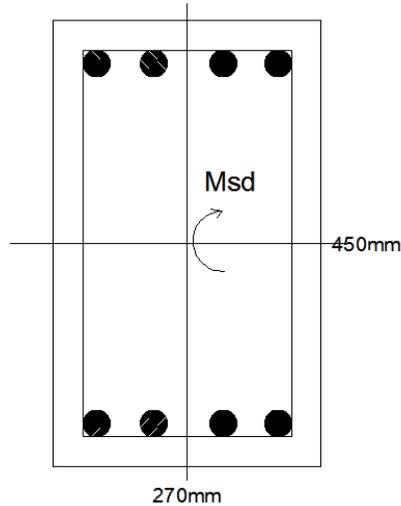


Example 4.1 [Uni-axial Column Design]

1. Design the braced short column to sustain a design load of 1100 kN and a design moment of 160 kNm which include all other effects. Use C25/30 and S460.

Take $\frac{d'}{H} = 0.1$ and section $270 \text{ mm} \times 450 \text{ mm}$



Solution

Step 1- Material

$$f_{cd} = \frac{0.85 * 25}{1.5} = 14.16667 \text{ mpa}$$

$$f_{yd} = \frac{460}{1.15} = 400 \text{ mpa}$$

Step 2-Determine the normalized axial and bending moment value

$$v_{sd} = \frac{N_{sd}}{f_{cd}bh} = \frac{1100 * 10^3}{14.1667 * 270 * 450} = 0.639$$

$$\mu_{sd} = \frac{m_{sd}}{f_{cd}bd^2} = \frac{160 * 10^6}{14.1667 * 270 * 450^2} = 0.2065$$

Step 3-Using $\frac{d'}{H} = 0.1$ read the mechanical steel ratio from uniaxial interaction chart for

$$V_{sd} = 0.639 \quad \mu_{sd} = 0.2065$$

From interaction chart $\omega = 0.3$

$$A_{s,tot} = \frac{\omega f_{cd} b d}{f_{yd}} = \frac{0.3 * 14.166 * 270 * 450}{400} = 1290.937 \text{ mm}^2$$

$$A = \frac{A_{s,tot}}{2} = \frac{1290.937}{2} = 645.468 \text{ mm}^2$$

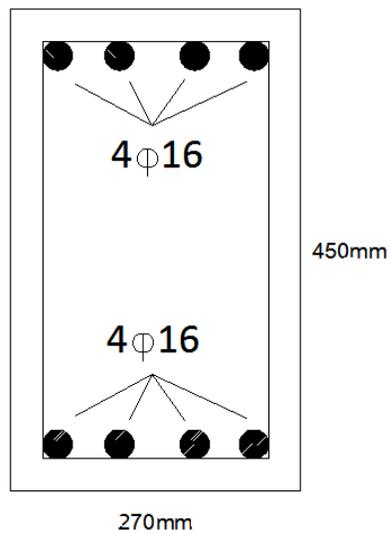
Check with maximum and minimum reinforcement limit

$$A_{s,min} = \max \left\{ \begin{array}{l} \frac{0.1 N_{ED}}{f_{yd}} = 275 \text{ mm}^2 \\ 0.002 A_c \end{array} \right. \quad \text{OK!}$$

$$A_{s,max} = 0.08 A_c = 0.08 * 270 * 450 = \quad \text{OK!}$$

Step 4- Detailing

Use 4Ø16 on each face



Example 4.2 [Biaxial column design]

Determine the longitudinal reinforcement for corner column of size 400*400 mm and the design factored moment and axial force of

$$P = 1360 \text{ KN} \quad M_{sd,h} = 200 \text{ KNm} \quad M_{sd,b} = 100 \text{ KNm}$$

Use C25/30 and S460 class 1 work take $\frac{h'}{h} = \frac{b'}{b} = 0.1$

Solution

Step 1- Material

$$f_{cd} = \frac{0.85 * 25}{1.5} = 14.16667 \text{ mpa}$$
$$f_{yd} = \frac{460}{1.15} = 400 \text{ mpa}$$

Step 2- Determine the normalized axial and bending moment value

$$v_{sd} = \frac{p}{f_{cd}bh} = \frac{1360 * 10^3}{14.1667 * 400 * 400} = 0.6$$

$$\mu_{sd,h} = \frac{m_{sd}}{f_{cd}bd^2} = \frac{200 * 10^6}{14.1667 * 400 * 400^2} = 0.2206$$

$$\mu_{sd,b} = \frac{m_{sd}}{f_{cd}db^2} = \frac{100 * 10^6}{14.1667 * 400 * 400^2} = 0.1103$$

Step 3- Find ω using $\frac{d'}{d} = \frac{b'}{B} = 0.1$, $V_{sd} = 0.6$,

$$\mu_{sd,h} = 0.2206 ,$$

$$\mu_{sd,b} = 0.1103$$

From biaxial chart $\omega = 0.6$

$$A_{s,tot} = \frac{\omega f_{cd}bd}{f_{yd}} = \frac{0.6 * 14.166 * 400 * 400}{400} = 3400 \text{ mm}^2$$

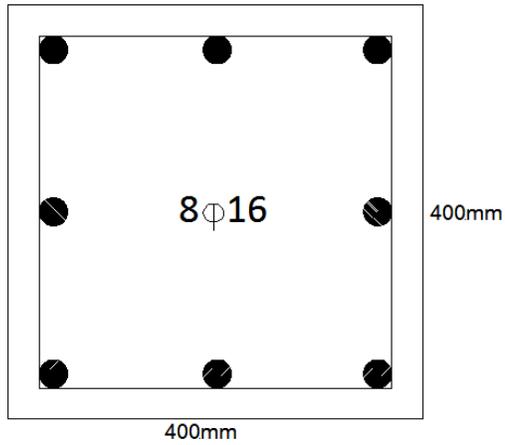
Check with maximum and minimum reinforcement limit

$$A_{s,min} = \max \left\{ \begin{array}{l} \frac{0.1 N_{ED}}{f_{yd}} = 340 \text{ mm}^2 \\ 0.002 A_c \end{array} \right. \quad \text{OK!}$$

$$A_{s,max} = 0.08 A_c = 0.08 * 400 * 400 = 12800 \quad \text{OK!}$$

Step 4- Detailing

$$\text{using } \phi 24 \quad n = \frac{3400}{452.16} = 7.52 \quad \text{so Use } 8\phi 24$$

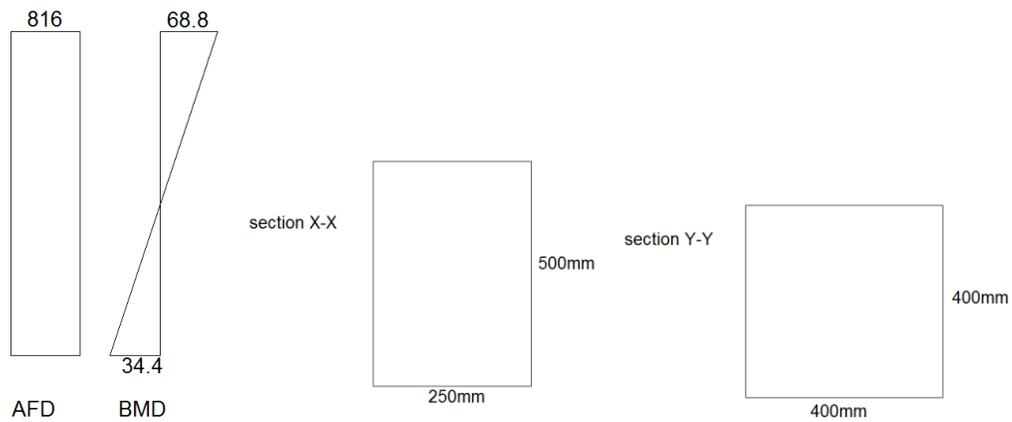
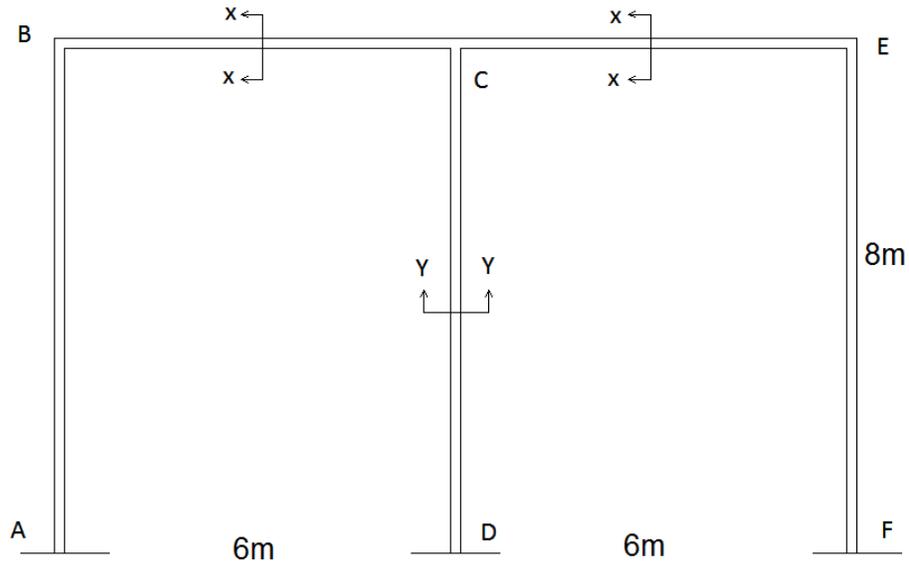


Example 4.3 [Column]

Determine whether the column CD is slender or not, if it is subjected to loads shown below.

Consider the frame to be non-sway

Use C25/30 $f_{cd} = 14.1667 \text{ mpa}$



Solution

Step 1- Slenderness limit

$$\lambda_{lim} = \frac{20ABC}{\sqrt{n}} \quad \text{take } A = 0.7 \quad B = 1.1 \quad C = 1.7 - r_m$$

$$\text{where } r_m = \frac{m_{01}}{m_{02}} = \frac{-34.4}{68.8} = -0.5 \quad C = 1.7 - (-0.5) = 2.2$$

$$n = \frac{N_{ed}}{A_c f_{cd}} = \frac{516 * 10^3}{14.1667 * 400 * 400} = 0.227647$$

$$\lambda_{lim} = \frac{20 * 0.7 * 1.1 * 2.2}{\sqrt{0.227647}} = 71.0088$$

Step 2-Find the slenderness of the column

2.1 Effective length

For Braced member

$$l_0 = 0.5l \sqrt{\left[1 + \frac{K_1}{0.5 + K_1}\right] \left[1 + \frac{K_2}{0.5 + K_2}\right]}$$

$$K = \frac{\text{Column stiffness}}{\sum \text{beam stiffness}}$$

$$K_i = \frac{(EI/l)_{\text{column}}}{2(2EI/l)_{\text{beam}}}$$

$$I_{\text{column}} = \frac{400 * 400^3}{12} = 2133333333 \text{ mm}^4$$

$$I_{\text{beam}} = \frac{250 * 500^3}{12} = 2604166667 \text{ mm}^4$$

$$K_1 = \frac{\frac{2133333333E}{8000}}{2\left(\frac{2 * 2604166667E}{6000}\right)} = 0.1536$$

For fixed restraint $K=0$ but in reality we cannot provide a fully fixed support so use $K_2 = 0.1$

$$l_0 = 0.5 * 6000 \sqrt{\left[1 + \frac{0.1536}{0.5 + 0.1536}\right] \left[1 + \frac{0.1}{0.5 + 0.1}\right]} = 3601.050 \text{ mm}$$

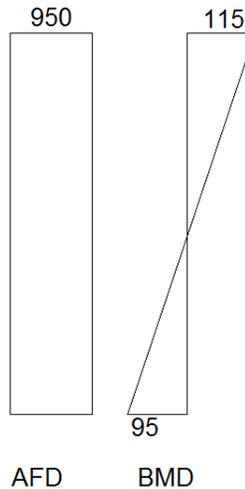
$$\lambda = \frac{l_0}{i} \quad i = \sqrt{\frac{I}{A}} = \sqrt{\frac{2133333333}{160000}} = 115.470 \text{ mm}$$

$$\lambda = \frac{3601.0504}{115.470} = 31.186 \text{ mm}$$

$$\lambda < \lambda_{lim} \quad \text{Short column}$$

Example 4.4 [Column Design]

Design the braced column to resist an axial load of 950 kN and a moment of $M_{sd} = 115$ kNm at the top and $M_{sd} = -95$ kNm at the bottom as shown below. Length of the column is 5.5 m and cross-section of 300*300 mm use C25/30 and S460 take $L_e = 0.66L$



Solution

Step 1- Material

$$f_{cd} = \frac{0.85 * 25}{1.5} = 14.16667 \text{ mpa}$$

$$f_{yd} = \frac{460}{1.15} = 400 \text{ mpa}$$

Step 2- Check slenderness limit

$$\lambda_{lim} = \frac{20ABC}{\sqrt{n}} \quad \text{take } A = 0.7 \quad B = 1.1 \quad C = 1.7 - r_m$$

$$\text{where } r_m = \frac{m_{01}}{m_{02}} = \frac{-95}{115} = -0.826 \quad C = 1.7 - (-0.826) = 2.526$$

$$n = \frac{N_{ed}}{A_c f_{cd}} = \frac{950 * 10^3}{14.1667 * 300 * 300} = 0.745$$

$$\lambda_{lim} = \frac{20 * 0.7 * 1.1 * 2.526}{\sqrt{0.745}} = 45.066$$

Step 3- Slenderness

$$\lambda = \frac{l_o}{i} \quad i = \sqrt{\frac{I}{A}} = \sqrt{\frac{675000000}{90000}} = 86.6025 \text{ mm}$$

$$\lambda = \frac{0.66 * 5500}{86.6025} = 41.915$$

$$\lambda < \lambda_{lim} \quad \text{Short column neglect second order effect}$$

Step 4- accidental eccentricity

$$e_a = \frac{l_o}{400} = \frac{3630}{400} = 9.075 \text{ mm}$$

Step 5- Equivalent first order eccentricity

$$e_e = \max \begin{cases} 0.6e_{02} + 0.4 e_{01} \\ 0.4e_{02} \end{cases}$$

$$e_{02} = \frac{M_{02}}{N_{sd}} = \frac{115 * 10^6}{950 * 10^3} = 121.052 \text{ mm}$$

$$e_{01} = \frac{M_{01}}{N_{sd}} = \frac{95 * 10^6}{950 * 10^3} = 100 \text{ mm}$$

$$e_e = \max \begin{cases} 0.6e_{02} + 0.4 e_{01} \\ 0.4e_{02} \end{cases} = 48.4208 \text{ mm}$$

$$e_{tot} = e_o + e_e + e_2 = 9.075 + 48.4208 + 0 = 57.4958 \text{ mm}$$

$$\text{check with } e = e_{02} + e_a = 121.052 + 9.075 = 130.127 \text{ mm}$$

$$\text{So take } e_{tot} = 130.127 \text{ mm}$$

Step 6- Design

$$N_{sd} = 950 \text{ KN} \quad M_{sd} = N_{sd} * e_{tot} = 123.62 \text{ KNm}$$

$$v_{sd} = \frac{p}{f_{cd}bh} = \frac{950 * 10^3}{14.1667 * 300 * 300} = 0.745$$

$$\mu_{sd} = \frac{m_{sd}}{f_{cd}bd^2} = \frac{123.62 * 10^6}{14.1667 * 300 * 300^2} = 0.3232$$

Using $\frac{d'}{d} = 0.15$ read the mechanical steel ratio from uniaxial interaction chart for

$$V_{sd} = 0.745$$

$$\mu_{sd} = 0.3232$$

$$\omega = 0.79$$

$$A_{s,tot} = \frac{\omega f_{cd}bd}{f_{yd}} = \frac{0.79 * 14.166 * 300 * 300}{400} = 2518.125 \text{ mm}^2$$

$$A = \frac{A_{s,tot}}{2} = \frac{2518.125}{2} = 1259.0625 \text{ mm}^2$$

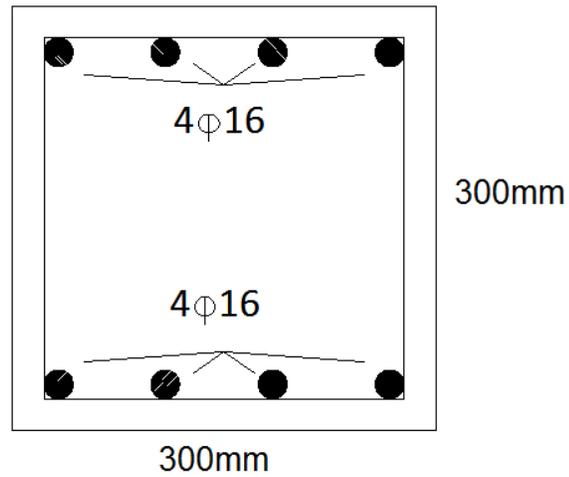
Check with maximum and minimum reinforcement limit

$$A_{s,min} = \max \left\{ \begin{array}{l} \frac{0.1 N_{ED}}{f_{yd}} = 237.5 \text{ mm}^2 \quad \text{OK!} \\ 0.002 A_c \end{array} \right.$$

$$A_{s,max} = 0.08 A_c = 0.08 * 300 * 300 = 7200 \text{ mm}^2 \quad \text{OK!}$$

Using $\phi 20$ provide $4\phi 20$ on each face

Step 7- Detailing



Example 4.5 [Column]

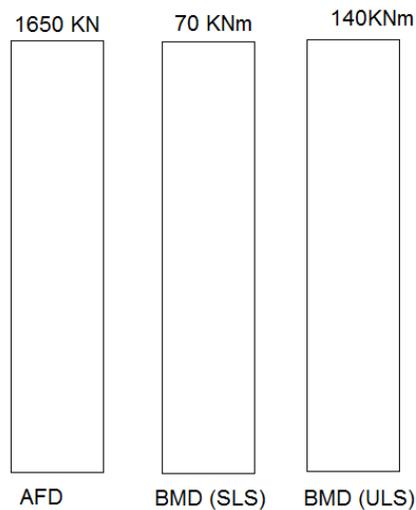
Design the braced column if it is subjected to the following loading .the column has total length of 6 m. $L_e=0.7L$

Use C25/30 and S460

If the column is slender .compute the total design moment using

- a) Nominal curvature
- b) Nominal stiffness

Use 400*400 mm section $\frac{d'}{d} = 0.1$ use $\phi(\infty, t_o) = 2$



Solution

Step 1. Material data

$$f_{cd} = \frac{0.85 * 25}{1.5} = 14.16667 \text{ mpa}$$

$$f_{yd} = \frac{460}{1.15} = 400 \text{ mpa}$$

$$E_{cm} = 30 \text{ Gpa}$$

$$E_s = 200 \text{ Gpa}$$

Step 2- Check slenderness limit

$$\lambda_{lim} = \frac{20ABC}{\sqrt{n}} \quad \text{take } A = 0.7 \quad B = 1.1 \quad C = 1.7 - r_m$$

$$\text{where } r_m = \frac{m_{01}}{m_{02}} = \frac{140}{140} = 1 \quad C = 1.7 - (1) = 0.7$$

$$n = \frac{N_{ed}}{A_c f_{cd}} = \frac{1650 * 10^3}{14.1667 * 400 * 400} = 0.72794$$

$$\lambda_{lim} = \frac{20 * 0.7 * 1.1 * 0.7}{\sqrt{0.72794}} = 12.63487$$

Step 3-slenderess

$$\lambda = \frac{l_o}{i} \quad i = \sqrt{\frac{I}{A}} = \sqrt{\frac{2133333333}{160000}} = 115.470 \text{ mm}$$

$$\lambda = \frac{0.7 * 6000}{115.470} = 36.373$$

$$\lambda > \lambda_{lim} \quad \text{Slender column consider second order effect}$$

Step 4- accidental eccentricity

$$e_a = \frac{l_o}{400} = \frac{4200}{400} = 10.5 \text{ mm}$$

Step 5- Equivalent first order eccentricity

$$e_e = \max \begin{cases} 0.6e_{02} + 0.4 e_{01} \\ 0.4e_{02} \end{cases}$$

$$e_{02} = \frac{M_{02}}{N_{sd}} = \frac{140 * 10^6}{1650 * 10^3} = 84.848 \text{ mm}$$

$$e_{01} = \frac{M_{01}}{N_{sd}} = \frac{140 * 10^6}{1650 * 10^3} = 84.848 \text{ mm}$$

$$e_e = \max \begin{cases} 0.6e_{02} + 0.4 e_{01} \\ 0.4e_{02} \end{cases} = 84.848 \text{ mm}$$

Step 6- Calculate the second order moment

a) Using Nominal curvature method

$$e_2 = \frac{1}{r} l_o^2 / C \quad C = 10 \quad \text{For constant cross - section}$$

$$\frac{1}{r} = K_r K_\phi \frac{1}{r_o} \quad K_\phi = 1 + \beta \phi_{eff}$$

$$\phi_{eff} = 0 \quad \text{if} \quad \begin{cases} \phi(\infty, t_o) \leq 2 \quad \text{OK} \\ \lambda \leq 75 \quad \text{OK} \\ \frac{M_{oed}}{N_{ed}} \geq h \quad \text{Not OK} \end{cases}$$

$$\phi_{eff} = \phi(\infty, t_o) \frac{M_{oeqp}}{M_{oed}}$$

where M_{oeqp} = first order moment in quasi – permanent load (SLS)

M_{oed} = First order moment in design load combination (ULS)

$$\phi_{eff} = \phi(\infty, t_o) \frac{M_{oeqp}}{M_{oed}} = 2 * \frac{70}{140} = 1$$

$$\beta = 0.35 + \frac{f_{ck}}{200} - \frac{\lambda}{150} = 0.35 + \frac{25}{200} - \frac{36.375}{150} = 0.2325$$

$$K_{\phi} = 1 + \beta \phi_{eff} = 1 + 0.2325 * 1 = 1.2325$$

$$\frac{1}{r_o} = \frac{\epsilon_{yd}}{0.45d} = \frac{2 * 10^{-3}}{360} = 123456 * 10^{-5} \quad d = \text{effective depth}$$

$$K_r = \frac{(n_u - n)}{(n_u - n_{bal})} \quad n_u = 1 + \omega \quad n = \frac{N_{ed}}{A_c f_{cd}} = \frac{1650 * 10^3}{14.166 * 400^2} \\ = 0.72974 \quad n_{bal} = 0.4$$

For first iteration take $e_2 = 0$

$$e_{tot} = e_o + e_e + e_2 = 10.5 + 84.848 + 0 = 95.348 \text{ mm}$$

$$N_{sd} = 1650 \text{ KN} \quad M_{sd} = N_{sd} * e_{tot} = 157.3242 \text{ KNm}$$

$$v_{sd} = \frac{N_{sd}}{f_{cd} b h} = \frac{1650 * 10^3}{14.1667 * 400 * 400} = 0.72794$$

$$\mu_{sd} = \frac{m_{sd}}{f_{cd} b d^2} = \frac{157.3242 * 10^6}{14.1667 * 400 * 400^2} = 0.17352$$

$$\text{Using } v_{sd} = 0.72794 \quad \mu_{sd} = 0.1752 \quad \frac{d'}{d} = 0.1 \quad \omega = 0.25$$

So

$$n_u = 1 + \omega = 1.25 \quad K_r = \frac{(n_u - n)}{(n_u - n_{bal})} = \frac{(1.25 - 0.72794)}{(1.25 - 0.4)} = 0.614$$

$$\frac{1}{r} = 0.614 * 1.2325 * 1.23456 * 10^{-5} = 9.3456 * 10^{-6}$$

$$e_2 = \frac{1}{r} 4200^2 / 10 = 16.485 \text{ mm}$$

For Second iteration take $e_2 = 16.485 \text{ mm}$

$$e_{tot} = e_o + e_e + e_2 = 10.5 + 84.848 + 16.485 = 111.833 \text{ mm}$$

$$N_{sd} = 1650 \text{ KN} \quad M_{sd} = N_{sd} * e_{tot} = 184.525 \text{ KNm}$$

$$\text{Using } v_{sd} = 0.72794 \quad \text{and } \mu_{sd} = 0.2035 \quad \omega = 0.35$$

$$n_u = 1 + \omega = 1.35 \quad K_r = \frac{(n_u - n)}{(n_u - n_{bal})} = \frac{(1.35 - 0.72794)}{(1.35 - 0.4)} = 0.6548$$

$$\frac{1}{r} = 0.6548 * 1.2325 * 1.23456 * 10^{-5} = 9.9634 * 10^{-6}$$

$$e_2 = \frac{1}{r} 4200^2 / 10 = 17.575 \text{ mm}$$

For their iteration take $e_2 = 17.575 \text{ mm}$

$$e_{tot} = e_o + e_e + e_2 = 10.5 + 84.848 + 17.575 = 112.923 \text{ mm}$$

$$N_{sd} = 1650 \text{ KN} \quad M_{sd} = N_{sd} * e_{tot} = 186.323 \text{ KNm}$$

$$\text{Using } v_{sd} = 0.72794 \text{ and } \mu_{sd} = 0.2055 \quad \omega = 0.35$$

The iteration **converges** with similar mechanical steel ratio $\omega = 0.35$.

$$A_{s,tot} = \frac{\omega f_{cd} b d}{f_{yd}} = \frac{0.35 * 14.166 * 400 * 400}{400} = 1983.33 \text{ mm}^2$$

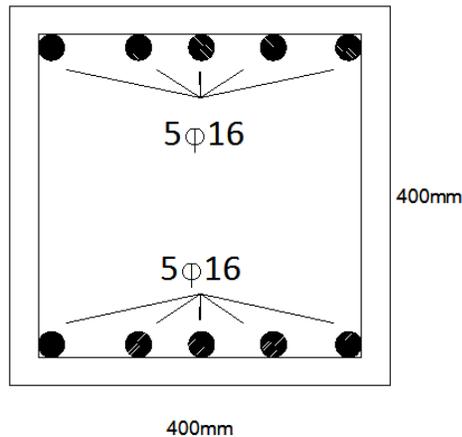
$$A = \frac{A_{s,tot}}{2} = \frac{1983.33}{2} = 991.666 \text{ mm}^2$$

Check with maximum and minimum reinforcement limit

$$A_{s,min} = \max \left\{ \begin{array}{l} \frac{0.1 N_{ED}}{f_{yd}} = 412.5 \text{ mm}^2 \\ 0.002 A_c \end{array} \right. \quad \text{OK!}$$

$$A_{s,max} = 0.08 A_c = 0.08 * 400 * 400 = 12800 \text{ mm}^2 \quad \text{OK!}$$

Using $\phi 16$ provide **5 $\phi 16$** on each face



b) Using Nominal stiffness method

$$EI = K_c E_{cd} I_c + K_s E_s I_s$$

$$E_{cd} = \frac{E_{cm}}{\gamma_{ce}} = \frac{30}{1.2} = 25 \text{ Gpa}$$

Initially let us assume $\rho \geq 0.01$ to use the simplified method

$$K_s = 0 \quad K_c = 0.3/1 + 0.5\phi_{eff}$$

$$\phi_{eff} = 1 \quad K_c = 0.2$$

$$I_c = \frac{bh^3}{12} = 2133333333 \text{ mm}^4$$

$$EI = K_c E_{cd} I_c + K_s E_s I_s = 0.2 * 25 * 10^3 * 2133333333 = 1.06667 * 10^{13}$$

$$N_b = \frac{\Pi^2 EI}{l_o^2} = \frac{\Pi^2 * 1.06667 * 10^{13}}{4200^2} = 5968.01475 \text{ KN}$$

N_b = Buckling load based on nominal stiffness

$$\text{Design moment } M_{ed} = M_{oed} \left[1 + \frac{\beta}{(N_b/N_{ed}) - 1} \right]$$

$$\beta = \Pi^2 / c_o$$

$$c_o = 8$$

$$M_{oed} = 140 \text{ KNm}$$

$$M_{ed} = M_{oed} \left[1 + \frac{\beta}{(N_b/N_{ed}) - 1} \right] = 140 * \left[1 + \frac{1.2337}{(5968.01475/1650) - 1} \right]$$

$$= 205.999 \text{ KNm}$$

For first iteration neglecting accidental eccentricity

$$v_{sd} = \frac{N_{sd}}{f_{cd}bh} = \frac{1650 * 10^3}{14.1667 * 400 * 400} = 0.72794$$

$$\mu_{sd} = \frac{m_{sd}}{f_{cd}bd^2} = \frac{205.999 * 10^6}{14.1667 * 400 * 400^2} = 0.2272$$

$$\text{Using } v_{sd} = 0.72794 \quad \mu_{sd} = 0.2272 \quad \frac{d'}{d} = 0.1 \quad \omega = 0.4$$

$$A_{s,tot} = \frac{\omega f_{cd}bd}{f_{yd}} = \frac{0.4 * 14.166 * 400 * 400}{400} = 2266.666 \text{ mm}^2$$

$$A = \frac{A_{s,tot}}{2} = \frac{2266.666}{2} = 1133.333 \text{ mm}^2$$

$$\rho = \frac{A_s}{bd} = \frac{1133.333}{400 * 360} = 7.870 * 10^{-3} \quad \rho < 0.01$$

We cannot use the simplified method

$$\text{for } \rho > 0.002 \quad K_s = 1$$

$$K_c = \frac{K_1 K_2}{(1 + \phi_{eff})}$$

$$K_1 = \sqrt{\frac{f_{ck}}{20}} = 1.11803$$

$$K_2 = n \frac{\lambda}{170} \leq 0.2$$

$$n = \frac{N_{ed}}{A_c f_{cd}} = 0.72794$$

$$K_2 = 0.2 \quad \text{So} \quad K_c = 0.111803$$

$$I_c = \frac{bh^3}{12} = 2133333333 \text{ mm}^4$$

$$I_s = 2 * [1133.333(360 - 200)^2] = 58026666.67 \text{ mm}^2$$

$$\begin{aligned} EI &= K_c E_{cd} I_c + K_s E_s I_s \\ &= 0.111803 * 25 * 10^3 * 2133333333 + 1 * 200 * 10^3 \\ &\quad * 58026666.6 \end{aligned}$$

$$EI = 1.756816 * 10^{13}$$

$$N_b = \frac{\Pi^2 EI}{l_o^2} = \frac{\Pi^2 * 1.756816 * 10^{13}}{4200^2} = 9829.40982 \text{ KN}$$

$$\begin{aligned} M_{ed} &= M_{oed} \left[1 + \frac{\beta}{\left(\frac{N_b}{N_{ed}} \right) - 1} \right] = 140 * \left[1 + \frac{1.2337}{\left(\frac{9829.40982}{1650} \right) - 1} \right] \\ &= 174.842 \text{ KNm} \end{aligned}$$

Design moment including accidental eccentricity is given by

$$M = 174.842 + 1650 * \left(\frac{10.5}{1000} \right) = 192.167 \text{ KNM}$$

$$v_{sd} = \frac{N_{sd}}{f_{cd} b h} = \frac{1650 * 10^3}{14.1667 * 400 * 400} = 0.72794$$

$$\mu_{sd} = \frac{m_{sd}}{f_{cd} b d^2} = \frac{192.167 * 10^6}{14.1667 * 400 * 400^2} = 0.212$$

$$\text{Using } v_{sd} = 0.72794 \quad \mu_{sd} = 0.212 \quad \frac{d'}{d} = 0.1 \quad \omega = 0.35$$

$$A_{s,tot} = \frac{\omega f_{cd} b d}{f_{yd}} = \frac{0.35 * 14.166 * 400 * 400}{400} = 1983.333 \text{ mm}^2$$

$$A = \frac{A_{s,tot}}{2} = \frac{1983.33}{2} = 991.666 \text{ mm}^2$$

$$\rho = \frac{A_s}{bd} = \frac{991.666}{400 * 360} = 6.886 * 10^{-3} \quad \rho > 0.002$$

Second Iteration

$$I_c = \frac{bh^3}{12} = 2133333333 \text{ mm}^4$$

$$I_s = 2 * [991.666(360 - 200)^2] = 50773333.33 \text{ mm}^2$$

$$EI = K_c E_{cd} I_c + K_s E_s I_s$$

$$= 0.111803 * 25 * 10^3 * 2133333333 + 1 * 200 * 10^3 * 50773333.3$$

$$EI = 1.611749 * 10^{13}$$

$$N_b = \frac{\Pi^2 EI}{l_o^2} = \frac{\Pi^2 * 1.611749 * 10^{13}}{4200^2} = 9017.7598 \text{ KN}$$

$$M_{ed} = M_{oed} \left[1 + \frac{\beta}{\left(\frac{N_b}{N_{ed}} \right) - 1} \right] = 140 * \left[1 + \frac{1.2337}{\left(\frac{9017.7598}{1650} \right) - 1} \right]$$

$$= \mathbf{178.679 \text{ KNm}}$$

Design moment including accidental eccentricity is given by

$$M = 178.679 + 1650 * \left(\frac{10.5}{1000} \right) = 196.004 \text{ KNM}$$

$$v_{sd} = \frac{N_{sd}}{f_{cd} b h} = \frac{1650 * 10^3}{14.1667 * 400 * 400} = 0.72794$$

$$\mu_{sd} = \frac{m_{sd}}{f_{cd} b d^2} = \frac{196.004 * 10^6}{14.1667 * 400 * 400^2} = 0.216$$

$$\text{Using } v_{sd} = 0.72794 \quad \mu_{sd} = 0.216 \quad \frac{d'}{d} = 0.1 \quad \omega = 0.35$$

The iteration converges with similar mechanical steel ratio $\omega = 0.35$.

$$A_{s,tot} = \frac{\omega f_{cd} b d}{f_{yd}} = \frac{0.35 * 14.166 * 400 * 400}{400} = 1983.33 \text{ mm}^2$$

$$A = \frac{A_{s,tot}}{2} = \frac{1983.33}{2} = 991.666 \text{ mm}^2$$

Check with maximum and minimum reinforcement limit

$$A_{s,min} = \max \left\{ \begin{array}{l} \frac{0.1 N_{ED}}{f_{yd}} = 412.5 \text{ mm}^2 \\ 0.002 A_c \end{array} \right. = \mathbf{OK!}$$

$$A_{s,max} = 0.08 A_c = 0.08 * 400 * 400 = 12800 \text{ mm}^2 \quad \mathbf{OK!}$$

Using $\phi 16$ provide $5\phi 16$ on each face

Step 7- Detailing

