2	3	4	5	6	7	8	9
Year	P rainfall (cm)	R runoff (cm)	P^2	R^2	PR	rank, m	R (Sorted annual runoff) (cm)	Exceedence probability, p
1975	118	54	13924	2916	6372	1	76	0.045
1976	98	45	9604	2025	4410	2	66	0.091
1977	112	51	12544	2601	5712	3	54	0.136
1978	97	41	9409	1681	3977	4	52	0.182
1979	84	21	7056	441	1764	5	51	0.227
1980	91	32	8281	1024	2912	6	48	0.273
1981	138	66	19044	4356	9108	7	45	0.318
1982	89	25	7921	625	2225	8	42	0.364
1983	104	42	10816	1764	4368	9	41	0.409
1984	80	11	6400	121	880	10	32	
1985	97	32	9409	1024	3104	11	32	
1986	75	17	5625	289	1275	12	32	0.545
1987	107	32	11449	1024	3424	13	28	0.591
1988	75	15	5625	225	1125	14	27	0.636
1989	93	28	8649	784	2604	15	26	0.682
1990	129	48	16641	2304	6192	16	25	0.727
1991	153	76	23409	5776	11628	17	21	0.773
1992	92	27	8464	729	2484	18	18	0.818
1993	84	18	7056	324	1512	19	17	0.864
1994	121	52	14641	2704	6292	20	15	0.909
1995	95	26	9025	676	2470	21	11	0.955
SUM	2132	759	224992	33413	83838			

By Eq. (5.3-b)
$$b = \frac{\Sigma R - a(\Sigma P)}{N} = \frac{(759) - 0.7938 \times (2138)}{21} = -44.44$$
Hence the required annual rainfall–runoff relationship of the catchment is given by
$$R = 0.7938\,P - 44.44 \text{ with both } P \text{ and } R \text{ being in cm and } R \geq 0.$$
By Eq. (5.4) coefficient of correlation
$$r = \frac{N(\Sigma PR) - (\Sigma P)(\Sigma R)}{\sqrt{[N(\Sigma P^2) - (\Sigma P)^2][N(\Sigma R^2) - (\Sigma R)^2]}}$$
$$= \frac{(21 \times 83838 - (2132)(759)}{\sqrt{[(21 \times 224992) - (4545424)][(21 \times 33413) - (576081)]}} = 0.949$$

As the value of r is nearer to unity the correlation is very good. Figure 5.5 represents the data points and the best fit straight line.

EMPIRICAL EQUATIONS

The importance of estimating the water availability from the available hydrologic data for purposes of planning water-resource projects was recognised by engineers even in
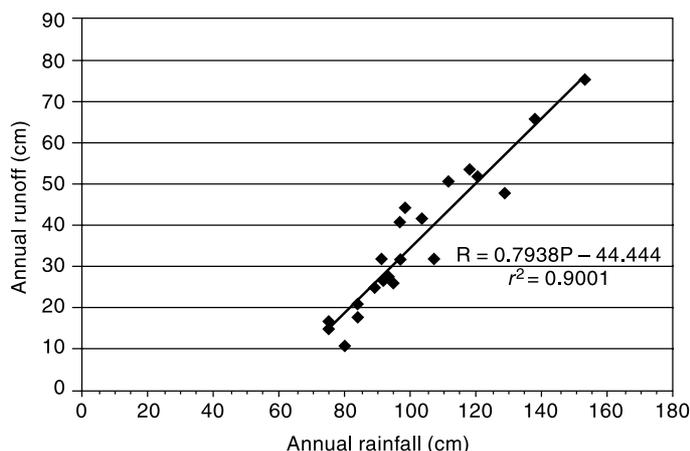
Fig. 5.5 Annual Rainfall–Runoff Correlation—Example 5.2

the last century. With a keen sense of observation in the region of their activity many engineers of the past have developed empirical runoff estimation formulae. However, these formulae are applicable only to the region in which they were derived. These formulae are essentially rainfall–runoff relations with additional third or fourth parameters to account for climatic or catchment characteristics. Some of the important formulae used in various parts of India are given below.

BINNIE'S PERCENTAGES   Sir Alexander Binnie measured the runoff from a small catchment near Nagpur (Area of 16 km^2) during 1869 and 1872 and developed curves of cumulative runoff against cumulative rainfall. The two curves were found to be similar. From these he established the percentages of runoff from rainfall. These percentages have been used in Madhya Pradesh and Vidarbha region of Maharashtra for the estimation of yield.

BARLOW'S TABLES   Barlow, the first Chief Engineer of the Hydro-Electric Survey of India (1915) on the basis of his study in small catchments (area ~130 km^2) in Uttar Pradesh expressed runoff R as

$$R = K_b P \tag{5.8}$$

where K_b = runoff coefficient which depends upon the type of catchment and nature of monsoon rainfall. Values of K_b are given in Table 5.2.

Table 5.2 Barlow's Runoff Coefficient K_b in Percentage (Developed for use in UP)

Class	Description of catchment	Values of K_b (percentage)		
		Season 1	Season 2	Season 3
A	Flat, cultivated and absorbent soils	7	10	15
B	Flat, partly cultivated, stiff soils	12	15	18
C	Average catchment	16	20	32
D	Hills and plains with little cultivation	28	35	60
E	Very hilly, steep and hardly any cultivation	36	45	81

Season 1: Light rain, no heavy downpour
Season 2: Average or varying rainfall, no continuous downpour
Season 3: Continuous downpour

STRANGE'S TABLES   Strange (1892) studied the available rainfall and runoff in the border areas of present-day Maharashtra and Karnataka and has obtained yield ratios as functions of indicators representing catchment characteristics. Catchments are classified as *good, average* and *bad* according to the relative magnitudes of yield they give. For example, catchments with good forest/vegetal cover and having soils of high permeability would be classified as *bad,* while catchments having soils of low permeability and having little or no vegetal cover is termed *good.* Two methods using tables for estimating the runoff volume in a season are given.

1. Runoff Volume from Total Monsoon Season Rainfall   A table giving the runoff volumes for the monsoon period (i.e. yield during monsoon season) for different total monsoon rainfall values and for the three classes of catchments (viz. *good, average and bad)* are given in Table 5.3-a. The correlation equations of best fitting lines relating percentage yield ratio (Y_r) to precipitation (P) could be expressed as

Table 5.3(a) Strange's Table of Total Mansoon Rainfall and estimated Runoff

Total Monsoon rainfall (inches)	Total Monsoon rainfall (mm)	Percentage of Runoff to rainfall			Total Monsoon rainfall (inches)	Total Monsoon rainfall (mm)	Percentage of Runoff to rainfall		
		Good catchment	Average catchment	Bad catchment			Good catchment	Average catchment	Bad catchment
1.0	25.4	0.1	0.1	0.1	31.0	787.4	27.4	20.5	13.7
2.0	50.8	0.2	0.2	0.1	32.0	812.8	28.5	21.3	14.2
3.0	76.2	0.4	0.3	0.2	33.0	838.2	29.6	22.2	14.8
4.0	101.6	0.7	0.5	0.3	34.0	863.6	30.8	23.1	15.4
5.0	127.0	1.0	0.7	0.5	35.0	889.0	31.9	23.9	15.9
6.0	152.4	1.5	1.1	0.7	36.0	914.4	33.0	24.7	16.5
7.0	177.8	2.1	1.5	1.0	37.0	939.8	34.1	25.5	17.0
8.0	203.2	2.8	2.1	1.4	38.0	965.2	35.3	26.4	17.6
9.0	228.6	3.5	2.6	1.7	39.0	990.6	36.4	27.3	18.2
10.0	254.0	4.3	3.2	2.1	40.0	1016.0	37.5	28.1	18.7
11.0	279.4	5.2	3.9	2.6	41.0	1 041.4	38.6	28.9	19.3
12.0	304.8	6.2	4.6	3.1	42.0	1066.8	39.8	29.8	19.9
13.0	330.2	7.2	5.4	3.6	43.0	1092.2	40.9	30.6	20.4
14.0	355.6	8.3	6.2	4.1	44.0	1117.6	42.0	31.5	21.0
15.0	381.0	9.4	7.0	4.7	45.0	1143.0	43.1	32.3	21.5
16.0	406.4	10.5	7.8	5.2	46.0	1168.4	44.3	33.2	22.1
17.0	431.8	11.6	8.7	5.8	47.0	1193.8	45.4	34.0	22.7
18.0	457.2	12.8	9.6	6.4	48.0	1219.2	46.5	34.8	23.2
19.0	482.6	13.9	10.4	6.9	49.0	1244.6	47.6	35.7	23.8
20.0	508.0	15.0	11.3	7.5	50.0	1270.0	48.8	36.6	24.4
21.0	533.4	16.1	12.0	8.0	51.0	1295.4	49.9	37.4	24.9
22.0	558.8	17.3	12.9	8.6	52.0	1320.8	51.0	38.2	25.5
23.0	584.2	18.4	13.8	9.2	53.0	1346.2	52.1	39.0	26.0
24.0	609.6	19.5	14.6	9.7	54.0	1371.6	53.3	39.9	26.6

(Contd.)

(*Contd.*)

25.0	635.0	20.6	15.4	10.3	55.0	1397.0	54.4	40.8	27.2
26.0	660.4	21.8	16.3	10.9	56.0	1422.4	55.5	41.6	27.7
27.0	685.8	22.9	17.1	11.4	57.0	1447.8	56.6	42.4	28.3
28.0	711.2	24.0	18.0	12.0	58.0	1473.2	57.8	43.3	28.9
29.0	736.6	25.1	18.8	12.5	59.0	1498.6	58.9	44.4	29.41
30.0	762.0	26.3	19.7	13.1	60.0	1524.0	60.0	45.0	30.0

For *Good* catchment:

For $P < 250$ mm, $Y_r = 7 \times 10^{-5} P^2 - 0.0003\ P$ having $r^2 = 0.9994$ (5.9a)

For $250 < P < 760$ $Y_r = 0.0438\ P - 7.1671$ having $r^2 = 0.9997$ (5.9b)

For $760 < P < 1500$ $Y_r = 0.0443\ P - 7.479$ having $r^2 = 1.0$ (5.9c)

For *Average* catchment:

For $P < 250$ mm, $Y_r = 6 \times 10^{-5} P^2 - 0.0022\ P + 0.1183$

having $r^2 = 0.9989$ (5.10a)

For $250 < P < 760$ $Y_r = 0.0328\ P - 5.3933$ having $r^2 = 0.9997$ (5.10b)

For $760 < P < 1500$ $Y_r = 0.0333\ P - 5.7101$ having $r^2 = 0.9999$ (5.10c)

For *Bad* catchment:

For $P < 250$ mm, $Y_r = 4 \times 10^{-5} P^2 - 0.0011\ P + 0.0567$

having $r^2 = 0.9985$ (5.11a)

For $250 < P < 760$ $Y_r = 0.0219\ P - 3.5918$ having $r^2 = 0.9997$ (5.11b)

For $760 < P < 1500$ $Y_r = 0.0221\ P - 3.771$ having $r^2 = 1.0$ (5.11c)

where Y_r = Percentage yield ratio = ratio of seasonal runoff to seasonal rainfall in percentage and P = monsoon season rainfall in mm.

Since there is no appreciable runoff due to the rains in the dry (non-monsoon) period, the monsoon season runoff volume is recommended to be taken as annual yield of the catchment. This table could be used to estimate the monthly yields also in the monsoon season. However, it is to be used with the understanding that the table indicates relationship between cumulative monthly rainfall starting at the beginning of the season and cumulative runoff, i.e. a *double mass curve* relationship.

Example 5.3 illustrates this procedure.

2. Estimating the Runoff Volume from Daily Rainfall   In this method Strange in a most intuitive way recognizes the role of antecedent moisture in modifying the runoff volume due to a rainfall event in a given catchment. Daily rainfall events are considered and three states of antecedent moisture conditions prior to the rainfall event as *dry, damp* and *wet* are recognized. The classification of these three states is as follows:

Wetting Process
  (a) **Transition from Dry to Damp**
       (i) 6 mm rainfall in the last 1 day   (iii) 25 mm in the last 7 days
       (ii) 12 mm in the last 3 days   (iv) 38 mm in the last 10 days
  (b) **Transition from Damp to Wet**
       (i) 8 mm rainfall in the last 1 day   (iii) 25 mm in the last 3 days
       (ii) 12 mm in the last 2 days   (iv) 38 mm in the last 5 days
  (c) **Direct Transition from Dry to Wet**
       Whenever 64 mm rain falls on the *previous* day or on the *same* day.

Drying Process

(d) **Transition from Wet to Damp**

    (i) 4 mm rainfall in the last 1 day   (iii) 12 mm in the last 4 days

    (ii) 6 mm in the last 2 days   (iv) 20 mm in the last 5 days

(e) **Transition from Damp to Dry**

    (i) 3 mm rainfall in the last 1 day   (iii) 12 mm in the last 7 days

    (ii) 6 mm in the last 3 days   (iv) 15 mm in the last 10 days

The percentage daily rainfall that will result in runoff for *average* (yield producing) catchment is given in Table 5.3(b). For *good* (yield producing) and *bad* (yield producing) catchments *add* or *deduct* 25% of the yield corresponding to the *average* catchment.

Table 5.3(b) Strange's Table of Runoff Volume from Daily Rainfall for an *Average* Catchment

Daily rainfall (mm)	Percentage of runoff volume to daily rainfall when original state of the ground was		
	Dry	**Damp**	**Wet**
6	—	—	8
13	—	6	12
19	—	8	16
25	3	11	18
32	5	14	22
38	6	16	25
45	8	19	30
51	10	22	34
64	15	29	43
76	20	37	55
102	30	50	70

Best fitting linear equations for the above table would read as below with K_s = runoff volume percentage and P = daily rainfall (mm):

For Dry AMC: $K_s = 0.5065\ P - 2.3716$ for $P > 20$ mm   (5.12a)

            with coefficient of determination $r^2 = 0.9947$

For Damp AMC: $K_s = 0.3259\ P - 5.1079$ for $P > 7$ mm   (5.12b)

            with coefficient of determination $r^2 = 0.9261$

For Wet AMC: $K_s = 0.6601\ P + 2.0643$ (5.12c)

            with coefficient of determination $r^2 = 0.9926$

Use of Strange's Tables   Strange's monsoon rainfall-runoff table (Table 5.3-a) and Table (5.3-b) for estimating daily runoff corresponding to a daily rainfall event are in use in parts of Karnataka, Andhra Pradesh and Tamil Nadu. A calculation procedure using Table (5.3-a) to calculate monthly runoff volumes in a monsoon season using cumulative monthly rainfalls is shown in Example 5.3.

EXAMPLE 5.3 *Monthly rainfall values of the 50% dependable year at a site selected for construction of an irrigation tank is given below. Estimate the monthly and annual runoff volume of this catchment of area 1500 ha.*
[Assume the catchment classification as Good catchment].

Month	June	July	Aug	Sept	Oct
Monthly rainfall (mm)	90	160	145	22	240

SOLUTION: Calculations are shown in the Table 5.4 given below.

Table 5.4 Calculation of Monthly Yields by Strange's Method — Example 5.3

No.	Month	June	July	August	September	October
1.	Monthly Rainfall (mm)	90	160	145	22	240
2.	Cumulative monthly rainfall (mm)	90	250	395	417	657
3.	Runoff/rainfall as % (From Strange's Table 5.3-a)	0.56	4.17	10.01	11.08	21.69
4.	Cumulative Runoff (mm)	0.50	10.43	39.54	46.20	142.50
5.	Monthly Runoff (mm)	0.50	9.92	29.11	6.66	96.30

Row 4 is obtained by using Strange's Tables 5.3. Note that cumulative monthly rainfall is used to get the cumulative runoff-ratio percentage at any month.

Total monsoon runoff $= 142.50$ mm $= (142.5/1000) \times (1500 \times 10^4)/10^6$ Mm^3
$= 2.1375$ Mm^3

Annual Runoff is taken as equal to monsoon runoff.

INGLIS AND DESOUZA FORMULA   As a result of careful stream gauging in 53 sites in Western India, Inglis and DeSouza (1929) evolved two regional formulae between annual runoff R in cm and annual rainfall P in cm as follows:

1. For Ghat regions of western India

$$R = 0.85\, P - 30.5 \qquad\qquad (5.13)$$

2. For Deccan plateau

$$R = \frac{1}{254}\, P\,(P - 17.8) \qquad\qquad (5.14)$$

KHOSLA'S FORMULA   Khosla (1960) analysed the rainfall, runoff and temperature data for various catchments in India and USA to arrive at an empirical relationship between runoff and rainfall. The time period is taken as a month. His relationship for monthly runoff is

$$R_m = P_m - L_m \qquad\qquad (5.15)$$

and $\qquad L_m = 0.48\, T_m$ for $T_m > 4.5°$ C

where R_m = monthly runoff in cm and $R_m \geq 0$
$\qquad P_m$ = monthly rainfall in cm
$\qquad L_m$ = monthly losses in cm
$\qquad T_m$ = mean monthly temperature of the catchment in ° C

For $T_m \leq 4.5°$C, the loss L_m may provisionally be assumed as

$T°$C	4.5	−1	−6.5
L_m (cm)	2.17	1.78	1.52

Annual runoff $= \Sigma R_m$

Khosla's formula is indirectly based on the water-balance concept and the mean monthly catchment temperature is used to reflect the losses due to evapotranspiration. The formula has been tested on a number of catchments in India and is found to give fairly good results for the annual yield for use in preliminary studies.

EXAMPLE 5.4 For a catchment in UP, India, the mean monthly temperatures are given. Estimate the annual runoff and annual runoff coefficient by Khosla's method.

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
Temp°C	12	16	21	27	31	34	31	29	28	29	19	14
Rainfall (P_m)(cm)	4	4	2	0	2	12	32	29	16	2	1	2

SOLUTION: In Khosla's formula applicable to the present case, $R_m = P_m - L_m$ with $L_m = (0.48 \times T\ °C)$ having a maximum value equal to corresponding P_m. The calculations are shown below:

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
Rainfall (P_m)(cm)	4	4	2	0	2	12	32	29	16	2	1	2
Temp°C	12	16	21	27	31	34	31	29	28	29	19	14
L_m (cm)	4	4	2	0	2	12	14.9	13.9	13.4	2	1	2
Runoff (R_m)(cm)	0	0	0	0	0	0	17.1	15.1	2.6	0	0	0

Total annual runoff = 34.8 cm
Annual runoff coefficient = (Annual runoff/Annual rainfall) = (34.8/116.0) = 0.30

WATERSHED SIMULATION The hydrologic water-budget equation for the determination of runoff for a given period is written as

$$R = R_s + G_0 = P - E_{et} - \Delta S \tag{5.16}$$

in which R_s = surface runoff, P = precipitation, E_{et} = actual evapotranspiration, G_0 = net groundwater outflow and ΔS = change in the soil moisture storage. The sum of R_s and G_0 is considered to be given by the total runoff R, i.e. streamflow.

Starting from an initial set of values, one can use Eq. (5.16) to calculate R by knowing values of P and functional dependence of E_{et}, ΔS and infiltration rates with catchment and climatic conditions. For accurate results the functional dependence of various parameters governing the runoff in the catchment and values of P at short time intervals are needed. Calculations can then be done sequentially to obtain the runoff at any time. However, the calculation effort involved is enormous if attempted manually. With the availability of digital computers the use of water budgeting as above to determine the runoff has become feasible. This technique of predicting the runoff, which is the catchment response to a given rainfall input is called *deterministic watershed simulation.* In this the mathematical relationships describing the interdependence of various parameters in the system are first prepared and this is called the *model.* The model is then calibrated, i.e. the numerical values of various coefficients determined by simulating the known rainfall-runoff records. The accuracy of the model is further checked by reproducing the results of another string of rainfall data for which runoff values are

known. This phase is known as *validation* or *verification* of the model. After this, the model is ready for use.

Crawford and Linsley (1959) pioneered this technique by proposing a watershed simulation model known as the Stanford Watershed Model (SWM). This underwent successive refinements and the Stanford Watershed Model-IV (SWM-IV) suitable for use on a wide variety of conditions was proposed in 1966. The flow chart of SWM-IV is shown in Fig. 5.6. The main inputs are hourly precipitation and daily evapotranspiration in addition to physical description of the catchment. The model considers the soil in three zones with distinct properties to simulate evapotranspiration, infiltration, overland flow, channel flow, interflow and baseflow phases of the runoff phenomenon. For calibration about 5 years of data are needed. In the calibration phase, the initial guess value of parameters are adjusted on a trial-and-error basis until the simulated response matches the recorded values. Using an additional length of rainfall-runoff of about 5 years duration, the model is verified for its ability to give proper response. A detailed description of the application of SWM to an Indian catchment is given in Ref. 11.
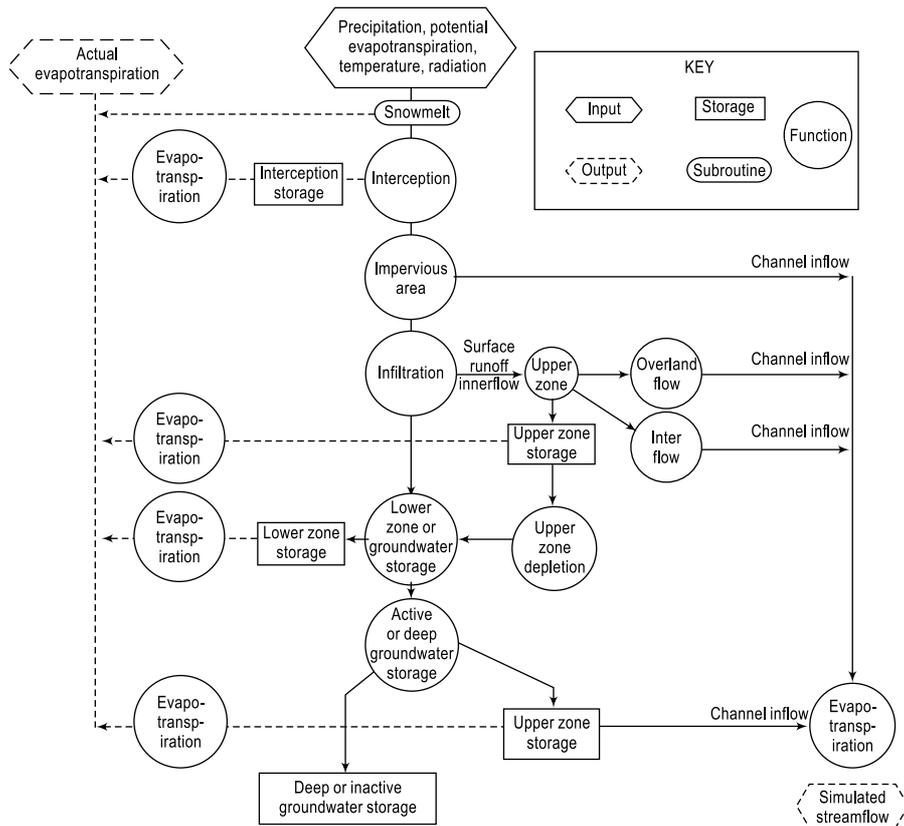
Fig. 5.6 Flow chart of SWM-IV

Based on the logic of SWM-IV many models and improved versions such as HSP (1966), SSARR (1968) and KWM (1970) were developed during late sixties and seventies. These models which simulate stream flow for long periods of time are called

Continuous Simulated Models. They permit generation of simulated long records for yield, drought and flood flow studies. In the early 1980s there were at least 75 hydrologic simulation models that were available and deemed suitable for small watersheds. In the past two decades considerable effort has been directed towards the development of process-based, spatially explicit, and physically-based models such as MIKE SHE (Refsgaard and Storm, 1955), and GSSHA—Gridded Surface/Subsurface Hydrologic Analysis (Downer et al., 2006). These are new generation of models that utilize GIS technology.

SCS-CN METHOD OF ESTIMATING RUNOFF VOLUME

SCS-CN method, developed by Soil Conservation Services (SCS) of USA in 1969, is a simple, predictable, and stable conceptual method for estimation of direct runoff depth based on storm rainfall depth. It relies on only one parameter, *CN*. Currently, it is a well-established method, having been widely accepted for use in USA and many other countries. The details of the method are described in this section.

BASIC THEORY   The *SCS-CN* method is based on the water balance equation of the rainfall in a known interval of time Δt, which can be expressed as

$$P = I_a + F + Q \tag{5.17}$$

where P = total precipitation, I_a = initial abstraction, F = Cumulative infiltration excluding I_a and Q = direct surface runoff (all in units of volume occurring in time Δt). Two other concepts as below are also used with Eq. (5.17).

(i) The first concept is that the ratio of actual amount of direct runoff (Q) to maximum potential runoff ($= P - I_a$) is equal to the ratio of actual infiltration (F) to the potential maximum retention (or infiltration), S. This proportionality concept can be schematically shown as in Fig. 5.7
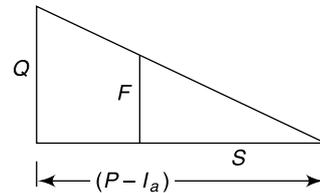
Fig. 5.7   Proportionality concept

Thus $\dfrac{Q}{P - I_a} = \dfrac{F}{S}$ (5.18)

(ii) The second concept is that the amount of initial abstraction (I_a) is some fraction of the potential maximum retention (S).
Thus $I_a = \lambda S$ (5.19)
Combining Eqs. (5.18) and (5.19), and using (5.17)

$$Q = \frac{(P - I_a)^2}{P - I_a + S} = \frac{(P - \lambda S)^2}{P + (1 - \lambda) S} \quad \text{for } P > \lambda S \tag{5.20a}$$

Further $Q = 0$ for $P \le \lambda S$ (5.20b)

For operation purposes a time interval $\Delta t = 1$ day is adopted. Thus P = daily rainfall and Q = daily runoff from the catchment.

CURVE NUMBER (CN)   The parameter S representing the potential maximum retention depends upon the soil–vegetation–land use complex of the catchment and also upon the antecedent soil moisture condition in the catchment just prior to the commencement of the rainfall event. For convenience in practical application the Soil Conservation Services (SCS) of USA has expressed S (in mm) in terms of a dimensionless parameter CN (the Curve number) as

$$S = \frac{25400}{CN} - 254 = 254\left(\frac{100}{CN} - 1\right) \tag{5.21}$$

The constant 254 is used to express S in mm.

The curve number CN is now related to S as

$$CN = \frac{25400}{S + 254} \tag{5.22}$$

and has a range of $100 \geq CN \geq 0$. A CN value of 100 represents a condition of zero potential retention (i.e. impervious catchment) and $CN = 0$ represents an infinitely abstracting catchment with $S = \infty$. This curve number CN depends upon

- Soil type
- Land use/cover
- Antecedent moisture condition

SOILS In the determination of CN, the hydrological soil classification is adopted. Here, soils are classified into four classes A, B, C and D based upon the infiltration and other characteristics. The important soil characteristics that influence hydrological classification of soils are effective depth of soil, average clay content, infiltration characteristics and permeability. Following is a brief description of four hydrologic soil groups:

- **Group-A**: **(Low Runoff Potential)**: Soils having high infiltration rates even when thoroughly wetted and consisting chiefly of deep, well to excessively drained sands or gravels. These soils have high rate of water transmission. [Example: Deep sand, Deep loess and Aggregated silt]
- **Group-B: (Moderately Low runoff Potential)**: Soils having moderate infiltration rates when thoroughly wetted and consisting chiefly of moderately deep to deep, moderately well to well-drained soils with moderately fine to moderately coarse textures. These soils have moderate rate of water transmission. [Example: Shallow loess, Sandy loam, Red loamy soil, Red sandy loam and Red sandy soil]
- **Group-C: (Moderately High Runoff Potential)**: Soils having low infiltration rates when thoroughly wetted and consisting chiefly of moderately deep to deep, moderately well to well drained soils with moderately fine to moderately coarse textures. These soils have moderate rate of water transmission. [Example: Clayey loam, Shallow sandy loam, Soils usually high in clay, Mixed red and black soils]
- **Group-D: (High Runoff Potential)**: Soils having very low infiltration rates when thoroughly wetted and consisting chiefly of clay soils with a high swelling potential, soils with a permanent high-water table, soils with a clay pan, or clay layer at or near the surface, and shallow soils over nearly impervious material. [Example: Heavy plastic clays, certain saline soils and deep black soils].

ANTECEDENT MOISTURE CONDITION (AMC) Antecedent Moisture Condition (AMC) refers to the moisture content present in the soil at the beginning of the rainfall-runoff event under consideration. It is well known that initial abstraction and infiltration are governed by AMC. For purposes of practical application three levels of AMC are recognized by SCS as follows:

AMC-I: Soils are dry but not to wilting point. Satisfactory cultivation has taken place.

AMC-II: Average conditions

AMC-III: Sufficient rainfall has occurred within the immediate past 5 days. Saturated soil conditions prevail.

The limits of these three AMC classes, based on total rainfall magnitude in the previous 5 days, are given in Table 5.5. It is to be noted that the limits also depend upon the seasons: two seasons, viz. growing season and dormant season are considered.

Table 5.5 Antecedent Moisture Conditions (AMC) for Determining the Value of CN

AMC Type	Total Rain in Previous 5 days	
	Dormant Season	Growing Season
I	Less than 13 mm	Less than 36 mm
II	13 to 28 mm	36 to 53 mm
III	More than 28 mm	More than 53 mm

LAND USE The variation of *CN* under AMC-II, called CN_{II}, for various land use conditions commonly found in practice are shown in Table 5.6(a, b and c).

Table 5.6(a) Runoff Curve Numbers [CN_{II}] for Hydrologic Soil Cover Complexes [Under AMC-II Conditions]

Land Use	Cover		Hydrologic soil group			
	Treatment or practice	Hydrologic condition	A	B	C	D
Cultivated	Straight row		76	86	90	93
Cultivated	Contoured	Poor	70	79	84	88
		Good	65	75	82	86
Cultivated	Contoured &	Poor	66	74	80	82
	Terraced	Good	62	71	77	81
Cultivated	Bunded	Poor	67	75	81	83
		Good	59	69	76	79
Cultivated	Paddy		95	95	95	95
Orchards	With understory cover		39	53	67	71
	Without understory cover		41	55	69	73
Forest	Dense		26	40	58	61
	Open		28	44	60	64
	Scrub		33	47	64	67
Pasture	Poor		68	79	86	89
	Fair		49	69	79	84
	Good		39	61	74	80
Wasteland			71	80	85	88
Roads (dirt)			73	83	88	90
Hard surface areas			77	86	91	93

[Source: Ref.7]

Note: Sugarcane has a separate supplementary Table of CN_{II} values (Table 5.6(b)).

The conversion of CN_{II} to other two AMC conditions can be made through the use of following correlation equations.[10]

For AMC-I: $$CN_I = \frac{CN_{II}}{2.281 - 0.01281\, CN_{II}}$$ (5.23)

Table 5.6(b) CN_{II} Values for Sugarcane

[Source: Ref.7]

Cover and treatment	Hydrologic soil group			
	A	B	C	D
Limited cover, Straight Row	67	78	85	89
Partial cover, Straight row	49	69	79	84
Complete cover, Straight row	39	61	74	80
Limited cover, Contoured	65	75	82	86
Partial cover, Contoured	25	59	45	83
Complete cover, Contoured	6	35	70	79

Table 5.6(c) CN_{II} Values for Suburban and Urban Land Uses (Ref. 3)

Cover and treatment	Hydrologic soil group			
	A	B	C	D
Open spaces, lawns, parks etc				
(i) In good condition, grass cover in more than 75% area	39	61	74	80
(ii) In fair condition, grass cover on 50 to 75% area	49	69	79	84
Commercial and business areas (85% impervious)	89	92	94	95
Industrial Districts (72% impervious)	81	88	91	93
Residential, average 65% impervious	77	85	90	92
Paved parking lots, paved roads with curbs, roofs, driveways, etc	98	98	98	98
Streets and roads				
Gravel	76	85	89	91
Dirt	72	82	87	89

For AMC-III:
$$CN_{III} = \frac{CN_{II}}{0.427 + 0.00573 \, CN_{II}} \tag{5.24}$$

The equations (5.23) and (5.24) are applicable in the CN_{II}, range of 55 to 95 which covers most of the practical range. Values of CN_I, and CN_{III} covering the full range of CN_{II} are available in Refs 3 and 7. Procedures for evaluation of CN from data on small watersheds are available in Ref. 7.

VALUE OF λ   On the basis of extensive measurements in small size catchments SCS (1985) adopted $\lambda = 0.2$ as a standard value. With this Eq. (5.20-a) becomes

$$Q = \frac{(P - 0.2\,S)^2}{P + 0.8\,S} \quad \text{for } P > 0.2S \tag{5.25}$$

where Q = daily runoff, P = daily rainfall and S = retention parameter, all in units of mm. Equation 5.25, which is well established, is called as the *Standard SCS-CN equation.*

SCS-CN EQUATION FOR INDIAN CONDITIONS   Values of λ varying in the range $0.1 \leq \lambda \leq 0.4$ have been documented in a number of studies from various geographical locations, which include USA and many other countries. For use in Indian conditions $\lambda = 0.1$ and 0.3 subject to certain constraints of soil type and AMC type has been recommended (Ref. 7) as below:

$$Q = \frac{(P - 0.1\,S)^2}{P + 0.9\,S} \quad \text{for } P > 0.1\,S,$$

valid *for Black soils under AMC of Type II and III* $\qquad$ (5.26)

$$Q = \frac{(P - 0.3\,S)^2}{P + 0.7\,S} \quad \text{for } P > 0.3S \text{ valid } \textit{for Black soils under}$$

AMC of Type 1 and for all other soils having AMC

of types I, II and III $\qquad$ (5.27)

These Eqs. (5.26 & 5.27) along with Table 5.6 (a & b) are recommended (Ref. 7) for use in Indian conditions in place of the Standard SCN-CN equation.

PROCEDURE FOR ESTIMATING RUNOFF VOLUME FROM A CATCHMENT

(i) Land use/cover information of the catchment under study is derived based on interpretation of multi-season satellite images. It is highly advantageous if the GIS database of the catchment is prepared and land use/cover data is linked to it.

(ii) The soil information of the catchment is obtained by using soil maps prepared by National Bureau of Soil Survey and Land use planning (NBSS & LUP) (1966). Soil data relevant to the catchment is identified and appropriate hydrological soil classification is made and the spatial form of this data is stored in GIS database.

(iii) Available rainfall data of various rain gauge stations in and around the catchment is collected, screened for consistency and accuracy and linked to the GIS database. For reasonable estimate of catchment yield it is desirable to have a rainfall record of at least 25 years duration.

(iv) Thiessen polygons are established for each identified rain gauge station.

(v) For each Thiessen cell, appropriate area weighted CN_{II} value is established by adequate consideration of spatial variation of land use and/cover and soil types. Further, for each cell, corresponding CN_I and CN_{III} values are determined by using Eqs. (5.23) and (5.24).

(vi) Using the relevant *SCS-CN* equations sequentially with the rainfall data, the corresponding daily runoff series is derived for each cell. From this the needed weekly/monthly/annual runoff time series is derived. Further, by combining the results of various cells constituting the catchment, the corres-ponding catchment runoff time series is obtained.

(vii) Appropriate summing of the above time series, yields seasonal/annual runoff volume series and from this the desired dependable catchment yield can be estimated.

CURRENT STATUS OF SCS-CN METHOD   The *SCS-CN* method has received considerable applications and research study since its introduction in 1969. Recently, Ponce and Hawkins[10] (1996) have critically examined the method, clarified its capabilities, limitations and uses. There is a growing body of literature on this method and a good bibliography on this subject is available in Ref. 10. The chief advantages of *SCS-CN* method can be summed up as:

- It is a simple, predictable, and stable conceptual method for estimation of direct runoff depth based on storm rainfall depth, supported by empirical data.
- It relies on only one parameter, *CN*. Even though *CN* can have a theoretical range of 0–100, in practice it is more likely to be in the range 40–98.

- It features readily grasped and reasonably well-documented environmental inputs.
- It is a well-established method, having been widely accepted for use in USA and many other countries. The modifications suggested by the Ministry of Agriculture, Govt. of India [7], (1972), make its use effective for Indian conditions.

EXAMPLE 5.5 *In a 350 ha watershed the CN value was assessed as 70 for AMC-III. (a) Estimate the value of direct runoff volume for the following 4 days of rainfall. The AMC on July 1st was of category III. Use standard SCS-CN equations.*

Date	July 1	July 2	July 3	July 4
Rainfall (mm)	50	20	30	18

(b) *What would be the runoff volume if the CN_{III} value were 80?*

SOLUTION:

(a) Given $CN_{III} = 70$ $S = (25400/70) - 254 = 108.6$

$$Q = \frac{(P - 0.2\,S)^2}{P + 0.8\,S} \quad \text{for } P > 0.2S$$

$$= \frac{[P - (0.2 \times 108.86)^2]}{P + (0.8 \times 108.86)} = \frac{[P - 21.78]^2}{P + 87.09} \quad \text{for } P > 21.78 \text{ mm}$$

Date	P (mm)	Q (mm)
July 1	50	5.81
July 2	20	0
July 3	30	0.58
July 4	18	0
Total	**118**	**6.39**

Total runoff volume over the catchment $V_r = 350 \times 10^4 \times 6.39/(1000)$
$$= \textbf{22,365 m}^3$$

(b) Given $CN_{III} = 80$ $S = (25400/80) - 254 = 63.5$

$$Q = \frac{(P - 0.2\,S)^2}{P + 0.8\,S} \quad \text{for } P > 0.2\ S$$

$$= \frac{[P - (0.2 \times 63.5)]^2}{P + (0.8 \times 63.5)} = \frac{[P - 12.7]^2}{P + 50.8} \quad \text{for } P > 12.7 \text{ mm}$$

Date	P (mm)	Q (mm)
July 1	50	13.80
July 2	20	0.75
July 3	30	3.70
July 4	18	0.41
Total	**118**	**18.66**

Total runoff volume over the catchment $V_r = 350 \times 10^4 \times 18.66/(1000)$
$$= \textbf{65,310 m}^3$$

EXAMPLE 5.6 *A small watershed is 250 ha in size has group C soil. The land cover can be classified as 30% open forest and 70% poor quality pasture. Assuming AMC at average condition and the soil to be black soil, estimate the direct runoff volume due to a rainfall of 75 mm in one day.*

SOLUTION: AMC = II. Hence $CN = CN(\text{II})$. Soil = Black soil. Referring to Table (5.6-a) for C-group soil

Land use	%	CN	Product
Open forest	30	60	1800
Pasture (poor)	70	86	6020
Total	**100**		**7820**

Average $\quad CN = 7820/100 = 78.2 \qquad S = (25400/78.2) - 254 = 70.81$
The relevant runoff equation for Black soil and *AMC*-II is

$$Q = \frac{(P - 0.1S)^2}{P + 0.9S} = \frac{[75 - (0.1 \times 70.81)]^2}{75 + (0.9 \times 70.81)} = 33.25 \text{ mm}$$

Total runoff volume over the catchment $V_r = 250 \times 10^4 \times 33.25/(1000) = \textbf{83,125 m}^3$

EXAMPLE 5.7 *The land use and soil characteristics of a 5000 ha watershed are as follows:*
Soil: Not a black soil. Hydrologic soil classification: 60% is Group B and 40% is Group C
Land Use:

$$\text{Hard surface areas} = 10\%$$
$$\text{Waste Land} = 5\%$$
$$\text{Orchard (without understory cover)} = 30\%$$
$$\text{Cultivated (Terraced), poor condition} = 55\%$$

Antecedent rain: The total rainfall in past five days was 30 mm. The season is dormant season.

(a) *Compute the runoff volume from a 125 mm rainfall in a day on the watershed*
(b) *What would have been the runoff if the rainfall in the previous 5 days was 10 mm?*
(c) *If the entire area is urbanized with 60% residential area (65% average impervious area), 10% of paved streets and 30% commercial and business area (85% impervious), estimate the runoff volume under AMC-II condition for one day rainfall of 125 mm.*

SOLUTION:

(a) Calculation of weighted *CN*
From Table 5.5 *AMC* = Type III. Using Table (5.6-a) weighted CN_{II} is calculated as below:

Land use	Total (%)	Soil Group B (60%)			Soil Group C (40%)		
		%	CN	Product	%	CN	Product
Hard surface	10	6	86	516	4	91	364
Waste land	5	3	80	240	2	85	170
Orchard	30	18	55	990	12	69	828
Cultivated land	55	33	71	2343	22	77	1694
Total				**4089**			**3056**

$$\text{Weighted } CN = \frac{(4089 + 3056)}{100} = 71.45$$

$$\text{By Eq. (5.24) } CN_{\text{III}} = \frac{71.45}{0.427 + (0.00573 \times 71.45)} = 85.42$$

Since the soil is not a black soil, Eq. (5.27) is used to compute the surface runoff.

$$Q = \frac{(P - 0.3S)^2}{P + 0.7S} \quad \text{for } P > 0.3S \text{ and}$$

$$S = \frac{25400}{CN} - 254 = (25400/85.42) - 254 = 43.35$$

$$Q = \frac{[125 - (0.3 \times 43.35)]^2}{125 + (0.7 \times 43.35)} = 80.74 \text{ mm}$$

Total runoff volume over the catchment $V_r = 5000 \times 10^4 \times 80.74/(1000)$
$$= \textbf{4,037,000 m}^3 = \textbf{4.037 Mm}^3$$

(b) Here AMC = Type I

$$\text{Hence} \qquad CN_{\text{I}} = \frac{71.45}{2.281 - (0.01281 \times 71.45)} = 52.32$$

$$S = (25400/52.32) - 254 = 231.47$$

$$Q = \frac{[125 - (0.3 \times 231.47)]^2}{125 + (0.7 \times 231.47)} = 10.75 \text{ mm}$$

Total runoff volume over the catchment $V_r = 5000 \times 10^4 \times 10.75/(1000)$
$$= \textbf{537500 m}^3 = \textbf{0.5375 Mm}^3$$

(c) From Table 5.5 AMC = Type III. Using Table 5.6-c weighted CN_{II} is calculated as below:

Land use (%)	Total %	Soil Group B (60%)			Soil Group C (40%)		
		%	CN	Product	%	CN	Product
Residential area (65% imp)	60	36	85	3060	24	90	2160
Commercial area (85% imp)	30	18	92	1656	12	94	1128
Paved roads	10	6	98	588	4	98	392
Total				**5304**			**3680**

$$\text{Weightd } CN_{\text{II}} = \frac{(5304 + 3680)}{100} = 89.8$$

$$\text{By Eq. (5.24)} \quad CN_{\text{III}} = \frac{89.8}{0.427 + (0.00573 \times 89.8)} = 95.37$$

$$S = \frac{25400}{CN} - 254 = (25400/95.37) - 254 = 12.33$$

Since the soil is not a black soil, Eq. (5.27) is used to compute the surface runoff volume.

$$Q = \frac{(P - 0.3S)^2}{P + 0.7S} \quad \text{for } P > 0.3S \text{ and}$$

$$Q = \frac{[125 - (0.3 \times 12.33)]^2}{125 + (0.7 \times 12.33)} = 110.11 \text{ mm}$$

Total runoff volume over the catchment $V_r = 5000 \times 10^4 \times 110.11/(1000)$
$$= 5,505,500 \text{ m}^3 = 5.5055 \text{ Mm}^3$$

CN AND C OF RATIONAL FORMULA   SCS-CN method estimates runoff volume while the rational formula (Chapter 7, Sec. 7.2) estimates runoff rate based on the runoff coefficient *C*. *CN* and *C* of are not easily related even though they depend on the same set of parameters. For an infinite sponge *C* is 0 and *CN* is 0. Similarly for an impervious surface *C* is 1.0 and *CN* is 100. While the end points in the mapping are easily identifiable the relationship between *CN* and *C* are nonlinear. In a general sense, high *C*s are likely to be found where *CN* values are also high.

5.5 FLOW–DURATION CURVE

It is well known that the streamflow varies over a water year. One of the popular methods of studying this streamflow variability is through flow-duration curves. A flow-duration curve of a stream is a plot of discharge against the per cent of time the flow was equalled or exceeded. This curve is also known as *discharge-frequency curve*.

The streamflow data is arranged in a descending order of discharges, using class intervals if the number of individual values is very large. The data used can be daily, weekly, ten daily or monthly values. If *N* number of data points are used in this listing, the plotting position of any discharge (or class value) *Q* is

$$P_p = \frac{m}{N+1} \times 100\% \tag{5.28}$$

where *m* is the order number of the discharge (or class value), P_p = percentage probability of the flow magnitude being equalled or exceeded. The plot of the discharge *Q* against P_p is the flow duration curve (Fig. 5.8). Arithmetic scale paper, or semi-log or log-log paper is used depending upon the range of data and use of the plot. The flow duration curve represents the cumulative fre-

Fig. 5.8   Flow Duration Curve

quency distribution and can be considered to represent the streamflow variation of an average year. The ordinate Q_p at any percentage probability P_p represents the flow magnitude in an average year that can be expected to be equalled or exceeded P_p per cent of time and is termed as P_p % dependable flow. In a perennial river Q_{100} = 100% dependable flow is a finite value. On the other hand in an intermittent or ephemeral river the streamflow is zero for a finite part of the year and as such Q_{100} is equal to zero.

The following characteristics of the flow duration curve are of interest.

- The slope of a flow duration curve depends upon the interval of data selected. For example, a daily stream flow data gives a steeper curve than a curve based on monthly data for the same stream. This is due to the smoothening of small peaks in the monthly data.

- The presence of a reservoir in a stream considerably modifies the virgin-flow duration curve depending on the nature of flow regulation. Figure 5.9 shows the typical reservoir regulation effect.

- The virgin-flow duration curve when plotted on a log probability paper plots as a straight line at least over the central region. From this property, various coefficients expressing the variability of the flow in a stream can be developed for the description and comparison of different streams.

- The chronological sequence of occurrence of the flow is masked in the flow-duration curve. A discharge of say 1000 m^3/s in a stream will have the same percentage P_p whether it has occurred in January or June. This aspect, a serious handicap, must be kept in mind while interpreting a flow-duration curve.
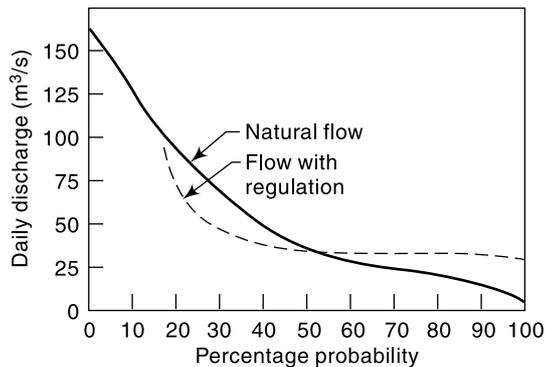
Fig. 5.9 Reservoir Regulation Effect

- The flow-duration curve plotted on a log-log paper (Fig. 5.10) is useful in comparing the flow characteristics of different streams. A steep slope of the curve indicates a stream with a highly variable discharge. On the other hand, a flat slope indicates a slow response of the catchment to the

$Q_{50} = 35$ m^3/s

$Q_{75} = 25$ m^3/s

P_P = Percentage time indicated discharge is equalled or exceeded
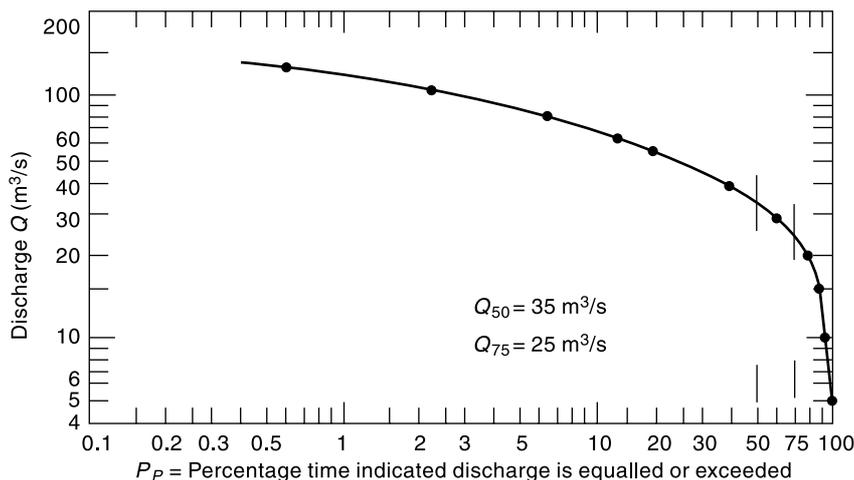
Fig. 5.10 Flow Duration Curve—Example 5.8

rainfall and also indicates small variability. At the lower end of the curve, a flat portion indicates considerable base flow. A flat curve on the upper portion is typical of river basins having large flood plains and also of rivers having large snowfall during a wet season.

Flow-duration curves find considerable use in water resources planning and development activities. Some of the important uses are:

1. In evaluating various dependable flows in the planning of water resources engineering projects
2. Evaluating the characteristics of the hydropower potential of a river
3. Designing of drainage systems
4. In flood-control studies
5. Computing the sediment load and dissolved solids load of a stream
6. Comparing the adjacent catchments with a view to extend the streamflow data.

EXAMPLE 5.8 *The daily flows of a river for three consecutive years are shown in Table 5.7. For convenience the discharges are shown in class intervals and the number of days the flow belonged to the class is shown. Calculate the 50 and 75% dependable flows for the river.*

SOLUTION: The data are arranged in descending order of class value. In Table 5.7, column 5 shows the total number of days in each class. Column 6 shows the cumulative total of column 5, i.e. the number of days the flow is equal to or greater than the class interval. This gives the value of m. The percentage probability P_p the probability of flow in the class interval being equalled or exceeded is given by Eq. (5.28),

$$P_p = \frac{m}{(N+1)} \times 100\%$$

Table 5.7 Calculation of Flow Duration Curve from Daily Flow Data— Example 5.8

Daily mean discharge (m³/s)	No. of days flow in each class interval			Total of columns 2, 3, 4 1961–64	Cumulative Total m	$P_p = \left(\dfrac{m}{N+1}\right) \times 100\%$
	1961–62	1962–63	1963–64			
1	2	3	4	5	6	7
140–120.1	0	1	5	6	6	0.55
120–100.1	2	7	10	19	25	2.28
100–80.1	12	18	15	45	70	6.38
80–60.1	15	32	15	62	132	12.03
60–50.1	30	29	45	104	236	21.51
50–40.1	70	60	64	194	430	39.19
40–30.1	84	75	76	235	665	60.62
30–25.1	61	50	61	172	837	76.30
25–20.1	43	45	38	126	963	87.78
20–15.1	28	30	25	83	1046	95.35
15–10.1	15	18	12	45	1091	99.45
10–5.1	5	—	—	5	1096	99.91
Total	365	365	366	$N = 1096$		

In the present case $N = 1096$. The smallest value of the discharge in each class interval is plotted against P_p on a log-log paper (Fig. 5.10). From this figure $Q_{50} = 50\%$ dependable flow = 35 m³/s and $Q_{75} = 75\%$ dependable flow = 26 m³/s.

5.6   FLOW-MASS CURVE

The flow-mass curve is a plot of the cumulative discharge volume against time plotted in chronological order. The ordinate of the mass curve, V at any time t is thus

$$V = \int_{t_0}^{t} Q \, dt \qquad (5.29)$$

where t_0 is the time at the beginning of the curve and Q is the discharge rate. Since the hydrograph is a plot of Q vs t, it is easy to see that the flow–mass curve is an integral curve (summation curve) of the hydrograph. The flow–mass curve is also known as *Rippl's mass curve* after Rippl (1882) who suggested its use first. Figure 5.9 shows a typical flow–mass curve. Note that the abscissa is chronological time in months in this figure. It can also be in days, weeks or months depending on the data being analysed. The ordinate is in units of volume in million m³. Other units employed for ordinate include m³/s day (cumec day), ha.m and cm over a catchment area.

The slope of the mass curve at any point represents $\dfrac{dV}{dt} = Q =$ rate of flow at that instant. If two points M and N are connected by a straight line, the slope of the line represents the average rate of flow that can be maintained between the times t_m and t_n if a reservoir of adequate storage is available. Thus the slope of the line AB joining the starting point and the last points of a mass curve represents the average discharge over the whole period of plotted record.

CALCULATION OF STORAGE VOLUME

Consider a reservoir on the stream whose mass curve is plotted in Fig. 5.11. If it is assumed that the reservoir is full at the beginning of a dry period, i.e. when the inflow rate is less than the withdrawal (demand) rate, the maximum amount of water drawn from the storage is the cumulative difference between supply and demand volumes from the beginning of the dry season. Thus the storage required S is

S = maximum of

$(\Sigma V_D - \Sigma V_s)$
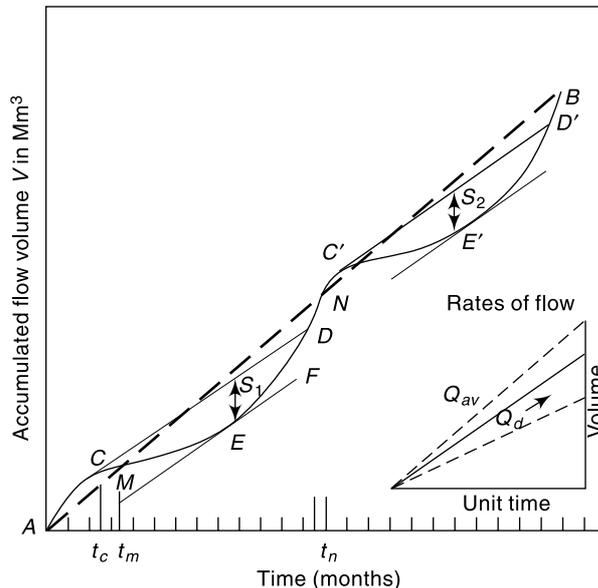
Fig. 5.11   Fow–Mass Curve

where V_D = demand volume, V_S = supply volume. The storage, S which is the maximum cumulative deficiency in any dry season is obtained as the maximum difference in the ordinate between mass curves of supply and demand. The minimum storage volume required by a reservoir is the largest of such S values over different dry periods.

Consider the line *CD* of slope Q_d drawn tangential to the mass curve at a high point on a ridge. This represents a constant rate of withdrawal Q_d from a reservoir and is called *demand line*. If the reservoir is full at *C* (at time t_c) then from point *C* to *E* the demand is larger than the supply rate as the slope of the flow–mass curve is smaller than the demand line *CD*. Thus the reservoir will be depleting and the lowest capacity is reached at *E*. The difference in the ordinates between the demand line *CD* and a line *EF* drawn parallel to it and tangential to the mass curve at *E* (S_1 in Fig. 5.11) represents the volume of water needed as storage to meet the demand from the time the reservoir was full. If the flow data for a large time period is available, the demand lines are drawn tangentially at various other ridges (e.g. *C′ D′* in Fig. 5.11) and the largest of the storages obtained is selected as the minimum storage required by a reservoir. Example 5.9 explains this use of the mass curve. Example 5.10 indicates, storage calculations by arithmetic calculations by adopting the mass-curve principle.

EXAMPLE 5.9 *The following table gives the mean monthly flows in a river during 1981. Calculate the minimum storage required to maintain a demand rate of* 40 m^3/s.

Month	Jan	Fcb	Mar	Apr	May	June	July	Aug	Sept	Oct	Nov	Dec
Mean Flow (m^3/s)	60	45	35	25	15	22	50	80	105	90	80	70

SOLUTION: From the given data the monthly flow volume and accumulated volumes and calculated as in Table 5.8. The actual number of days in the month are used in calculating of the monthly flow volume. Volumes are calculated in units of cumec. day (= 8.64×10^4).

Table 5.8 Calculation of Mass Curve — Example 5.9

Month	Mean flow (m^3/s)	Monthly flow volume (cumec-day)	Accumulated volume (cumec-day)
Jan	60	1860	1860
Feb	45	1260	3120
Mar	35	1085	4205
April	25	750	4955
May	15	465	5420
June	22	660	6080
July	50	1550	7630
Aug	80	2480	10,110
Sep	105	3150	13,260
Oct	90	2790	16,050
Nov	80	2400	18,450
Dec	70	2170	20,620

A mass curve of accumulated flow volume against time is plotted (Fig. 5.12). In this figure all the months are assumed to be of average duration of 30.4 days. A demand line

with slope of 40 m^3/s is drawn tangential to the *hump* at the beginning of the curve; line *AB* in Fig. 5.12. A line parallel to this line is drawn tangential to the mass curve at the *valley* portion; line *A′B′*. The vertical distance S_1 between these parallel lines is the minimum storage required to maintain the demand. The value of S_1 is found to be 2100 cumec. Days = 181.4 million m^3.

EXAMPLE 5.10 *Work out the Example 5.9 through arithmetic calculation without the use of mass curve. What is the maximum constant demand that can be sustained by this river?*
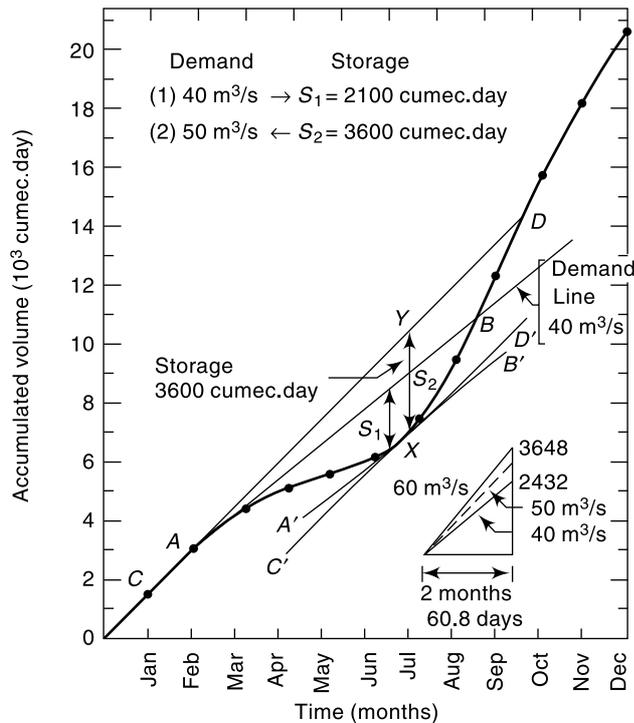
Fig. 5.12 Flow-Mass Curve—Example 5.9

Table 5.9 Calculation of Storage—Example 5.9

Month	Mean inflow rate (m^3/s)	Inflow volume (cumec. day)	Demand rate (m^3/s)	Demand volume (cumec. day)	Departure [col. 3- col. 5]	Cum. excess demand volume (cumec. day)	Cum. excess inflow volume (cumec. day)
Jan	60	1860	40	1240	620		620
Feb	45	1260	40	1120	140		760
Mar	35	1085	40	1240	−155	−155	
Apr	25	750	40	1200	−450	−605	
May	15	465	40	1240	−775	−1380	
Jun	22	660	40	1200	−540	−1920	
July	50	1550	40	1240	310		310
Aug	80	2480	40	1240	1240		1550
Sept	105	3150	40	1200	1950		3500
Oct	90	2790	40	1240	1550		5050
Nov	80	2400	40	1200	1200		6250
Dec	70	2170	40	1240	930		7180
	Monthly mean =	**1718.3**					

SOLUTION: The inflow and demand volumes of each month are calculated as in Table 5.9. Column 6 indicating the departure of the inflow volume from the demand. The negative values indicate the excess of demand over the inflow and these have to be met by the storage. Column 7 indicates the cumulative excess demand (i.e., the cumulative excess negative departures). This column indicates the depletion of storage, the first entry of negative value indicates the beginning of *dry period* and the last value the end of the dry period. Col. 8 indicates the filling up of storage and spill over (if any). Each dry period and each filling up stage is to be calculated separately as indicated in Table 5.9.

The maximum value in Col. 7 represents the minimum storage necessary to meet the demand pattern. In the present case, there is only one dry period and the storage requirement is 1920 cumec.day. Note that the difference between this value and the value of 2100 cumec.day obtained by using the mass curve is due to the curvilinear variation of inflow volumes obtained by drawing a smooth mass curve. The arithmetic calculation assumes a linear variation of the mass curve ordinates between two adjacent time units. [***Note:*** It is usual to take data pertaining to a number of N full years. When the analysis of the given data series of length N causes the first entry in Col. 7 to be a negative value and the last entry is also a negative value, then the calculation of the maximum deficit may pose some confusion. In such cases, repeating the data sequence by one more data cycle of N years in continuation with the last entry would overcome this confusion. (See Sec. 5.7, item 2.) There are many other combinations of factors that may cause confusion in interpretation of the results and as such the use of *Sequent Peak Algorithm* described in Sec. 5.7 is recommended as the foolproof method that can be used with confidence in all situations.]

Column 8 indicates the cumulative excess inflow volume from each demand withdrawal from the storage. This indicates the filling up of the reservoir and volume in excess of the provided storage (in the present case 1920 cumec.day) represent spill over. The calculation of this column is necessary to know whether the reservoir fills up after a depletion by meeting a critical demand and if so, when? In the present case the cumulative excess inflow volume will reach +1920 cumec.day in the beginning of September. The reservoir will be full after that time and will be spilling till end of February.

Average of the inflow volume per month = Annual inflow volume/12 = average monthly demand that can be sustained by this river = 1718.33 cumec.day.

CALCULATION OF MAINTAINABLE DEMAND The converse problem of determining the maximum demand rate that can be maintained by a given storage volume can also be solved by using a mass curve. In this case tangents are drawn from the "ridges" of the mass curves across the next "valley" at various slopes. The demand line that requires just the given storage ($u_1 v_1$ in Fig. 5.13) is the proper demand that can be sustained by the reservoir in that dry period. Similar demand lines are drawn at other "valleys" in the mass curve (e.g. $u_2 v_2$ and the demand rates determined. The smallest of the various demand rates thus found denotes the maximum firm demand that can be sustained by the given storage. It may be noted that this problem involves a trial-and-error procedure for its solution. Example 5.10 indicates this use of the mass curve.

The following salient points in the use of the mass curve are worth noting:
- The vertical distance between two successive tangents to a mass curve at the ridges (points v_1 and u_2 in Fig. 5.13) represent the water "wasted" over the spillway.
- A demand line must intersect the mass curve if the reservoir is to refill. Nonintersection of the demand line and mass curve indicates insufficient inflow.
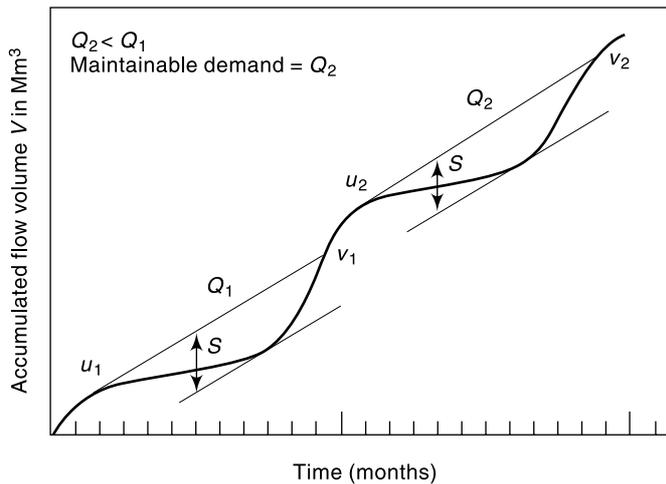
Fig. 5.13 Determination of Maintainable Demand

EXAMPLE 5.11 *Using the mass curve of Example 5.9 obtain the maximum uniform rate that can be maintained by a storage of 3600 m³/s days.*

SOLUTION: An ordinate XY of magnitude 3600 Cumec-days is drawn in Fig. 5.12 at an approximate lowest position in the dip of the mass curve and a line passing through Y and tangential to the "hump" of the mass curve at C is drawn (line CYD in Fig. 5.12). A line parallel to CD at the lowest position of the mass curve is now drawn and the vertical interval between the two measured. If the original guess location of Y is correct, this vertical distance will be 3600 m³/s day. If not, a new location for Y will have to be chosen and the above procedure repeated.

The slope of the line CD corresponding to the final location of XY is the required demand rate. In this example this rate is found to be 50 m³/s.

VARIABLE DEMAND In the examples given above a constant demand rate was assumed to simplify the problem. In practice, it is more likely that the demand rate varies with time to meet various end uses, such as irrigation, power and water-supply needs. In such cases a mass curve of demand, also known as *variable use line* is prepared and superposed on the flow–mass curve with proper matching of time. For example, the demand for the month of February must be against the inflow for the same month. If the reservoir is full at first point of intersection of the two curves, the maximum intercept between the two curves represents the needed storage of the reservoir (Fig. 5.14). Such a plot is sometimes known as *regulation diagram* of a reservoir.
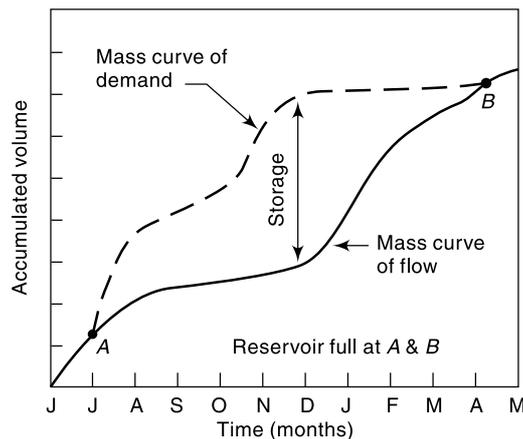
Fig. 5.14 Variable Use Line

In the analysis of problems related to the reservoirs it is necessary to account for evaporation, leakage and other losses from the reservoir. These losses in the volume of water in a known interval of time can either be included in demand rates or deducted from inflow rates. In the latter method, which is generally preferred, the mass curve may have negative slopes at some points. Example 5.12 gives an arithmetic calculation procedure for calculating storage under variable demand.

EXAMPLE 5.12 *For a proposed reservoir the following data were calculated. The prior water rights required the release of natural flow or 5 m^3/s, whichever is less. Assuming an average reservoir area of 20 km^2, estimate the storage required to meet these demands. (Assume the runoff coefficient of the area submerged by the reservoir = 0.5.)*

Month	Mean flow (m^3/s)	Demand (million m^3)	Monthly evaporation (cm)	Monthly rainfall (cm)
Jan	25	22.0	12	2
Feb	20	23.0	13	2
Mar	. 15	24.0	17	1
April	10	26.0	18	1
May	4	26.0	20	1
June	9	26.0	16	13
July	100	16.0	12	24
Aug	108	16.0	12	19
Sept	80	16.0	12	19
Oct	40	16.0	12	1
Nov	30	16.0	11	6
Dec	30	22.0	17	2

SOLUTION: Use actual number of days in a month for calculating the monthly flow and an average month of 30.4 days for prior right release.

Prior right release = $5 \times 30.4 \times 8.64 \times 10^4 = 13.1$ Mm^3 when $Q > 5.0$ m^3/s.

$$\text{Evaporation volume} = \frac{E}{100} \times 20 \times 10^6 = 0.2 \text{ E Mm}^3$$

$$\text{Rainfall volume} = \frac{P}{100} \times (1 - 0.5) \times 20 = 0.1 \text{ P Mm}^3$$

Inflow volume: $I \times$ (No. of days in the month) $\times 8.64 \times 10^4$ m^3

The calculations are shown in Table 5.6 and the required storage capacity is 64.5 Mm^3.

The mass-curve method assumes a definite sequence of events and this is its major drawback. In practice, the runoff is subject to considerable time variations and definite sequential occurrences represent only an idealized situation. The mass-curve analysis is thus adequate for small projects or preliminary studies of large storage projects. The latter ones require sophisticated methods such as *time-series analysis* of data for the final design.

5.7 SEQUENT PEAK ALGORITHM

The mass curve method of estimating the minimum storage capacity to meet a specified demand pattern, described in the previous section has a number of different forms of use in its practical application. However, the following basic assumptions are made in all the adaptations of the mass-curve method of storage analysis.

Table 5.10 Calculation of Reservoir Storage-Example 5.12

| Mo-nth | In-flow volume (Mm³) | Withdrawal | | | | Total with-drawal (3+4+5+6) (Mm³) | Depar-ture (Mm³) | Cum. Excess demand (Mm³) | Cum. Excess flow volume (Mm³) |
		Demand (Mm³)	Prior rights (Mm³)	Evapo-ration (Mm³)	Rain-fall (Mm³)				
1	2	3	4	5	6	7	8	9	10
Jan	67.0	22.0	13.1	2.4	–0.2	37.3	+29.7	—	29.7
Feb	48.4	23.0	13.1	2.6	–0.2	38.5	+9.9	—	39.6
Mar	40.2	24.0	13.1	3.4	–0.1	40.4	–0.2	–0.2	—
Apr	25.9	26.0	13.1	3.6	–0.1	42.6	–16.7	–16.9	—
May	10.7	26.0	10.7	4.0	–0.1	40.6	–29.9	–46.8	
June	23.3	26.0	13.1	3.2	–1.3	41.0	–17.7	–64.5	
July	267.8	16.0	13.1	2.4	–2.4	29.1	+238.7	—	238.7
Aug	289.3	16.0	13.1	2.4	–1.9	29.6	259.7		498.4
Sept	207.4	16.0	13.1	2.4	–1.9	29.6	177.8		676.2
Oct	107.1	16.0	13.1	2.4	–0.1	31.4	75.7		751.9
Nov	77.8	16.0	12.1	2.2	–0.6	30.7	47.1		799.0
Dec	80.4	22.0	13.1	3.4	–0.2	38.3	42.1		841.1

- If N years of data are available, the inflows and demands are assumed to repeat in cyclic progression of N year cycles. It is to be noted that in historical data this leads to an implicit assumption that future flows will not contain a more severe drought than what has already been included in the data.
- The reservoir is assumed to be full at the beginning of a dry period. Thus, while using the mass curve method the beginning of the dry period should be noted and the minimum storage required to pass each drought period calculated. Sometimes, for example in Problem 5.7, it may be necessary to repeat the given data series of N years sequentially for a minimum of one cycle, i.e. for additional N years, to arrive at the desired minimum storage requirement.

The mass curve method is widely used for the analysis of reservoir capacity-demand problems. However, there are many variations of the basic method to facilitate graphical plotting, handling of large data, etc. A variation of the arithmetical calculation described in Examples 5.10 and 5.12 called the *sequent peak algorithm* is particularly suited for the analysis of large data with the help of a computer. This procedure, first given by Thomas (1963), is described in this section.

Let the data be available for N consecutive periods not necessarily of uniform length. These periods can be year, month, day or hours depending upon the problem. In the ith period let x_i = inflow volume and D_i = demand volume. The surplus or deficit of storage in that period is the *net-flow volume* given by

Net-flow volume = Inflow volume – Outflow volume

$$= x_i – D_i$$

In the sequent peak algorithm a mass curve of cumulative net-flow volume against chronological time is used. This curve, known as *residual mass curve* (shown typically in Fig. 5.15), will have peaks (local maximums) and troughs (local minimums).
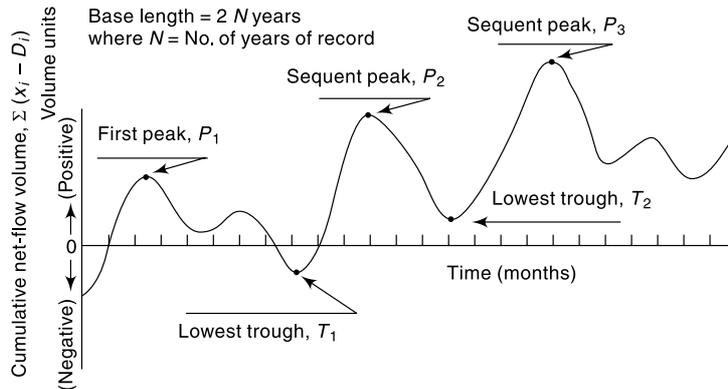
Fig. 5.15 Residual Mass Curve—Definition Sketch for Sequent Peak Algorithm

For any peak P, the next following peak of magnitude greater than P, is called a *sequent peak*. Using two cycles of N periods, where N is the number of periods of the data series, the required storage volume is calculated by the following procedure:

1. Calculate the cumulative net-flow volumes, viz.

$$\sum_{}^{t}(x_i - D_i) \qquad \text{for } t = 1, 2, 3 \ldots, 2\,N$$

2. Locate the first peak P_1 and the sequent peak P_2 which is the next peak of greater magnitude than P_1 (Fig. 5.15).
3. Find the *lowest trough* T_1 between P_1 and P_2 and calculate $(P_1 - T_1)$.
4. Starting with P_2 find the next sequent peak P_3 and the lowest through T_2 and calculate $(P_2 - T_2)$.
5. Repeat the procedure for all the sequent peaks available in the $2N$ periods, i.e. determine the sequent peak P_j, the corresponding T_j and the jth storage $(P_j - T_j)$ for all j values.
6. The required reservoir storage capacity is
$$S = \text{maximum of } (P_j - T_j) \text{ values}$$

EXAMPLE 5.13 *The average monthly flows into a reservoir in a period of two consecutive dry years 1981-82 and 1982-83 is given below.*

Month	Mean monthly flow (m³/s)	Month	Mean monthly flow (m³/s)
1981— June	20	1982—June	15
July	60	July	50
Aug	200	Aug	150
Sept	300	Sept	200
Oct	200	Oct	80
Nov	150	Nov	50
Dec	100	Dec	110
1982— Jan	80	1983—Jan	100
Feb	60	Feb	60
March	40	March	45
April	30	April	35
May	25	May	30

If a uniform discharge at 90 m³/s is desired from this reservoir calculate the minimum storage capacity required.

SOLUTION: The data is for 2 years. As such, the sequent peak calculations are performed for $2 \times 2 = 4$ years. The calculations are shown in Table 5.11.

Scanning the cumulative net-flow volume values (Col. 7) from the start, the first peak P_1 is identified as having a magnitude of 12,200 cumec. day which occurs in the end of the seventh month. The sequent peak P_2 is the peak next to P_1 and of magnitude higher

Table 5.11 Sequent Peak Algorithm Calculations — Example 5.13

S.l. No.	Month	Mean inflow rate (m³/s)	Inflow volume x_i (cumec. day)	Demand rate (m³/s)	Demand volume D_i (cumec. day)	Net-flow volume $(x_i - D_i)$ (cumec. day)	Cumula- tive net- flow volume $\Sigma(x_i - D_i)$ (cumec. day)	Remark
1	June	20	600	90	2700	−2100	−2,100	I Cycle
2	July	60	1860	90	2790	−930	−3,030	
3	Aug.	200	6200	90	2790	+3410	+380	
4	Sept.	300	9000	90	2700	6300	6,680	
5	Oct.	200	6200	90	2790	3410	10,090	
6	Nov.	150	4500	90	2700	1800	11,890	
7	Dec.	100	3100	90	2790	310	12,200*	First peak
8	Jan.	80	2480	90	2790	−310	11,890	P_1
9	Feb.	60	1680	90	2520	−840	11,050	
10	March	40	1240	90	2790	−1550	9,500	
11	April	30	900	90	2700	−1800	7,700	
12	May	25	775	90	2790	−2015	5,685	
13	June	15	450	90	2700	−2250	3,435	
14	July	50	1550	90	2790	−1240	2,195	
15	Aug.	150	4650	90	2790	1860	4,055	
16	Sept.	200	6000	90	2700	3300	7,355	
17	Oct.	80	2480	90	2790	−310	7,045	
18	Nov.	50	1500	90	2700	−1200	5,845	
19	Dec.	110	3410	90	2790	620	6,465	
20	Jan.	100	3100	90	2790	310	6,775	
21	Feb.	60	1680	90	2520	−840	5,935	
22	March	45	1395	90	2790	−1395	4,540	
23	April	35	1050	90	2700	−1650	2,890	
24	May	30	930	90	2790	−1860	1,030	
25	June	20	600	90	2700	−2100	1,070	II Cycle
26	July	60	1860	90	2790	−930	−2,000*	Lowest
27	Aug.	200	6200	90	270	3410	1,410	trough T_1
28	Sept.	300	9000	90	2700	6300	7,710	between P_1
29	Oct.	200	6200	90	2790	3410	11,120	and P_2
30	Nov.	150	4500	90	2700	1800	12,920	
31	Dec.	100	3100	90	2790	310	13,230*	Sequent
32	Jan.	80	2480	90	2790	−310	12,920	Peak P_2
33	Feb.	60	1680	90	2520	−840	12,080	

(Contd.)

Table 5.11 (*Contd.*)

S.l. No.	Month	Mean inflow rate (m³/s)	Inflow volume x_i (cumec. day)	Demand rate (m³/s)	Demand volume D_i (cumec. day)	Net-flow volume $(x_i - D_i)$ (cumec. day)	Cumulative net-flow volume $\Sigma(x_i - D_i)$ (cumec. day)	Remark
34	March	40	1240	90	2790	−1550	10,530	
35	April	30	900	90	2700	−1800	8,730	
36	May	25	775	90	2790	−2015	6,715	
37	June	15	450	90	2700	−2250	4,465	
38	July	50	1550	90	2790	−1240	3,225	
39	Aug.	150	4650	90	2790	1860	5,085	
40	Sept.	200	6000	90	2700	3300	8,385	
41	Oct.	80	2480	90	2790	−310	8,075	
42	Nov.	50	1500	90	2700	−1200	6,875	
43	Dec.	110	3410	90	2790	620	7,495	
44	Jan.	100	3100	90	2790	310	7,805	
45	Feb.	60	1680	90	2520	−840	6,965	
46	March	45	1395	90	2790	−1395	5,570	
47	April	38	1050	90	2700	−1650	3,920	
48	May	30	930	90	2790	−1860	2,060	

(*Note:* Since $N = 2$ years the data is run for 2 cycles of 2 years each.)

than 12,200. This P_2 is identified as having a magnitude of 13,230 cumec. day and occurs in the end of the 31st month from the start. Between P_1 and P_2 the lowest trough T_1 has a magnitude of (–2,000) cumec. day and occurs at the end of the 26th month. In the present data run for two cycles of total duration 4 years, no further sequent peak is observed.

$$P_1 - T_1 = 12,000 - (-2000) = 14,200 \text{ cumec. day}$$

Since there is no second trough,

$$\text{The required minimum storage} = \text{maximum of } (P_j - T_j) \text{ values}$$
$$= (P_1 - T_1) = 14,200 \text{ cumec. day}$$

5.8 DROUGHTS

In the previous sections of this chapter the variability of the stream flow was considered in the flow duration curve and flow mass curve. However, the extremes of the stream flow as reflected in floods and droughts need special study. They are natural disasters causing large scale human suffering and huge economic loss and considerable effort is devoted by the world over to control or mitigate the ill effects of these two hydrological extremes. The various aspects of floods are discussed in Chapters 7 and 8. The topic of drought, which is not only complex but also region specific is discussed, rather briefly, in this section. The classification of droughts and the general nature of drought studies are indicated with special reference to the Indian conditions. For further details the reader is referred to References 1, 2, 4 and 6.

DEFINITION AND CLASSIFICATION

Drought is a climatic anomaly characterized by deficit supply of moisture. This may result from subnormal rainfall over large regions causing below normal natural avail-

ability of water over long periods of time. Drought phenomenon is a hydrological extreme like flood and is a natural disaster. However, unlike floods the droughts are of the creeping kind; they develop in a region over a length of time and sometimes may extend to continental scale. The consequences of droughts on the agricultural production, hydropower generation and the regional economy in general is well known. Further, during droughts the quality of available water will be highly degraded resulting in serious environmental and health problems.

Many classifications of droughts are available in literature. The following classification into three categories proposed by the National Commission on Agriculture (1976) is widely adopted in the country:

- *Meteorological drought:*
  It is a situation where there is more than 25% decrease in precipitation from normal over an area.
- *Hydrological drought:*
  Meteorological drought, if prolonged, results in hydrological drought with marked depletion of surface water and groundwater. The consequences are the drying up of tanks, reservoirs, streams and rivers, cessation of springs and fall in the groundwater level.
- *Agricultural drought:*
  This occurs when the soil moisture and rainfall are inadequate during the growing season to support healthy crop growth to maturity. There will be extreme crop stress and wilt conditions.

METEOROLOGICAL DROUGHT The India Meteorological Department (IMD) has adopted the following criteria for sub-classification of meteorological droughts. A meteorological sub-division is considered to be affected by drought if it receives a total seasonal rainfall less than that of 75% of the normal value. Also, the drought is classified as *moderate* if the seasonal deficiency is between 26% and 50%. The drought is said to be *severe* if the deficiency is above 50% of the normal value. Further, a year is considered to be a *drought year* in case the area affected by moderate or severe drought either individually or collectively is more than 20% of the total area of the country.

If the drought occurs in an area with a probability $0.2 \leq P \leq 0.4$ the area is classified as *drought prone area*, if the probability of occurrence of drought at a place is greater than 0.4, such an area is called as *chronically drought prone area.* Further, in India the meteorological drought is in general related to the onset, breaks and withdrawal times of monsoon in the region. As such, the prediction of the occurrence of drought in a region in the country is closely related to the forecast of deficient monsoon season and its distribution. Accurate forecast of drought, unfortunately, is still not possible.

HYDROLOGICAL DROUGHT From a hydrologist's point of view drought means below average values of stream flow, contents in tanks and reservoirs, groundwater and soil moisture. Such a hydrological drought has four components:

(a) Magnitude (= amount of deficiency)
(b) Duration
(c) Severity (= cumulative amount of deficiency)
(d) Frequency of occurrence

The beginning of a drought is rather difficult to determine as drought is a creeping phenomenon. However, the end of the drought when adequate rainfall saturates the soil mass and restores the stream flow and reservoir contents to normal values is relatively easy to determine.

In the studies on hydrological drought different techniques have to be adopted for study of (i) surface water deficit, and (ii) groundwater deficit. The surface water aspect of drought studies is essentially related to the stream and the following techniques are commonly adopted:

  (a) Low-flow duration curve
  (b) Low-flow frequency analysis and
  (c) Stream flow modelling.

Such studies are particularly important in connection with the design and operation of reservoirs, diversion of stream flow for irrigation, power and drinking water needs; and in all activities related to water quality.

AGRICULTURAL DROUGHT   Deficiency of rainfall has been the principal criteria for defining agricultural drought. However, depending on whether the study is at regional level, crop level or plant level there have been a variety of definitions. Considering the various phases of growth of a crop and its corresponding water requirements, the time scale for water deficiency in agricultural drought will have to be much smaller than in hydrological drought studies. Further, these will be not only regional specific but also crop and soil specific.

An *aridity index* (AI) is defined as

$$AI = \frac{PET - AET}{PET} \times 100 \qquad (5.30)$$

where *PET* = *Potential evapotranspiration* and *AET* = *Actual evapotranspiration*. In this *AI* calculation, *AET* is calculated according to *Thornthwite's water balance technique*, taking in to account *PET*, actual rainfall and field capacity of the soil. It is common to calculate *AI* on weekly or bi-weekly basis. *AI* is used as an indicator of possible moisture stress experienced by crops. The departure of *AI* from its corresponding normal value, known as *AI anomaly*, represents moisture shortage. Based on *AI* anomaly, the intensity of agricultural drought is classified as follows:

AI anomaly	Severity class
Zero or negative	Non-arid
1 –25	Mild arid
26 –50	Moderate arid
> 50	Severe arid

In addition to AI index, there are other indices such as *Palmer index* (PI) and *Moisture availability index* (MAI) which are used to characterize agricultural drought. IMD produces aridity index (AI) anomaly maps of India on a bi-weekly basis based on data from 210 stations representing different agro-climatic zones in the country. These are useful in planning and management of agricultural operations especially in the drought prone areas. Remote sensing techniques using imageries offer excellent possibilities for monitoring agricultural drought over large areas.

Drought Management

The causes of drought are essentially due to temporal and spatial aberrations in the rainfall, improper management of available water and lack of soil and water conservation. Drought management involves development of both short-term and long-term strategies. *Short-term strategies* include early warning, monitoring and assessment of droughts The *long-term strategies* aim at providing drought mitigating measures through proper soil and water conservation, irrigation scheduling and cropping patterns. Figure 5.16 shows some impacts and possible modifications of various drought components. The following is a list of possible measures for making drought prone areas less vulnerable to drought associated problems:
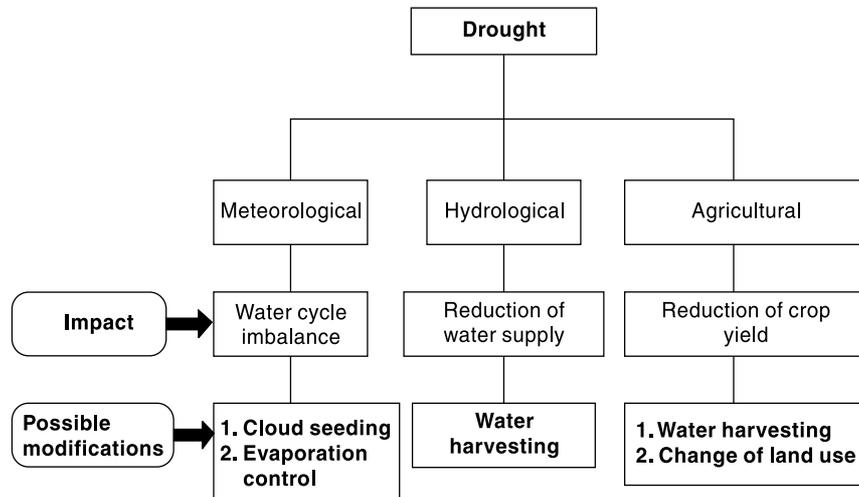
Fig. 5.16   Impact and Possible Modification of Drought Components

- Creation of water storages through appropriate water resources development
- Inter-basin transfer of surface waters from surplus water areas to drought prone areas
- Development and management of ground water potential
- Development of appropriate water harvesting practices
- In situ soil moisture conservation measures
- Economic use of water in irrigation through practices such as drip irrigation, sprinkler irrigation, etc.
- Reduction of evaporation from soil and water surfaces
- Development of afforestation, agro-forestry and agro-horticulture practices
- Development of fuelwood and fodder
- Sand dune stabilization

Drought-proofing of a region calls for integrated approach, taking into account the multi-dimensional interlinkages between various natural resources, environment and local socio-economic factors.

Salient features of water harvesting, which forms an important component in modification of drought components is described in the next sub-section.

WATER HARVESTING

Water harvesting is a general term to include all systems that concentrate, collect and store runoff from small catchments for later use in smaller user areas. FAO defines water harvesting as, "*Water harvesting* is defined as the process of collecting and concentrating runoff water from a runoff area into a run-on area, where the collected water is either directly applied to the cropping area and stored in the soil profile for immediate use by the crop, i.e. runoff farming, or stored in an on-farm water reservoir for future productive uses, i.e. domestic use, livestock watering, aquaculture and irrigation." The collected water can also be used for groundwater recharge and storage in the aquifer, i.e. recharge enhancement. As a general rule the catchment area from which the water is drawn is larger than the command area, where it is collected and used. The ratio of catchment, to command is inversely related to the amount and intensity of rainfall, the impermeability of soil, and the slope of the land on which it falls.

Water harvesting is essentially a traditional system used since many centuries, now being made over to meet present-day needs. Depending upon the nature of collecting surface and type of storages water harvesting is classified into several categories as mentioned in Fig. 5.17.
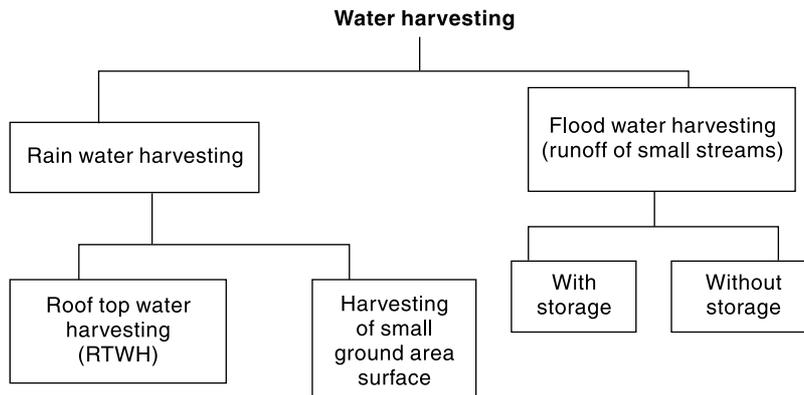
Fig. 5.17   Classification of Water Harvesting Techniques

ROOF TOP WATER HARVESTING   The productive utilization of rain water falling on roof-tops of structures is known as *Roof Top Water Harvesting* (RTWH). In urban areas the roof tops are usually impervious and occupy considerable land area. Also, generally the municipal water supply is likely to be inadequate, inefficient or unreliable. In such situations, collection of runoff from roof tops of individual structures and storing them for later use has been found to be very attractive and economical proposition in many cases. Inadequacy of water availability and cost of supply has made many industries and large institutions in urban areas situated in arid and semi-arid regions to adopt RTWH systems in a big way. Factors like water quality, methods for efficient and economical collection and storage are some factors that have to be worked out in designing an efficient system to meet specific needs. The cost of adequate size storage is, generally, a constraint in economical RTWH design. In many cases, water collected from roof top is used for recharging the ground water. Charac-

teristics of the rainfall at the place, such as intensity, duration, nature of the rainfall season, average number of rainy days, determine the design of the RTWH design.

MICRO CATCHMENT SYSTEM (WITHIN THE FIELD) OF RAINWATER HARVESTING   In this system the catchment is a small area which is not put for any productive purpose. The catchment length is usually between 1 and 30 metres and the overland flow from this during a storm is harvested by collecting and delivering it to a small cultivated plot. The ratio of catchment to the cultivated area is usually 1:1 to 3:1 and the runoff is stored in soil profile. Normally there will be no provision for overflow. Rainwater harvesting in Micro catchments is sometimes referred to as *Within-Field Catchment System.*

Typical examples of such Rainwater harvesting in micro catchments are:
- Negarim Micro Catchments (for trees)
- Contour Bunds (for trees)
- Contour Ridges (for crops)
- Semi-Circular Bunds (for range and fodder)

Negarim micro catchment technique was originally developed in Israel; the word Negarim is derived from Hebrew word *Neger* meaning runoff. This technique consists of dividing the catchments into a large number of micro catchments in a diamond pattern along the slope. Each micro catchment is of square shape with a small earthen bunds at its boundary and an infiltration pit is provided at the lowest corner as shown in Fig. 5.18. The pit is the cultivated area and usually a tree is grown in the pit. This arrangement of micro catchments of sizes $10\,\text{m}^2$ to $100\,\text{m}^2$, has been found to be very beneficial in arid and semiarid areas where rainfall can be as low as 150 mm.
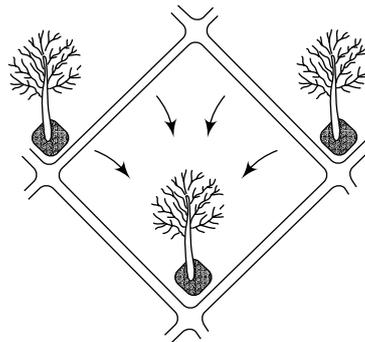
Fig. 5.18   Micro Catchment System: Negarim Micro Catchment for Trees

MACRO CATCHMENT SYSTEM (WITHIN THE FIELD) OF RAINWATER HARVESTING   This system is designed for slightly larger catchment areas wherein overland flow and rill flow is collected behind a bund and allowed to be stored in the soil profile through infiltration. The catchment is usually 30 to 200 m long and the ratio of catchment to cultivated area is in the range 2:1 to 10:1. Typical arrangement consists of one row or two staggered rows of trapezoidal bunds with wing walls. Contour bunds made of piled up stones is also used in this system. It is usual to provide overflow arrangements for disposing of the excess runoff water. Infiltration area behind the bunds is used to grow crops.

FLOODWATER FARMING (FLOODWATER HARVESTING)   This system is used for larger catchments and the flow in the drainage is harvested. The catchment areas are several kilometres long and the ratio of catchment to command is larger than 10:1. Two sub-systems mentioned below are in common use:
1. Water Harvesting using Storage Structures
2. Water Harvesting through Spreading of Water over Command

STORAGE STRUCTURES SYSTEMS   Small storage structures are built across the drainage to store a part of the runoff. While the stored surface water would serve as a source of utilisable water to the community for some time the infiltration from this water body would provide valuable recharge to the ground water. The commonly used structures are *Check dams* and *Nalabunds*. These structures have the additional advantage of arresting erosion products from the catchment. Further, these structures prevent the deepening and widening of gullies.

The check dams usually have a masonry overflow spillway and the flanks can be of either masonry construction or of earthen embankment. They are constructed on lower order streams (up to 3) with median slopes. Generally check dams are proposed where water table fluctuations are high and the stream is influent.

Nalabunds are structures constructed across nalas (streams) for impounding runoff flow to cause a small storage. Increased water percolation and improving of soil moisture regime are its main objective. Nalabunds are of small dimension and are constructed by locally available material, usually an earthen embankment. In a Nalabund the spillway is normally a stone lined or rock cut steep channel taking off from one of the ends of the bund at appropriate level. Structures similar to a nalabund but of larger dimension are known as *percolation tanks.* Nalabunds and percolation tanks are constructed in flat reach of a stream with slopes less than 2%.

The irrigation tanks of south India are also sometimes termed as water harvesting structures. Tanks on local streams form a significant source of irrigation in states of Andhra Pradesh, Karnataka, Maharashtra and Tamil Nadu. These are small storage structures formed by earthen bunds to store runoff, of a small stream. The embankment, surplus weir and a sluice outlet form the essential component of a tank. The tank system in a region, which can be a group of independent tanks or a set of tanks in cascade, form an important source of surface water for domestic use, drinking water for life stock, agriculture for growing food and fodder and recharge of subsurface aquifers.

SPREADING OF WATER   In this method a diversion across the drainage would cause the runoff to flow on to the adjacent land. Appropriate bunds either of rock or of earth would cause spreading the water over the command. The spread water infiltrates into the soil and is retained as soil moisture and this is used for growing crops. Provision for overflow spillway at the diversion structure, to pass excess water onto the downstream side of the diversion structure, is an important component of the diversion structure.

General: The specific aspects related to the design of water harvesting structures depends upon the rainfall in the region, soil characteristics and terrain slope. It is usual to take up water harvesting activity at a place as a part of intergraded watershed management programme. Norms for estimating recharge from water harvesting structures are given in Sec. 9.13 of Chapter 9.

The water harvesting methods described above are particularly useful in dry land agriculture and form important draught management tool. Community participation in construction and management of water harvesting structure system is essential for economical and sustainable use of the system. Rehabilitation of old irrigation tanks through de-silting to bring it back to its original capacity is now recognized as a feasible and desirable activity in drought proofing of a region.

DROUGHTS IN INDIA

Even though India receives a normal annual precipitation of 117 cm, the spatial and temporal variations lead to anomalies that lead to floods and droughts. Consequently droughts have been an everpresent feature of the country. While drought has remained localized in some part of the country in most of the years they have become wide spread and severe in some years. In the past four decades, wide spread and severe droughts have occurred in the years 1965–66, 1971–73, 1979–80, 1982–83, 1984–87, 1994–96, 1999–2000, 2001–02. These droughts affected the agricultural production and the economy significantly and caused immense hardship and misery to a very large population.

Since 1875 till 2004, India faced 29 drought years; the 1918 being the worst year in which about 70% of the country was affected by drought. Analysis of records since 1801 reveals that nearly equal number droughts occurred in 19th century and in 20th century and that there is a lower number of occurrences in the second quarter of both centuries.

It has been estimated that nearly one third of the area of the country (about 1 M ha) is drought prone. Most of the drought prone areas lie in the states of Rajasthan, Karnataka, Andhra Pradesh, Maharashtra, Gujarat and Orissa. Roughly 50% of the drought prone area of the country lies in Deccan plateau. Further, while Rajasthan has a return period of about 2 years for severe droughts it is about 3 years in the Deccan plateau region. It is difficult to estimate the economic losses of drought, as it is a creeping phenomenon with wide spatial coverage. However, a wide spread drought in the country would cover agricultural areas of the order of 100 lakh ha and the consequential loss due to damaged crops could be of the order of Rs 5000 crores.

5.9 SURFACE WATER RESOURCES OF INDIA

SURFACE WATER RESOURCES

Natural (Virgin) Flow in a river basin is reckoned as surface resource of a basin. In view of prior water resources development activities, such as construction of storage reservoirs in a basin, assessment of natural flow is a very complex activity. In most of the basins of the country, water resources have already been developed and utilized to various extents through construction of diversion structures and storage reservoirs for purposes of irrigation, drinking water supply and industrial uses. These utilizations in turn produce *return flows* of varying extent; return flow being defined as the non-consumptive part of any diversion returned back. Return flows to the stream from irrigation use in the basin are usually assumed to be 10% of the water diverted from the reservoir or diversion structure on the stream for irrigation. The return flows from diversions for domestic and industrial use is usually assumed as 80% of the use. The return flow to the stream from ground water use is commonly ignored.

The natural flow in a given period at a site is obtained through water budgeting of observed flow, upstream utilization and increase in storage, evaporation and other consumptive uses and return flows. The surface and groundwater components are generally treated separately.

Estimation of surface water resources of the country has been attempted at various times. Significant recent attempts are:
- A.N. Khosla's estimate (1949), based on empirical relationships, of total annual flow of all the river systems of the country as 1673 km³.

- CWC (1988), on the basis of statistical analysis of available data, and on rainfall–runoff relationships where flow data was meagre or not available, estimated the total annual runoff of the river systems of India as 1881 km^3.
- The National Commission for Integrated Water Resources Development (1999) used the then available estimates and data and assessed the total surface water resources of the country as 1952.87 km^3 (say 1953 km^3).

It should be noted that the average annual natural (Virgin) flow at the terminal point of a river is generally taken as the surface water resources of the basin. But this resource is available with a probability of about 50% whereas it is customary to design *irrigation projects* with 75% dependability and *domestic water supply projects* for nearly 100% dependability. Obviously, the magnitude of water at higher values of dependability (say 75% and above) will be smaller than the average value.

The total catchment area of all the rivers in India is approximately 3.05 million km^2. This can be considered to be made up of three classes of catchments:

1. Large catchments with basin area larger than 20,000 km^2;
2. Medium catchments with area between 20,000 to 2000 km^2; and
3. Small catchments with area less than 2000 km^2.

Rao[9] has estimated that large catchments occupy nearly 85% of the country's total drainage area and produce nearly 85% of the runoff. The medium and minor catchments account for 7% and 8% of annual runoff volumes respectively. In the major river basin of the country two mighty rivers the Brahmaputra and the Ganga together constitute 71.5% of the total yield in their class and contribute 61% of the country's river flow. Further, these two rivers rank eighth and tenth respectively in the list of the world's ten largest rivers (Table 5.12). It is interesting to note that the ten rivers listed in Table 5.12 account for nearly 50% of the world's annual runoff.

Table 5.12 World's Ten Largest Rivers

Sl. No	River	Annual runoff (Billion m^3)
1.	Amazon	6307
2.	Platt	1358
3.	Congo	1245
4.	Orinoco	1000
5.	Yangtze	927
6.	Mississippi	593
7.	Yenisei	550
8.	Brahmputra	510
9.	Mekong	500
10.	Ganga	493

According to an analysis of CWC, about 80% of average annual flow in the rivers of India is carried during monsoon months. This highlights the need for creating storages for proper utilization of surface water resources of the country. Another interesting aspect of Indian rivers is that almost all the rivers flow through more than one state, highlighting the need for inter-state co-operation in the optimum development of water resources.

UTILIZABLE WATER RESOURCES

Utilizable water resources mean the quantum of water withdrawable from its place of natural occurrence. Withdrawal of water from a river depends on topographic conditions and availability of land for the stated project. As a result of various limitations such as to topography, environmental consideration, non-availability of suitable locations and technological shortcomings, it will not be possible to utilize the entire surface water resources of the country. Further, surface water storage structures, such as reservoirs, cause considerable loss by evaporation and percolation. Also, environmental considerations preclude total utilization or diversion of surface water resources of a basin. From these considerations, it is necessary to estimate the optimum utilizable surface runoff of the country for planning purposes. Normally, the optimum utilizable surface runoff of a basin will be around 70% of the total surface runoff potential of the basin.

CWC in 1988 estimated the utilizable surface water resource of the country as 690.32 km^3. The National Commission for Integrated Water Resources Development[8] (1999) has adopted this value in preparing estimates of future water demand–supply scenarios up to the year 2050. Table 5.13 gives the basinwise distribution of utilizable surface water resource of the country.

Table 5.13 Average Flow and Utilizable Surface Water Resource of Various Basins

[Unit: km^3/Year] (Source: Ref. 8]

S. No.	River Basin	Surface water resources	Utilizable surface water resources
1.	Indus	73.31	46
2.	Ganga–Brahmaputra–Meghna Basin		
	2a Ganga sub-basin	525.02	250.0
	2b Brahmaputra sub-basin and	629.05	24.0
	2c Meghna (Barak) sub-basin	48.36	
3.	Subarnarekha	12.37	6.81
4.	Brahmani–Baitarani	28.48	18.30
5.	Mahanadi	66.88	49.99
6.	Godavari	110.54	76.30
7.	Krishna	69.81	58.00
8.	Pennar	6.86	6.32
9.	Cauvery	21.36	19.00
10.	Tapi	14.88	14.50
11.	Narmada	45.64	34.50
12.	Mahi	11.02	3.10
13.	Sabarmati	3.81	1.93
14.	West flowing rivers of Kutchch and Saurashtra	15.10	14.96
15.	West flowing rivers south of Tapi	200.94	36.21
16.	East flowing rivers between Mahanadi and Godavari	17.08	
17.	East flowing rivers between Godavari and Krishna	1.81	13.11

(Contd.)

(*Contd.*)

18.	East flowing rivers between Krishna and Pennar	3.63	
19.	East flowing rivers between Pennar and Cauvery	9.98	16.73
20.	East flowing rivers south of Cauvery	6.48	
21.	Area North of Ladakh not draining into India	0	0
22.	Rivers draining into Bangladesh	8.57	0
23.	Rivers draining into Myanmar	22.43	0
24.	Drainage areas of Andaman, Nicobar and Lakshadweep islands	0	0
	Total	**1952.87**	**690.32**

In the computation of utilizable water resources as 690 km^3 it is assumed that adequate storage facility is available for balancing the monsoon flows into an average year round availability. The minimum storage required to achieve this is estimated as 460 km^3 against the present estimated total available storage capacity of 253 km^3. If more storage capacity could be developed carry-over from years of above normal rainfall to dry years would be possible. For comparison purposes, for about the same annual runoff the USA has storage of 700 km^3.

UTILIZABLE DYNAMIC GROUNDWATER RESOURCES   The total replenish-able groundwater resources of the country (dynamic) has been estimated by CGWB as 431.89 km^3/year and the utilizable dynamic groundwater potential as 396 km^3/year (details in Chapter 9, Section 9.12).

WATER AVAILABLE FROM RETURN FLOWS   Water used for a specific activity such as irrigation and domestic water supply includes consumptive and non-consumptive components. The non-consumptive component part of water use is returned back to hydrologic system either as surface flow or as addition to groundwater system or as soil moisture. However, due to economic and technological constraints and due to possibilities of diminished water quality, only a part of the return flow is recoverable for re-use. The utilizable return flow is an important component to be considered in the demand–supply analysis of utilizable water resources.

TOTAL WATER REQUIREMENT AND AVAILABLE RESOURCES SCENARIO

TOTAL WATER REQUIREMENT FOR DIFFERENT USES   The estimated total water requirements, estimated by NCIWRD[8], for the two scenarios and for various sectors at three future horizons are shown in Table 5.14. Irrigation would continue to have the highest water requirement (about 68% of total water requirement), followed by domestic water including drinking and bovine needs.

EVAPORATION   In water resources evaluation studies it is common to adopt a percentage of the live capacity of a reservoir as evaporation losses. The NCIWRD has adopted a national average value of 15% of the live storage capacity of major projects and 25% of the live storage capacity of minor projects as evaporation losses in the country. The estimated evaporation losses from reservoirs are 42 km^3, 50 km^3 and 76 km^3 by the years 2010, 2025 and 2050 respectively.

DEMAND AND AVAILABLE WATER RESOURCES   The summary of NCIWRD[8] (1999) study relating to national level assessment of demand and available water

Table 5.14   Water Requirement for Different Uses

(Unit: Cubic Kilometer) [Source: Ref. 8]

Sl No.	Uses	Year 2010			Year 2025			Year 2050		
		Low	High	%	Low	High	%	Low	High	%
Surface Water										
1.	Irrigation	330	339	48	325	366	43	375	463	39
2.	Domestic	23	24	3	30	36	5	48	65	6
3.	Industries	26	26	4	47	47	6	57	57	5
4.	Power	14	15	2	25	26	3	50	56	5
5.	Inland Navigation	7	7	1	10	10	1	15	15	1
6.	Environment (Ecology)	5	5	1	10	10	1	20	20	2
7.	Evaporation Losses	42	42	6	50	50	6	76	76	6
	Total	**447**	**458**	**65**	**497**	**545**	**65**	**641**	**752**	**64**
Ground Water										
1.	Irrigation	213	218	31	236	245	29	253	344	29
2.	Domestic	19	19	2	25	26	3	42	46	4
3.	Indusrtries	11	11	1	20	20	2	24	24	2
4.	Power	4	4	1	6	7	1	13	14	1
	Total	**247**	**252**	**35**	**287**	**298**	**35**	**332**	**428**	**36**
	Grand Total	**694**	**710**	**100**	**784**	**843**	**100**	**973**	**1180**	**100**

resources is given in Table 5.15. The utilizable return flow is an important component to be considered in the demand–supply analysis of utilizable water resources. Estimated utilizable return flows of the country in surface and groundwater mode for different time horizons are shown in Table 5.15. It may be noted that the return flow contributes to an extent of nearly 20–25% in reducing the demand.

Table 5.15   Utilizable Water, Requirements and Return Flow

(Quantity in Cubic Kilometre) [Source: Ref. 8]

Sl. No.	Particulars	Year 2010		Year 2025		Year 2050	
		Low Demand	High Demand	Low Demand	High Demand	Low Demand	High Demand
1	**Utilizable Water**						
	Surface Water	690	690	690	690	690	690
	Ground water	396	396	396	396	396	396
	Augmentation from canal Irrigation	90	90	90	90	90	90
	Total	**996**	**996**	**996**	**996**	**996**	**996**
	Total Water						

(*Contd.*)

2	**Requirement**						
	Surface Water	447	458	497	545	641	752
	Ground Water	247	252	287	298	332	428
	Total	**694**	**710**	**784**	**843**	**973**	**1180**
3	**Return Flow**						
	Surface Water	52	52	70	74	91	104
	Ground Water	144	148	127	141	122	155
	Total	**196**	**200**	**197**	**215**	**213**	**259**
4	**Residual Utilizable water**						
	Surface Water	295	284	263	219	140	42
	Ground Water	203	202	146	149	96	33
	Total	**498**	**486**	**409**	**463**	**236**	**75**

While the table is self-explanatory, the following significant aspects may be noted:

(a) The available water resources of the country are adequate to meet the low demand scenario up to year 2050. However, at high demand scenario it barely meets the demand.

(b) Need for utmost efficiency in management of every aspect of water use, conservation of water resources and reducing the water demand to low demand scenario are highlighted.

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REVISION QUESTIONS

5.1 List the factors affecting the seasonal and annual runoff (Yield) of a catchment. Describe briefly the interactions of factors listed by you.

5.2 With the help of typical hydrographs describe the salient features of (i) Perennial, (ii) intermittent, and (iii) ephemeral steams.

5.3 Explain briefly:

  (a) Water year   (b) Natural (Virgin) flow

5.4 What is meant by 75% dependable yield of a catchment? Indicate a procedure to estimate the same by using annual runoff volume time series.

5.5 Describe briefly the *SCS-CN* method of estimation yield of a catchment through use of daily rainfall record.

5.6 Indicate a procedure to estimate the annual yield of a catchment by using Strange's tables.

5.7 Explain clearly the procedure for calculating 75% dependable yield of a basin at a flow gauging station. List the essential data series required for this analysis.

5.8 Distinguish between yield and surface water resources potential of a basin having substantial water resources development for meeting irrigation, domestic and industrial needs within the basin.

5.9 What is watershed simulation? Explain briefly the various stages in the simulation study.

5.10 What is a flow-duration curve? What information can be gathered from a study of the flow duration curve of a stream at a site?

5.11 Sketch a typical flow mass curve and explain how it could be used for the determination of

  (a) the minimum storage needed to meet a constant demand

  (b) the maximum constant maintainable demand from a given storage.

5.12 Describe the use of flow mass curve to estimate the storage requirement of a reservoir to meet a specific demand pattern. What are the limitations of flow mass curve?

5.13 What is a residual mass curve? Explain the sequent peak algorithm for the calculation of minimum storage required to meet a demand.

5.14 What is a hydrological drought? What are its components and their possible effects?

5.15 List the measures that can be adopted to lessen the effects of drought in a region.

5.16 Describe briefly the surface water resources of India.

| PROBLEMS |

5.1 Long-term observations at a streamflow-measuring station at the outlet of a catchment in a mountainous area gives a mean annual discharge of 65 m^3/s. An isohyetal map for the annual rainfall over the catchment gives the following areas closed by isohyets and the divide of the catchment:

Isohyet (cm)	Area (km²)	Isohyet (cm)	Area (km²)
140–135	50	120–115	600
135–130	300	115–110	400
130–125	450	110–105	200
125–120	700		

Calculate   (a) the mean annual depth of rainfall over the catchment,

                 (b) the runoff coefficient.

5.2 A small stream with a catchment area of 70 km^2 was gauged at a location some distance downstream of a reservoir. The data of the mean monthly gauged flow, rainfall and upstream diversion are given. The regenerated flow reaching the stream upstream of the gauging station can be assumed to be constant at a value of 0.20 Mm^3/month. Obtain the rainfall runoff relation for this stream. What virgin flow can be expected for a monthly rainfall value or 15.5 cm?

Month	Monthly rainfall (cm)	Gauged monthly flow (Mm^3)	Upstream utilization (Mm^3)
1.	5.2	1.09	0.60
2.	8.6	2.27	0.70
3.	7.1	1.95	0.70
4.	9.2	2.80	0.70
5.	11.0	3.25	0.70
6.	1.2	0.28	0.30
7.	10.5	2.90	0.70
8.	11.5	2.98	0.70
9.	14.0	3.80	0.70
10.	3.7	0.84	0.30
11.	1.6	0.28	0.30
12.	3.0	0.40	0.30

5.3 The following table shows the observed annual rainfall and the corresponding annual runoff for a small catchment. Develop the rainfall–runoff correlation equation for this catchment and find the correlation coefficient. What annual runoff can be expected from this catchment for an annual rainfall of 100 cm?

Year	1964	1965	1966	1967	1968	1969
Annual Rainfall (cm)	90.5	111.0	38.7	129.5	145.5	99.8
Annual Runoff (cm)	30.1	50.2	5.3	61.5	74.8	39.9
Year	1970	1971	1972	1973	1974	1975
Annual Rainfall (cm)	147.6	50.9	120.2	90.3	65.2	75.9
Annual Runoff (cm)	64.7	6.5	46.1	36.2	24.6	20.0

5.4 Flow measurement of river Netravati at Bantwal (catchment area = 3184 km^2) yielded the following annual flow volumes:

Year	Observed annual flow (Mm^3)	Year	Observed annual flow (Mm^3)
1970–71	15925	1980–81	16585
1971–72	14813	1981–82	14649
1972–73	11726	1982–83	10662
1973–74	11818	1983–84	11555
1974–75	12617	1984–85	10821
1975–76	15704	1985–86	9466
1976–77	8334	1986–87	9732
1977–78	12864		
1978–79	16195		
1979–80	10392		

The withdrawal upstream of the gauging station [for meeting irrigation, drinking water and industrial needs are 91 Mm^3 in 1970–71 and is found to increase linearly at a rate of 2 Mm^3/year. The annual evaporation loses from water bodies on the river can be assumed to be 4 Mm^3. Estimate the 75% dependable yield at Bantwal. If the catchment area at the mouth of the river is 3222 km^2, estimate the average yield for the whole basin.

5.5 The mean monthly rainfall and temperature of a catchment near Bangalore are given below. Estimate the annual runoff volume and the corresponding runoff coefficient by using Khosla's runoff formula.

Month	Jan	Feb	Mar	Apr	May	Jun	July	Aug	Sep	Oct	Nov	Dec
Temp (°C)	24	27	32	33	31	26	24	24	23	21	20	21
Rainfall (mm)	7	9	11	45	107	71	111	137	164	153	61	13

5.6 An irrigation tank has a catchment of 900 ha. Estimate, by using Strange's method, the monthly and total runoff volumes into the tank due to following monthly rainfall values.

Month	July	Aug	Sept	Oct
Monthly Rainfall (mm)	210	180	69	215

5.7 For a 500 ha watershed in South India with predominantly non-black cotton soil, the CN_{II} has been estimated as 68. (a) If the total rainfall in the past five days is 25 cm and the season is dormant season, estimate the runoff volume due to 80 mm of rainfall in a day? (b) What would be the runoff volume if the rainfall in the past five days were 35 mm?

5.8 Estimate the values of CN_I, CN_{II} and CN_{III} for a catchment with the following land use:

Land use	Soil group C (%)	Soil group D (%)	Total % area
Cultivated land (Paddy)	30	45	75
Scrub forest	6	4	10
Waste land	9	6	15

5.9 A 400 ha watershed has predominantly black cotton soil and its CN_{II} value is estimated as 73. Estimate the runoff volume due to two consecutive days of rainfall as follows:

Day	Day 1	Day 2
Rainfall (mm)	65	80

The AMC can be assumed to be Type III.

5.10 Compute the runoff volume due to a rainfall of 15 cm in a day on a 550 ha watershed. The hydrological soil groups are 50% of group C and 50% of group D, randomly distributed in the watershed. The land use is 55% cultivated with good quality bunding and 45% waste land. Assume antecedent moisture condition of Type-III and use standard *SCS-CN* equations.

5.11 A watershed having an area 680 ha has a CN_{III} value of 77. Estimate the runoff volume due to 3 days of rainfall as below:

Day	Day 1	Day 2	Day 3
Rainfall (mm)	30	50	13

Assume the AMC at Day 1 to be of Type III. Use standard *SCS-CN* equations.

5.12 A watershed has the following land use:
   (a) 400 ha of row crop with poor hydrologic condition and
   (b) 100 ha of good pasture land
The soil is of hydrologic soil group B. Estimate the runoff volume for the watershed under antecedent moisture category III when 2 days of consecutive rainfall of 100 mm and 90 mm occur. Use standard *SCS-CN* equations.

5.13 (a) Compute the runoff from a 2000 ha watershed due to 15 cm rainfall in a day. The watershed has 35% group B soil, 40% group C soil and 25% group D soil. The land

use is 80% residential that is 65% impervious and 20% paved roads. Assume AMC II conditions.

(b) If the land were pasture land in poor condition prior to the development, what would have been the runoff volume under the same rainfall? What is the percentage increase in runoff volume due to urbanization?

[*Note:* Use standard *SCS-CN* equations.]

5.14 Discharges in a river are considered in 10 class intervals. Three consecutive years of data of the discharge in the river are given below. Draw the flow-duration curve for the river and determine the 75% dependable flow.

Discharge range (m³/s)	< 6	6.0–9.9	10 14.9	15–24.9	25–39	40–99	100–149	–150 249	250–349	>350
No. of occurrences	20	137	183	232	169	137	121	60	30	6

5.15 The average monthly inflow into a reservoir in a dry year is given below:

Month	Jun	Jul	Aug	Sep	Oct	Nov	Dec	Jan	Feb	Mar	Apr	May
Mean monthly flow (m³/s)	20	60	200	300	200	150	100	80	60	40	30	25

If a uniform discharge at 90 m³/s is desired from this reservoir what minimum storage capacity is required?

(*Hints:* Assume the next year to have similar flows as the present year.)

5.16 For the data given in Prob. 5.15, plot the flow mass curve and find:

(a) The minimum storage required to sustain a uniform demand of 70 m³/s;

(b) If the reservoir capacity is 7500 cumec-day, estimate the maximum uniform rate of withdrawal possible from this reservoir.

5.17 The following table gives the monthly inflow and contemplated demand from a proposed reservoir. Estimate the minimum storage that is necessary to meet the demand

Month	Jan	Feb	Mar	Apr	May	Jun	July	Aug	Sept	Oct	Nov	Dec
Monthly inflow (Mm³)	50	40	30	25	20	30	200	225	150	90	70	60
Monthly demand (Mm³)	70	75	80	85	130	120	25	25	40	45	50	60

5.18 For the reservoir in Prob. 5.17 the mean monthly evaporation and rainfall are given below.

Month	Jan	Feb	Mar	Apr	May	Jun	July	Aug	Sept	Oct	Nov	Dee
Evapo-ration (cm)	6	8	13	17	22	22	14	11	13	12	7	5
Rainfall (cm)	1	0	0	0	0	19	43	39	22	6	2	1

If the average reservoir area can be assumed to be 30 km^2, estimate the change in the storage requirement necessitated by this additional data. Assume the runoff coefficient of the area flooded by the reservoir as equal to 0.4.

5.19 Following is the stream flow record of a stream and covers a critical 2 year period. What is the minimum size of the reservoir required on this stream to provide a constant downstream flow of 0.07 cumecs? Use Sequent Peak Algorithm.

Month (1st Year)	Monthly Discharge (ha.m)	Month (2nd Year)	Monthly Discharge (ha.m)
Jan	57.4	Jan	10.2
Feb	65.5	Feb	30.8
March	28.6	March	43.1
April	32.8	April	53.1
May	36.9	May	38.9
June	24.6	June	28.9
July	10.2	July	16.4
Aug	2.1	Aug	12.3
Sept	2.1	Sept	12.3
Oct	2.1	Oct	4.1
Nov	4.1	Nov	8.2
Dec	8.2	Dec	2.1

5.20 Solve Problem 5.18 using Sequent Peak Algorithm method.

5.21 An unregulated stream provides the following volumes through each successive 4-day period over a 40-day duration at a possible reservoir site. What would be the reservoir capacity needed to ensure maintaining the average flow over these 40 days, if the reservoir is full to start with? What is the average flow? What would be the approximate quantity of water wasted in spillage in this case?

Day	0	4	8	12	16	20	24	28	32	36	40
Runoff volume (Mm^3)	0	9.6	5.4	2.3	3.5	2.3	2.2	1.4	6.4	12.4	10.9

5.22 A reservoir is located in a region where the normal annual precipitation is 160 cm and the normal annual US class A pan evaporation is 200 cm. The average area of reservoir water surface is 75 km^2. If under conditions of 35% of the rainfall on the land occupied by the reservoir runoff into the stream, estimate the net annual increase or decrease in the stream flow as result of the reservoir. Assume evaporation pan coefficient = 0.70.

—| OBJECTIVE QUESTIONS |—

5.1 A mean annual runoff of 1 m^3/s from a catchment of area 31.54 km^2 represents an effective rainfall of
  (a) 100 cm   (b) 1.0 cm   (e) 100 mm   (d) 3.17 cm

5.2 Direct runoff is made up of
  (a) Surface runoff, prompt interflow and channel precipitation
  (b) Surface runoff, infiltration and evapotranspiration
  (c) Overland flow and infiltration
  (d) Rainfall and evaporation

5.3 A hydrograph is a plot of
  (a) rainfall intensity against time   (b) stream discharge against time
  (c) cumulative rainfall against time   (d) cumulative runoff against time

5.4 The term *base flow* denotes
  (a) delayed groundwater flow reaching a stream
  (b) delayed groundwater and snowmelt reaching a stream
  (c) delayed groundwater and interflow
  (d) the annual minimum flow in a stream

5.5 *Virgin flow* is
  (a) the flow in the river downstream of a gauging station
  (b) the flow in the river upstream of a gauging station
  (c) the flow unaffected by works of man
  (d) the flow that would exist in the stream if there were no abstractions to the precipitation

5.6 The water year in India starts from the first day of
  (a) January   (b) April   (c) June   (d) September

5.7 An ephemeral stream
  (a) is one which always carries some flow
  (b) does not have any base flow contribution
  (c) is one which has limited contribution of groundwater in wet season
  (d) is one which carries only snow-melt water.

5.8 An intermittent stream
  (a) has water table above the stream bed throughout the year
  (b) has only flash flows in response to storms
  (c) has flows in the stream during wet season due to contribution of groundwater.
  (d) does not have any contribution of ground water at any time

5.9 Khosla's formula for monthly runoff R_m due to a monthly rainfall P_m is $R_m = P_m - L_m$ where L_m is
  (a) a constant
  (b) monthly loss and depends on the mean monthly catchment temperature
  (c) a monthly loss coefficient depending on the antecedent precipitation index
  (d) a monthly loss depending on the infiltration characteristics of the catchment

5.10 The flow-duration curve is a plot of
  (a) accumulated flow against time
  (b) discharge against time in chronological order
  (c) the base flow against the percentage of times the flow is exceeded
  (d) the stream discharge against the percentage of times the flow is equalled or exceeded.

5.11 In a flow–mass curve study the demand line drawn from a ridge in the curve did not interest the mass curve again. This represents that
  (a) the reservoir was not full at the beginning
  (b) the storage was not adequate
  (c) the demand cannot be met by the inflow as the reservoir will not refill
  (d) the reservoir is wasting water by spill.

5.12 If in a flow–mass curve, a demand line drawn tangent to the lowest point in a valley of the curve does not intersect the mass curve at an earlier time period, it represents that
  (a) the storage is inadequate
  (b) the reservoir will not be full at the start of the dry period
  (c) the reservoir is full at the beginning of the dry period
  (d) the reservoir is wasting later by spill.

5.13 The flow-mass curve is an integral curve of
  (a) the hydrograph   (b) the hyetograph
  (c) the flow duration curve   (d) the S-curve.

5.14 The total rainfall in a catchment of area 1200 km^2 during a 6-h storm is 16 cm while the surface runoff due to the storm is 1.2×10^8 m^3. The ϕ index is
  (a) 0.1 cm/h   (b) 1.0 cm/h
  (c) 0.2 cm/h   (d) cannot be estimated with the given data.

5.15 In India, a meteorological subdivision is considered to be affected by moderate drought if it receives a total seasonal rainfall which is
  (a) less than 25% of normal value
  (b) between 25% and 49% of normal value
  (c) between 50% and 74% of normal value
  (d) between 75% and 99% of normal value

5.16 An area is classified as a *drought prone area* if the probability P of occurrence of a drought is
  (a) $0.4 < P \le 1.0$ (b) $0.2 \le P \le 0.40$
  (c) $0.1 \le P < 0.20$ (d) $0.0 < P < 0.20$

5.17 In the standard SCS-CN method of modelling runoff due to daily rainfall, the maximum daily rainfall that would not produce runoff in a watershed with $CN = 50$ is about
  (a) 65 mm   (b) 35 mm   (c) 50 mm   (d) 25 mm

5.18 In the standard *SCS-CN* method, if $CN = 73$ the runoff volume for a one day rainfall of 100 mm is about
  (a) 38 mm   (b) 2 mm   (c) 56 mm   (d) 81 mm

HYDROGRAPHS

6.1 INTRODUCTION

While long-term runoff concerned with the estimation of yield was discussed in the previous chapter, the present chapter examines in detail the short-term runoff phenomenon. The storm hydrograph is the focal point of the present chapter.

Consider a concentrated storm producing a fairly uniform rainfall of duration, *D* over a catchment. After the initial losses and infiltration losses are met, the rainfall excess reaches the stream through overland and channel flows. In the process of translation a certain amount of storage is built up in the overland and channel-flow phases. This storage gradually depletes after the cessation of the rainfall. Thus there is a time lag between the occurrence of rainfall in the basin and the time when that water passes the gauging station at the basin outlet. The runoff measured at the stream-gauging station will give a typical hydrograph as shown in Fig. 6.1. The duration of the rainfall is also marked in this figure to indicate the time lag in the rainfall and runoff. The hydrograph of this kind which results due to an isolated storm is typically single-peaked skew distribution of discharge and is known variously as *storm hydrograph*, *flood hydrograph* or simply *hydrograph*. It has three characteristic regions: (i) the rising limb *AB*, joining point *A*, the starting point of the rising curve and point *B*, the point of inflection, (ii) the crest segment *BC* between the two points of inflection with a peak *P* in between, (iii) the falling limb or *depletion curve CD* starting from the second point of inflection *C*.

Hydrograph components
MA = base flow recession
AB = rising limb
BC = crest segment
CD = falling limb
DN = base flow recession

Points *B* and *C* = inflection points
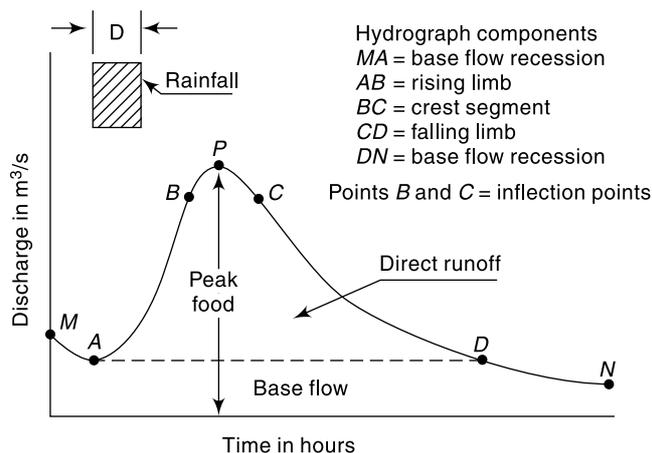
Fig. 6.1 Elements of a Flood Hydrograph

The hydrograph is the response of a given catchment to a rainfall input. It consists of flow in all the three phases of runoff, viz. surface runoff, interflow and base flow, and embodies in itself the integrated effects of a wide variety of catchment and rainfall parameters having complex interactions. Thus two different storms in a given catchment produce hydrographs differing from each other. Similarly, identical storms in two catchments produce hydrographs that are different. The interactions of various storms and catchments are in general extremely complex. If one examines the record of a large number of flood hydrographs of a stream, it will be found that many of them will have kinks, multiple peaks, etc. resulting in shapes much different from the simple single-peaked hydrograph of Fig. 6.1. These complex hydrographs are the result of storm and catchment peculiarities and their complex interactions. While it is theoretically possible to resolve a complex hydrograph into a set of simple hydrographs for purposes of hydrograph analysis, the requisite data of acceptable quality are seldom available. Hence, simple hydrographs resulting from isolated storms are preferred for hydrograph studies.

6.2   FACTORS AFFECTING FLOOD HYDROGRAPH

The factors that affect the shape of the hydrograph can be broadly grouped into climatic factors and physiographic factors. Each of these two groups contains a host of factors and the important ones are listed in Table 6.1. Generally, the climatic factors control the rising limb and the recession limb is independent of storm characteristics, being determined by catchment characteristics only. Many of the factors listed in Table 6.1 are interdependent. Further, their effects are very varied and complicated. As such only important effects are listed below in qualitative terms only.

Table 6.1   Factors Affecting Flood Hydrograph

Physiographic factors	Climatic factors
1. Basin characterstics: (a) Shape (b) size (c) slope (d) nature of the valley (e) elevation (f) drainage density	1. Storm characterstics: precipitation, intensity, duration, magnitude and movement of storm. 2. Initial loss 3. Evapotranspiration
2. Infiltration characteristics: (a) land use and cover (b) soil type and geological conditions (c) lakes, swamps and other storage 3. Channel characteristics: cross-section, roughness and storage capacity	

SHAPE OF THE BASIN

The shape of the basin influences the time taken for water from the remote parts of the catchment to arrive at the outlet. Thus the occurrence of the peak and hence the shape

of the hydrograph are affected by the basin shape. Fan-shaped, i.e. nearly semi-circular shaped catchments give high peak and narrow hydrographs while elongated catchments give broad and low-peaked hydrographs. Figure 6.2 shows schematically the hydrographs from three catchments having identical infiltration characteristics due to identical rainfall over the catchment. In catchment *A* the hydrograph is skewed to the left, i.e. the peak occurs relatively quickly. In catchment *B*, the hydrograph is skewed to the right, the peak occurring with a relatively longer lag. Catchment *C* indicates the complex hydrograph produced by a composite shape.
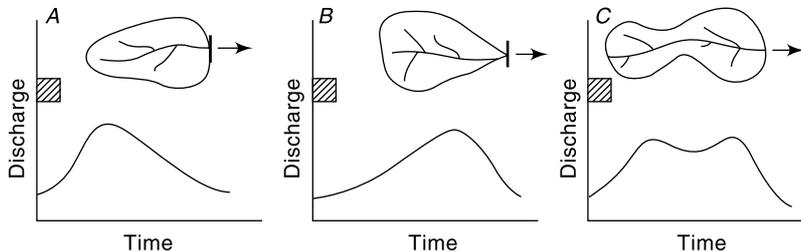
Fig. 6.2   Effect of Catchment Shape on the Hydrograph

Size

Small basins behave different from the large ones in terms of the relative importance of various phases of the runoff phenomenon. In small catchments the overland flow phase is predominant over the channel flow. Hence the land use and intensity of rainfall have important role on the peak flood. On large basins these effects are suppressed as the channel flow phase is more predominant. The peak discharge is found to vary as A^n where A is the catchment area and n is an exponent whose value is less than unity, being about 0.5. The time base of the hydro-graphs from larger basins will be larger than those of corresponding hydrographs from smaller basins. The duration of the surface runoff from the time of occurrence of the peak is proportional to A^m, where m is an exponent less than unity and is of the order of magnitude of 0.2.

Slope

The slope of the main stream controls the velocity of flow in the channel. As the recession limb of the hydrograph represents the depletion of storage, the stream channel slope will have a pronounced effect on this part of the hydrograph. Large stream slopes give rise to quicker depletion of storage and hence result in steeper recession limbs of hydrographs. This would obviously result in a smaller time base.

The basin slope is important in small catchments where the overland flow is relatively more important. In such cases the steeper slope of the catchment results in larger peak discharges.

Drainage Density

The drainage density is defined as the ratio of the total channel length to the total drainage area. A large drainage density creates situation conducive for quick disposal of runoff down the channels. This fast response is reflected in a pronounced peaked discharge. In basins with smaller drainage densities, the overland flow is predominant and the resulting hydrograph is squat with a slowly rising limb (Fig. 6.3).

LAND USE

Vegetation and forests increase the infiltration and storage capacities of the soils. Further, they cause considerable retardance to the overland flow. Thus the vegetal cover reduces the peak flow. This effect is usually very pronounced in small catchments of area less than 150 km^2. Further, the effect of the vegetal cover is prominent in small storms. In general, for two catchments of equal area, other factors being identical, the peak discharge is higher for a catchment that has a

Fig. 6.3 Role of Drainage Density on the Hydrograph

lower density of forest cover. Of the various factors that control the peak discharge, probably the only factor that can be manipulated is land use and thus it represents the only practical means of exercising long-term natural control over the flood hydrograph of a catchment.

CLIMATIC FACTORS

Among climatic factors the intensity, duration and direction of storm movement are the three important ones affecting the shape of a flood hydrograph. For a given duration, the peak and volume of the surface runoff are essentially proportional to the intensity of rainfall. This aspect is made use of in the unit hydrograph theory of estimating peak-flow hydrographs, as discussed in subsequent sections of this chapter. In very small catchments, the shape of the hydrograph can also be affected by the intensity.

The duration of storm of given intensity also has a direct proportional effect on the volume of runoff. The effect of duration is reflected in the rising limb and peak flow. Ideally, if a rainfall of given intensity i lasts sufficiently long enough, a state of equilibrium discharge proportional to iA is reached.

If the storm moves from upstream of the catchment to the downstream end, there will be a quicker concentration of flow at the basin outlet. This results in a peaked hydrograph. Conversely, if the storm movement is up the catchment, the resulting hydrograph will have a lower peak and longer time base. This effect is further accentuated by the shape of the catchment, with long and narrow catchments having hydrographs most sensitive to the storm-movement direction.

6.3   COMPONENTS OF A HYDROGRAPH

As indicated earlier, the essential components of a hydrograph are: (i) the rising limb, (ii) the crest segment, and (iii) the recession limb (Fig. 6.1). A few salient features of these components are described below.

RISING LIMB

The rising limb of a hydrograph, also known as *concentration curve* represents the increase in discharge due to the gradual building up of storage in channels and over the catchment surface. The initial losses and high infiltration losses during the early period of a storm cause the discharge to rise rather slowly in the initial periods. As the

storm continues, more and more flow from distant parts reach the basin outlet. Simultaneously the infiltration losses also decrease with time. Thus under a uniform storm over the catchment, the runoff increases rapidly with time. As indicated earlier, the basin and storm characteristics control the shape of the rising limb of a hydrograph.

CREST SEGMENT

The crest segment is one of the most important parts of a hydrograph as it contains the peak flow. The peak flow occurs when the runoff from various parts of the catchment simultaneously contribute amounts to achieve the maximum amount of flow at the basin outlet. Generally for large catchments, the peak flow occurs after the cessation of rainfall, the time interval from the centre of mass of rainfall to the peak being essentially controlled by basin and storm characteristics. Multiple-peaked complex hydrographs in a basin can occur when two or more storms occur in succession. Estimation of the peak flow and its occurrence, being important in flood-flow studies are dealt with in detail elsewhere in this book.

RECESSION LIMB

The recession limb, which extends from the point of inflection at the end of the crest segment (point C in Fig. 6.1) to the commencement of the natural groundwater flow (point D in Fig. 6.1) represents the withdrawal of water from the storage built up in the basin during the earlier phases of the hydrograph. The starting point of the recession limb, i.e. the point of inflection represents the condition of maximum storage. Since the depletion of storage takes place after the cessation of rainfall, the shape of this part of the hydrograph is independent of storm characteristics and depends entirely on the basin characteristics.

The storage of water in the basin exists as (i) surface storage, which includes both surface detention and channel storage, (ii) interflow storage, and (iii) groundwater storage, i.e. base-flow storage. Barnes (1940) showed that the recession of a storage can be expressed as

$$Q_t = Q_0 K_r^t \tag{6.1}$$

in which Q_t is the discharge at a time t and Q_0 is the discharge at $t = 0$; K_r is a recession constant of value less than unity. Equation (6.1) can also be expressed in an alternative form of the exponential decay as

$$Q_t = Q_0 e^{-at} \tag{6.1a}$$

where $a = -\ln K_r$.

The recession constant K_r can be considered to be made up of three components to account for the three types of storages as

$$K_r = K_{rs} \cdot K_{ri} \cdot K_{rb}$$

where K_{rs} = recession constant for surface storage, K_{ri} = recession constant for interflow and K_{rb} = recession constant for base flow. Typically the values of these recession constants, when time t is in days, are

$$K_{rs} = 0.05 \text{ to } 0.20 \qquad K_{ri} = 0.50 \text{ to } 0.85 \qquad K_{rb} = 0.85 \text{ to } 0.99$$

When the interflow is not significant, K_{ri} can be assumed to be unity.

If suffixes 1 and 2 denote the conditions at two time instances t_1 and t_2,

from Eq. (6.1)

$$\frac{Q_1}{Q_2} = K_r^{(t_1 - t_2)} \tag{6.2}$$

or from Eq. (6.1a)

$$\frac{Q_1}{Q_2} = e^{-a(t_1 - t_2)} \tag{6.2a}$$

Equation 6.1 (and also 6.1a) plots as a straight line when plotted on a semi-log paper with discharge on the log–scale. The slope of this line represents the recession constant. Using this property and using Eq. 6.2 (or 6.2a) the value of K_r for a basin can be estimated by using observed recession data of a flood hydrograph. Example 6.1 explains the procedure in detail.

The storage S_t remaining at any time t is obtained as

$$S_t = \int_t^\infty Q_t\, dt = \int_t^\infty Q_0\, e^{-at}\, dt = \frac{Q_t}{a} \tag{6.3}$$

EXAMPLE 6.1 *The recession limb of a flood hydrograph is given below. The time is indicated from the arrival of peak. Assuming the interflow component to be negligible, estimate the base flow and surface flow recession coefficients. Also, estimate the storage at the end of day-3.*

Time from peak (day)	Discharge (m^3/s)	Time from Peak (day)	Discharge (m^3/s)
0.0	90	3.5	5.0
0.5	66	4.0	3.8
1.0	34	4.5	3.0
1.5	20	5.0	2.6
2.0	13	5.5	2.2
2.5	9.0	6.0	1.8
3.0	6.7	6.5	1.6
		7.0	1.5

SOLUTION: The data are plotted on a semi-log paper with discharge on the log-scale. The data points from $t = 4.5$ days to 7.0 days are seen to lie on straight line (line AB in Fig. 6.4). This indicates that the surface flow terminates at $t = 4.5$ days. The best fitting exponential curve for this straight-line portion (obtained by use of MS Excel) is

$$Q_t = 11.033 e^{-0.2927t} \text{ with } R^2 = 0.9805.$$

The base flow recession coefficient K_{rb} is obtained as
ln $K_{rb} = -0.2927$ and as such $K_{rb} = 0.746$.
[Alternatively, by using the graph, the value of K_{rb} could be obtained by selecting two points 1 and 2 on the straight line AB and using Eq. (6.2)].

The base flow recession curve is extended till $t \approx 1$ day as shown by line ABM Fig. 6.4. The Surface runoff depletion is obtained by subtracting the base flow from the given recession limb of the flood hydrograph. The computations are shown in the Table given on the next page.

The surface flow values (Col. 4 of Table above) are plotted against time as shown in Fig. 6.4. It is seen that these points lie on a straight line, *XY*. The best fitting exponential curve for this straight-line portion *XY* (obtained by use of MS Excel) is

$$Q_t = 106.84 e^{-1.3603t} \text{ with } R^2 = 0.9951$$
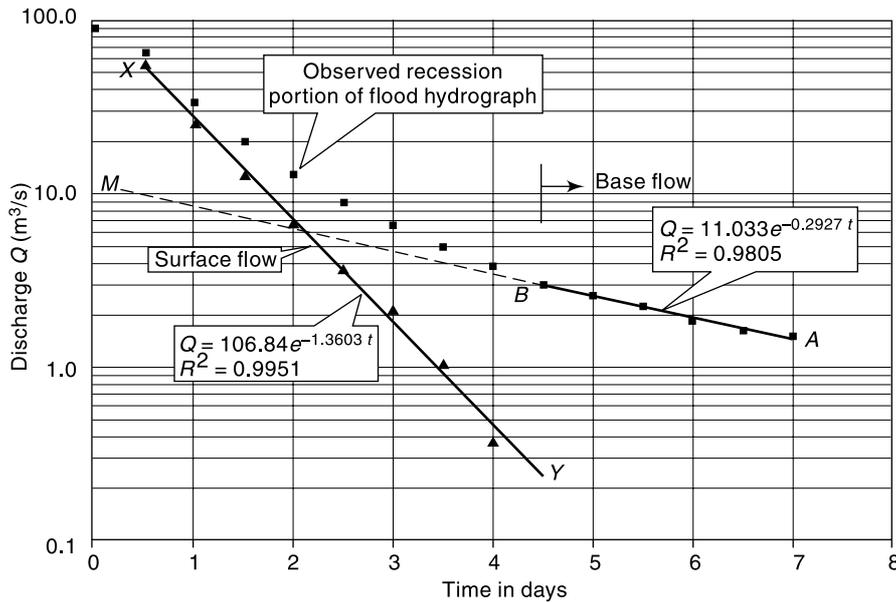
Fig. 6.4 Storage Recession Curve—Example 6.1

Time from peak (days)	Recession Limb of given flood hydrograph (m³/s)	Base flow (Obtained by using $K_{rb} = 0.746$)	Surface runoff (m³/s)
0.0	90.0		
0.5	66.0	10.455	55.545
1.0	34.0	7.945	26.055
1.5	20.0	6.581	13.419
2.0	13.0	5.613	7.387
2.5	9.0	4.862	4.138
3.0	6.7	4.249	2.451
3.5	5.0	3.730	1.270
4.0	3.8	3.281	0.519
4.5	3.0	2.884	
5.0	2.6	2.530	
5.5	2.2	2.209	
6.0	1.8	1.917	
6.5	1.6	1.647	
7.0	1.5	1.398	

The *Surface flow recession coefficient* K_{rs} is obtained as $\ln K_{rs} = -1.3603$ and as such $K_{rs} = 0.257$.
[Alternatively, by using the graph, the value of K_{rs} could be obtained by selecting two points 1 and 2 on the straight line *XY* and using Eq. (6.2)].

The storage available at the end of day-3 is the sum of the storages in surface flow and groundwater recession modes and is given by

$$S_{t3} = \left(\frac{Q_{s3}}{-\ln K_{rs}} + \frac{Q_{b3}}{-\ln K_{rb}} \right)$$

For the surface flow recession using the best fit equation:

$$Q_{s3} = 106.84e^{-1.3603 \times 3} = 1.8048; \; -\ln K_{rs} = 1.3603$$

$$\frac{Q_{s3}}{-\ln K_{rs}} = \frac{1.8048}{1.3603} = 1.3267 \text{ cumec-days}$$

Similarly for the base flow recession:

$$Q_{b3} = 11.033e^{-0.2927 \times 3} = 4.585; \; -\ln K_{rb} = 0.2927$$

$$\frac{Q_{b3}}{-\ln K_{rb}} = \frac{4.585}{0.2927} = 15.665 \text{ cumec-days}$$

Hence, total storage at the end of 3 days = S_{t3} = 1.3267 + 15.665
$$= 16.9917 \text{ cumec. days} = 1.468 \text{ Mm}^3$$

6.4 BASE FLOW SEPARATION

In many hydrograph analyses a relationship between the surface-flow hydrograph and the effective rainfall (i.e. rainfall minus losses) is sought to be established. The surface-flow hydrograph is obtained from the total storm hydrograph by separating the quick-response flow from the slow response runoff. It is usual to consider the interflow as a part of the surface flow in view of its quick response. Thus only the base flow is to be deducted from the total storm hydrograph to obtain the surface flow hydrograph.

There are three methods of base-flow separation that are in common use.

METHODS OF BASE-FLOW SEPARATION

METHOD I–STRAIGHT-LINE METHOD In this method the separation of the base flow is achieved by joining with a straight line the beginning of the surface runoff to a point on the recession limb representing the end of the direct runoff. In Fig. 6.5 point A represents the beginning of the direct runoff and it is usually easy to identify in view of the sharp change in the runoff rate at that point.

Fig. 6.5 Base Flow Seperation Methods

Point B, marking the end of the direct runoff is rather difficult to locate exactly. An empirical equation for the time interval N (days) from the peak to the point B is

$$N = 0.83A^{0.2} \tag{6.4}$$

where A = drainage area in km^2 and N is in days. Points A and B are joined by a straight line to demarcate to the base flow and surface runoff. It should be realised that the value of N obtained as above is only approximate and the position of B should be decided by considering a number of hydrographs for the catchment. This method of base-flow separation is the simplest of all the three methods.

METHOD 2 In this method the base flow curve existing prior to the commencement of the surface runoff is extended till it intersects the ordinate drawn at the peak (point C in Fig. 6.5). This point is joined to point B by a straight line. Segment AC and CB demarcate the base flow and surface runoff. This is probably the most widely used base-flow separation procedure.

METHOD 3 In this method the base flow recession curve after the depletion of the flood water is extended backwards till it intersects the ordinate at the point of inflection (line *EF* in Fig. 6.5). Points *A* and *F* are joined by an arbitrary smooth curve. This method of base-flow separation is realistic in situations where the groundwater contributions are significant and reach the stream quickly.

It is seen that all the three methods of base-flow separation are rather arbitrary. The selection of anyone of them depends upon the local practice and successful predictions achieved in the past. The surface runoff hydrograph obtained after the base-flow separation is also known as *direct runoff hydrograph* (DRH).

6.5 EFFECTIVE RAINFALL (ER)

Effective rainfall (also known as *Excess rainfall*) (ER) is that part of the rainfall that becomes direct runoff at the outlet of the watershed. It is thus the total rainfall in a given duration from which abstractions such as infiltration and initial losses are subtracted. As such, ER could be defined as that rainfall that is neither retained on the land surface nor infiltrated into the soil.

For purposes of correlating DRH with the rainfall which produced the flow, the hyetograph of the rainfall is also pruned by deducting the losses. Figure 6.6 shows the hyetograph of a storm. The initial loss and infiltration losses are subtracted from it. The resulting hyetograph is known as *effective rainfall hyetograph* (ERH). It is also known as *excess rainfall hyetograph*.
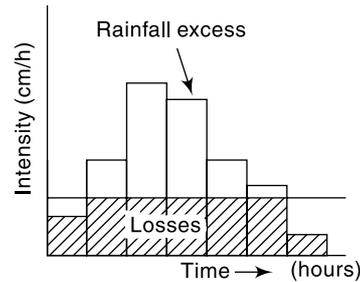
Fig. 6.6 Effective Rainfall Hyetograph (ERH)

Both DRH and ERH represent the same total quantity but in different units. Since ERH is usually in cm/h plotted against time, the area of ERH multiplied by the catchment area gives the total volume of direct runoff which is the same as the area of DRH. The initial loss and infiltration losses are estimated based on the available data of the catchment.

EXAMPLE 6.2 *Rainfall of magnitude 3.8 cm and 2.8 cm occurring on two consecutive 4-h durations on a catchment of area 27 km² produced the following hydrograph of flow at the outlet of the catchment. Estimate the rainfall excess and ϕ index.*

Time from start of rainfall (h)	−6	0	6	12	18	24	30	36	42	48	54	60	66
Observed flow (m³/s)		6	5	13	26	21	16	12	9	7	5	5	4.5	4.5

SOLUTION: The hydrograph is plotted to scale (Fig. 6.7). It is seen that the storm hydrograph has a base-flow component. For using the simple straight-line method of base-flow separation, by eg. (6.4)

$$N = 0.83 \times (27)^{0.2} = 1.6 \text{ days} = 38.5 \text{ h}$$

However, by inspection, DRH starts at $t = 0$, has the peak at $t = 12$ h and ends at $t = 48$ h (which gives a value of $N = 48 - 12 = 36$ h). As $N = 36$ h appears to be more satisfactory
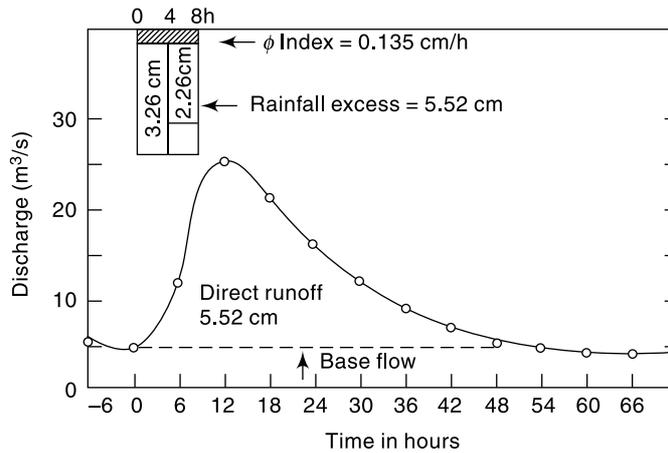
Fig. 6.7 Base Flow Separation—Example 6.2

than $N = 38.5$ h, in the present case DRH is assumed to exist from $t = 0$ to 48 h. A straight line base flow separation gives a constant value of 5 m^3/s for the base flow.

$$\text{Area of DRH} = (6 \times 60 \times 60)\left[\frac{1}{2}(8) + \frac{1}{2}(8+21) + \frac{1}{2}(21+16) + \frac{1}{2}(16+11)\right.$$

$$\left. + \frac{1}{2}(11+7) + \frac{1}{2}(7+4) + \frac{1}{2}(4+2) + \frac{1}{2}(2)\right]$$

$$= 3600 \times 6 \times (8 + 21 + 16 + 11 + 7 + 4 + 2) = 1.4904 \times 10^6 \text{ m}^3$$

$$= \text{Total direct runoff due to storm}$$

$$\text{Runoff depth} = \frac{\text{runoff volume}}{\text{catchment area}} = \frac{1.4904 \times 10^6}{27 \times 10^6} = 0.0552 \text{ m}$$

$$= 5.52 \text{ cm} = \text{rainfall excess}$$

$$\text{Total rainfall} = 3.8 + 2.8 = 6.6 \text{ cm}$$

$$\text{Duration} = 8 \text{ h}$$

$$\phi \text{ index} = \frac{6.6 - 5.52}{8} = 0.135 \text{ cm/h}$$

EXAMPLE 6.3 *A storm over a catchment of area 5.0 km^2 had a duration of 14 hours. The mass curve of rainfall of the storm is as follows:*

Time from start of storm (h)	0	2	4	6	8	10	12	14
Accumulated rainfall (cm)	0	0.6	2.8	5.2	6.6	7.5	9.2	9.6

If the ϕ index for the catchment is 0.4 cm/h, determine the effective rainfall hyetograph and the volume of direct runoff from the catchment due to the storm.

SOLUTION: First the depth of rainfall in a time interval $\Delta t = 2$ hours, in total duration of the storm is calculated, (col. 4 of Table 6.2).

Table 6.2 Calculation for Example 6.3

Time from start of storm, t (h)	Time interval Δt (h)	Accumulated rainfall in time t (cm)	Depth of rainfall in Δt (cm)	$\varphi \Delta t$ (cm)	ER (cm)	Intensity of ER (cm/h)
1	2	3	4	5	6	7
0	—	0	—	—	—	—
2	2	0.6	0.6	0.8	0	0
4	2	2.8	2.2	0.8	1.4	0.7
6	2	5.2	2.4	0.8	1.6	0.8
8	2	6.7	1.5	0.8	0.7	0.35
10	2	7.5	0.8	0.8	0	0
12	2	9.2	1.7	0.8	0.9	0.45
14	2	9.6	0.4	0.8	0	0

In a given time interval Δt, effective rainfall (ER) is given by

$$ER = (\text{actual depth of rainfall} - \phi \Delta t)$$

or $\qquad$ ER = 0, whichever is larger.

The calculations are shown in Table 6.2. For plotting the hyetograph, the intensity of effective rainfall is calculated in col. 7.

The effective rainfall hyetograph is obtained by plotting ER intensity (col. 7) against time from start of storm (col. 1), and is shown in Fig. 6.8.

Total effective rainfall = Direct runoff due to storm = area of ER hyetograph = $(0.7 + 0.8 + 0.35 + 0.45) \times 2 = 4.6$ cm

Volume of Direct runoff = $\dfrac{4.6}{1000}$
$\times 5.0 \times (1000)^2 = 23000$ m^3
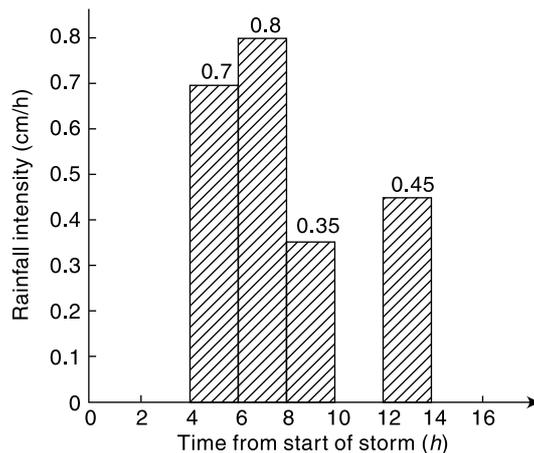
Fig. 6.8 ERH of Storm—Example 6.3

6.6 UNIT HYDROGRAPH

The problem of predicting the flood hydrograph resulting from a known storm in a catchment has received considerable attention. A large number of methods are proposed to solve this problem and of them probably the most popular and widely used method is the *unit-hydrograph method*. This method was first suggested by Sherman in 1932 and has undergone many refinements since then.

A *unit hydrograph* is defined as the hydrograph of direct runoff resulting from one unit depth (1 cm) of rainfall excess occurring uniformly over the basin and at a uniform rate for a specified duration (D hours). The term unit here refers to a unit depth of rainfall excess which is usually taken as 1 cm. The duration, being a very important characteristic, is used as a prefix to a specific unit hydrograph. Thus one has a 6-h unit hydrograph, 12-h unit hydrograph, etc. and in general a *D-h* unit hydrograph applicable to a given catchment. The definition of a unit hydrograph implies the following:

- The unit hydrograph represents the lumped response of the catchment to a unit rainfall excess of D-h duration to produce a direct-runoff hydrograph. It relates only the direct runoff to the rainfall excess. Hence the volume of water contained in the unit hydrograph must be equal to the rainfall excess. As 1 cm depth of rainfall excess is considered the area of the unit hydrograph is equal to a volume given by 1 cm over the catchment.
- The rainfall is considered to have an average intensity of *excess rainfall* (ER) of $1/D$ cm/h for the duration D-h of the storm.
- The distribution of the storm is considered to be uniform all over the catchment.

Figure 6.9 shows a typical 6-h unit hydrograph. Here the duration of the rainfall excess is 6 h.

Area under the unit hydrograph $= 12.92 \times 10^6$ m^3
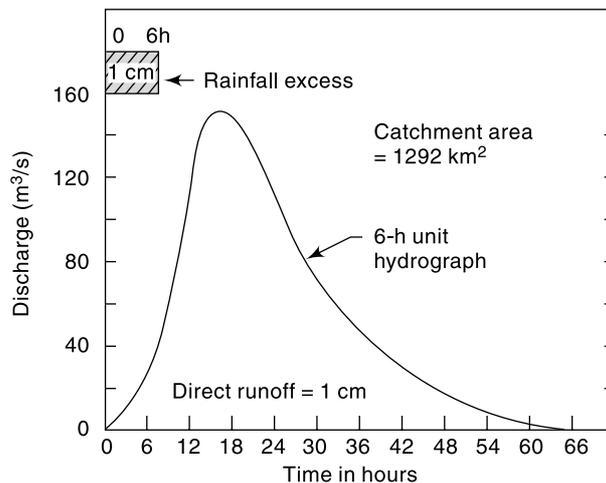
Fig. 6.9 Typical 6-h Unit Hydrograph

Hence

Catchment area of the basin $= 1292$ km^2

Two basic assumptions constitute the foundations for the unit-hydrograph theory. These are: (i) the time invariance and (ii) the linear response.

TIME INVARIANCE

This first basic assumption is that the direct-runoff response to a given effective rainfall in a catchment is time-invariant. This implies that the DRH for a given ER in a catchment is always the same irrespective of when it occurs.

LINEAR RESPONSE

The direct-runoff response to the rainfall excess is assumed to be linear. This is the most important assumption of the unit-hydrograph theory. Linear response means that if an input $x_1(t)$ causes an output $y_1(t)$ and an input $x_2(t)$ causes an output $y_2(t)$, then an input $x_1(t) + x_2(t)$ gives an output $y_1(t) + y_2(t)$. Consequently, if $x_2(t) = r\, x_1(t)$,

then $y_2(t) = r\,y_1(t)$. Thus, if the rainfall excess in a duration D is r times the unit depth, the resulting DRH will have ordinates bearing ratio r to those of the corresponding D-h unit hydrograph. Since the area of the resulting DRH should increase by the ratio r, the base of the DRH will be the same as that of the unit hydrograph.

The assumption of linear response in a unit hydrograph enables the method of superposition to be used to derive DRHs. Accordingly, if two rainfall excess of D-h duration each occur consecutively, their combined effect is obtained by superposing the respective DRHs with due care being taken to account for the proper sequence of events. These aspects resulting from the assumption of linear response are made clearer in the following two illustrative examples.

EXAMPLE 6.4 *Given below are the ordinates of a 6-h unit hydrograph for a catchment. Calculate the ordinates of the DRH due to a rainfall excess of 3.5 cm occurring in 6 h.*

Time (h)	0	3	6	9	12	15	18	24	30	36	42	48	54	60	69
UH ordinate (m³/s)	0	25	50	85	125	160	185	160	110	60	36	25	16	8	0

SOLUTION: The desired ordinates of the DRH are obtained by multiplying the ordinates of the unit hydrograph by a factor of 3.5 as in Table 6.3. The resulting DRH as also the unit hydrograph are shown in Fig. 6.10 (a). Note that the time base of DRH is not changed and remains the same as that of the unit hydrograph. The intervals of coordinates of the unit hydrograph (shown in column 1) are not in any way related to the duration of the rainfall excess and can be any convenient value.

Table 6.3 Calculation of DRH Due to 3.5 ER — Example 6.4

Time (h)	Ordinate of 6-h unit hydrograph (m³/s)	Ordinate of 3.5 cm DRH (m³/s)
1	2	3
0	0	0
3	25	87.5
6	50	175.0
9	85	297.5
12	125	437.5
15	160	560.0
18	185	647.5
24	160	560.0
30	110	385.0
36	60	210.0
42	36	126.0
48	25	87.5
54	16	56.0
60	8	28.0
69	0	0
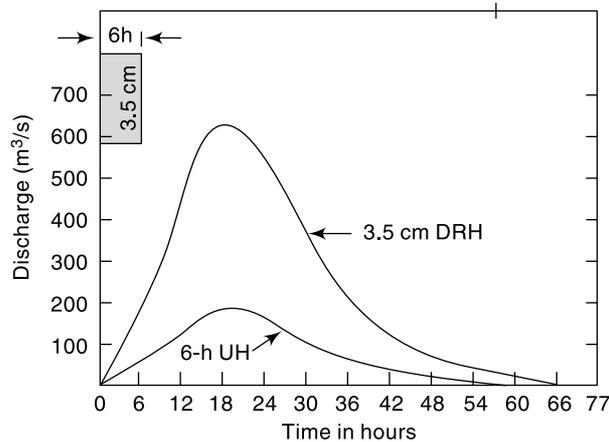
Fig. 6.10(a) 3.5 cm DRH derived from 6-h Unit Hydrograph—Example 6.4

EXAMPLE 6.5 *Two storms each of 6-h duration and having rainfall excess values of 3.0 and 2.0 cm respectively occur successively. The 2-cm ER rain follows the 3-cm rain. The 6-h unit hydrograph for the catchment is the same as given in Example 6.4. Calculate the resulting DRH.*

SOLUTION: First, the DRHs due to 3.0 and 2.0 cm ER are calculated, as in Example 6.3 by multiplying the ordinates of the unit hydrograph by 3 and 2 respectively. Noting that the 2-cm DRH occurs after the 3-cm DRH, the ordinates of the 2-cm DRH are lagged by 6 hrs as shown in column 4 of Table 6.4. Columns 3 and 4 give the proper sequence of the two DRHs. Using the method of superposition, the ordinates of the resulting DRH are obtained by combining the ordinates of the 3- and 2-cm DRHs at any instant. By this process the ordinates of the 5 cm DRH are obtained in column 5. Figure 6.10(b) shows the component 3- and 2-cm DRHs as well as the composite 5-cm DRH obtained by the method of superposition.

Table 6.4 Calculation of DRH by method of Superposition—Example 6.5

Time (h)	Ordinate of 6-h UH (m^3/s)	Ordinate of 3-cm DRH (col. 2) × 3	Ordinate of 2-cm DRH (col. 2 lagged by 6 h) × 2	Ordinate of 5-cm DRH (col. 3 + col. 4) (m^3/s)	Remarks
1	2	3	4	5	6
0	0	0	0	0	
3	25	75	0	75	
6	50	150	0	150	
9	85	255	50	305	
12	125	375	100	475	
15	160	480	170	650	
18	185	555	250	805	

(Contd.)

(*Contd.*)

(21)	(172.5)	(517.5)	(320)	(837.5)	Interpolated value
24	160	480	370	850	
30	110	330	320	650	
36	60	180	220	400	
42	36	108	120	228	
48	25	75	72	147	
54	16	48	50	98	
60	8	24	32	56	
(66)	(2.7)	(8.1)	(16)	(24.1)	Interpolated value
69	0	0	(10.6)	(10.6)	Interpolated value
75	0	0	0	0	

Note: 1. The entries in col. 4 are shifted by 6 h in time relative to col. 2.

2. Due to unequal time interval of ordinates a few entries have to be interpolated to complete the table. These interpolated values are shown in parentheses.
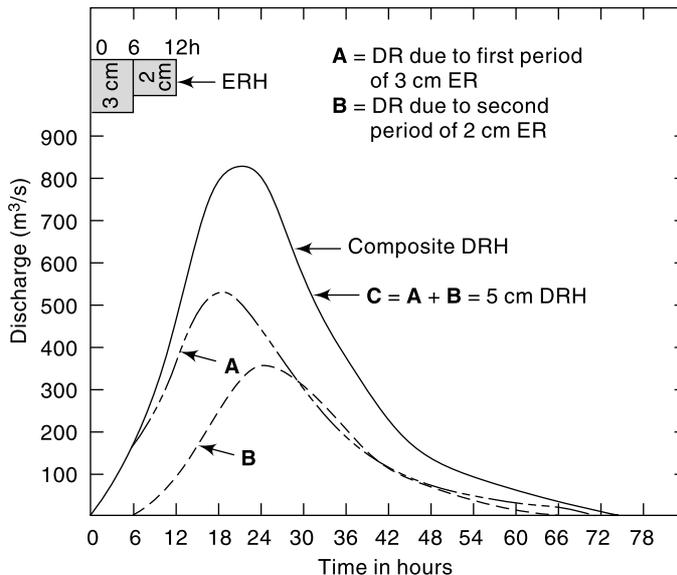
Fig. 6.10(b) Principle of Superposition—Example 6.5

APPLICATION OF UNIT HYDROGRAPH

Using the basic principles of the unit hydrograph, one can easily calculate the DRH in a catchment due to a given storm if an appropriate unit hydrograph was available. Let it be assumed that a *D-h* unit-hydrograph and the storm hyetograph are available. The initial losses and infiltration losses are estimated and deducted from the storm hyetograph to obtain the ERH (Sec. 6.5). The ERH is then divided into *M* blocks of

D-h duration each. The rainfall excess in each *D*-h duration is then operated upon the unit hydrograph successively to get the various DRH curves. The ordinates of these DRHs are suitably lagged to obtain the proper time sequence and are then collected and added at each time element to obtain the required net DRH due to the storm.

Consider Fig. 6.11 in which a sequence of *M* rainfall excess values R_1, R_2, ..., R_i, ... R_m each of duration *D*-h is shown. The line *u* [*t*] is the ordinate of a *D*-h unit hydrograph at *t* h from the beginning.
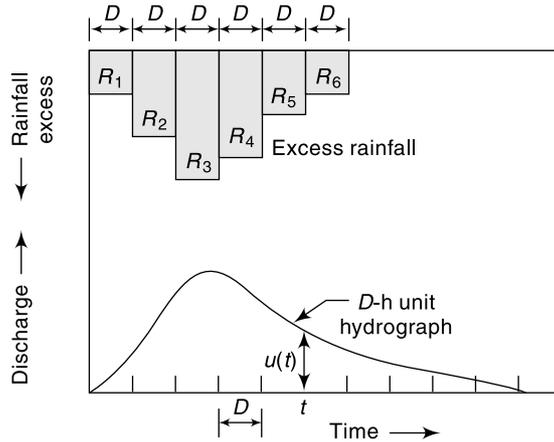
Fig. 6.11   DRH due to an ERH

The direct runoff due to R_1 at time *t* is
$$Q_1 = R_1 \cdot u[t]$$
The direct runoff due to R_2 at time (*t* – *D*) is
$$Q_2 = R_2 \cdot u\,[t - D]$$
Similarly, $Q_i = R_i \cdot u\,[t - (i - 1)\,D]$
and $Q_m = R_m \cdot u\,[t - (M - 1)\,D]$
Thus at any time *t*, the total direct runoff is
$$Q_t = \sum_{i=1}^{M} Q_i = \sum_{i=1}^{M} R_i \cdot u[t - (i - 1)\,D] \tag{6.5}$$

The arithmetic calculations of Eq. (6.5) are best performed in a tabular manner as indicated in Examples 6.5 and 6.6. After deriving the net DRH, the estimated base flow is then added to obtain the total flood hydrograph.

Digital computers are extremely useful in the calculations of flood hydrographs through the use of unit hydrograph. The electronic spread sheet (such as MS Excel) is ideally suited to perform the DRH calculations and to view the final DRH and flood hydrographs.

EXAMPLE 6.6   *The ordinates of a 6-hour unit hydrograph of a catchment is given below.*

Time (h)	0	3	6	9	12	15	18	24	30	36	42	48
Ordinate of 6-h UH	0	25	50	85	125	160	185	160	110	60	36	25

Time (h)	54	60	69
Ordinate of 6-h UH	16	8	0

Derive the flood hydrograph in the catchment due to the storm given below:

Time from start of storm (h)	0	6	12	18
Accumulated rainfall (cm)	0	3.5	11.0	16.5

The storm loss rate (ϕ – index) for the catchment is estimated as 0.25 cm/h. The base flow can be assumed to be 15 m³/s at the beginning and increasing by 2.0 m³/s for every 12 hours till the end of the direct-runoff hydrograph.

SOLUTION: The effective rainfall hyetograph is calculated as in the following table. The direct runoff hydrograph is next calculated by the method of superposition as indicated in Table 6.5. The ordinates of the unit hydrograph are multiplied by the ER values successively. The second and third set of ordinates are advanced by 6 and 12 h respectively and the ordinates at a given time interval added. The base flow is then added to obtain the flood hydrograph shown in Col 8, Table 6.6.

Interval	1st 6 hours	2nd 6 hours	3rd 6 hours
Rainfall depth (cm)	3.5	(11.0 – 3.5) = 7.5	(16.5 – 11.0) = 5.5
Loss @ 0.25 cm/h for 6 h	1.5	1.5	1.5
Effective rainfall (cm)	2.0	6.0	4.0

Table 6.5 Calculation of Flood Hydrograph due to a known *ERH – Example 6.6*

Time	Ordinates of UH	DRH due to 2 cm ER Col. 2 × 2.0	DRH due to 2 cm ER Col. 2 × 6.0 (Advanced by 6 h)	DRH due to 4 cm ER Col. 2 × 4.0 (Advanced by 12 h)	Ordinates of final DRH (Col. 3 + 4 + 5)	Base flow (m³/s)	Ordinates of flood hydro- graph (m³/s) (Col. 6 + 7)
1	2	3	4	5	6	7	8
0	0	0	0	0	0	]5	15
3	25	50	0	0	50	15	65
6	50	100	0	0	100	15	115
9	85	170	150	0	320	15	335
12	125	250	300	0	550	17	567
15	160	320	510	100	930	17	947
18	185	370	750	200	1320	17	1337
(21)	(172.5)	(345)	960	340	1645	(17)	1662
24	160	320	1110	500	1930	19	1949
(27)	(135)	(270)	(1035)	640	1945	19	1964
30	110	220	960	740	1920	19	1939
36	60	120	660	640	1420	21	1441
42	36	72	360	440	872	21	893
48	25	50	216	240	506	23	529
54	16	32	150	144	326	23	349
60	8	16	96	100	212	25	237
66	(2.7)	(5.4)	48	64	117	25	142
69	0	0	—	—	—	—	—
72		0	16	32	48	27	75
75		0	0	—	—	—	—
78		0	0	(10.8)	(11)	27	49
81				0	0	27	27
84						27	27

Note: Due to the unequal time intervals of unit hydrograph ordinates, a few entries, indicated in parentheses have to be interpolated to complete the table.

6.7 DERIVATION OF UNIT HYDROGRAPHS

A number of isolated storm hydrographs caused by short spells of rainfall excess, each of approximately same duration [0.90 to 1.1 *D* h] are selected from a study of the continuously gauged runoff of the stream. For each of these storm hydrographs, the base flow is separated by adopting one of the methods indicated in Sec. 6.4.

The area under each DRH is evaluated and the volume of the direct runoff obtained is divided by the catchment area to obtain the depth of ER. The ordinates of the various DRHs are divided by the respective ER values to obtain the ordinates of the unit hydrograph.

Flood hydrographs used in the analysis should be selected to meet the following desirable features with respect to the storms responsible for them.
- The storms should be isolated storms occurring individually.
- The rainfall should be fairly uniform during the duration and should cover the entire catchment area.
- The duration of the rainfall should be 1/5 to 1/3 of the basin lag.
- The rainfall excess of the selected storm should be high. A range of ER values of 1.0 to 4.0 cm is sometimes preferred.

A number of unit hydrographs of a given duration are derived by the above method and then plotted on a common pair of axes as shown in Fig. 6.12. Due to the rainfall variations both in space and time and due to storm departures from the assumptions of the unit hydrograph theory, the various unit hydrographs thus developed will not be identical. It is a common practice to adopt a mean of such curves as the unit hydrograph of a given duration for the catchment. While deriving the mean curve, the average of peak flows and time to peaks are first calculated. Then a mean curve of best fit, judged by eye, is drawn through the averaged peak to close on an averaged base length. The volume of DRH is calculated and any departure from unity is corrected by adjusting the value of the peak. The averaged ERH of unit depth is customarily drawn in the plot of the unit hydrograph to indicate the type and duration of rainfall causing the unit hydrograph.
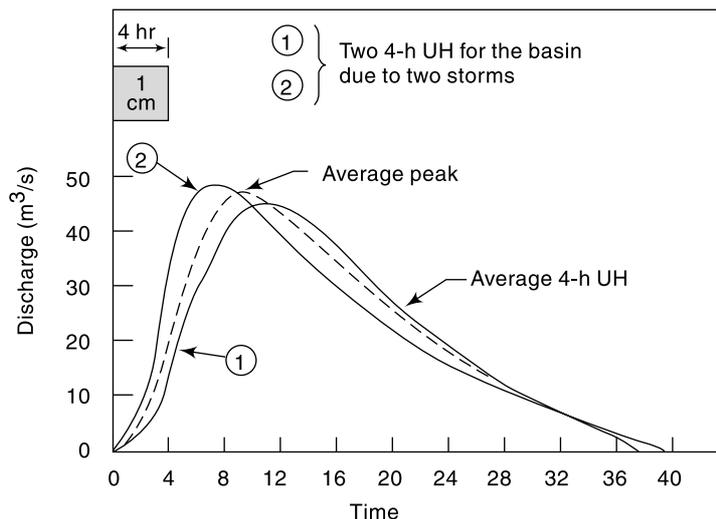
Fig. 6.12 Derivation of an Average Unit Hydrograph

By definition the rainfall excess is assumed to occur uniformly over the catchment during duration D of a unit hydrograph. An. ideal duration for a unit hydrograph is one wherein small fluctuations in the intensity of rainfall within this duration do not have any significant effect on the runoff. The catchment has a damping effect on the fluctuations of the rainfall intensity in the runoff-producing process and this damping is a function of the catchment area. This indicates that larger durations are admissible for larger catchments. By experience it is found that the duration of the unit hydrograph should not exceed 1/5 to 1/3 basin lag. For catchments of sizes larger than 250 km² the duration of 6 h is generally satisfactory.

EXAMPLE 6.7 *Following are the ordinates of a storm hydrograph of a river draining a catchment area of 423 km² due to a 6-h isolated storm. Derive the ordinates of a 6-h unit hydrograph for the catchment*

Time from start of storm (h)	−6	0	6	12	18	24	30	36	42	48
Discharge (m³/s)	10	10	30	87.5	115.5	102.5	85.0	71.0	59.0	47.5

Time from start of storm (h)	54	60	66	72	78	84	90	96	102
Discharge (m³/s)	39.0	31.5	26.0	21.5	17.5	15.0	12.5	12.0	12.0

SOLUTION: The flood hydrograph is plotted to scale (Fig. 6.13). Denoting the time from beginning of storm as t, by inspection of Fig. 6.12,
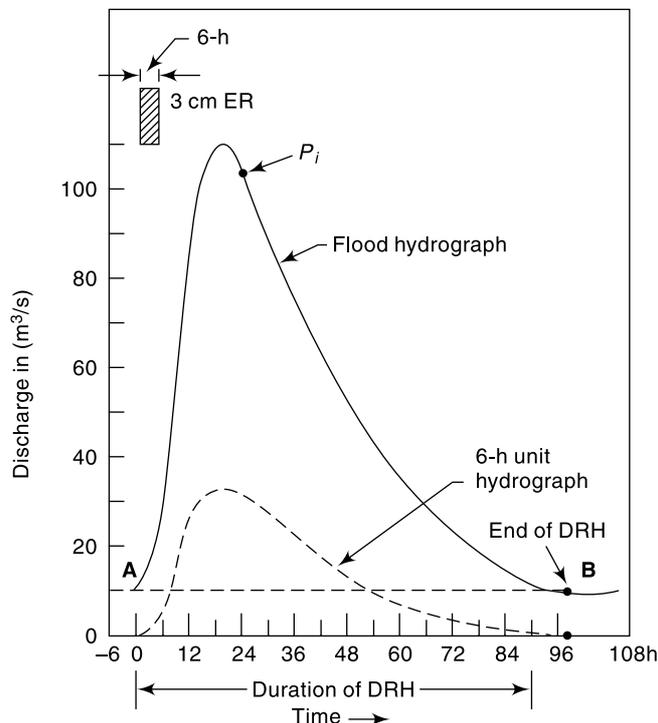
Fig. 6.13   Derivation of Unit Hydrograph from a flood Hydrograph

$$A = \text{beginning of DRH} \qquad t = 0$$
$$B = \text{end of DRH} \qquad t = 90 \text{ h}$$
$$P_m = \text{peak} \qquad t = 20 \text{ h}$$

Hence

$$N = (90 - 20) = 70 \text{ h} = 2.91 \text{ days}$$

By Eq. (6.4),

$$N = 0.83 \, (423)^{0.2} = 2.78 \text{ days}$$

However, $N = 2.91$ days is adopted for convenience. A straight line joining A and B is taken as the divide line for base-flow separation. The ordinates of DRH are obtained by subtracting the base flow from the ordinates of the storm hydrograph. The calculations are shown in Table 6.6.

$$\text{Volume of DRH} = 60 \times 60 \times 6 \times (\text{sum of DRH ordinates})$$
$$= 60 \times 60 \times 6 \times 587 = 12.68 \text{ Mm}^3$$
$$\text{Drainage area} = 423 \text{ km}^2 = 423 \text{ Mm}^2$$
$$\text{Runoff depth} = \text{ER depth} = \frac{12.68}{423} = 0.03 \text{ m} = 3 \text{ cm}.$$

The ordinates of DRH (col. 4) are divided by 3 to obtain the ordinates of the 6-h unit hydrograph (see Table 6.6).

Table 6.6 Calculation of the Ordinates of a 6-H Unit Hydrograph— Example 6.7

Time from beginning of storm (h)	Ordinate of flood hydro- graph (m³/s)	Base Flow (m³/s)	Ordinate of DRH (m³/s)	Ordinate of 6-h unit hydro- graph (Col. 4)/3
1	2	3	4	5
−6	10.0	10.0	0	0
0	10.0	10.0	0	0
6	30.0	10.0	20.0	6.7
12	87.5	10.5	77.0	25.7
18	111.5	10.5	101.0	33.7
24	102.5	10.5	101.0	33.7
30	85.0	11.0	74.0	24.7
36	71.0	11.0	60.0	20.0
42	59.0	11.0	48.0	16.0
48	47.5	11.5	36.0	12.0
54	39.0	11.5	27.5	9.2
60	31.5	11.5	20.0	
66	26.0	12.0	14.0	
72	21.5	12.0	9.5	
78	17.5	12.0	5.5	
84	15.0	12.5	2.5	
90	12.5	12.5	0	
96	12.0	12.0	0	
102	12.0	12.0	0	

EXAMPLE 6.8 *(a) The peak of flood hydrograph due to a 3-h duration isolated storm in a catchment is 270 m³/s. The total depth of rainfall is 5.9 cm. Assuming an average infiltration loss of 0.3 cm/h and a constant base flow of 20 m³/s, estimate the peak of the 3-h unit hydrograph (UH) of this catchment.*
(b) If the area of the catchment is 567 km² determine the base width of the 3-h unit hydrograph by assuming it to be triangular in shape.

SOLUTION:
(a) Duration of rainfall excess = 3 h   Loss @ 0.3 cm/h for 3 h = 0.9 cm
     Total depth of rainfall = 5.9 cm   Rainfall excess = 5.9–0.9 = 5.0 cm
 Peak flow:
     Peak of flood hydrograph = 270 m³/s   Peak of DRH = 250 m³/s
     Base flow = 20 m³/s

$$\text{Peak of 3-h unit hydrograph} = \frac{\text{peak of DRH}}{\text{rainfall excess}} = \frac{250}{5.0} = 50 \text{ m}^3/\text{s}$$

(b) Let B = base width of the 3-h UH in hours.
    Volume represented by the area of UH = volume of 1 cm depth over the catchment
           Area of UH = (Area of catchment × 1 cm)

$$\frac{1}{2} \times B \times 60 \times 60 \times 50 = 567 \times 10^6 \times \frac{1}{100}$$

$$B = \frac{567 \times 10^4}{9 \times 10^4} = 63 \text{ hours.}$$

UNIT HYDROGRAPH FROM A COMPLEX STORM

When suitable simple isolated storms are not available, data from complex storms of long duration will have to be used in unit-hydrograph derivation. The problem is to decompose a measured composite flood hydrograph into its component DRHs and base flow. A common unit hydrograph of appropriate duration is assumed to exist. This problem is thus the inverse of the derivation of flood hydrograph through use of Eq. (6.5). Consider a rainfall excess made up of three consecutive durations of *D*-h and ER values of R_1, R_2 and R_3. Figure 6.14 shows the ERR. By base flow separation of the resulting composite flood hydrograph a composite DRH is obtained (Fig. 6.14). Let the ordinates of the composite DRH be drawn at a time interval of *D*-h. At various time intervals 1*D*, 2*D*, 3*D*, … from the start of the ERH, let the ordinates of the unit hydrograph be $u_1, u_2, u_3, \ldots$ and the ordinates of the composite DRH be $Q_1, Q_2, Q_3, \ldots$,
Then

$$Q_1 = R_1 u_1$$
$$Q_2 = R_1 u_2 + R_2 u_1$$
$$Q_3 = R_1 u_3 + R_2 u_2 + R_3 u_1$$

Fig. 6.14 Unit hydrograph from a Complex Storm

$$Q_4 = R_1 u_4 + R_2 u_3 + R_3 u_2$$
$$Q_5 = R_1 u_5 + R_2 u_4 + R_3 u_3$$
$$\cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot$$

(6.6)

so on.

From Eq. (6.6) the values of $u_1, u_2, u_3, \ldots$ can be determined. However, this method suffers from the disadvantage that the errors propagate and increase as the calculations proceed. In the presence of errors the recession limb of the derived D-h unit hydrograph can contain oscillations and even negative values. Matrix methods with optimisation schemes are available for solving Eq. (6.6) in a digital computer.

6.8   UNIT HYDROGRAPHS OF DIFFERENT DURATIONS

Ideally, unit hydrographs are derived from simple isolated storms and if the duration of the various storms do not differ very much, say within a band of $\pm$ 20% D, they would all be grouped under one average duration of D-h. If in practical applications unit hydrographs of different durations are needed they are best derived from field data. Lack of adequate data normally precludes development of unit hydrographs covering a wide range of durations for a given catchment. Under such conditions a D hour unit hydrograph is used to develop unit hydrographs of differing durations nD. Two methods are available for this purpose.

- Method of superposition
- The S-curve

These are discussed below.

METHOD OF SUPERPOSITION

If a D-h unit hydrograph is available, and it is desired to develop a unit hydrograph of nD h, where n is an integer, it is easily accomplished by superposing n unit hydrographs with each graph separated from the previous on by D-h. Figure 6.15 shows three 4-h unit hydrographs A, B and C. Curve B begins 4 h after A and C begins 4-h, after B. Thus the combination of these three curves is a DRH of 3 cm due to an ER of 12-h duration. If the ordinates of this DRH are now divided by 3, one obtains a 12-h unit hydrograph. The calculations are easy if performed in a tabular form (Table 6.7).

EXAMPLE 6.9 *Given the ordinates of a 4-h unit hydrograph as below derive the ordinates of a 12-h unit hydrograph for the same catchment.*

Time (h)	0	4	8	12	16	20	24	28	32	36	40	44
Ordinate of 4-h UH	0	20	80	130	150	130	90	52	27	15	5	0

SOLUTION: The calculations are performed in a tabular form in Table 6.7. In this
   Column 3 = ordinates of 4-h UH lagged by 4-h
   Column 4 = ordinates of 4-h UH lagged by 8-h
   Column 5 = ordinates of DRH representing 3 cm ER in 12-h
   Column 6 = ordinates of 12-h UH = (Column 5)/3
The 12-h unit hydrograph is shown in Fig. 6.15.

THE S-CURVE

If it is desired to develop a unit hydrograph of duration mD, where m is a fraction, the method of superposition cannot be used. A different technique known as the S-curve method is adopted in such cases, and this method is applicable for rational values of m.

Table 6.7 Calculation of a 12-h Unit Hydrograph from a 4-H Unit Hydrograph—Example 6.9

| Time (h) | Ordinates of 4-h UH (m³/s) | | | DRH of 3 cm in 12-h (m³/s) (Col. 2+3+4) | Ordinate of 12-h UH (m³/s) (Col. 5)/3 |
	A	B Lagged by 4-h	C Lagged by 8-h		
1	2	3	4	5	6
0	0	—	—	0	0
4	20	0	—	20	6.7
8	80	20	0	100	33.3
12	130	80	20	230	76.7
16	150	130	80	360	120.0
20	130	150	130	410	136.7
24	90	130	150	370	123.3
28	52	90	130	272	90.7
32	27	52	90	169	56.3
36	15	27	52	94	31.3
40	5	15	27	47	15.7
44	0	5	15	20	6.7
48		0	5	5	1.7
52			0	0	0
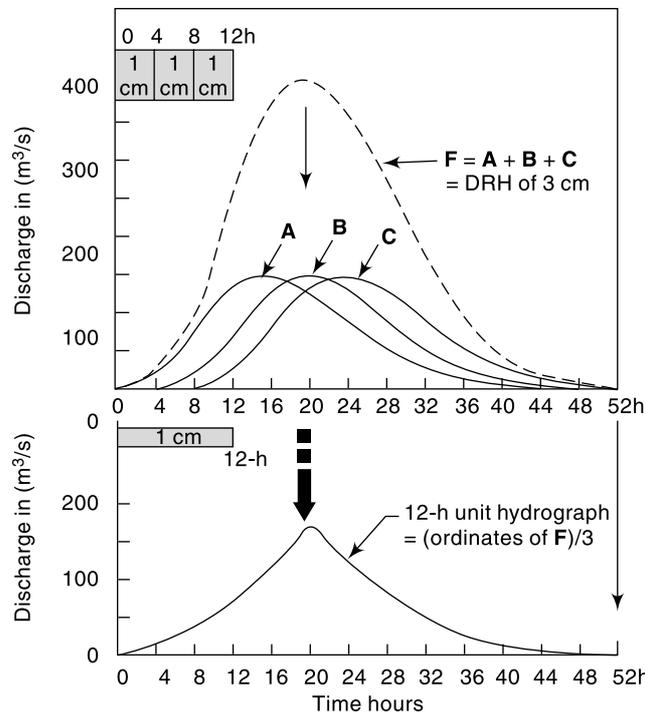
Fig. 6.15 Construction of a 12-h Unit Hydrograph from a 4-h Unit Hydrograph—Example 6.9

The *S-curve*, also known as *S-hydrograph* is a hydrograph produced by a continuous effective rainfall at a constant rate for an infinite period. It is a curve obtained by summation of an infinite series of *D*-h unit hydrographs spaced *D*-h apart. Figure 6.16 shows such a series of *D*-h hydrograph arranged with their starting points *D*-h apart. At any given time the ordinates of the various curves occurring at that time coordinate are summed up to obtain ordinates of the *S*-curve. A smooth curve through these ordinates result in an *S*-shaped curve called *S*-curve.
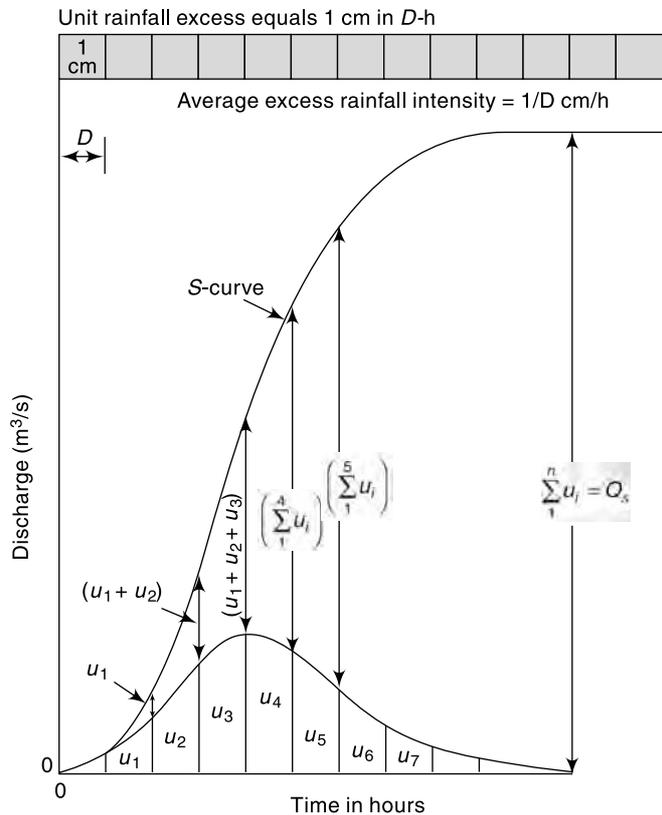
Fig. 6.16 *S*-curve

This *S*-curve is due to a *D*-h unit hydrograph. It has an initial steep portion and reaches a maximum equilibrium discharge at a time equal to the time base of the first unit hydrograph. The average intensity of ER producing the *S*-curve is $1/D$ cm/h and the equilibrium discharge,

$$Q_s = \left(\frac{A}{D} \times 10^4\right) \text{m}^3/\text{h},$$

where A = area of the catchment in km^2 and D = duration in hours of ER of the unit hydrograph used in deriving the *S*-curve. Alternatively

$$Q_s = 2.778 \frac{A}{D} \text{ m}^3/\text{s} \tag{6.7}$$

where A is the km^2 and D is in h. The quantity Q_s represents the maximum rate at which an ER intensity of $1/D$ cm/h can drain out of a catchment of area A. In actual

construction of an S-curve, it is found that the curve oscillates in the top portion at around the equilibrium value due to magnification and accumulation of small errors in the hydrograph. When it occurs, an average smooth curve is drawn such that it reaches a value Q_s at the time base of the unit hydrograph.

[**Note:** It is desirable to designate the S-curve due to D-hour unit hydrograph as S_D-curve to give an indication that the average rainfall excess of the curve is $(1/D)$ cm/h. It is particularly advantageous when more than one S-curve is used as in such cases the curves would be designated as S_{D1}, S_{D2}, ... etc. to avoid possible confusion and mistakes.]

CONSTRUCTION OF S—CURVE   By definition an S-curve is obtained by adding a string of D-h unit hydrographs each lagged by D-hours from one another. Further, if T_b = base period of the unit hydrograph, addition of only T_b/D unit hydrographs are sufficient to obtain the S-curve. However, an easier procedure based on the basic property of the S-curve is available for the construction of S-curves.

i.e. $\qquad\qquad U(t) = S(t) - S(t–D)$

or $\qquad\qquad S(t) = U(t) + S(t–D)$ $\qquad\qquad\qquad\qquad$ (6.8)

The term $S(t–D)$ could be called S-curve addition at time t so that

Ordinate of S-curve at any time t $\quad$ = Ordinate of D-h unit hydrograph at time t
$\qquad\qquad\qquad\qquad\qquad\qquad\qquad$ + S-curve addition at time t

Noting that for all $t \le D$, $S(t-D) = 0$, Eq. (6.8) provides a simple recursive procedure for computation of S-curve ordinates. The procedure is explained in Example 6.10.

EXAMPLE 6.10   *Derive the S-curve for the 4-h unit hydrograph given below.*

Time (h)	0	4	8	12	16	20	24	28
Ordinate of 4-h UH (m³/s)	0	10	30	25	18	10	5	0

SOLUTION: Computations are shown in Table 6.8. In this table col. 2 shows the ordinates of the 4-h unit hydrograph. col. 3 gives the S-curve additions and col. 4 gives the ordinates of the S-curve. The sequence of entry in col. 3 is shown by arrows. Values of entries in col. 4 is obtained by using Eq. (6.8), i.e. by summing up of entries in col. 2 and col. 4 along each row.

Table 6.8   Construction of S-curve—Example 6.10

Time in hours	Ordinate of 4-h UH	S-curve addition (m³/s)	S_4-curve ordinate (m³/s). (col. 2 + col. 3)
1	2	3	4
0	0		0
4	10	0	10
8	30	10	40
12	25	40	65
16	18	65	83
20	10	83	93
24	5	93	98
28	0	98	98

At $i = 4$ hours; Ordinate of 4-hUH = 10 m³/s.

      S-curve addition = ordinate of 4-h UH @$\{t = (4-4) \neq 0$ hours$\} = 0$

      Hence S-curve ordinate Eq. (6.8) = 10 + 0 = 10 m³/s,

At $t = 8$ hours; Ordinate of 4-hUH = 30 m³/s.

      S-curve addition = ordinate of 4-hUH @$\{t = (8-4) = 4$ hours$\} = 10$ m³/s

      Hence S-curve ordinate by Eq. (6.8) = 30 + 10 = 40 m³/s.

At $t = 12$ hours; Ordinate of 4-hUH = 25 m³/s.

      S-curve addition = ordinate of 4-hUH @$\{t = (12-4) = 48$ hours$\} = 40$ m³/s

      Hence S-curve ordinate by Eq. (6.8) = 25 + 40 = 65 m³/s.

This calculation is repeated for all time intervals till t = base width of UH = 28 hours. Plots of the 4-h UH and the derived S-curve are shown in Fig. 6.17.
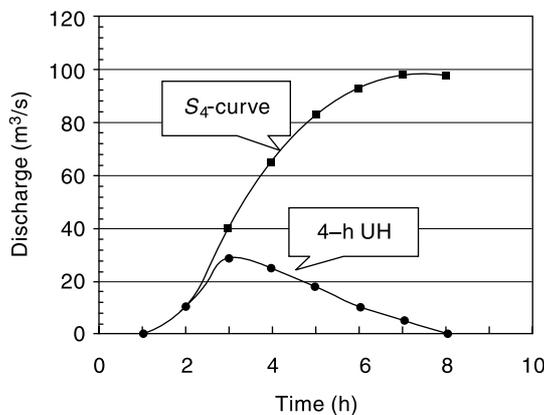

Fig. 6.17   Construction of S_4-curve — (Example 6.10)

DERIVATION OF T-HOUR UNIT HYDROGRAPH

Consider two D-h S-curves A and B displaced by T-h (Fig. 6.18). If the ordinates of B are subtracted from that of A, the resulting curve is a DRH produced by a rainfall
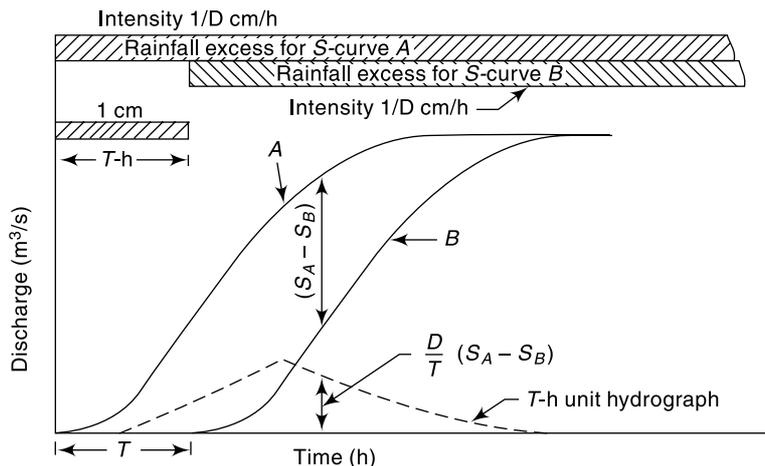

Fig. 6.18   Derivation of a T-h Unit Hydrograph by S-curve Lagging Method

excess of duration T-h and magnitude $\left(\dfrac{1}{D} \times T\right)$ cm. Hence if the ordinate differences of A and B, i.e. $(S_A - S_B)$ are divided by T/D, the resulting ordinates denote a hydrograph due to an ER of 1 cm and of duration T-h, i.e. a T-h unit hydrograph. The derivation of a T-h unit hydrograph as above can be achieved either by graphical means or by arithmetic computations in a tabular form as indicated in Example 6.11.

EXAMPLE 6.11 *Solve Example 6.9 by the S-Curve method.*

SOLUTION: Computations are shown in Table 6.9. Column 2 shows the ordinates of the 4-h unit hydrograph. Column 3 gives the S-curve additions and Column 4 the S-curve ordinates. The sequence of additions are shown by arrows. At $t = 4$ h, ordinate of the 4-h UH = ordinate of the S-curve. This value becomes the S-curve addition at $t = 2 \times 4 = 8$ h. At this $t = 8$ h, the ordinate of UH (80) + S-curve addition (20) = S-curve ordinate (100). The S-curve addition at $3 \times 4 = 12$ h is 100, and so on. Column 5 shows the S-curve lagged by 12 h. Column 6 gives the ordinate of DRH of (T/D) = 3 cm. Ordinates shown in Column 6 are divided by (T/D = 3) to obtain the ordinates of the 12-h unit hydrograph shown in Column 7.

Table 6.9 Determination of a 12-H Unit Hydrograph by S-Curve Method — Example 6.11

Time (h)	Ordinate of 4-h UH (m³/s)	S-curve addition (m³/s)	S-curve ordinate (m³/s) (Col. 2 + Col. 3)	S-curve lagged by 12 h (m³/s)	(Col. 4 – Col. 5)	Col. 6 / (12/4) = 12-h UH ordinates (m³/s)
1	2	3	4	5	6	7
0	0	—	0	—	0	0
4	20	0	20	—	20	6.7
8	80	20	100	—	100	33.3
12	130	100	230	0	230	76.7
16	150	230	380	20	360	120.0
20	130	380	510	100	410	136.7
24	90	510	600	230	370	123.3
28	52	600	652	380	272	90.7
32	27	652	679	510	169	56.3
36	15	679	694	600	94	31.3
40	5	694	699	652	47	15.7
44	0	699	699	679	20	6.7
48		699	699	694	5	1.7
52			699	699	0	0

EXAMPLE 6.12 *Ordinates of a 4-h unit hydrograph are given. Using this derive the ordinates of a 2-h unit hydrograph for the same catchment.*

Time (h)	0	4	8	12	16	20	24	28	32	36	40	44
Ordinate or 4-h UH (m³/s)	0	20	80	130	150	130	90	52	27	15	5	0

SOLUTION: In this case the time interval of the ordinates of the given unit hydrograph should be at least 2 h. As the given ordinates are at 4-h intervals, the unit-hydrograph is plotted and its ordinates at 2-h intervals determined. The ordinates are shown in column 2 of Table 6.10. The S-curve additions and S-curve ordinates are shown in columns 3 and 4 respectively. First, the S-curve ordinates corresponding to the time intervals equal to successive durations of the given unit hydrograph (in this case at 0, 4, 8, 12 … h) are determined by following the method of Example 6.11. Next, the ordinates at intermediate intervals (viz. at $t = 2, 6, 10, 14 … h$) are determined by having another series of S-curve additions. The sequence of these are shown by distinctive arrows in Table 6.9. To obtain a 2-h unit hydrograph the S-curve is lagged by 2 h (column 5) and this is subtracted from column 4 and the results listed in column 6. The ordinates in column 6 are now divided by $T/D = 2/4 = 0.5$, to obtain the required 2-h unit hydrograph ordinates, shown in column 7.

Table 6.10 Determination of 2-h Unit Hydrograph from A 4-h Unit Hydrograph—Example 6.12

Time (h)	Ordinate of 4-h UH (m³/s)	S-curve addition (m³/s)	S-curve ordinate (Col. (2) + (3)) (m³/s)	S-curve lagged by 2 h	(Col. (4) – Col. (5)) DRH of $\left(\dfrac{2}{4}\right) = 0.5$ cm	2-h UH ordinates Col. (6) (2/4) (m³/s)
1	2	3	4	5	6	7
0	0	—	0	—	0	0
2	8	—	8	0	8	16
4	20	0	20	8	12	24
6	43	8	51	20	31	62
8	80	20	100	51	49	98
10	110	51	161	100	61	122
12	130	100	230	161	69	138
14	146	161	307	230	77	154
16	150	230	380	307	73	146
18	142	307	449	380	69	138
20	130	380	510	449	61	122
22	112	449	561	510	51	102
24	90	510	600	561	39	78
26	70	561	631	600	31	62
28	52	600	652	631	21	42
30	38	631	669	652	17	34
32	27	652	679	669	10	20
34	20	669	689	679	10	(20)15
36	15	679	694	689	5	(10)10
38	10	689	699	694	5	(10)6
40	5	694	699	699	(0)	(0)3
42	2	699	701	699	(2)	(4)0
44	0	699	699	701	(–2)	(–4)0

Final adjusted values are given in col. 7.
Unadjusted values are given in parentheses.

The errors in interpolation of unit hydrograph ordinates often result in oscillation of S-curve at the equilibrium value. This results in the derived *T-h* unit hydrograph having an abnormal sequence of discharges (sometimes even negative values) at the tail end. This is adjusted by fairing the S-curve and also the resulting *T*-h unit-hydrograph by smooth curves. For example, in the present example the 2-h unit hydrograph ordinates at time > 36-h are rather abnormal. These values are shown in parentheses. The adjusted values are entered in column 7.

6.9   USE AND LIMITATIONS OF UNIT HYDROGRAPH

As the unit hydrographs establish a relationship between the ERH and DRH for a catchment, they are of immense value in the study of the hydrology of a catchment. They are of great use in (i) the development of flood hydrographs for extreme rainfall magnitudes for use in the design of hydraulic structures, (ii) extension of flood-flow records based on rainfall records, and (iii) development of flood forecasting and warning systems based on rainfall.

Unit hydrographs assume uniform distribution of rainfall over the catchment. Also, the intensity is assumed constant for the duration of the rainfall excess. In practice, these two conditions are never strictly satisfied. Non-uniform areal distribution and variation in intensity within a storm are very common. Under such conditions unit hydrographs can still be used if the areal distribution is consistent between different storms. However, the size of the catchment imposes an upper limit on the applicability of the unit hydrograph. This is because in very large basins the centre of the storm can vary from storm to storm and each can give different DRHs under otherwise identical situations. It is generally felt that about 5000 km^2 is the upper limit for unit-hydrograph use. Flood hydrographs in very large basins can be studied by dividing them into a number of smaller subbasins and developing DRHs by the unit-hydrograph method. These DRHs can then be routed through their respective channels to obtain the composite DRH at the basin outlet.

There is a lower limit also for the application of unit hydrographs. This limit is usually taken as about 200 ha. At this level of area, a number of factors affect the rainfall-runoff relationship and the unit hydrograph is not accurate enough for the prediction of DRH.

Other limitations to the use of unit hydrographs are:
- Precipitation must be from rainfall only. Snow-melt runoff cannot be satisfactory represented by unit hydrograph.
- The catchment should not have unusually large storages in terms of tanks, ponds, large flood-bank storages, etc. which affect the linear relationship between storage and discharge.
- If the precipitation is decidedly nonuniform, unit hydrographs cannot be expected to give good results.

In the use of unit hydrographs very accurate reproduction of results should not be expected. Variations in the hydrograph base of as much as ±20% and in the peak discharge by ±10% are normally considered acceptable.

6.10   DURATION OF THE UNIT HYDROGRAPH

The choice of the duration of the unit hydrograph depends on the rainfall records. If recording raingauge data are available any convenient time depending on the size of

the basin can be used. The choice is not much if only daily rainfall records are available. A rough guide for the choice of duration D is that it should not exceed the least of (i) the time of rise, (ii) the basin lag, and (iii) the time of concentration. A value of D equal to about 1/4 of the basin lag is about the best choice. Generally, for basins with areas more than 1200 km^2 a duration D = 12 hours is preferred.

6.11 DISTRIBUTION GRAPH

The distribution graph introduced by Bernard (1935) is a variation of the unit hydrograph. It is basically a D-h unit hydrograph with ordinates showing the percentage of the surface runoff occurring in successive periods of equal time intervals of D-h. The duration of the rainfall excess (D-h) is taken as the unit interval and distribution-graph ordinates are indicated at successive such unit intervals. Figure
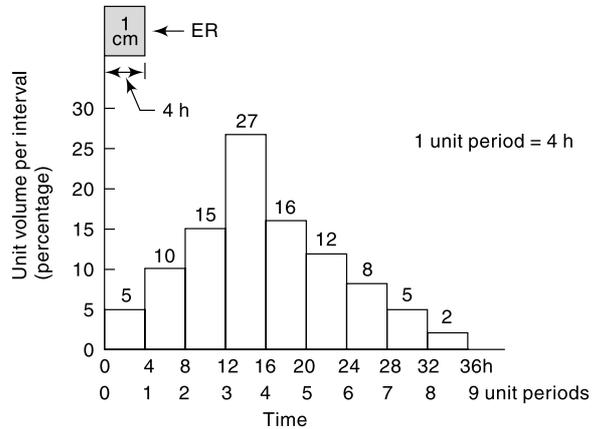
Fig. 6.19 Four-hour Distribution Graph

6.19 shows a typical 4-h distribution graph. Note the ordinates plotted at 4-h intervals and the total area under the distribution graph adds up to 100%. The use of the distribution graph to generate a DRH for a known ERH is exactly the same as that of a unit hydrograph (Example 6.13). Distribution graphs are useful in comparing the runoff characteristics of different catchments.

EXAMPLE 6.13 *A catchment of 200 hectares area has rainfalls of 7.5 cm, 2.0 cm and 5.0 cm in three consecutive days. The average ϕ index can be assumed to be 2.5 cm/day. Distribution-graph percentages of the surface runoff which extended over 6 days for every rainfall of 1-day duration are 5, 15, 40, 25, 10 and 5. Determine the ordinates of the discharge hydrograph by neglecting the base flow.*

SOLUTION: The calculations are performed in a tabular form in Table 6.11.

Table 6.11 Calculation of DRH using Distribution Graph—Example 6.13

Time interval (days)	Rainfall (cm)	Infiltration loss (cm)	Effective rainfall (cm)	Average distribuition ratio (percent)	Distributed runoff for rainfall excess of			Runoff	
					5 cm	0	2.5 cm	cm	m³/s × 10⁻²
0–1	7.5	2.5	5.0	5	0.250	0		0.250	5.79
1–2	2.0	2.5	0	15	0.750	0	0	0.750	17.36
2–3	5.0	2.5	2.5	40	2.000	0	0.125	2.750	49.19

(*Contd.*)

(*Contd.*)

3–4			25	1.250	0	0.375	2.125	37.62
4–5			10	0.500	0	1.000	1.625	34.72
5–6			5	0.250	0	0.625	1.500	20.25
6–7			0	0	0	0.250	0.875	5.79
7–8					0	0.125	0.250	2.89
8–9						0	0.125	0

$$[\text{Runoff of 1 cm in 1 day} = \frac{200 \times 100 \times 100}{86400 \times 100} \, \text{m}^3\text{/s for 1 day} = 0.23148 \, \text{m}^3\text{/s for 1 day}]$$

(The runoff ordinates are plotted at the mid-points of the respective time intervals to obtain the DRH)

6.12 SYNTHETIC UNIT HYDROGRAPH

INTRODUCTION

To develop unit hydrographs to a catchment, detailed information about the rainfall and the resulting flood hydrograph are needed. However, such information would be available only at a few locations and in a majority of catchments, especially those which are at remote locations, the data would normally be very scanty. In order to construct unit hydrographs for such areas, empirical equations of regional validity which relate the salient hydrograph characteristics to the basin characteristics are available. Unit hydrographs derived from such relationships are known as *synthetic-unit hydrographs*. A number of methods for developing synthetic-unit hydrographs are reported in literature. It should, however, be remembered that these methods being based on empirical correlations are applicable only to the specific regions in which they were developed and should not be considered as general relationships for use in all regions.

SNYDER'S METHOD

Snyder (1938), based on a study of a large number of catchments in the Appalachian Highlands of eastern United States developed a set of empirical equations for synthetic-unit hydrographs in those areas. These equations are in use in the USA, and with some modifications in many other countries, and constitute what is known as *Snyder's synthetic-unit hydrograph.*

The most important characteristic of a basin affecting a hydrograph due to a storm is *basin lag.* While actually basin lag (also known as *lag time*) is the time difference between the centroid of the input (rainfall excess) and the output (direct runoff hydrograph), because of the difficulty in determining the centroid of the direct runoff hydrograph (DRH) it is defined for practical purposes as the elapsed time between the centroid of rainfall excess and peak of DRH. Physically, lag time represents the mean time of travel of water from all parts of the watershed to the outlet during a given storm. Its value is determined essentially on the topographical features, such as the size, shape, stream density, length of main stream, slope, land use and land cover. The modified definition of basin time is very commonly adopted in the derivation of synthetic unit hydrographs for a given watershed.

The first of the Snyder's equation relates the basin lag t_p, defined as the time interval from the mid-point of rainfall excess to the peak of the unit hydrograph (Fig. 6.20), to the basin characteri-stics as

$$t_p = C_t(LL_{ca})^{0.3} \qquad (6.9)$$

where t_p = basin lag in hours
L = basin length measured along the water course from the basin divide to the gauging station in km

Fig. 6.20   Elements of a Synthetic Unit Hydrograph

L_{ca} = distance along the main water course from the gauging station to a point opposite to the watershed centroid in km

C_t = a regional constant representing watershed slope and storage effects.

The value of C_t in Snyder's study ranged from 1.35 to 1.65. However, studies by many other investigators have shown that C_t depends upon the region under study and wide variations with the value of C_t ranging from 0.3 to 6.0 have been reported[6].

Linsley et al.[5] found that the basin lag t_p is better correlated with the catchment parameter $\left(\dfrac{LL_{ca}}{\sqrt{S}}\right)$ where S = basin slope. Hence, a modified form of Eq. (6.9) was suggested by them as

$$t_p = C_{tL}\left(\frac{LL_{ca}}{\sqrt{S}}\right)^n \qquad (6.10)$$

where C_{tL} and n are basin constants. For the basins in the USA studied n by them n was found to be equal to 0.38 and the values of C_{tL} were 1.715 for mountainous n drainage areas, 1.03 for foot-hill drainage areas and 0.50 for valley drainage areas.

Snyder adopted a standard duration t_r hours of effective rainfall given by

$$t_r = \frac{t_p}{5.5} \qquad (6.11)$$

The peak discharge Q_{ps} (m³/s) of a unit hydrograph of *standard duration* t_r h is given by Snyder as

$$Q_{ps} = \frac{2.78\,C_p\,A}{t_p} \qquad (6.12)$$

where A = catchment area in km² and C_p = a regional constant. This equation is based on the assumption that the peak discharge is proportional to the average discharge of $\left(\dfrac{1\text{ cm} \times \text{catchment area}}{\text{duration of rainfall excess}}\right)$. The values of the coefficient C_p range from 0.56 to 0.69 for Snyder's study areas and is considered as an indication of the retention and storage capacity of the watershed. Like C_t, the values of C_p also vary quite considerably
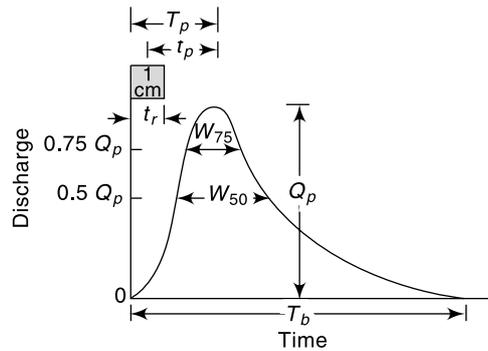
depending on the characteristics of the region and values of C_p in the range 0.31 to 0.93 have been reported.

If a non-standard rainfall duration t_R h is adopted, instead of the standard value t_r to derive a unit hydrograph the value of the basin lag is affected. The modified basin lag is given by

$$t_p' = t_p + \frac{t_R - t_r}{4} = \frac{21}{22} t_p + \frac{t_R}{4} \tag{6.13}$$

where t_p' = basin lag in hours for an effective duration of t_R h and t_p is as given by Eq. (6.9) or (6.10). The value of t_p' must be used instead of t_p in Eq. (6.11). Thus the peak discharge for a nonstandard ER of duration t_R is in m^3/s

$$Q_p = 2.78 \, C_p \, A/t_p' \tag{6.12a}$$

Note that when $t_R = t_r$

$$Q_p = Q_{ps}$$

The time base of a unit hydrograph (Fig. 6.20) is given by Synder as

$$T_b = 3 + \frac{t_p'}{8} \text{ days} = (72 + 3t_p') \text{ hours} \tag{6.14}$$

where T_b = time base. While Eq. (6.14) gives reasonable estimates of T_b for large catchments, it may give excessively large values of the time base for small catchments. Taylor and Schwartz[1] recommend

$$T_b = 5\left(t_p' + \frac{t_R}{2}\right) \text{ hours} \tag{6.15}$$

with t_b (given in h) taken as the next larger integer value divisible by t_R, i.e. T_b is about five times the time-to-peak.

To assist in the sketching of unit hydrographs, the widths of unit hydrographs at 50 and 75% of the peak (Fig. 6.20) have been found for US catchments by the US Army Corps of Engineers. These widths (in time units) are correlated to the peak discharge intensity and are given by

$$W_{50} = \frac{5.87}{q^{1.08}} \tag{6.16}$$

and $\qquad W_{75} = W_{50}/1.75 \tag{6.17}$

where

W_{50} = width of unit hydrograph in h at 50% peak discharge
W_{75} = width of unit hydrograph in h at 75% peak discharge
$q = Q_p/A$ = peak discharge per unit catchment area in $m^3/s/km^2$

Since the coefficients C_t and C_p vary from region to region, in practical applications it is advisable that the value of these coefficients are determined from known unit hydrographs of a meteorologically homogeneous catchment and then used in the basin under study. This way Snyder's equations are of use in scaling the hydrograph information from one catchment to another similar catchment.

EXAMPLE 6.14 *Two catchments A and B are considered meteorologically similar. Their catchment characteristics are given below.*

Catchment A	Catchment B
L = 30 km	L = 45 km
L_{ca} = 15 km	L_{ca} = 25 km
A = 250 km^2	A = 400 km^2

For catchment A, a 2-h unit hydrograph was developed and was found to have a peak discharge of 50 m^3/s. The time to peak from the beginning of the rainfall excess in this unit hydrograph was 9.0 h. Using Snyder's method, develop a unit hydrograph for catchment B.

SOLUTION: **For Catchment A:**

$$t_R = 2.0 \text{ h}$$

Time to peak from beginning of ER

$$T_p = \frac{t_R}{2} + t'_p = 9.0 \text{ h}$$

∴ $t'_p = 8.0 \text{ h}$

From Eq. (6.13),

$$t'_p = \frac{21}{22}t_p + \frac{t_R}{4} = \frac{21}{22}t_p + 0.5 = 8.0$$

$$t_p = \frac{7.5 \times 22}{21} = 7.857 \text{ h}$$

From Eq. (6.9),

$$t_p = C_t(L\,L_{ca})^{0.3} \qquad 7.857 = C_t(30 \times 15)^{0.3} \qquad C_t = 1.257$$

From Eq. (6.12a),

$$Q_p = 2.78\,C_p\,A/t'_p \qquad 50 = 2.78 \times C_p \times 250/8.0 \qquad C_p = 0.576$$

For Catchment B: Using the values of C_t = 1.257 and C_p = 0.576 in catchment B, the parameters of the synthetic-unit hydrograph for catchment B are determined. From Eq. (6.9),

$$t_p = 1.257\,(45 \times 25)^{0.3} = 10.34 \text{ h}$$

By Eq. (6.11),

$$t_r = \frac{10.34}{5.5} = 1.88 \text{ h}$$

Using t_R = 2.0 h, i.e. for a 2-h unit hydrograph, by Eq. (6.12),

$$t'_p = 10.34 \times \frac{21}{22} + \frac{2.0}{4} = 10.37 \text{ h}$$

By Eq. (6.12a),

$$Q_p = \frac{2.78 \times 0.576 \times 400}{10.37} = 61.77 \text{ m}^3/\text{s, say 62 m}^3/\text{s}$$

From Eq. (6.16),

$$W_{50} = \frac{5.87}{(62/400)^{1.08}} = 44 \text{ h}$$

By Eq. (6.17),

$$W_{75} = \frac{44}{1.75} = 25 \text{ h}$$

Time base: From Eq. (6.14), $T_b = 72 + (3 \times 10.37) = 103$ h

From Eq. (6.14), $T_b = 5 (10.37 + 10) \approx 58$ h

Considering the values of W_{50} and W_{75} and noting that the area of catchment B is rather small, $T_b \approx 58$ h is more appropriate in this case.

FINALIZING OF SYNTHETIC-UNIT HYDROGRAPH After obtaining the values of Q_p, t_R, t'_p, W_{75}, W_{50} and T_b from Snyder's equations, a tentative unit hydrograph is sketched and S-curve is then developed and plotted. As the ordinates of the unit hydrograph are tentative, the S-curve thus obtained will have kinks. These are then smoothened and a logical pattern of the S-curve is sketched. Using this S-curve t_R hour unit hydrograph is then derived back. Further, the area under the unit hydrograph is checked to see that it represents 1 cm of runoff. The procedure of adjustments through the S-curve is repeated till satisfactory results are obtained. It should be noted that out of the various parameters of the synthetic unit hydrograph the least accurate will be the time base T_b and this can be changed to meet other requirements.

SCS DIMENSIONLESS UNIT HYDROGRAPH

Dimensionless unit hydrographs based on a study of a large number of unit hydrographs are recommended by various agencies to facilitate construction of synthetic unit hydrographs. A typical dimensionless unit hydrograph developed by the US Soil Conservation Services (SCS) is shown in Fig. 6.21(a). In this the ordinate is (Q/Q_p) which is the discharge Q expressed as a ratio to the peak discharge Q_p, and the abscissa is (t/T_p), which is the time t expressed as a ratio of the time to peak T_p. By definition, $Q/Q_p = 1.0$ when $t/T_p = 1.0$. The coordinates of the SCS dimensionless unit hydrograph is given in Table 6.12 for use in developing a synthetic unit hydrograph in place of Snyder's equations (6.14) through (6.17).

Table 6.12 Coordinates of SCS Dimensionless Unit Hydrograph[4]

t/T_p	Q/Q_p	t/T_p	Q/Q_p	t/T_p	Q/Q_p
0.0	0.000	1.10	0.980	2.80	0.098
0.1	0.015	1.20	0.92	3.00	0.074
0.2	0.075	1.30	0.840	3.50	0.036
0.3	0.160	1.40	0.750	4.00	0.018
0.4	0.280	1.50	0.660	4.50	0.009
0.5	0.430	1.60	0.560	5.00	0.004
0.6	0.600	1.80	0.420		
0.7	0.770	2.00	0.320		
0.8	0.890	2.20	0.240		
0.9	0.970	2.40	0.180		
1.0	1.000	2.60	0.130		

SCS TRIANGULAR UNIT HYDRO-GRAPH The value of Q_p and T_p may be estimated using a simplified model of a triangular unit hydrograph (Fig. 6.21(b)) suggested by SCS. This triangular unit hydrograph has the same percentage of volume on the rising side as the dimensionless unit hydrograph of Fig. 6.21(a).
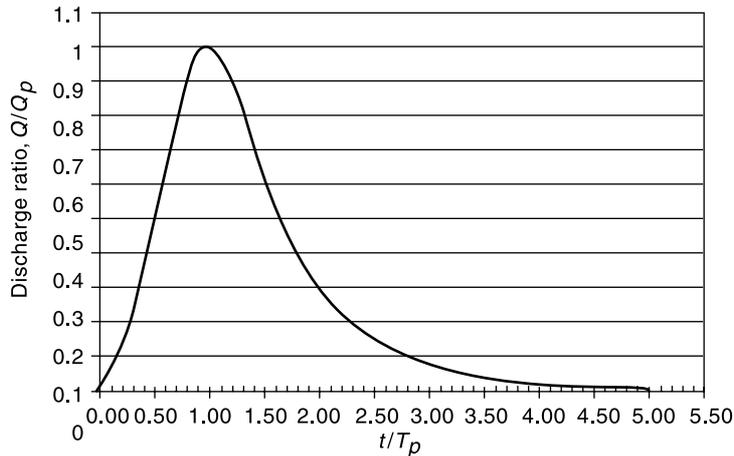
Fig. 6.21(a) Dimensionless SCS Unit Hydrograph

In Fig. 6.21(b),

Q_p = peak discharge in m^3/s

t_r = duration of effective rainfall

T_p = time of rise = time to peak = $(t_r/2) + t_p$

t_p = lag time

T_b = base length

SCS suggests that the time of recession = $(T_b - T_p) = 1.67\ T_p$

Thus $T_b = 2.67\ T_p$

Since the area under the unit hydrograph is equal to 1 cm,

If A = area of the watershed in km^2,

Fig. 6.21(b) SCS Triangular Unit Hydrograph

$$\frac{1}{2}Q_F \times (2.67 T_p) \times (3600) = \frac{1}{100} \times A \times 10^6$$

$$Q_p = \frac{2A \times 10^4}{3600 \times 2.67 T_p} = 2.08 \frac{A}{T_p} \qquad (6.18)$$

Further on the basis of a large number of small rural watesheds, SCS found that $t_p \approx 0.6\ t_c$, where t_c = time of concentration (described in detail in Sec. 7.2, Chapter 7).

Thus $$T_p = \left(\frac{t_r}{2} + 0.6 t_c\right) \qquad (6.19)$$

The SCS triangular unit hydrograph is a popular method used in watershed development activities, especially in small watersheds.

EXAMPLE 6.15 *Develop a 30 minute SCS triangular unit hydrograph for a watershed of area 550 ha and time of concentration of 50 minutes.*

SOLUTION: $A = 550$ ha $= 5.5$ km^2

$t_r = 30$ min $= 0.50$ h $\qquad$ $t_c = 50$ min $= 0.833$ h

lag time $\qquad$ $t_p = 0.6\, t_c = 0.6 \times 0.833 = 0.50$ h

$$T_p = \left(\frac{t_r}{2} + t_p \right) = 0.25 + 0.50 = 0.75 \text{ h}$$

$$Q_p = 2.08\, \frac{A}{T_p} = 2.08 \times \frac{5.5}{0.75} = 15.25 \text{ m}^3/\text{s}$$

$$T_b = 2.67\, T_p = 2.67 \times 0.75 = 2.00 \text{ h}$$

The derived triangular unit hydrograph is shown in Fig. 6.22
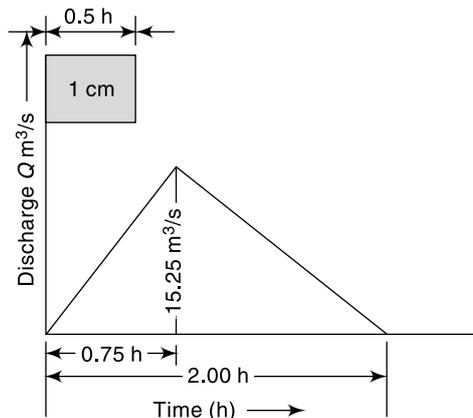
Fig. 6.22 Triangular Unit Hydrograph—Example 6.15

THE INDIAN PRACTICE

Two approaches (short term plan and long term plan) were adopted by CWC to develop methodologies for estimation of design flood discharges applicable to small and medium catchments (25–1000 ha) of India.

Under the *short-term plan*, a quick method of estimating design flood peak has been developed[2] as follows:

The peak discharge of a D-h unit hydrograph Q_{pd} in m^3/s is

$$Q_{pd} = 1.79A^{3/4} \qquad\qquad \text{for } S_m > 0.0028 \qquad\qquad (6.20)$$

and $\qquad$ $Q_{pd} = 37.4A^{3/4} S_m^{2/3} \qquad\qquad \text{for } S_m < 0.0028 \qquad\qquad (6.21)$

where A = catchment area in km^2 and S_m = weighted mean slope given by

$$S_m = \left[\frac{L_{ca}}{(L_1/S_1)^{1/2} + (L_2/S_2)^{1/2} + \cdots + (L_n/S_n)^{1/2}} \right]^2 \qquad\qquad (6.22)$$

in which L_{ca} = distance along the river from the gauging station to a point opposite to the centre of gravity of the area.

$L_1, L_2, \ldots L_n$ = length of main channel having slopes $S_I, S_2, \ldots S_n$ respectively, obtained from topographic maps.

The lag time in hours (i.e. time interval from the mid-point of the rainfall excess to the peak) of a 1-h unit hydrograph, t_{p1} is given by

$$t_{P1} = \frac{1.56}{[Q_{pd}/A]^{0.9}} \qquad (6.23)$$

For design purposes the duration of rainfall excess in hours is taken as

$$D = 1.1\, t_{p1} \qquad (6.24)$$

Equations (6.20) through (6.22) enable one to determine the duration and peak discharge of a design unit hydrograph. The time to peak has to be determined separately by using Eq. (6.9) or (6.10).

Under the *long-term plan*, a separate regional methodology has been developed by CWC. In this, the country is divided into 26 hydrometeorologically homogeneous subzones. For each subzone, a regional synthetic unit hydrograph has been developed. Detailed reports containing the synthetic unit hydrograph relations, details of the computation procedure and limitations of the method have been prepared, [e.g. CWC Reports No. CB/11/1985 and GP/10/1984 deal with flood estimation in Kaveri Basin (Sub-zone – 3i) and Middle Ganga Plains (Sub-zone – 1f) respectively.]

6.13 INSTANTANEOUS UNIT HYDROGRAPH (IUH)

The unit-hydrograph concept discussed in the preceding sections considered a D-h unit hydrograph. For a given catchment a number of unit hydrographs of different durations are possible. The shape of these different unit hydrographs depend upon the value of D. Figure 6.23 shows a typical variation of the shape of unit hydrographs for different values of D. As D is reduced, the intensity of rainfall excess being equal to $1/D$ increases and the unit hydrograph becomes more skewed. A finite unit hydrograph is indicated as the duration $D \to 0$. The limiting case of a unit hydrograph of zero duration is known as *instantaneous unit hydrograph* (IUH). Thus IUH is a fictitious, conceptual unit hydrograph which represents the surface runoff from the catchment due to
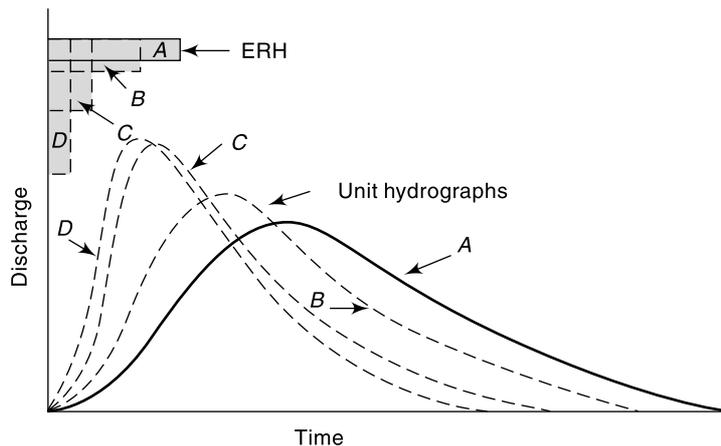
Fig. 6.23 Unit Hydrographs of Different Durations

an instantaneous precipitation of the rainfall excess volume of 1 cm. IUH is designated as $u(t)$ or sometimes as $u(0, t)$. It is a single-peaked hydrograph with a finite base width and its important properties can be listed as below:

1. $0 \leq u(t) \leq$ a positive value,   for $t > 0$;
2. $u(t) = 0$ for $t \leq 0$;
3. $u(t) \rightarrow = 0$ as $t \rightarrow \infty$;

4. $\int_0^\infty u(t)\, dt =$ unit depth over the catchment; and

5. time to the peak time to the centroid of the curve.

Consider an effective rainfall $I(\tau)$ of duration t_0 applied to a catchment as in Fig. 6.24. Each infinitesimal element of this ERH will operate on the IUH to produce a DRH whose discharge at time t is given by

$$Q(t) = \int_0^{t'} u(t - \tau)\, I(\tau)\, d\tau \tag{6.25}$$

where $t' = t$ when $t < t_0$ and $t' = t_0$ when $t \geq t_0$
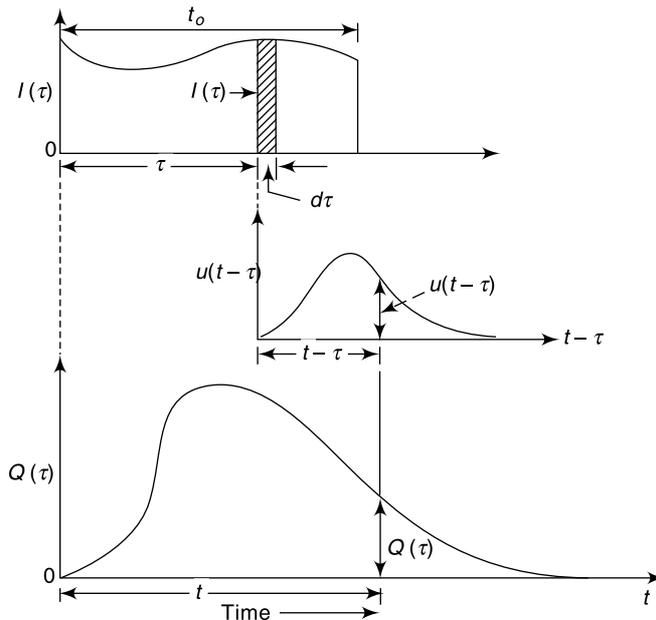
Fig. 6.24   Convolution of $I(\tau)$ and IUH

Equation (6.25) is called the *convolution integral* or *Duhamel integral.* The integral of Eq. (6.25) is essentially the same as the arithmetical computation of Eq. (6.5).

The main advantage of IUH is that it is independent of the duration of ERH and thus has one parameter less than a D-h unit hydrograph. This fact and the definition of IUH make it eminently suitable for theoretical analysis of rainfall excess-runoff relationship of a catchment. For a given catchment IUH, being independent of rainfall characteristics, is indicative of the catchment storage characteristics.

DERIVATION OF IUH

Consider an S-curve, designated as S_1, derived from a D-h unit hydrograph. In this the intensity of rainfall excess, $i = 1/D$ cm/h. Let S_2 be another S-curve of intensity i cm/h. If S_2 is separated from S_1 by a time interval dt and the ordinates are subtracted, a DRH due to a rainfall excess of duration dt and magnitude $i\, dt = dt/D$ h is obtained. A unit hydrograph of dt hours is obtained from this by dividing the above DRH by $i\, dt$.

Thus the dt-h unit hydrograph will have ordinates equal to $\left(\dfrac{S_2 - S_1}{i\, dt}\right)$. As dt is made smaller and smaller, i.e. as $dt \rightarrow 0$, an IUH results. Thus for an IUH, the ordinate at any time t is

$$u(t) = \lim_{dt \to 0}\left(\frac{S_2 - S_1}{i\, dt}\right) = \frac{1}{i}\frac{dS}{dt} \qquad (6.26)$$

If $i = 1$, then $u(t) = dS'/dt$, $\qquad\qquad\qquad\qquad\qquad\qquad\qquad$ (6.27)
where S' represents a S-curve of intensity 1 cm/h. Thus the ordinate of an IUH at any time t is the slope of the S-curve of intensity 1 cm/h (i.e. S-curve derived from a unit hydrograph of 1-h duration) at the corresponding time. Equation (6.26) can be used in deriving IUH approximately.

IUHs can be derived in many other ways, notably by (i) harmonic analysis (ii) Laplace transform, and (iii) conceptual models. Details of these methods are beyond the scope of this book and can be obtained from Ref. 3. However, two simple models viz., Clark's model and Nash's model are described in Chapter 8 (Sections 8.8 and 8.9).

DERIVATION OF D-HOUR UNIT HYDROGRAPH FROM IUH   For simple geometric forms of IUH, Eq. (6.25) can be used to derive a D-hour unit hydrograph. For complex shaped IUHs the numerical computation techniques used in deriving unit hydrographs of different durations (Sec. 6.7) can be adopted.

From Eq. 6.27, $dS' = u(t)\, dt$
Integrating between two points 1 and 2

$$S_2' - S_1' = \int_{t_1}^{t_2} u(t)\, dt \qquad (6.28)$$

If $u(t)$ is essentially linear within the range 1–2, then for small values of $\Delta t = (t_2 - t_1)$, by taking

$$u(t) = \bar{u}\,(t) = \frac{1}{2}\,[u(t_1) + u(t_2)]$$

$$S_2' - S_1' = \frac{1}{2}\,[u(t_1) + u(t_2)]\,(t_2 - t_1) \qquad (6.29)$$

But $(S_2' - S_1')/(t_2 - t_1) =$ ordinate of a unit hydrograph of duration $D_1 = (t_2 - t_1)$. Thus, in general terms, for small values of D_1, the ordinates of a D_1-hour unit hydrograph are obtained by the equation

$$(D_1\text{-hour UH})_t = \frac{1}{2}\,[(\text{IUH})_t + (\text{IUH})_{t - D_1}] \qquad (6.30)$$

Thus if two IUHs are lagged by D_1–hour where D_1 is small and their corresponding ordinates are summed up and divided by two, the resulting hydrograph will be a D_1-hour UH. After obtaining the ordinates of a D-hour unit hydrograph from

Eq. (6.30), the ordinates of any D-hour UH can be obtained by the superposition method or S-curve method described in Sec. 6.7. From accuracy considerations, unless the limbs of IUH can be approximated as linear, it is desirable to confine D_1 to a value of 1-hour or less.

EXAMPLE 6.16 *The coordinates of the IUH of a catchment are given below. Derive the direct runoff hydrograph (DRH) for this catchment due to a storm of duration 4 hours and having a rainfall excess of 5 cm.*

Time (hours)	0	1	2	3	4	5	6	7	8	9	10	11	12
IUH ordinate $u(t)$ (m³/s)	0	8	35	50	47	40	31	23	15	10	6	3	0

SOLUTION: The calculations are performed in Table 6.13.

1. First, the ordinates of 1-h UH are derived by using Eq. (6.30)
   In Table 6.13, Col. 2 = ordinates of given IUH = $u(t)$
   Col. 3 = ordinates of IUH lagged by 1-h

   Col. 4 = $\frac{1}{2}$ (Col. 2 + Col. 3) = ordinates of 1-h UH by Eq. (6.30)

2. Using the 1-hour UH, the S-curve is obtained and lagging it by 4 hours the ordinates of 4-h UH are obtained.
   In Table 6.12, Col. 5 = S-curve additions
   Col. 6 = (Col. 4 + Col. 5) = S-curve ordinates
   Col. 7 = Col. 6 lagged by 4 hours = S-curve ordinates lagged by 4-h.
   Col. 8 = (Col. 6 – Col. 7) = Ordinates of a DRH due to 4 cm of ER in 4 hours.
   Col. 9 = (Col. 8)/4 = Ordinates of 4-hour UH

3. The required DRH ordinates due to 5.0 cm ER in 4 hours are obtained by multiplying the ordinates of 4-h UH by 5.0
   In Table 6.12, Col. 10 = (Col. 9) × 5.0 = ordinates of required DRH
   [***Note:*** Calculation of 4-hour UH directly by using D_1 = 4-h in Eq. (6.30) will lead to errors as the assumptions of linearity of $u(t)$ during D_1 may not be satisfied.]

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---| REVISION QUESTIONS |---

6.1 List the factors affecting a flood hydrograph. Discuss the role of these factors.
6.2 Describe the analysis of the recession limb of a flood hydrograph.
6.3 Explain the term Rainfall Excess (ER). How is ERH of a storm obtained?
6.4 Why is base flow separated from the flood hydrograph in the process of developing a unit hydrograph?
6.5 What is a unit hydrograph? List the assumptions involved in the unit hydrograph theory.

Table 6.13 Determination of DRH from IUH – Example 6.16

1	2	3	4	5	6	7	8	9	10
Time (h)	$u(t)$ (m³/s)	$u(t)$ lagged by 1 hour	Ordinate of 1-h UH (m³/s)	S-Curve addition (m³/s)	S-Curve ordinate (m³/s)	S-Curve lagged by 4 hours (m³/s)	DRH of 4 cm in 4 hours	Ordinate of 4-h UH (m³/s)	DRH due to 5 cm ER in 4 hours (m³/s)
			([2] + [3])/2		[4] + [5]		[6]–[7]	[8]/4	[9] × 5
0	0		0		0		0.0	0.00	0.00
1	8	0	4.0	0	4.0		4.0	1.00	5.00
2	35	8	21.5	4.0	25.5		25.5	6.38	31.88
3	50	35	42.5	25.5	68.0		68.0	17.00	85.00
4	47	50	48.5	68.0	116.5	0.0	116.5	29.13	145.63
5	40	47	43.5	116.5	160.0	4.0	156.0	39.00	195.00
6	31	40	35.5	160.0	195.5	25.5	170.0	42.50	212.50
7	23	31	27.0	195.5	222.5	68.0	154.5	38.63	193.13
8	15	23	19.0	222.5	241.5	116.5	125.0	31.25	156.25
9	10	15	12.5	241.5	254.0	160.0	94.0	23.50	117.50
10	6	10	8.0	254.0	262.0	195.5	66.5	16.63	83.13
11	3	6	4.5	262.0	266.5	222.5	44.0	11.00	55.00
12	0	3	1.5	266.5	268.0	241.5	26.5	6.63	33.13
13		0	0.0	268.0	268.0	254.0	14.0	3.50	17.50
14		0	0.0	268.0	268.0	262.0	6.0	1.50	7.50
15		0	0.0	268.0	268.0	266.5	1.5	0.38	1.88
16		0	0.0	268.0	268.0	268.0	0.0	0.00	0.00

6.6 Describe briefly the procedure of preparing a D-hour unit hydrograph for a catchment.

6.7 Explain the procedure of using a unit hydrograph to develop the flood hydrograph due to a storm in a catchment.

6.8 Describe the S-curve method of developing a 6-h UH by using 12-h UH of the catchment.

6.9 Explain a procedure of deriving a synthetic unit hydrograph for a catchment by using Snyder's method.

6.10 What is an IUH? What are its characteristics?

6.11 Explain a procedure of deriving a D-h unit hydrograph from the IUH of the catchment.

6.12 Distinguish between

    (a) Hyetograph and hydrograph   (b) D-h UH and IUH

PROBLEMS

6.1 The flood hydrograph of a small stream is given below. Analyse the recession limb of the hydrograph and determine the recession coefficients. Neglect interflow.

Time (days)	Discharge (m³/s)	Time (days)	Discharge (m³/s)	Time (days)	Discharge (m³/s)
0	155	2.0	9.0	4.0	1.9
0.5	70.0	2.5	5.5	5.0	1.4
1.0	38.0	3.0	3.5	6.0	1.2
1.5	19.0	3.5	2.5	7.0	1.1

Estimate the groundwater storage at the end of 7th day from the occurrence of peak.

6.2 On June 1, 1980 the discharge in a stream was measured as 80 m³/s. Another measurement on June 21, 1980 yielded the stream discharge as 40 m³/s. There was no rainfall in the catchment from April 15, 1980. Estimate the (a) recession coefficient, (b) expected stream flow and groundwater storage available on July 10, 1980. Assume that there is no further rainfall in the catchment up to that date.

6.3 If $Q(t) = Q_0 K^t$ describes the base flow recession in a stream, prove that the storage $S(t_1)$ left in the basin at any time for supplying base flow follows the linear reservoir model, viz. $S(t_1) = C Q (t_1)$, where C is a constant.

[**Hint:** Use the boundary condition: at $t = \infty$, $S_\infty = 0$ and $Q_\infty = 0$]

6.4 A 4-hour storm occurs over an 80 km² watershed. The details of the catchment are as follows.

Sub Area (km²)	ϕ-Index (mm/hour)	Hourly Rain (mm)			
		1st hour	2nd hour	3rd hour	4th hour
15	10	16	48	22	10
25	15	16	42	20	8
35	21	12	40	18	6
5	16	15	42	18	8

Calculate the runoff from the catchment and the hourly distribution of the effective rainfall for the whole catchment.

6.5 Given below are observed flows from a storm of 6-h duration on a stream with a catchment area of 500 km²

Time (h)	0	6	12	18	24	30	36	42	48	54	60	66	72
Observed flow (m³/s)	0	100	250	200	150	100	70	50	35	25	15	5	0

Assuming the base flow to be zero, derive the ordinates of the 6-h unit hydrograph.

6.6 A flood hydrograph of a river draining a catchment of 189 km^2 due to a 6 hour isolated storm is in the form of a triangle with a base of 66 hour and a peak ordinate of 30 m^3/s occurring at 10 hours from the start. Assuming zero base flow, develop the 6-hour unit hydrograph for this catchment.

6.7 The following are the ordinates of the hydrograph of flow from a catchment area of 770 km^2 due to a 6-h rainfall. Derive the ordinates of the 6-h unit hydrograph. Make suitable assumptions regarding the base flow.

Time from beginning of storm (h)	0	6	12	18	24	30	36	42	48	54	60	66	72
Discharge (m^3/s)	40	65	215	360	400	350	270	205	145	100	70	50	42

6.8 Analysis of the surface runoff records of a 1-day storm over a catchment yielded the following data:

Time (days)	0	1	2	3	4	5	6	7	8	9
Discharge (m^3/s)	20	63	151	133	90	63	44	29	20	20
Estimated base flow (m^3/s)	20	22	25	28	28	26	23	21	20	20

Determine the 24-h distribution graph percentages. If the catchment area is 600 km^2, determine the depth of rainfall excess.

6.9 The ordinates of a hydrograph of surface runoff resulting from 4.5 cm of rainfall excess of duration 8 h in a catchment are as follows:

Time (h)	0	5	13	21	28	32	35	41	45	55
Discharge (m^3/s)	0	40	210	400	600	820	1150	1440	1510	1420

Time (h)	61	91	98	115	138
Discharge (m^3/s)	1190	650	520	290	0

Determine the ordinates of the 8-h unit hydrograph for this catchment.

6.10 The peak of a flood hydrograph due to a 6-h storm is 470 m^3/s. The mean depth of rainfall is 8.0 cm. Assume an average infiltration loss of 0.25 cm/h and a constant base flow of 15 m^3/s and estimate the peak discharge of the 6-h unit hydrograph for this catchment.

6.11 Given the following data about a catchment of area 100 km^2, determine the volume of surface runoff and peak surface runoff discharge corresponding to a storm of 60 mm in 1 hour.

Time (h)	**0**	**1**	**2**	**3**	**4**	**5**
Rainfall (mm)	0	40	0	0	0	0
Runoff (m^3/s)	300	300	1200	450	300	300

6.12 The ordinates of a 6-h unit hydrograph are given.

Time (h)	0	3	6	9	12	18	24	30	36	42	48	54	60	66
6-h UH ordinate (m^2/s)	0	150	250	450	600	800	700	600	450	320	200	100	50	0

A storm had three successive 6-h intervals of rainfall magnitude of 3.0, 5.0 and 4.0 cm, respectively. Assuming a ϕ index of 0.20 cm/h and a base flow of 30 m³/s, determine and plot the resulting hydrograph of flow.

6.13 The ordinates of a 6-h unit hydrograph are as given below:

Time (h)	0	6	12	18	24	30	36	42	48	54	60	66
ordinate of 6-h UH (m³/s)	0	20	60	150	120	90	66	50	32	20	10	0

If two storms, each of 1-cm rainfall excess and 6-h duration occur in succession, calculate the resulting hydrograph of flow. Assume base flow to be uniform at 10 m³/s.

6.14 Using the 6-h unit hydrograph of Prob. 6.13 derive a 12-h unit hydrograph for the catchment.

6.15 The ordinates of the 2-h unit hydrograph of a basin are given:

Time (h)	0	2	4	6	8	10	12	14	16	18	20	22
2-h UH ordinate (m³/s)	0	25	100	160	190	170	110	70	30	20	6	0

Determine the ordinates of the S_2-curve hydrograph and using this S_2-curve, determine the ordinates of the 4-h unit hydrograph of the basin.

6.16 The 6-hour unit hydrograph of a catchment is triangular in shape with a base width of 64 hours and a peak ordinate of 30 m³/s. Calculate the equilibrium discharge of the S_6-curve of the basin.

6.17 Ordinates of the one hour unit hydrograph of a basin at one-hour intervals are 5, 8, 5, 3 and 1 m³/s. Calculate the
(i) watershed area represented by this unit hydrograph.   (ii) S_1-curve hydrograph.
(iii) 2-hour unit hydrograph for the catchment.

6.18 Using the ordinates of a 12-h unit hydrograph given below, compute the ordinates of the 6-h unit hydrograph of the basin.

Time (h)	Ordinate of 12-h UH (m³/s)	Time (h)	Ordinate of 12-h UH (m³/s)	Time (h)	Ordinate of 12-h UH (m³/s)
0	0	54	130	108	17
6	10	60	114	114	12
12	37	66	99	120	8
18	76	72	84	126	6
24	111	78	71	132	3
30	136	84	58	138	2
36	150	90	46	144	0
42	153	96	35		
48	146	106	25		

[Note that the tail portion of the resulting 6-h UH needs fairing.]

6.19 The 3-h unit hydrograph for a basin has the following ordinates. Using the S-curve method, determine the 9-h unit hydrograph ordinates of the basin.

Time (h)	0	3	6	9	12	15	18	21	24	27	30
3-h UH ordinates (m³/s)	0	12	75	132	180	210	183	156	135	144	96

Time (h)	33	36	39	42	45	48	51	54	57	60	
3-h UH ordinates (m³/s)	87	66	54	42	33	24	18	12	6	6	

6.20 Using the given 6-h unit hydrograph derive the flood hydrograph due to the storm given below.

UH:

Time (h)	0	6	12	18	24	30	36	42	48	54	60	66
6-h UH ordinates (m³/s)	0	20	60	150	120	90	66	50	32	20	10	0

Storm:

Time from beginning of the storm (h)	0	6	12	18
Accumulated rainfall (cm)	0	4	5	10

The φ index for the storm can be assumed to be 0.167 cm/h. Assume the base flow to be 20 m³/s constant throughout.

6.21 The 6-hour unit hydrograph of a basin is triangular in shape with a peak of 100 m³/s occurring at 24-h from the start. The base is 72-h.
  (a) What is the area of the catchment represented by this unit hydrograph?
  (b) Calculate the flood hydrograph due to a storm of rainfall excess of 2.0 cm during the first 6 hours and 4.0 cm during the second 6 hours interval. The base flow can be assumed to be 25 m³/s constant throughout.

6.22 The 6-h unit hydrograph of a catchment of area 1000 km² can be approximated as a triangle with base of 69 h. Calculate the peak ordinate of this unit hydrograph.

6.23 The 4-h, distribution graph of a catchment of 50 km² area has the following ordinates:

Unit periods (4-h units)	1	2	3	4	5	6
Distribution (percentage)	5	20	40	20	10	5

If the catchment has rainfalls of 3.5. 2.2 and 1.8 cm in three consecutive 4-h periods, determine the resulting direct runoff hydrograph by assuming the φ-index for the storm as 0.25 cm/h.

6.24 The 6-h unit hydrograph of a catchment of area 259.2 km² is triangular in shape with a base width of 48 hours. The peak occurs at 12 h from the start. Derive the coordinates of the 6-h distribution graph for this catchment.

6.25 The one-hour unit hydrograph of a small rural catchment is triangular in shape with a peak value of 3.6 m³/s occurring at 3 hours from the start and a base time of 9 hours. Following urbanisation over a period of two decades, the infiltration index φ has decreased from 0.70 cm/h to 0.40 cm/h. Also the one-hour unit hydrograph has now a peak of 6.0 m³/s at 1.5 hours and a time base of 6 hours. If a design storm has intensities of 4.0 cm/h and 3.0 cm/h for two consecutive one hour intervals, estimate the percentage increase in the peak storm runoff and in the volume of flood runoff, due to urbanisation.

6.26 The following table gives the ordinates of a direct-runoff hydrograph resulting from two successive 3-h durations of rainfall excess values of 2 and 4 cm, respectively. Derive the 3-h unit hydrograph for the catchment.

Time (h)	0	3	6	9	12	15	18	21	24	27	30
Direct runoff (m³/s)	0	120	480	660	460	260	160	100	50	20	0

6.27 Characteristics of two catchments M and N measured from a map are given below:

Item	Catchment M	Catchment N
L_{ca}	76 km	52 km
L	148 km	106 km
A	2718 km²	1400 km²

For the 6-h unit hydrograph in catchment M, the peak discharge is at 200 m³/s and occurs at 37 h from the start of the rainfall excess. Assuming the catchments M and N are meteorologically similar, determine the elements of the 6-h synthetic unit hydrograph for catchment N by using Snyder's method.

6.28 A basin has an area of 400 km², and the following characteristics:

L = basin length = 35 km

L_{ca} = Length up to the centroid of the basin = 10 km

Snyder's coefficients: C_t = 1.5 and C_p = 0.70.

Develop synthetically the 3-h synthetic-unit hydrograph for this basin using Snyder's method.

6.29 Using the peak discharge and time to peak values of the unit hydrograph derived in Prob. 6.27, develop the full unit hydrograph by using the SCS dimensionless-unit hydrograph.

6.30 The rainfall excess of a storm is modelled as

$I(t)$ = 6 cm/s   for $0 \leq t \leq 4$ h

$I(t)$ = 0   for $t \geq 4$ h

The corresponding direct runoff hydrograph is expressed in terms of depth over unit catchment area per hour (cm/h) as

$Q(t)$ = 6.0 t cm/h   for $0 \leq t \leq 4$ h

$Q(t)$ = 48 – 6.0 t cm/h   for $8 > t \geq 4$ h

$Q(t)$ = 0   for $t > 8$

where t is in hours. Determine the (i) 4-h unit hydrograph of the catchment and corresponding S-curve of the catchment (ii) 3-h unit hydrogen of the catchment.

6.31 A 2-h unit hydrograph is given by

$U(t)$ = 0.5 cm/h   for $0 \leq t \leq 2$ h

$U(t)$ = 0   for $t \geq 4$ h

(i) Determine the S-curve corresponding to the given 2-h UH

(ii) Using the S-curve developed above, determine the 4-h unit hydrograph

6.32 A 1-h unit hydrograph is rectangular in shape with a base of 3 hours and peak of 100 m³/s. Develop the DRH due to an ERH given below:

Time since start (h)	1	2	3
Excess Rainfall (cm)	3	0	5

6.33 A 750 ha watershed has a time of concentration of 90 minutes.

(i) Derive the 15-minute unit hydrograph for this watershed by using SCS triangular unit hydrograph method.

(ii) What would be the DRH for a 15-minute storm having 4.0 cm of rainfall?

6.34 The IUH of a catchment is triangular in shape with a base of 36 h and peak of 20 m^3/s occurring at 8 hours from the start. Derive the 2-h unit hydrograph for this catchment.

6.35 The coordinates of the IUH of a catchment are as below:

Time (h)	0	1	2	3	4	5	6	8	10	12	14	16	18	20
Ordinates (m^3/s)	0	11	37	60	71	75	72	60	45	33	21	12	6	0

(a) What is the areal extent of the catchment?

(b) Derive the 3-hour unit hydrograph for this catchment.

─────────── OBJECTIVE QUESTIONS ───────────

6.1 The recession limb of a flood hydrograph can be expressed with positive values of coefficients, as $Q_t/Q_0 =$

(a) K_c^{at} (b) $a\,K_t^{-at}$ (c) a^{-at} (d) e^{-at^2}

6.2 For a given storm, other factors remaining same,
(a) basins having low drainage density give smaller peaks in flood hydrographs
(b) basins with larger drainage densities give smaller flood peaks
(c) low drainage density basins give shorter time bases of hydrographs
(d) the flood peak is independent of the drainage density.

6.3 Base-flow separation is performed
(a) on a unit hydrograph to get the direct-runoff hydrograph
(b) on a flood hydrograph to obtain the magnitude of effective rainfall
(c) on flood hydrographs to obtain the rainfall hyetograph
(d) on hydrographs of effluent streams only.

6.4 A direct-runoff hydrograph due to a storm was found to be triangular in shape with a peak of 150 m^3/s, time from start of effective storm to peak of 24 h and a total time base of 72 h. The duration of the storm in this case was
(a) < 24 h   (b) between 24 to 72 h
(c) 72 h   (d) > 72 h.

6.5 A unit hydrograph has one unit of
(a) peak discharge   (b) rainfall duration
(c) direct runoff   (d) the time base of direct runoff.

6.6 The basic assumptions of the unit-hydrograph theory are
(a) nonlinear response and time invariance
(b) time invariance and linear response
(c) linear response and linear time variance
(d) nonlinear time variance and linear response.

6.7 The *D*-hour unit hydrograph of a catchment may be obtained by dividing the ordinates of a single peak direct runoff hydrograph (DRH) due to a storm of *D* hour duration by the
(a) Total runoff volume (in cm)   (b) Direct runoff volume (in cm)
(c) Duration of DRH   (d) Total rainfall (in cm)

6.8 A storm hydrograph was due to 3 h of effective rainfall. It contained 6 cm of direct runoff. The ordinates of DRH of this storm
(a) when divided by 3 give the ordinates of a 6-h unit hydrograph
(b) when divided by 6 give the ordinates of a 3-h unit hydrograph

(c) when divided by 3 give the ordinates of a 3-h unit hydrograph

(d) when divided by 6 give the ordinates of a 6-h unit hydrograph.

6.9 A 3-hour storm over a watershed had an average depth of 27 mm. The resulting flood hydrograph was found to have a peak flow of 200 m^3/s and a base flow of 20 m^3/s. If the loss rate could be estimated as 0.3 cm/h, a 3-h unit hydrograph for this watershed will have a peak of

(a) 66.7 m^3/s   (b) 100 m^3/s   (c) 111.1 m^3/s   (d) 33.3 m^3/s

6.10 A triangular DRH due to a storm has a time base of 80 hrs and a peak flow of 50 m^3/s occurring at 20 hours from the start. If the catchment area is 144 km^2, the rainfall excess in the storm was

(a) 20 cm   (b) 7.2 cm   (c) 5 cm   (d) none of these.

6.11 The 12-hr unit hydrograph of a catchment is triangular in shape with a base width of 144 hours and a peak discharge value of 23 m^3/s. This unit hydrograph refers to a catchment of area

(a) 756 km^2 (b) 596 km^2 (c) 1000 km^2 (d) none of these.

6.12 The 6-h unit hydrograph of a catchment is triangular in shape with a base width of 64 h and peak ordinate of 20 m^3/s. If a 0.5 cm rainfall excess occurs in 6 h in that catchment, the resulting surface-runoff hydrograph will have

(a) a base of 128 h   (b) a base of 32 h

(c) a peak of 40 m^3/s   (d) a peak of 10 m^3/s

6.13 A 90 km^2 catchment has the 4-h unit hydrograph which can be approximated as a triangle. If the peak ordinate of this unit hydrograph is 10 m^3/s the time base is

(a) 120 h   (b) 64 h   (c) 50 h   (d) none of these.

6.14 A triangular DRH due to a 6-h storm in a catchment has a time base of 100 h and a peak flow of 40 m^3/s. The catchment area is 180 km^2. The 6-h unit hydrograph of this catchment will have a peak flow in m^3/s of

(a) 10   (b) 20   (c) 30   (d) none of these.

6.15 The 3-hour unit hydrograph U_1 of a catchment of area 250 km^2 is in the form of a triangle with peak discharge of 40 m^3/s. Another 3-hour unit hydrograph U_2 is also triangular in shape and has the same base width as U_1 but with a peak flow of 80 m^3/s. The catchment which U_2 refers to has an area of

(a) 125 km^2 (b) 250 km^2 (c) 1000 km^2 (d) 500 km^2

6.16 U_c is the 6-h unit hydrograph for a basin representing 1 cm of direct runoff and U_m is the direct runoff hydrograph for the same basin due to a rainfall excess of 1 mm in a storm of 6 hour duration.

(a) Ordinates of U_m are 1/10 the corresponding ordinates of U_c

(b) Base of U_m is 1/10 the base of U_c

(c) Ordinates of U_m are 10 times the corresponding ordinates of U_c

(d) Base of U_m is 10 times the base of U_c

6.17 A basin with an area of 756 km^2 has the 6-h unit hydrograph which could be approximated as a triangle with a base of 70 hours. The peak discharge of direct runoff hydrograph due to 5 cm of rainfall excess in 6 hours from that basin is

(a) 535 m^3/s   (b) 60 m^3/s   (c) 756 m^3/s   (d) 300 m^3/s

6.18 The peak flow of a flood hydrograph caused by isolated storm was observed to be 120 m^3/s. The storm was of 6 hours duration and had a total rainfall of 7.5 cm. If the base flow and the φ-index are assumed to be 30 m^3/s and 0.25 cm/h respectively, the peak ordinate of the 6-h unit hydrograph of the catchment is

(a) 12.0 m^3/s   (b) 15.0 m^3/s   (c) 16.0 m^3/s   (d) 20.0 m^3/s

6.19 The peak ordinate of 4-h unit hydrograph a basin is 80 m^3/s. An isolated storm of 4-hours duration in the basin was recorded to have a total rainfall of 7.0 cm. If it is assumed that the base flow and the φ-index are 20 m^3/s and 0.25 cm/h respectively, the peak of the flood discharge due to the storm could be estimated as
 (a) 580 m^3/s
 (b) 360 m^3/s
 (c) 480 m^3/s
 (d) 500 m^3/s

6.20 The peak flow of a flood hydrograph caused by isolated storm was observed to be 100 m^3/s. The storm had a duration of 8.0 hours and the total depth of rainfall of 7.0 cm. The base flow and the φ-index were estimated as 20 m^3/s and 0.25 cm/h respectively. If in the above storm the total rainfall were 9.5 cm in the same duration of 8 hours, the flood peak would have been larger by
 (a) 35.7%
 (b) 40%
 (c) 50%
 (d) 20%

6.21 For a catchment with an area of 360 km^2 the equilibrium discharge of the *S*-curve obtained by summation of 4-h unit hydrograph is
 (a) 250 m^3/s
 (b) 90 m^3/s
 (c) 278 m^3/s
 (d) 360 m^3/s

6.22 For a catchment of area *A* an *S*-curve has been derived by using the *D*-hour unit hydrograph which has a time base *T*. In this *S*-curve
 (a) the equilibrium discharge is independent of *D*
 (b) the time at which the *S*-curve attains its maximum value is equal to *T*
 (c) the time at which the *S*-curve attains its maximum value is equal to *D*
 (d) the equilibrium discharge is independent of *A*

6.23 An IUH is a direct runoff hydrograph of
 (a) of one cm magnitude due to rainfall excess of 1-h duration
 (b) that occurs instantaneously due to a rainfall excess of 1-h duration
 (c) of unit rainfall excess precipitating instantaneously over the catchment
 (d) occurring at any instant in long duration

6.24 An instantaneous unit hydrograph is a hydrograph of
 (a) unit duration and infinitely small rainfall excess
 (b) infinitely small duration and of unit rainfall excess
 (c) infinitely small duration and of unit rainfall excess of an infinitely small area
 (d) unit rainfall excess on infinitely small area

Chapter
7

FLOODS

7.1 INTRODUCTION

A flood is an unusually high stage in a river, normally the level at which the river overflows its banks and inundates the adjoining area. The damages caused by floods in terms of loss of life, property and economic loss due to disruption of economic activity are all too well known. Thousands of crores of rupees are spent every year in flood control and flood forecasting. The hydrograph of extreme floods and stages corresponding to flood peaks provide valuable data for purposes of hydrologic design. Further, of the various characteristics of the flood hydrograph, probably the most important and widely used parameter is the flood peak. At a given location in a stream, flood peaks vary from year to year and their magnitude constitutes a hydrologic series which enable one to assign a frequency to a given flood-peak value. In the design of practically all hydraulic structures the peak flow that can be expected with an assigned frequency (say 1 in 100 years) is of primary importance to adequately proportion the structure to accommodate its effect. The design of bridges, culvert waterways and spillways for dams and estimation of scour at a hydraulic structure are some examples wherein flood-peak values are required.

To estimate the magnitude of a flood peak the following alternative methods are available:

1. Rational method   2. Empirical method
3. Unit-hydrograph technique   4. Flood-frequency studies

The use of a particular method depends upon (i) the desired objective, (ii) the available data, and (iii) the importance of the project. Further the *rational formula* is only applicable to small-size (< 50 km^2) catchments and the unit-hydrograph method is normally restricted to moderate-size catchments with areas less than 5000 km^2.

7.2 RATIONAL METHOD

Consider a rainfall of uniform intensity and very long duration occurring over a basin. The runoff rate gradually increases from zero to a constant value as indicated in Fig. 7.1. The runoff increases as more and more flow from remote areas of the catchment reach the outlet. Designating the time taken for a drop of water from the farthest part of the catchment to reach the outlet as t_c = time of concentration, it is obvious that if the rainfall continues beyond t_c, the runoff will be constant and at the peak value. The peak value of the runoff is given by

$$Q_p = C\,A\,i;\ \text{for}\ t \geq t_c \tag{7.1}$$

Rainfall

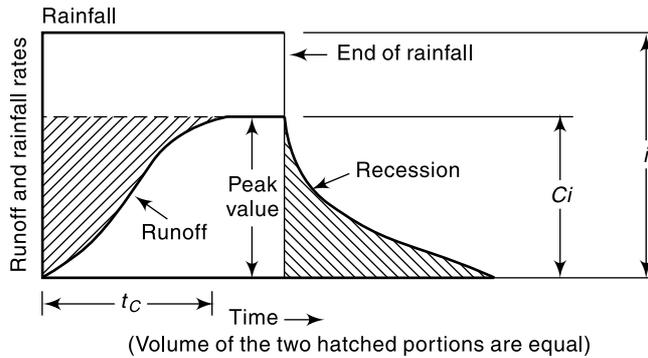(Volume of the two hatched portions are equal)

Fig. 7.1 Runoff Hydrograph due to Uniform Rainfall

where C = coefficient of runoff = (runoff/rainfall), A = area of the catchment and i = intensity of rainfall. This is the basic equation of the *rational method.* Using the commonly used units, Eq. (7.1) is written for field application as

$$Q_p = \frac{1}{3.6} C (i_{tc,p}) A \qquad (7.2)$$

where

Q_p = peak discharge (m³/s)

C = coefficient of runoff

$(i_{tc,p})$ = the mean intensity of precipitation (mm/h) for a duration equal to t_c and an exceedence probability P

A = drainage area in km²

The use of this method to compute Q_p requires three parameters: t_c, $(i_{tc,p})$ and C.

TIME OF CONCENTRATION (t_c)

There are a number of empirical equations available for the estimation of the time of concentration. Two of these are described below.

US PRACTICE For small drainage basins, the time of concentration is assumed to be equal to the lag time of the peak flow. Thus

$$t_c = t_p \text{ of Eq. (6.10)} = C_{tL} \left(\frac{LL_{ca}}{\sqrt{S}} \right)^n \qquad (7.3)$$

where t_c = time of concentration in hours, C_{tL}, L, L_{ca}, n and S have the same meaning as in Eq. (6.10) of Chapter 6.

KIRPICH EQUATION (1940) This is the popularly used formula relating the time of concentration of the length of travel and slope of the catchment as

$$t_c = 0.01947 \, L^{0.77} \, S^{-0.385} \qquad (7.4)$$

where t_c = time of concentration (minutes)

L = maximum length of travel of water (m), and

S = slope of the catchment = $\Delta H/L$ in which

ΔH = difference in elevation between the most remote point on the catchment and the outlet.

For easy use Eq. (7.4) is sometimes written as

$$t_c = 0.01947 \, K_1^{0.77} \tag{7.4a}$$

where $K_1 = \sqrt{\dfrac{L^3}{\Delta H}}$

RAINFALL INTENSITY ($i_{tc,p}$) The rainfall intensity corresponding to a duration t_c and the desired probability of exceedence P, (i.e. return period $T = 1/P$) is found from the rainfall-frequency-duration relationship for the given catchment area (Chap. 2). This will usually be a relationship of the form of Eq. (2.15), viz.

$$i_{tc,p} = \frac{KT^x}{(t_c + a)^n}$$

in which the coefficients K, a, x and n are specific to a given area. Table 2.8 (preferably in its expanded form) could be used to estimate these coefficients to a specific catchment. In USA the peak discharges for purposes of urban area drainage are calculated by using $P = 0.05$ to 0.1. The recommended frequencies for various types of structures used in watershed development projects in India are as below:

Sl. No	Types of structure	Return Period (Years)
1	Storage and Diversion dams having permanent spillways	50–100
2	Earth dams having natural spillways	25–50
3	Stock water dams	25
4	Small permanent masonry and vegetated waterways	10–15
5	Terrace outlets and vegetated waterways	10
6	Field diversions	15

RUNOFF COEFFICIENT (C)

The coefficient C represents the integrated effect of the catchment losses and hence depends upon the nature of the surface, surface slope and rainfall intensity. The effect of rainfall intensity is not considered in the available tables of values of C. Some typical values of C are indicated in Table 7.1(a & b).

Equation (7.2) assumes a homogeneous catchment surface. If however, the catchment is non-homogeneous but can be divided into distinct sub areas each having a different runoff coefficient, then the runoff from each sub area is calculated separately and merged in proper time sequence. Sometimes, a non-homogeneous catchment may have component sub areas distributed in such a complex manner that distinct sub zones cannot be separated. In such cases a weighted equivalent runoff coefficient C_e as below is used.

$$C_e = \frac{\sum\limits_{1}^{N} C_i A_i}{A} \tag{7.5}$$

Table 7.1(a) Value of the Coefficient C in Eq. (7.2)

Types of area	Value of C
A. *Urban area* (P = 0.05 to 0.10)	
Lawns: Sandy-soil, flat, 2%	0.05–0.10
Sandy soil, steep, 7%	0.15–0.20
Heavy soil, average, 2.7%	0.18–0.22
Residential areas:	
Single family areas	0.30–0.50
Multi units, attached	0.60–0.75
Industrial:	
Light	0.50–0.80
Heavy	0.60–0.90
Streets	0.70–0.95
B. *Agricultural Area*	
Flat: Tight clay;cultivated	0.50
woodland	0.40
Sandy loam;cultivated	0.20
woodland	0.10
Hilly: Tight clay;cultivated	0.70
woodland	0.60
Sandy loam;cultivated	0.40
woodland	0.30

Table 7.1(b) Values of C in Rational Formula for Watersheds with Agricultural and Forest Land Covers

Sl. No	Vegetative cover and Slope (%)		Sandy Loam	Clay and Silty Loam	Stiff Clay
				Soil Texture	
1	Cultivated Land				
		0–5	0.30	0.50	0.60
		5–10	0.40	0.60	0.70
		10–30	0.52	0.72	0.82
2	Pasture Land				
		0–5	0.10	0.30	0.40
		5–10	0.16	0.36	0.55
		10–30	0.22	0.42	0.60
3	Forest Land				
		0–5	0.10	0.30	0.40
		5–10	0.25	0.35	0.50
		10–30	0.30	0.50	0.60

where A_i = the areal extent of the sub area i having a runoff coefficient C_i and N = number of sub areas in the catchment.

The rational formula is found to be suitable for peak-flow prediction in small catchments up to 50 km^2 in area. It finds considerable application in urban drainage designs and in the design of small culverts and bridges.

It should be noted that the word *rational* is rather a misnomer as the method involves the determination of parameters t_c and C in a subjective manner. Detailed description and the practice followed in using the rational method in various countries are given in detail in Ref. 7.

EXAMPLE 7.1 (a) *An urban catchment has an area of 85 ha. The slope of the catchment is 0.006 and the maximum length of travel of water is 950 m. The maximum depth of rainfall with a 25-year return period is as below:*

Duration (min)	5	10	20	30	40	60
Depth of rainfall (mm)	17	26	40	50	57	62

If a culvert for drainage at the outlet of this area is to be designed for a return period of 25 years, estimate the required peak-flow rate, by assuming the runoff coefficient as 0.3.

SOLUTION: The time of concentration is obtained by the Kirpich formula [Eq.(7.4)] as
$$t_c = 0.01947 \times (950)^{0.77} \times (0.006)^{-0.385} = 27.4 \text{ minutes}$$
By interpolation,
Maximum depth of rainfall for 27.4-min duration
$$= \frac{(50 - 40)}{10} \times 7.4 + 40 = 47.4 \text{ mm}$$

$$\text{Average intensity} = i_{tc, p} = \frac{47.4}{27.4} \times 60 = 103.8 \text{ mm/h}$$

By Eq. (7.2),
$$Q_p = \frac{0.30 \times 103.8 \times 0.85}{3.6} = 7.35 \text{ m}^3/\text{s}$$

EXAMPLE 7.1 (b) *If in the urban area of Example 7.1(a), the land use of the area and the corresponding runoff coefficients are as given below, calculate the equivalent runoff coefficient.*

Land use	Area (ha)	Runoff coefficient
Roads	8	0.70
Lawn	17	0.10
Residential area	50	0.30
Industrial area	10	0.80

SOLUTION: Equivalent runoff coefficient $C_e = \dfrac{\sum\limits_{1}^{N} C_i \, A_i}{A}$

$$C_e = \frac{[(0.7 \times 8) + (0.1 \times 17) + (0.3 \times 50) + (0.8 \times 10)]}{[8 + 17 + 50 + 10]}$$

$$= \frac{30.3}{85} = 0.36$$

EXAMPLE 7.2 *A 500 ha watershed has the land use/cover and corresponding runoff coefficient as given below:*

Land use/cover	Area (ha)	Runoff coefficient
Forest	250	0.10
Pasture	50	0.11
Cultivated land	200	0.30

The maximum length of travel of water in the watershed is about 3000 m and the elevation difference between the highest and outlet points of the watershed is 25 m. The maximum intensity duration frequency relationship of the watershed is given by

$$i = \frac{6.311 T^{0.1523}}{(D + 0.50)^{0.945}}$$

water i = intensity in cm/h, T = Return period in years and D = duration of the rainfall in hours. Estimate the (i) 25 year peak runoff from the watershed and (ii) the 25 year peak runoff if the forest cover has decreased to 50 ha and the cultivated land has encroached upon the pasture and forset lands to have a total coverage of 450 ha.

SOLUTION:

Case 1: Equivalent runoff coefficient $C_e = \dfrac{\sum\limits_{1}^{N} C_i\, A_i}{A}$

$$= \frac{[(0.10 \times 250) + (0.11 \times 50) + (0.30 \times 200)]}{500} = 0.181$$

By Eq. (7.4a) time of concentration $t_c = 0.01947 (K_1)^{0.77}$ with $K_1 = \sqrt{\dfrac{L^3}{\Delta H}}$

Since $\qquad L = 3000$ m and $\Delta H = 25$ m $\qquad K_1 = \sqrt{\dfrac{(3000)^3}{25}} = 32863$

$\qquad t_c = 0.01947 (32863)^{0.77} = 58.5$ min $= 0.975$ h

Calculation of $i_{tc,p}$: Here $D = t_c = 0.975$ h. $T = 25$ years. Hence

$$i = \frac{6.311 (25)^{0.1523}}{(0.975 + 0.50)^{0.945}} = 10.304/1.447 = 7.123 \text{ cm/h} = 71.23 \text{ mm/h}$$

Peak Flow by Eq. (7.2), $Q_p = (1/3.6)(C_e\, i\, A)$

$$= \frac{0.181 \times 71.23 \times (500/100)}{3.6} = 64.46 \text{ m}^3/\text{s}$$

Case 2: Here Equivalent $C = C_e = \dfrac{[(0.10 \times 50) + (0.30 \times 450)]}{500} = 0.28$

$$i = 71.23 \text{ mm/h and } A = 500 \text{ ha} = 5 \text{ (km)}^2$$

$$Q_p = \frac{0.28 \times 71.23 \times 5}{3.6} = 99.72 \text{ m}^3/\text{s}$$

$$i = 71.23 \text{ mm/h and } A = 500 \text{ ha} = 5 \text{ km}^2$$

$$Q_p = \frac{0.28 \times 71.23 \times 5}{3.6} = 99.72 \text{ m}^3/\text{s}$$

7.3 EMPIRICAL FORMULAE

The empirical formulae used for the estimation of the flood peak are essentially regional formulae based on statistical correlation of the observed peak and important catchment properties. To simplify the form of the equation, only a few of the many parameters affecting the flood peak are used. For example, almost all formulae use the catchment area as a parameter affecting the flood peak and most of them neglect the flood frequency as a parameter. In view of these, the empirical formulae are applicable only in the region from which they were developed and when applied to other areas they can at best give approximate values.

FLOOD PEAK-AREA RELATIONSHIPS

By far the simplest of the empirical relationships are those which relate the flood peak to the drainage area. The maximum flood discharge Q_p from a catchment area A is given by these formulae as

$$Q_p = f(A)$$

While there are a vast number of formulae of this kind proposed for various parts of the world, only a few popular formulae used in various parts of India are given below.

DICKENS FORMULA (1865)

$$Q_p = C_D A^{3/4} \tag{7.6}$$

where Q_p = maximum flood discharge (m³/s) A = catchment area (km²)
C_D = Dickens constant with value between 6 to 30

The following are some guidelines in selecting the value of C_D:

	Value of C_D
North-Indian plains	6
North-Indian hilly regions	11–14
Central India	14–28
Coastal Andhra and Orissa	22–28

For actual use the local experience will be of aid in the proper selection of C_D. Dickens formula is used in the central and northern parts of the country.

RYVES FORMULA (1884)

$$Q_p = C_R A^{2/3} \tag{7.7}$$

where Q_p = maximum flood discharge (m³/s) A = catchment area (km²)
and C_R = Ryves coefficient

This formula originally developed for the Tamil Nadu region, is in use in Tamil Nadu and parts of Karnataka and Andhra Pradesh. The values of C_R recommended by Ryves for use are:

C_R = 6.8 for areas within 80 km from the east coast
= 8.5 for areas which are 80–160 km from the east coast
= 10.2 for limited areas near hills

INGLIS FORMULA (1930) This formula is based on flood data of catchments in Western Ghats in Maharashtra. The flood peak Q_p in m³/s is expressed as

$$Q_p = \frac{124 A}{\sqrt{A + 10.4}} \tag{7.8}$$

where A is the catchment area in km^2.

Equation (7.8) with small modifications in the constant in the numerator (124) is in use Maharashtra for designs in small catchments.

OTHER FORMULAE

There are many such empirical formulae developed in various parts of the world. References 3 and 5 list many such formulae suggested for use in various parts of India as well as of the world.

There are some empirical formulae which relate the peak discharge to the basin area and also include the flood frequency. Fuller's formula (1914) derived for catchments in USA is a typical one of this kind and is given by

$$Q_{Tp} = C_f A^{0.8} (1 + 0.8 \log T) \tag{7.9}$$

where Q_{Tp} = maximum 24-h flood with a frequency of T years in m^3/s, A = catchment area in km^2, C_f = a constant with values between 0.18 to 1.88.

ENVELOPE CURVES

In regions having same climatological characteristics, if the available flood data are meagre, the enveloping curve technique can be used to develop a relationship between the maximum flood flow and drainage area. In this method the available flood peak data from a large number of catchments which do not significantly differ from each other in terms of meteorological and topographical characteristics are collected. The data are then plotted on a log-log paper as flood peak *vs* catchment area. This would result in a plot in which the data would be scattered. If an enveloping curve that would encompass all the plotted data points is drawn, it can be used to obtain maximum peak discharges for any given area. Envelop curves thus obtained are very useful in getting quick rough estimations of peak values. If equations are fitted to these enveloping curves, they provide empirical flood formulae of the type, $Q = f(A)$.

Kanwarsain and Karpov (1967) have presented enveloping curves representing the relationship between the peak-flood flow and catchment area for Indian conditions. Two curves, one for the south Indian rivers and the other for north Indian and central Indian rivers, are developed (Fig. 7.2). These two curves are based on data covering large catchment areas, in the range 10^3 to 10^6 km^2.

Based on the maximum recorded floods throughout the world, Baird and McIllwraith (1951) have correlated the maximum flood discharge Q_{mp} in m^3/s with catchment area A in km^2 as

$$Q_{mp} = \frac{3025 A}{(278 + A)^{0.78}} \tag{7.10}$$

EXAMPLE 7.3 *Estimate the maximum flood flow for the following catchments by using an appropriate empirical formula:*

1. *$A_1 = 40.5 \ km^2$ for western Ghat area, Maharashtra*
2. *$A_2 = 40.5 \ km^2$ in Gangetic plain*
3. *$A_3 = 40.5 \ km^2$ in the Cauvery delta, Tamil Nadu*
4. *What is the peak discharge for $A = 40.5 \ km^2$ by maximum world flood experience?*
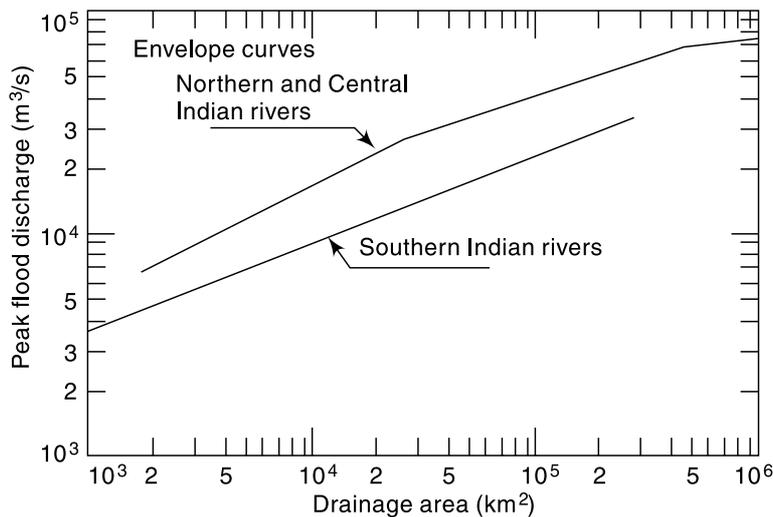
Fig. 7.2 Enveloping Curves for Indian Rivers

SOLUTION:

1. For this catchment, the Inglis formula is recommended.
   By the Inglis formula [Eq. (7.8)],

   $$Q_p = \frac{124 \times 40.5}{\sqrt{40.5 + 10.4}} = 704 \text{ m}^3/\text{s}$$

2. In this case Dickens formula [Eq. (7.6)] with $C_D = 6.0$ is recommended. Hence

   $$Q_p = 6.0 \times (40.5)^{0.75} = 96.3 \text{ m}^3/\text{s}$$

3. In this case Ryves formula [Eq. (7.7)] with $C_R = 6.8$ is preferred, and this gives

   $$Q_p = 6.8 \, (40.5)^{2/3} = 80.2 \text{ m}^3/\text{s}$$

4. By Eq. (7.10) for maximum peak discharge based on world experience,

   $$Q_{mp} = \frac{3025 \times 40.5}{(278 + 40.5)^{0.78}} = 1367 \text{ m}^3/\text{s.}$$

7.4 UNIT HYDROGRAPH METHOD

The unit hydrograph technique described in the previous chapter can be used to predict the peak-flood hydrograph if the rainfall producing the flood, infiltration characteristics of the catchment and the appropriate unit hydrograph are available. For design purposes, extreme rainfall situations are used to obtain the design storm, viz. the hydrograph of the rainfall excess causing extreme floods. The known or derived unit hydrograph of the catchment is then operated upon by the design storm to generate the desired flood hydrograph. Details about this use of unit hydrograph are given in Sec. 7.12.

7.5 FLOOD FREQUENCY STUDIES

Hydrologic processes such as floods are exceedingly complex natural events. They are resultants of a number of component parameters and are therefore very difficult to model analytically. For example, the floods in a catchment depend upon the

characteristics of the catchment, rainfall and antecedent conditions, each one of these factors in turn depend upon a host of constituent parameters. This makes the estimation of the flood peak a very complex problem leading to many different approaches. The empirical formulae and unit hydrograph methods presented in the previous sections are some of them. Another approach to the prediction of flood flows, and also applicable to other hydrologic processes such as rainfall etc. is the statistical method of frequency analysis.

The values of the annual maximum flood from a given catchment area for large number of successive years constitute a hydrologic data series called the *annual series.* The data are then arranged in decreasing order of magnitude and the probability *P* of each event being equalled to or exceeded (plotting position) is calculated by the plotting-position formula

$$P = \frac{m}{N+1} \tag{7.11}$$

where *m* = order number of the event and *N* = total number of events in the data. The recurrence interval, *T* (also called the *return period* or *frequency*) is calculated as
$$T = 1/P \tag{7.12}$$

The relationship between *T* and the probability of occurrence of various events is the same as described in Sec. 2.11. Thus, for example, the probability of occurrence of the event *r* times in *n* successive years is given by

$$P_{rn} = {}^nC_r P^r q^{n-r} = \frac{n!}{(n-r)!\,r!} P^r q^{n-r}$$

where $\qquad q = 1 - P$

Consider, for example, a list of flood magnitudes of a river arranged in descending order as shown in Table 7.2. The length of the record is 50 years.

Table 7.2 Calculation of Frequency *T*

Order No. m	Flood magnitude Q (m³/s)	T in years = 51/m
1	160	51.00
2	135	25.50
3	128	17.00
4	116	12.75
:	:	:
:	:	:
:	:	:
49	65	1.04
50	63	1.02

The last column shows the return period *T* of various flood magnitude, *Q*. A plot of *Q vs T* yields the probability distribution. For small return periods (i.e. for interpolation) or where limited extrapolation is required, a simple best-fitting curve through plotted points can be used as the probability distribution. A logarithmic scale for *T* is often advantageous. However, when larger extrapolations of *T* are involved, theoretical probability distributions have to be used. In frequency analysis of floods the usual

problem is to predict extreme flood events. Towards this, specific extreme-value distributions are assumed and the required statistical parameters calculated from the available data. Using these the flood magnitude for a specific return period is estimated.

Chow (1951) has shown that most frequency distribution functions applicable in hydrologic studies can be expressed by the following equation known as the *general equation of hydrologic frequency analysis:*

$$x_T = \bar{x} + K\sigma \tag{7.13}$$

where x_T = value of the variate X of a random hydrologic series with a return period T, $\bar{x}$ = mean of the variate, σ = standard deviation of the variate, K = frequency factor which depends upon the return period, T and the assumed frequency distribution. Some of the commonly used frequency distribution functions for the predication of extreme flood values are

1. Gumbel's extreme-value distribution,
2. Log-Pearson Type III distribution
3. Log normal distribution.

Only the first two distributions are dealt with in this book with emphasis on application. Further details and theoretical basis of these and other methods are available in Refs. 2, 3, 7 and 8.

7.6 GUMBEL'S METHOD

This extreme value distribution was introduced by Gumbel (1941) and is commonly known as Gumbel's distribution. It is one of the most widely used probability distribution functions for extreme values in hydrologic and meteorologic studies for prediction of flood peaks, maximum rainfalls, maximum wind speed, etc.

Gumbel defined a flood as the largest of the 365 daily flows and the annual series of flood flows constitute a series of largest values of flows. According to his theory of extreme events, the probability of occurrence of an event equal to or larger than a value x_0 is

$$P\,(X \geq x_0) = 1 - e^{-e^{-y}} \tag{7.14}$$

in which y is a dimensionless variable given by

$$y = \alpha\,(x - a) \qquad a = \bar{x} - 0.45005\,\sigma_x \qquad \alpha = 1.2825/\sigma_x$$

Thus
$$y = \frac{1.285(x - \bar{x})}{\sigma_x} + 0.577 \tag{7.15}$$

where $\bar{x}$ = mean and σ_x = standard deviation of the variate X. In practice it is the value of X for a given P that is required and as such Eq. (7.14) is transposed as

$$y_p = -\ln\,[-\ln\,(1 - P)] \tag{7.16}$$

Noting that the return period $T = 1/P$ and designating

y_T = the value of y, commonly called the reduced variate, for a given T

$$y_T = -\left[\ln.\,\ln\,\frac{T}{T-1}\right] \tag{7.17}$$

or
$$y_T = -\left[0.834 + 2.303\,\log\log\frac{T}{T-1}\right] \tag{7.17a}$$

Now rearranging Eq. (7.15), the value of the variate X with a return period T is

$$x_T = \bar{x} + K \, \sigma_x \qquad (7.18)$$

where

$$K = \frac{(y_T - 0.577)}{1.2825} \qquad (7.19)$$

Note that Eq. (7.18) is of the same form as the general equation of hydrologic-frequency analysis (Eq. (7.13)). Further, Eqs. (7.18) and (7.19) constitute the basic Gumbel's equations and are applicable to an infinite sample size (i.e. $N \to \infty$).

Since practical annual data series of extreme events such as floods, maximum rainfall depths, etc., all have finite lengths of record (Eq. (7.19)) is modified to account for finite N as given below for practical use.

GUMBEL'S EQUATION FOR PRACTICAL USE

Equation (7.18) giving the value of the variate X with a recurrence interval T is used as

$$x_T = \bar{x} + K \, \sigma_{n-1} \qquad (7.20)$$

where σ_{n-1} = standard deviation of the sample of size $N = \sqrt{\dfrac{\Sigma(x - \bar{x})^2}{N-1}}$

K = frequency factor expressed as

$$K = \frac{y_T - \bar{y}_n}{S_n} \qquad (7.21)$$

in which y_T = reduced variate, a function of T and is given by

$$y_T = -\left[\ln. \ln \frac{T}{T-1} \right] \qquad (7.22)$$

or $y_T = -\left[0.834 + 2.303 \log \log \dfrac{T}{T-1} \right]$

$\bar{y}_n$ = reduced mean, a function of sample size N and is given in Table 7.3; for $N \to \infty$, $\bar{y}_n \to 0.577$

S_n = reduced standard deviation, a function of sample size N and is given in Table 7.4; for $N \to \infty$, $S_n \to 1.2825$

These equations are used under the following procedure to estimate the flood magnitude corresponding to a given return based on an annual flood series.

1. Assemble the discharge data and note the sample size N. Here the annual flood value is the variate X. Find $\bar{x}$ and σ_{n-1} for the given data.
2. Using Tables 7.3 and 7.4 determine $\bar{y}_n$ and S_n appropriate to given N.
3. Find y_T for a given T by Eq. (7.22).
4. Find K by Eq. (7.21).
5. Determine the required x_T by Eq. (7.20).

The method is illustrated in Example 7.3.

To verify whether the given data follow the assumed Gumbel's distribution, the following procedure may be adopted. The value of x_T for some return periods $T < N$ are calculated by using Gumbel's formula and plotted as x_T vs T on a convenient paper such as a semi-log, log-log or Gumbel probability paper. The use of Gumbel probability paper results in a straight line for x_T vs T plot. Gumbel's distribution has the property

Table 7.3 Reduced mean $\bar{y}_n$ in Gumbel's Extreme Value Distribution

N = sample size

N	0	1	2	3	4	5	6	7	8	9
10	0.4952	0.4996	0.5035	0.5070	0.5100	0.5128	0.5157	0.5181	0.5202	0.5220
20	0.5236	0.5252	0.5268	0.5283	0.5296	0.5309	0.5320	0.5332	0.5343	0.5353
30	0.5362	0.5371	0.5380	0.5388	0.5396	0.5402	0.5410	0.5418	0.5424	0.5430
40	0.5436	0.5442	0.5448	0.5453	0.5458	0.5463	0.5468	0.5473	0.5477	0.5481
50	0.5485	0.5489	0.5493	0.5497	0.5501	0.5504	0.5508	0.5511	0.5515	0.5518
60	0.5521	0.5524	0.5527	0.5530	0.5533	0.5535	0.5538	0.5540	0.5543	0.5545
70	0.5548	0.5550	0.5552	0.5555	0.5557	0.5559	0.5561	0.5563	0.5565	0.5567
80	0.5569	0.5570	0.5572	0.5574	0.5576	0.5578	0.5580	0.5581	0.5583	0.5585
90	0.5586	0.5587	0.5589	0.5591	0.5592	0.5593	0.5595	0.5596	0.5598	0.5599
100	0.5600									

Table 7.4 Reduced Standard Deviation S_n in Gumbel's Extreme Value Distribution

N = sample size

N	0	1	2	3	4	5	6	7	8	9
10	0.9496	0.9676	0.9833	0.9971	1.0095	1.0206	1.0316	1.0411	1.0493	1.0565
20	1.0628	1.0696	1.0754	1.0811	1.0864	1.0915	1.0961	1.1004	1.1047	1.1086
30	1.1124	1.1159	1.1193	1.1226	1.1255	1.1285	1.1313	1.1339	1.1363	1.1388
40	1.1413	1.1436	1.1458	1.1480	1.1499	1.1519	1.1538	1.1557	1.1574	1.1590
50	1.1607	1.1623	1.1638	1.1658	1.1667	1.1681	1.1696	1.1708	1.1721	1.1734
60	1.1747	1.1759	1.1770	1.1782	1.1793	1.1803	1.1814	1.1824	1.1834	1.1844
70	1.1854	1.1863	1.1873	1.1881	1.1890	1.1898	1.1906	1.1915	1.1923	1.1930
80	1.1938	1.1945	1.1953	1.1959	1.1967	1.1973	1.1980	1.1987	1.1994	1.2001
90	1.2007	1.2013	1.2020	1.2026	1.2032	1.2038	1.2044	1.2049	1.2055	1.2060
100	1.2065									

which gives $T = 2.33$ years for the average of the annual series when N is very large. Thus the value of a flood with $T = 2.33$ years is called the *mean annual flood.* In graphical plots this gives a mandatory point through which the line showing variation of x_T with T must pass. For the given data, values of return periods (plotting positions) for various recorded values, x of the variate are obtained by the relation $T = (N + 1)/m$ and plotted on the graph described above. Figure 7.3 shows a good fit of observed data with the theoretical variation line indicating the applicability of Gumbel's distribution to the given data series. By extrapolation of the straight line x_T vs T, values of x_T for $T > N$ can be determined easily (Example 7.3).

GUMBEL PROBABILITY PAPER

The Gumbel probability paper is an aid for convenient graphical representation of Gumbel's distribution. It consists of an abscissa specially marked for various convenient values of the return period T. To construct the T scale on the abscissa, first construct an arithmetic scale of y_T values, say from –2 to +7, as in Fig. 7.3. For selected values of T, say 2, 10, 50, 100, 500 and 1000, find the values of y_T by Eq. (7.22) and mark off those positions on the abscissa. The T-scale is now ready for use as shown in Fig. 7.3.
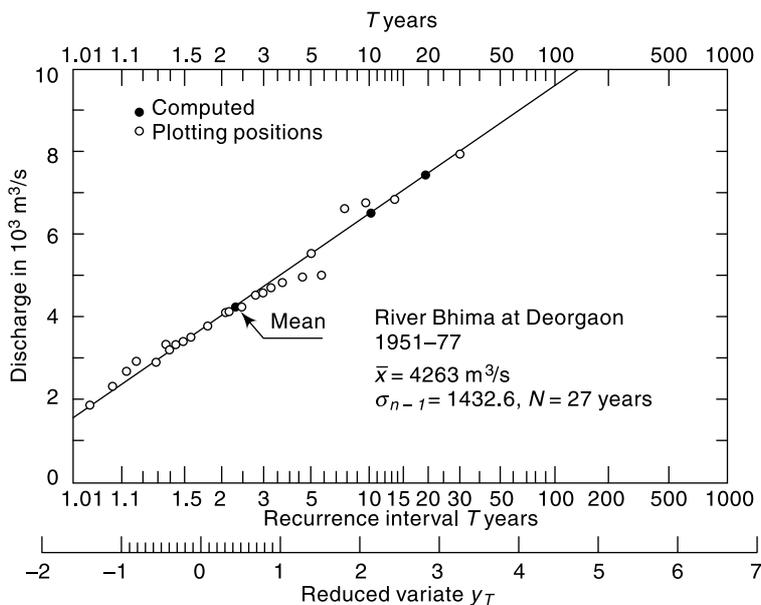

Fig. 7.3   Flood probability analysis by Gumbel's Distribution

The ordinate of a Gumbel paper on which the value of the variate, x_T (flood discharge, maximum rainfall depth, etc.) are plotted may have either an arithmetic scale or logarithmic scale. Since by Eqs (7.18) and (7.19) x_T varies linearly with y_T, a Gumbel distribution will plot as a straight line on a Gumbel probability paper. This property can be used advantageously for graphical extrapolation, wherever necessary.

EXAMPLE 7.4 *Annual maximum recorded floods in the river Bhima at Deorgaon, a tributary of the river Krishna, for the period 1951 to 1977 is given below. Verify whether the Gumbel extreme-value distribution fit the recorded values. Estimate the flood discharge with recurrence interval of (i) 100 years and (ii) 150 years by graphical extrapolation.*

Year	1951	1952	1953	1954	1955	1956	1957	1958	1959
Max. flood (m³/s)	2947	3521	2399	4124	3496	2947	5060	4903	3757

Year	1960	1961	1962	1963	1964	1965	1966	1967	1968
Max. flood (m³/s)	4798	4290	4652	5050	6900	4366	3380	7826	3320

Year	1969	1970	1971	1972	1973	1974	1975	1976	1977
Max. flood (m³/s)	6599	3700	4175	2988	2709	3873	4593	6761	1971

SOLUTION: The flood discharge values are arranged in descending order and the plotting position recurrence interval T_p for each discharge is obtained as

$$T_p = \frac{N+1}{m} = \frac{28}{m}$$

where m = order number. The discharge magnitude Q are plotted against the corresponding T_p on a Gumbel extreme probability paper (Fig. 7.3).

The statistics $\bar{x}$ and an σ_{n-1} for the series are next calculated and are shown in Table 7.5. Using these the discharge x_T for some chosen recurrence interval is calculated by using Gumbel's formulae [Eqs. (7.22), (7.21) and (7.20)].

Table 7.5 Calculation of T_p for Observed Data—*Example 7.4*

Order number m	Flood discharge x (m³/s)	T_p (years)	Order number m	Flood discharge x (m³/s)	T_p (years)
1	7826	28.00	15	3873	1.87
2	6900	14.00	16	3757	1.75
3	6761	9.33	17	3700	1.65
4	6599	7.00	18	3521	1.56
5	5060	5.60	19	3496	1.47
6	5050	4.67	20	3380	1.40
7	4903	4.00	21	3320	1.33
8	4798	3.50	22	2988	1.27
9	4652	3.11	23	2947	—
10	4593	2.80	24	2947	1.17
11	4366	2.55	25	2709	1.12
12	4290	2.33	26	2399	1.08
13	4175	2.15	27	1971	1.04
14	4124	2.00			

$N = 27$ years, $\bar{x} = 4263$ m³/s, $\sigma_{n-1} = 1432.6$ m³/s

From Tables 7.3 and 7.4, for $N = 27$, $y_n = 0.5332$ and $S_n = 1.1004$.

Choosing $T = 10$ years, by Eq. (7.22),

$$y_T = -[\ln \times \ln (10/9)] = 2.25037$$

$$K = \frac{2.25307 - 0.5332}{1.1004} = 1.56$$

$\bar{x}_T = 4263 + (1.56 \times 1432.6) = 6499 \text{ m}^3/\text{s}$

Similarly, values of x_T are calculated for two more T values as shown below.

T years	x_T [obtained by Eq. (7.20)] (m^3/s)
5.0	5522
10.0	6499
20.0	7436

These values are shown in Fig. 7.3. It is seen that due to the property of the Gumbel's extreme probability paper these points lie on a straight line. A straight line is drawn through these points. It is seen that the observed data fit well with the theoretical Gumbel's extreme-value distribution.

[*Note:* In view of the linear relationship of the theoretical x_T and T on a Gumbel probability paper it is enough if only two values of T and the corresponding x_T are calculated. However, if Gumbel's probability paper is not available, a semi-log plot with log scale for T will have to be used and a large set of (x_T, T) values are needed to identify the theoretical curve.]

By extrapolation of the theoretical x_T vs T relationship, from Fig. 7.3,

At $T = 100$ years, $\quad\quad\quad x_T = 9600 \text{ m}^3/\text{s}$

At $T = 150$ years, $\quad\quad\quad x_T = 10{,}700 \text{ m}^3/\text{s}$

[By using Eqs (7.20) to (7.22), $x_{100} = 9558 \text{ m}^3/\text{s}$ and $x_{150} = 10{,}088 \text{ m}^3/\text{s}$.]

EXAMPLE 7.5 *Flood-frequency computations for the river Chambal at Gandhisagar dam, by using Gumbel's method, yielded the following results:*

Return period T (years)	Peak flood (m^3/s)
50	40,809
100	46,300

Estimate the flood magnitude in this river with a return period of 500 years.

SOLUTION: By Eq. (7.20),

$x_{100} = \bar{x} + K_{100}\,\sigma_{n-1} \quad\quad x_{50} = \bar{x} + K_{50}\,\sigma_{n-1}$

$(K_{100} - K_{50})\sigma_{n-1} = x_{100} - x_{50} = 46300 - 40809 = 5491$

But $\quad\quad K_T = \dfrac{y_T}{S_n} - \dfrac{\bar{y}_n}{S_n}$

where S_n and $\bar{y}_n$ are constants for the given data series.

$\therefore \quad\quad (y_{100} - y_{50})\dfrac{\sigma_{n-1}}{S_n} = 5491$

By Eq. (7.22)

$y_{100} = -[\ln \times \ln(100/99)] = 4.60015$

$y_{50} = -[\ln \times \ln(50/99)] = 3.90194$

$\dfrac{\sigma_{n-1}}{S_n} = \dfrac{5491}{(4.60015 - 3.90194)} = 7864$

For $T = 500$ years, by Eq. (7.22),

$$y_{500} = - [\ln \times \ln (500/499)] = 6.21361$$

$$(y_{500} - y_{100}) \frac{\sigma_{n-1}}{S_n} = x_{500} - x_{100}$$

$$(6.21361 - 4.60015) \times 7864 = x_{500} - 46300$$

$$x_{500} = 58988, \text{ say } 59,000 \text{ m}^3/\text{s}$$

EXAMPLE 7.6 *The mean annual flood of a river is 600 m³/s and the standard deviation of the annual flood time series is 150 m³/s. What is the probability of a flood of magnitude 1000 m³/s occurring in the river within next 5 years? Use Gumbel's method and assume the sample size to be very large.*

SOLUTION: $\bar{x} = 600 \text{ m}^3/\text{s}$ and $\sigma_{n-1} = 150 \text{ m}^3/\text{s}$ $x_T = \bar{x} + K\sigma_{n-1}$

$$1000 = 600 + K(150)$$

$$K = 2.6667 = \frac{y_T - 0.577}{1.2825}$$

Hence $y_T = 3.9970$

Also, $y_T = 3.9970 = - \left[\ln \cdot \ln \frac{T}{T-1} \right]$

$\therefore$ $\frac{T}{T-1} = 1.01854$

$$T = 54.9 \text{ years, say } 55 \text{ years}$$

Probability of occurrence of a flood of magnitude 1000 m³/s = $p = 1/55 = 0.0182$
The probability of a flood of magnitude 1000 m³/s occurring at least once in 5 years =

$$p_1 = 1 - (1 - p)^5 = 1 - (0.9818)^5 = 0.0877 = 11.4\%$$

CONFIDENCE LIMITS

Since the value of the variate for a given return period, x_T determined by Gumbel's method can have errors due to the limited sample data used, an estimate of the confidence limits of the estimate is desirable. The confidence interval indicates the limits about the calculated value between which the true value can be said to lie with a specific probability based on sampling errors only.

For a confidence probability c, the confidence interval of the variate x_T is bounded by values x_1 and x_2 given by[6]

$$x_{1/2} = x_T \pm f(c) \, S_e \tag{7.23}$$

where $f(c)$ = function of the confidence probability c determined by using the table of normal variates as

c in per cent	50	68	80	90	95	99
$f(c)$	0.674	1.00	1.282	1.645	1.96	2.58

$$S_e = \text{probable error} = b \frac{\sigma_{n-1}}{\sqrt{N}} \tag{7.23a}$$

$$b = \sqrt{1 + 1.3 K + 1.1 K^2}$$

K = frequency factor given by Eq. (7.21)

σ_{n-1} = standard deviation of the sample

N = sample size.

It is seen that for a given sample and T, 80% confidence limits are twice as large as the 50% limits and 95% limits are thrice as large as 50% limits.

EXAMPLE 7.7 *Data covering a period of 92 years for the river Ganga at Raiwala yielded the mean and standard derivation of the annual flood series as 6437 and 2951 m^3/s respectively. Using Gumbel's method estimate the flood discharge with a return period of 500 years. What are the (a) 95% and (b) 80% confidence limits for this estimate.*

SOLUTION: From Table 7.3 for $N = 92$ years, $\bar{y}_n = 0.5589$ and $S_n = 1.2020$ from Table 7.4.

$$Y_{500} = -[\ln \times \ln (500/499)] = 6.21361$$

$$K_{500} = \frac{6.21361 - 0.5589}{1.2020} = 4.7044$$

$$x_{500} = 6437 + 4.7044 \times 2951 = 20320 \text{ m}^3/s$$

From Eq. (7.33a)

$$b = \sqrt{1 + 1.3(4.7044) + 1.1(4.7044)^2} = 5.61$$

$$S_e = \text{probable error} = 5.61 \times \frac{2951}{\sqrt{92}} = 1726$$

(a) For 95% confidence probability $f(c) = 1.96$ and by Eq. (7.23)
  $x_{1/2} = 20320 \pm (1.96 \times 1726)$ $x_1 = 23703 \text{ m}^3/s$ and $x_2 = 16937 \text{ m}^3/s$
  Thus estimated discharge of 20320 m³/s has a 95% probability of lying between 23700 and 16940 m³/s

(b) For 80% confidence probability, $f(c) = 1.282$ and by Eq. (7.23)
  $x_{1/2} = 20320 \pm (1.282 \times 1726)$ $x_1 = 22533 \text{ m}^3/s$ and $x_2 = 18107 \text{ m}^3/s$
  The estimated discharge of 20320 m³/s has a 80% probability of lying between 22530 and 18110 m³/s.

For the data of Example 7.7, the values of x_T for different values of T are calculated and shown plotted on a Gumbel probability paper in Fig. 7.4. This variation is marked as "fitted line" in the figure. Also shown in this plot are the 95 and 80% confidence limits for various values of T. It is seen that as the confidence probability increases, the confidence interval also increases. Further, an increase in the return period T causes the confidence band to spread. Theoretical work by Alexeev (1961) has shown that for Gumbel's distribution the coefficient of skew $C_s \rightarrow 1.14$ for very low values of N. Thus the Gumbel's distribution will give erroneous results if the sample has a value of C_s very much different from 1.14.
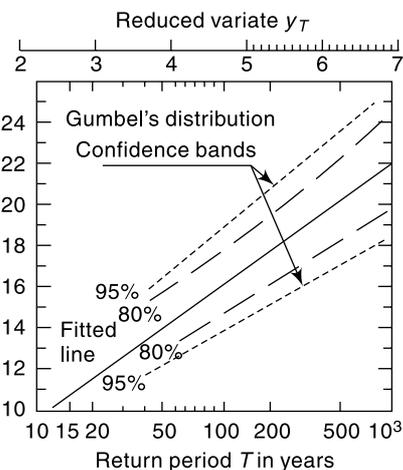

Fig. 7.4 Confidence Bands for Gumbels Distribution — Example 7.7

(*Contd.*)

1.2	−0.195	1.340	2.087	2.626	3.149	3.661	4.820
1.0	−0.164	1.340	2.043	2.542	3.022	3.489	4.540
0.9	−0.148	1.339	2.018	2.498	2.957	3.401	4.395
0.8	−0.132	1.336	1.998	2.453	2.891	3.312	4.250
0.7	−0.116	1.333	1.967	2.407	2.824	3.223	4.105
0.6	−0.099	1.328	1.939	2.359	2.755	3.132	3.960
0.5	−0.083	1.323	1.910	2.311	2.686	3.041	3.815
0.4	−0.066	1.317	1.880	2.261	2.615	2.949	3.670
0.3	−0.050	1.309	1.849	2.211	2.544	2.856	3.525
0.2	−0.033	1.301	1.818	2.159	2.472	2.763	3.380
0.1	−0.017	1.292	1.785	2.107	2.400	2.670	3.235
0.0	**0.000**	**1.282**	**1.751**	**2.054**	**2.326**	**2.576**	**3.090**
−0.1	0.017	1.270	1.716	2.000	2.252	2.482	2.950
−0.2	0.033	1.258	1.680	1.945	2.178	2.388	2.810
−0.3	0.050	1.245	1.643	1.890	2.104	2.294	2.675
−0.4	0.066	1.231	1.606	1.834	2.029	2.201	2.540
−0.5	0.083	1.216	1.567	1.777	1.955	2.108	2.400
−0.6	0.099	1.200	1.528	1.720	1.880	2.016	2.275
−0.7	0.116	1.183	1.488	1.663	1.806	1.926	2.150
−0.8	0.132	1.166	1.448	1.606	1.733	1.837	2.035
−0.9	0.148	1.147	1.407	1.549	1.660	1.749	1.910
−1.0	0.164	1.128	1.366	1.492	1.588	1.664	1.880
−1.4	0.225	1.041	1.198	1.270	1.318	1.351	1.465
−1.8	0.282	0.945	1.035	1.069	1.087	1.097	1.130
−2.2	0.330	0.844	0.888	0.900	0.905	0.907	0.910
−3.0	0.396	0.660	0.666	0.666	0.667	0.667	0.668

[*Note:* $C_s = 0$ corresponds to log-normal distribution]

EXAMPLE 7.8 *For the annual flood series data given in Example 7.4, estimate the flood discharge for a return period of (a) 100 years (b) 200 years and (c) 1000 years by using log-Pearson Type III distribution.*

SOLUTION: The variate $z = \log x$ is first calculated for all the discharges (Table 7.7). Then the statistics $\bar{Z}$, σ_z and C_s are calculated from Table 7.7 to obtain

Table 7.7 Variate Z—*Example* 7.8

Year	Flood x (m³/s)	$z = \log x$	Year	Flood x (m³/s)	$z = \log x$
1951	2947	3.4694	1965	4366	3.6401
1952	3521	3.5467	1966	3380	3.5289
1953	2399	3.3800	1967	7826	3.8935
1954	4124	3.6153	1968	3320	3.5211
1955	3496	3.5436	1969	6599	3.8195
1956	2947	3.4694	1970	3700	3.5682

(*Contd.*)

(*Contd.*)

1957	5060	3.7042	1971	4175	3.6207
1958	4903	3.6905	1972	2988	3.4754
1959	3751	3.5748	1973	2709	3.4328
1960	4798	3.6811	1974	3873	3.5880
1961	4290	3.6325	1975	4593	3.6621
1962	4652	3.6676	1976	6761	3.8300
1963	5050	3.7033	1977	1971	3.2947
1964	6900	3.8388			

$$\sigma_z = 0.1427 \qquad C_s = \frac{27 \times 0.0030}{(26)\,(25)\,(0.1427)^3}$$

$$\bar{Z} = 3.6071 \qquad C_s = 0.043$$

The flood discharge for a given T is calculated as below. Here, values of K_z for given T and $C_s = 0.043$ are read from Table 7.6.

| | $\bar{Z} = 3.6071$ | $\sigma_z = 0.1427$ | $C_s = 0.043$ | |
T (years)	K_z (from Table 7.6) (for $C_s = 0.043$)	$K_z\sigma_z$	$Z_T = \bar{Z} + K_z\sigma_z$	x_T = antilog z_T (m³/s)
100	2.358	0.3365	3.9436	8782
200	2.616	0.3733	3.9804	9559
1000	3.152	0.4498	4.0569	11400

EXAMPLE 7.9 *For the annual flood series data analyzed in Example 7.8 estimate the flood discharge for a return period of (a) 100 years, (b) 200 years, and (c) 1000 years by using log-normal distribution. Compare the results with those of Example 7.8.*

SOLUTION: Log-normal distribution is a special case of log-Pearson type III distribution with $C_s = 0$. Thus in this case C_s is taken as zero. The other statistics are $\bar{z} = 3.6071$ and $\sigma_z = 0.1427$ as calculated in Example 7.8.

The value of K for a given return period T and $C_s = 0$ is read from Table 7.6. The estimation of the required flood discharge is done as shown below.

| | $\bar{z} = 3.6071$ | $\sigma_z = 0.1427$ | $C_s = 0$ | |
T (years)	K_z (from Table 7.6)	$K_z\,\sigma_z$	$Z_T = \bar{Z} + K_z\,\sigma_z$	x_T = antilog z_T (m³/s)
100	2.326	0.3319	3.9390	8690
200	2.576	0.3676	3.9747	9434
1000	3.090	0.4409	4.0480	11170

On comparing the estimated x_T with the corresponding values in Example 7.8, it is seen that the inclusion of the positive coefficient of skew ($C_s = 0.047$) in log-Pearson type III method gives higher values than those obtained by the log-normal distribution method. However, as the value of C_s is small, the difference in the corresponding values of x_T by the two methods is not appreciable.

[*Note:* If the coefficient of skew is negative, the log-Pearson type III method gives consistently lower values than those obtained by the log-normal distribution method.]

7.8 PARTIAL DURATION SERIES

In the annual hydrologic data series of floods, only one maximum value of flood per year is selected as the data point. It is likely that in some catchments there are more than one independent floods in a year and many of these may be of appreciably high magnitude. To enable all the large flood peaks to be considered for analysis, a flood magnitude larger than an arbitrary selected base value are included in the analysis. Such a data series is called *partial-duration series.*

In using the partial-duration series, it is necessary to establish that all events considered are independent. Hence the partial-duration series is adopted mostly for rainfall analysis where the conditions of independency of events are easy to establish. Its use in flood studies is rather rare. The recurrence interval of an event obtained by annual series (T_A) and by the partial duration series (T_p) are related by

$$T_P = \frac{1}{\ln T_A - \ln (T_A - 1)} \qquad (7.28)$$

From this it can be seen that the difference between T_A and T_P is significant for $T_A < 10$ years and that for $T_A > 20$, the difference is negligibly small.

7.9 REGIONAL FLOOD FREQUENCY ANALYSIS

When the available data at a catchment is too short to conduct frequency analysis, a regional analysis is adopted. In this a hydrologically homogeneous region from the statistical point of view is considered. Available long time data from neighbouring catchments are tested for homogeneity and a group of stations satisfying the test are identified. This group of stations constitutes a region and all the station data of this region are pooled and analysed as a group to find the frequency characteristics of the region. The mean annual flood Q_{ma}, which corres-ponds to a recurrence interval of 2.33 years is used for nondimensionalising the results. The variation of Q_{ma} with drainage area and the variation of Q_T/Q_{ma} with T where Q_T is the discharge for any T are the basic plots prepared in this analysis. Details of the method are available in Ref. 2.

7.10 DATA FOR FREQUENCY STUDIES

The flood-frequency analysis described in the previous sections is a direct means of estimating the desired flood based upon the available flood flow data of the catchment. The results of the frequency analysis depend upon the length of data. The minimum number of years of record required to obtain satisfactory estimates depends upon the variability of data and hence on the physical and climatological characteristics of the basin. Generally a minimum of 30 years of data is considered as essential. Smaller lengths of records are also used when it is unavoidable. However, frequency analysis should not be adopted if the length of records is less than 10 years.

In the frequency analysis of time series, such as of annual floods, annual yields and of precipitation, some times one comes across very long (say of the order of 100 years) times series. In such cases it is necessary to test the series for *Homogeneity* to ascertain that there is no significant difference in the causative hydrological processes over the span of the time series. A time series is called time-homogeneous (also known as *stationary*) if identical events under consideration in the series are likely to occur at all times. Departure from time homogeneity is reflected either in trend or periodicity

or persistence of the variable over time. Potential non-homogeneity region, (if any), could be detected by (i) mass curve or (ii) by moving mean of the variable. Statistical tests like *F-test* for equality of variances and *t-test* for significance of differences of means are adopted to identify non- homogeneous region/s in the series. Only the contiguous homogeneous region of the series covering the recent past is to be adopted for frequency analysis. However, it is prudent to test all time series, whether long or short, for time-homogeneity before proceeding with the frequency analysis. Thus the cardinal rule with the data of time series would be that the data should be reliable and homogeneous.

Flood frequency studies are most reliable in climates that are uniform from year to year. In such cases a relatively short record gives a reliable picture of the frequency distribution.

7.11   DESIGN FLOOD

In the design of hydraulic structures it is not practical from economic considerations to provide for the safety of the structure and the system at the maximum possible flood in the catchment. Small structures such as culverts and storm drainages can be designed for less severe floods as the consequences of a higher than design flood may not be very serious. It can cause temporary inconvenience like the disruption of traffic and very rarely severe property damage and loss of life. On the other hand, storage structures such as dams demand greater attention to the magnitude of floods used in the design. The failure of these structures causes large loss of life and great property damage on the downstream of the structure. From this it is apparent that the type, importance of the structure and economic development of the surrounding area dictate the design criteria for choosing the flood magnitude. This section highlights the procedures adopted in selecting the flood magnitude for the design of some hydraulic structures.

The following definitions are first noted.

DESIGN FLOOD   Flood adopted for the design of a structure.

SPILLWAY DESIGN FLOOD   Design flood used for the specific purpose of designing the spillway of a storage structure. This term is frequently used to denote the maximum discharge that can be passed in a hydraulic structure without any damage or serious threat to the stability of the structure.

STANDARD PROJECT FLOOD (SPF)   The flood that would result from a severe combination of meteorological and hydrological factors that are reasonably applicable to the region. Extremely rare combinations of factors are excluded.

PROBABLE MAXIMUM FLOOD (PMF)   The extreme flood that is physically possible in a region as a result of severemost combinations, including rare combinations of meteorological and hydrological factors.

The PMF is used in situations where the failure of the structure would result in loss of life and catastrophic damage and as such complete security from potential floods is sought. On the other hand, SPF is often used where the failure of a structure would cause less severe damages. Typically, the SPF is about 40 to 60% of the PMF for the same drainage basin. The criteria used for selecting the design flood for various

Table 7.8   Guidelines for Selecting Design Floods (CWC, India)[1]

S. No.	Structure	Recommended design flood
1.	Spillways for major and medium projects with storages more than 60 Mm^3	(a) PMF determined by unit hydrograph and probable maximum precipitation (PMP) (b) If (a) is not applicable or possible flood-frequency method with $T = 1000$ years
2.	Permanent barrage and minor dams with capacity less than 60 Mm^3	(a) SPF determined by unit hydrograph and standard project storm (SPS) which is usually the largest recorded storm in the region (b) Flood with a return period of 100 years. (a) or (b) whichever gives higher value.
3.	Pickup weirs	Flood with a return period of 100 or 50 years depending on the importance of the project.
4.	Aqueducts (a) Waterway (b) Foundations and free board	Flood with $T = 50$ years Flood with $T = 100$ years Empirical formulae
5.	Project with very scanty or in-adequate data	

hydraulic structures vary from one country to another. Table 7.8 gives a brief summary of the guidelines adopted by CWC India, to select design floods.

THE INDIAN STANDARD GUIDELINES FOR DESIGN OF FLOODS FOR DAMS

"IS : 11223—1985 : Guidelines for fixing spillway capacity" (Ref. 4) is currently used in India for selection of design floods for dams. In these guidelines, dams are classified according to size by using the hydraulic head and the gross storage behind the dam. The hydraulic head is defined as the difference between the maximum water level on the upstream and the normal annual average flood level on the downstream. The classification is shown in Table 7.9(a). The overall size classifications for dams would be greater of that indicated by either of the two parameters. For example, a dam with a gross storage of 5 Mm^3 and hydraulic head of 15 m would be classified as *Intermediate* size dam.

Table 7.9(a)   Size Classification of Dams

Class	Gross storage (Mm^3)	Hydraulic head (m)
Small	0.5 to 10.0	7.5 to 12.0
Intermediate	10.0 to 60.0	12.0 to 30.0
Large	> 60.0	> 30.0

The inflow design flood (IDF) for safety of the dam is taken for each class of dam as given in Table 7.9(b).

Table 7.9(b)   Inflow Design Flood for Dams

Size/Class (based on Table 7.9(a))	Inflow design flood for safety
Small	100-year flood
Intermediate	Standard project flood (SPF)
Large	Probable Maximum flood (PMF)

7.12 DESIGN STORM

To estimate the design flood for a project by the use of a unit hydrograph, one needs the design storm. This can be the storm-producing probable maximum precipitation (PMP) for deriving PMF or a standard project storm (SPS) for SPF calculations. The computations are performed by experienced hydrometeorologists by using meteorological data. Various methods ranging from highly sophisticated hydrometeorological methods to simple analysis of past rainfall data are in use depending on the availability of reliable relevant data and expertise.

The following is a brief outline of a procedure followed in India:

- The duration of the critical rainfall is first selected. This will be the basin lag if the flood peak is of interest. If the flood volume is of prime interest, the duration of the longest storm experienced in the basin is selected.
- Past major storms in the region which conceivably could have occurred in the basin under study are selected. DAD analysis is performed and the enveloping curve representing maximum depth–duration relation for the study basin obtained.
- Rainfall depths for convenient time intervals (e.g. 6 h) are scaled from the enveloping curve. These increments are to be arranged to get a critical sequence which produces the maximum flood peak when applied to the relevant unit hydrograph of the basin.

  The critical sequence of rainfall increments can be obtained by trial and error. Alternatively, increments of precipitation are first arranged in a table of relevant unit hydrograph ordinates, such that (i) the maximum rainfall increment is against the maximum unit hydrograph ordinate, (ii) the second highest rainfall increment is against the second largest unit hydrograph ordinate, and so on, and (iii) the sequence of rainfall increments arranged above is now reversed, with the last item first and first item last. The new sequence gives the design storm (Example 7.8).

- The design storm is then combined with hydrologic abstractions most conducive to high runoff, viz. low initial loss and lowest infiltration rate to get the hyetograph of rainfall excess to operate upon the unit hydrograph.

  Further details about the above procedure and other methods for computing design storms are available in Ref. 7. Reference 1 gives details of the estimation of the design flood peak by unit hydrographs for small drainage basins of areas from 25–500 km^2.

EXAMPLE 7.10 *The ordinates of cumulative rainfall from the enveloping maximum depth–duration curve for a basin are given below. Also given are the ordinates of a 6-h unit hydrograph. Design the critical sequence of rainfall excesses by taking the φ index to be 0.15 cm/h.*

SOLUTION: The critical storm and rainfall excesses are calculated in a tabular form in Table 7.10.

Time from start (h)	0	6	12	18	24	30	36	42	48	54	60
Cumulative rainfall (cm)	0	15	24.1	30	34	37	39	40.5	41.3		
6-h UH ordinate (m^3/s)	0	20	54	98	126	146	154	152	138	122	106

Time from start (h)	66	72	78	84	90	96	102	108	114	129	132
6-h UH ordinate (m^3/s)	92	79	64	52	40	30	20	14	10	6	0

Table 7.10 Calculation of Critical Storm — *Example* 7.10

Time (h)	Cumulative rainfall (cm)	6-h incremental rainfall (cm)	Ordinate of 6-h UH (m^3/s)	First arrangement of rainfall increment	Design sequence of rainfall increment	Infiltration loss (cm)	Rainfall excess of design storm (cm)
1	2	3	4	5	6	7	8
0	0		0		0	0	0
6	15.0	15.0	20		1.5	0.9	0.6
12	24.1	9.1	54		2.0	0.9	1.1
18	30.0	5.9	98	0.8	4.0	0.9	3.1
24	34.0	4.0	126	3.0	9.1	0.9	8.2
30	37.0	3.0	146	5.9	15.0	0.9	14.1
36	39.0	2.0	154	15.0	5.9	0.9	5.0
42	40.5	1.5	152	9.1	3.0	0.9	2.1
48	41.3	0.8	138	4.0	0.8	0.9	0
54			122	2.0			
60			106	1.5			
66			92				
72			79				
78			64				
84			52				
90			40				
96			30				
102			20				
108			14				
114			10				
120			6				
132			0				

1. (Column 6 is reversed sequence of column 5)
2. Infiltration loss = 0.15 cm/h = 0.9 cm/6 h