

Example 2.3 [shear design, Ribbed slab]

Design the ribbed slab system in example 2 for shear using the same material properties and loading.

Solution

A. Rib shear design

Step 1. Material property

Concrete	$f_{cu}=25\text{Mpa}$	$f_{ck}=20\text{Mpa}$
	$f_{cd}=11.33\text{Mpa}$	$f_{ctk}=1.5\text{ Mpa}$
	$f_{ctm}=2.2\text{ Mpa}$	$f_{ctd}=1.0\text{ Mpa}$
Steel	$f_{yk}=300\text{ Mpa}$	$f_{yd}=260.87\text{Mpa}$
	$\epsilon_{yd}=1.3\text{‰}$	$E_s= 200\text{ Gpa}$

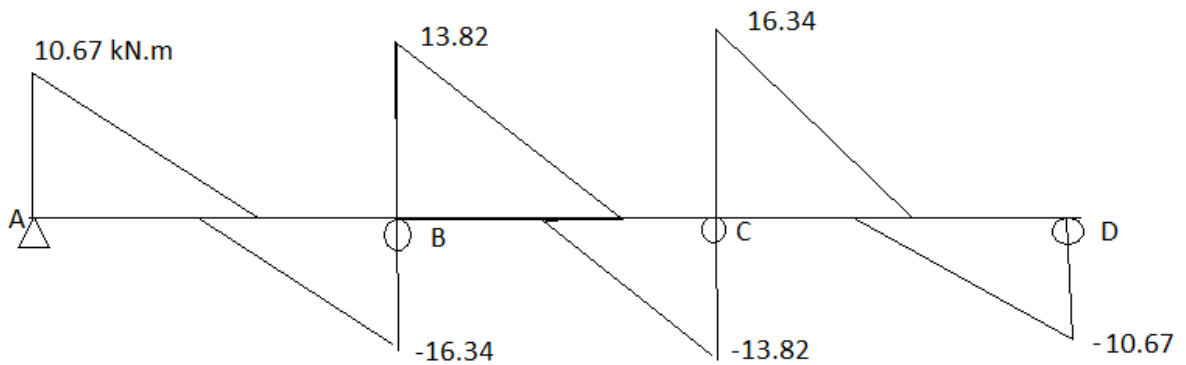
Step 2. Loading on Ribs

$G_d= 4.17\text{ KN/m}$

$Q_d = 2.4\text{ KN/m}$

Step 3. Analysis

- Shear envelope diagram



Step 4. Concrete shear capacity

$$V_{Rd,c} = \left[C_{Rd,c} \cdot K \cdot (100\rho_1 \cdot f_{ck})^{\frac{1}{3}} + K_1 \sigma_{cp} \right] b_w \cdot d > (V_{min} + K_1 \cdot \sigma_{cp}) b_w \cdot d$$

Where:

- $C_{Rd,c} = \frac{0.18}{\gamma_c} = \frac{0.18}{1.5} = 0.12$
- $K = 1 + \sqrt{\frac{200}{d}} \leq 2.0 \quad d = 233$
 $K=1.92$
- $\rho_1 = \frac{A_s}{b_w \cdot d} < 0.02$

$$\rho_1 = \begin{cases} \frac{226.19}{80 \times 233} = 0.0121, & \text{for sections with } 2\phi 12 \\ \frac{157.07}{80 \times 235} = 0.0085, & \text{for sections with } 2\phi 10 \end{cases}$$
- $f_{ck} = 20 \text{ Mpa}$
- $K1 = 0.15$
- $\sigma_{cp} = \frac{N_{ED}}{A_c} < 0.2 f_{cd} = 0 \dots \dots \dots (N_{ED} = 0)$
- $V_{min} = 0.035 \cdot K^{\frac{3}{2}} \cdot f_{ck}^{\frac{1}{2}} = 0.416$

Therefore

$$\text{For sections with } 2\phi 12 \Rightarrow V_{Rd,c} = 12.43 \text{ KN} > 7.75 \text{ KN}$$

$$\text{For sections with } 2\phi 10 \Rightarrow V_{Rd,c} = 10.137 \text{ KN} > 7.75 \text{ KN}$$

Step 5: Diagonal compression check of concrete

$$V_{Rd,max} = \frac{\alpha_{cw} \cdot b_w \cdot Z \cdot v \cdot f_{cd}}{(\cot \theta + \tan \theta)}$$

$$V_{Rd,s} = \frac{A_{sw}}{S} \cdot Z \cdot f_{ywd} \cdot \cot \theta$$

$$V_{Rd}(\text{minimum of}) = \begin{cases} V_{Rd,max} \\ V_{Rd,s} \end{cases}$$

where

$$\alpha_{cw} = 1 \quad \text{recommended value for non – prestressed member}$$

$$\text{limit } \theta \Rightarrow 1 \leq \cot \theta \leq 2.5$$

$$\text{Take } \dots \cot \theta = 2.5$$

$$b_w = 80 \text{ mm}$$

$$f_{cd} = 11.33 \text{ Mpa}$$

$$Z = 0.9x d = 209.7$$

$$\Rightarrow V_{Rd,max} = \frac{1x80x209.7x0.6x11.33}{\left(2.5 + \frac{1}{2.5}\right)} = 39.325 \text{ KN}$$

Check this value with values form the shear envelop

$$\Rightarrow V_{Rd,max} > V_{ED} \dots \dots \text{at all locations, } \mathbf{therefore Ok!}$$

Step 6. Calculate the required shear reinforcement

$$\frac{A_{sw} \cdot f_{yd}}{b_w \cdot S} \leq \frac{1}{2} \cdot \alpha_c \cdot v \cdot f_{cd}$$

$$S_{max} = 0.75 \cdot d \cdot (1 + \cot \alpha), \quad \alpha = 90^\circ$$

$$S_{max} = 0.75d$$

$$\rho_{min} = \frac{0.08 \cdot \sqrt{f_{ck}}}{f_{yk}} = 0.00119$$

$$S = \frac{A_{sw}}{b_w \cdot \rho_w \cdot \sin \alpha} = \frac{2x(\emptyset 6^2 \frac{\pi}{4})}{80x0.00119x1} = 593.99 \text{ mm}$$

Check this value with S_{max}

Required: shear reinforcement

$$\frac{A_{sw}}{S} = \frac{V_{ed}}{0.78 * d * f_{yk} * \cot \theta}$$

$$A_{sw} = \frac{2 * \pi * 6^2}{4} = 56.54 \text{ mm}^2$$

$$S = \frac{A_{sw} * 0.78 * d * f_{yk} * \cot \theta}{V_{ed}}$$

V_{Ed} — d from the face of the columns but since the loads are small just take the values at the centre of the columns.

θ - since $V_{Rd,max} > V_{Ed}$ lets take the conservative value

$$\theta = 22^\circ \quad \cot \theta = 2.5$$

$$S = \frac{56.54 * 0.78 * 233 * 300 * 2.5}{V_{ed}} = \frac{7706.68}{V_{ed}} \text{ KNmm}$$

span	Location	VEd(KN)	Scal (mm)	Sprovid
AB	near A	10.67	722	φ 6 C/C 175 mm
	near B	-16.34	471	φ 6 C/C 175 mm
BC	near B	13.825	557.44	φ 6 C/C 175 mm
	near C	13.825	557.44	φ 6 C/C 175 mm
CD	near C	16.34	471.64	φ 6 C/C 175 mm
	near D	10.67	722.27	φ 6 C/C 175 mm

$$S_{\min} = 594 \text{ mm}$$

$$S_{\max} = 0.75 * d = 0.75 * 233 = 174.75 \rightarrow 175\text{mm}$$

Provide φ 6 C/C 175 mm throughout

➔ Additional torsion force on the longitudinal reinforcement.

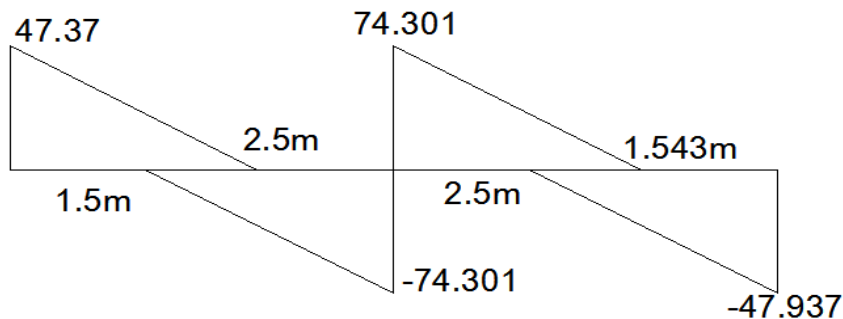
$$\Delta F_{td} = 0.5 * V_{Ed} * \cot\theta \quad \text{take } V_{Ed} = 16.34 \text{ (the largest value)}$$

$$\Delta F_{td} = 0.5 * 16.34 * \cot(45) = \mathbf{20.425KN}$$

Note: this has to be added to the Flexural computation (on the tension reinforcements.)

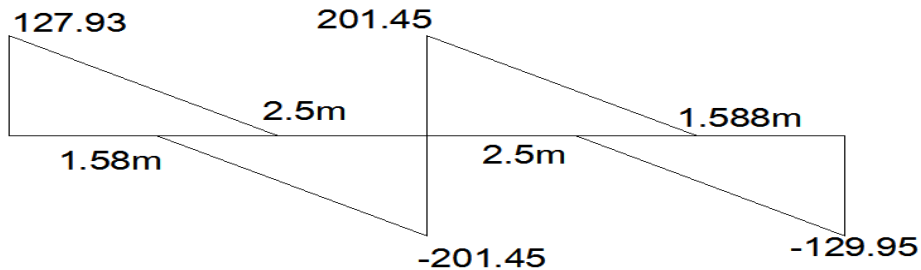
Step 1: Shear envelope

- A and D
 - $b_w = 300$, $D = 300\text{mm}$, $d = 259$
 - φ8 stirrup, φ 16 rebar



- B and C
 - $b_w = 600$, $D = 300\text{mm}$, $d = 257$

- $\phi 8$ stirrup, $\phi 20$ rebar



Step 2: concrete shear capacity

$$VR_{d,c} = [CR_{d,c} * k * (\log f_{ck})^{\frac{1}{3}} + K1 * \rho_{scp}] * b_{co} * d$$

$$> [V_{min} + K1 * \sigma_{cp}] * b_{co} * d$$

$$CR_{d,c} = 0.12$$

$$K = 1 + \sqrt{\frac{200}{d}} = 1 + \sqrt{\frac{200}{233}} \leq 2.0$$

$$K = 1.926$$

$$\rho = \frac{A_s}{b_w * d} < 0.02$$

For A and D:

Support: $6\phi 16$

$$\rho = \frac{1206.37}{300 * 259} = 0.0155$$

Span: $4\phi 16$, $\rho = 0.01035$

For B and C:

Support: $10\phi 20$, $\rho = 0.02$

Span: $4\phi 16$, $\rho = 0.0122$

$$f_{ck} = 20 \text{ Mpa}$$

$$\sigma_{cp} = 0$$

$$V_{min} = 0.035 * k^{\frac{3}{2}} * f_{ck}^{\frac{1}{2}} = 0.416$$

➤ **A and D**

- Span - $V_{RD,c} = 56.412 \text{ KN} > 32.3 \text{ KN}$
- Support - $V_{RD,c} = 49.22 \text{ KN} > 32.2 \text{ KN}$

➤ **B and C**

- Span - $V_{RD,c} = 121.88 \text{ KN} > 32.3 \text{ KN}$
- Support - $V_{RD,c} = 103.36 \text{ KN} > 32.3 \text{ KN}$

Step 3: Diagonal compression check of concrete

$$V_{Rd,max} = \frac{\alpha_{cw} * b_w * f * v * fcd}{\cot \theta + \tan \theta}$$

➤ **Girder A and D**

- $\alpha_{cw} = 1$
- $V = 0.6$
- $b_w = 300\text{mm}$
- $fcd = 11.33\text{Mpa}$
- $\cot \theta = 2.5$
- $z = 0.9 * d = 0.9 * 239 = 233.1$

$$V_{Rd,max} = \frac{1 * 0.6 * 300 * 233.1 * 11.33}{2.5 * \frac{1}{2.5}}$$

$$V_{Rd,max} = 163.92\text{KN}$$

- $V_{Rd,max} > V_{Rd} \dots \dots \dots \text{OK}$

➤ **Girder A and D**

- $\alpha_{cw} = 1$
- $V = 0.6$
- $b_w = 600\text{mm}$
- $fcd = 11.33\text{Mpa}$
- $\cot \theta = 2.5$
- $z = 0.9 * d = 0.9 * 257 = 231.3$

$$V_{Rd,max} = \frac{1 * 0.6 * 600 * 231.3 * 11.33}{2.5 * \frac{1}{2.5}}$$

$$V_{Rd,max} = 325.32\text{KN}$$

- $V_{Rd,max} > V_{Rd} \dots \dots \dots \text{OK}$

Step 4: Shear reinforcement required

$$\frac{A_{sw,max} * f_{yd}}{b_w * s} < \frac{1}{2} * \alpha_c * V_{yc}$$

$$\frac{A_{sw}}{s} = \frac{V_{Ed}}{0.78 * 5 * f_{yd} * \cot \theta}$$

$$A_{sw} = 2 * \frac{\pi * 8^2}{4} = 100.53$$

$$S = \frac{0.78 * d * f_{yk} * A_{sw} * \cot \theta}{V_{ed}}$$

$$S_{max} = 0.75 * d * (1 + \cot \theta)$$

$$S_{max} = 194.25 \text{ mm for A and D}$$

$$S_{max} = 192.74 \text{ mm for B and C}$$

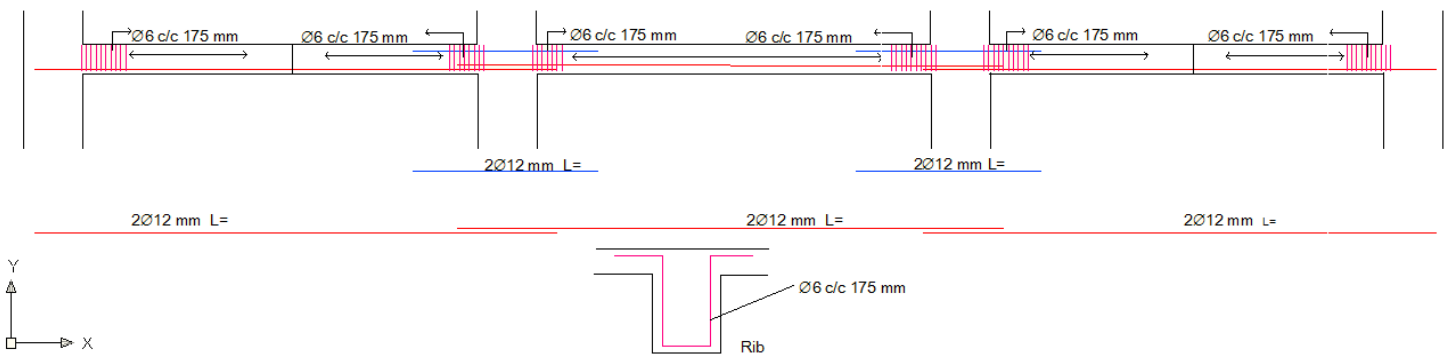
$$S_{min} = \frac{A_{sw}}{b_w * \rho_w * \sin x} = 281.59 \text{ for A and D}$$

$$S_{min} = 140.79 \text{ mm for B and C}$$

Span	location	V _{Ed} (KN)	d	S _{cal} (mm)	S provided			
A and D	near 1	39.67	259	767.92	ϕ 8 C/C 560 mm			
	near 2	66.6	259	456.92	ϕ 8 C/C 450 mm			
	near 2	66.6	259	456.92	ϕ 8 C/C 450 mm			
	near 3	39.67	259	767.92	ϕ 8 C/C 560 mm			
B and C	near 1	107.24	257	281.86	ϕ 8 C/C 280 mm			
	near 2	180.74	257	167.24	ϕ 8 C/C 190 mm			
	near 2	180.74	257 </tr <tr> <td>near 3</td> <td>107.24</td> <td>257</td> <td>281.86</td> <td>ϕ 8 C/C 280 mm</td> </tr>	near 3	107.24	257	281.86	ϕ 8 C/C 280 mm
	near 3	107.24	257	281.86	ϕ 8 C/C 280 mm			

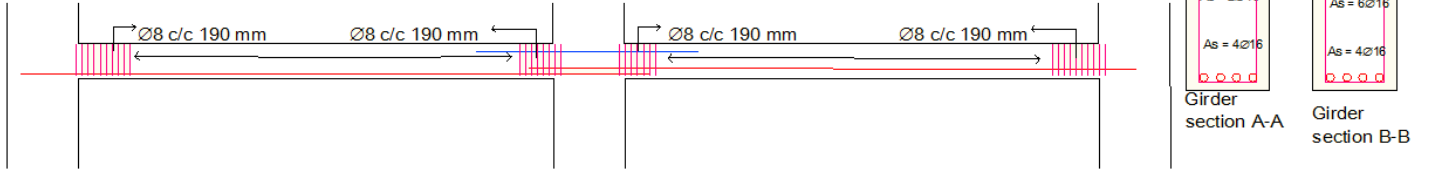
Step 7. Detailing

Shear Reinforcement detailing for Ribs

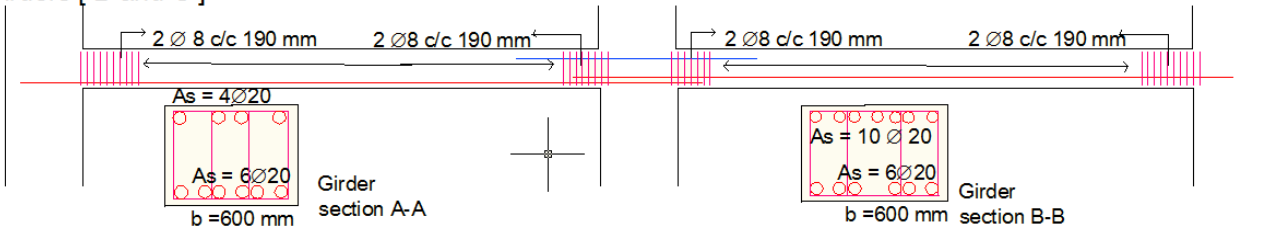


Shear Reinforcement detailing for girders

Girders [A and D]



Girders [B and C]



Shear Reinforcement detailing for Beams

