M.Y.H. Bangash

Structures for Nuclear Facilities Analysis, Design, and Construction



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Two well-known scientists, Dr. A.Q. KHAN and Professor Abdus Salam, have been chosen and this book is dedicated to them for their services to science and technology.

DR. A.Q. KHAN, a towering individual, has many achievements in the field of science and technology. The direction of his research reflects his deep passion for advanced materials. He deserves this dedication because of his deliverance of advanced nuclear technology to his country, Pakistan, and the establishment of advanced laboratories including the famous Kahuta Research Laboratories for existing and future practical implementations. His research is recommandable.

PROFESSOR ABDUS SALAM attained the pinnacle of his physics career when he shared a Nobel Prize with two other scientists on "Unification of Electromagnetism and the Weak Nuclear Force". The most revealing of it was the existence of a new particle at extreme energies – the conditions that would be similar to the few moments in the birth of the universe. These fleeting moments were confirmed under cosmic conditions at the CERN Accelerator. He had extended his hands to developing countries. He deserves this dedication.

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Chapter 1 Nuclear Power Plant Facilities and Regulatory Guides

1.1 General Introduction

A number of nuclear power stations exist worldwide. This chapter concentrates on British, American, Canadian and European research and commercial reactors and nuclear power stations. The directory exists on the past, present and future planning for the NPS and are continuously being updated. In this chapter carefully selected nuclear stations with various design parameters have been clearly dealt with. British research and commercial nuclear power stations are first named. Various design and other parameters are given with reasonable artwork explaining the concepts behind the research and commercial reactor stations. Listings are provided for BWR, AGR, BHWR, PWR and FBR types and others in major countries of the world. Those countries that have designed and supplied the respective systems are named together with the suppliers. This chapter ends with relevant references for those who can carry out an in-depth study for initiating and planning of next generation of nuclear power stations. Owing to restrictions, some have been listed without explanatory notes and designs.

1.2 British Commercial Nuclear Power Station – Commissioned and Non-commissioned

1.2.1 General

The following well-known stations have been constructed and commissioned:

- Berkeley (275 MW) decommissioned
- Bradwell (300 MW) decommissioned
- Latina (200 MW)
- Dungeness A (550 MW)
- Dungeness B (500 MW)
- Oldbury (600 MW) decommissioned
- Hinkley A (500 MW)

- Hinkley B (550 MW)
- Hartlepool (550 MW)
- Wylfa (550 MW)
- Sizewell B PWR (1300 MW)

Ther are many others which are mentioned later on in the text.

1.2.1.1 Berkeley NPS

They have two units:

Unit 1 reactor on power: 12 June 1962 Unit 2 reactor on power: 2 November 1962

These are gas-cooled reactors, graphite moderated using natural uranium as fuel and are equipped with one-load charge/discharge machinery. Each reactor is associated with light heat exchangers which supply steam to 4No. 83 MW dual-purpose turbo alternators. Plate 1.1 shows the pictoral view of the Berkeley N.P.S. and Plate 1.2 gives an outline of the sectional elevation of this situation. The station was designed by TNPG – a consortium of engineering firms for the then Central Electricity Generating Board (CEGB).



Plate 1.1 A pictoral view of Berkeley nuclear power station



Plate 1.2 A sectional elevation of Berkeley nuclear power station

The station parameters:

| Station net electric output | 275 MW |
|----------------------------------|---|
| Heat per reactor | 560 MW |
| Moderator | Graphite |
| Diameter of active core | 13.1 m |
| Height of active core | 7.45 m |
| Fuel | Natural uranium solid rod in Magnox can |
| Rod diameter | 27.9 mm |
| Rod length | 0.48 m |
| No. of fuel channels | 3265 |
| No. of fuel elements per channel | 13 |
| Weight of fuel per reactor | 230.8 t |
| Reactor vessel | Steel cylinder |
| Internal diameter | 15.2 m |
| No. of standpipes Control | 133 |
| Charge | 60 |
| Blowers | 8 per reactor |
| Coolant | Carbon dioxide |
| Reactor gas inlet temperature | 160°C |
| Reactor gas outlet temperature | 345°C |
| Power per blower | 2.34 MW |
| Boilers | 8 per reactor |
| Overall height | 21.3 m |
| Diameter | 5.3 m |
| | |

| | (continued) | | | |
|---------|----------------------------|------------------------------------|--|--|
| Fuel ha | andling | On load | | |
| Turbo | alternators | 4 | | |
| Speed | 1 | 3000 rpm | | |
| Ratin | g | 80 MW | | |
| Steam | conditions (at stop valve) | | | |
| HP | Flow | 70.5 kg/s | | |
| | Pressure | $21.8 \text{ kg/cm}^2 \text{ abs}$ | | |
| | Temperature | 316°C | | |
| LP | Flow | 32.6 kg/s | | |
| | Pressure | $5.1 \text{ kg/cm}^2 \text{ abs}$ | | |
| | Temperature | 316°C | | |

Station status: Completed life service and decommissioned

1.2.1.2 Bradwell

Bradwell has two gas-cooled graphite-moderated reactors fuelled with natural uranium. There have been two units commercially operated:

Reactor 1 on power: 1 July 1962 Reactor 2 on power: 12 November 1962

Each reactor has six heat chambers supplying steam at two pressures to six 52.4 MW turbo alternators. For on-load refuelling universal charge and discharge machines are used. Plates 1.3 and 1.4 show the pictoral view and outline sectional elevation of the station, respectively.



Plate 1.3 A pictoral view of Bradwell nuclear power station (with compliments of CEGB)



Plate 1.4 A sectional elevation of Bradwell nuclear power station (with compliments of CEGB)

| Th | e sta | ition | para | ame | ters: |
|----|-------|-------|------|-----|-------|
|----|-------|-------|------|-----|-------|

| Station net electric output | 300 MW |
|----------------------------------|---|
| Heat per reactor | 531 MW |
| Moderator | Graphite |
| Diameter of active core | 12.2 m |
| Height of active core | 7.90 m |
| Fuel | Natural uranium solid rod in magnox can |
| Rod diameter | 29.3 mm |
| Rod length | 0.91 m |
| No. of fuel channels | 2564 |
| No. of fuel elements per channel | 8 |
| Weight of fuel per reactor | 239 t |
| Reactor vessel | Steel sphere |
| Internal diameter | 20.3 m |
| No. of standpipes Control | 168 |
| Charge | 88 |
| Blowers | 6 per reactor |
| Coolant | Carbon dioxide |
| Reactor gas inlet temperature | 180°C |
| Reactor gas outlet temperature | 390°C |
| Power per blower | 2.47 MW |
| Boilers | 6 per reactor |
| Overall height | 28.1 m |
| Diameter Top | 5.8 m |
| Bottom | 6.1 m |

| | (continued) | | | |
|---------|-------------------------------|------------------------------------|--|--|
| Fuel h | andling | On load | | |
| No. | of charge machines | 2 per reactor | | |
| Main | turbo alternators | 6 | | |
| Spee | d | 3000 rpm | | |
| Rati | ng | 52 MW | | |
| Auxili | ary turbo alternators (blower | | | |
| drive)3 | 3 | 3 | | |
| Spee | d | 3000 rpm | | |
| Steam | conditions (at stop valve) | | | |
| HP | Flow | 43.1 kg/s | | |
| | Pressure | $52.4 \text{ kg/cm}^2 \text{ abs}$ | | |
| | Temperature | 371°C | | |
| LP | Flow | 15.9 kg/s | | |
| | Pressure | 13.7 kg/cm ² abs | | |
| | Temperature | 371°C | | |

Station status: Completed life service

1.2.1.3 Latina

The power station is located some 40 miles south of Rome and was designed and constructed by TNPG in collaboration with refinements in the reactor design. It is a single refined gas-cooled graphite-moderated reactor which supplies steam to 3No.70 MW turbo alternator.

Reactor on power: 12 May 1963

Plates 1.5 and 1.6 show the pictoral view and outline sectional elevation of the structure, respectively.

| Station net electric output | 200 MW |
|----------------------------------|---|
| Reactor heat | 705 MW |
| Moderator | Graphite |
| Diameter of active core | 12.7m |
| Height of active core | 7.88m |
| Fuel | Natural uranium solid rod in magnox can |
| Rod diameter | 29.3mm |
| Rod length | 0.91 m |
| No. of fuel channels | 2929 |
| No. of fuel elements per channel | 8 |
| Weight of fuel | 268 t |
| Reactor vessel | Steel sphere |
| Internal diameter | 20.3 m |
| No. of standpipes | 197 |
| Blowers | 6 |

The station parameters:



Plate 1.5 Pictoral view of Latina (with compliments from TNPG a part of Mcalpine consultants)



Plate 1.6 Outline of the sectional elevation of Latina

| (continued) | | |
|--|-----------------------------|------------------------------------|
| Cool | ant | Carbon dioxide |
| Read | ctor gas inlet temperature | 180°C |
| Read | ctor gas outlet temperature | 390°C |
| Powe | er per blower | 3.06 MW |
| Boiler | S | 6 |
| Over | all height | 24.1 m |
| Dian | neter | 5.6m |
| Fuel h | andling | On load |
| No. | of charge machines | 2 |
| Main turbo alternators | | 3 |
| Speed | | 3000 rpm |
| Rating | | 70 MW |
| Auxiliary turbo alternators (blower drive) | | 2 |
| Speed | | 2263 rpm |
| Steam | conditions (at stop valve) | |
| HP | Flow | 57.6 kg/s |
| | Pressure | $52.4 \text{ kg/cm}^2 \text{ abs}$ |
| | Temperature | 371°C |
| LP | Flow | 21.1 kg/s |
| | Pressure | $13.7 \text{ kg/cm}^2 \text{ abs}$ |
| | Temperature | 371°C |

Station status: Completed life service

1.2.1.4 Dungeness A

The TNPG, a consortium, installed two gas-cooled graphite-moderated type, using natural uranium as fuel with on-load refuelling. The number of gas circuits has been reduced to four back pressure steam turbines providing gas circulator drive. The turbine house contains 4No. 142.5 MW turbo alternators.

No. 1 reactor in power: 21 September 1965 No. 2 reactor in power: 18 November 1965

Plates 1.7 and 1.8 show the pictoral view and the outline elevation of the station, respectively.

The station parameters:

| Station net electric output | 550 MW |
|-----------------------------|---|
| Heat per reactor | 840 MW |
| Moderator | Graphite |
| Diameter of active core | 13.9 m |
| Height of active core | 7.47 m |
| Fuel | Natural uranium solid rod in magnox can |
| Rod diameter | 27.9 mm |



Plate 1.7 A pictoral view of the Dungeness A nuclear power station (with compliments of CEGB)



Plate 1.8 Outline of the sectional elevation of the Dungeness A nuclear power station (with compliments of CEGB)

| (001 | (indea) |
|----------------------------------|------------------------------------|
| Rod length | 0.972 m |
| No. of fuel channels | 3876 |
| No. of fuel elements per channel | 7 |
| Weight of fuel per reactor | 300 t |
| Reactor vessel | Steel sphere |
| Internal diameter | 19.1 m |
| Blowers | 4 per reactor |
| Coolant | Carbon dioxide |
| Reactor gas inlet temperature | 250°C |
| Reactor gas outlet temperature | $410^{\circ}\mathrm{C}$ |
| Power per blower | 7.16 MW |
| Boilers | 4 per reactor |
| Overall height | 22.9 m |
| Diameter | 7.2 m |
| Fuel handling | On load |
| No. of charge machines | 2 per reactor |
| Turbo alternators | 4 |
| Speed | 1500 rpm |
| Rating | 142.5 MW |
| Steam conditions | |
| Pressure | $41.5 \text{ kg/cm}^2 \text{ abs}$ |
| Temperature | 393°C |

(continued)

Station status: Under service operation

Commissioning date: Reactor number 1: July 1965 Reactor number 2: 2 September 1965

The station is situated on the coast on the western side of Dungeness in Kent. There are two reactors, housed in spherical-type pressure vessels of 62.5 ft mean diameter, constructed of steel plates having a general thickness of 4 in. Each reactor has four boilers. Generating plant comprises four 1,500 rpm turbo alternators each with rated output of 142.5 MW at 0.8 power factor (lagging). The total guaranteed net output of the station in megawatts is planned as 550 MW which was expected to be achieved by the end of 1965.

| Location: | Dungeness Point Kent |
|-----------------------|--|
| Reactor type: | Magnox |
| Reactor power: | 840 MW (Th.), 275 MW (E) net from each of two reactors |
| Designer: | The Nuclear Power Group |
| Builder: | The Nuclear Power Group |
| Fuel element: | Natural uranium bars in Magnox cans |
| Data for each | |
| reactor | |
| Number of elements: | 27,515 in 3932 channels. |
| | Total 300 t natural uranium |
| Moderator: | 1500 t graphite |

| (continued) | |
|-----------------|--|
| Coolant: | Carbon dioxide, outlet temperature 410°C |
| Core size: | 24 –sided prism: 13.83 m diameter, 7.39 m high |
| Specific power: | 2.78 kW/kg uranium |
| Control: | 91 bulk rods; 9 sector rods; 8 trim rods of boron steel in stainless |
| | steel sheath |
| Shielding: | Biological: 167.6–289.6 cm concrete |
| | |

(continued)

(With compliments from TNPG)

1.2.1.5 Dungeness B Advanced Gas-Cooled Reactor Station

The pressure vessel built in concrete, i.e. the PCPV, has been thoroughly investigated in this test.

1.2.1.6 Oldbury

An advancement is made on the gas-cooled reactor design. Each of the two reactor does have its core, boilers and gas circulators enclosed in a prestressed concrete pressure vessel. Natural uranium used as a fuel. In a turbine house unit generating sets are used, each one rated at 313 MW. It is four miles from Berkeley.

Both reactors on power in 1966/1967

Plates 1.9 and 1.10 show pictoral view and an outline elevation of the station, respectively.



Plate 1.9 A pictoral view of the Oldbury nuclear power station (with compliments of Mr. Ghalib of TNPG)



Plate 1.10 An outline sectional elevation of the Oldbury nuclear power station (with compliments of Mr. Ghalib of TNPG)

| Station net electric output | 600 MW |
|----------------------------------|---|
| Heat per reactor | 892 MW |
| Moderator | Graphite |
| Diameter of active core | 12.8 m |
| Height of active core | 8.53 m |
| Fuel | Natural uranium solid rod in Magnox can |
| Rod diameter | 27.9 mm |
| Rod length | 0.972 m |
| No. of fuel channels | 3308 |
| No. of fuel elements per channel | 8 |
| Weight of fuel | 292 t |
| Reactor vessel | Prestressed concrete cylinder |
| Internal diameter | 23.5 m |
| Internal height | 18.3 m |
| Blowers | 4 per reactor |
| Coolant | Carbon dioxide |
| Blower drive | Back pressure steam turbine |
| Reactor gas inlet temperature | 250°C |
| Reactor gas outlet temperature | 411°C |
| Power per blower | 4.9 MW |

Station parameters:

| Boilers4 annular per reactorHeight over banks11 mWidth of annulus $3.1 m$ Fuel handlingOn loadNo. of charge machinesOne per reactorTurbo alternators 2 Speed1500 rpmRating $313 MW$ Steam conditions $190 kg/s$ Pressure $98.3 kg/cm^2 abs$ Temperature $393^{\circ}C$ LPFlow $149 kg/s$ Pressure $49.5 kg/cm^2 abs$ Temperature $393^{\circ}C$ | (continued) | |
|--|------------------------|------------------------------------|
| Height over banks11 mWidth of annulus 3.1 m Fuel handlingOn loadNo. of charge machinesOne per reactorTurbo alternators 2 Speed1500 rpmRating 313 MW Steam conditions 190 kg/s Pressure $98.3 \text{ kg/cm}^2 \text{ abs}$ Temperature 393°C LPFlow 149 kg/s Pressure $49.5 \text{ kg/cm}^2 \text{ abs}$ Temperature 393°C | Boilers | 4 annular per reactor |
| Width of annulus 3.1 m Fuel handlingOn loadNo. of charge machinesOne per reactorTurbo alternators 2 Speed1500 rpmRating 313 MW Steam conditions 190 kg/s HPFlow 190 kg/s Pressure $98.3 \text{ kg/cm}^2 \text{ abs}$ Temperature 393°C LPFlow 149 kg/s Pressure $49.5 \text{ kg/cm}^2 \text{ abs}$ Temperature 393°C | Height over banks | 11 m |
| Fuel handlingOn loadNo. of charge machinesOne per reactorTurbo alternators2Speed1500 rpmRating313 MWSteam conditions98.3 kg/cm² absHPFlow190 kg/sPressure98.3 kg/cm² absTemperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | Width of annulus | 3.1 m |
| No. of charge machinesOne per reactorTurbo alternators2Speed1500 rpmRating313 MWSteam conditions98.3 kg/cm² absHPFlow190 kg/sPressure98.3 kg/cm² absTemperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | Fuel handling | On load |
| Turbo alternators2Speed1500 rpmRating313 MWSteam conditions190 kg/sHPFlow190 kg/sPressure98.3 kg/cm² absTemperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | No. of charge machines | One per reactor |
| Speed1500 rpmRating313 MWSteam conditions90 kg/sHPFlow190 kg/sPressure98.3 kg/cm² absTemperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | Turbo alternators | 2 |
| Rating313 MWSteam conditions190 kg/sHPFlow190 kg/sPressure98.3 kg/cm² absTemperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | Speed | 1500 rpm |
| Steam conditionsHPFlow190 kg/sPressure98.3 kg/cm² absTemperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | Rating | 313 MW |
| $ \begin{array}{cccc} HP & Flow & 190 \ kg/s \\ Pressure & 98.3 \ kg/cm^2 \ abs \\ Temperature & 393^{\circ}C \\ LP & Flow & 149 \ kg/s \\ Pressure & 49.5 \ kg/cm^2 \ abs \\ Temperature & 393^{\circ}C \end{array} $ | Steam conditions | |
| Pressure98.3 kg/cm² absTemperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | HP Flow | 190 kg/s |
| Temperature393°CLPFlow149 kg/sPressure49.5 kg/cm² absTemperature393°C | Pressure | 98.3 kg/cm ² abs |
| LP Flow 149 kg/s Pressure 49.5 kg/cm ² abs Temperature 393°C | Temperature | 393°C |
| Pressure 49.5 kg/cm ² abs Temperature 393°C | LP Flow | 149 kg/s |
| Temperature 393°C | Pressure | $49.5 \text{ kg/cm}^2 \text{ abs}$ |
| | Temperature | 393°C |

Station status: Originally completed life service

1.2.1.7 Hinkley

The station has a capacity of 1300 MW (c) twin reactor of AGR. It is similar to Oldbury for the internal arrangement of core and boilers. The significant features of the design are

- (a) Gas pressure 42.5 kg/cm^2 (600 psia)
- (b) Fully encapsulated gas coolers, removable under pressure
- (c) Boiler shield walls of calcium hydroxide

The station is located in the north Somerset on the Bristol Channel.

Plates 1.11 and 1.12 show pictoral view and outline sectional elevation of the station, respectively.

Station parameters: Similar to Oldbury N.P.S.

Recent improvements in the design of the core have been given a mean fuel rating 30% higher than the figure published for Dungeness 'B'. The reactors are refuelled on load. No axial or radial shuffling of the fuel is required during its life in the reactor.

The overall performance parameters of the station are as follows:

| Electrical output (net) | 2×630 MW (+ 40 MW from gas turbines) |
|-------------------------|---|
| Reactor heat output | 1500 MW |
| Fuel rating | 5.14 MW (e)/t |
| Thermal efficiency | 42.0% |

Station status: Completed life performance



Plate 1.11 A pictoral view of the Hinkley 'B' nuclear power station (with compliments of Mr. Ghalib of TNPG)



Plate 1.12 A sectional elevation of the Hinkley 'B' Nuclear power station (with compliments of Mr. Ghalib of TNPG)

1.2.1.8 Other British Reactors: Commercial and Research Types

General Information

The reactors mentioned in this section are collected from a number of sources. The information given herein is for research and advanced commercial reactors which are listed as under:

Each of the above station is supported by the respective station parameters. Some of them have completed their expected life with the possibility of demolition or replacement.

Gleep

Graphite Low-Energy Experiment Pile Commissioning date: 15 August 1947

A thermal heterogeneous reactor, using natural uranium as fuel: graphite moderated and reflected, air cooled.

The reactor is formed from a graphite cube of 21 ft (6.4m) side width made of 682 channels. Natural uranium bars and aluminium clad, are placed in these channels to provide the fuel.5 ft (1.52m) thick barytes concrete forms biological shield. The listings of the other NP stations are first listed underneath.

| Location: | A E R E Harwell Berkshire |
|------------------------|---|
| Reactor type: | Thermal, heterogeneous |
| Reactor power: | Variable up to 4.5 kW (Th.) |
| Designer: | Ministry of Supply |
| Builder: | Ministry of Works |
| Fuel element: | Natural uranium bars in plain aluminium cans |
| Number of elements: | 11,594 in 682 channels, total 32.5 t natural uranium |
| Moderator: | 505 t graphite |
| Coolant: | Air at ambient temperature |
| Core size: | Cylindrical 552 cm diameter, 518 cm long |
| Specific power: | 0.14 kW/t uranium |
| Control: | One safety rod and two sets of three shut-off rods; one fine, four coarse control rods of boron carbide in stainless steel annulus |
| Shielding: | Biological: concrete 152 cm thick. No thermal shield |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Bepo

British Experimental Pile OperationCommissioning date: 5 July 1948A thermal heterogeneous reactor with natural or low-enrichment uranium as fuel, graphite moderated and reflected, air cooled.

Magnox Reactors

AGR

HTGFRe

- Gleep
- Bepo
- Lido
- Dido
- Pluto
- DMTR
- Horace
- Herald

Research Reactors

- Zenith
- Vera
- Nestor
- Hero
- Daphne
- Dimple
- Zebra
- Hector
- Jund
- Tokaimura
- Calder Hall
- Chapelcross
- Hunterston
- Hinkley Point A
- Trawsfynydd
- Dungeness A
- Sizewell
- Wylfa
- Hartlepool
- Dungeness B
- SGHWR, Winfirth
- DFR
- Dragon

The reacting core is a cylinder 20 ft diameter by 20 ft long and there are 20 fuel elements in each of 880 channels. Fuel is canned in aluminium, finned to improve heat transfer. Air is drawn at sub-atmospheric pressure through the core and is discharged from a high chimney. Shielding consists of a 6 in. cast iron thermal shield and $6\frac{1}{2}$ ft of barytes concrete.

| Location: | A E R E Harwell Berkshire |
|-----------------------|---|
| Reactor type: | Thermal heterogeneous |
| Reactor power: | 6 MW (Th.) |
| Designer: | Ministry of Supply |
| Builder: | Ministry of Works |
| Fuel element: | Natural or low-enriched uranium in finned aluminium cans |
| Number of | 16,558 in 830 channels total 39 t natural uranium |
| elements: | |
| Moderator: | 863 t graphite |
| Coolant: | Air outlet temperature 120°C |
| Core size: | Cylindrical 610 cm diameter, 610 cm long |
| Specific power: | 0.15 kW/kg uranium |
| Control: | Two vertical shut-off rods: four horizontal control rods (falling under |
| | gravity) of hollow steel lined or filled with boron carbide |
| Shielding | Biological: concrete 198 cm thick. Thermal: cast iron 15.2 cm thick |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Lido

Commissioning date: 20 September 1956

Thermal heterogeneous swimming pool type, enriched uranium fuel, H₂O moderated and cooled.

The concrete tank has 7 ft thick walls and is 28 ft long, \times 8 ft wide and 24 ft deep internally and contains light water. Three large aluminium 'windows' are fitted in the tank and these allow heavy shielding experiments to be set up outside. Three beam holes are also fitted. The reactor core is made up of uranium/aluminium plates clad in aluminium; it can be moved through the water into position on the inner side of any window. The water is circulated for cooling and cleaning.

| Location: | A E R E Harwell Berkshire |
|-----------------------|---|
| Reactor type: | Thermal heterogeneous swimming pool |
| Reactor power: | 100 kW (Th.) |
| Designer: | UKAEA |
| Builder: | Vickers Armstrong |
| Fuel element: | MTR-type curved plates 46% enriched uranium alloyed with aluminium; clad in aluminium |
| Number of elements: | 22 standard elements, 4 control rod elements, a few partial elements, total 3.47 kg U-235 |
| Moderator: | 155,000 l demineralised water |

| | (continued) |
|-----------------|--|
| Coolant: | Water outlet temperature (core) 45°C |
| Core size: | Rectangular prism 46 cm square, 63.5 cm high |
| Specific power: | 29 kW/kg U-235 |
| Control: | Two safety rods, one shim rod; one regulating rod of cadmium strip |
| | clad in stainless steel, all rods operating in special fuel elements |
| Shielding: | The water is contained in a concrete tank 213 cm thick |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Dido Pluto DMTR

The authority has three *Material Testing Reactors* essentially of the same design: Dido and Pluto at Harwell and DMTR at Dounreay. Their main purpose is to test fuel, coolants and materials which may be used in future rectors, principally to study the effects of radiations under reactor conditions. Dido and Pluto are also used for the production of isotopes of high specific activity and for research in physics, chemistry and metallurgy.

Dido: Deuterium oxide-moderated reactor i.e. D₂O or DDO

Pluto: Loop Testing Reactor Commissioning dates: **Dido:** 7 November 1956 **Pluto:** 28 October 1957

| Location: | Dido and Pluto: A E R E Harwell Berkshire |
|-----------------------|---|
| Reactor type: | Thermal heterogeneous, MTR |
| Reactor power: | 15 MW (Th.) |
| Designer: | UKAEA |
| Builder: | Head Wrightson Processes Ltd. |
| | MTR-type plates 80% enriched uranium alloyed with aluminium; |
| Fuel element: | clad in aluminium |
| Number of | Dido: 25 arranged in rows 4, 6, 5, 6, 4 Total 3.75 kg U-235 |
| elements: | |
| | Pluto: 26 arranged in rows 4, 6, 6, 6, 4 Total 3.9 kg U-235 |
| Moderator: | 10 nt D ₂ O |
| Coolant: | D_2O outlet temperature 53°C (bulk) |
| Core size: | Approximate vertical cylinder, 61 cm high |
| | Dido: equivalent diameter 84 cm |
| | Pluto: equivalent diameter 87.5 cm |
| Specific power: | Dido: 4,000 kW/kg U-235 |
| | Pluto: 3,850,000 kW/kg U-235 |
| Control: | Coarse control/shut-off: six arms (Pluto seven arms) cadmium in |
| | stainless steel sheath, two vertical safety rods, one vertical fine control rod |
| | of cadmium in stainless steel tubes, D ₂ O reflector dumping |
| Shielding: | Dido: 0.65 cm boral, 10.2 cm lead (water cooled) surrounded by |
| | 152 cm barytes concrete |
| | Pluto: 0.65 cm boral, 10.2 cm lead (water cooled) about 45 cm, iron |
| | shot concrete (variable thickness) followed by not less than 120 cm of |
| | barytes concrete |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Horace

H₂O Reacot Aldermaston Critical Experiment Commissioning date: May 1958 A zero energy reactor, H₂O moderated, with MTR-type fuel

The reactor core is a duplicate of the research reactor Herald core and is used for reactivity measurements required for the operation of Herald and the safety assessment of experiments.

| Location: | A W R E Aldermaston Berkshire |
|-----------------------|--|
| Reactor type: | Thermal heterogeneous swimming pool |
| Reactor power: | 5 MW (Th.) |
| Designer: | UKAEA |
| Builder: | A W R E Aldermaston |
| Fuel element: | 80% enriched U-235 in uranium-aluminium alloy in aluminium plates |
| Number of | Up to 70 in various configurations made up of elements, beryllium |
| elements: | reflectors and mock-ups of incore rigs |
| Moderator: | Light water |
| Coolant: | Light water |
| Core size: | Maximum approximately 68.6 cm \times 58.4 cm \times 61 cm high |
| Specific power: | Zero energy |
| Control: | six flat absorbers, cadmium in stainless steel, with aluminium followers |
| Shielding: | Screening wall 366 cm high, 30.5 cm thick of aggregate concrete blocks |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Herald

| Location: | A W R E Aldermaston Berkshire |
|-----------------------|--|
| Reactor type: | Thermal heterogeneous swimming pool |
| Reactor power: | 5 MW (Th.) |
| Designer: | A E l-John Thompson Nuclear Energy Co. Ltd. and AWRE |
| Builder: | A E l-John Thompson Nuclear Energy Co. Ltd. |
| Fuel element: | Aluminium MTR type 14 fuel plates per element |
| Number of | Up to 50 fuel elements, total 6 kg U-235 |
| elements: | |
| Moderator: | Light water |
| Coolant: | Light water up to 50°C |
| Core size: | $68.6 \text{ cm} \times 58.4 \text{ cm} \times 61 \text{ cm}$ high |
| Specific power: | 800 kW/kg U-235 |
| Control: | Six flat cadmium sheet absorbers in stainless steel with aluminium |
| | followers operating together |
| Shielding: | Biological: 61 cm iron shot concrete and 122 cm barytes concrete |
| | Thermal: 10.2 cm lead cast in aluminium segments |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Zenith

Zero Energy Nitrogen-Heated Thermal Reactor Commissioning date: December 1959 A thermal, near-homogeneous, reactor with variable fuel-graphite moder-

ated and reflected. Nitrogen is used as heating gas.

Zenith is designed for the study of the physics of high-temperature gas-cooled systems. Circulation of nitrogen gas over a 250 kW heater at the base of the core allows the core and side reflector regions to be heated to 800° C and 400° C respectively.

| Location: | A E E Winfirth Dorset |
|------------------------|---|
| Reactor type: | Thermal near-heterogeneous variable fuel |
| Reactor power: | Zero energy [max. 200 W (Th.)] |
| Designer: | UKAE and General Electric Company Ltd. |
| Builder: | General Electric Company Ltd. |
| Fuel element: | 93% enriched uranium or plutonium alloy containing 97.5% Pu-239, 2.4% Pu-240 and 0.1% Pu-241 |
| Number of elements: | 235 fuel elements made of pallets in graphite tubes giving a variable core loading |
| Moderator: | Graphite (in the fuel element tubes) |
| Coolant: | Nitrogen is used as heating gas to give 800°C maximum core temperature |
| Core size: | Cylindrical 183 cm high, 122 cm diameter |
| Specific power: | Not applicable |
| Control: | 1–10 motorised boron carbide safety rods; 3–6 motorised boron carbide shut-off rods; 1 fine, 1 coarse boron carbide control rod |
| Shielding: | 1.91 cm thick mild steel pressure vessel in contained pit of 122 cm thick barytes concrete |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Vera

Versatile Experimental Reactor Assembly Commissioning date: 22 February 1961

A zero-energy fast reactor built on a lattice plate which is separated into two halves for convenience and safety on loading. Fuelled with U-235 or Plutonium and designed for research in fast reactor physics, particularly for the purpose of checking nuclear data and calculation methods.

| Location: | AWRE Aldermaston Berkshire |
|-----------------------|--|
| Reactor type: | Fast, zero energy |
| Reactor power: | 10 W (Th.) |
| Designer: | UKAEA |
| Builder: | UKAEA |
| Fuel element: | U-235, square plates unclad, sprayed with lacquer. Pu-239 square |
| | plates clad in soft-soldered copper |

| | (continued) |
|---------------------|---|
| Number of elements: | Normally 40–60 in a maximum of 144 channels – the remainder, containing standard elements of reflector material |
| Moderator: | Variable (graphite, steel, polythene etc.) in square plates or blocks |
| Coolant: | None |
| Core size: | Maximum 55.8 cm cube. A typical core is a 35.6 cm isometric pseudo- cylinder |
| Specific power: | Not applicable |
| Control: | Four safety rods of standard fuel reflector elements, three control rods of similar elements |
| Shielding: | No integral shielding – the reactor is located in a shielded laboratory |
| (Data provided by | the Late Lord Marshall of UKAEA 1989) |

(continued)

Nestor

Neutron Source Thermal Reactor Commissioning date: September 1961 A thermal heterogeneous reactor, fuelled with highly enriched uranium, light water moderated and cooled, graphite reflected.

The Nestor reactor provides a source of neutrons and accordingly has a number of special features. It consists of an annular core structure containing highly enriched uranium–aluminium alloy as fuel plates immersed in water. Graphite fills the centre of the annulus and surrounds it externally. The graphite serves two important purposes. It reduces the amount of uranium required to obtain a self-sustaining chain reaction in the core. In addition, it screens the reactor from the experimental assemblies and ensures that the power level, control and safety of the reactor are not significantly affected by rearrangements in the experimental assemblies.

| Location: | AEE Winfirth Dorset |
|-----------------------|---|
| Reactor type: | Thermal heterogeneous (modified Jason type) |
| Reactor power: | 10 kW (Th.) rising to 30 kW in 1964 |
| Designer: | Hawker Siddley/Nuclear Power Co. and UKAEA |
| Builder: | Hawker Siddley/Nuclear Power Co. and Turriff Construction Corporation Ltd. |
| Fuel element: | MTR-type plates containing 80% enriched U-235 in aluminium alloy clad in aluminium |
| Number of elements: | 16–24 channel spaces not occupied by fuel elements are filled by aluminium-clad graphite blocks. Total 4.6 kg uranium |
| Moderator: | Demineralised water |
| Coolant: | Demineralised water at 35°C |
| Core size: | Fuel elements from an annulus 15.24 cm wide and 76.2 cm mean diameter in cylindrical aluminium tank |
| Specific power: | 2.18 kW/kg U-235 |
| Control: | Two safety plates of cadmium clad in stainless steel; two similar control plates. Water moderator can be dumped |
| Shielding: | 76 cm of iron shot concrete |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Hero

Hot Experimental Reactor of 0 (zero) power Commissioning date: 5 February 1962

This zero-energy reactor was designed to complement the Advance Gascooled Reactor at Windscale in providing physics information on the AGR system.

The graphite-moderated core is cylindrical, both height and diameter being 18 ft and the design is such that it can be dismantled and re-assembled so that it could be used to study a verity of core geometries but as planned the reactor is mainly used for testing lattices at the AGR lattice pitch. Carbon dioxide is circulated through the core and external heaters are provided which can heat the gas to give core temperature up to 500°C, thus enabling operating conditions of the temperature of the AGR to be simulated without the development of residual radioactivity, which would hamper experimental work.

| Location: | Windscale Cumberland |
|-----------------------|---|
| Reactor type: | Head lattice test reactor |
| Reactor power: | 3 kW (Th.) |
| Designer: | UKAEA |
| Builder: | UKAEA |
| Fuel element: | Enriched UO ₂ (1.8% U-235) clad in stainless steel |
| Number of | Variable 325 channels (maximum) are variable for use |
| elements: | |
| Moderator: | Graphite, raised to 500°C by electrically heated CO ₂ |
| Coolant: | CO_2 |
| Core size: | Vertical axis cylinder 549 cm high, 554 cm diameter |
| Specific power: | $20	imes 10^{-3}\mathrm{kW/kg}$ |
| Control: | Variable; up to 6 boron steel safety rods, 2 fine control and 16 coarse |
| | control rods dependent on the experiment |
| Shielding: | 122 cm high-density concrete |

Daphne

Dido and Pluto Handmaiden for Nuclear Experiments Commissioning date: 20 February 1962

A thermal heterogeneous reactor, fuelled with enriched uranium. D_2O moderated and cooled, D_2O and partial graphite reflectors.

Designed to provide basic physics support to Dido and Pluto and therefore is very similar to these reactors in the main design features. It can be loaded with fuel elements, rigs and beam tubes to stimulate Dido, Pluto or other reactors of this class. The reactor operates at powers up to 100 W and is shielded by 4 ft thick concrete blocks.

| Location: | AERE Harewell Berkshire |
|-----------------------|--|
| Reactor type: | Thermal heterogeneous |
| Reactor power: | 100 W (Th.) |
| Designer: | UKAEA |
| Builder: | UKAEA |
| Fuel element: | MTR-type plates 80% enriched uranium alloyed with aluminium; clad in aluminium l |
| Number of | 25 for Dido simulation (3.75 kg U-235), 26 for Pluto simulation |
| elements: | (3.9 kg U-235) |
| Moderator: | D_2O at 7 t at ambient temperature |
| Coolant: | D ₂ O at ambient temperature |
| Core size: | Approximate vertical cylinder 61 cm high, equivalent diameter about 86 cm |
| Specific power: | 27 kW/t U-235 |
| Control: | Four safety rods cadmium in stainless steel sheath in hollow fuel elements, vertical fine control rod (same type). Control is by variation by D_2O level and/or reactor fine control rod. Signal-type coarse control arms (cadmium in stainless steel sheath) may be adjusted when sub-critical to stimulate coarse control/shut-off arms in Dido and Pluto |
| Shielding: | 120 cm Portland concrete |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Dimple

Deuterium-Moderated Pile of Low Energy

Commissioning date at Winfirth: 18 June 1962

A thermal heterogeneous reactor, with fuel and moderator variable; removable graphite reflectors no coolant.

The Zero-Energy Reactor, Dimple, which was used at Harwell until late 1960, has been extensively modified and rebuilt at Winfirth. Dimple can now be used to study the physics of reactor systems moderated by light or heavy water or by an organic moderator. Containment and monitoring equipment have been provided to permit the use of plutonium-bearing fuels. A wide variety of coarse structures can be built into Dimple ranging from large pressure tube systems to small close packed systems moderated with H₂O or H₂O/D₂O mixtures, which are of interest in the field of marine propulsion. The reactor may be heated uniformly to about 90°C.

| Location: | AEE Winfirth Dorset |
|-----------------------|---|
| Reactor type: | Thermal heterogeneous variable moderator and fuel |
| Reactor power: | 100 W (Th.) |
| Designer: | UKAEA |
| Builder: | UKAEA |
| Fuel element: | Uranium or plutonium as required |
| Number of | Variable |
| elements: | |

| | (continued) |
|-----------------|---|
| Moderator: | Liquid; variable in amount and composition |
| Coolant: | None |
| Core size: | Variable: A maximum 259 cm diameter 249 cm high |
| Specific power: | Negligible |
| Control: | Safety rods: either two separate banks containing up to 10 rods per |
| | bank (variable in size and composition) or fast internal moderator |
| | dump into cavity within tank. Coarse and fine control rods of |
| | variable composition and number, the difference being achieved by |
| | different gear speeds |
| Shielding: | 122 cm thick concrete block construction |
| | |

(continued)

(Data provided by the Late Lord Marshall of UKAEA 1989)

Zebra

Zero-Energy Breeder Reactor Assembly Commissioning date: 19 December 1962

A fast reactor fuelled with plutonium and/or highly enriched uranium, enrichment variable; no moderator; reflector composition variable but commonly natural uranium; no coolant.

To date, experimental fast reactors have compromised very small highly enriched cores. For example, the core of the Dounreay experimental fast reactor is about 2 ft diameter and 2 ft high. For power producing fast reactor to be used in electricity generating stations much larger reactors with lower enrichment are envisaged.

The neutron physics of the reactor will be studied in Zebra.

| Location: | AEE Winfirth Dorset |
|-----------------------|---|
| Reactor type: | Zero-energy fast breeder |
| Reactor power: | 100 W (Th.) maximum |
| Designer: | UKAEA |
| Builder: | UKAEA |
| Fuel element: | Plates: initial experimental programme provided 350 kg U-235 as 93% enriched uranium, unclad; 150 kg U-235 as $36\frac{1}{2}$ % enriched uranium, unclad; 100 kg plutonium clad in thin layers of copper |
| Number of elements: | Variable |
| Moderator: | None |
| Coolant: | None |
| Core size: | Variable |
| Specific power: | Variable |
| Control: | Nine control rods: five screw type operated from below; four cable type operated from above; two screw type used as safety rods; two groups of cable type used as shut-off rods: three screw-type rods used as regulating rods; one (of smaller worth) is used for fine control |
| Shielding: | 106 cm Portland concrete; 2 heavy concrete doors roll back to give access to the top of the reactor |

(Data provided by the Late Lord Marshall of UKAEA 1989)
Hector

Heated Experimental Carbon Thermal Oscillator Reactor Commissioning date: 10 March 1963

A zero-energy thermal reactor; two-region core; graphite moderated and reflected with carbon dioxide heating and cooling.

Hector is designed for obtaining information on the physics of power reactors by means of experiments using small quantities of material. A sample of the material is introduced into the centre of the reactor and the observed rate of change of the reactor power gives a measure of the neutron absorbing properties of the sample. An alternative technique is to move the sample in and out of the reactor periodically and to observe the resultant fluctuation of the power level. The reactor lattice in the neighbourhood of the sample is adjusted so as to simulate the conditions existing in a power reactor.

The rector core consists of two regions. The outer region is an annulus of graphite containing fuel in the form of plates of an alloy of highly enriched uranium and aluminium. This is known as the 'driver' region. Within this annulus is a central region which may be heated to a temperature of up to 450°C by a stream of electrically heated carbon dioxide gas. A variety of assemblies of fuel and moderators may be lodged into this region.

| Logation | AFE Winfirth Doroot |
|-----------------------|--|
| Location: | |
| Reactor type: | Zero energy thermal |
| Reactor power: | 100 W |
| Designer: | Fairey Engineering Ltd. to AEA specification |
| Builder: | Fairey Engineering Ltd. |
| Fuel element: | Central core region: variable. |
| | Outer core region: Dido-type flat plates |
| Number of | Central core region: 128 channels |
| elements: | |
| | Outer core region: 216 channels |
| Moderator: | Graphite |
| Coolant: | CO ₂ used to heat the central region and cool the outer region |
| Core size: | Central: octagonal graphite stack 91.1 cm across flats by 285 cm high with outer diameter 359 cm and octagonal hole 123 cm across flats along axis |
| Specific power: | Very small |
| Control: | All control and safety rods are B.C packed in steel tubes; six safety rods and six shutdown rods; two coarse control rods and one fine |
| Shielding: | control rod; up to eight temperature rods |
| - | 122 cm concrete with shield doors which open to expose whole top surface of reactor vessel |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Juno

Commissioning date: April 1964

Juno is a dual-purpose assembly for the study either of compact liquidmoderated cores or of pressure tube-type liquid-moderated lattices in critical configurations. It may alternatively be used as an experimental system, driven external neutron sources, for the study of pressure tube-type cores.

It will be used for the study of the physics of the reactor systems moderated by light or heavy water supplementing the work of the reactor Dimple to which it bears many similarities.

When required, it may be modified to permit the use of plutonium-bearing fuel. A wide variety of core structures can be built into Juno ranging from critical cores of closed pack fuel assemblies moderated by light or heavy water (of interest of marine work) to large cores of Steam-Generating Heavy Water type. These may be studied exponentially if required.

When in use as a compact critical assembly, emergency shutdown is provided by a rapid internal dump system which is ideally suited for the study of close packed cores where the provision of control rods involves an unacceptable perturbation of the core.

| Location: | AEE Winfirth Dorset |
|-----------------------|---|
| Reactor type: | Thermal, heterogeneous, variable moderator and fuel |
| Reactor power: | 100 W (Th.) |
| Designer: | UKAEA |
| Builder: | UKAEA |
| Fuel element: | Uranium or plutonium as required |
| Number of | Variable |
| elements: | |
| Moderator: | Liquid; variable in amount and composition |
| Coolant: | None |
| Core size: | Variable – maximum 190 cm diameter, 350 cm high |
| Specific power: | Negligible |
| Control: | Fast shutdown: Internal moderator dump into cavity within tank for compact cores. Two banks of thermal absorbers may be fitted for pressure tube-type lattices. |
| | Fine control: Variation of moderator level or insertion of fine control |
| | rods |
| Shielding: | 4 ft thick concrete block construction |

(Data provided by the Late Lord Marshall of UKAEA 1989)

Tokai Mura Nuclear

Commissioning date: estimated July 1965

This Japan Atomic Power Company's Tokai nuclear power station is situated on the Pacific coast about 70 miles north-east of Tokyo. The station is a single reactor housed in a skirt-supported spherical pressure vessel having a mean diameter of 18.4 m (60.4 ft) and made from steel plates 92 mm (3.6 in.) and 80 mm (3.16 in.) thick. There are four steam-raising units feeding two 85 MW turbo generators. Also operating from the main HP steam circuit are four 8700 hp back-pressure turbines which drive the centrifugal coolant-circulators. Of particular interest are the special design features introduced because of the potential earthquake hazard. These include substantial reinforcement of the concrete foundation raft and super-structure; additional restraints at the top of the reactor vessel and steam-raising units; an earthquake-resistant support system for main gas ducts; a new type of core restraint structure and a specially designed brick and key system of core construction. In addition, there is a secondary shutdown system capable of operating even if damage to the core should prevent normal functioning of the control rods.

| Location: | Tokai Mura, Ibaraki-ken, Japan | | | |
|---------------------------------|--|---|--|--|
| Reactor type: | Magnox | | | |
| Reactor power: | 585 MW (Th.), 157 MW (E) net f | rom one reactor | | |
| Designer: | GEC/Simon-Carves Atomic Ener | gy Group | | |
| Builder: | British General Electric Company of Japan Ltd. The First Atomic Power Industrial Group (Japan) | | | |
| Fuel element: | Natural uranium hollow rods in M | agnox cans with graphite sleeves | | |
| Number of elements: | 16,357 in 2048 channels. Total 18 | 7 t natural uranium | | |
| Moderator: | 870 t graphite | | | |
| Coolant: | Carbon dioxide; outlet temperatu | re 390°C | | |
| Core size exclude reflector: | Cylinder mean diameter 11.72 m, | height 6.63 m | | |
| Specific power: | 3.14 kW/kg uranium 9 Safety rods 63 Coarse (Shim) rods 10 Sector (Auto) control rods 16 flattering and trim rods | <pre>boron steel Stainless clad mild steel Stainless clad</pre> | | |
| Reactor control: | 44 secondary shutdown Devices | } boron steel balls. | | |
| Shielding: | Biological: 3.1 m concrete | | | |

(With compliments of Japan Atomic Power, CO, Tokai, Japan 1970) (Also to CEGB, England)

Calder Hall and Chapelcross

Commissioning date: Calder Hall: October 1956, Chapelcross: May 1959

Each station consists of four reactors housed in cylindrical mild steel pressure vessels which are 70/71 ft high and 37 ft in diameter. Six fuel elements are stacked vertically in each of the 1696 channels per reactor. Each reactor has four heat exchangers generating high- and low-pressure steam simultaneously. Generating plant comprises eight 3000 rpm turbo alternators.

Design study work began in 1951, and construction work on Calder site commenced in August 1953. The first reactor became critical in May 1956 and power was first fed to the National Grid in October 1956. Construction at

Chaplecross had begun in October 1955. Heat and electricity output had been increased in stages at both stations to well beyond the design figures. Present heat output per reactor is 235/240 MW compared with the design output of 180 MW, a 30% improvement. The turbines have been rebladed to utilise this additional power. The Calder reactors also supply the steam requirements of the adjacent Windscale factory for space heating and for the operation of the chemical plant.

In 1964 an average load factor in excess of 92% was achieved at both stations and full load was maintained for 98% of the time during the severe winter of 1962/1963. Up to 28 February 1965 the total electricity supplied to the national grid from each station has been as follows:

| Location: | Magnox |
|-----------------------|---|
| Reactor power: | Calder Hall: 235 MW (Th.) 45 MW (E) Net. Chapelcross: 235/ |
| | 240 MW (Th.) 45 MW (E) net from each of four reactors |
| Designer: | UKAEA |
| Builder: | Various contractors |
| Fuel element: | Natural uranium in Magnox cans |
| Data for each reactor | |
| Number of elements: | 10,176 in 1696 channels |
| | Total 127 t natural uranium |
| Moderator: | 650 t of graphite in 58,000 bricks |
| Coolant: | Carbon dioxide, outlet temperature 340°C |
| Core size: | Polygonal prism: 9.45 m diameter, 6.40 m high |
| Specific power: | 1.35 kW/kg uranium |
| Control: | 48 rods also used as safety rods (8 inner zone, 16 outer zone); any 4 |
| | can be selected as time-regulating rods of boron steel in stainless |
| | steel tubes |
| Shielding: | Biological: 213 cm concrete |
| | Thermal: 15.25 cm steel |
| | |

Calder 8280 million units Chapelcross 7020 million units

(Data collected from Natural Grid 1956)

Hunterston

Commissioning date: Reactor number 1: February 1964 Reactor number 2: July 1964

The South of Scotland Electricity Board's nuclear generating station at Hunterston, on the Ayrshire coast, is one of the first three civil stations – each with an electrical output of about 300 MW from two reactors – to be built under the government's nuclear power programme of 1957.

The design of the station embodies several features which are not available in other early stations and which should increase output, operational economy and safety.

These features include the charging and discharging of fuel from the bottom of the reactor vessels where the temperature is lower, the provision of separate fuel-handling machines at the top of the vessels if required and the provision of remotely adjustable rods for the maintenance of reactivity balance.

In addition each fuel element is separately contained and supported within a graphite sleeve -a refinement which eliminates bowing and the sticking of the elements and gives protection against the build-up of Wigner energy.

Each reactor at Hunterston is associated with a group of eight steam-raising units feeding three 60 MW turbo alternators. The station operates on the base load and feeds electricity into the 275 kV grid at Nielston, Renfrewshire.

| Location: | Hunterston Ayrshire Scotland |
|-----------------------|---|
| Reactor type: | Magnox |
| Reactor power: | 535 MW (Th.), 150 MW (E) net from each of two reactors |
| Designer: | GEC/Simon Carves Atomic Energy Group |
| Builder: | General Electric Company Ltd. (Main) |
| Fuel element: | Natural uranium bars in Magnox cans, with graphite sleeves |
| Data for each | |
| reactor | |
| Number of | 32,880 in 3288 channels. |
| elements: | Total 251 t natural uranium |
| Moderator: | 1200 t graphite |
| Coolant: | Carbon dioxide, outlet temperature 395°C |
| Core size: | Right cylinder: 13.5 m diameter, 7.01 m high |
| Specific power: | 2.13 kW/kg uranium |
| Control: | 8 safety rods; 130 coarse regulating rods; 18 fine regulating rods of stainless steel with 4% boron |
| Shielding: | Biological: 282 cm of concrete |

(Data provided by GEC/Simon Curves Atomic Energy Group, U.K. (1972))

Hinkley Point 'A'

Commissioning Date: Reactor number 1: February 1965 Reactor number 2: 2 April 1965

Hinkley point is located on the north coast of Somerset on the Bristol Channel, some 8 miles north-west of Bridgewater. The 'A' station consists of two reactors housed in steel spherical pressure vessels of 67 ft diameter, made of plates 3 in. thick. Each reactor has six boilers. Generating plant consists of six 3.5 MW turbo alternators and three 33 MW turbo alternators to provide auxiliary supplies. Total output of the station is 500 MW, which is fed into the 75 kV Supergrid system running between Melksham and Taunton.

Hinkley Point 'B'

Extensive land reclamation was carried out, and in view of the advantages of the site, the circulating water system was designed to cater for a further station,

| Hinkley 'B' | to be | built at s | ome late | r date. | The | Minister | of . | Power | has | gıven | his |
|-------------|----------------|------------|----------|---------|--------|--------------|-------|---------|------|-------|-----|
| consent for | 'B' sta | tion about | t 1000 M | W outp | out. I | t is identio | cal t | to Hart | leyp | ool N | PS. |

| Location: | Hinkley point Somerset |
|-----------------------|---|
| Reactor type: | Magnox |
| Reactor power: | 971 MW (Th.), 250 MW (E) net from each of two reactors |
| Designer: | English Electric–Babcock & Wilcox–Taylor, Woodrow Atomic Power Group |
| Builder: | English Electric–Babcock & Wilcox–Taylor, Woodrow Atomic Power Group |
| Fuel element: | Natural uranium bars in Magnox cans |
| Data for each reactor | |
| Number of elements: | 36,000 in 4500 channels. |
| | Total 376 t natural uranium |
| Moderator: | 2475 t graphite |
| Coolant: | Carbon dioxide, outlet temperature 378°C |
| Core size: | 24-Sided prism, 14.9 m diameter, 7.63 m high |
| Specific power: | 2.55 kW/kg uranium |
| Control: | 130 control rods in 12 zones; 15 safety rods of boron steel tubes |
| Shielding: | Biological: 22.8 cm + 297 cm concrete |

(Data with compliments from Taylor Woodrow Atomic Power Group, Southall, Middlesex)

Trawsfynydd

Commissioning date: Reactor number 1: January 1961 Reactor number 2: 2 March 1965

Trawsfynydd is situated on the artificial lake of that name created some 30 years ago as a storage reservoir for the Maentwrog hydroelectric power station and lies within the Snowdonia National Park, North Wales. The station consists of two reactors, housed in spherical-type pressure vessels made of steel, $3\frac{1}{2}in$. thick, with an internal diameter each of 61 ft. Each reactor supplies heat to six boiler units. Generating plant comprises four 3000 rpm turbo alternators each with a rated output of 145 MW at 0.8 power factor (lagging). The total guaranteed net output of the station in megawatts sent is 500 MW.

Total cost of the power station, including the plant and the roadworking, etc., is estimated at £68.5 million, giving a capital cost of £137 per kilowatt sent out, and an estimated cost per unit of 0.96d.

Output from the station is fed into the 275 kV grid system, the main connection being to Connah' Quay and Ffestiniog. Some output will also reinforce the 33 kV main distribution system, North Wales.

| Location: | Trawsfynydd Merionethshire Wales |
|-----------------------|---|
| Reactor type: | Magnox |
| Reactor power: | 860 MW (Th.), 250 MW (E)net from each of two reactors |
| Designer: | Atomic Power Construction Ltd. |

| Builder: | Atomic Power Construction Ltd. (now part of the United Power |
|-----------------|---|
| | Company Ltd.) |
| Fuel element: | Natural uranium bars in Magnox cans |
| Data for each | |
| reactor | |
| Number of | 33,480 in 3720 channels |
| elements: | Total 280 t natural uranium |
| Moderator: | 2090 t graphite |
| Coolant: | Carbon dioxide, outlet temperature 394°C |
| Core size: | Cylinder: 13.56 m diameter, 7.31 m high |
| Specific power: | 3.11 kW/kg uranium |
| Control: | 185 control rods arranged in 9 sectors; 12 safety rods of boron steel |
| | in stainless steel tubes |
| Shielding: | Biological: 304 cm concrete |

(continued)

(Data provided by Atomic Power Construction Ltd, 1967)

Sizewell A

Commissioning date: Reactor number 1: August 1965 Reactor number 2: February 1966

Sizewell is situated on the Suffolk coast between Aldeburgh and Southwold. The station has two reactors housed in spherical-type pressure vessels 63 ft 6 in. in diameter and formed from mild steel plates $4\frac{1}{8}in$. thick. Each reactor has four boilers. Generating plant comprises two 3000 rpm turbo alternators, each with a rated output of 324.7 MW at 0.85 power facoter (lagging). The total guaranteed net output of the station on megawatts sent out is planned as 580 MW, estimated to be achieved by spring 1966.

| Reactor type: | Magnox |
|--------------------------|--|
| Reactor power: | 948 MW (Th.), 290 MW (E) net from each of two reactors |
| Designer: | English Electric-Babcock & Wilcox-Taylor Woodrow Atomic Power Group |
| Builder: | English Electric–Babcock & Wilcox–Taylor Woodrow Atomic Power Group |
| Fuel element: | Natural uranium bars in Magnox cans |
| Data for each reactor | |
| Number of | 26,600 in 3800 channels |
| elements: | Total 321 t natural uranium |
| Moderator: | 2237 t graphite |
| Coolant: | Carbon dioxide, outlet temperature 410°C |
| Core size: | 24 – sided prism: 13.7 m diameter, 7.92 m high |
| Specific power: | 2.96 kW/kg uranium |
| Control: | 99 control rods in 9 zones; 8 safety rods of boron steel or mild steel |
| Shielding: | Biological: 304.8 cm concrete |

(With compliment of Taylor Woodrow and English Electric, UK.)

Sizewell B PWR

It is the pressurised water reactor station. The containment vessel has been analysed in this text against all eventualities.

WYLFA

Commissioning date: Reactor number 1: 1968 Reactor number 2: 1969

Wylfa is situated on the North-West coast of the Isle of Anglesey at WYLFA Head. The station is found on rocks and large blasting programme was entailed in its construction. Each of the two units comprises a prestressed concrete pressure vessel, reactor core and internal shielding, boiler and gas circulator. The pressure vessel has a spherical internal shape of 96 ft diameter and a minimum wall thickness of 11 ft. The boilers, one to each vessel, are single pressure one through type with four associated gas circulators. Generating plant consists of four 3000 rpm turbo alternators each with a rated output of 370.22 MW at 0.9 power factor (lagging). The total guaranteed net output of the station in megawatts sent out is planned as 1180 MW, the most powerful nuclear power station under construction anywhere in the world.

| Location | Wylfa Point Anglesey North Wales |
|--------------------------|---|
| Reactor type | Magnox |
| Reactor power: | 1,875 MW (Th.), 590 MW (E) net from each of two reactors |
| Designer: | English Electric-Babcock & Wilcox-Taylor Woodrow Atomic |
| Builder: | Power Group |
| | English Electric–Babcock & Wilcox–Taylor Woodrow Atomic Power Group |
| Fuel element: | Natural uranium bars in Magnox cans |
| Data for each reactor | |
| Number of | 49,200 in 6150 channels. |
| elements: | Total 595 t natural uranium |
| Moderator: | 3740 t graphite |
| Coolant: | Carbon dioxide, outlet temperature 414°C |
| Core size: | 16-sided cylinder: 17.3.7 m diameter, 9.14 m high |
| Specific power: | 3.16 kW/kg uranium |
| Control: | 167 control rods in 16 zones; 18 safety rods of boron steel or mild steel |
| Shielding: | The prestressed concrete reactor pressure vessel is 353.3 cm thick |

(With compliments of English Electric, WYLFA and Taylor Woodrow, Southall, Middlesex, 1966)

SGHWR

Steam-Generating Heavy Water Reactor (SGHWR) Commissioning date:Late 1967 SGHWR is a steam-generating heavy water moderated reactor

The core of the reactor consists of a bank of pressure tubes which pass through vertical tubes in a calandria, or tank, containing the heavy water moderator. Fuel is contained within the pressure tubes and the heat generated is removed by light water passing up these tubes and being partially turned into steam. After separation into steam drum, most of the steam passes directly to a turbine; the rest is passed through eight super-heat channels which will raise the steam to an outlet temperature of about 1000°F. This steam is then mixed with main steam flow before being fed to the turbine.

About 13% of the light water which is circulated over the fuel elements in the most highly rated boiling channel is converted into steam to give a turbine a stop valve pressure of 900 psig. The heavy water moderator has its own cooling and purification circuit and the light water coolant has circuits for water treatment and the detection of fuel element can failure.

Construction began at Winfirth in 1963 and the reactor will have an electrical output of 100 MW.

| Location: | Winfirth Heath Dorset |
|------------------------|--|
| Reactor type: | Steam-generating heavy water moderator (SGHWM). Direct cycle |
| • • | pressure tube |
| Reactor power: | 294 MW gross thermal. 100 MW gross electrical |
| Designer: | UKAEA |
| Builder: | Main contractors: Turriff, AEI, International Combustion, Fairey Aviation |
| Fuel element: | Boiling channels: UO_2 pellets clad in zircaloy-2. |
| | Superheat channels: UO ₂ pellets clad in stainless steel |
| Number of elements: | Boiling: 3744 fuel pins, 36 pins per assembly. 1 assembly per channel, 104 boiling channels, one of which is connected to an independent cooling circuit for testing fuel. Total 21,100 kg uranium. Superheating: 184 fuel pins, 24 pins per assembly, 1 assembly per |
| Modorator | channel 8 superheat channels. Total 950 kg uranium |
| wiouerator. | Heavy water in calandria (some moderation also in boiling light |
| Coolant: | water coolant) |
| | Direct cycle light water, boiling channel outlet temperature 283°C, |
| Core size: | superheat channel outlet temperature 504°C |
| Control: | Cylinder: 311 cm diameter (excluding D ₂ O reflectors), 366 cm long (excluding D ₂ O reflectors) |
| Specific power: | Boiling channels 19.7 kW/kg. |
| | Superheat channel 15.3 kW/kg |
| | Shutdown: Boric acid solution in interlattice tubes, plus D_2O dump. |
| | Control: D ₂ O height for power control. Boric acid concentration in moderator for long-term reactivity changes. Flooding groups of interlattice tubes for spectral shift flux control |
| Shielding: | Water and steel plus concrete biological shield, 282 cm thick |

DFR

Dounreay Fast Reactor Commissioning Date: 14 November 1959

The reactor has been designed to establish the feasibility of the fast breeder system and to provide information and operating experience needed to design a prototype reactor for full-scale power production.

The reactor core is hexagonal, 21 in. high and $20\frac{1}{2}in$. across the flats, containing 324 fuel channels, with a central hexagon 5 in. across the flats, which can accommodate experimental fuel pins or sub-assemblies. The core is surrounded by a breeder blanket of 1872 channels. A number of channels in both the core and the blanket are also used for experimental fuel elements. Control and shutdown are provided by 12 groups each of 10 fuel elements around the edge of the core, mounted in carriers which can be raised or lowered. Liquid sodium–potassium alloy is used as coolant and transfers heat from the fuel to secondary liquid metal circuit in 24 heat exchangers set around the reactor vessel within the biological shield. This field is in the form of a concrete vault 90 ft in diameter and 5 ft thick and occupies the lower half of the steel containment sphere, 135 ft in diameter.

The principal use of the rector is now as a testbed for plutonium-based fuels for the prototype power fast reactor, in relation to both performance and to the effects of high burn-up.

| Location: | DERE Dounreay Scotland |
|------------------------|---|
| Reactor type: | Fast breeder |
| Reactor power: | 60 MW gross (Th.); 13 MW (E) |
| Designer: | UKAEA |
| Builder: | (Main) John Thompson Ltd., Motherwell Bridge and Engineering Co. Ltd., Whatlings Ltd. and others |
| Fuel element: | 45.5% enriched U-235, seven rods per element with 15 cm natural uranium as a top blanket. Cladding niobium |
| Number of elements: | Variable according to the experimental programme. The driver charge coantains approximately 200 kg U-235 |
| Moderator: | None |
| Coolant: | Liquid sodium potassium alloy (NaK) at 350°C (outlet) |
| Core size: | Hexagonal prism 52.5 cm across flats, 52.5 cm high |
| Specific power: | Approx. 300 kW/kg U-235 |
| Control: | 12 groups of fuel elements comprised of 6 regulating groups, 4 shut- down and 2 safety groups |
| Shielding: | Biological: concrete 152 cm thick. Vessel: 120 cm of borated graphite |



Plate 1.13 DFR. Dounreay Fast Reactor. The photo provided by SSEB Scotland 1988

Dragon

Commissioning date: 22 October 1964

The chief purpose of the reactor experiment is to demonstrate the principles on which any high-temperature gas-cooled reactor must be based. The entire power station is now dismantled.

The main features of the reactor, arising from the high operating temperature in the core, are the use of helium as a coolant with the fuel elements made from impermeable graphite containing uranium and thorium dicarbide mixed with graphite in a suitable ceramic form. Each element consists of a seven-rod cluster, provision being made from fission products which escape from fuel inserts by passing a fraction of the total coolant through a system of fission traps, and coolant circuit is expected to be slightly radioactive.

The steel reactor vessel consists of main cylindrical portion 11 ft 6 in. diameters, containing the core and reflector, with a 'neck' 6 ft 3 in. diameter through which the fuel elements are inserted and removed. The whole reactor, with its shielding, primary coolant circuit and much of the ancillary plant, is enclosed in the containment vessel with an inner shell of steel 66 ft diameter, 81 ft high and an outer shell of concrete 110 ft diameter, 86 ft high with wall 2 ft thick.

| Location: | AEE Winfirth Dorset |
|----------------------|---|
| Reactor type: | High-temperature reactor project |
| Reactor power: | 20 MW (Th.) |
| Designer: | OECD high-temperature reactor project |
| Builder: | Contractors in signatory countries |
| Fuel element: | Outer annular region (27 elements) pyrolytic carbon-coated U-235/ zirconium monocarbide spherical particles consolidated in graphite matrix, to form inserts, 30 per fuel rod. Inner central region (10 elements) pyrolytic carbon and silicon carbide-coated U-235 thorium carbide spherical particles. Zr:U-235 ratio 8:1 Th:U-235 ratio 10:1 |
| Number of | 37 elements, 259 rods |
| elements: | Total weight: 14 kg U-235 uniformly distributed |
| Moderator: | Graphite, integral with fuel elements |
| Coolant: | Helium, outlet temperature 750°C |
| Core size: | Equivalent diameter of assembly 107 cm. Length of core 160 cm |
| Specific power: | 1.4 kW/kg |
| Control: | 24 symmetrical granular boron carbide absorber rods are provided. Three or 4 are used as safety rods, 1 is an automatic regulator, 19 or 20 remainder can be used manually as regulators |
| Shielding: | Primary: 92 cm graphite reflector, 5 cm steel baffle, 5 cm steel pressure vessel, 38 cm thermal shield (alternate layers of steel and water) 175 cm concrete.Secondary: 61 cm (minimum) concrete |

1.3 Reactor Power Stations Based on BWR, PHWR and PWR

1.3.1 Boiling Water Reactors (BWR)

All boiling water reactors in Scandinavia are of Asea-Atom design. Containment is based on the pressure suppression (PS) principle, i.e. at a major pipe rupture the steam is led from the upper part, dry well, through a number of pipes to the lower part of the containment, wet wall, with a water pool, where condensation takes place. This principle of the volume of the containment has been kept small, about one-fifth of that of a dry containment with the same design pressure.

The layout of the containments varies from plant to plant. The fuel element pools, together with the pool for the storage of reactor internals, rest on the containment proper, which is statically independent from the pool structure and from the surrounding outer reactor building which houses the reactor auxiliary systems. For Ringhals 1 the containment vessel has been built more integrally with the fuel element pools. In later designs the external circulation pumps have been replaced by internal circulation pumps, where the motor housing forms an integral part of the reactor vessel. Consequently, the layout of the containment can be simplified to cylinder with a solid partition slab between the dry-well and wet-well compartments. he PS containments are all prestressed horizontally and vertically, the latter for internal gas pressure minus the overlying weight. The design pressures are between 460 and 550 kN/m² (absolute pressure). In most cases the fuel element pools, which are partially cantilevered, are provided with prestressing tendons in the side walls. The top of the containment over the reactor vessel has to be removable for the refuelling operation and is designed as a steel dome.

A further development of the layout of the containment and adjoining structural units is showing the Asea-Atom current design. Consideration has also been taken to earthquake and airplane crash loading. The structural connection between the fuel pools and the containment proper has been further simplified.

ALL BWR plants, except Barsebäck 1 and 2, are founded on rock. In Barsebäck 1 and 2 the bottom of the containment consists of a thick slab on hard moraine-clay.

Six BWR plants exist in Japan at present. Table 1.1 gives a summary of BWR stations and structures associated with them.

1.3.2 Pressurised Heavy Water Reactors (PHWR)

Generally this system is based on 'CANDU'. Table 1.1 shows six of them built in Canada and six of them built in India; one of them exists in Romania, one is constructed in South Korea and one is in existence in Pakistan.

1.3.3 Pressurised Water Reactors (PWR)

PWR nuclear plants, Ringhals 2, 3 and 4, are all standard Westlinghouse design, except for the arrangement of the liner. They are provided with a dry containment in the shape of a cylinder with a dome roof, both in prestressed concrete. The design pressure is 510 kN/m^2 .

1.3.3.1 Design Details

A special feature in the design of the Scandinavian reactor containments is that the steel liner is usually embedded in the concrete. The internal concrete cover, approximately 250 mm, serves as an efficient protection for the liner against missiles during an accident while at the same time the liner is protected against corrosion. Furthermore, thermal expansion of the steel liner due to the elevated temperatures (155–180°C) during the initial phase of an accident is avoided, resulting in a saving of prestressing steel. The disadvantage of the embedment is that if leakage occurs during a test it may be difficult to locate and repair. For that reason the liner in some of the State Power Board plants has been provided with steel channels along all welds. The channels are connected in sections and with the outside, whereby leaking gas, if any, can be located and vented.

| | | Table | 1.1 BWR and PHWR Nuc | clear Pow | er Stations in the World | - | | |
|-------------|-----------------------|-------|-------------------------|-----------|--------------------------|-------|----------|----------|
| | | | | | No. of similar units | First | Design | Start of |
| Country | Name | Type | Nuclear system supplier | Power | onsite | power | pressure | erection |
| Japan | Kashiwazaki 4 | BWR | Hitachi | 1100 | 2 | 1993 | 0.416 | 1988 |
| Japan | Kashiwazaki 6 ABWR | BWR | Toshiba Hitachi GE | 1356 | 2 | 1995 | 0.416 | 1991 |
| Japan | Kashiwazaki 1 | BWR | Toshiba | 1100 | 3 | 1984 | 0.385 | 1978 |
| Japan | Shika 1 (NOTO) | BWR | Hitachi | 540 | 1 | 1992 | 0.535 | 1988 |
| Japan | Shimane 2 | BWR | Hitachi | 520 | 1 | 1988 | 0.535 | 1984 |
| Japan | Tokai | BWR | GE ET Hitachi | 1100 | 1 | 1978 | 0.385 | 1973 |
| USA | Gra Gulf 1 | BWR | General Electric | 1305 | 1 | 1982 | 0.203 | 1974 |
| USA | Hatch 2 | BWR | General Electric | 844 | 1 | 1978 | | 1972 |
| USA | Hope Creek | BWR | General Electric | 1118 | 1 | 1986 | 0.528 | 1976 |
| USA | La Salle 1 | BWR | General Electric | 1122 | 2 | 1984 | 0.410 | 1974 |
| USA | Susquehanna 1 | BWR | General Electric | 1132 | 2 | 1982 | | 1973 |
| USA | WNP-2 Hanford | BWR | General Electric | 1164 | 1 | 1984 | | 1972 |
| USA | Shoreham | BWR | General Electric | 849 | 1 | | 0.389 | 1972 |
| USA | Clinton 1 | BWR | General Electric | 985 | 1 | 1987 | 0.204 | 1975 |
| Switzerland | Leibstadt | BWR | BBC-GESTCO | 1030 | 1 | 1984 | 0.203 | 1975 |
| Taiwan | Kuosheng 1 | BWR | General Electric | 985 | 2 | 1982 | | 1974 |
| Taiwan | Lugmen | ABWR | General Electric | 1350 | 2 | 2004 | | 1999 |
| Sweden | Forsmark 3 | BWR | ABM Atom | 1155 | 1 | 1984 | 0.60 | 1977 |
| Sweden | Oskershamn 3 | BWR | ABM Atom | 1160 | 2 | 1985 | 0.60 | 1981 |
| S. Korea | Wolsong 1 | PHWR | AECL | 679 | 4 | 1983 | 0.156 | 1979 |
| Lituania | Ignalina 1 | RBMK | Minatomenergo | 1500 | 2 | 1986 | | 1978 |
| Mexico | Laguna Negra 1 | BWR | General Electric | 675 | 2 | 1988 | | 1974 |
| | | | | | | | | |

| | | | Table 1.1 (c | continued | | | | |
|----------------------|----------------|------|---------------------------------|-----------|----------------------|-------|----------|----------|
| | | | | | No. of similar units | First | Design | Start of |
| Country | Name | Type | Nuclear system supplier | Power | onsite | power | pressure | erection |
| Spain | Cofrentes | BWR | General Electric | 066 | 1 | 1984 | | 1975 |
| Romania | Cernavoda | PHWR | Atomic Energy | | | | | |
| of Canada Ltd. | 706 | - | 1996 | | 1980 | | | |
| India | Kaiga 1 | PHWR | Nuclear Power | | | | | |
| Co. of India Ltd. | 220 | - | 2000 | 0.273 | 1989 | | | |
| India | Kaiga 2 | PHWR | Nuclear PowerCo of India Ldt | 220 | 1 | 2000 | 0.273 | 1989 |
| India | Kakrapara l | PHWR | Nuclear Power | | | | | |
| Co. of India Ltd. | 220 | 7 | 1993 | 0.225 | 1985 | | | |
| India | Narora 1 | PHWR | Assoc. CanadaGe and AECL | 220 | 2 | 1991 | 0.225 | 1976 |
| India | Rajasthan 3 | PHWR | Nuclear PowerCo of India Ldt | 220 | 2 | 2000 | 0.273 | 1989 |
| India | Tarapur 3 | PHWR | Atomstrojex-port/ KWU | 500 | 2 | | 0.244 | 1998 |
| Iran | Busher | PWR | Hitachi | 1000 | 2 | | | 1995 |
| Japan | Fukushima 1-4 | BWR | Atomic Energyof Canada Ltd. | 784 | 3 | 1978 | 0.49 | 1972 |
| Japan | Fukushima 1-6 | BWR | GE and Toshiba | 1100 | ю | 1979 | 0.385 | 1973 |
| Japan | Fukushima 11-1 | BWR | Toshiba | 1100 | 4 | 1982 | 0.385 | 1975 |
| Canada | Bruce A1 | PHWR | Atomic Energy of Canada Ltd. | 904 | 3 | 1976 | | 1972 |

| | | | Table Lange Lange Line Lange Line Lange | continuad | | | | |
|----------------------------------|---|--------------------------|--|------------|----------------------|-------|----------|----------|
| | | | | | No. of similar units | First | Design | Start of |
| Country | Name | Type | Nuclear system supplier | Power | onsite | power | pressure | erection |
| Canada | Bruce B5 | PHWR | Atomic Energyof Canada Ltd. | 904 | 4 | 1984 | 0.291 | 1978 |
| Canada | Darlington | PHWR | Atomic Energyof Canada Ltd. | 935 | 4 | 1990 | 0.197 | 1982 |
| Canada | Gentilly 2 | PHWR | Atomic Energy | | | | | |
| of Canada Ltd. | 675 | - | 1983 | 0.217 | 1979 | | | |
| Canada | Pickering B5 | PHWR | Atomic Energyof Canada Ltd. | 540 | 4 | 1982 | 0.141 | 1974 |
| Canada | Point Lepreau 1 | PHWR | Atomic Energyof Canada Ltd. | 680 | 1 | 1982 | 0.104 | 1975 |
| Argentina | Emblase | PHWR | Atomic Energy of Canada Ltd. | 648 | 1 | 1983 | | 1974 |
| China | Qinshan 3 | PHWR | Atomic Energyof Canada Ltd. | 700 | 2 | | 0.224 | 1996 |
| Note: Data col Data collected | lected from Nuclear from Atomic Energy | Journals ov of Canada | er a period of 10 years ; , over a period of 10 years ; | and are pl | aced in the order | | | |

Table 1.1 (continued)

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1.3.3.2 Design Criteria

The containment is designed for a sudden rupture of one (or in some cases two) of the main pipes. Diagram of transient pressures and temperatures in different parts of the containment for two conditions at Forsmark 1. It is conservatively assumed that 5% of the cladding metal in the fuel elements reacts with water causing generation of hydrogen gas. Maximum design temperature is 180°C.

Local reactions and missile forces and jet impingement during design basis accident are specified by the supplier of nuclear systems. Table 1.2 gives the PWR system and VVER adopted in several countries. This system has been widely used in the USA, France, Japan and Germany. In the Russian state, it is with small variation, named VVER. This system is adopted in the Eastern European countries. A typical pictoral view of the Tricastin Power Station based on PWR is shown in Plate 1.14.



Plate 1.14 Tricastin power station, PWR nuclear power station (Central France)

1.4 Additional Advanced Reactor Stations

1.4.1 General Introduction

Recent events in the energy field have emphasised the need for more thoughtful uses of energy and action on securing its transformation and its distribution. The fast breeder reactor has its natural, reasonable rate of development. The Dounreay prototype fast reactor has successfully ended its useful purpose in

| | | Table | • 1.2 PWR and VVER Stations in th | ne World | | | | |
|-----------|-------------------|-------|-----------------------------------|----------|--------------|-------|----------|----------|
| | | | | | No. of | | | |
| | | | | | similar | First | Design | Start of |
| Country | Name | Type | Nuclear System Supplier | Power | units onsite | power | pressure | erection |
| JAPAN | Genkai 4 | PWR | Mitsubishi Atomic Power Indust. | 1180 | 2 | 1997 | 0.500 | 1985 |
| JAPAN | Ohi 1 | PWR | Westinghouse Electric Corp. | 1175 | 2 | 1978 | 0.540 | 1972 |
| JAPAN | Ikata 1 | PWR | Mitsubishi Atomic Power Indust. | 566 | 2 | 1977 | 0.345 | 1973 |
| JAPAN | Ikata 3 | PWR | Mitsubishi Atomic Power Indust. | 890 | 1 | 1981 | 0.389 | 1978 |
| JAPAN | Mihama 3 | PWR | Mitsubishi Atomic Power Indust. | 826 | 1 | 1976 | 0.340 | 1972 |
| ARMENIA | Medzamor 2 | VVER | Minatomenergo | 408 | 1 | 1995 | 0.200 | 1995 |
| BELGIUM | Doel 3 | PWR | Framaceco | 970 | 2 | 1982 | 0.450 | 1975 |
| BELGIUM | Tihange 2 | PWR | Framaceco | 960 | 1 | 1983 | 0.450 | 1976 |
| BELGIUM | Tihange 3 | PWR | Acecowen | 1070 | 1 | 1985 | | 1978 |
| BRAZIL | Angra 1 | PWR | Westinghouse | 657 | 1 | 1982 | | 1972 |
| BULGARIA | Kozloduy 5 | VVER | Atomenergoproekt | 1000 | 2 | 1987 | | |
| CHINA | Qinshan II-1 | PWR | CNEIC | 009 | 2 | | 0.450 | 1997 |
| CHINA | Tiawan | VVER | Atomenergoexport | 1000 | 4 | | 0.500 | 1999 |
| CZECH.REP | Dukovany | VVER | Skoda | 440 | 4 | 1985 | | 1974 |
| CZECH.REP | Temelin | VVER | | 972 | 2 | | 0.490 | 1982 |
| FINLAND | Olkiluoto (TVO) 1 | BWR | ASEA-Atom | 820 | 2 | 1978 | 0.470 | 1973 |
| FRANCE | Belleville 1 | PWR | Framatome | 1300 | 2 | 1987 | 0.520 | 1981 |
| FRANCE | Blayais 1 | PWR | Framatome | 900 | 4 | 1981 | 0.500 | 1976 |
| FRANCE | Bugey | PWR | Framatome | 900 | 4 | 1978 | 0.500 | 1971 |
| FRANCE | Cattenom 1 | PWR | Framatome | 1300 | 4 | 1986 | 0.520 | 1979 |
| FRANCE | Chinon B1 | PWR | Framatome | 900 | 4 | 1982 | 0.500 | 1977 |
| FRANCE | Chooz 1 | PWR | Framatome | 1455 | 2 | 1996 | 0.530 | 1984 |
| FRANCE | Civaux 1 | PWR | Framatome | 1455 | 1 | 1997 | 0.530 | 1991 |
| FRANCE | Civaux 2 | PWR | Framatome | 1455 | 1 | | 0.530 | 1993 |
| FRANCE | Cruas 1 | PWR | Framatome | 900 | 4 | 1980 | 0.500 | 1974 |
| FRANCE | Dampierre 1 | PWR | Framatome | 900 | 4 | 1980 | 0.500 | 1974 |

| | | | Table 1.2 (continued) | | | | | |
|---------|-------------------------|------|--------------------------|-------|--------------|-------|----------|----------|
| | | | | | No. of | | | |
| (| ; | E | - | ¢ | similar | First | Design | Start of |
| Country | Name | Type | Nuclear System Supplier | Power | units onsite | power | pressure | erection |
| FRANCE | Fessenheim | PWR | Framatome | 006 | 2 | 1979 | 0.473 | 1972 |
| FRANCE | Flamanville 1 | PWR | Framatome | 1300 | 2 | 1985 | 0.480 | 1979 |
| FRANCE | Golfech 1 | PWR | Framatome | 1300 | 2 | 1990 | 0.520 | 1983 |
| FRANCE | Gravelines 1 | PWR | Framatome | 900 | 6 | 1980 | 0.500 | 1974 |
| FRANCE | Nogent 1 | PWR | Framatome | 1300 | 2 | 1987 | 0.520 | 1981 |
| FRANCE | Paluel 1 | PWR | Framatome | 1300 | 4 | 1984 | 0.480 | 1977 |
| FRANCE | Penly 1 | PWR | Framatome | 1300 | 2 | 1990 | 0.520 | 1983 |
| FRANCE | St Alban 1 | PWR | Framatome | 1300 | 2 | 1985 | 0.480 | 1979 |
| FRANCE | St Laurent B1 | PWR | Framatome | 006 | 2 | 1983 | 0.500 | 1978 |
| FRANCE | Tricastin | PWR | Framatome | 006 | 4 | 1980 | 0.500 | 1974 |
| GERMANY | Brokdorf | PWR | KWU | 1440 | 1 | 1986 | 0.750 | 1976 |
| GERMANY | Emsland | PWR | KWU | 1363 | 1 | 1982 | 0.630 | 1982 |
| GERMANY | Grafenrheinfeld | PWR | KWU | 1345 | 1 | 1981 | | 1974 |
| GERMANY | Grohnde | PWR | KWU | 1430 | 1 | 1984 | | 1976 |
| GERMANY | Gundremmingen KRB II | BWR | SIEMENS | 1344 | 2 | 1984 | 0.430 | 1976 |
| GERMANY | Isar 1 | BWR | AEG-KWU | 907 | 1 | 1977 | | 1972 |
| GERMANY | Isar 2 | PWR | KWU | 1440 | 1 | 1988 | 0.630 | 1982 |
| GERMANY | Krummel | BWR | AEG-KWU | 1316 | 1 | 1983 | | 1974 |
| GERMANY | Mulheim Karlich | PWR | BBC-BBR | 1302 | 1 | 1986 | | 1975 |
| GERMANY | Neckar 1 | PWR | SIEM-KWU | 840 | 1 | 1976 | 0.570 | 1972 |
| GERMANY | Neckar 2 | PWR | KWU | 1365 | 1 | 1988 | 0.630 | 1982 |
| GERMANY | Philppsburg 2 | PWR | KWU | 1424 | 1 | 1984 | | 1977 |
| GERMANY | Unterweiser | PWR | SIEMENS-KWU | 1350 | 1 | 1978 | 0.580 | 1972 |
| JAPAN | Ohi 3 | PWR | Mitsubishi Atomic PoVVER | 1180 | 2 | 1992 | 0.500 | 1987 |
| | | | Indust. | | | | | |

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| | | | Table 1.2 (continued) | | | | | |
|----------|---------------|------|-------------------------------------|-------|--------------|-------|----------|----------|
| | | | | | No. of | | | |
| | | | | | similar | First | Design | Start of |
| Country | Name | Type | Nuclear System Supplier | Power | units onsite | power | pressure | erection |
| JAPAN | Sendai 1 | PWR | Mitsubishi Atomic PoVVER Indust. | 890 | 2 | 1985 | 0.325 | 1981 |
| JAPAN | Tomari 1 | PWR | Mitsubishi Atomic PoVVER Indust. | 579 | 2 | 1990 | 0.360 | 1984 |
| JAPAN | Tsuruga 2 | PWR | Mitsubishi Atomic PoVVER Indust. | 1160 | 1 | 1987 | 0.500 | 1982 |
| JAPAN | Takahama 3 | PWR | Mitsubishi Atomic PoVVER Indust. | 870 | 7 | 1984 | 0.360 | 1981 |
| PAKISTAN | Chasma | PWR | China National Nuclear Corp. | 300 | 1 | 2000 | | 1993 |
| RUSSIA | Balakovo 1 | VVER | Minatomenergo (MAE) | 1000 | 4 | 1985 | 0.490 | 1980 |
| RUSSIA | Balakovo 5 | VVER | Minatomenergo (MAE) | 1000 | 1 | | 0.490 | 1987 |
| RUSSIA | Balakovo 6 | VVER | Minatomenergo (MAE) | 1000 | 1 | | 0.490 | 1987 |
| RUSSIA | Kalinin 1 | VVER | Minatomenergo (MAE) | 1000 | 2 | 1984 | 0.455 | 1977 |
| CHINA | Daya Bay | PWR | Framatome | 985 | 2 | 1993 | 0.520 | 1985 |
| CHINA | Lingao | PWR | Framatome | 985 | 2 | | 0.520 | 1997 |
| CHINA | Qinshan 1 | PWR | Shanghai Boiler factory | 300 | 1 | 1991 | 0.360 | 1984 |
| RUSSIA | Kalinin 3 | VVER | Minatomenergo (MAE) | 1000 | 1 | | 0.490 | 1988 |
| RUSSIA | Kursk | RBMK | Minatomenergo | 1000 | 4 | 1976 | | 1972 |
| RUSSIA | Novovoronej 5 | VVER | Minatomenergo (MAE) | 1000 | 1 | 1980 | 0.455 | 1974 |
| RUSSIA | Novovoronej 6 | VVER | Minatomenergo (MAE) | 1000 | 1 | | 0.490 | 1990 |
| RUSSIA | Novovoronej 7 | VVER | Minatomenergo (MAE) | 1000 | 1 | | 0.490 | 1990 |
| RUSSIA | Rostov 1 | VVER | Minatomenergo (MAE) | 1000 | 2 | 2000 | 0.490 | 1984 |
| RUSSIA | Smolensk 1 | RBMK | Minatomenergo | 1000 | 3 | 1982 | | 1975 |
| SLOVAKIA | Bohunice 1 | VVER | Atomenergoproekt & Skoda | 430 | 4 | 1978 | | 1973 |
| SLOVAKIA | Mochovce 1 | VVER | Atomenergoproekt & Skoda | 432 | 4 | | | 1983 |
| SLOVENIA | Krsko | PWR | Westinghouse | 664 | 1 | 1981 | | 1974 |

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| e Type erg PWR 3 PWR gwant 1 PWR gwant 1 PWR 1 PWR 2 PWR 1 PWR 2 PWR 1 P | Nuclear System Supplier Framatome Westinghouse Electric Corp Framatome KHIC-ABBCE Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. KWU | Power 965 950 950 950 975 930 966 1066 | No. of similar units onsite 2 2 2 2 2 2 1 1 1 | First power 1984 1985 1986 1986 1981 | Design pressure 0.500 | Start of erection 1976 |
|--|--|--|--|--|--|---|
| e Type berg PWR 3 PWR 3 PWR ggwant 1 PWR 1 PWR 1 PWR 2 PWR 1 PWR 6llos 2 PWR hals 3 PWR hals 3 PWR hals 3 PWR hals 4 PWR hals 4 PWR hals 2 PWR hals 2 PWR hals 2 PWR hals 2 PWR hals 3 PWR hals 3 PWR hals 3 PWR | Nuclear System Supplier Framatome Westinghouse Electric Corp KHIC-ABBCE Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. KWU Westinghouse Electric Corp. | Power 965 950 950 950 975 930 966 1066 | similar units onsite 2 2 2 2 2 2 2 1 1 1 1 | First power 1984 1985 1986 1986 1981 | Design pressure 0.500 | Start of erection 1976 |
| e Type berg PWR 3 PWR 1 PWR ggwant 1 PWR 1 PWR 1 PWR 2 PWR 1 PWR 1 PWR 1 PWR 1 PWR hals 3 PWR hals 3 PWR hals 3 PWR hals 4 PWR hals 4 PWR hals 4 PWR hals 2 PWR hals 2 PWR hals 2 PWR hals 2 PWR hals 2 PWR hals 3 PWR hals 3 PWR hals 3 PWR hals 3 PWR | Nuclear System Supplier Framatome Westinghouse Electric Corp KHIC-ABBCE Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. KWU Westinghouse Electric Corp. | Power 965 950 950 950 950 975 975 975 975 975 975 975 975 975 975 | units onsite | power 1984 1985 1988 1986 1981 1981 | pressure 0.500 0.520 | erection 1976 |
| berg PWR 3 PWR gewant 1 PWR uraz 1 PWR 1 PWR 2 PWR 1 PWR 2 PWR 1 PWR 2 P | Framatome Westinghouse Electric Corp Framatome KHIC-ABBCE Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. KWU | 965 950 950 950 975 930 966 1066 | 0 000000 | 1984 1985 1988 1986 1981 | 0.500 | 1976 |
| 3PWR1PWRggwant 1PWRtraz 1PWR2PWR1PWR1PWR1PWR1PWR1PWRellos 2PWRhals 3PWRnahan 1PWRnshan 1PWRelnitsky 2VVER | Westinghouse Electric Corp Framatome KHIC-ABBCE Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. Westinghouse Electric Corp. | 950 950 975 975 975 975 966 1066 | 0 0 0 0 0 0 | 1985 1988 1986 1981 | 0.520 | |
| 1PWRggwant 1PWRuraz 1PWR2PWR1PWR1PWR1PWRellos 2PWRhals 3PWRenitsky 1VVERelnitsky 2VVER | Framatome KHIC-ABBCE Westinghouse Electric Corp. Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. Westinghouse Electric Corp. | 950 950 975 930 966 1006 | 0 0 0 0 0 | 1988 1986 1981 | 277.0 | 1979 |
| ggwant 1 PWR traz 1 PWR 2 PWR 0 1 PWR ellos 2 PWR lellos 2 PWR hals 3 PWR hals 3 PWR enitsky 1 VVER elnitsky 2 VVER | KHIC-ABBCE Westinghouse Electric Corp. Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. Westinghouse Electric Corp. | 950 975 930 966 1066 1009 | 0 0 0 0 | 1986 1981 1982 | 0.500 | 1982 |
| rraz 1 PWR 1 PWR 2 PWR 1 PWR ellos 2 PWR hals 3 PWR entisky 1 VVER elnitsky 2 VVER | Westinghouse Electric Corp. Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. Westinghouse Electric Corp. | 975 930 966 1066 1009 | 0 0 0 | 1981 1083 | 0.520 | 1980 |
| 1 PWR 2 PWR 1 PWR lellos 2 PWR hals 3 PWR cen PWR nshan 1 PWR elnitsky 2 VVER | Westinghouse Electric Corp. Westinghouse Electric Corp. KWU Westinghouse Electric Corp. Westinghouse | 930 966 1066 1009 | 0 0 | 1002 | | 1972 |
| 2 PWR 1 PWR lellos 2 PWR hals 3 PWR entities and a PWR ellitisky 1 VVER ellitisky 2 VVER | Westinghouse Electric Corp. KWU Westinghouse Electric Corp. Westinghouse | 966 1066 1009 | (| C0/1 | 0.480 | 1973 |
| o 1 PWR lellos 2 PWR hals 3 PWR cen PWR nshan 1 PWR elnitsky 1 VVER elnitsky 2 VVER | KWU Westinghouse Electric Corp. Westinghouse | 1066 1009 | | 1985 | | 1974 |
| lellos 2 PWR hals 3 PWR en 1 PWR enitsky 1 VVER enitsky 2 VVER | Westinghouse Electric Corp. Westinghouse | 1009 | c | 1988 | | 1979 |
| hals 3 PWR en nshan 1 PWR elnitsky 1 VVER elnitsky 2 VVER | Westinghouse | 210 | ſ | 1987 | | 1976 |
| en PWR ashan 1 PWR elnitsky 1 VVER elnitsky 2 VVER | | C16 | 1 | 1980 | 0.514 | 1972 |
| elnitsky 1 VVER elnitsky 2 VVER | KWU | 1020 | 1 | 1979 | 0.589 | 1973 |
| elnitsky 1 VVER elnitsky 2 VVER | Westinghouse | 915 | 2 | 1984 | | 1977 |
| elnitsky 2 VVER | Minatomenergo (MAE) | 1000 | 2 | 1987 | 0.490 | 1981 |
| | Minatomenergo (MAE) | 1000 | 1 | | 0.490 | 1985 |
| 10 I VVER | Minatomenergo (MAE) | 402 | 2 | 1980 | | 1976 |
| to 3 VVER | Minatomenergo (MAE) | 1000 | 2 | 1986 | 0.490 | 1981 |
| to 4 VVER | Minatomenergo (MAE) | 1000 | 1 | | 0.490 | 1981 |
| Ukraine 1 VVER | Minatomenergo (MAE) | 1000 | .0 | 1982 | 0.490 | 1977 |
| rnobyl 3 RBMK | Minatomenergo | 1000 | 1 | 1981 | | 1977 |
| rozhe 5 VVER | Minatomenergo (MAE) | 1000 | 9 | 1989 | 0.490 | 1985 |
| iwood 1 PWR | Westinghouse | 1175 | 2 | 1987 | 0.455 | 1975 |
| n 1 PWR | Westinghouse | 1175 | 2 | 1985 | 0.445 | 1975 |
| way-1 PWR | Westinghouse Electric Corp. | 1234 | 1 | 1984 | | 1976 |
| wba 1 PWR | Westinghouse | 1205 | 2 | 1985 | 0.204 | 1974 |
| | | | | | | |
| no 4 VVER Ukraine 1 VVER rrobyl 3 RBMK rozhe 5 VVER lwood 1 PWR n 1 PWR way-1 PWR wba 1 PWR | Minatomenergo (MAE) Minatomenergo (MAE) Minatomenergo Minatomenergo (MAE) Westinghouse Westinghouse Westinghouse Westinghouse Westinghouse | 1000 1000 1000 1175 1175 1234 1205 | 0 1 0 0 0 1 0 1 | | 1982 1981 1989 1987 1985 1985 1985 | 0.490 1982 0.490 1981 0.490 1987 0.455 1985 0.445 1984 0.445 1985 0.445 |

| | | | | | No. of | | | |
|---------|-------------------|------|-----------------------------|-------|--------------|-------|----------|----------|
| | | | | | similar | First | Design | Start of |
| Country | Name | Type | Nuclear System Supplier | Power | units onsite | power | pressure | erection |
| USA | Comanche 1 | PWR | Westinghouse Electric Corp. | 1161 | 2 | 1993 | 0.445 | 1975 |
| USA | Millstone 3 | PWR | Westinghouse | 1209 | 1 | 1986 | | 1974 |
| USA | Nine Mile Point 2 | BWR | General Electric | 1205 | 1 | 1987 | 0.411 | 1975 |
| USA | Palo Verde 1 | PWR | Combustion Engineering Co | 1307 | 3 | 1985 | 0.514 | 1976 |
| USA | Perry 1 | BWR | General Electric | 1250 | 1 | 1986 | 0.204 | 1974 |
| USA | Rover Bend 1 | BWR | General Electric | 166 | 1 | 1985 | 0.204 | 1975 |
| USA | San Onofre 2 | PWR | Combustion Engineering Co | 1127 | 2 | 1982 | 0.514 | 1974 |
| USA | Seabrook 1 | PWR | Westinghouse | 1197 | 1 | 1989 | 0.459 | 1976 |
| USA | Shearon-Harris 1 | PWR | Westinghouse Electric Corp. | 096 | 1 | 1987 | | 1974 |
| USA | South Texas | PWR | Westinghouse Electric Corp. | 1315 | 2 | 1988 | | 1975 |
| USA | St Lucie 2 | PWR | Combustion Engineering Co | 882 | 1 | 1983 | 0.376 | 1976 |
| USA | Summer 1 | PWR | Westinghouse Electric Corp. | 950 | 1 | 1982 | | 1973 |
| USA | Vogtle 1 | PWR | Westinghouse Electric Corp. | 1223 | 2 | 1987 | 0.459 | 1977 |
| NSA | Waterford 3 | PWR | Combustion Engineering Co | 1153 | 1 | 1985 | | 1972 |
| USA | Watts Bar 1 | PWR | Westinghouse Electric Corp. | 1218 | 1 | 1996 | 0.193 | 1973 |
| NSA | Wolf Creek | PWR | Westinghouse Electric Corp. | 1214 | 1 | 1985 | | 1977 |
| | | | | | | | | |

Table 1.2 (continued)

| Country | Name | Туре | Nuclear system supplies | Power (MW) | Unit | Status/ erection/ commission |
|---------|-------------------|------|--|---------------|------|------------------------------------|
| India | FBTR Kalpakkam | FR | Dept. of Atomic Energy | 15 | 1 | 1472/1985 |
| Japan | Monju | FR | Power reactor and nuclear fuel development | 280 | 1 | 1994/1985 |
| Russia | BN350 | FR | - | 150 | 1 | 1973/1969 |
| Russia | BOR360 | FR | | 60 | 1 | 1973/1970 |
| France | PHENIX | FR | EDF | 253 | 1 | 1973/1971 |
| USA | EBR II | FR | USAEC | 62.5 | 1 | 1981/1975 |
| USA | LMFBR | FR | TVA/AEC | 975 | 1 | 1981/1976 |
| Germany | KNK II | FR | | 60 | 1 | 1972/1969 |

Table 1.3 Fast Breeder Nuclear Power Plant

Note: The Indian and Japanese reactors are installed using single-walled PCPR. The minatom of Russia reported installed power of 600 MW, the Japanese 280 MW stations.

Data collected from 15 years of Nuclear Engineering of Design, Elsevier, Holland.

Scotland. PHENIX in France went critical on 21 August 1973. The large prototype reactor SNR300 developed jointly by Germany, Belgium and the Netherlands did go critical on 1 January 1979. These projects gave around 800 MW_{e} . The Italian 130 MW_t PLC reactor does give considerable experience in this type of reactor system. Table 1.3 gives a brief of these reactors. In addition, British gas-cooled reactors are mentioned and other new diversified reactors are identified which are under planning.

1.4.2 Fast Breeder Reactor

Apart from the ones mentioned regarding fast reactors, it is therefore necessary to explain some technical aspects.

The design and construction and commissioning of PFR by the UKAEA on 14 December 1973 has in brief the following features:

- Reactor contained within a concrete vault situated between ground level.
- Possibility of raising and lowering the leak jacket during various stages of reactor construction.
- An existence of support lower around top of the vault and a system for jacking the roof structure offers a correct positioning for welding the diagrid support structures and primary tank to the roof, filling the top strake in solutions and welding the leak jacket to the roof. The diagrid was proof loaded to simulate the core and neutron shield rods.
- Commissioning sequence:
- Primary circuit
 - Heat and purge and prepare sodium fill
 - Dynamic running and sodium cleanup

- Vibration tests and functional testing of charge machine
- Fuel loading
- Zero energy test
- Hot dynamic running
- Run up to power
- Secondary circuits
 - All the above
 - Hot helium leak test
 - Commission water side
 - Hydrogen detection system tests
- Turbine and ancilliaries
 - Commissioning temporary boilers
 - Runup power

1.4.2.1 Fermi I Project

The Enrico Fermi project on fast breeder reactor was formally committed on 8 August 1955. In its 17-year history, the Fermi project has made significant contributions to fast rector technology. The following reports summed up Fermi I project.

- (a) Alexanderson E.L. et al. Enrico-Fermi Atomic Power plant operating experience through 900 MW_t ANS-101, April 1967.
- (b) Duffy I.G. et al. Operating experience with major components of the Enrico-Fermi Atomic power plant. IAEA-SM-127/40, Vienna, 1970.

1.4.2.2 British Gas-Cooled System

The advanced gas-cooled reactor systems are given in Table 1.4. The reactor pressure vessels are made either in prestressed concrete pressure vessels or in double PCCV.

The high-temperature gas-cooled reactors have been installed in Europe. Typical multi-cavity vessels have been thoroughly analysed in this Chapter.

| | Table | 1.4 British sy | stem | | |
|---------------|-------------|----------------|------|-----|----------|
| Country | Name | Туре | MW | No. | Erection |
| Great Britain | Heysham | AGR | 660 | 4 | 1987 |
| Great Britain | Sizewell B | PWR | 1258 | 1 | 1995 |
| Great Britain | Tomess PT 1 | AGR | 582 | 2 | 1987 |

1.4.3 New Diversified Systems

The following new systems have been planned.

1.4.4 EU-APWR

MHI has developed the EU-APWR based on 1538 MW planned for the PS using power station units 3 and 4 for the Japan Atomic Power Company.

1.4.4.1 PBMR

China is planning to develop the world's first commercially operated pebble bed nuclear power reactor of 195 MW_e station in Shandong Province.

1.5 Regulator Guides

The following are some of the useful guides for structures and appartances in nuclear power stations:

(a) US Nuclear Regulatory Commission

| | | Issued year/ |
|---|------|--------------|
| Title | Rev. | month |
| Net positive suction head for Emergency core cooling and | | 70/11 |
| containment | | |
| Heat removal system pumps (safety guide 1) | | |
| Thermal shock to reactor pressure vessels (safety guide 2) | | 70/11 |
| Assumption used for elevating the potential radiological | | 70/11 |
| consequence of a loss-of-coolant accident for boiling water | 1 | 73/06 |
| reactors | 2 | 74/06 |
| Assumption used for elevating the potential radiological | | 70/11 |
| consequence of a loss-of-coolant accident for pressurised water | 1 | 73/06 |
| reactors | 2 | 71/03 |
| Assumption used for elevating the potential radiological | | 71/03 |
| consequence of a steam line break accident for boiling | | |
| water Reactors (safety guide 5) | | |
| Independent between redundant standby (onsite) | | 71/03 |
| power sources | | |
| and between their distribution systems (safety guide 6) | | |
| Control of combustible gas concentrations in | | 71/03 |
| containment following | 1 | 76/09 |
| a loss-of-coolant accident | 2 | 78/11 |
| Personnel selection and training | | 71/03 |
| | 1 | 75/09 |
| | 1-R | 77/05 |
| Selection, design and qualification of diesel generator units used as | | 71/03 |
| onsite electric power systems at nuclear power plants (for comment) | | 78/11 |
| Mechanical (cad weld) splices in reinforcing bars of category 1 | | 71/03 |
| concrete structures | 1 | 73/01 |
| Instrument lines penetrating primary reactor containment (safety | | 71/03 |
| guide 11) | | |

| | | Issued year/ |
|--|------|---------------|
| Title | Rev. | month |
| Supplement to safety guide 11, backfitting considerations | | 72/02 |
| Instruments for earthquakes | | 71/03 |
| - | 1 | 74/04 |
| Spent fuel storage facility design basis (for comment) | | 71/03 |
| | 1 | 75/12 |
| Reactor coolant pump flywheel integrity (for comment) | | 71/1075/08 |
| | 1 | |
| Testing of reinforcing bars for category 1 concrete structures | | 71/10 |
| | 1 | 72/12 |
| Reporting of operating information-Appendix A technical | | 71/10 |
| specifications (for comment) | 1 | 73/10 |
| | 2 | 74/09 |
| | 3 | 75/01 |
| | 4 | 75/08 |
| Protection of nuclear power plants against industrial sabotage | | 71/10 |
| | 1 | 73/06 |
| Structural acceptance test for concrete primary reactor | | 71/10 |
| containments | 1 | 72/12 |
| Non-destructive examination of primary containment liner welds | | 71/12 |
| safety Guide 19 | 1 | 72/08 |
| Comprehensive vibration assessment programme for reactor | | 71/12 |
| internals during preoperational and initial startup testing | 1 | 75/06 |
| | 2 | 76/05 |
| Measuring, elevating and reporting radioactivity in solid wastes | | 71/12 |
| and releases of radioactive materials in liquid and gaseous | 1 | 74/06 |
| effluents from light-water-cooled nuclear power plants | | |
| Periodic testing of protection system actuation functions | | 72/02 |
| (safety guide 22) | | |
| Onsite meteorological programmes (safety guide 23) | | 72/02 |
| Assumption used for elevating the potential radiological | | 72/03 |
| consequences of a pressurised water reactor gas storage tank | | |
| failure (safety guide 24) | | |
| Assumption used for elevating the potential radiological | | 72/03 |
| consequences of a fuel handing accident in fuel handling and | | |
| storage facility for boiling and pressurised water | | |
| (safety guide 25) | | |
| Quality group classifications and standards for water-, steam- and | | 72/03 |
| radioactive-waste-containing components of nuclear power plants | 1 | 74/09 |
| (for comment) | 2 | 75/06 |
| | 3 | 76/02 |
| Ultimate heat sink for nuclear power plants (for comment) | | 72/0374/0376/ |
| | 12 | 01 |
| Quality Assurance programme requirements (design and | | 72/06 |
| construction) (for comment) | 1 | 78/03 |
| Seismic design classification | | /2/06 |

1.5 Regulator Guides

| | | Issued year/ |
|---|------|--------------|
| Title | Rev. | month |
| | 1 | 73/08 |
| | 2 | 76/02 |
| | 3 | 78/09 |
| Quality assurance requirements for the installation, inspection and testing of instrumentation and electric equipment (safety guide 30) | | 72/08 |
| Control of ferrite content in stainless steel weld metal | | 72/08 |
| | 1 | 73/06 |
| | 2 | 77/05 |
| | 3 | 78/04 |
| Criteria for safety-related electric power systems for nuclear power | ••• | 72/08 |
| plants | 1 | 76/03 |
| | 2 | 77/02 |
| Quality assurance programme requirements (operation) | | 72/11 |
| | 1 | 77/02 |
| | 3 | 78/02 |
| Control of electric weld properties | | 72/12 |
| In-service inspection of ungrouted tendons in prestressed concrete | | 73/02 |
| containment structures | 1 | 74/06 |
| | 2 | 76/01 |
| Non-metallic thermal insulation for austenitic stainless steel | | 73/02 |
| Quality assurance requirements for cleaning of fluid systems and | | |
| associated components of water-cooled nuclear power plants | | 73/03 |
| Quality assurance requirements for packaging, shipping, receiving, | | 73/03 |
| storage and handling of items for water-cooled nuclear power plants | 1 | 76/10 |
| | 2 | 77/05 |
| Housekeeping requirements for water-cooled nuclear power plants | | 73/03 |
| | 1 | 76/10 |
| | 2 | 77/09 |
| Qualification test for continuous-duty motors installed inside the containment of water-cooled nuclear power plants | | 73/03 |
| Preoperational testing of redundant on-site electric power systems to verify proper load group assignments | ••• | 73/03 |
| (withdrawn – See 41 FR 11891, 3/22/.76) | | |
| Control of stainless steel weld cladding of low-alloy steel components | | 73/05 |
| Control of the use of sensitised stainless steel | | 73/05 |
| Reactor coolant pressure boundary leakage detection systems | | 73/05 |
| Protection against pipe whip inside containment | | 73/05 |
| Bypassed and inoperable status indication for nuclear power plant safety systems | •••• | 73/05 |
| Design limits and loading combinations of seismic category 1 fluid system components | | 73/05 |
| Power levels of nuclear power plants | | 73/05 |
| | 1 | 73/12 |

| | | Issued year/ |
|---|-------|---------------|
| Title | Rev. | month |
| Control of preheat temperature for welding of low-llloy steel | | 73/05 |
| (withdrawn - see 40 FR 30510, 7/21/75) | | |
| Design, testing and maintenance criteria for post-accident | | |
| engineered- | | 73/06 |
| safety-feature atmosphere cleanup system, air filtration and | 1 | 76/07 |
| adsorption units of light-water-cooled nuclear power plants | 2 | 78/03 |
| Application of the single-failure criterion to nuclear power plant protection systems | | 73/06 |
| Quality assurance requirements for protective coating Applied to water-cooled nuclear power plants | | 73/06 |
| Concrete placement in category 1 structures | | 73/06 |
| Maintenance of water purity in boiling water reactor (for | | 73/06 |
| comment) | 1 | 78/07 |
| Design limits and loading combinations for metal primary reactor containment system components | | 73/06 |
| Qualification of nuclear power plant inspection, examination and testing personnel | | 73/08 |
| Design basis floods for nuclear power plants | | 73/0876/0477/ |
| | 12 | 08 |
| Design response spectra for seismic design of nuclear power plants | | 73/10 |
| | 1 | 73/12 |
| Damping values for seismic design of nuclear power plants | | 73/10 |
| Manual initiation of protective actions | | 73/10 |
| Electric penetration assemblies in containment structures for | | 73/10 |
| light-water-cooled nuclear power plants | 1 | 77/05 |
| | 2 | 78/07 |
| Quality assurance requirements for the design of nuclear power | | 73/10 |
| Plants | 1 | 75/02 |
| | 2 | 76/06 |
| Material and inspections for reactor vessel closure study | - | 73/10 |
| (withdrawn – see 42 FR 54478, $10/06/77$ | | , 0, 10 |
| Installation of overpressure protection devices | | 73/10 |
| Initial test programmes for water-cooled reactor power plants | | 73/11 |
| findur test programmes for water cooled reactor power plants | 1 | 77/01 |
| | 2 | 78/08 |
| Preoperational and initial startup testing of feedwater and | 2 | /0/00 |
| condensate systems for boiling water reactor power plants | | 75/12 |
| condensate systems for bonning water reactor power plants | 1 | 77/01 |
| Initial startup test programme to demonstrate remote shutdown | 1 | 77/01 |
| comphility for water cooled nuclear power plants | 1 | 78/08 |
| Standard format and content of sofety analysis reports for nuclear | 1 | 78/08 |
| nower plants | 1 | 72/02 |
| power plants | 1 | 72/10 |
| | 2 | 79/11 |
| W-14-man-116-stime for some of 1' is 1 in 11'1's | 3 | / 0/ 1 1 |
| weider qualification for areas of limited accessibility | | 15/12 |

1.5 Regulator Guides

| Title | Rev | Issued year/ |
|---|-------|--------------|
| Spray pond nining made from fibrealass-reinforced thermosetting | 10011 | 73/12 |
| resin | 1 | 78/01 |
| | 2 | 78/11 |
| Qualification test of electric valve operators installed inside the | - | , 0/11 |
| containment of nuclear power plant | | 74/01 |
| Quality assurance terms and definitions | | 74/02 |
| Physical independence of electrical system | | 74/02 |
| | 1 | 75/01 |
| | 2 | 78/09 |
| Design basis tornado for nuclear power plants | - | 74/04 |
| Assumptions used for evaluating a control bed ejection accident | | , ., |
| for pressurised water reactors | | 74/05 |
| Assumptions for evaluating habitability of a nuclear power plant | | , ,, , , , |
| control room during a postulated hazardous chemical release | | 74/06 |
| Preoperational testing Of emergency core cooling system of | | 74/06 |
| Pressurised water reactor | 1 | 75/09 |
| Preoperational testing of instrument air system | | 74/06 |
| Shared emergency and shutdown electric systems for multi-unit | | 74/06 |
| nuclear power plants | 1 | 75/01 |
| Sumps of emergency core cooling and containment spray systems | | 74/06 |
| In-service inspection of pressurised water reactor steam generator | | 74/06 |
| tubes | 1 | 75/07 |
| Code case acceptability – ASME section III design and fabrication | | 74/06 |
| | | 76/03 |
| Protection against low-trajectory turbine missiles | 1 | 77/07 |
| Quality assurance requirements for installation, inspection and | | 76/07 |
| testing of mechanical equipments and systems | O-R | 75/05 |
| | | 76/07 |
| Tornado design classification | 1 | 78/04 |
| Periodic testing of electrical power and protection systems | | 76/06 |
| | 1 | 77/11 |
| | 2 | 78/06 |
| (withdrawn - see 42 FR 33387, 6/30/77) | | |
| Fire protection guidelines for nuclear power plants (for comment) | | 76/06 |
| | 1 | 77/11 |
| Bases for plugging degraded PWR steam generator tubes (for comment) | | 76/08 |
| Development of floor design response spectra for seismic design of | | 76/10 |
| floor-supported equipment or components | 1 | 77/07 |
| Quality assurance requirements for control of procurement of items | | 76/10 |
| and service for nuclear power plants | 1 | 77/07 |
| Overhead crane handling for nuclear power plants (for comment) | | 76/02 |
| | | 75/11 |
| Instrument set points | 1 | 76/11 |
| Thermal overload protection for electric motors on motor-operated | | 75/11 |

| | | Issued year/ |
|---|------|--------------|
| Title | Rev. | month |
| valves | 1 | 77/03 |
| Qualifications for cement grouting for prestressing tendons in | | 75/11 |
| containment structures | 1 | 77/02 |
| Periodic testing of diesel generator units used as onsite electric | | 76/08 |
| power systems at nuclear power plants | 1 | 77/08 |
| Calculation of annual doses to man from routine releases of reactor | | 76/03 |
| effluents for the purpose of evaluating compliance with 10 CFR Part 50, Appendix 1 | 1 | 77/10 |
| Cost-benefit analysis for radwaste systems for light-water- cooled nuclear power reactors (for comment) | ••• | 76/03 |
| Methods of estimating atmospheric transport and dispersion of | | 76/03 |
| gaseous effluents in routine releases rrom light-water-cooled reactors | 1 | 77/07 |
| Calculation of releases of radioactive materials in gaseous and | | 76/04 |
| liquid effluents rrom light-water-cooled power reactors | 1 | 77/05 |
| Estimating aquatic dispersion of effluents from accidental and | | 76/05 |
| routine reactor releases for the purpose of implementing Appendix 1 | 1 | 77/04 |
| Guidance on being operator at the controls of a nuclear power plant | | 76/02 |
| | 1 | 76/01 |
| Service limits and loading combinations for class 1 linear-type | | 76/11 |
| component supports | 1 | 78/01 |
| Physical models for design and operation of hydraulic structures | | 77/03 |
| and systems for nuclear power plants | 1 | 78/10 |
| An acceptable model and related statistical methods for the analysis | | 77/03 |
| of fuel densification | 1 | 78/03 |
| Inspection of water-cooled structures associated with nuclear | | 77/04 |
| power plants | 1 | 78/03 |
| Installation design and installation of large lead storage batteries for | | 77/04 |
| nuclear power plants | 1 | 78/10 |
| Maintenance, testing and replacement of large lead storage | | 77/04 |
| batteries for nuclear power plants | 1 | 78/02 |
| Service limits and loading combinations for class 1 plate-and-shell- | | 77/07 |
| type component supports | 1 | 78/10 |
| Qualification test of electrical cables, field splices and connection | | 77/08 |
| for light-water-cooled nuclear water plants (for comment) | | 77/09 |
| Site investigations for foundations of nuclear power plant (for comment) | | 77/09 |
| Loose-part detection programme for the primary system of light- water- | | 77/09 |
| cooled reactors (for comment) | | |
| Medical certification and monitoring of personnel requiring | | 77/09 |
| operator licences (for comment) | | |
| Normal water level and dischcarge at nuclear power plant (for comment) | | 77/09 |

1.5 Regulator Guides

| | | Issued year/ |
|---|------|--------------|
| Title | Rev. | month |
| Material for concrete containments | | 77/11 |
| | 1 | 78/10 |
| Fuel-oil systems are standby diesel generator (for comment) | | 78/01 |
| Laboratory investigations of soils for engineering analysis and | | 78/04 |
| design of nuclear power plant (for comment) | | |
| Guidance for residual heat removal (for comment) | | 78/05 |
| Design, testing and maintenance criteria for national ventilation | | 78/03 |
| Exhaust system air filtration and adsoprption units of light | | |
| water-cooled nuclear power plants (for comment) | | |
| Containment isolation provisions for fluid systems (for comment) | | 78/04 |
| Safety-related concrete structures for nuclear power plants (other | | 78/04 |
| than reactor vessels and containments) (for comment) | | |
| Design guidance for radioactive waste management systems, structures and components installed in light-water-cooled nuclear | | 78/07 |
| power plants (for comment) | | |

(continued)

(b) American Nuclear Society, Nuclear Standard Projects of Prime Interest to Structural Engineers

| ANS 2 | Site elevation |
|----------|--|
| ANS 2.1 | Guidelines for determining the vibratory found motions for the design earthquake for nuclear facilities |
| ANS 2.3 | Standards for estimating tornadoes, hurricanes and other extreme wind parameters at power reactor sites |
| ANS 2.4 | Guidelines for determining tsunami criteria for power reactor sites |
| ANS 2.7 | Guidelines for assessing capability for surface faulting at nuclear power reactor sites |
| ANS 2.8 | Standards for determining design basis flooding at power reactor sites |
| ANS 2.10 | Guidelines for retrieval, review, processing and elevation of records obtained from seismic instrumentations |
| ANS 2.11 | Guidelines for elevating site-related geotechnical parameters at power reactor sites |
| ANS 2.12 | Guidelines for combining natural and external man-made hazards at power reactor sites |
| ANS 2.14 | Determination of the shape of the response spectra for use in nuclearFacilities design |
| ANS 2.19 | Guidelines for elevating site related parameters for independent spent fuel storage facilities |

| ANS 4 | Criteria, control and dynamics |
|----------|--|
| ANS 4.1 | Design basis criteria for safety system in nuclear power generating stations |
| ANS 58.1 | Plant design against missiles |
| ANS 58.2 | Design basis for protection of nuclear power plants against effects of postulated pipe rupture |
| ANS 58.5 | Probabilistic risk assessment |
| | |

ANS 51 Pressurized water reactor

| ANS 51.1 | Nuclear safety criteria for the design of stationary pressurized water |
|----------|--|
| | reactor plants |
| ANS 51.7 | Single failure criteria for PWR fluid systems |

| NS 52 | Boiling water reactor | |
|-------|------------------------------|---|
| | | Î |

| ANS 52.1 | Nuclear safety criteria for the design of stationary boiling water reactor plants |
|----------|---|
| ANS 58.9 | LWR single failure criteria |

| ANS 53 | High-cooled gas-cooled reactor management committee |
|-----------|--|
| ANS 53.1 | Nuclear safety criteria for the design of stationary gas cooled reactor plants |
| ANS 53.6 | Gas-cooled reactor plant containment system |
| ANS 53.21 | Gas-cooled reactor plant secondary coolant systems |

| ANS 54 | Liquid metal fast breeder reactor |
|-----------|---|
| ANS 54.1 | LMFBR general design criteria |
| ANS 543 | Principal design criteria for LMFBR containments |
| ANS 54.6 | LMFBR safety classification and related requirements |
| ANS 54.10 | Risk limit guidelines for LMFBR design |
| ANS 54.11 | application of risk limit guidelines for LMFBR design |
| ANS 54.12 | Event categorisation guidelines for LMFBR design |

| ANS 55 | Fuel and radwaste |
|----------|---|
| ANS 57.5 | Away from reactor's spent dual-storage facilities |

| ANS 56 | Containment |
|----------|---|
| ANS 56.3 | Overpressure protection of low-pressure system connected to the reactor |
| | coolant pressure boundary |
| ANS 54.6 | Pressure/temperature transient analysis for LWR containments |
| ANS 56.8 | Reactor containment leakage testing requirements |
| ANS 56.9 | Environmental envelopes to be considered in safety-related equipment |

Subsections NCA-NG, boiler and pressure vessel code section III, division I–nuclear power plant components

Boiler and pressure vessel code section III, division 2–subsection CB and CC concrete reactor vessels and containment

Section XI boiler and pressure vessel code-fuels for inservice inspection of nuclear power plant components

- N626.3-1978 Qualification and duties of personnel engaged in ASME boiler and pressure vessel code section III divisions 1 and 2 certifying activities
- N626.0-1974 Qualifications and duties for authorised nuclear Inspection
- N626.1-1975 Qualifications and duties for authorised inservice Inspection
- N626.2-1976 Qualifications and duties for authorised nuclear inspection (concrete)
- N45.2/N45.2-1977 Quality assurance programme requirements for nuclear facilities QA-76-2
- N45.2.5-1978 Supplementary Quality assurance requirements for installation, inspection and testing of structural concrete and structural steel, sails and foundations during the constructional phase of nuclear power plant QA-76-5
- N45.2.6-1973 Qualifications of inspection, examination and testing personnel for the construction phase of nuclear power plants QA-76-6
- N45.2.10-1973 Quality assurance Terms and definitions QA-76-10
- N45.2.11-1974 Quality assurance requirements for the design of nuclear power plants QA-76-11
- N45.2.20 Supplementary quality assurance requirements for subsurface investigation prior to construction phase of nuclear power plant

1.6 Boiling Water Reactors (BWR), Pressurised Heavy Water Reactor (PHWR) and Pressurised Water Reactor (PWR)

Since the publication of this book, many reactors of specific systems would have been planned and constructed throughout the world. Every offer has been made for the benefit of the readers under BWR, PHWR and PWR. They are constructed facilities.

Tables 1.1 and 1.2 give a list of well-known nuclear power stations. For others references can be made to various journals in the field of nuclear facilities.

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- 23. UKAEA Private Communications on British Nuclear Power Stations: Winfirth, 1984.
- 24. TNPG Group. Design of nuclear power stations belonging to TNPG consortium inclusive of Mccalpine Engineering 1979.
- 25. NRC list of regulatory guides related to nuclear power stations listed below and other guides:
- 26. The following NRC Regulatory guides apply in particular to containment structural design and construction:
- 27. Regulatory Guide 1.10—Mechanical (Cadweld) Splices in Reinforcing Bars of Category I Concrete Structures.
- 28. Regulatory Guide 1.15—Testing of Reinforcing Bars for Category I Concrete Structures.
- 29. Regulatory Guide 1.18—Structural Acceptance Test for Concrete Primary Reactor Containments.
- 30. Regulatory Guide 1.19—Non-destructive Examination of Primary Containment Liner Welds.
- 31. Regulatory Guide 1.29—Seismic Design Classification.

- 32. Regulatory Guide 1.35—In-service Inspection of Ungrouted Tendons in Prestressed Concrete Containment Structures.
- 33. Regulatory Guide 1 .46—Protection Against Pipe Whip Inside Containment.
- 34. Regulatory Guide 1.54—Quality Assurance Requirements for Protective Coatings Applied to Water-Cooled Nuclear Power Plants.
- 35. Regulatory Guide 1.55—Concrete Placement in Category I Structures.
- 36. Regulatory Guide 1.57—Design Limits and Loading Combinations for Metal
- 37. Primary Reactor Containment System Components.
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Chapter 2 Loads and Material Properties for Nuclear Facilities – A General Survey

2.1 Introduction

The probable failure assessment of structures for nuclear power facilities has bearings on the choice and postulation of the loads and load combinations, since the exact magnitude of the loads encountered in nuclear power plant design cannot be easily predicted. The loads are normally treated as random variables. These loads are generally defined in terms of probability of strength in different components/elements of structures for a nuclear facility. Together with the strength of characteristics of elements, it would be possible to determine the probability of the structure being able to perform the functions for which it has been designed. For obtaining reliable results a proper accounting of uncertainties practically at every stage of stress determination is necessary. The stress determination is the end product of

- (a) the analysis and prediction of postulated even loads;
- (b) the probability distribution of different variables involved causing the loads to occur. One form is the statistical sampling technique. The data and probability distribution will lead to the load to be considered.

In addition to the two load levels considered in conventional design, nuclear facilities are typically designed for third load level, termed the extreme load. Extreme loads include such natural phenomena as the maximum earthquake potential for a site considering regional and local geology, seismology, local foundation conditions, tornado wind and associated air-borne missile loads. It also includes postulated design basis accident loads consisting of high-energy system rupture that results in pipe break reaction and impingement loads, pipe whip and associated accident-generated missiles and pressurisation of building components, flooding and high thermal transients.

In the USA structures for nuclear facilities are designed for service load conditions. Three methods are recommended such as working stress design (WSD), factor load deign (FLD) and factor load reduction design (FLRD). In Europe the limit state design (LSD) is generally recommended using partial safety factors for materials and loads or actions. Where service load design parameters and material strength data for nuclear facilities are not given or
| Loads or stresses | Design load or range of actions | Notation |
|--|--|--------------------|
| Dead load | | D |
| Reinforced/prestressed Concrete | $6.7 - 7.5 kN/m^2$ | dead load |
| Structural steel | $24 \mathrm{kN/m}$ | |
| Structural aluminium | | |
| Structural wood | Specified, ANSI A59 1 100 year interval | TTT |
| 1. S-snow load | specified: AINSI A38.1 100-year interval | L,LL Live or |
| | BS6399 Part 2 (see text table in this chapter) | imposed or |
| II Construction | $1.73 \text{ kN}/\text{m}^2$ | action |
| II. Construction | 1.75 kiv/m | P |
| IV Earth pressure (lateral) | 0.91 KIN/III | D F |
| (a) Active (b) Passive (c) At rest Foundation below grade | $3.14 - 18.84 \text{ kN/m}^2/\text{m}$ $3.14 - 70.65 \text{ kN/m}^2/\text{m}$ $6.28 - 23.55 \text{ kN/m}^2/\text{m}$ | Lp |
| V. Piping equipment reaction | Depends on the piping analysis \rightarrow variable | R _t |
| VI. Hatch for containment equipment | $67 kN/m^2$ | $H_{\rm e}$ |
| (a) Uniform load assumed | 2000 kN | |
| (b) Concentrated load | | |
| moving type | | $H_{\rm p}$ |
| <i>Note</i> : Not concurrent with uniform lived load | | |
| (c) Personnel hatch | $67 \mathrm{kN/m^2}$ | |
| uniform load moving type | 44.5 kN | |
| VII. Linear for concrete containment | | |
| (a) Concentrated load | 6.67 kN | |
| (b) Line load | 2.2 kN/m | |
| (c) Uniform load | $25 \mathrm{kN/m^2}$ | |
| (a) Reactor building operating deck | $1675 kN/m^2$ | |
| (b) Stairs, passage and | $67 \mathrm{kN/m^2}(\mathrm{uniform})$ | |
| escalator/moving walks | Plus concentrated from manufacturer B | |
| IX. Wind load | $F_{\rm w} = q_{\rm ref}.c_{\rm e}(z_{\rm e}).c_{\rm d}.c_{\rm fi}(A_{\rm ref})$ | W or $F_{\rm w}$ |
| | where | P |
| (a) Euro code and BS6399 | $z_{\rm e}$ height above ground | |
| | $q_{\rm ref}$ mean wind velocity pressure | |
| | $c_{\rm f}$ derived force coefficient | |
| | $c_{\rm e}$ exposure coefficient; $c_{\rm d}$ dynamic factor | |

Table 2.1 Service load parameters

2.1 Introduction

| | Table 2.1 (continued) | |
|---|--|---------------------------|
| Loads or stresses | Design load or range of actions | Notation |
| (b) Based on BS6399 | $c_{\rm fi}$ force coefficient $A_{\rm ref}$ reference area of $c_{\rm f}$ $v_{\rm ref} = c_{\rm DIR}.c_{\rm TEM}.c_{\rm ALT}.v_{\rm refo}$ $v_{\rm refo}$ basic value of reference wind velocity $c_{\rm DIR}$ directional factor taken generally as 1.0 $c_{\rm TEM}$ seasonal factor taken generally as 1.0 $c_{\rm ALT}$ altitude factor taken generally as 1.0 $c_{\rm ALT}$ altitude factor taken to be 1.0 unless specified $q_{\rm ref} =$ wind mean velocity pressure $Xv_{\rm ref} = Fw$ $V_{\rm s} =$ site velocity $= V_{\rm o}S_{\rm a}S_{\rm d}S_{\rm s}S_{\rm p}$ $V_{\rm b} =$ basic wind speed $\rightarrow v_{\rm refo}$ $S_{\rm a} =$ altitude factor $\rightarrow c_{\rm ALT}$ $S_{\rm d} =$ Direction factor $\rightarrow c_{\rm DIR} = 1$ $S_{\rm s} =$ seasonal factor $\rightarrow c_{\rm TEM} = 1$ $S_{\rm p} =$ probability factor $= 1$ $q =$ wind dynamic pressure $= kV_{\rm s}^2$ where $k = 0.613$ $V_{\rm e} = V_{\rm s} \times V_{\rm p}$ - terrain factor Example for $V_{\rm b} = 45$ m/s; $s_1 = 1$; $s_2 = 0.83$ | |
| P = net wind load on the surface | Solution based on BS 6399 $V_b = V_b S_a S_d S_s S_p;$ $V_b = basic wind speed = 23.5 m/s$ $S_a = 1 + 0.001 \times 100 = 1.1$ $S_p = 1.0$ $S_s = 0.62$ $S_p = 1.0$ $V_s = 16.03 m/s$ $V_e = SV_s S_b$ $S_b = S_c T_c [1 + (g_t S_t T_y) + S_h]$ $= 1.08(0.863)[1 + (2.52 \times 1.71 \times 1.38) + 0]$ = 1.486 $V_e = 16.03 \times 1.486 = 23.82 m/s$ q = dynamic pressure $= 0.613(23.83)^2 = 348 N/m^2$ where $S_c = fetch factor$ | |
| P = pA_{ref} P = net pressure across the surface (c) American codes | $S_{\rm h}$ = topography factor $S_{\rm t}$ = turbulence factor $g_{\rm f}$ = gust factor $T_{\rm y}$ = Turbulant adjust factor $T_{\rm c}$ = fetch factor for adjustment ANSI A58.1 for exposure C Fig. 2 of the code Load based on 100-year recurrence wind, speed with gust factor and wind profile distribution | P _{cont} . To |
| X. Containments Internal Pressure | $p \geq 345 \mathrm{kN/m^2}$ for PWR | |

| | Table 2.1 (continued) | | |
|---|--|----------|--|
| Loads or stresses | Design load or range of actions | Notation | |
| XI. Operating thermal load | | | |
| (a) Thermal gradients through the wall of containment | -11.2 (outside) + 6.672°C (inside) +5.5 (outside) + 6.672°C (inside) | | |
| (b) Range of ambient temperatures at placement of concrete in containment | 22.24 $< t < 50^{\circ}$ C | | |
| (c) Thermal gradient through reactor coolant compartment walls (d) Buses of empirical | ±16.7°C gradient | V | |
| (d) Range of ambient temperatures at placement of concrete (e) Thermal gradients through spent fuel pit walls | 55.6°C $< t < 6.7$ °C 6.67°C max.mean temperature 4.5°C min.mean temperature -11.2 (outside) + 100°C (inside) | | |
| XII. Resulting from the internal drop in containment (load) | $0.13 kN/m^2$ | | |
| XIII. Internal pressure for advanced cooled reactor vessels | \geq 6900 kN/m ² | | |
| XIV. Combination of Actions and Load Factors at the ultimate state (a) Permanent + variable (b) Permanent + wind + variable (c) Permanent + variable | $\begin{array}{cccc} G_{\rm k} & Q_{\rm k} & W \mbox{ or } W_{\rm k} \\ 1.0 & 0 & 1.5 \\ 1.0 & 0 & 1.5 \\ 1.0 & 0 & 1.5 \\ 1.4 & 1.5 \\ 1.4 & 0 & 1.5 \end{array}$ | | |
| (d) Permanent + wind XV. Prestressed concrete reactor pressure vessel Load combinations for elastic/work analysis | Loadings Case 1 Prestress and ambient temperature Case 2 Prestress $1.15 \times \text{design pressure} +$ ambient temperature Case 3* Prestress + design pressure + temperature Case 4* Overload (prestress + increasing pressure + temperature) | | |
| $P' = P_0(\text{transfer force}) - \alpha$ $\infty = \text{Losses in tendons}$ $P_o = (\text{transfer force})$ $F_{\text{rdu}} = P$ | * Short- and long-term conditions apply $= \bar{\alpha} f_{ck} \left[\frac{A_{cl}^{0.5}}{A_{co}} \right] \le 2 f_{ck}$ $\bar{\alpha}$ = depending upon adopted system range 0.67 - 0.85 A_{cl} = loaded area of the anchorage plate A_{co} = Anchorage area of the concrete block or block of material | | |

 Table 2.1 (continued)

 Table 2.2
 Concrete stresses based on American and European codes

| 1.Concrete stresses sased on ACI 359 $f'_c, f_{\rm ck}$ Cylindrical Strength(a) Membrane $0.35f'_c$ Strength(b) Membrane $0.45f'_c$ Strength(c) Membrane $0.45f'_c$ Strength(a) Membrane $0.45f'_c$ Strength(b) Membrane $0.45f'_c$ Strength(c) Membrane $0.45f'_c$ Strength(d) Membrane $0.45f'_c$ Strength(e) Membrane $0.45f'_c$ Strength(f) Membrane $0.30f'_c$ Strength(g) Membrane $0.30f'_c$ Strength(g) Membrane $0.45f'_c$ Strength(h) Membrane $0.45f'_c$ Strength(h) Membrane $0.30f'_c$ Strength(h) Membrane $0.30f'_c$ Strength(h) Membrane $0.45f'_c$ Strength(h) Membrane $0.30f'_c$ Strength <t< th=""><th>Stresses</th><th>Design stresses under range of actions</th><th>Notation</th></t<> | Stresses | Design stresses under range of actions | Notation |
|--|---|---|--------------------------|
| ACI 359Cylindrical StrengthContainment-primary0.35f'c(a) Membrane0.35f'c(b) Membrane plus bending0.45f'c(concrete (after losses)0.60f'cContainment-primary0.30f'c(a) Membrane0.45f'c(b) Membrane plus bending0.60f'cContainment-primary0.30f'c(a) Membrane0.45f'c(b) Membrane0.45f'c(concrete material properties0.45f'cfac, σ _w = minimum cub-41.34 kN/mm²Strength of conceret at 280.43 kN/mm²days-41.34 kN/mm²f _x = cylindrical strength-0.66σ _{cu} q ₁ = tensile strength+0.1σ _{cu} E = elastic modulus+41.4 kN/mm²E _p = plastic modulus+0.476Eε _{ac} = shrinkage strain0.0035v = Poisson ratio0.18x _T = coefficient of linear8.0 µM/m°Cthermal conductivity1.75 W/m°Ca' = coefficient of0.65,0.68, 0.87,0.87aggregates | 1. Concrete stresses sased on | | $f'_{\rm c}, f_{\rm ck}$ |
| Containment-primaryStrength(a) Membrane $0.35f'_c$ (b) Membrane plus bending $0.45f'_c$ (containment-secondary $0.45f'_c$ (a) Membrane $0.45f'_c$ (b) Membrane plus bending $0.60f'_c$ Containment-secondary $0.30f'_c$ (a) Membrane $0.45f'_c$ (b) Membrane plus bending $0.45f'_c$ Containment-secondary $0.30f'_c$ $0.45f'_c$ $0.45f'_c$ 2. Euro code 2 $0.45f'_c$ Concrete material properties $0.45f'_c$ $f_{kt}, \sigma_u = minimum cube-41.34 \text{ kN/mm^2}Strength of concerte at 28daysf_r = resplic modulus+0.1\sigma_{cu}E = clasic modulus+0.476Ee_{cu} = ultimate strains0.0035v = Poisson ratio0.18x_{T} = coefficient of linear8.0 \ \mu M/m^2Cthermal expansion4516 \ MN/mm^2(50\omega) \text{ or } 750E = clastic modulus4400 \ (25\omega) \text{ or } 725e_{ct} = shrinkage strain200 \times 10^{-6}Concrete thermal expansion500 \ N/mm^2f_r = coefficient of linear500 \ N/mm^2e_{rt} = coefficient of linear500 \ N/mm^2f_r = \sigma_r = yield strength4516 \ MN/mm^2f_r = \sigma_r = yield strength4516 \ MN/mm^2f_r = coefficient of linear500 \ N/mm^2r_r = coefficient of linear500 \ N/mm^2r_r = coefficient of linear3.4 \times 10^6 \ N/mm^2r_r = coefficient of linear500 \ N/mm^2r_r = coefficient of$ | ACI 359 | | Cylindrical |
| (a) Membrane 0.35 f'_c (b) Membrane plus bending 0.45 f'_c (containment-secondary (a) Membrane plus bending 0.60 f'_c Containment-serinary (a) Membrane plus bending 0.60 f'_c Containment-secondary 0.30 f'_c (b) Membrane plus bending 0.45 f'_c Containment-secondary 0.30 f'_c (c) Membrane plus bending 0.45 f'_c 2. Euro code 2 Concrete material properties $f_{ck} = \bigcirc lintical strength 25 - 60 N/mm^290 > N/mm^2$ $f_{ck} = \bigcirc lintical strength -0.66\sigma_{cu}q_i = tensile strength -0.16\sigma_{cu}q_i = tensile strength -0.16\sigma_{cu}q_i = tensile strength -0.16\sigma_{cu}q_i = tensile strength -0.18z_r = coefficient of linear 8.0 \muM/m°Cthermal conductivity 1.75 W/m°C 0.750E_r = lastic modulus 4400 (25\omega) or 750E_r = coefficient of linear 8.0 (N/mm^2)f_{a} = coefficient of linear 0.18 = 20 (N/mm^2)g_i = \sigma_y = yield strength 4516 MN/mm^2 (50\omega) or 750E_r = lastic modulus 4400 (25\omega) or 750E_r = coefficient of linear 0.1E = 20 (N/mm^2)r_i = coefficient of linear 3.4 × 10^5 (N/mm^2)f_x = coefficient of linear 3.4 × 10^5 (N/mm^2)$ | Containment-primary | | Strength |
| (b) Membrane plus bending $0.45f'_{c}$ (a) Membrane $0.45f'_{c}$ (b) Membrane plus bending $0.60f'_{c}$ concrete (after losses) Containments-primary (a) Membrane (b) Membrane plus bending Containment-secondary $0.30f'_{c}$ (containment-secondary $0.30f'_{c}$ Contrainment-secondary $0.30f'_{c}$ Contrainment-secondary $0.30f'_{c}$ Contrainment-secondary $0.30f'_{c}$ Contrainment-secondary $0.30f'_{c}$ Contrainment-secondary $0.30f'_{c}$ Contrainment-secondary $0.30f'_{c}$ Contrainment-secondary $0.45f'_{c}$ 2. Euro code 2 Concrete material properties $f_{a} \in \text{cylindrical strength}$ $f_{a} \in \text{cylindrical strength}$ $f_{a} = \text{coefficient of linear}$ $f_{a} = \text{coefficient of linear}$ $f_{a} = \text{cylindrical strength}$ $f_{a} = \text{cylindrical strength}$ $f_{a} = \text{characteristic strength}$ $f_{a} = \text{characteristic strength}$ $f_{a} = \text{characteristic strength}$ $f_{b} = \text{characteristic strength}$ $f_{b} = \text{characteristic strength}$ $f_{a} = \text{coefficient of linear}$ $f_{a} =$ | (a) Membrane | $0.35f'_{\rm c}$ | |
| containment-secondary $0.45f'_{c}$ (a) Membrane $0.45f'_{c}$ (b) Membrane plus bending $0.60f'_{c}$ <i>Containments-primary</i> $0.30f'_{c}$ (a) Membrane $0.30f'_{c}$ (b) Membrane $0.30f'_{c}$ (c) Membrane $0.30f'_{c}$ (d) Membrane $0.45f'_{c}$ 2. Euro code 2 $0.45f'_{c}$ <i>Concrete material properties</i> $f_{c}, \sigma_{u} = \mininum cubef_{ck}, \sigma_{u} = \mininum cube-41.34 \text{ kN/mm^2}Strength of concrete at 28daysf_{q}, \sigma_{u} = pinimum cube-41.34 \text{ kN/mm^2}F_{p} = plastic modulus+41.4 \text{ kN/mm^2}E_{p} = plastic modulus+0.1\sigma_{cu}E = elastic modulus+0.1\sigma_{cu}\pi_{l} = conflicient of linear0.035v = Poisson ratio0.18w_{l} = conflicient of linear0.65, 0.68, 0.87, 0.87a_{g} argegates200 \times 10^{-6}Conventional steel7i = \sigma_{y} = yield strength\overline{\gamma} = \sigma_{y} = yield strength4516 \text{ MN/mm^2(50\omega) \text{ or } 750E = elastic modulus200 \times 10^{-6}Conventional steel7i = \sigma_{y} = yield strength\overline{\gamma} = \sigma_{y} = yield strength500 \text{ N/mm^2}Iuner12 \text{ mm} + 10\%\tau_{z} = coefficient of linear0.1E = 20 \text{ kN/mm^2}\overline{\gamma} = \sigma_{y} = yield strength25 \text{ mm up to 25 \text{ m}\overline{\gamma} = \sigma_{y} = yield strength3.4 \times 10^{5} \text{ kN/mm^2}\overline{\gamma} = \sigma_{y} = yield strength25 \text{ mm up to 25 \text{ m}\overline{\gamma} = coefficient of linear$ | (b) Membrane plus bending | $0.45f'_{\rm c}$ | |
| (a) Membrane 0.45 f'_{c} (b) Membrane plus bending 0.60 f'_{c} Containments-primary (a) Membrane (b) Membrane plus bending Containment-secondary 0.30 f'_{c} (b) Membrane plus bending Containment-secondary 0.30 f'_{c} (c) Membrane plus bending Containment-secondary 0.30 f'_{c} (c) Membrane plus bending Concrete material properties $f_{ck} = \sigma_{cl}$ minimum cube -41.34 kN/mm ² Strength of conceret at 28 days $f_{cs}, \sigma_{s} = minimum cube -41.34 kN/mm2 E = elastic modulus +0.1\sigma_{cu}E = elastic modulus +0.476E\varepsilon_{cu} = ultimate strains 0.0035v = Poisson ratio 0.18w_{T} = coefficient of linear 8.0 \muM/m°Cthermal expansionK = thermal conductivity 1.75 W/m°C a a = coefficient of 10 extremation 4400 (25a) or 750E = elastic modulus 200 \times 10^{-6}Conventional steel\overline{\gamma} = \sigma_{y} = yield strength 500 N/mm2 x_{r} = coefficient of linear 0.1E = 20 kN/mm2 f_{y} = characteristic strength 500 N/mm2 f_{y} = \sigma_{y} = yield strength 500 N/mm2 f_{y} = \sigma_{x} = yield strength 500 N/mm2 f_{y} = coefficient of linear 0.1E = 20 kN/mm2 f_{y} = \sigma_{y} = yield strength 500 N/mm2 f_{y} = \sigma_{y} = yield strength 500 N/mm2 f_{y} = coefficient of linear 0.1E = 20 kN/mm2 f_{y} = coefficient of linear 0.1E = 20 kN/mm2 f_{y} = coefficient of linear 0.1E = 20 kN/mm2 f_{y} = coefficient of linear 0.1E = 0 kN/mm2 f_{y} = coefficient of linear 3.4 \times 10^{5} kN/mm2thermal expansion f_{y} = horanger b_{y} = horanger $ | containment–secondary | | |
| (b) Membrane plus bending $0.60f'_{c}$ concrete (after losses) Containments-primary (a) Membrane (b) Membrane plus bending Containment-secondary $0.30f'_{c}$ $0.45f'_{c}$ 2. Euro code 2 Concrete material properties $f_{ck}, \sigma_{a} = \mininimum cube -41.34 kN/mm^2$ Strength of concerete at 28 days $f_{y}, \sigma_{y} = yield strength -0.66\sigma_{cu}$ $\sigma_{i} = tensile strength +0.1\sigma_{cu}$ E = elastic modulus +0.476E $e_{cu} = ultimate strains 0.0035$ v = Poisson ratio 0.18 $\alpha_{T} = coefficient of linear 8.0 \muM/mcCthermal conductivity 1.75 W/mcCa' = coefficient of 0.65,0.68, 0.87,0.87aggregatese_{ct} = shrinkage strain 200×10^{-6}Convertional steel\overline{Y} = \sigma_{y} = yield strength 4516 MN/mm^{2}(50\omega) \text{ or } 750\overline{F} = e_{acteristic strength} 500 N/mm^{2}Liner 12 200 N/mm2Liner$ 12 mm + 10% $L_{i} = thickness 19 mm + 5%$ $Up to 40 mm max to 400 mm up to 25 m \alpha_{z} = coefficient of linear 3.4 × 10^{5} kN/mm^{2}Liner 12 mm + 10%L_{i} = - officient of linear 3.4 × 10^{5} kN/mm^{2}Liner 12 mm + 10%L_{i} = - officient of linear 3.4 × 10^{5} kN/mm^{2}Liner 12 mm + 10%L_{i} = thickness 19 mm + 5%Up to 40 mm max to 400 mm up to 25 m \alpha_{z} = coefficient of linear 3.4 × 10^{5} kN/mm^{2}Liner 13 mm + 5%L_{i} = thicknes 19 mm + 5%Reference is made to the manufacturer's catalogues for various systemsf_{mas}(at service) 0.6 -0.75f_{ck} 80 for ce: see catalogues 100 kM/m2 10 por max to a porticular systems 100 kM/m2 10 porticular syste$ | (a) Membrane | $0.45f'_{\rm c}$ | |
| concrete (after losses) Containments-primary (a) Membrane (b) Membrane plus bending Containment-secondary (b) Membrane plus bending Contrainment-secondary (c) $45f'_{c}$ 2. Euro code 2 Concrete material properties f_{ck}, σ_{a} minimum cube -41.34 kN/mm^2 Strength of conceret at 28 days $f_{y}, \sigma_{y} = \text{yield strength}$ $-0.66\sigma_{cu}$ σ_{a} tensile strength $-0.66\sigma_{cu}$ σ_{a} tensile strength $-0.66\sigma_{cu}$ σ_{a} tensile strength $-0.66\sigma_{cu}$ σ_{a} tensile strength $+0.1\sigma_{cu}$ E = elastic modulus $+41.4 \text{ kN/mm}^2$ $E_p = \text{plastic modulus}$ +0.476E $e_{cu} = \text{ultimate strains}$ 0.0035 v = Poisson ratio r = coefficient of linear R = thermal conductivity $T, 5 \text{ W/m}^{\circ}\text{C}$ T = coefficient of linear $e_{ct} = \text{shrinkage strain}$ 200×10^{-6} Conventional steel $\overline{\gamma} = \sigma_{y} = \text{yield strength}$ $f_{y} = characteristic strength$ Liner $f_{x} = \text{thormal expansion}$ $f_{yk} = \text{characteristic strength}$ Liner $f_{x} = \text{thormal to strength}$ Liner $f_{x} = \text{coefficient of linear}$ $f_{y} = \sigma_{y} = \text{yield strength}$ Liner $f_{x} = \text{coefficient of linear}$ $f_{y} = \sigma_{y} = \text{yield strength}$ $f_{x} = \text{coefficient of linear}$ $f_{yk} = \text{characteristic strength}$ Liner $f_{x} = \text{coefficient of linear}$ $f_{x} = coeffi$ | (b) Membrane plus bending | $0.60f'_{\rm c}$ | |
| Containments-primary(a) Membrane(b) Membrane plus bendingContainment-secondary $0.30f'_c$ $0.45f'_c$ $0.45f'_c$ 2. Euro code 2 $0.45f'_c$ $Concrete material propertiesf_c, \sigma_u = minimum cubef_ck, \sigma_u = minimum cube-41.34 \text{ kN/mm^2}Strength of concerte at 28daysdays-0.66\sigma_{cu}\sigma_i = tensile strength+0.1\sigma_{cu}E = elastic modulus+41.4 \text{ kN/mm^2}E_p = plastic modulus+0.476Ee_u = ultimate strains0.0035v = Poisson ratio0.18\alpha_T = coefficient of finear8.0 \ \mu M/m^\circ Cthermal expansionK = thermal conductivityK = thermal conductivity1.75 \ W/m^\circ Ca_q = coefficient of0.65, 0.68, 0.87, 0.87aggregates200 \times 10^{-6}Conventional steel7 = \sigma_y = yield strength\overline{\gamma} = \sigma_y = yield strength200 \ kN/mm^2x_T = coefficient of finear0.1E = 20 \ kN/mm^2concrete thermal expansion500 \ N/mm^2f_x = coefficient of finear0.1E = 20 \ kN/mm^2\tau_s = outristic strength25 \ mm up to 25 \ mm up$ | concrete (after losses) | | |
| (a) Membrane (b) Membrane plus bending Containment-secondary 0.30 f'_c 0.45 f'_c 2. Euro code 2 Concrete material properties $f_{ck} = cylindrical strength f_{ck}, \sigma_u = \minunum cubef_{ck}, \sigma_u = \minunum cubef_{ck} = cylindrical strength f_{ck}, \sigma_u = \minunum cubef_{ck}, \sigma_u = coefficient of linear K = thermal conductivityf_{c} = coefficient of linear f_{c} = \sigma_{c} = coefficient of linear f_{c} = coefficient of l$ | Containments-primary | | |
| (b) Membrane plus bending Containment-secondary 0.30f'c $0.45f'_c$ 2. Euro code 2 Concrete material properties $f_{ck} \sim \sigma_u$ minimum cube Strength of concerte at 28 days f_{y}, σ_y = yield strength -0.66 σ_{cu} σ_i = tensile strength +0.1 σ_{cu} E = elastic modulus +41.4 kN/mm ² $E_p = plastic modulus$ +0.476 E $e_{cu} = ultimate strains 0.0035 v = Poisson ratio 0.18\alpha_T = coefficient of linear 8.0 \muM/m°Cthermal expansionK = thermal conductivity 1.75 W/m°C a' = coefficient of 0.65,0.68, 0.87,0.87aggregatese_{ct} = shrinkage strain 200×10^{-6}Conventional steel\bar{\gamma} = \sigma_y = yield strength 4516 MN/mm2(50\omega) or 750E = elastic modulus 400 (25\omega) or 750F = \sigma_y = yield strength 4516 MN/mm2f_y = \sigma_y = yield strength 25 mm up to 25 ma_x = coefficient of linear 3.4 \times 10^5 kN/mm2thermal expansion 10 \muM/m°CK = thermal conductivity 41.6 W/m°CFrestress Reference is made to the manufacturer's catalogues for various systemsf_{mas}(at service) 0.6 -0.75f_{ck} force : see catalogues for various systems 41.6 M/m2 catalogues for various asystems 41.6 M/m2 catalogues for vari$ | (a) Membrane | | |
| Containment-secondary $0.30f'_{c}$ $0.45f'_{c}$ 2. Euro code 2 Concrete material properties $0.45f'_{c}$ $f_{ck} = q$ = quindrical strength $25 - 60 \text{ N/mm}^290 \neq \text{N/mm}^2$ -41.34 kN/mm^2 Strength of concerete at 28 days $-0.66\sigma_{cu}$ -41.34 kN/mm^2 $f_{y}, \sigma_y = yield strength-0.66\sigma_{cu}+0.1\sigma_{cu}E = elastic modulus+41.4 \text{ kN/mm}^2E_p = plastic modulus+0.476Ee_{cu} = ultimate strains0.0035v = \text{Poisson ratio}\sigma_1 = \text{coefficient of linear}8.0 \ \mu\text{M/m}^\circ\text{C}thermal expansion1.75 \ W/m^\circ\text{C}a = coefficient of linear\vec{x} = \text{thermal conductivity}1.75 \ W/m^\circ\text{C}a = coefficient of linear\vec{y} = \sigma_y = yield strength200 \times 10^{-6}\vec{y} = \sigma_y = yield strength4516 \ MN/mm^2(50\omega) \text{ or } 750\vec{x} = \text{characteristic strength}200 \times N/mm^21.16 = 20 \ kN/mm^2\vec{x} = \text{characteristic strength}200 \ N/mm^21.2 \ mm + 10\%\vec{x} = \text{coefficient of linear}3.4 \times 10^3 \ \text{kN/mm}^2\vec{x} = \text{coefficient of linear}3.4 \times 10^3 \ \text{kN/mm}^2\vec{x} = \text{coefficient of linear}0.1E = 20 \ \text{kN/mm}^2\vec{x} = \text{coefficient of linear}0.1E = 20 \ \text{kN/mm}^2\vec{x} = \text{coefficient of linear}0.16 \ \text{Comment max}\vec{y} = \sigma_y = yield strength25 \ \text{mm} \text{m} to 240 \ \text{mm} \text{m} to 25 \ \text{m} \text{m} to 200 \ \text{N/mm}^2\vec{x} = \text{coefficient of linear}3.4 \times 10^3 \ \text{kN/mm}^2\vec{y} = \sigma_y = yield strength25 \ \text{mm} \text{m} \text{c} Coeffi$ | (b) Membrane plus bending | | |
| 2. Euro code 2 Concrete material properties $f_{ck} = cylindrical strength f_{ck}, \sigma_u = \mininum cubeStrength of concerete at 28daysf_y, \sigma_y = yield strength= tensile strength= te$ | Containment-secondary | $0.30f'_{\rm c}$ | |
| 2. Euro code 2 Concrete material properties $f_{ck} = cylindrical strength f_{ck}, \sigma_u = \minunum cubeStrength of concerete at 28daysf_{y}, \sigma_y = yield strengthf_y, \sigma_y = yield strengthf_y, \sigma_y = yield strengthf_y, \sigma_y = yield strengthf_y = a_y = plastic modulusf_y = a_y = plastic modulusf_y = a_y = plastic modulusf_y = a_y = poisson ratiof_y = coefficient of linear f_y = a_y = yield strengthf_y = \sigma_y = yield strengthf_y = \sigma_y = yield strengthf_y = a_y = $ | | $0.45f'_{\rm c}$ | |
| Concrete material properties $f_{ck} = cylindrical strength25 - 60 N/mm290 \geq N/mm2f_{ck}, \sigma_u = minimum cube-41.34 kN/mm2Strength of concerete at 28days\sigma_i = tensile strength-0.66\sigma_{cu}\sigma_i = tensile strength+0.1\sigma_{cu}E = elastic modulus+41.4 kN/mm2E_p = plastic modulus+0.476Ee_{cu} = ultimate strains0.0035v = Poisson ratio0.18\alpha_T = coefficient of linear8.0 µM/m°Cthermal expansion1.75 W/m°CK = thermal conductivity1.75 W/m°Caggregates200 \times 10^{-6}e_{cu} = shrinkage strain200 \times 10^{-6}Conventional steel7 = \sigma_y = yield strength\overline{\gamma} = \sigma_y = yield strength4516 MN/mm2(50\omega) or T50E = elastic modulus200 \text{ kN/mm^2}\alpha_T = coefficient of linear0.1E = 20 \text{ kN/mm^2}correte thermal expansionf_y = \sigma_y = yield strengthf_y = \sigma_y = yield strength500 \text{ N/mm^2}tiner25 \text{ mm up to 25 m}\sigma_i = coefficient of linear3.4 \times 10^5 \text{ kN/mm^2}thermal expansion10 \mu M/m^{\circ}C\bar{X} = thermal conductivity1.6 \text{ W/m^2C}\bar{X} = thickness19 \text{ mm} + 5\%Up to 40 \text{ mm max to 400 mm up to}\bar{Y} = \sigma_y = yield strength25 \text{ mm up to 25 m}\sigma_i = coefficient of linear3.4 \times 10^5 \text{ kN/mm^2}f_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6 - 0.75f_{ck}$ | 2. Euro code 2 | | |
| $f_{ck} = cylindrical strength25 - 60 \text{ N/mm}^2 9 \neq \text{N/mm}^2f_{ck}, \sigma_u = \mininimum cube-41.34 \text{ kN/mm}^2Strength of concerete at 28daysf_y, \sigma_y = yield strength-0.66\sigma_{cu}\tau_i = tensile strength+0.1\sigma_{cu}E = elastic modulus+41.4 \text{ kN/mm}^2E_p = plastic modulus+0.76E_0e_{cu} = ultimate strains0.0035v = Poisson ratio0.18\alpha_T = coefficient of linear8.0 \mu M/m^\circ Cthermal expansionKK = thermal conductivity1.75 \text{ W/m}^\circ Ca'_g = coefficient of0.65, 0.68, 0.87, 0.87aggregates200 \times 10^{-6}v_{ect} = shrinkage strain200 \times 10^{-6}Conventional steel7i = \sigma_y = yield strengthF_p = plastic modulus200 \times 10^{-6}E_p = plastic modulus200 \times 10^{-6}V_{ect} = coefficient of linear0.1E = 20 \text{ kN/mm}^2\sigma_{ect} = shrinkage strain200 \times 10^{-6}Conventional steel500 \text{ N/mm}^2\overline{\gamma} = \sigma_y = yield strength500 \text{ N/mm}^2Liner12 \text{ mm} + 10\%I_s = coefficient of linear3.4 \times 10^5 \text{ kN/mm}^2f_y = \sigma_y = yield strength25 \text{ mm} up to 25 \text{ m}f_x = coefficient of linear3.4 \times 10^5 \text{ kN/mm}^2I_s = functional expansionI_p M/m^\circ Cf_x = coefficient of linear3.4 \times 10^5 \text{ kN/mm}^2I_s = functional expansionI_p M/m^\circ Cf_{mas}(at service)0.6 - 0.75f_{ck}<$ | Concrete material properties | | |
| $f_{ck}, \sigma_u = \mininium cube$ -41.34 kN/mm^2 Strength of concerete at 28days $f_y, \sigma_y = yield strength$ $-0.66\sigma_{cu}$ $\sigma_i = \text{tensile strength}$ $+0.1\sigma_{cu}$ $E = \text{elastic modulus}$ $+41.4 \text{ kN/mm}^2$ $E_p = \text{plastic modulus}$ $+0.476E$ $e_{cu} = \text{ultimate strains}$ 0.0035 $v = \text{Poisson ratio}$ 0.18 $\alpha_T = \text{coefficient of linear}$ $8.0 \ \mu\text{M/m}^\circ\text{C}$ thermal expansion K $K = \text{thermal conductivity}$ $1.75 \text{ W/m}^\circ\text{C}$ $a = \text{coefficient of}$ $0.65, 0.68, 0.87, 0.87$ $aggregates$ 200×10^{-6} $E_{et} = \text{shrinkage strain}$ 200×10^{-6} $E = \text{elastic modulus}$ $4400 (25\omega) \text{ or } 750$ $E = \text{elastic modulus}$ 200 kN/mm^2 $\sigma_T = \text{coefficient of linear}$ $0.1E = 20 \text{ kN/mm}^2$ $\sigma_T = \text{coefficient of linear}$ $0.1E = 20 \text{ kN/mm}^2$ $f_y = \sigma_{haracteristic strength}$ 500 N/mm^2 $f_x = \text{coefficient of linear}$ $0.1E = 20 \text{ kN/mm}^2$ $f_y = \sigma_y$ yield strength 500 N/mm^2 $f_x = \text{coefficient of linear}$ $0.1E = 20 \text{ kN/mm}^2$ $f_y = \sigma_y$ yield strength 500 N/mm^2 $f_x = \text{coefficient of linear}$ $3.4 \times 10^5 \text{ kN/mm}^2$ $f_x = \text{thirkness}$ $19 \text{ mm} + 5\%$ Up to 40 mm max to 400 mm up to 25 mm up to 25 m $f_x = \text{coefficient of linear}$ $3.4 \times 10^5 \text{ kN/mm}^2$ $f_{ar} = \text{coefficient of linear}$ $0.6 - 0.75f_{ck}$ $f_{mas}(at service)$ <t< td=""><td>$f_{\rm ck} =$ cylindrical strength</td><td>$25 - 60 \text{ N/mm}^2 90 \ge \text{N/mm}^2$</td><td></td></t<> | $f_{\rm ck} =$ cylindrical strength | $25 - 60 \text{ N/mm}^2 90 \ge \text{N/mm}^2$ | |
| Strength of concerete at 28 days-0.66 σ_{cu} $\sigma_1 = tensile strength-0.66\sigma_{cu}\sigma_1 = tensile strength-0.1\sigma_{cu}E = elastic modulus+41.4 kN/mm²E_p = plastic modulus+0.476Ee_{cu} = ultimate strains0.0035v = Poisson ratio0.18x_T = coefficient of linear8.0 \muM/m°Cthermal expansion1.75 W/m°Caggregatese_{ct} = shrinkage strain200 × 10^{-6}Conventional steel\overline{\gamma} = \sigma_y = yield strength4516 MN/mm²(50\omega) or T50\overline{\gamma} = \sigma_y = yield strength4516 MN/mm²T = coefficient of linear0.1E = 20 kN/mm²concret thermal expansion0.1E = 20 kN/mm²f_y = \sigma_y = yield strength500 N/mm²\chi_T = coefficient of linear0.1E = 20 kN/mm²concret thermal expansion500 N/mm²f_y = \sigma_y = yield strength25 mm up to 25 m\chi_r = coefficient of linear3.4 \times 10^5 kN/mm²t_s = thickness10 \ \mu M/m°CK = thermal conductivity41.6 W/m°CFrestressReference is made to the manufacturer'scatalogues for various systemsf_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6f_{max} = P_0transfer force : see cataloguesfor current of various systems$ | $f_{\rm ck}, \sigma_{\rm u} =$ minimum cube | -41.34 kN/mm^2 | |
| days $f_y, \sigma_y = yield strength-0.66\sigma_{cu}$ $\sigma_i = tensile strength+0.1\sigma_{cu}E = elastic modulus+41.4 k N/mm²E_p = plastic modulus+0.476E\varepsilon_{cu} = ultimate strains0.0035v = Poisson ratio0.18\sigma_T = coefficient of linear8.0 \muM/m°Cthermal expansionKK = thermal conductivity1.75 W/m°Ca' = coefficient of0.65,0.68, 0.87,0.87aggregates200 × 10^{-6}\mathcal{C}_{onventional steel}200 × 10^{-6}\overline{\gamma} = \sigma_y = yield strength4516 MN/mm²(50\omega) or 750E = elastic modulus200 kN/mm²\Delta \tau_T = coefficient of linear0.1E = 20 kN/mm²concrete thermal expansionf_y = \sigma_y = yield strengthf_y = \sigma_y = yield strength500 N/mm²Liner12 mm + 10%Liner25 mm up to 25 m\sigma_\tau = coefficient of linear3.4 \times 10^5 kN/mm²Liner12 mm + 5%Up to 40 mm max to 400 mm up to\bar{Y} = \sigma_y = yield strength25 mm up to 25 m\sigma_\tau = coefficient of linear3.4 \times 10^5 kN/mm²thermal expansion10 \muM/m°CK = thermal conductivity41.6 W/m°CFrestressReference is made to the manufacturer's catalogues for various systemsf_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6f_{max} = P_0transfer force : see catalogues for various systems$ | Strength of concerete at 28 | | |
| $ \begin{array}{llllllllllllllllllllllllllllllllllll$ | days | | |
| $ \begin{aligned} \sigma_t &= \text{tensile strength} &+ 0.1 \sigma_{cu} \\ E &= \text{elastic modulus} &+ 41.4 \text{ kN/mm}^2 \\ E_p &= \text{plastic modulus} &+ 0.476E \\ e_{cu} &= \text{ultimate strains} & 0.0035 \\ v &= \text{Poisson ratio} & 0.18 \\ \alpha_T &= \text{coefficient of linear} & 8.0 \ \mu\text{M/m}^\circ\text{C} \\ \text{thermal expansion} \\ K^{=} \text{thermal conductivity} & 1.75 \ \text{W/m}^\circ\text{C} \\ a' &= \text{coefficient of} & 0.65, 0.68, 0.87, 0.87 \\ aggregates \\ e_{ct} &= \text{shrinkage strain} & 200 \times 10^{-6} \\ Conventional steel \\ \overline{\gamma} &= \sigma_y = \text{yield strength} & 4516 \ \text{MN/mm}^2(50\omega) \text{ or } T50 \\ E &= \text{elastic modulus} & 200 \times 10^{-6} \\ Conventional steel \\ \overline{\gamma} &= \sigma_y = \text{yield strength} & 4516 \ \text{MN/mm}^2 \\ \alpha_T &= \text{coefficient of linear} & 0.1E &= 20 \ \text{kN/mm}^2 \\ \alpha_T &= \text{coefficient of linear} & 0.1E &= 20 \ \text{kN/mm}^2 \\ \sigma_T &= \text{coefficient of linear} & 0.1E &= 20 \ \text{kN/mm}^2 \\ \sigma_T &= \text{coefficient of linear} & 0.1E &= 20 \ \text{kN/mm}^2 \\ \sigma_T &= \text{coefficient of linear} & 0.1E &= 20 \ \text{kN/mm}^2 \\ \sigma_T &= \text{coefficient of linear} & 0.1E &= 20 \ \text{kN/mm}^2 \\ \sigma_T &= \text{coefficient of linear} & 12 \ \text{mm} + 10\% \\ t_s &= \text{thickness} & 19 \ \text{mm} + 5\% \\ \text{Up to 40 \ mm max to 400 \ mm up to} \\ \overline{Y} &= \sigma_y &= \text{yield strength} & 25 \ \text{mm up to 25 m} \\ \sigma_{\tau} &= \text{coefficient of linear} & 3.4 \times 10^5 \ \text{kN/mm}^2 \\ \text{thermal expansion} & 10 \ \mu\text{M/m}^\circ\text{C} \\ K &= \text{thermal conductivity} & 41.6 \ \text{W/m}^\circ\text{C} \\ F &= \text{thermal conductivity} & 41.6 \ \text{W/m}^\circ\text{C} \\ F &= \text{coefficient of linear} & 0.6 &= 0.75f_{ck} \\ f_{mas}(\text{at service}) & 0.6 &= 0.75f_{ck} \\ f_{mas}(\text{at service}) & 0.6f_{max} &= P_0 \text{transfer force} : \text{see catalogues} \\ for a vectore for a count a consersement \\ for a vectore for a count a consersement \\ for a vectore for a count on consersement \\ for a vectore for a count on consersement \\ for a vectore for a count on consersement \\ for a vectore for a count on consersement \\ for a vectore for a count on consersement \\ for a vectore for a count on consersement \\ for a vectore for a count on consersement \\ for a vectore for a count on consersement \\ for a$ | $f_{\rm y}, \sigma_{\rm y} =$ yield strength | $-0.66\sigma_{\rm cu}$ | |
| $\begin{array}{llllllllllllllllllllllllllllllllllll$ | σ_t = tensile strength | $+0.1\sigma_{\rm cu}$ | |
| $\begin{array}{llllllllllllllllllllllllllllllllllll$ | E = elastic modulus | $+41.4 \text{ kN/mm}^2$ | |
| ε_{cu} = ultimate strains0.0035 $v = Poisson ratio$ 0.18 $\alpha_T = coefficient of linear8.0 \muM/m°Cthermal expansionK = thermal conductivityK = thermal conductivity1.75 W/m°Ca' = coefficient of0.65,0.68, 0.87,0.87aggregates\varepsilon_{ct} = shrinkage strain\varepsilon_{ct} = shrinkage strain200 \times 10^{-6}Conventional steel7 = \sigma_y = yield strength\overline{\gamma} = \sigma_y = yield strength4516 \text{ MN/mm^2}(50\omega) \text{ or } T50E = elastic modulus200 \times 10^{-6}E_p = plastic modulus200 \times N/mm^2\alpha_T = coefficient of linear0.1E = 20 \text{ kN/mm^2}concrete thermal expansion500 \text{ N/mm^2}f_{yk} = characteristic strength500 \text{ N/mm^2}Liner12 \text{ mm} + 10\%Liner12 \text{ mm} + 5\%Up to 40 \text{ mm} max to 400 mm up to\overline{Y} = \sigma_y = yield strength3.4 \times 10^5 \text{ kN/mm^2}hermal expansion10 \ \mu M/m^\circ C\overline{Y} = \sigma_y = sield strength3.6 \times 10^5 \text{ kN/mm^2}Liner1.6 \text{ W/m}^\circ CF = ray = sield strength3.6 \times 10^5 \text{ kN/mm^2}f_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6f_{max} = P_o transfer force : see cataloguesf_{mas}(at service)0.6f_{max} = Fo_{attransfer force : see catalogues$ | $E_{\rm p} = {\rm plastic \ modulus}$ | +0.476E | |
| $v = Poisson ratio0.18\alpha_{\rm T} = coefficient of linear8.0 \muM/m°Cthermal expansion1.75 W/m°CK = thermal conductivity1.75 W/m°Ca' = coefficient of0.65,0.68, 0.87,0.87aggregates200×10-6\mathcal{E}_{ct} = shrinkage strain200×10-6Conventional steel4516 MN/mm²(50\omega) or T50F = \sigma_{\rm y} = yield strength4516 MN/mm²(50\omega) or T25E_{\rm p} = plastic modulus200 kN/mm²\alpha_{\rm T} = coefficient of linear0.1E = 20 kN/mm²concrete thermal expansion500 N/mm²f_{\rm yk} = characteristic strength500 N/mm²Liner12 mm + 10%t_{\rm s} = thickness19 mm + 5%Up to 40 mm max to 400 mm up to\bar{Y} = \sigma_{\rm y} = yield strength25 m up to 25 m\alpha_{\rm \tau} = coefficient of linear3.4 × 105 kN/mm²thermal expansion10 \muM/m°CK = thermal conductivity41.6 W/m°CPrestressReference is made to the manufacturer's catalogues for various systemsf_{mas}(at service)0.6 - 0.75fckf_{mas}(at service)0.6 f_max = P_o transfer force : see catalogues for various systems$ | $\varepsilon_{\rm cu}$ = ultimate strains | 0.0035 | |
| $\alpha_{\rm T}$ = coefficient of linear $8.0 \ \mu M/{\rm m}^{\circ}{\rm C}$ thermal expansion $K =$ thermal conductivity $1.75 \ W/{\rm m}^{\circ}{\rm C}$ $K =$ thermal conductivity $1.75 \ W/{\rm m}^{\circ}{\rm C}$ $a =$ coefficient of $0.65, 0.68, 0.87, 0.87$ $p = p_{\rm stic}$ modules 200×10^{-6} $E =$ elastic modulus $4516 \ MN/mm^2(50\omega)$ or $T50$ $E_p =$ plastic modulus $200 \ k/mm^2$ $\alpha_{\rm T} =$ coefficient of linear $0.1E = 20 \ kN/mm^2$ $concrete thermal expansion500 \ N/mm^2f_{\rm y} = characteristic strength500 \ N/mm^2Liner12 \ mm + 10\%t_s = thickness19 \ mm + 5\%Up to 40 mm max to 400 mm up to\bar{Y} = \sigma_{\rm y} = yield strength25 \ mm up to 25 \ m\alpha_{\rm \tau} = coefficient of linear3.4 \times 10^5 \ kN/mm^2thermal expansion10 \ \mu M/m^{\circ}CK = thermal conductivity41.6 \ W/m^{\circ}CPrestressReference is made to the manufacturer's catalogues for various systemsf_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6f_{max} = P_o transfer force : see cataloguesf_{mas}(at service)0.6f_{max} = F_o transfer force : see catalogues$ | v = Poisson ratio | 0.18 | |
| thermal expansion $K =$ thermal conductivity $1.75 \text{ W/m}^{\circ}\text{C}$ $a' = \text{coefficient of}$ $0.65, 0.68, 0.87, 0.87$ $aggregates200 \times 10^{-6}\mathcal{C}onventional steel200 \times 10^{-6}\bar{\gamma} = \sigma_y = \text{yield strength}4516 \text{ MN/mm}^2(50\omega) \text{ or } 750E = \text{elastic modulus}4400 (25\omega) \text{ or } 725E_p = \text{plastic modulus}200 \text{ kN/mm}^2\alpha_T = \text{coefficient of linear}0.1E = 20 \text{ kN/mm}^2\sigma_r = \text{coefficient of linear}0.1E = 20 \text{ kN/mm}^2f_{yk} = \text{characteristic strength}500 \text{ N/mm}^2Liner12 \text{ mm} + 10\%t_s = \text{thickness}19 \text{ mm} + 5\%\nabla p = y = yield strength25 \text{ mm} up to 25 \text{ m}\alpha_\tau = \text{coefficient of linear}3.4 \times 10^5 \text{ kN/mm}^2thermal expansion10 \ \mu\text{M/m}^{\circ}\text{C}K = \text{thermal conductivity}41.6 \text{ W/m}^{\circ}\text{C}Prestress0.6 - 0.75f_{ck}f_{mas}(\text{at service})0.6 - 0.75f_{ck}f_{mas}(\text{at service})0.6f_{max} = P_o transfer force : see catalogues for exervate accessment$ | $\alpha_{\rm T} = {\rm coefficient \ of \ linear}$ | $8.0 \ \mu M/m^{\circ}C$ | |
| $K =$ thermal conductivity $1.75 \text{ W/m}^{\circ}\text{C}$ $a' = \text{coefficient of}$ $0.65, 0.68, 0.87, 0.87$ $aggregates$ $\varepsilon_{ct} = \text{shrinkage strain}$ 200×10^{-6} $Conventional steel$ $\overline{\gamma} = \sigma_y = \text{yield strength}$ $4516 \text{ MN/mm}^2(50\omega) \text{ or } T50$ $E = \text{elastic modulus}$ $4400 (25\omega) \text{ or } T25$ $E_p = \text{plastic modulus}$ 200 kN/mm^2 $\alpha_T = \text{coefficient of linear}$ $0.1E = 20 \text{ kN/mm}^2$ concrete thermal expansion 500 N/mm^2 $f_x = \text{characteristic strength}$ 500 N/mm^2 $Liner$ $12 \text{ mm} + 10\%$ $t_s = \text{thickness}$ $19 \text{ mm} + 5\%$ Vp to 40 mm max to 400 mm up to $\overline{Y} = \sigma_y = \text{yield strength}$ 2.5 mm up to 25 m $\alpha_\tau = \text{coefficient of linear}$ $10 \ \mu\text{M/m}^{\circ}\text{C}$ $K = \text{thermal conductivity}$ $41.6 \text{ W/m}^{\circ}\text{C}$ $Prestress$ Reference is made to the manufacturer's catalogues for various systems $f_{mas}(\text{at service})$ $0.6 - 0.75f_{ck}$ $f_{mas}(\text{at service})$ $0.6f_{max} = P_o transfer force : see catalogues$ | thermal expansion | | |
| $a = \operatorname{coefficient}$ of aggregates0.65,0.68, 0.87,0.87 $\varepsilon_{ct} = \operatorname{shrinkage strain}$ 200×10^{-6} $Conventional steel$ $\overline{\gamma} = \sigma_y = \operatorname{yield}$ strength $4516 \text{ MN/mm}^2(50\omega) \text{ or } 750$ $E = \operatorname{elastic}$ modulus $4400 (25\omega) \text{ or } 725$ $E_p = \operatorname{plastic}$ modulus 200 kN/mm^2 $\alpha_T = \operatorname{coefficient}$ of linear $0.1E = 20 \text{ kN/mm}^2$ concrete thermal expansion 500 N/mm^2 $f_y = \operatorname{characteristic strength}$ 500 N/mm^2 Liner $12 \text{ mm} + 10\%$ $t_s = \operatorname{thickness}$ $19 \text{ mm} + 5\%$ Up to 40 mm max to 400 mm up to $\overline{Y} = \sigma_y = \operatorname{yield}$ strength 25 mm up to 25 m $\alpha_\tau = \operatorname{coefficient}$ of linear $10 \ \mu M/m^\circ C$ $K = \operatorname{thermal conductivity}$ $41.6 \text{ W/m}^\circ C$ PrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(\operatorname{at service})$ $0.6 - 0.75f_{ck}$ $f_{mas}(\operatorname{at service})$ $0.6f_{max} = P_o \operatorname{transfer}$ force : see catalogues | K = thermal conductivity | 1.75 W/m°C | |
| aggregates $\varepsilon_{ct} = shrinkage strain200 \times 10^{-6}Conventional steel\bar{\gamma} = \sigma_y = yield strength4516 \text{ MN/mm}^2(50\omega) \text{ or } T50E = elastic modulus4400 (25\omega) \text{ or } T25E_p = plastic modulus200 \text{ kN/mm}^2\alpha_T = coefficient of linear0.1E = 20 \text{ kN/mm}^2concrete thermal expansion500 \text{ N/mm}^2f_y = characteristic strength500 \text{ N/mm}^2Liner12 \text{ mm} + 10\%t_s = \text{thickness}19 \text{ mm} + 5\%Up to 40 mm max to 400 mm up to\bar{Y} = \sigma_y = yield strength25 \text{ mm} up to 25 \text{ m}\alpha_\tau = coefficient of linear10 \ \mu M/m^\circ CK = \text{thermal conductivity}41.6 \text{ W/m}^\circ CPrestressReference is made to the manufacturer's catalogues for various systemsf_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6f_{max} = P_o transfer force : see catalogues$ | a = coefficient of | 0.65,0.68, 0.87,0.87 | |
| $\varepsilon_{ct} = \operatorname{shrinkage strain}$ 200×10^{-6} Conventional steel $\overline{\gamma} = \sigma_y = \operatorname{yield strength}$ $4516 \mathrm{MN/mm^2(50\omega)} \text{ or } 750$ $\overline{p} = \sigma_y = \operatorname{yield strength}$ $4516 \mathrm{MN/mm^2(50\omega)} \text{ or } 750$ $E = \operatorname{elastic modulus}$ $200 \mathrm{kN/mm^2}$ $\sigma_T = \operatorname{coefficient of linear}$ $0.1E = 20 \mathrm{kN/mm^2}$ concrete thermal expansion $0.1E = 20 \mathrm{kN/mm^2}$ $f_{yk} = \operatorname{characteristic strength}$ $500 \mathrm{N/mm^2}$ Liner $12 \mathrm{mm} + 10\%$ $t_s = \operatorname{thickness}$ $19 \mathrm{mm} + 5\%$ Up to 40 mm max to 400 mm up to $\overline{Y} = \sigma_y = \operatorname{yield strength}$ $2.5 \mathrm{mm}$ up to $25 \mathrm{m}$ $\alpha_\tau = \operatorname{coefficient of linear}$ $3.4 \times 10^5 \mathrm{kN/mm^2}$ thermal expansion $10 \mu \mathrm{M/m^\circ C}$ $K = \operatorname{thermal conductivity}$ $41.6 \mathrm{W/m^\circ C}$ Prestress $0.6 - 0.75f_{ck}$ $f_{mas}(\operatorname{at service})$ $0.6f_{max} = P_o \operatorname{transfer force}$: see catalogues $f_{mas}(\operatorname{at service})$ $0.6f_{max} = P_o \operatorname{transfer force}$: see catalogues | aggregates | • • • • • • • | |
| Conventional steel $4516 \text{ MN/mm}^2(50\omega) \text{ or } 750$ $\bar{\gamma} = \sigma_y = \text{yield strength}$ $4516 \text{ MN/mm}^2(50\omega) \text{ or } 750$ $E = \text{elastic modulus}$ 200 kN/mm^2 $\alpha_T = \text{coefficient of linear}$ $0.1E = 20 \text{ kN/mm}^2$ concrete thermal expansion $0.1E = 20 \text{ kN/mm}^2$ $f_{yk} = \text{characteristic strength}$ 500 N/mm^2 Liner $12 \text{ mm} + 10\%$ $t_s = \text{thickness}$ $19 \text{ mm} + 5\%$ Up to 40 mm max to 400 mm up to $\bar{Y} = \sigma_y = \text{yield strength}$ $25 \text{ mm up to } 25 \text{ m}$ $\alpha_\tau = \text{coefficient of linear}$ $10 \ \mu\text{M/m}^\circ\text{C}$ $K = \text{thermal conductivity}$ $41.6 \text{ W/m}^\circ\text{C}$ Prestress $0.6 - 0.75f_{ck}$ $f_{mas}(\text{at service})$ $0.6f_{max} = P_o \text{transfer force : see catalogues for various systems}$ | $\varepsilon_{\rm ct} = {\rm shrinkage \ strain}$ | 200×10^{-6} | |
| $\overline{\gamma} = \sigma_y$ = yield strength4310 MN/min (500) of 730 $E =$ elastic modulus4400 (25 ω) or 725 E_p = plastic modulus200 kN/mm² α_T = coefficient of linear0.1 $E = 20$ kN/mm²concrete thermal expansion500 N/mm² f_{yk} = characteristic strength500 N/mm² $Liner$ 12 mm + 10% t_s = thickness19 mm + 5% $\overline{Y} = \sigma_y$ = yield strength25 mm up to 25 m α_τ = coefficient of linear3.4 × 10 ⁵ kN/mm²thermal expansion10 μ M/m°CK = thermal conductivity41.6 W/m°CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at service)$ 0.6 - 0.75 f_{ck} $f_{mas}(at service)$ 0.6f_max = P_o transfer force : see catalogues | Conventional steel | $4516 \text{ MN}/\text{mm}^2(50 \text{ cm}) \text{ cm} T50$ | |
| $E =$ elastic modulus4400 (250) or 725 $E_p =$ plastic modulus200 kN/mm² $\alpha_T =$ coefficient of linear $0.1E = 20 \text{ kN/mm²}$ concrete thermal expansion 500 N/mm² $f_{yk} =$ characteristic strength 500 N/mm² Liner12 mm + 10% $t_s =$ thickness19 mm + 5% $\bar{Y} = \sigma_y =$ yield strength25 mm up to 25 m $\alpha_\tau =$ coefficient of linear $3.4 \times 10^5 \text{ kN/mm²}$ thermal expansion10 μ M/m°C $K =$ thermal conductivity41.6 W/m°CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at service)$ $0.6 - 0.75f_{ck}$ $f_{mas}(at service)$ $0.6f_{max} = P_o transfer force : see catalogues$ | $\bar{\gamma} = \sigma_{\rm y} =$ yield strength | 4310 MIN/IIIII (300) 01 730 | |
| E_p = plastic modulus200 kN/mm² α_T = coefficient of linear $0.1E = 20 \text{ kN/mm²}$ $concrete thermal expansion0.1E = 20 \text{ kN/mm²}f_{yk} = characteristic strength500 \text{ N/mm²}Liner12 \text{ mm} + 10\%t_s = thickness19 \text{ mm} + 5\%\bar{Y} = \sigma_y = yield strength25 \text{ mm} up to 25 \text{ m}\alpha_{\tau} = coefficient of linear3.4 \times 10^5 \text{ kN/mm²}thermal expansion10 \mu M/m°CK = thermal conductivity41.6 \text{ W/m°C}PrestressReference is made to the manufacturer's catalogues for various systemsf_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6f_{max} = P_o transfer force : see catalogues$ | E = elastic modulus | 4400 (250) or 125 | |
| $\alpha_{\rm T}$ = coefficient of linear $0.1E = 20 \text{ kN/mm}^2$ concrete thermal expansion f_{yk} = characteristic strength 500 N/mm^2 Liner12 mm + 10% t_s = thickness19 mm + 5% $\bar{Y} = \sigma_y$ = yield strength25 mm up to 25 m α_{τ} = coefficient of linear $3.4 \times 10^5 \text{ kN/mm}^2$ thermal expansion10 μ M/m°CK = thermal conductivity41.6 W/m°CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at service)$ $0.6 - 0.75f_{ck}$ $f_{mas}(at service)$ $0.6f_{max} = P_o transfer force : see catalogues$ | $E_{\rm p} = {\rm plastic modulus}$ | 200 kN/mm^2 | |
| concrete thermal expansion $f_{yk} = characteristic strength$ 500 N/mm^2 Liner $12 \text{ mm} + 10\%$ $t_s = thickness$ $19 \text{ mm} + 5\%$ $\bar{Y} = \sigma_y = yield strength$ 25 mm up to 25 m $\alpha_\tau = coefficient of linear3.4 \times 10^5 \text{ kN/mm}^2thermal expansion10 \ \mu\text{M/m}^\circ\text{C}K = thermal conductivity41.6 \ W/m^\circ\text{C}PrestressReference is made to the manufacturer's catalogues for various systemsf_{mas}(at service)0.6 - 0.75f_{ck}f_{mas}(at service)0.6f_{max} = P_o transfer force : see catalogues$ | $\alpha_{\rm T} = {\rm coefficient of linear}$ | $0.1E = 20 \text{ kN/mm}^2$ | |
| $f_{yk} =$ characteristic strength500 N/mm²Liner12 mm + 10% $t_s =$ thickness19 mm + 5% $\bar{Y} = \sigma_y =$ yield strength25 mm up to 25 m $\bar{x}_\tau =$ coefficient of linear 3.4×10^5 kN/mm²thermal expansion10 μ M/m°C $K =$ thermal conductivity41.6 W/m°CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at service)$ $0.6 - 0.75f_{ck}$ $f_{mas}(at service)$ $0.6f_{max} = P_o transfer force : see catalogues$ | concrete thermal expansion | 500 NI / 2 | |
| Liner12 mm + 10% $t_s = \text{thickness}$ 19 mm + 5% $\bar{Y} = \sigma_y = \text{yield strength}$ 25 mm up to 25 m $\alpha_\tau = \text{coefficient of linear}$ $3.4 \times 10^5 \text{ kN/mm^2}$ thermal expansion10 μ M/m°C $K = \text{thermal conductivity}$ 41.6 W/m°CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(\text{at service})$ $0.6 - 0.75f_{ck}$ $f_{mas}(\text{at service})$ $0.6f_{max} = P_o transfer force : see catalogues for accurate accessment$ | $f_{yk} = characteristic strength$ | 12 mm + 1007 | |
| $I_s = \text{thickness}$ 19 mm + 5% Up to 40 mm max to 400 mm up to 25 mm up to 25 m $\alpha_{\tau} = \text{coefficient of linear}$ 25 mm up to 25 m $3.4 \times 10^5 \text{ kN/mm}^2$ thermal expansion $\pi = \text{coefficient of linear}$ $3.4 \times 10^5 \text{ kN/mm}^2$ $10 \mu\text{M/m}^\circ\text{C}$ $K = \text{thermal conductivity}$ $41.6 \text{ W/m}^\circ\text{C}$ $Prestress$ Reference is made to the manufacturer's catalogues for various systems $f_{\text{mas}}(\text{at service})$ $0.6 - 0.75f_{\text{ck}}$ $f_{\text{mas}}(\text{at service})$ $0.6f_{\text{max}} = P_{\text{o}} \text{transfer force}$: see catalogues | Liner | 12 mm + 10% | |
| $\bar{Y} = \sigma_y = yield strength$ 25 mm up to 25 m $\alpha_\tau = coefficient of linear3.4 \times 10^5 \text{ kN/mm^2}thermal expansion10 \ \mu\text{M/m}^\circ\text{C}K = thermal conductivity41.6 \ W/m^\circ\text{C}PrestressReference is made to the manufacturer's catalogues for various systemsf_{mas}(at \text{ service})0.6 - 0.75f_{ck}f_{mas}(at \text{ service})0.6f_{max} = P_o transfer force : see catalogues for accurate accessment$ | $l_{\rm s}$ – thickness | 19 mm + 3% | |
| $T = \sigma_y - yield strength$ 25 mm up to 25 m $\alpha_\tau = \text{coefficient of linear}$ $3.4 \times 10^5 \text{ kN/mm^2}$ thermal expansion $10 \ \mu\text{M/m}^\circ\text{C}$ $K = \text{thermal conductivity}$ $41.6 \ \text{W/m}^\circ\text{C}$ PrestressReference is made to the manufacturer's catalogues for various systems $f_{\text{mas}}(\text{at service})$ $0.6 - 0.75 f_{\text{ck}}$ $f_{\text{mas}}(\text{at service})$ $0.6 f_{\text{max}} = P_{\text{o}} \text{transfer force : see catalogues for accurate assessment}$ | $\overline{\mathbf{V}}$ = - yield stream at h | Up to 40 mm max to 400 mm up to 25 mm up to 25 mm | |
| α_{τ} - coefficient of linear $5.4 \times 10^{\circ}$ kN/linethermal expansion 10μ M/m°C $K =$ thermal conductivity $41.6 $ W/m°CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at $ service) $0.6 - 0.75 f_{ck}$ $f_{mas}(at $ service) $0.6 f_{max} = P_o transfer force : see cataloguesfor exervice for accurate assessment$ | $I \equiv \sigma_y - y$ ield strengtn | 2.5 mm up to 2.5 m 2.4 × 105 kN/mm ² | |
| Intermal expansionTo $\mu m/m C$ K = thermal conductivity41.6 W/m°CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at service)$ $0.6 - 0.75 f_{ck}$ $f_{mas}(at service)$ $0.6 f_{max} = P_o transfer force : see catalogues$ | u_{τ} – coefficient of intear thermal expansion | $3.4 \times 10^{\circ}$ KIN/IIIII 10 µM/m°C | |
| $R =$ incrimat conductivity41.0 w/m CPrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at service)$ $0.6 - 0.75 f_{ck}$ $f_{mas}(at service)$ $0.6 f_{max} = P_o transfer force : see cataloguesfor excurate assessment$ | K = thermal conductivity | $10 \mu W/m^{\circ}C$ | |
| TrestressReference is made to the manufacturer's catalogues for various systems $f_{mas}(at \ service)$ $0.6 - 0.75 f_{ck}$ $f_{mas}(at \ service)$ $0.6 f_{max} = P_o \text{transfer force : see catalogues}for exervice second seco$ | R – thermal conductivity | HI.U W/III C Deference is made to the manufacturer's | |
| $f_{mas}(at \text{ service})$ $f_{mas}(at \text{ service})$ $f_{mas}(at \text{ service})$ $0.6 - 0.75 f_{ck}$ $0.6 f_{max} = P_o \text{transfer force}$: see catalogues $f_{or excutation of the second s$ | 110311033 | catalogues for various systems | |
| $f_{max}(at service)$ $0.6 - 0.73/ck$ $f_{max}(at service)$ $0.6f_{max} = P_o transfer force : see catalogues$ $f_{or severate assessment}$ | f (at service) | $0.6 = 0.75f_{\odot}$ | |
| $f_{mas}(at service) = 1_0 transfer role . see catalogues for systems for accurate assessment$ | f (at service) | $0.6f_{\text{max}} = P_{\text{transfer force}}$: see catalogues | |
| | Jmas (at service) | for systems for accurate assessment | • |

| Se | rvice load parameters and stres | ses | | |
|----|--|---|---|----------|
| Lo | oads or stresses | Design load or range o | f actions | Notation |
| 1. | Structural steel based on EC-3 (a) Conventional steel design, load | | | |
| | Dead load | $1.46G_{\rm b}$ or $Y_{\rm c}E_{\rm b}$ | | D |
| | Dead load + restraining overturning | $1.0G_k$ | | D |
| | Dead + imposed load Dead + imposed + wind E'_{c} recent version F_{d} design action | $\frac{1.4G_{k} + 1.6Q_{k}}{1.2(G_{k} + Q_{k} + W_{k})}$ | | |
| 2. | Structural steel Euro codes-3 (EC-3) | $\gamma_G = 1.35: \gamma_Q = 1.5$ | | |
| | (a) Grade shapes S275 | $F_y = design strength$ | $f_y = stress, N/mm^2$ | Grade S |
| | \$355 | $F_{e}430 \le 16$ ≤ 40 $F_{510} \le 16$ | 275 275 355 | |
| | 6555 | ≤ 40 | 355 | |
| | (b) Quenched tempered plates | $f_{\rm y} = 690 \text{ N/mm}^2$ | | |
| | (c) Alloy bars – tension members | $f_{\rm y} = 1030 \ {\rm N/mm^2}$ | | |
| | (d) High-carbon hard- drawn wires for cables | $f_{\rm y} = 1700 \ {\rm N/mm^2}$ | | |
| 3. | Load and resistance factor design (LRFD) (a) The design strength must equal or exceed the required strength <i>R</i>_u (b) Required strength and load combination for LRFD based on ASCE-7 Section 2.3 | $R_{\rm u} \le \omega R_{\rm n};$ $R_{\rm n} =$ safe working loa $R_{\rm n} =$ normal strength LRFD load combinati $\emptyset =$ Resistance factor g Specification for a part 0.5 | d × safety factor determined ons given by the cicular limit state | Ø |
| | | 1.4D 1.2D + 1.6L + 0.5(L_r or 1.2D + 1.6 (L_r or S or 1.2D + 1.6 (L_r or S or 1.2D + 1.6 W + 0.5L + 1.2D ± 1.0E + 0.5L + 0.9D ± (1.6 W or 1.0E) D = dead load L = live load due to occ L_r = roof live load S = snow load R = nominal load due to rainwater or ice W = wind load E = earthquake load | or S or R) R + (0.5L or 0.8 W) $0.5 (L_r \text{ or } S \text{ or } R)$ 0.2S o initial | |

 Table 2.3
 Structural steel

| Loads or stresses | Design load or range of actions | Notation |
|---|--|----------|
| (c) Simplified determination of required strength based on LRFD. Based on effective length method where P-δ factor is small | $LRFD$ $M_{\rm r} = B_1 M_{\rm m} + B_2 M_{\rm u} = B_2 M_{\rm u}$ $P_{\rm r} = P_{\rm nt} + B_2 P_{\rm it} = B_2 P_{\rm u}$ $B_1 \le 1.05 \not> B_2$ $B_2 > 1.5 \text{simplified method is not valid}$ $\frac{\triangle 2nd}{\triangle 1.5}$ $\text{storey gravity load} = \text{minimum } 2\%$ $K = 1 \text{ for braced frame}$ $K \text{ value to be determined}$ for moment frames using | Δ |
| (d) Stability design | sideway buckling analysis or $P_r \le 0.5P_y$; $\alpha = 1.0$ for LFRD P_r = required axial compressive strength P_v = member yield strength = AF_v | |
| (e) The required compressive strength contributing to stability (lateral) by flexural stiffness(f) Pin connected members i. Tensile strength | $P_{n} = 2tb_{\text{eff}}.F_{u} \qquad \theta_{r} = 0.75 \text{ for LFRD}$ $P_{n} = 0.6F_{u}A_{\text{sf}}; \qquad A_{\text{sf}} = 2t(a + d/z)$ $a = \text{shorter distance from}$ $the edge in mm$ $d = \text{pin diameter in mm}$ $t = \text{place thickness in mm}$ $b_{\text{eff}} = (2t + 16 \text{ mm})$ | |
| ii. Shear rupture | <i>Note</i> : For complete design specifications, a reference is made to steel construction manual (AISCE) 13th edition Dec 2005 ISBN 1-56424-055x or forward editions | |

 Table 2.3 (continued)

| Service load parameters a | nd stresses | |
|--|---|----------|
| Aluminium structures | | Notation |
| Aluminium structures | | |
| Characteristic values based on Euro code-9 | | |
| $f_{\rm u}$ = ultimate strength $f_{\rm o}$ = 0.2% proof strength | $L = \text{longitudinal} = 310 \frac{N}{\text{mm}^2}$ Temper T6 $T = \text{transfer} = 260 \text{ N/mm}^2$ A = minimum elongation = 6%: Buckling class A | |
| (a) Alloy EN-AW 6082 100 mm thickness | $E = 74,000 \text{ N/mm}^2$ $G = 27,000 \text{ N/mm}^2$ $v = \text{Poisson's ratio} = 0.3$ $\alpha = \text{coefficient} = 23 \times 10^{-6} \text{ per }^\circ C \text{ of linear expansion}$ | |
| (b) 6061 | $P = \text{unit mass} = 2700 \text{ kg/m}^2$ T6/T651 thickness < 12.5 $f_o = 110 \text{ N/mm}^2$ $f_u = 205 \text{ N/mm}^2$ | |
| (c) Bolts for 6082 T6 aluminium alloy | $A_{so} = 12$ dia ≤ 6 $f_o = 250 \text{ N/mm}^2$ $f_u = 320 \text{ N/mm}^2$ | |

| Service load parameters and stresses | | | |
|---|---|-----------------|--|
| Loads or stresses | Design load or range of actions | Notation | |
| Structural composites based on EC-4 | | | |
| (a) Design parameters $b_{\rm e}$ $b_{\rm e}$ = effective breadth | | | |
| L_z = distance between points of zero moment | $L_{\rm z}/8 \not>$ half the distance of adjacent beam | b _e | |
| Concrete slab stress | 0.45 <i>f</i> _{ck} | | |
| Steel stress | $0.95f_{\rm y}$ | | |
| $p_v =$ shear capacity <i>Moment</i> | | $P_{ m v} M$ | |
| $M_{\rm api.RD} > M_{\rm cd}$ Moment resistance of the steel beam | $W_{\rm pl}f_{\rm d}$ | | |
| $R_{\rm c} = $ compressible resistance of slab | $0.85 f_{ m ck}/\gamma_{ m c} \times b_{ m eff} \times b_{ m c} = 0.45 f_{ m ckx} b_{ m eff} b_{ m c}$ | $R_{\rm c}$ | |
| $f_{ck} = \text{concrete cylindrical}$ | $0.85f_{cu}$ or $0.8f_{k(cu)}$ $v_{e} = partial safety factor = 1.5$ | $f_{\rm ck}$ | |
| $R_{\rm s} = {\rm compressive \ resistance}$ of steel section | $f_{\rm d}$ $A_{\rm a}$ | $M_{\rm pl,Rd}$ | |
| $M_{\rm pl.Rd}$ = moment or resistance of composite beam | $R_{\rm s}\left[\frac{h}{2}+h_{\rm c}+h_{\rm p}-R_{\rm s}^{h_{\rm c}}/2R_{\rm c}\right]$ | | |
| $V_{\rm pl.Rd} =$ shear resistance | $\frac{f_{\rm y}A_{\rm v}}{(r_{\rm a}\sqrt{3})}$ $0.5V_{\rm pLRD} > V_{\rm s}d$ | | |
| Shear connector | pinto | | |
| Failure of concrete | | | |
| $P_{\rm Rd}$ | $0.29\alpha d^2 \sqrt{Cf_{\rm ck}E_{\rm c}\gamma_{\rm r}}$ | | |
| | or $R_{\rm d} = \frac{0.8 f_{\rm u} \pi d^2}{4 \gamma_{\rm v}}$ shear failure of the steel at its weld | | |

 Table 2.5
 Structural composites

available, the data given in this chapter shall be adopted by individual clients or their consultants. Tables 2.1, 2.2, 2.3, 2.4 and 2.5 give data on service load parameter and relevant acceptable stresses for the design of conventional structures for nuclear facilities, within the USA. In addition the Euro codes are mentioned for the design of conventional structures called ancilliary or auxiliary structures associated with nuclear facilities. Loads (actions) and stresses are tabulated from the US and the European codes. For detailed design a reference is made to the relevant codes where necessary.

2.2 Loads

2.2.1 Service Loads

Service load conditions are those loadings encountered during construction and in the normal operation of nuclear power facilities. A suggested summary of the list of loads is given below.

2.2.1.1 Dead Load (D)

Dead load is vertical load due to the weight of all permanent structural and nonstructural components of a building, such as walls, floors, roofs and fixed service equipment as specified by the relevant codes and standards such as BS6399.

2.2.1.2 Operating Live Load (L)

Live load is the load superimposed by the used and occupancy of the building not including the wind load, earthquake load and impact load as specified by the relevant codes and standards.

2.2.1.3 Uniformly Distributed Loads (LL)

The live load is to be assumed in the design of building and other structures shall be the largest loads that can be expected to be produced by the intended use or occupancy, but in no case shall be less than the minimum uniformly distributed unit loads specified by the relevant codes and standards such as BS6399-1 to 3 or EC2, EC3.

2.2.1.4 Concentrated Loads (L_c)

Floors shall be designed to support safely a concentrated load simultaneously with the floor live loads. In European codes it is termed as knife edge loads.

2.2.1.5 Railroad Support (C_E)

For design purpose Cooper's E-72 loading should be used unless otherwise specified by intended use, such as support spent fuel cask handling car or other heavy equipment.

2.2.1.6 Truck Support (H₂₀)

For design purposes, AASHO H-20-S16 loading should be used unless otherwise specified by intended use. The equivalent European track load can also be adopted instead.

2.2.1.7 Ordinary Impact Loads (I)

Machinery

The weight of machinery and moving loads should be increased to allow for impact. Some suggested values are 100% for elevator machinery; 20% for light machinery, shaft or motor driven; 50% for reciprocating machinery or powerdriven units. All percentages should be increased or decreased as required by the design specification or manufacturer's recommendation.

Craneways

It is suggested that all craneways have their design loads increased for impact as follows: A vertical force equal to 25% of the maximum wheel load; a lateral force equal to 20% of the weight of trolley and lifter load only, applied one-half at the top of each rail; and longitudinal force of 10% at the maximum wheel loads of the crane applied at the top of rail. All percentages shall be increased or decreased if so recommended by the manufacturer or if otherwise specified by governing codes.

2.2.1.8 Construction Loads

Consideration shall be given to temporary large, heavy loads based on the 'Building Codes Requirements for Minimum Design Load in Building and Other Structures' (ANSI A58.1-1972)[1]. These provisions specifically exclude consideration of tornadoes. For extreme loads due to tornadoes, Section 3.3.2 should be referred to. Account should be taken of hurricane winds by comparison with the provisions of Section 3.3.3 for hurricane-susceptible sites. While using European codes a reference is made to BS6399, part 2 and Eurocode ENV1991-2-4 for wind loading. Table 2.1 part IX gives a brief relevant equation for the determination of loads caused by the wind.

2.2.1.9 Snow Loads (S)

Basic snow load requirements as a function of geographical area can also be found in ANSI Standard A58.1972. Table 2.1 gives a brief based on European code BS 6399-2-4.

Soil and Hydrostatic Pressure (E_p) and Buoyancy (B)

In designing nuclear facilities which are partly or wholly below grade, provision shall be made for the lateral pressure of adjacent soil, namely active pressure and at-rest pressure. The effect of dynamic pressure due to earthquake also should be given consideration. Due allowance shall be made for possible surcharge from fixed or moving loads. When a portion or the whole of the adjacent soil is below a free-water surface, computations shall be based on the weight of the soil diminished by buoyancy plus hydrostatic pressure. In the design of slabs below grade, the upward pressure of water, if any, shall be taken as the full hydrostatic pressure applied over the entire area. The hydrostatic head shall be measured from the underside of the slab. These are recommended also by the Nuclear Regulatory Commission (NRC) and ASCE of the USA.

Piping Equipment Reaction Load (R_0)

Piping system is attached directly to building structures through hangers, struts, restraints, anchors and snubbers. Hangers and struts are unidirectional, transmitting loads in one direction only. Hangers transmit only vertical loads. Restraints will transmit loads in any one or more of the coordinate directions. Anchors are capable of transmitting loads and moments in all three coordinate directions. Snubbers are unidirectional and transmit dynamic loads only.

Equipment loads include dead weight, restrained thermal expansion and dynamic effect such as pressure transients, changes in momentum, water and steam hammer in the equipment and earthquake. They also may include the effect of the restraint of attached piping. The effect of such phenomena must be considered in the design check.

Operating Pressure and Temperature (P_0, T_0)

In many cases compartments or sub-compartments within a structure which house highly radioactive pipes or equipment are maintained at lower pressure than the outside of the compartment in order to prevent out-leakage. Even though the differential pressure is not considerable, the magnitude should be determined and its effect evaluated particularly for steel structures which are more likely to experience external pressure buckling modes of failure.

2.2.2 Operating Basis Earthquake (E_o)

The respective nuclear organisation and regulatory commissions have criteria for the seismic design of nuclear power plants. The Operation Basis Earthquake (OBE) does consider the effect on a plant site during the operational life of the plant. Both local geology and seismology are related to specific characteristics of local subsurface materials.

Earthquakes can cause local soil failure, surface ruptures and structural damage of nuclear power plants. The most significant earthquake effects on plants or their structural components result from the seismic waves which propagate outwards in all directions from the earthquake focus. These different types of waves can cause significant ground movements up to several hundred miles from the source. The movements depend upon the intensity, sequence, duration and the frequency content of the earthquake-induced ground motions. For design purposes ground motion is described by the history of hypothesised ground acceleration and is commonly expressed in terms of response spectrum derived from that history. When records are unavailable or insufficient, smoothed response spectra are devised for design purposes to characterise the ground motion. In principal, the designers describe the ground motions in terms of two perpendicular horizontal components and a vertical component for the entire base of the nuclear power plants. A 3D analysis is essential using hybrid finite element non-linear method.

When the history of ground shaking at a particular site or the response spectrum derived from this history is known, plants' theoretical response can be calculated by various methods; these are described later.

The minimum acceptable acceleration for the OBE will be taken at least onehalf of the Safe Shutdown Earthquake (SSE) acceleration. Sometimes OBE < SSEhave been permitted in some cases where SSE return period is such duration as not to be reasonably expected during the life of the nuclear power plant. If the vibratory ground acceleration of the site is equal to or greater than OBE acceleration, the US Federal Regulation makes it mandatory to shut the nuclear power plant for inspection.

2.2.2.1 Response Spectra

The main cause of the structural damage during earthquake is its response to ground motion which is in fact input to the base of the structure. To evaluate the behaviour of the plant under this type of loading condition knowledge of structural dynamics is required. The static analysis and design can now be changed to separate time-dependent analysis and design. The loading and all aspects of response vary with time which result in an infinite number of possible solutions at each instant during the time interval. For a design engineer the maximum values of the plant response are needed for the structural design.

The response may be deflection, shear, equivalent acceleration, etc: the response curves are generally similar with majority variations occurring in the vertical coordinates. The variation occurs with magnitude of the earthquake and the location of the recording instruments. Accelerations derived from actual earthquakes are surprisingly high as compared with the force used in designs and the main reason is the effect of different degrees of damping.

The recorded earthquake ground accelerations have no doubt similar properties to those of non-stationary random functions but owing to a lack of statistical properties related to such motions artificially generated accelerograms are used which are flexible for any duration.

The following three major aspects must be considered:

- (a) Location of vibratory ground motion for OBE
- (b) Direction of motion for OBE
- (c) Vertical Acceleration associated with OBE

This book covers all aspects in detail when earthquake analysis of nuclear plant is considered. The reader is advised to examine the author's book on *Earthquake-Assistant Buildings* published by Springer-Verlag, Germany (2010) particularly using analyses and loadings with and without seismic devices.

2.2.3 Extreme or Severe Loads

These loads include extreme environmental conditions, such as tornadoes and the safe shutdown earthquake postulated to occur during the life of the facility. Also included are effects resulting from a postulated rupture of a high-energy system during normal operation, startup or shutdown of the plant or other postulated design basis accident.

2.2.3.1 Safe Shutdown Earthquake (E^1)

The Nuclear Regulatory Commission's Federal Regulation 10 CFR 100 Appendix A, entitled 'Siesmic and Geology Siting Criteria for Nuclear Power Plants' sets forth principal seismic and geological considerations which shall be used by the Commission in its evaluation of the suitability of proposed sites for nuclear power plants. Contained within this Appendix are definitions and procedures which are to be used as guidelines in establishing the various seismic input motion and potential faulting hazard for nuclear power plants, in the USA. Specifically, the safe shutdown earthquake (SSE) is defined as that earthquake which produces the vibratory ground motion for which structures, systems and components are important for safety of the structures or systems.

Required Investigations

Paragraph IV entitled 'Required Investigations.' in Appendix A of 10 CFR 100 sets forth the required geologic and seismic investigations that should be carried out to establish vibratory ground motion requirements and surface faulting. Sub-paragraph A entitled 'Required Investigation for vibratory Ground Motion' sets forth the specific investigations that should be carried out to establish the ground motion input associated with the SSE. Briefly, the items that should be considered to establish the ground motion input associated with SSE are as follows:

- 1. geologic conditions at the site;
- 2. tectonic structure determination;
- 3. identication of effects of prior earthquakes;
- 4. determination of static and dynamic characteristics of underlying materials;
- 5. historical listings of all earthquakes which may have affected the site;
- 6. correlation of epicentre;
- 7. determination of fault locations;
- 8. characteristics of faults in the vicinity.

Locations of Vibratory Ground Motion for SSE should be considered to be acting at the ground surface in the free field. The maximum acceleration of the vibratory ground motion for the SSE should be considered on the basis of evaluating the result of the investigation as stated above required investigation. The guideline shall be on this maximum acceleration as the largest possible acceleration at the site due to a postulated fault activity.

The direction of motion for SSE shall generally be assumed as resultant motion to correspond with one of the principal horizontal directions of the structure for the facility being analysed.

The vertical motion associated with SSE can be established on the basis of the information developed from the above-mentioned investigation. The value should not be less than 2/3 of the maximum horizontal ground acceleration of the SSE. The frequency strength is between 3.5 and 33 Hz. The vertical acceleration shall be equal in intensity to the horizontal component.

2.2.3.2 Tornado Loads (W_t)

Structures for the nuclear facility shall be designed to resist the maximum tornado load for a given plant site. The basis of the design shall be such that the safety class equipment remains functional; even a safe shutdown of the facility is accomplished in totality without endangering the plant. The AEC Regulatory Guide 1.76 recommends the design basis tornado.

The effects of a tornado that are manifested in structural damage are generated from three separate phenomena: wind, differential atmospheric pressure and missiles. These effects interact with structures and cause damage through three principal mechanisms:

- 1. pressure forces created by drag and lift as air flows around and over structure;
- 2. pressure forces created by relatively rapid changes in atmospheric pressure resulting in differential pressure between the interior and exterior of the building;
- 3. penetration, spalling and impact forces created by missiles.

Tornado missiles (Y_m) : Tornado-generated missiles carry objects which are accelerated by the forces induced by the extreme wind speeds of the tornado. The parameters specified in the design basis tornado are translated into pressures and forces acting on the structures and its components. The important case is the real analysis that would be necessary to perform on the structure. The analysis is known as tornado structure interaction. In this analysis the load evaluated using a specific path width of the tornado field that experiences wind velocities \geq 75 mph (120 km/h) is generally considered.

2.2.3.3 Hurricane Loads

A hurricane by definition is a cyclone storm having rotational wind velocities in excess of 70 mph (119 km/h). The dynamic strength of a hurricane builds up over water, but as it comes inland boundary layer drag forces cause a tremendous dissipation of the kinetic energy of the storm and the wind.

As regards wind distribution which is one aspect of hurricane loads, the maximum wind velocities generally occur to the right of the eye of the hurricane looking along the direction of its path. This is due to vectoral addition of the translational and rotational components of the wind. The following data can be adopted in the absence of specific data not available for the site under consideration:

- 1. $\alpha =$ Inclination of the direction of the wind = 20-30° (towards the centre of the hurricane)
- 2. Wind gust > the sustained wind by 30-50%
- 3. Hurricane diameter: 15 miles (24 km) to 100 miles (160 km)
- 4. Gale force wind: 40 mph (64 km/h occurring within 30 miles (560 km) to 400 miles (640 km)

Where sea swell surge and flooding occur, specific calculations would be required to algebraically evaluate the additional load occurring when considered along with other loads.

2.2.3.4 Tsunami Loads

Tsunami are long ocean water waves generated by mechanisms such as earthquakes or underwater explosions, which impinge on coastal areas. With regard to earthquakes tsunami appeared to be primarily associated with those tectonic movements having substantial vertical components of motion (dip-slip). The design of nuclear facilities to resist the effects of tsunami must be undertaken for all nuclear site adjacent to coastal areas, especially those bordering the Pacific Ocean. The basic criteria for tsunami are set forth in the NRC's Standard Format and the Contents of Safety Analysis Reports for Nuclear Power Plant. These silent feature must be known such as the

- (i) Location relevant to the site
- (ii) Magnitude
- (iii) Tsunami wave height
- (iv) Influence of harbour/break water and hydrography
- (v) Records of the region with valuable statistics

The direct dynamic force of the moving tsunami wave impinging against structures of power facilities shall be algebraically added to the force produced due to the impact of the floating debris and water-borne missiles.

2.2.3.5 Missile Load (Ym)

In nuclear facility design, safety class structures shall be protected against loss of functions due to postulated plant generated and extreme environmental missiles depending on aircraft crash should be considered.

The effect of missile impact on a target on the material and geometric properties of the impacting bodies. The phenomenon can be described in general as the formation of an impulse measured by the momentum exchange between the two bodies during the impact. Table 2.6 gives data on tornado and wind-generated missiles.

| Service load parameter and str | Service load parameter and stresses | | | | |
|---|-------------------------------------|---------------|-------------------------------|-------------------|----------------|
| | Ge | cometry | | | |
| Missile type | Diameter (mm) | Length (m) | Impact area (m ²) | Velocity (m/s) | Weight (kg) |
| Wooden plank | _ | 3.67 | 0.03 | 41.5 | 56.7 |
| Wooden pole | 200 | 3.67 | 0.03 | 5.73 | 94.8 |
| Circular | 168.3 | 4 | 0.000026 | 70.2 | 60 |
| hollow sections in steel (average) | | | | | |
| Sign boards (average) | _ | - | 6.0 | 57 | 56 |
| Steel I-beam light sections (average) | _ | 4 | 0.000032 | 40.5 | 100 |
| Steel members channel sections (average) | — | 3 | 0.000013 | 50.5 | 30 |
| Steel members | _ | 3 | 0.000015 | 45.5 | 36 |
| L-sections (average) | | | | | |
| Steel rafters | _ | 3 | 0.000018 | 45.5 | 42 |
| T-sections (average) | | | | | |
| Steel rod | 25 | 0.92 | 0.00049 | 75.6 | 3.63 |
| Concrete lintels | _ | 3 | 0.025 | 60.5 | 1.8 |
| Concrete sleepers | _ | 2.7 | 0.0031 | 75 | 0.2 |
| Precast concrete beams or piles at delivery stage | | 9 | 0.09 | 60.5 | 19.44 |
| Precast concrete wall panels | | 5 | 11.5 | 2.5 | 1380 |
| Prestressed | 400 | - | _ | - | 1.1 |
| concrete pipes | 500 | - | _ | - | 1.375 |
| | 600 | - | _ | - | 1.65 |
| | 700 | - | _ | - | 1.92 |
| | 800 | - | _ | - | 2.2 |
| | 900 | - | — | - | 2.474 |
| | 1676 | 6 | 0.032 | - | 4.608 |
| Prestressed | _ | 17 | 0.0019 | 30.5 | 65.7 |
| concrete poles | | 12 | 0.0008 | 50.1 | 14.46 |
| | | 9 | 0.000025 | 65.2 | 9.65 |

 Table 2.6 Tornado and wind-generated missiles and their characteristics: wood, steel and concrete building components

Missiles are usually classified by source as plant (accident)-generated missile and extreme environmental missiles. Typical plant-generated missiles include valve stems, valve bonnets, (caused by rupture of high-energy systems) and turbine discs and other rotating masses (caused by rupture of rotating parts). Extreme environmental missiles which are of major concern include tornadogenerated missile and aircraft.

Table 2.7 gives a list of plant-generated missiles and their characteristics. They depend on their region, ranges of size, weight and impact velocity.

Tables 2.8, 2.9, 2.10, 2.11, 2.12, 2.13, 2.14 and 2.15 give various aircraft parameters and their characteristics and impact parameters.

| Service load parameters and stress | es | | |
|------------------------------------|-------------|--------------------------------|----------------|
| Missile type | Weight (kg) | Impact area (cm ²) | Velocity (m/s) |
| Control rod mechanism or fuel | 53 | 15.5 | 91.5 |
| Disc 90° sector | 1288 | 495 | 125 |
| Disc 120° sector | 1600 | 6573 | 156 |
| Hexagon head bolts | | | |
| 1.4 cm dia | 0.20 | 1.54 | 250 |
| 2.0 cm dia | 0.30 | 2.30 | 230 |
| 2.4 cm dia | 0.37 | 2.84 | 189 |
| 3.3 cm dia | 0.42 | 3.22 | 150 |
| 6.8 cm dia | 0.97 | 7.44 | 100 |
| Turbine rotor fragments | | | |
| High trajectory | | | |
| Heavy | 3649 | 5805 | 198 |
| Moderate | 1825 | 3638 | 235 |
| Light | 89 | 420 | 300 |
| Low trajectory | | | |
| Heavy | 3649 | 5805 | 128 |
| Moderate | 1825 | 3638 | 162 |
| Light | 89 | 420 | 244 |
| Valve bonnets | | | |
| Heavy | 445 | 851 | 79 |
| Moderate | 178 | 181 | 43 |
| Light | 33 | 129 | 37 |
| Valve stems | | | |
| Heavy | 23 | 25 | 37.5 |
| Moderate | 14 | 9.7 | 20 |
| Others | | | |
| 30 cm pipe | 33.7 | 260 | 68 |
| 12 cm hard steel disc | 1.6 | 113 | 140 |
| Steel washer | 0.0005 | 3 | 250 |
| Winfirth test missile | 15.6 | 176 | 240 |

 Table 2.7
 Plant-generated missile and their characteristics

| Service load parameters and stresses | | |
|---|--|--|
| Data on civilian a | nd military aircraft | |
| Civilian aircraft normally in service includes C and Tupolov | Concorde, Airbus, Boeing, Antonov, Ilyushin | |
| S = span; $L = $ length; $H = $ heigh | nt; $A_{\rm w}$ = wing area; $P_{\rm L}$ = payload | |
| $V =$ speed; $W_{a} =$ weig | ht at take-off or loading | |
| Basic parameters of Concorde | | |
| Power Plant | | |
| $4 \times 38,050$ lb (169 kN) | | |
| Rolls-Royce/Si | neema Olympus | |
| 593 Mk60 two | -spool turbojet | |
| <i>S</i> (m) | 25.61 | |
| <i>L</i> (m) | 62.1 | |
| <i>H</i> (m) | 12.19 | |
| $A \sim (\mathrm{m}^2)$ | 358 | |
| $P_{1\sim}(\text{kg})$ | 11,340 | |
| V (km/h) | 2150 | |
| $w_{\rm a}$ (kg) 186,800 | | |

Table 2.8 Civilian sircraft

Tables 2.16, 2.17, 2.18, 2.19, 2.20, 2.21, 2.22 and 2.23 dictate again various military missiles with their characteristics and impact parameters.

For details and in-depth study references are made to the following authors:

- (a) Impact Explosion Analysis and Design, Blackwell, 1993.
- (b) Manual of Numerical Methods in Concrete, Thomas Tefford.
- (c) Shock, Impact & Explosion, Springer, 2008.

2.2.3.6 Design Basis Accident Load

In addition to accident-generated missile loads there are several loading phenomena generated as the result of a design basis accident which normally includes all postulated high-energy system ruptures. Included in this category are all accident-induced pressure and temperatures, as well as high-energy fluid jet impingement and rupture reaction loads. The criteria for defining design basis high-energy system ruptures are found in the NRC Standard Review Plan.

Accident Pressure (P_a) and Temperature (T_a)

These pressures and temperatures are typically developed as a result of the blowdown of a high-energy system into a confined space. They typically include the containment design pressure and temperature as well as differential pressure and temperature across interior partitions or structures which house ruptured high-energy systems.

| | Table 2.9 (| a) Data on the | : Airbus famil | y and (b) data | for Antonov a | aircraft | | |
|---|-------------|----------------|----------------|----------------|------------------|------------------|--------|-------------|
| | | S | Г | Н | A_{w} | P_{L} | Δ | $W_{\rm a}$ |
| Type Power plant | | (m) | (m) | (m) | (m^2) | (kg) | (km/h) | (kg) |
| (a) Data for Airbus family A300B2-100 2×51,000 lb (227 kN) | | | | | | | | |
| GE CF6-50C | | 44.84 | 53.75 | 16.53 | 260 | 14,900 | 869 | 34,585 |
| turbofans | | | | | | | | |
| A300B2-200 2×51,000 lb (227 kN) | | | | | | | | |
| GE CF6-50C | | 44.84 | 53.57 | 16.53 | 260 | 34,585 | 869 | 142,900 |
| turbofans | | | | | | | | |
| A300B2-l00 2×51,000 lb (227 kN) | | | | | | | | |
| GE CF6-50C | | 44.84 | 53.57 | 16.53 | 260 | 35,925 | 869 | 158,400 |
| turbofans | | | | | | | | |
| A300B4200 2×52,500 lb (233.5 kN) | | | | | | | | |
| CF6-50C1 | | 44.84 | 53.57 | 16.53 | 260 | 35,600 | 869 | 165,900 |
| turbofans | | | | | | | | |
| A310202 2×48,000 lb (218 kN) | | | | | | | | |
| GE CF6-80A | | 13.9 | 46.66 | 15.8 | 219 | 32,400 | 780 | 132,000 |
| turbofans | | | | | | | | |

2.2 Loads

| | | | Table 2.9 (col | ntinued) | | | | |
|----------------|---|-------|----------------|----------|-------------|------------------|--------|------------|
| | | S | Г | Н | $A_{\rm w}$ | P_{L} | Α | $W_{ m a}$ |
| Type | Power plant | (m) | (m) | (m) | (m^2) | (kg) | (km/h) | (kg) |
| (b) Antonov | / aircraft | | | | | | | |
| An-12 | 4 	imes 4000 ehp Ivchenko | | | | | | | |
| | A1-20 K turboprops | 38 | 37 | 9.83 | 119.5 | 10,000 | 550 | 54,000 |
| An-22 | 4×15000 ehp Kuznetsov | | | | | | | |
| | NK-12MA turboprops | 64.4 | 57.8 | 12.53 | 345 | 80,000 | 679 | 250,000 |
| An-24 | 2×2500 ehp Ivenchenlko | | | | | | | |
| | A1-24 Seviiny 11 | | | | | | | |
| | turboprops | 29.2 | 23.53 | 8.32 | 74.98 | 13,300 | 450 | 21,000 |
| $An{\sim}26^*$ | 2×2800 ebp Ivenchenko | | | | | | | |
| | A1-24T turboprops | 29.4 | 23.8 | 8.575 | 74.98 | 5500 | 435 | 24,000 |
| An-28 | 2×970 ehp Glushenkov | | | | | | | |
| | TVD-10B turboprops | 21.99 | 12.98 | 4.6 | 39.72 | 1550 | 350 | 6100 |
| | (similar to An-14) | | | | | | | |
| An-72 | $2 	imes 14,330 	ext{ 1b} (6500 	ext{ kg})$ | | | | | | | |
| | Lotarev D-36 | | | | | | | |
| | turbofans | 25.8 | 26.58 | 8.24 | 74.98 | 7500 | 720 | 30,500 |
| An-30 and Ai | 1-32 have similar status to An-26 | | | | | | | |

| Table 2.10 (a) Data fo | r Boeing aircraft; (b) Data for the Ilyushin aircraft; a | and (c) I | ata foi | the T | upolev se | eries of a | aircraft | |
|------------------------------------|--|-----------|----------|-------|-----------|--------------------------|----------|-------------------------|
| Service load parameters and stress | es | | | | | | | |
| Tune | Downer nlant | (m) | (m) L | (m) | A_{w} | $P_{\rm L}^{(h,\alpha)}$ | (4/m4) | $W_{\rm a}^{(L\alpha)}$ |
| 1)pc (-) D E D | I OWEL PLAIL | (m) | (111) | (111) | (m) | (Su) | | (gy) |
| (a) Data for boeing aircraft | | | | | | | | |
| 727-200 | $3 \times 16000 \text{ lb} (71.2 \text{ kN})$ | 32.9 | 461 | 10.4 | 153.2 | 18,594 | 883 | 95,238 |
| | Fratt and Winniey JT8D-17 | | | | | | | |
| | turbofans | | | | | | | |
| 737-200 | $2 \times 16,000$ 1b (71.2 kN) | 28.3 | 30.5 | 11.4 | 91 | 15,422 | 775 | 53,297 |
| | Pratt and Whitney | | | | | | | |
| | JT8D-17 | | | | | | | |
| | turbofans | | | | | | | |
| 767 | $2 \times 44,300 \text{ 1b} (1.97 \text{ kN})$ | 47.24 | 48.46 | 15.38 | 200 | 40,224 | 800 | 128,030 |
| | Pratt and Whitney | | | | | | | |
| | JT9D-7R 4A | | | | | | | |
| | turbofans | | | | | | | |
| 757 | $2 \times 37400 \text{ 1b} (166.43 \text{ kN})$ | 37.95 | 47.32 | 13.56 | 181.25 | 71,530 | 899 | 29,8880 |
| | Rolls-Royce | | | | | | | |
| | RB211-535C | | | | | | | |
| 747-200 B | $4 \times 50,000 \text{ lb} (222 \text{ kN})$ | 59.6 | 70.5 | 19.3 | 512 | 71,530 | 907 | 366,500 |
| | Pratt and Whitney | | | | | | | |
| | JT9D-7F (wet) | | | | | | | |
| | turbofans | | | | | | | |
| 747-200B | $4 \times 53,000 \text{ lb} (236 \text{ kN})$ | 59.6 | 70.5 | 19.3 | 512 | 69,900 | 907 | 373,300 |
| | Pratt and Whitney | | | | | | | |
| | JT9D-7Q | | | | | | | |
| | turbofans | | | | | | | |
| 747-200 B | $4 \times 52,500 \text{ lb} (234 \text{ kN})$ | 59.6 | 70.5 | 19.3 | 512 | 69,080 | 907 | 373,300 |
| | General Electric | | | | | | | |
| | CF6-50E2 | | | | | | | |
| | turbofans | | | | | | | |
| 767-200B | $4 \times 52,500 \text{ lb} (234 \text{ kN})$ | 76.65 | 70.5 | 19.3 | 512 | 69,080 | 907 | 373,300 |
| | General Electric | | | | | | | |

2.2 Loads

| | Table 2.10 (continued) | | | | | | | |
|---|---|------------|---------------|-----------|-----------------------------|---------------------|-------------|------------------|
| Service load parameters and stress | se | | | | | | | |
| Type | Power plant | S (m) | L (m) | (m) | $\stackrel{A_{w}}{(m^{2})}$ | $P_{\rm L}^{}$ (kg) | V (km/h) | $W_{\rm a}$ (kg) |
| 747-100B | CF6-50E2 turbofans 4 × 52,500 lb (234 kN) General Electric CF6-50E2 turbofens | 65.0 | 70.71 | 19.18 | 512 | 69,080 | 206 | 373,300 |
| (b) Data for Ilyushin aircraft Ilyushin II-18 | $4 \times Ivenchenko A1-20 M$ | 37.4 | 35.9 | 10.17 | 140 | 14,000 | 625 | 64,000 |
| Ilyushin II-62 | turboprops 4250ehp $4 \times 25,000$ lb (l13kN) | 43.2 | 53.1 | 12.4 | 280 | 23,000 | 860 | 165,000 |
| Ilyushin II-76T | Solovier 20-30-KU turbofans 4× Solovier D.30KP turbofans. Each with | 50.5 | 46.6 | 14.76 | 300 | 40,000 | 850 | 157,000 |
| Ilyushin 11-86 | 20,455 ID St (120,00 kg) 4 × Kuznetsov turbofans, each with 28,635 Ib St each with 28,635 Ib St | 48.06 | 59.5 | 15.81 | 320 | 42,000 | 006 | 206,000 |
| (c) Data for Tupolev aircraft | 2×21,385 lb (97 kN) Mikulin AM 3M500 | 3454 | 25.85 | 11.9 | 174.4 | 006 | 800 | 76,000 |
| TU-124 TU-134 | turbojet 2 × 11,905 lb (54 kN) Soloviev D-20P turbofans 2 × 15 000 lb (66 5 kN) Soloviev D-30 turbofans | 25.5 29 | 30.58 34 9 | 8.08 9 | 1.19 | 3500 77 000 | 800 849 | 26,300 45 200 |
| TU-144 | 4×44,000 lb St | 28.8 | 6K7 | 12.85 | 438 | 14,000 | 2500 | 180,000 |
| TU-154) | (20,000 kg) with Kuznetsoy NK-144 turbofans 3 × 21,000 lb (93.5kN) Kuznetsov NK-8-2 turbofans | 37.5 | 48 | 11.4 | 202 | 20,000 | 006 | 91,000 |
| For 13767-200EH 46.55 48.46 16.1 For B747-400 65.00 70.71 19.18 Fc | 155 For other details, reference is made to this Chapter or other details, reference is made to this Chapter | | | | | | | |

Aircraft information

Boeing 767-200ER

General specifications

| Passengers Typical 3-class configuration Typical 2-class configuration Typical 1-class configuration | 181 224 up to 255 |
|--|---|
| Cargo | 2,875 ft ³ (81.4)m ³ |
| Engines' maximum thrust Pratt & Whitney PW4062 General Electric CF6-80C2B7F | £63,300 (28,713 kg) £62,100 (28,169 kg) |
| Maximum fuel capacity | 23,980 U.S. gallons (90,770 liters) |
| Maximum takeoff weight | £ 395,000 (179,170 kg) |
| Maximum range Typical city pairs: New York–Beijing | 6,600 nautical miles 12,200 km |
| Typical cruise speed at 33,000 ft | 0.80 Mach 530 mph (850 km/h) |
| Basic dimensions Wing span Overall length Tail height Interior cabin width | 156 ft 1 in. (47.6 m) 159 ft 2 in. (48.5 m) 52 ft (15.8 m) 15 ft 6 in. (4.7 m) |

FEDERAL EMERGENCY MANAGEMENT AGENCY Service load parameters and stresses

Note: This aircraft has been used in the Twin Tower collapse.

| | Table 2.12 Military aircraft | |
|--|--|--|
| Service load p | $S = \text{span}; L = \text{length}; H = \text{height}; A_w = \text{wing area}; P_L = 1$ parameters and stresses $V = \text{speed}; W_a = \text{weight at takeoff or loading}$ | ayload |
| | Data on the Tornado IDS and ADV aircraft Power plant Turbo-Union RB 199-34R (101 or 103) after burning turbofan MK 8090 lb (3670 kg) to 15,950 lb (7253 kg) after burning thrust | Air Defense Variant (ADV) As for IDS, with MK 104 |
| <i>S</i> (m) <i>L</i> (m) <i>H</i> (m) | 8.60 max swept 13.90 max unswept 16.67 5.95 | 18.68 5.95 |
| $egin{array}{l} A \sim ({ m m}^2) \ P_{1 \sim} ({ m kg}) \ V ({ m km/h}) \ w_{ m a} ({ m kg}) \end{array}$ | 9000 Mach 2 at high level Mach 1 at low level 28,000 | 9000 Mach 2.2 28,000 |
| Armament | 4× MK 13/15 1000 lb (454.74 kg) bombs 2 AIM-9L missiles 8 MK 83 retarded bombs 2 CBLS-200 practice bomb containers 4 Kormoram ASM 8 × BL755 cluster bombs | |
| | Basic parameters for the F-5E and F-20 aircraft Engine 2GEJ 85-21 Engine 5000 lb (2268 kg) thrust each | GEF404-GE100 1800 lb (8164 kg) thrust each |
| S (m) | 7.98 with missiles 8.53 without missiles | 8.5 with missile |

| Service load p | S = span; L = leng arameters and stresses $V = \text{spec}$ | gth; H = height; $A_{\rm w}$ = wing area; $P_{\rm L}$ = p. ed; $W_{\rm a}$ = weight at takeoff or loading | ayload | |
|---------------------------|--|--|--|--|
| <i>L</i> (m) | 14.45 | | 14.42 | |
| <i>H</i> (in.) | 4.07 | | 4.10 (4.73 with wheels) | |
| $A_{\rm w} ({ m m}^2)$ | 28.1 | | 27.5 | |
| P_1 . (kg) | 6350 | | 7263 | |
| V (miles/h) | 850 | | 1300 | |
| $W_{\rm a}.({ m kg})$ | 11,213.8 | | 12,700 | |
| Armament | Air-to-air 2 No. 20 mm guns and AIM 9 sid. Air-to-ground 2 No. 20 mm guns and 9 bom | ewinder missiles 1bs of 3020 kg | | |
| | Data on the F-110 series F-16A and F-16B | Data on the F-16 series of aircraft F-l6C and F-16D | F-16 N | TF-16 N |
| Power plant | Pratt and Whitney turbofan two shaft 24,000 lb (10,885 kg) thrust F100-PW- 100 | F100-PW-200F100-PW-200 F110- GE-100 25,000 lb (11,340 kg) thrust | F110-GE-100 25,000 lb (11,340 kg) thrust | F110-GE-100 25,000 lb (11,340 kg) thrust |
| <i>S</i> (m) | 9.45 | 9.45 | 9.895 | |
| | 10.01 | 10.01 | (without sidewinder) | |
| | (with sidewinder) | (with sidewinder) | | |
| <i>L</i> (m) | 14.52 | 15.03 | 15.1 | |
| H(m) | 5.01 | 5.09 | 5.1 | |
| A_{s} (m ²) | 27.87 | 2787 | 27.87 | |
| $P_{\rm L}$ (kg) | 33,000 1b (14,969 kg) | 37,500 lb (16,781 kg) | 37,500 lb (16,781 kg) | |
| V (mile/h) | 1300 | 1300 | 1300 | |
| $W_{\rm a}$ (kg) | 12,000 1b (5443 kg) | 12,430 1b (5638 kg) | 17,278 lb (7836 kg) | |

Table 2.12 (continued)

| Service load parameters and s | stresses | |
|-------------------------------|--|--|
| (a) Data on F-15 | Power p | lant |
| | 2 No. Pratt and Whitney F-100-PW-220 each with 24,000 lb thrust | |
| <i>S</i> (m) | 13.05 | |
| <i>L</i> (m) | 19.45 | |
| <i>H</i> (m) | 5.64 | |
| $A_{\rm w}\left(m^2 ight)$ | | |
| $P_{\rm L}$ (kg) | 7000 | |
| V (km/h) | 2500 | |
| $w_{\rm a}$ (kg) | 20,000 | |
| Armament | 4 AIM-9L/M infrared-guide 7F/M radar-guided Sparr range air-to-air missiles (Gatling gun with 940 rou Accommodates a full ran | ed Sidewinder missiles; 4 AIM- ow missiles: 8 advanced medium- AMRAAMs); M-61 20 mm nds of ammunition. ge of air-to-ground ordnance |
| (b) Data on F/A -18 Hornet | Pov | ver plant |
| | 2 No. F404-UF'-400 | - |
| | Low bypass turbofan engine thrust and with a thrust/w | es each in 1600 lb (70.53 kN) veight ratio of 8:1 |
| S (m) | 11.43 | |
| <i>L</i> (m) | 17.06 | |
| <i>H</i> (m) | 4.7 | |
| $A_{\rm w} (m^2)$ | 37.2 | |
| $P_{\rm L}$ (kg) | | |
| V (km/h) | 2700 | |
| $w_{\rm a}$ (kg) | 24,402 | |
| Armament | Up to 7711 kg maximum or sidewinder heat-seeking r air-to-ground ordnance; t radar-guided missiles, air nacelle fuselages for Spar centreline for weapons, se 20 mm cannon mounted i | a nine stations: two wing-tips for nissiles; two outboard wings for wo inboard wings for Sparrow -to-ground or fuel tanks; two row missiles or sensor pods: one ensor pods or tank. Internal in nose |
| (c) Data on F-14 Tomcat | Pov | ver plant |
| | F-14A | F-14B, C |
| | 2 × 20,900 lb (9480 kg) thrust Pratt and Whitney TF3O-1412A | $2 \times 28,090$ lb (12,741 kg) thrust Pratt and Whitney F401-400 |
| | Two shaft after-but | ming turbofans |
| <i>S</i> (m) | 11.630 (68° sweep) 19.54 (20° sweep) | Safely landing |
| <i>L</i> (m) | 18.89 | |
| $H(\mathbf{m})$ | 4.88 | |
| $A_{\rm w} ({ m m}^2)$ | | |

Table 2.13 (a) Data on the F-15; (b) data on the F/A-18 Hornet and (c) data for the Grumman F-14 Tomcat

| Service load parameters as | nd stresses |
|----------------------------|---|
| $P_{\rm L}({\rm kg})$ | 17010 |
| V (km/h) | Mach 2.3 or 1564 mph maximum speed 400–500 km/h cruise speed |
| w_a (kg) | 27216 |
| Armament | AIM-54 Phoenix missiles AIM-7 Sparrow missiles AIM-9 Sidewinder missiles |

 Table 2.13 (continued)

| Service lo | ad parameters a | nd stresses | | | |
|------------------------|---------------------|------------------------|--------------------------------------|---|---------------------------------------|
| Power | MIG-19 | | MIG-23 | MIG-25 | |
| plant | (Mikoyan) | MIG-21 | (Flogger) | (Foxbat) | MIG-27 |
| Engines | Single seater | Single seater | Single seater | Single seater | Single seater |
| | 2×600 lb | Range turbojet | 17,640 lb | 27,000 lb | 17,640 lb |
| | (3040 kg) | 11,240 lb (5100 kg) | (8000 kg) | (12,250 kg) | (800 kg) |
| | to 2×7165 lb | to | to | thrust, 2 | to |
| | (3250 kg) Kimov | 4150 lb (6600 kg) | 25,350 lb | Tumansky R-266 | 25,350 lb (11,500) |
| | RD-39B turbojets | Tumanskey | (11,500 kg) | after- burning | thrust, 1- |
| | | single shaft | thrust, 1 Tumansky turbofan | turbojets | Tumansky after-burning turbofan |
| <i>S</i> (m) | 9 | 7.15 | 8.7 (72°sweep) 14.4 (16 sweep) | 14 Foxbat A | 8.7 (72°sweep) 14.4 (16 sweep) |
| <i>L</i> (m) | 13.08 (S-5F) | 14.35 | 16.15 | 22.3 (Foxbat A) 22.7 (Foxbat R) 23.16 (Foxbat U) | 16.5 |
| <i>H</i> (m) | 4.02 | 4.5 | 3.96 | 5.6 | 4.6 |
| $A_{\rm w}({\rm m}^2)$ | | | | | |
| $P_{\rm L}({\rm kg})$ | 3760 | 4600 | 7050 | 14,970 | 9900 |
| V | Mach 1.3 or | Mach 2.1 or | Mach 1.1 or | Mach 3.2 or | |
| (km/h) | 1480 km/h | 2070 km/h | 1350 km/h | 3380 km/h | |
| | (92 mph) | (1285mph) | (840 mph) | (2100 mph) | |
| $w_{\rm a}$ (kg) | 9500 | 9800 | 15,000 | 34,930 | 17,750 |

| Service load param | eters and stresses |
|-------------------------|--|
| | Power plant |
| | 2 No. Rolls-Royce Terbomeca Adour two shaft turbofans 7305 lb (3313 kg) to 8000 lb (3630 kg)thrust |
| <i>S</i> (m) | 8.69 |
| <i>L</i> (m) | 15.4–16.42 |
| $H(\mathbf{m})$ | 4.92 |
| $A_{\rm w} ({\rm m}^2)$ | |
| $P_{\rm L}$ (kg) | 6800 |
| V (km/h) | 1450 |
| $w_{\rm a}$ (kg) | 1550 |
| Armament and | 2 No. 30 mm DFA 553 each with 150 rounds |
| other data | 5 No. pylons with total external loads of 4536 kg with guns |
| | 2 No. 30 mm Aden for its T-2 model |
| | Matra 550 Magic air-to-air missiles |
| Jaguar A and B and | l EMK 102 Audor engines |
| Jaguar S | MK 104s Audor engines Using digital quadruplex fly-by-wire Control system |
| Jaguar Act | |
| Jaguar FBW | J |

Table 2.14 (continued)

Jet Reaction (Y_r)

As a result of the postulated rupture of a high-energy system there develops an unbalanced differential pressure force plus a mass transfer momentum effect due to fluid being ejected from the rupture. In actuality an unbalanced external force develops on the system at each change in area and direction in the system. Typical reaction load characteristics due to a postulated rupture are given in the ANS N-176 guide.

Jet Impingement (Y_i)

As a result of a high-energy system rupture a high-energy fluid jet may form which would impinge on structures within its path. These structures in general would be designed 40 resist the momentum transfer resulting from the structure stopping the jet.

Reaction Load Due to Accident-Induced Differential Movement (R_a)

Many structures and components are supported by primary structures which would undergo deformation from an accident condition and thereby induce loads in the supported structure or component. Examples of this effect would be loads on piping systems attached to the containment, which would be induced when the containment expands due to accident pressure and temperature effects.

Table 2.15 Data on the Dassault aircraft

| Service load parameters and | l stresses | | | | | | |
|--|------------------|---------|----------|-------------|-------------|--------|--------|
| | S | L | Н | $A_{\rm w}$ | $P_{\rm L}$ | V | Wa |
| Type and power plant | (m) | (m) | (m) | (mm) | (kg) | (km/h) | (kg) |
| Dassault Breguet Fl | 8.4 | 15 | 4.5 | - | 7400 | 1472 | 14,900 |
| Single-seater multi- mission fighter, 7200 kg thrust, SNECMA Atar, | | | | | | | |
| 9 K-50 single shaft | | | | | | | |
| turbojet | 0.6 | 144 | 1.20 | | 5900 | 1002 | 10.000 |
| Single seater strike fighter | 9.0 | 14.4 | 4.20 | - | 3800 | 1085 | 10,000 |
| 4400 kg thrust, SNECMA Atar. | | | | | | | |
| 8B single shaft turbojet | | | | | | | |
| Super Estendard single- seater strike fighter, 5110 kg thrust, | 9.6 | 14.31 | 4.26 | _ | 6300 | 1200 | 11,500 |
| 8 K-50 single shaft | | | | | | | |
| turboiet | | | | | | | |
| Mirage 3 and 5 | 8.22 | 15.5 | 4.25 | _ | 6156 | 1390 | 12,000 |
| Single-seater or two-seater | | | | | | | |
| interceptor, | | | | | | | |
| trainer and reconnaissance | | | | | | | |
| 6000 kg thrust SNECMA | | | | | | | |
| Atar, | | | | | | | |
| 9B single shaft turbojet | | | | | | | |
| Mirage 2000 | 9 | 15 | 4.5 | - | 7800 | 2200 | 9000 |
| Mirage 315 and F-l improved version of these aircraft with engines SNECMA turbofans | | | | | | | |
| Mirage 4000 | 12 | 18.7 | 4.5 | - | 13000 | 2300 | 16,100 |
| SNECMA M53, single shaft bypass turbofan 8 stage axial compressor 2 \times 14,500 lb (2 \times 6579 kg) thrust | | | | | | | |
| Armament Mirage 4000 | Bombs | | | | | | |
| Internal cannons $2 \times 30 \text{ mm}$ | | Anti-r | unway I | Durandal | up to 27 | | |
| 4 long-range missiles | | Clean | or retar | ded (250 | kg) up to | 27 | |
| 4 air-to-ground missiles | D 1 (| Laser g | guided (| 250) up t | io 27 | | |
| 2 air-to-surface missiles | Rockets 68 mm | | | | | | |

| | Table 2.16 Comparative data | of some important | combat aircrafi | | | | |
|-----------------------------------|---|------------------------------|-----------------|-------|-------------|--------------|-------------|
| | | S | Г | Н | $P_{\rm L}$ | Λ | $w_{\rm a}$ |
| Type | Power plant | (m) | (m) | (m) | (kg) | (km/h) | (kg) |
| BAe Harrier | $1 \times 21,500 \text{ lb} (9752 \text{ kg}) \text{ thrust}$ | 7.7 | 13.87 | 3.43 | 6200 | 1.2 | 11,793 |
| GR-3 model | Rolls-Royce Pegasus 103 | | 17.0 (GR-3) | | | 860 | |
| T-Mark 4 model (AV-8A, | two shaft turbofan | | | | | | |
| TAV-8A) FRS-I model | (US designation F-400) | | | | | | |
| Single-seater, two-seater | | | | | | | |
| F-6 Sheriyang (or NATO's | 2x Axial turbojets | 10.2 | 15.25 | 3.35 | 4500 | 1 | 10,700 |
| name FANTAN 'A') Single seater | MD manufactured | | | | | 760 | |
| Rockwell B-I | $4 \times 30,000 \text{ lb} (13,610 \text{ kg})$ | 41.4 | 45.6 | 10.24 | 11,5670 | 0.85 | 179, 170 |
| Four seater | General Electric F101-100 two shaft augmented turbofans | | | | | | |
| Saab 37 AJ, JA | 1 Svenska flying motor RMB; | 10.6 | AJ: 10.6 | 5.6 | 4500 | 2 | 16,000 |
| Viggen SF, SH, | Pratt and Whitney two shaft | | JA: 16.3 | | | 1320 | |
| SK versions | 25,970 lb (11,790 kg) to 28,086 lb | | | | | | |
| Single seater | | | | | | | |
| SU-9 Fishpot BSU-11 | (12,750 kg) thrust | 8.43 | SU-9: 18.5 | 4.9 | 4540 | 0.95 | 13,610 |
| Fishpot C | 1 Lyulka single shaft | | SU-11: 17.4 | | | 1195 | |
| Single seater | turbojet; 19,840 lb (9000 kg) thrust (SU-9) and 22,040 lb | | | | | | |
| | (10,000 kg) thrust (SU-11) | | | | | | |
| SU-15 (Flagen A | 2x Tumonsky R-25 turhofans: | 9.5 D model | 21.5 | 5 | 10,100 D | 2.3 | 21,000 D |
| to E models) | 16,530 lb (7500 kg) thrust after | | | | 5100 A | 1520 | 16,000 A |
| Single | burner (17) | | | | | | |
| seater | | , | | | | | |
| SU-17. SU-20 and | 1-Lyulka AL-21 F-3 | 14 (28 [°] sweep) | 18.75 | 4.75 | 0006 | 1.05 | 19,000 |
| SU-22 models | Thrust single shaft 17,200 lb | 10.6 (62 [°] sweep) | | | | 798 | |
| Single seater | (7800 kg) (20–22) AL-7F | | | | | To | |
| | 22,046 lb (10,000 kg) | | | | | 2.17 1432 | |

2 Loads and Material Properties for Nuclear Facilities

| | | Table 2.1 | 17 Types of | of shells, bombs, rifles | | | | |
|---|--|----------------------------|---------------------|-----------------------------|--------|--------|------|--------------------|
| Service load parameters and | d stresses | | | | | | | |
| Types of shells and bombs | Manufacturers | Dimensions | $w_{\rm L}(\rm kg)$ | | | | | |
| Double base | International | d = 1.25 | : | Porous disc | Short | : | : | Guns |
| Shot gun | - - - | 0.01.0 - 1 | | - - | 5 | | | (|
| Single or double base rim fire | International | d = 0.8/0 t = 0.1 | : | Porous disc | Short | : | : | Cuns |
| Double base | International | d=1 | : | Porous disc | Short | : | : | Guns |
| revolver | | t = 0.125 | | | | | | |
| Single base rifle | International | d = 1.25 | : | Tubular | Short | : | : | Guns |
| | | d = 0.375 | | | | | | |
| | | t = 0.045 | | | | | | |
| GBU-15 | Rockwell | L = 3.75 | MK84 | The forward guidance system | Medium | : | : | Free fall |
| HOBOS-guided | International | MK84 | 2240 | is KMU-353 or electro- | | | | bomb from |
| bomb | NSA | S = 112 | 1016 | optical with TV camera or | | | | |
| | | d = 46 | M118 | target-seeker optics | | | | |
| | | (M118) | 3404 | | | | | |
| | | S = 132 | | | | | | |
| | | d = 61 | | | | | | |
| Bofor | Sweden | : | 0.12 | 5500 kg guns | 3.7 km | 10,005 | 0.88 | Trajectory fall |
| ZSU-23-4 | USSR | L = 654 | 20.5 | SPAA vehicles 4×3 | Short | 7000 | : | Guns |
| | | d = 29.5 | | automatic | | | | |
| | | 3400 rounds | | | | | | |
| GBU-15(V)2 glide bomb | USA | L = 388 | | Imaging infrared | Short | | 1111 | |
| (smart bomb) | | | | | | | | |
| d = diameter (mm); t = web w _L = weight; S = span (cm); | thickness (mm); $L = $; $R = $ distance; $V = $ v | = length (cm); velocity | | | | | | |
| | | | | | | | | |

| | | Table 2.18 M | lissiles for arm | ned forces (ICBM and AL | CM) (USA, U | SSR) | | |
|------------------------------|---------------------------|--------------|------------------|--|-----------------|-----------|------------------------|------------|
| Service load paran | neters | | | | | | | |
| | Manufacturer/ | | | | | | | |
| Types of missiles/rockets | country of manufacture | Dimensions | WL lb (kg) | Power plant and guidance | R miles (km) | V mach | Warhead manufacture | Mechanisms |
| AGM-86A air- | Boeing. | L = 4.27 | 1900 | Williams Research | 760 | 0.6 - 0.8 | Thermo | B-52 |
| launched cruise | ò | | | F107- | | | nuclear | |
| missile (ALCM) | Aerospace, | S = 289 | 862 | WR-100 2. No shaft | 1200 | 200 kt | | |
| | Seattle, USA | d = 64 | | thrust; McDonnell Douglas | | | | |
| | | | | Tercom with inertial | | | | |
| | | | | system | | | | |
| LGM-30 | Boeing | L = 18.2 | Model II | I-Stage: Triokol TU- 120 | II stage: | 1500 mph | Thermo nuclear | SG |
| Minuteman | Aerospace, | d = 183 | 70,116 | (M55E), 2×10^{5} lb | 7000 | | | |
| (ICBM) missile, | Ogden, USA | | 31,800 | $(9 \times 10^5 \text{ kg})$ thrust | 11,250 | | 15 Mt | |
| located in silos | | | Model III | Il Stage: Hercules | Ill stage: | | II stage: | |
| | | | | rocket | | | | |
| | | | 76,015 | 35×40^{3} lb (16×3 kg) | 8000 | | AVCO MK | |
| | | | 34,475 | thrust | 12,875 | | 11C | |
| | | | | III-Stage: Aerojet 35 x | | | Ill stage: GE | |
| | | | | 10 ³ lb (16 x 10 ³ kg) | | | MK-12 | |
| | | | | thrust | | | MIRV | |
| RS-121SS13 | USSR | I | I | Solid fuel propellant; three stages | 9400 | 0.8 | Nuclear 75 kt | SG |
| Savage (ICBM) | | | | | | | | |
| RS-16/SSI7 | USSR | | | Liquid cold launch; two stages | 11,000 | 0.8 | 3.6 Mt mode 2 | SG |
| (ICBM) | | | |) | 1000 | | or MIRV 4 < 2004 | |
| | | | | | | | | |

| | | | T. | ible 2.18 (continued) | | | | |
|--------------------|---------------|------------|---------|------------------------|------------|------|-------------|------------|
| Service load parai | meters | | | | | | | |
| | Manufacturer/ | | | | | | | |
| Types of | country of | | WL | Power plant and | R | ^ | Warhead | |
| missiles/rockets | manufacture | Dimensions | lb (kg) | guidance | miles (km) | mach | manufacture | Mechanisms |
| RS-20!SS18 | USSR | | | Liquid propellant; two | 10,000 | 1 | 5-lOMt | |
| | | | | stages | | | | |
| (ICBM) | | | | | | | mode 2 | |
| SS-23 Scalpel | USSR | I | Ι | Solid cold launch | 10,000 | 1 | Nuclear | Rail |
| | | | | propellant: | | | MIRV | |
| (ICBM) | | | | three stages | | | 8-10x | mobile |
| SS-25 Sickle | USSR | Ι | Ι | Solid cold launch | 10,500 | 1 | Nuclear 550 | |
| | | | | propellant; | | | kt | |
| (IRBM) | | | | three stages | | | | |
| | | | | | | | | |

| | | Table 2.1 | 19 Mis | ssiles f | or arme | d forces (BGM, M, MK, RGM, etc.) (U | SA, France, | Israel) | |
|------------|--------|--------------------|--------|----------|---------|---|-------------|---------------------------|--------------------------|
| TOW 2 | USA | L = 140 | | | 21.5 | Solid propulsion; wire manual or | 3.75 | Heat conventional | SSM |
| (BGM-71 D) | | d = 15 | | | | auto | | | anti-tank |
| Copperhead | USA | L = 137 | | | 63.5 | Cannon launched: laser homing | 16 | Heat 6.4 kg | SSM |
| (M712) | | d = 15 | | | | | | | anti-tank |
| Gabriel | Israel | Г | S | d | | Two-stage solid | | Conventional | SSM |
| MK I | | 335 | 135 | 34 | 430 | propulsion; auto | 18 | 100 kg | shipborne |
| MK II | | 341 | 135 | 34 | 430 | pilot/command | 36 | 100 kg | |
| MK III | | 381 | 135 | 34 | 560 | | 36 + | 150 kg | |
| MK IV | | 381 | 135 | 34 | 560 | Turbojet propulsion: | 200 | | |
| | | | | | | inertial and active radar homing | | | |
| SS-N-3 | USSR | L = 1020 | | | 4700 | Solid boosters: | 460-735 | Nuclear and | SSM |
| | | | | | | | | Conventional | shipborne |
| Shaddock | | d = 86 | | | | internal turbojet radio | | | |
| | | | | | | command | | | |
| (IMINC) | | | | | | | | | |
| Harpoon | NSA | L = 384 | | | 519 | Solid booster turbojet cruise: inertial and radar | 90 | Conventional | SSM |
| (RGM-84A) | | S = 830 J = -24 | | | | | | | shipborne |
| Deadeve 5 | USA | u = 34 L = 384 | | | 47.5 | Solid propulsion: | 24 | 1 | Guided |
| . | | d = 12.7 | | | | laser homing | | | projectile; shinhorne |
| Crotale | France | L = 290 | | | 80 | Solid propulsion: radio command | 18 | 15 kg | NSA |
| | | S = 54 | | | | | | conventiona | |
| | F | d = 15 | | | t | - - - | | | |
| Sadral | France | L = 180 $d = 16$ | | | 1/ | Solid propulsion; infrared homing | 0.3-0 | 5 kg neat conventional | AGN |
| | | | | | | | | | |

2 Loads and Material Properties for Nuclear Facilities

| | | | Table 2.20 | Data and parameters on missile | types | | | |
|-----------------|----------------------|-------------------|------------|--|-------|---------------------------|---------------------|--|
| Service load pa | rameters and stresse | SS | | | | | | |
| Barak missile | Israel Aircraft | L = 217 d = 17 | 86 - | Semi-active radar-horning missile with disposable | 10 | Conventional 2 nuclear | NSA small patrol | |
| | Industries (IAI) | | | launch canister, manually | | 7 kg | boats | |
| | | | | fitted to an 8-round | | | | |
| | | | | MBT TCM-30 twin 30 mm | | | | |
| | | | | anti-aircraft gun mounted | | | | |
| SA-N-3 | USSR | L = 620 | 550 | Solid propulsion: | 55 | $80 \mathrm{kg}$ | NSA | |
| | | | | semi-active homing | | | | |
| Goblet | | S = 150 | | semi-active homing | | conventional | | |
| | | d = 33.5 | | | | | | |
| SA-N-4 | USSR | L = 320 | 190 | Solid propulsion: | 14.8 | 50 kg | NSA | |
| | | | | semi-active homing | | | | |
| | | d = 21 | | semi-active homing | | | | |
| Roland 3 | France and Italy | L = 260 | 85 | Solid propulsion and | 8 | 9 kg | ADM | |
| | | | | command | | | | |
| | | S = 50 | | | | conventional | | |
| | | d = 27 | | | | | | |
| SA-4 Gancf | USSR | L = 880 | 100,000 | Ramjet and solid | 70 | 135 kg | ADM | |
| | | | | boosters; | | | | |
| | | | | radio command | | | | |
| (SRM) | | S = 290 | | | | | | |
| SA-lO | USSR | L = 700 | 1500 | Solid propulsion | 100 | Nuclear | ADM | |
| Grumble | | | | | | | | |
| OIMM | | S = 10 | | | | | | |
| | | d = 45 | | | | | | |
| SA-12 | USSR | L = 50 | 2000 | Solid propulsion: | 80 | 150 kg | | |
| Gladiator | | S = 350 | | semi-active radar | | conventional | ADM | |
| | | d = 50 | | | | | | |

2.2 Loads

| | | | | Table 2.20 (continued) | | | | |
|----------------------------|----------------------|-----------------|--------------|--------------------------|--------|------------------------|--------------------|----|
| Service load pai | rameters and stresse | S | | | | | | |
| SA-13 | USSR | L = 220 | 55 | Solid propulsion: | 10 | 4 kg | ADM | |
| Gopher | | | | infra-red homing | | | | |
| (HJ-8) | | S = 40 $d = 12$ | | infrared homing | | conventional | | |
| BGM-109 | General | L = 5.56 | 2200 | Williams Research F107 | 1 727 | 0.72 | Thermo- | SG |
| Tomahawk cruise missile | Dynamics | <i>S</i> = 2.45 | 1000 | Turbofan 600 lb (272 kg) | 2780 | (550 mph/ 885 km/h) | nuclear nuclear | |
| | Convair. | d = 0.53 | to | Thrust guidance | | | 1000 lb | |
| (IRBM) | San Diego, 11SA | | 4000 1814 | MD Tercom and inertial | | | (454 kg) | |
| CSS-2 | China | I | | Liquid propellant | 120.00 | 0.8 | Nuclear | SG |
| CSS-3 | | | | Stage 2 | | | 2 Mt | |
| (IRBM) | | | | Stage 3 | | | 1-5 Mt | |
| CSS-1 | China | I | I | Liquid propellant | 1200 | 0.7 | Nuclear | SG |
| CSS-2 | | | | Two stages | 2700 | | 20 kt | |
| (IRBM) | | | | | | | 1 –3 Mt | |
| Sandal | | | | Two stages | 2000 | | 1 Mt | |
| (IRBM) | I | Ι | I | | | | | |
| SSBS S-3 | France | I | | Solid propellant | 3000 | 0.65 | Nuclear | |
| | | | | Two stages | | | 1.2 Mt | |
| SS-N-20 | USSR | I | | Solid propellant | 3000 | 0.65 | Nuclear | |
| Sturgeon (1RBM) | | | | | | | 1.2 Mt | |

| | | | | Table 2.20 (continued) | | | | |
|-------------------|-------------------------------|-----------|--------|---|--------|----|-------------------|-----------|
| Service load p | parameters and stresse | s | | | | | | |
| UGM-73 | Lock heed | L = 10.36 | 65000 | Solid motor Thiokol as | 3230 | 10 | Lockheed | Submarine |
| Poseidon | Missiles and | d = 1.88 | -29500 | first stage: Hercules as second stage; guidance: | 5200 | | MIRV | launch |
| missile (IRBM) | Space Company, California. | | | inertial | | | carrying 50 kt | |
| ~ | USA | | | | | | Rvs | |
| UGM-27 | Lockheed, | L = 9.45 | 35000 | Aerojet solid motor with | 2875 | 10 | MIRV | Submarine |
| | | | | jetavator control as first stage: Hercules motor missile with liquid injection as second stage | | | | |
| Polaris | California, | d = 1.37 | -15850 | 0 | (4631) | | 200 kt | launch |
| (ICBM) | USA | | | | | | | |
| | | | | | | | | |
| | | Table 2 | .21 Miss | siles and rockets | | | |
|-------------------|----------------------|------------|------------------|--------------------------|---------------|--------------|--------------------|
| Service load para | meters and stresses | | | | | | |
| Type of | Manufacturer/country | | w_{L} | | R | | |
| missile/rockets | of manufacture | Dimensions | (Ib) | Power plant and guidance | (km) | Warhead | Mechanisms |
| Blood hound | UK | L = 846 | | Ramjet and solid | 80 | Conventional | ADM |
| | | S = 283 | | boosters; | | | |
| | | d = 55 | | semi-active | | | |
| | | | | radar homing | | | |
| Blow pipe | UK | L = 139 | 20.7 | Solid propulsion; | Any short | | |
| | | S = 270 | | radio command | distance 3 | | |
| Javelin | UK | L = 40 | | Solid propulsion; | + + | Conventional | ADM |
| | | d = 8 | | Saclos | | | shoulder- fixed |
| Hawk | USA | L = 503 | 627.3 | Solid propulsion; | 40 | Conventional | ADM |
| MIM-23B | | S = 119 | | semi-active | | | |
| | | d = 36 | | Homing | | | |
| Stinger | USA | L = 152 | 15.8 | Solid propulsion; | Short | Conventional | ADM |
| FIM-92A | | S = 14 | | infrared homing | range | | |
| | | d = 7 | | | ŝ | | |
| MIM | USA | L = 1210 | 4858 | Solid propulsion; | 140 | Nuclear and | ADM |
| Hercules | | d = 80 | | command | | conventional | |
| L-5B | China | L = 289 | 85 | Solid propulsion; | 5 | Conventional | AAM |
| | | S = 66 | | infrared | | | |
| | | d = 13 | | | | | |
| L-7 | China | L = 25 | 06 | Solid propulsion; | 5 | Conventional | AAM |
| | | S = 66 | | infrared | | | |
| | | d = 16 | | | | | |
| Mistrel | France | L = 180 | 18 | Solid propulsion; | Э | 3 kg | AAM |
| | | d = b | | infrared | | conventional | |
| Super 530 | France | L = 354 | 250 | Solid propulsion | 25 | 3 kg | AAM |

2 Loads and Material Properties for Nuclear Facilities

| | | Ta | ble 2.21 (| continued) | | | |
|----------------------------|--|--|------------------------|---|-----------|--------------|-----------------|
| Service load para | meters and stresses | | | | | | |
| Type of missile/rockets | Manufacturer/country of manufacture | Dimensions | ^w L (1b) | Power plant and guidance | R (km) | Warhead | Mechanisms |
| M Type (SRM) | China | L = 910 | 6200 | Solid propulsion; inertial | 600 | Nuclear | SSM |
| Frog-7 (SRM) | France | L = 910 d = 85 | 2300 | Solid propulsion | 70 | Nuclear | SSM |
| SS-IC Scud B | USSR | L = 1125 d = 85 | 6370 | Storable liquid; inertial | 280 | Nuclear | |
| SS-23 Spider | USSR | L = 605 d = 100 | 3500 | Solid propulsion; inertial | 525 miles | Nuclear | SSM |
| Exocet MM10 | France | L = 578 | 850 | Solid propulsion; | 70 | 165 kg | SSM ship |
| | | S = 100 d = 35 | | two stages: inertial and active radar Homing | | Conventional | |
| RBS 15 | Sweden | L = 435 | 600 | Turbojet boosters | 150 | Conventional | SSM ship |
| Arrow 8(Hj-8) | China | C = 00 $L = 99.8$ $S = 47$ | 11.3 | Solid propulsion; wire guided | 0.1 - 3 | Heat | SSM antitank |
| Spandrel | USSR | $\begin{array}{c} a = 10.2 \\ L = 100 \\ 1 & 10 \end{array}$ | 12 - 18 | Solid propulsion; | 4 | Heat | SSM |
| Vigilant | UK | d = 10 $L = 107$ $S = 28$ $d = 11$ | 14 | semt-automatic Solid propulsion; two stages: wire manual | 1.375 | Heat 6 kg | anutatuv |
| | | | | | 1 | Heat | SSM |
| Dragon 1M47 | USA | L = 74 $S = 33$ $d = 13$ | 13.8 | Muutpie sond propulsion; wire manual | | | anthann |

| | | T | able 2.22 M | issiles with warhead mech | anisms | | | |
|------------------------------|---|-------------|-------------|--|-------------------------|---------------|--------------|------------|
| Service load para | meters and stresses | | | | | | | |
| Types of missiles/rockets | Manufacturer/ country ofmanufacture | Dimensions | w, lh (kα) | Power plant and puidance | × | $V_{ m mach}$ | Warhead | Mechanisms |
| | | P S I | (Q) 2.7 | 000000 | ; | (mdm) | | |
| C-601 | China | 738 280 92 | 2440 | Liquid propulsion | 100 km | I | 400 kg | ASM |
| HY-4 | | 736 280 7.6 | 1740 | Turbofan propulsion | 150 km | | to | ASM |
| C-801 | | 480 165 55 | 1025 | Solid propulsion | 150 km | I | 500 kg | ASM |
| | | | | All active radar | | | Conventional | |
| | | L S d | | | | | | |
| S-9 | USSR | 600 150 50 | 750 | Solid propulsion: | 150 km | | Conventional | ASM |
| S-10 | | 350 90 30 | 300 | semi-active laser | | | | |
| AS-II | USSR | L = 350 | 300 | Solid propulsion: | 300 km min | Ι | Conventional | ASM |
| | | S = 90 | | infrared | | | | |
| | | d = 30 | | | | | | |
| Sea Eagle | UK | L = 414 | 600 | Turbofan inertial: | 110 km | I | Conventional | ASM |
| | | S = 120 | | active radar | | | | |
| | | d = 40 | | | | | | |
| AGM-65 | Hughes | L = 246 | 462 (210) | Thiokol TX-481 solid motor: AGM-65C laser guidance | 8 miles | 6-10 | Mk 19 113 kg | ASM |
| Maverick | Aircraft, | S = 71 | | 1 | (13 km) to | | | |
| | Tulson, | d = 44.5 | | | 14 miles | | | |
| | USA | | | | (22.5 km) | | | |
| AGM-69A | Boeing | L = 4127 | 2230 | LPC (Lockheed | High 105 | 200 | Conventional | ASM |
| SRAM | | | | Company) | miles (170 km): | | | |
| | Aerospace, | S = 89 | 1010 | Propulsion two-pulse solid motor: | low 35 miles (56 km) | | Nuclear | Rocket |
| | Seattle, | d = 44.5 | | guidance: inertial | ~ | | 170 kT | |

100

2 Loads and Material Properties for Nuclear Facilities

| Bervice load parameters and stresses Manufacturer/ Types of country Types of country Manufacturer/ missiles/rockets Manufacturer/ (mph) Manufacturer/ mode USA USA Nc 0 10 | | | | Tab | le 2.22 (contir | (pant | | | |
|--|------------------------------|---|--------------------|------------------------|-------------------------------------|---|---------------------|---------------------------------------|----------------------|
| Types of missiles/rockets Manufacturer/ country Manufacture Manufacturer/ missiles/rockets Manufacturer/ mplue Manufacturer 10SA USA USA Nothendlacture No | Service load para | meters and stresses | S | | | | | | |
| $ \begin{array}{c c c c c c c c c c c c c c c c c c c $ | Types of missiles/rockets | Manufacturer/ country ofmanufacture | Dimensions | w _L lb (kg) | Power plant a guidance | nd R | $V_{ m mach}$ (mph) | Warhead | Mechanisms |
| Missile $S = 89$ 1200ramjet: guidance: inertial with TercomMK II $d = 44.5$ guidance: inertial with TercomMK II $d = 44.5$ guidance: inertial with TercomTypes ofManufacturer/country w_1 bPower plant and guidanceTypes ofManufacturer/country w_1 bPower plant and guidanceTypes ofManufacturer/country w_1 bPower plant and guidanceTypes ofManufacturer/country w_1 bPower plant and guidanceStomacicFrance $L = 275$ Solid propulsion; ford propulsion; for miceStomacicL = 233-Up toRocket dyne, Thiokol, miceSidewinderWeapon 2.91 190Bernite or Naval miceSidewinderSidewinderSingle Grain solid high spaceSingle Grain solid maxGeneral ElectricAmicSingle Grain solid highSingle Grain solid highGeneral ElectricAmicPower servo-system, highAmic | ASLAM | USA McDonnell Douglas, USA | L = 4127 | 2700 | Internal rocke | r. | 6-10 | 170 kt nuclear and conventional | ASM |
| Types of missiles/rocketsManufacturer/country of manufacture w_1 lb bimensionsPower plant and guidanceA550 MagicFranceDimensions (kg) guidance R Warhead550 MagicFrance $L = 275$ Solid propulsion;5 kmConventional550 MagicFrance $L = 275$ Solid propulsion;5 kmConventional550 MagicRete $L = 275$ Solid propulsion;5 kmConventional66 $d = 16$ Naval $L = 283-$ Up toRocket dyne, Thiokol, $2.5+$ XM 248AIM-9Naval $L = 283-$ Up toRocket dyne, Thiokol, $2.5+$ XM 248SidewinderWeapon 2.91 190Bermite or NavalcruisehighCentre, $S = 56 86$ propellant; 6 milesexplosivePhilco-Ford 64 MK $17, 36, 86;$ guidance: 9E to 9L, 150 Space MK MK MK MK MK | Missile MK III MK IV | | S = 89 d = 44.5 | 1200 | ramjet: guidance: iner Tercom | tial with | | | |
| 550 MagicFrance $L = 275$ Solid propulsion; 5 kmConventional $S = 66$ Infrared $d = 16$ AIM-9Naval $L = 283$ -Up toRocket dyne, Thiokol, $2.5 +$ $XM 248$ SidewinderWeapon 2.91 190Bermite or NavalcruisehighSidewinderWeapon 2.91 190Bermite or NavalcruisehighCentre, $S = 56$ - 86 propellant; 6 milesexplosivePhilco-Ford 64 $MK 17, 36, 86;$ $MK 17, 36, 86;$ max $(150 1b)$ space $d = 12.7$ $MK 17, 36, 86;$ max $(150 1b)$ General Electric $d = 12.7$ $MK 17, 36, 86;$ max $(150 1b)$ AM/ MM MM MM MM MM | Types of missiles/rockets | Manufactur of manufact | er/country ure | Dimen | $w_{\rm L}$ lb sions (kg) | Power plant and guidance | R | Warhead | Mechanisms |
| d=16 $d=16$ $d=16$ $L=283-$ Up toRocket dyne, Thiokol, $2.5+$ XM 248SidewinderWeapon 2.91 190Bermite or NavaleruisehighCentre, $S=56 86$ propellant; 6 milesexplosivePhilco-Ford 64 Single Grain solidmax $(150 lb)$ Ford Aero- $d=12.7$ MK $17, 36, 86;$ max $(150 lb)$ space $d=12.7$ puidance: 9E to 9L,highGeneral Electric $AM/$ $AM/$ $AM/$ | 550 Magic | France | | L = 27; $S = 66$ | \$ | Solid propulsion; Infrared | 5 km | Conventional | AAM |
| SidewinderWeapon2.91190Bermite or NavalcruisehighCentre, $S = 56 86$ propellant; 6 milesexplosivePhilco-Ford 64 Single Grain solidmax $(150 lb)$ Ford Aero- $d = 12.7$ MK 17, 36, 86; $guidance: 9E to 9L,$ spacehighpower servo-system, AMI | 9-MIA | Naval | | d = 16 L = 28 | 3- Up to | Rocket dyne, Thiokol, | 2.5+ miles | XM 248 | AAM |
| Philco-Ford 64 Single Grain solidmax(150 lb)Ford Aero- $d=12.7$ MK 17, 36, 86;spacespaceindance: 9E to 9L,spacehighhighpower servo-system, | Sidewinder | Weapon Centre, | | 2.91 S = 56- | - 190 - | Bermite or Naval propellant; | cruise 6 miles | high explosive | (F-16, F-20, F-5E |
| General Electric power servo-system, | | Philco-Ford Ford Aero- space | | d=12. | 7 | Single Grain solid MK 17, 36, 86; guidance: 9E to 9L, high | max | (01 0 1 1) | aurcraft) |
| | | General Ele | ctric | | | power servo-system, AM/ | | | |

| | | Table 2.22 | (continu | ed) | | | |
|------------------------------|--|------------------------------|------------------------|--------------------------|---------------------|--------------|------------|
| Types of missiles/rockets | Manufacturer/country of manufacture | Dimensions | $w_{\rm L}$ lb (kg) | Power plant and guidance | R | Warhead | Mechanisms |
| | USA | | | FM IR conical scan | | | |
| | | | | head or Raytheon | | | |
| | | | | track | | | |
| | | | | via missile | | | |
| Alamo | USSR | L = 400 | 200 | Solid propulsion; | $30 \ \mathrm{km}$ | Conventional | AAM |
| AA-10 | | S = 70 | | semi-active or | | | |
| | | d = 19 | | infrared | | | |
| AMBAAM | USA | L = 357 | 150 | Solid propulsion; | 12 km | Conventional | AAM |
| | | | | command and inertial | | | |
| | | S = 63 | | | | | |
| | | d = 18 | | | | | |
| Falcon | USA | L = 213 | 115 | Solid propulsion; | 8 km | Conventional | AAM |
| | | S = 639 | | semi-active radar | | | |
| | | d = 29 | | | | | |
| Phoenix | USA | L = 396 | 454 | Solid propulsion; | 150 km | Conventional | AAM |
| | | S = 92 | | semi-active radar | | | |
| | | d = 38 | | | | | |
| Sparrow | USA | L = 366 | 227 | Solid propulsion; | $140 \ \mathrm{km}$ | Conventional | AAM |
| AIM-7 M | | S = 102 | | infrared | | | |
| | | d = 20 | | | | | |
| L = length (cm), S = | wingspan (cm), $d =$ diameter (cm), | $W_{\rm L} = {\rm launch} v$ | weight, R | = range | | | |

| | | Table 2.23 | Missiles f | or armed forces (ADM and NSA types) | (UK, US | 5A) | | |
|-----------------------|---------------------|-------------------|----------------|--|------------------|-------|--------------------------------------|--------------------|
| Service load | parameters and stre | sses | | | | | | |
| Types of | Manufacturer/ | | | | R | Λ | | |
| missiles/ | country of | | $w_{\rm L}$ lb | | miles | mach | | |
| rockets | manufacture | Dimensions | (kg) | Power plantand guidance | (km) | (mph) | Warhead | Mechanisms |
| MGM- 31A | Martin, | L = 10.51 | 10,150 | 2 No. Thiokul | 100 | 8 | Nuclear | Mohile |
| Pershing missile | Orlando, | S = 202 $d = 101$ | 4600 | solid motors: first stage – M105,second stage – M106, guidance: | 160 | | 400 kt | tactical system |
| | NSA | | | Inertial | to 520 840 | | | ADM/SSM |
| MGM- 51C | Ford, New Post | L = 1.14 | 60 | Amoco single- | ŝ | 800 | Octal- | Battle tank, |
| Shillelagh missile | Beach, USA | S = 29 $d = 15.2$ | -27 | stage solid jetavators: guidance: optical tracking and infrared command link | | | shaped charge 15 lb (h.8 kg) | ADM/SSM |
| BGM-71 TOW | Hughes | L = 1.17 | 42 | Quad boost | up to | 620 | Shaped | Vehicles, |
| Missile | Aircraft, | S = 34 $d = 14.7$ | 19 | motor for recoil-less launch: | 3.75 | | Charge | aircraft, |
| | Culver City, | | | guidance: with optical sighting and trailing wire | | | containing | ADM/SSM |
| | USA | | | , | | | 5.3 lb (2.4 kg) high explosive | |
| | | | | | | | | |

2.2 Loads

| - - | | | | Table 2.23 (continued) | | | | |
|---------------------|------------------------|--------------------|----------------|---|-------|-------|--------------|--------------------|
| Service load | I parameters and stre | SSSES | | | | | | |
| Types of | Manufacturer/ | | | | R | Δ | | |
| missiles/ | country of | | $w_{\rm L}$ lb | | miles | mach | | |
| rockets | manufacture | Dimensions | (kg) | Power plantand guidance | (km) | (mph) | Warhead | Mechanisms |
| Sea Dart | British | L = 4.4 | 550 | Marconi radar | 30 | | Conventional | NSA patrol |
| Missile | | d = 42 | | | | | and nuclear | boats and ships |
| | Aerospace, UK | | | 805 SW tracker with type 909 illuminator; guidance: semi | | | | 4 |
| Sea Wolf | British | L = 1.9 | 82 | GWS 25 | 30 | | Conventional | NSA/SSM |
| Missile | Aerospace, | d = 18 | | Marconi radar | | | and nuclear | boats and |
| | UK | | | (805547) search, tracking radars, Ferranti fire-control computer; guidance: radio command | | | | Ships |
| Sea Cat | Short Brothers, | L = 1.47 | 63 | Radio command | 30 | | Conventional | NSA/SSM |
| Missile | Belfast, UK | d = 19 | | guidance with optical remote TV and radar- aided tracking | | | and nuclear | boats and ships |
| Raytheon/ Martin | Martin Orlando | L = 5.31 | 3740 | Thiokol TX-486 | 30 | 3-5 | Nuclear and | Advanced |
| XMIM- 104A | Division, USA | S = 87 | 1696 | single-thrust solid | 48 | | conventional | mobile |
| Patriot missile | | d = 41 | | motor | | | | system SAM |
| L = length(i) | cm), $S =$ wingspan (i | cm), $d = diamete$ | er (cm), 14 | L = launch weight, $R =$ range; $V =$ spee | pa | | | |

Ę .E 9

Helicopters

Helicopters are more vulnerable than aircraft in warfare. In peace time a helicopter may crash after losing a rotor or hitting objects such as offshore platforms, buildings, helipads or their surrounding structures. Table 73 gives useful data for some types of helicopters in the book "Shock, Impact and Explosion" by the authors published by Springer-Verlag (Germany) 2008.

2.2.3.7 Load Combinations

Based on American Standards

Load Combinations for Concrete Structures

Design load combinations for concrete structures are given in the following two industry standards, depending on the type of structure being designed.

- 1. Code for Concrete Reactor Vessels and Containments –ASME Section III, Division 2 and ACI 359-77. Prepared by Joint ACI-ASME Technical Committee on Concrete Pressure Components for Nuclear Service.
- 2. Standard for Design of Concrete Structures in Nuclear Service other than Pressure Retaining Components ACI-349.

The loading equations found in these industry standards may not agree with NRC published guidelines. In such cases the designer should be assured the load combinations used are acceptable to the regulatory authorities.

- 3. Load Combinations for Steel Structures –For steel structures, a definitive industry standard (ANSI N690) is still used. In general, load combinations are acceptable if they are found in accordance with the following
- 4. For service load conditions, either the elastic analysis working stress design (WSD) methods of Part 1 of the AISC Specification or the plastic (limit) analysis load factor design (LRFD) methods of Part 2 of the AISC Specification may be used.

If the elastic analysis WFD methods are used, the following load combinations should be considered:

1. D + L2. $D + L + E_0$ 3. D + L + W

If thermal stresses due to T_0 and R are present, the following combinations should also be considered:

1a. $D + L + T_a + R_0$ 2a. $D + L + T_0 + R_0 + E_0$ 3a. $D + L + T_0 + R_0 + W$

Both cases of L having its full value or being completely absent should be checked.

If plastic (limit) analysis LRFD methods are used, the following load combinations should be considered:

- 1. 1.7D + 1.7L
- 2. $1.7D + 1.7L + 1.7E_0$
- 3. 1.7D + 1.7L + 1.7 W

If thermal stresses due to T_0 and R_0 are present, the following combinations should also be considered:

lb. $1.3(D+L+T_0+R_0)$ 2b. $1.3(D+L+E_0+T_0+R_0)$ 3b. $1.3(D+L+W+T_0+R_0)$

Both cases of L having its full value or being completely absent should be checked.

For factored load conditions which represent extreme loads the following load combinations should be considered:

Elastic analysis WSD methods are used:

4. $D + L + T_0 + R_0 + E_{ss}^1$ 5. $D + L + T_0 + R_0 + W_t$ 6. $D + L + T_a + R_a + P_a$ 7. $D + L + T_a + R_a + P_a + 10(Y_j + Y_r + Y_m) + E_0$ 8. $D + L + T_a + R_a + P_a + 10(Y_j + Y_r + Y_m) + E_{ss}^1$

If plastic (limit) analysis LRFD methods are used:

4.
$$D + L + T_0 + R_0 + E_{ss}^1$$

5. $D + L + T_0 + R_0 + W_t$
6. $D + L + T_a + R_a + 1.5P_a$
7. $D + L + T_a + R_a + 1.25P_a + 1.0(Y_j + Y_r + Y_m) + 1.25E_a$
8. $D + + T_a + R_a + 1.0P_a + 1.0(Y_j + Y_r + Y_m) + 1.25E_{ss}^1$

European Codes

The most important codes indulging in nuclear facilities are EC2, EC3, EC8, EC9, etc. It is extremely difficult to specifically assign combination for nuclear facility. The best possible combination can be given after examining various design practices in Europe where European codes are used, all loads can be calculated using respective codes. The following combinations of various loads are given below:

U = 1.4D + 1.7L $U = 0.75(1.4D + 1.7L \pm 1.87E)$ $U = 0.75(1.4D + 1.7L \pm 1.7W)$ $U = 0.9D \pm 1.43E$ $U = 0.9D \pm 1.3W$ $U = 1.4D + 1.7L + L^{7}H_{mep}$ U = 0.9D + 1.7H $U = 0.75(1.4D + 1.4T_{\rm d} + 1.7L)$ $U = 1.4(D + T_d)$

For reinforced concrete the following modifications are introduced where earthquakes are involved:

 $U = 1.4(D + L \pm E)$ $U = 0.9D \pm 1.4E$

where U = required strength to resist factored loads or related internal moments and forces; D = dead loads or related internal moments and forces; L = live loads or related internal moments and forces; W = wind loads or related internal moments and forces; E = load effects of earthquake or related moments and forces; T_d = internal moments and forces due to differential settlement, creep, shrinkage or temperature effects; H_{mep} = moments or forces due to earth pressure.

Loads computed from the Euro codes can still be combined using American practices given above. Care should be taken that all industrial concerns have been consulted and approvals are obtained for the design of various structural elements of nuclear facilities.

2.3 Determination of Impulse/Impact caused by Aircraft and Missiles: Load (1)

2.3.1 General

An impactor in the form of an aircraft or a missile develops from initial velocity to a velocity caused by its movement under the action of its own weight or a booster's force. In any circumstances, if the kind of velocity is not vertical it will move in a curve and its flight can be evaluated in terms of horizontal and vertical components of displacement, velocity and acceleration. Alternatively, the directions are controlled in any specific direction from the control centre.

2.3.1.1 Direct Impulse/Impact and Momentum

An impulse is defined as a force multiplied by time, such that

$$F_1(t) = \int F dt \tag{2.1}$$

where $F_1(t)$ is the impulse, F is the force and t is the time. The momentum of a body is the product of its mass and its velocity:

$$Momentum = mv \tag{2.2}$$

where *m* is the mass and *v* is the velocity = dx/dt. Both velocity and momentum are vector quantities; their directions are the same. If a body is moving with a

constant velocity, its momentum is constant. If velocity is to be changed, a force F must act on the body. It follows that a force F must act in order to change the momentum.

$$F = mdv/dt \tag{2.2a}$$

or

$$Fdt = mdv$$

Integrating both sides

$$\int_{t_z}^{t_2} = \int_{u}^{v} m dv$$

$$F_1(t) = m(v - u)$$
(2.3)

where u and v are the velocities at times t_1 and t_2 , respectively. If the initial velocity u = 0, Eq. (2.3) becomes

$$I = mv \tag{2.3a}$$

Thus the impulse of a force is equal to the change in momentum which it produces.

2.3.1.2 Impacts/Collisions of Aircraft

When two solid aircrafts are in contact, they exert equal and opposite forces or impulses on each other and they are in contact for the same time. If no external force affects the motion, the total momentum in the specific direction remains constant. This is known as the *principle of conservation of linear momentum*. When two aircrafts m_1 and m_2 , collide (Fig. 2.1), the mass ratios are then calculated from Eq. (2.1):

$$F_{11}(t) = m_1(v_1 - u_1) = \int F_1 dt$$

$$F_{12}(t) = m(v_2 - u_2) = \int F_2 dt$$
(2.4)



Aircraft II

Fig. 2.1 Direct impact

Since $\int F_1 dt = \int F_2 dt = 0$, the relationship between the velocity change and mass becomes

$$m_2/m_1 = (v_1 u_1)/(v_2 - u_2)$$
 (2.5)

During the collision process, although the momentum is conserved, there is a loss of energy on impact which is determined using the concept of the *coefficient of restitution*, *e*, which is defined as the relative velocity of the two masses after impact divided by the relative velocity of the two masses before impact. Before impact

$$e = (v_1 - v_2) / - (u_1 - u_2) = 0$$

When the relative velocity vanishes, and

$$e = (v_1 - v_2) / - (u_1 - u_2) = 1$$
 (2.5a)

there is no loss of relative velocity.

Where e < 1, it is related to the loss in kinetic energy, and where $u_2 = 0$ (refer to Eq. (2.5a)

$$m_1(v_1 - u_1) + m_2(v_2) = 0$$

$$v_1 - v_2 = eu_1$$
(2.6)

Hence

$$v_1 = u_1(m_1 - em_2)/(m_1 + m_2)$$
 (2.6a)

$$v_2 = u_1[(1+e)m_1/(m_1+m_2)]$$
 (2.6b)

The original kinetic energy (KE)['] = $\frac{1}{2}m_1u_1^2$ The final kinetic energy (KE)^{''} = $\frac{1}{2}(m_1v_1^2 + m_2v_2^2)$

$$(KE)' - (KE)'' = \frac{1}{2}m_1u_1^2 - \frac{1}{2}(m_1v_1^2 + m_2v_2^2)$$
(2.7)

Substituting the values of v_1 and v_2

$$(KE)' - (KE)'' = (KE)'[m_1(1 - e^2)/(m_1 + m_2)]$$
 (2.8)

The displacement resulting from a short-duration (τ) impact is given by

$$x = b(t - \tau) \tag{2.9}$$

where *t* is the time beyond τ . For dynamic analysis, the impact time is divided into *ns* small segments and, using Eq. (2.3a),

$$x = \frac{1}{m} \sum_{0}^{n} v_n I_n(\mathbf{t} - \tau_n)$$

$$= \frac{1}{m} \int_0^t F(t - \tau) d\tau$$
 (2.10)

The impact is divided into two phases such that in the first, from time t_1 to t_0 , there will be compression and distortion until $(v_1 + v_2)$ are both reduced to zero (the both aircrafts moving together); in the second, the elastic strain energies in the aircraft are restored and are separated by a negative velocity, $-V_2 = (v_1 + v_2)$.

During the second phase the impulse relation between the aircraft $(F_T - F_{TO})$ will be proportional to F_{TO} and the coefficient or restitution *e* defined above is written as

$$e = (F_T - F_{\rm T0})/F_{\rm T0} \tag{2.11}$$

where $F_{\rm T}$ is the total impulse during the impact and $F_{\rm TO}$ is the impulse in phase one.

At time t_0

$$V_0 = v_{10} + v_{20} = v_1 + \left(\frac{F_{\text{T0}}}{m_1} + v_2 - \frac{F_{\text{T0}}}{m_2}\right) = 0$$
(2.12)

hence

$$V = v_1 + v_2 = \left(\frac{1}{m_1} + \frac{1}{m_2}\right) F_{T_0}$$
(2.13)

Similarly, at time t_2 the relationship becomes

$$V_0 - V_2 = F_T \left(\frac{1}{m_1} + \frac{1}{m_2} \right)$$
(2.14)

Using Eq. (2.11), the expression given in Eq. (2.5a) may be written in the form

$$-\frac{V_2}{V}e\tag{2.15}$$

Equations (2.6), (2.6a) (2.6b) result from the above method. However, from Eq. (2.11) the total impulse is rewritten as

$$F_T = \left(\frac{m_1 m_2}{m_1 + m_2}\right) (1 + e)(v_1 + v_2)$$

$$M(1 + e)V$$
(2.16)

where M is the equivalent combined mass of the aircrafts.

The changes in velocity after impact of the aircrafts are written as

$$\Delta V_1 = \frac{M}{m_1} (1+e)(v_1+v_2) = \frac{M}{m_2} (1+e)V$$

$$\Delta V_2 = \frac{M}{m_2} (1+e)V$$
(2.17)

2.3.1.3 Oblique Impact

When two aircrafts collide and their axes do not coincide, the problem becomes more complex. With oblique impact, as shown in Fig. 2.2, two impulses are generated: the direct impulse, F_T , and the tangential impulse, F'_T . The latter is caused by friction between the impacting surfaces and by local interlocking of the two aircraft in the common surface. Let the angular velocity of the two aircrafts be θ_1 and θ_2 , respectively. If $F'_T/F_T = \lambda'$ and the body's centre of gravity has a coordinate system X and Y, the components of the vector velocity, v_1 and u_1 , normal to the impact surface may be written as follows:

 $x_1 - y_1$ system

$$\mathbf{v}_1 = |\bar{\mathbf{v}}_1| \cos \theta_1 \tag{2.18}$$

$$u = |\bar{v}_1 \sin \theta_1 \tag{2.18a}$$



Fig. 2.2 Oblique impact of the bodies of two different objects

Similarly, v_2 is written as

$$|\bar{v}_2| = V(v_2^2 + u_2^2)$$
(2.19)

$$\beta = \tan^{-1}(u_2/v_2) \tag{2.19a}$$

The momentum equations for the bodies are summarised below:

where v'_1 , v'_2 , u'_1 and u'_2 are for t_1 and t_2 .

 $x_2 - y_2$ system

$$m_2 v_1'' - F_T = m_2 v_2'' \qquad body 2 \\ m_2 v_1'' - 2' F_T = m_2 v_1' \qquad (2.21)$$

$$m_2 u_1 - \lambda F_{\rm T} = m_1 u_2$$

$$m_2 R^2_2 \theta'_2 + F_T y_2 - \lambda' F_{\rm T} x_2 = m_2 R^2_2 \theta'_2$$

$$(2.21)$$

where mR_1^2 and mR_2^2 are the second moment of inertia about the vertical axis passing through the centre of gravity. The rate of approach and the sliding of the two surfaces at the point of contact can be written as

.

$$\Delta V_1 = v_1 + v_2 - \theta_1 y_1 - \theta_2 y_2$$
 (2.22)

$$\Delta V_2 = u_1 + u_2 - \dot{\theta}_1 x_1 - \dot{\theta}_2 x_2 \tag{2.23}$$

The addition to these equations is the restitution given by Eq. (2.15) in which when Eq. (2.22) is substituted and then, in the final equation, Eq. (2.20) is substituted, the value of $F_{\rm T}$ is evaluated as

$$F_T = \frac{V(1+e)}{C_1 - \lambda C_2}$$
(2.24)

where

$$C_1 = \frac{1}{m_1} \left(1 + \frac{y^2_1}{R^2_1} \right) + \frac{1}{m_2} \left(1 + \frac{y^2_2}{R^2_2} \right)$$
(2.24a)

$$C_2 = \left(\frac{x_1 y_1}{m_1 R_1^2} + \frac{x_2 y_2}{m_2 R_2^2}\right)$$
(2.24b)

Using Eqs. (2.20) and (2.21)

$$v'_{2} = v'_{1} - (F_{T}/m_{1})$$

$$u'_{2} = u'_{1} - (\lambda'F_{T}/m_{1})$$

$$\dot{\theta}_{2} = \dot{\theta}_{1} + \frac{y_{1} - \lambda'x_{2}}{m_{1}R_{1}^{2}}F_{T}$$
(2.25)

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$$v''_{2} = v''_{1} - \frac{F_{\rm T}}{m_{2}}$$

$$u''_{2} = u''_{1} - \frac{\lambda' F_{T}}{m_{2}}$$

$$\dot{\theta}_{2} = \dot{\theta}_{1} + \frac{y_{2} - \lambda' x_{2}}{m_{2} R_{2}^{2}} F_{\rm T}$$
(2.26)

Figure 2.3 shows plots for Eqs. (2.25) and (2.26). It is interesting to note that larger values of λ' show greater interlocking of the surfaces of the two aircrafts and with *e* reaching zero, a greater plastic deformation occurs.



Fig. 2.3 Velocity versus λ' for oblique impact problems

2.3.1.4 Case Studies

(1) One aircraft impacting a rigid barrier, or containment vessel located with no angular velocity

$$\frac{1}{m_2} = 0, \quad v_1 = 0, \quad u_1 = 0, \quad \theta_1 = 0$$
 (2.27)

$$C_1 = \frac{1}{m_1} \left(\mathbf{1} + \frac{y_1^2}{R_1^2} \right); \quad C_2 = \left(\frac{x_1 y_1}{m_1 R_1^2} \right)$$
(2.27a)

$$v_2' = v_1'(y_1^2 - \lambda' x_1 y_1 - R^2)/\bar{\lambda}$$
 (2.27b)

$$u'_{2} = u'_{1} - v'_{1} \left(\frac{\lambda'(1+e)R^{2}}{\lambda} \right); \quad \dot{\theta}_{1} = \frac{(1+e)(y_{1} - \lambda'x_{1})}{\lambda}$$
 (2.27c)

$$\bar{\lambda} = y^2_1 - \lambda'^{x_1 y_1} + R^2$$
 (2.27d)

where

(2) Circular impactor with radius r_1 .

 $x_1 = r_1 \quad \text{and} \quad y_1 = 0 \tag{2.28}$

$$v_2' = ev_1' \tag{2.28a}$$

$$u'_2 = u_1 - \lambda' v'_1 (1+e)$$
 (2.28b)

$$\dot{\theta}_1 = -v_1' \lambda' r_1 (1+e) / R^2$$
 (2.28c)

For a circular impactor, $R^2 = 2r_1^2/5$

$$\dot{\theta} = -v_1'(5\lambda'(1+e)/2r_1)$$
 (2.28d)

(3) Inelastic collisions. The value of e = 0 in the above case studies: Case study (1)

$$v'_{2} = v'_{1}(y^{2}_{1} - \lambda' x_{1}y_{1})/\bar{\lambda}$$

$$u'_{2} = u'_{1} - v'_{1}(\lambda' R^{2}/\bar{\lambda})$$

$$\theta_{1} = (y_{1} - \lambda' x_{1})/\bar{\lambda}$$
(2.29)

Case study (2)

$$v_{2}' = 0, u_{2}' = u_{1}' - \lambda' v_{1}'$$

$$\theta_{1} = -v_{1}' \lambda r_{1} / R^{2} = -2.5 v_{1}' \lambda / r_{1}$$
(2.30)

 (4) Where no interlocking exists, λ' in the above expressions. This means the aircrafts do not interlock each other but their bodies have created damages.

2.3.2 Aircraft Impact on Nuclear Structures – Peak Displacement and Frequency

2.3.2.1 General

A great deal of work has been carried out on the subject of missile and aircraft impact. Tall structures are more vulnerable to civilian, wide-bodied jets or multi-role combat aircraft. A great deal of work on this subject will be reported later. In this section a preliminary analysis is given for the determination of peak displacement and frequency of a tall structure when subject to an aircraft impact. As shown in Fig. 2.4, the overall dimensions of the building are given. Let *A* be the base area and *h* be the maximum height of the building. According to the principle of the conservation of momentum, if *m* is mass and v_1 is the velocity of the aircraft approaching the building, then using a linear deflection profile

$$I(t) = F_1(t) = mv_1 = \left(\frac{\rho Ah}{2g}\right)v_{20}$$
(2.31)





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where ρ is the density or average specific weight and v_{20} is the velocity of the tip of the nuclear facility.

The initial velocity, v_{20} , of the facility can thus be evaluated from Eq. (2.31). Free vibrations studied by the time-dependent displacement $\delta(t)$ is given by

$$\delta(t) = \left(\frac{v_{20}}{\omega}\right) \sin \omega t$$

= $\left[v_{20}/(2\pi/T)\right] \sin \omega t$ (2.32)
= $\left[v_{20}/\sqrt{(k_s/m_s)}\right] \sin \omega t$

where ω is the circular frequency and k_s and m_s are the equivalent nuclear facility stiffness and mass, respectively.

Using Eq. (2.31) for v_{20} and $\sin \omega t = 1$ for $\delta_{\max}(t)$, the peak dynamic displacement, $\delta_{\max}(t)$, is given by

$$\delta_{\max}(t) = m v_1 g T / \pi \rho A h \tag{2.32a}$$

The equivalent point load generated for the peak dynamic displacement is given by Eq. (2.32a). If that load is $F_1(t)$, then work done is equal to the energy stored and

$$F_1(t) \times \delta_{\max}(t) = \frac{1}{2} k_{\rm s} \delta_{\max}^2(t)$$
(2.33)

for which

$$F_1(t) = \frac{1}{2}k_s\delta_{\max}(t) \tag{2.33a}$$

While momentum is conserved, a portion of energy of the aircraft is lost on impact. The loss of energy E_1 is then written as

$$E_1 = \frac{1}{3} \left(\rho Ah/mg\right) \left(v_{20}/v_1\right)^2 \tag{2.34}$$

Equation in case study (1) and Eq. (2.29) for inelastic collisions are applied with and without the interlocking parameter, λ' .

The velocity of the new target for the ideal plastic impact is given by

$$\dot{u}_{t} = \left[(m_{b}(t) + m_{t})\dot{u}_{i}^{-} + m_{t}\dot{u}_{i}^{-} \right] / \left[(m_{b}(t) + 2m_{t}) \right]$$
(2.35)

Again the superscripts + and - indicate just after and just before impact. Wolf et al. (3.169) tested their work on rigid and deformable targets. Data used in their work are reported below: Rigid target Boeing 707-320 $m_a = 127.5 \text{ Mg}$ $m_w = 38.6 \text{ Mg}$ included in m_a $\varepsilon_y = 2 \times 10^{-3}$; $\varepsilon r = 5 \times 10^{-2}$ Deformable target Impact area = 37.2-45.1 m²

Private Communication Feb 1993. Also reported in the Author's book "Impact & Explosion 1993" published by Blackwell Science, Oxford 1993.

The tables given for aircrafts and other impacts give data to be used for load-time function or relationship for rigid and deformable targets. The elastic and inelastic systems have been included.

The method of Wolf et al. was idealised into 3D Finite Element method using programs BANG and ISOPAR. Both flexible and rigid targets of 15,000–350,000 isoparametric elements with 750,000 hybrid mixed elements for the aircraft were adopted. The force time–function relationships were combined and they are plotted for various aircrafts. The comparative study is given for these aircraft in (Fig. 2.5). This graph is readily available for the respective impact or crash analysis of any structure. These graphs can be improved by analysing other types of aircrafts.



Fig. 2.5 Model aircraft impacting against a rigid surface

2.3.3 Finite Element Applications

This subject has been dealt with in much greater detail in Chapter 3 using dynamic finite element technique. The analysis given under Sections 2.3.1 and 2.3.2 are taken as basis for the finite element approach. Various

load-time functions for different aircrafts have been evaluated so as to suite specific aircraft crash analysis, particularly on containment vessels. A list of containment vessels adopted for various nuclear power stations is given in a tabulated form in Tables 2.24 and 2.25. They can be treated as test examples on the lines given in a sample design example on the TVA containment vessel. The design pressures are given in Tables 2.24 and 2.25 with changed dimensions, loads and material properties; new calculations can be made for the existing vessels and for containments of future BWR and PWR nuclear stations. The dynamic analysis given in chapter 3 can also be used when these containments are accurately analysed under environmental and other anticipated loads such as aircraft and missile crashes, fire and explosion, earthquakes and other hazards.

2.3.4 Additional Data on Containment Parameters

2.3.4.1 General Introduction

Tables 2.24 and 2.25 show containments with internal pressures. Some of them are chosen in this section as test examples for readers who wish to test the work in this text.

| (a) | Doel 4: Status P.W.R 1041 MW in Belgium-FRAMATONE |
|-----|---|
| | Double walled-double dome resting on piles |
| | R = 21.90 m inside cylinder |
| | Space between walls $= 3.34 \text{ m}$ |
| | Total height $= 55 \text{ m}$ |
| | Spherical domical space $= 3.34 \text{ m}$ |
| | Wall and dome thickness $= 0.8-1.3$ m |
| (b) | Tricastin: Status P.W.R 900 MW in France-FRAMATONE $R = 18.5$ m inside cylinder |
| | Wall thickness = 0.9 m ; 12 m buttresses Total height = 59.5 m thick above ground level Base slab = 5 m , base slab = 55.2 m with keys, 1.5 m keys depth variable |
| (c) | Civaux: Status P.W.R 1400 MW in France-FAMATONE Double wall type Double dome type Total height of walls = 545 m Spaces = 3.34 m along the walls Base slab = 50.90 m |
| (d) | Sizewell B: Status P.W.R 1258 MW in UK. WESTING HOUSE Dimensions given as an example in the text |

| Country | Name | Type | Containment type | Design pressure |
|------------|-------------------|------|------------------------------|--------------------|
| Argentina | Embalse | PHWR | Steel and RC | |
| Armenia | Medzamor 2 | WER | Reinforced concrete (RC) | 0.200 |
| Belgium | Doel 3 | PWR | Double PC/RC | 0.450 |
| Belgium | Tihange 2 | PWR | Double PC/RC | 0.450 |
| Belgium | Tihange 3 | PWR | Double PC/RC | |
| Brazil | Angra 1 | PWR | Steel and RC | |
| Bulgaria | Kozloduy 5 | WER | Prestressed concrete (PC) | |
| Canada | Bruce A1 | PHWR | Reinforced concrete (RC) | |
| Canada | Bruce B5 | PHWR | Reinforced concrete (RC) | 0.291 |
| Canada | Darlington | PHWR | Prestressed concrete (PC) | 0.197 |
| Canada | Gentilly 2 | PHWR | Prestressed concrete (PC) | 0.217 |
| Canada | Pickering B 5 | PHWR | Reinforced concrete (RC) | 0.141 |
| Canada | Point Lepreau 1 | PHWR | Prestressed concrete (PC) | 0.104 |
| China | Daya Bay | PWR | Prestressed concrete (PC) | 0.520 |
| China | Lingao | PWR | Prestressed concrete (PC) | 0.520 |
| China | Qinshan 1 | PWR | Prestressed concrete (PC) | 0.360 |
| China | Qinshan 3 | PHWR | Prestressed concrete (PC) | 0.224 |
| China | Qinshan II-1 | PWR | Prestressed concrete (PC) | 0.450 |
| China | Tianwan | WER | Double PC/RC | 0.500 |
| Czech. Rep | Dukovany | WER | | |
| Czech. Rep | Temelin | WER | Prestressed concrete (PC) | 0.490 |
| Finland | Olkiluoto (TVO) 1 | BWR | Prestressed concrete (PC) | 0.470 |
| France | Belleville 1 | PWR | Double PC/RC | 0.520 |
| France | Blayais 1 | PWR | Prestressed concrete (PC) | 0.500 |
| France | Bugey | PWR | Prestressed concrete (PC) | 0.500 |
| France | Cattenom 1 | PWR | Double PC/RC | 0.520 |
| France | Chinon B1 | PWR | Prestressed concrete (PC) | 0.500 |
| France | Chooz 1 | PWR | Double PC/RC | 0.530 |
| France | Civaux 1 | PWR | Double PC/RC | 0.530 |

 Table 2.24
 Nuclear Power Plants: Containment types and design pressures

| | | | | Design |
|------------------|-------------------------|------|------------------------------|----------|
| Country | Name | Type | Containment type | pressure |
| France | Civaux 2 | PWR | Double PC/RC | 0.530 |
| France | Cruas 1 | PWR | Prestressed concrete (PC) | 0.500 |
| France | Dampierre 1 | PWR | Prestressed concrete (PC) | 0.500 |
| France | Fessenheim | PWR | Prestressed concrete (PC) | 0.473 |
| France | Flamanville 1 | PWR | Double PC/RC | 0.480 |
| France | Golfech 1 | PWR | Double PC/RC | 0.520 |
| France | Granvelines 1 | PWR | Prestressed concrete (PC) | 0.500 |
| France | Nogent 1 | PWR | Double PC/RC | 0.520 |
| France | Paluel 1 | PWR | Double PC/RC | 0.480 |
| France | Penly 1 | PWR | Double PC/RC | 0.520 |
| France | St Alban 1 | PWR | Double PC/RC | 0.480 |
| France | St Laurent B1 | PWR | Prestressed concrete (PC) | 0.500 |
| France | Tricastin | PWR | Prestressed concrete (PC) | 0.500 |
| Germany | Brokdorf | PWR | | 0.750 |
| Germany | Emsland | PWR | Steel and RC | 0.630 |
| Germany | Grafenrheinfeld | PWR | | |
| Germany | Grohnde | PWR | | |
| Germany | Gundremmingen KRB II | BWR | Reinforced concrete (RC) | 0.430 |
| Germany | Isar 1 | BWR | | |
| Germany | Isar 2 | PWR | Steel and RC | 0.630 |
| Germany | Krummel | BWR | | |
| Germany | Mulheim Karlich | PWR | | |
| Germany | Neckar 1 | PWR | Steel | 0.570 |
| Germany | Neckar 2 | PWR | Steel and RC | 0.630 |
| Germany | Philppsburg 2 | PWR | | |
| Germany | Unterweiser | PWR | Steel | 0.580 |
| Great Britian | Heysham | AGR | Prestressed concrete (PC) | |
| Great Britian | Sizewell B | PWR | Double PC/RC | 0.445 |
| Great Britian | Tomess PT 1 | AGR | Prestressed concrete (PC) | |
| Hungary | Paks 1 | VVER | | |
| India | FBTR Kalpakkam | FR | | |
| India | Kaiga 1 | PHWR | Double PC/RC | 0.273 |
| India | Kaiga 2 | PHWR | Double PC/RC | 0.273 |
| India | Kakrapara 1 | PHWR | Double PC/RC | 0.225 |
| India | Narora 1 | PHWR | Double PC/RC | 0.225 |
| India | Rajasthan 3 | PHWR | | 0.273 |

 Table 2.24 (continued)

| | | | | Design |
|---------|--------------------|------|------------------------------|----------|
| Country | Name | Type | Containment type | pressure |
| India | Tarapur 3 | PHWR | Double PC/RC | 0.244 |
| Iran | Busher | PWR | Steel | |
| Japan | Fukushima 1-4 | BWR | Steel | 0.490 |
| Japan | Fukushima 1-6 | BWR | Steel | 0.385 |
| Japan | Fukushima II-1 | BWR | Steel | 0.385 |
| Japan | Genkai 4 | PWR | Prestressed concrete (PC) | 0.500 |
| Japan | Hamaoka 2 | BWR | Steel | 0.492 |
| Japan | Hamaoka 3 | BWR | Steel | 0.535 |
| Japan | Ikata 1 | PWR | Steel | 0.345 |
| Japan | Ikata 3 | PWR | Steel | 0.389 |
| Japan | Kashiwazaki 4 | BWR | Steel | 0.416 |
| Japan | Kashiwazaki 6 ABWR | BWR | Reinforced concrete (RC) | 0.416 |
| Japan | Kashiwazaki 1 | BWR | Steel | 0.385 |
| Japan | Mihama 3 | PWR | Steel | 0.340 |
| Japan | Monju | FR | | |
| Japan | Ohi 1 | PWR | Steel | 0.540 |

 Table 2.24 (continued)

 Table 2.25
 Nuclear Power Plants–PWR, PHWR, RBMK, WER (Containments and design pressures)

| C | NT | Ŧ | | Design |
|----------|----------------|------|---------------------------|----------|
| Country | Name | Type | Containment type | Pressure |
| Japan | Ohi 3 | PWR | Prestressed concrete (PC) | 0.500 |
| Japan | Sendai 1 | PWR | Steel | 0.325 |
| Japan | Shika 1 (NOTO) | BWR | Steel | 0.535 |
| Japan | Shimane 2 | BWR | Steel | 0.535 |
| Japan | Takahama 3 | PWR | Steel | 0.360 |
| Japan | Tokai 2 | BWR | Steel | 0.385 |
| Japan | Tomari 1 | PWR | Steel | 0.360 |
| Japan | Tsuruga 2 | PWR | Prestressed concrete (PC) | 0.500 |
| Lituania | Ignalina 1 | RBMK | | |
| Mexico | Laguna Negra 1 | BWR | | |
| Pakistan | Chasma | PWR | Prestressed concrete (PC) | |
| Romania | Cernavoda | PHWR | | |
| Russia | Balakovo 1 | WER | Prestressed concrete (PC) | 0.490 |
| Russia | Balakovo 5 | WER | Prestressed concrete (PC) | 0.490 |
| Russia | Balakovo 6 | WER | Prestressed concrete (PC) | 0.490 |
| Russia | Kalinin 1 | WER | Prestressed concrete (PC) | 0.455 |
| Russia | Kalinin 3 | WER | Prestressed concrete (PC) | 0.490 |
| Russia | Kursk | RBMK | | |
| Russia | Novovoronej 5 | WER | Prestressed concrete (PC) | 0.455 |
| Russia | Novovoronej 6 | WER | Prestressed concrete (PC) | 0.490 |
| Russia | Novovoronej7 | WER | Prestressed concrete (PC) | 0.490 |

| | | | | Design |
|-------------|---------------------|------------|---|----------|
| Country | Name | Туре | Containment type | Pressure |
| Russia | Rostov 1 | WER | Prestressed concrete (PC) | 0.490 |
| Russia | Smolensk 1 | RBMK | | |
| Slovakia | Bohunice 1 | WER | | |
| Slovakia | Mochovce 1 | WER | | |
| Slovenia | Krsko | PWR | Steel and RC | |
| South | Koeberg | PWR | Prestressed concrete (PC) | 0.500 |
| Africa | | | | |
| South | Kori 3 | PWR | Prestressed concrete (PC) | 0.520 |
| Korea | | | | |
| South | Uljin 1 | PWR | Prestressed concrete (PC) | 0.500 |
| Korea | | | | |
| South | Wolsong 1 | PHWR | Prestressed concrete (PC) | 0.156 |
| Korea | XZ 1 | DUVD | | 0.520 |
| South | Yonggwang I | PWK | Prestressed concrete (PC) | 0.520 |
| Spain | Almoroz 1 | DWD | | |
| Spain | | | Prostroggod concrete (PC) | 0.480 |
| Spain | Asco 1 | | Flestressed colletete (FC) | 0.460 |
| Spain | Asco 2 Cofrontes | | | |
| Spain | Trillo 1 | | | |
| Spain | Vandellos 2 | | | |
| Spann | Foremark 3 | | $\mathbf{P}_{\mathbf{r}}$ as transferred concrete ($\mathbf{P}_{\mathbf{C}}$) | 0.600 |
| Sweden | Ockarshamn 2 | | Prestressed concrete (PC) | 0.000 |
| Sweden | Dinghale 3 | DWR DWR | Prestressed concrete (PC) | 0.514 |
| Switzerland | Gösgen | PWR | Steel | 0.589 |
| Switzerland | Leibetadt | RWR | Steel and RC | 0.203 |
| Taiwan | Kuosheng 1 | BWR | Steel and Re | 0.205 |
| Taiwan | Lugmen | ABWR | Reincorced concrete | |
| Taiwaii | Luginen | | (RC) | |
| Taiwan | Maanshan 1 | PWR | | |
| Ukraine | Khmelnitsky 1 | WER | Prestressed concrete (PC) | 0.490 |
| Ukraine | Khmelnitsky 2 | WER | Prestressed concrete (PC) | 0.490 |
| Ukraine | Rovno 1 | WER | | |
| Ukraine | Rovno 3 | WER | Prestressed concrete (PC) | 0.490 |
| Ukraine | Rovno 4 | WER | Prestressed concrete (PC) | 0.490 |
| Ukraine | Sud Ukraine 1 | WER | Prestressed concrete (PC) | 0.490 |
| Ukraine | Tchernobyl 3 | RBMK | | |
| Ukraine | Zaporozhe 5 | WER | Prestressed concrete (PC) | 0.490 |
| USA | Braidwood 1 | PWR | Prestressed concrete (PC) | 0.445 |
| USA | Byron 1 | PWR | Prestressed concrete (PC) | 0.445 |
| USA | Callaway -1 | PWR | Reinforced concrete | |
| | | DUUD | (RC) | 0.004 |
| USA | Catawba 1 | PWR | Steel and RC | 0.204 |
| USA | Clinton 1 | BWR | Reinforced concrete (RC) | 0.204 |
| USA | Comanche 1 | PWR | Reinforced concrete | 0.445 |
| | | | (RC) | |

 Table 2.25 (continued)

| | | | | Design |
|---------|-------------------|------|------------------------------|----------|
| Country | Name | Type | Containment type | Pressure |
| USA | Gran Gulf 1 | BWR | Reinforced concrete (RC) | 0.203 |
| USA | Hatch 2 | BWR | | |
| USA | Hope Creek | BWR | Steel | 0.528 |
| USA | La Salle 1 | BWR | Prestressed concrete (PC) | 0.410 |
| USA | Millstone 3 | PWR | Reinforced concrete (RC) | |
| USA | Nine Mile Point 2 | BWR | Reinforced concrete (RC) | 0.411 |
| USA | Palo Verde 1 | PWR | Prestressed Concrete (PC) | 0.514 |
| USA | Perry 1 | BWR | Steel | 0.204 |
| USA | River Bend 1 | BWR | Steel | 0.204 |
| USA | San Onofre 2 | PWR | Prestressed concrete (PC) | 0.514 |
| USA | Seabrook 1 | PWR | Reinforced concrete (RC) | 0.459 |
| USA | Shearon-Harris 1 | PWR | Reinforced concrete (RC) | |
| USA | Shoreham | BWR | Reinforced concrete (RC) | 0.389 |
| USA | South Texas | PWR | Prestressed concrete (PC) | |
| USA | St. Lucie 2 | PWR | Steel and RC | 0.376 |
| USA | Summer 1 | PWR | Prestressed concrete (PC) | |
| USA | Susquehanna 1 | BWR | Reinforced concrete (RC) | |
| USA | Vogtle 1 | PWR | Prestressed concrete (PC) | 0.459 |
| USA | Waterford 3 | PWR | Steel and RC | |
| USA | Watts Bar 1 | PWR | Steel and RC | 0.193 |
| USA | WNP-2 Hanford | BWR | Steel | |
| USA | Wolf Creek | PWR | Prestressed concrete (PC) | |

Table 2.25 (continued)

- (e) GenKai 4: P.W.R 1180 MW in Japan-MITSUBISHI R = 22.150 m Total height of walls = single-type 43 m wall thickness = 0.75–1.3 m Single dome height = 22.6 m Dome thickness = 1 m Dome radius = 22.650 Base slab inclusive gallents = 44.30 m Thickness varies from 10.2 m to 15.8 m
 (f) Kaiga-I: P.H.W.R 220 MW in India (Double Wall Type) R = radius inside = 21.28 m
 - Total height of the wall = 48.235 m
 - Inner space of walls = 2.0 m

Inner space of dome = 2.0 mRadius to centroid = 33.57 m inner Radius of the dome spherical = 39.60 outerBase slab (without keys) thickness = 3.5 mBase slab (with keys) thickness = 5.5 mBase slab total dimension = 49.0 mKey base = 8.5 m

Note: LOCA ranges in all from 0.3 to 0.35 MPa. Exceptional causes LOCA = 0.47-0.60 MPa related to BWR types.

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Chapter 3 Dynamic Finite Element Analysis

3.1 Introduction

A great deal of work has been published on finite element techniques.

This chapter presents the linear and non-linear dynamic finite element analysis intended to be used for nuclear facilities. Plasticity and cracking models are included. Solid isoparametric elements, panel and line elements are included which represent various materials. Solution procedures are recommended. Programs ISOPAR, F-BANG and other computer packages are recommend for the dynamic non-linear analysis of structures for nuclear facilities with and without cracking.

3.1.1 Finite Element Equations

A 3D finite element analysis is developed in which a provision has been made for time-dependent plasticity and rupturing in steel and cracking in materials such as concrete. The influence of studs, tugs and connectors is included. Concrete steel liners and studs are represented by solid isoparametric elements, shell elements and line elements with or without bond linkages. To begin with, a displacement finite element is adopted.

The displacement field within each element is defined in Fig. 3.1 as

$$\{\mathbf{x}\} = [N]\{\mathbf{x}\}^{e} = \sum_{i=1}^{n} (N_{i}[I]\{\mathbf{x}\}_{i})$$
(3.1)

The strains and stresses can then be expressed as

$$\epsilon \{x\}^{\mathrm{e}} = \sum_{i=1}^{n} ([B_i]\{x\}_i) = [D]\{\sigma\}$$
(3.2)

In order to maintain equilibrium with the element, a system of external nodal forces $\{F\}^{C}$ is applied which will reduce the virtual work (*dW*) to zero. In the


Fig. 3.1 (a) Isoparametric elements: (i) parent element, 3D isoparametric derived element; (ii) solid element (20-noded); (iii) 32-noded solid element. (b) Line elements within the body of the solid isoparametric elements (ISS – isoperametric solid element)







general equilibrium equation, both Eqs. (3.1) and (3.2) are included. The final equation becomes

$$(\{\boldsymbol{d\delta}\}^{\mathrm{e}})^{T}\{\boldsymbol{F}\}^{\mathrm{e}} = (\{\boldsymbol{d\delta}\}^{\mathrm{e}})^{T} \int_{\mathrm{vol}} [\boldsymbol{B}]^{T}\{\boldsymbol{\sigma}\} \boldsymbol{dV}$$
(3.3)

In terms of the local coordinate { $\{\xi, \eta, \zeta\}$ } system, Eq. (3.3) is written as

$$\{F\}^{\mathbf{e}} = \int_{\mathrm{vol}} [B]^{T} [D] \{\epsilon\} d\xi, d\eta, d\zeta \det[J] \{x\}^{\mathbf{e}}$$
(3.4)

The force-displacement relationship for each element is given by

$$\{F\}^{e} = [K]^{e} \{u\}^{e} + \{F_{b}\}^{e} + \{F_{s}\}^{e} + \{F_{\sigma}\}^{e}_{i} + \{F_{\varepsilon}\}^{e}_{c}$$
(3.5)

where the element stiffness matrix is

$$[\mathbf{K}_{c}] = \int_{vol} [\mathbf{B}]^{T} [\mathbf{D}] [\mathbf{B}] dV$$
(3.5a)

The nodal force due to the body force is

$$\{F_{\rm b}\}^{\rm e} = -\int_{\rm vol} [N]^T \{G\} dV \qquad (3.5b)$$

The nodal force due to the surface force is

$$\{F_{\rm s}\}^{\rm e} = -\int_{\rm s} [N]^T \{p\} ds \qquad (3.5c)$$

The nodal force due to the initial stress is

$$\{\boldsymbol{p}_{\boldsymbol{\sigma}}\}_{i}^{e} = \int_{vol} [\boldsymbol{B}]^{T} \{\boldsymbol{\sigma}_{o}\} d\boldsymbol{V}$$
(3.5d)

The nodal force due to the initial strain is

$$\{\boldsymbol{p}_{\boldsymbol{\epsilon}}\}_{i}^{\mathrm{e}} = -\int_{\mathrm{vol}} [\boldsymbol{B}]^{T} [\boldsymbol{D}] \{\boldsymbol{\epsilon}_{\mathrm{o}}\} d\boldsymbol{V}$$
(3.5e)

Equations (3.4) and (3.5) represent the relationships of the nodal loads to the stiffness and displacement of the structure. These equations now require modification to include the influence of the liner and its studs. The material compliance matrices [D] are given in Tables 3.1 and 3.2. The numerical values are given for various materials or their combinations in Tables 3.3, 3.4, 3.5 and 3.6. These values of the constitutive matrices are recommended in the absence of specific information.

(a) [D] for steel components (isotropic)

Constant Young's modulus and Poisson's ratio

(b) [D] for concrete: variable E and constant v

$$D_{11} = \frac{E_1(E_1^{3} - E_{\alpha})}{E_1} \qquad D_{12} = \frac{vE_1E_2(E_1^{3} + E_{\alpha})}{2} \qquad D_{13} = \frac{vE_1E_2(E_1^{3} + E_{\alpha})}{2} \qquad D_{13} = \frac{vE_1E_2(E_1^{3} + E_{\alpha})}{2} \qquad D_{14} = 0 \qquad D_{15} = 0 \qquad D_{16} = 0 \qquad D_{16} = 0 \qquad D_{26} = 0 \qquad D_{26}$$

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| able 3.2 $[D]$ with variable Young's modulus : |
| Table 3.2 [D] with variable Young's modulus : |
| Table 3.2 [D] with variable Young's modulus : |
| Table 3.2 [D] with variable Young's modulus : |

 $\overline{E} - 1 - v_{12}v_{21} - v_{13}v_{31} - v_{23}v_{32} - v_{12}v_{23}v_{31} - v_{21}v_{13}v_{32}$ $E_1v_{21} = E_2v_{12} \quad D_{44} = G_{12}$ $E_2v_{32} = E_3v_{23} \quad D_{55} = G_{23}$

 $D_{66} = G_{13}$

 $E_3 v_{13} = E_1 v_{31}$

The values of G_{12} , G_{23} and G_{13} are calculated in terms of the modulus of elasticity and Poisson's ratio as follows:

$$G_{12} = \frac{1}{2} \left[\frac{E_1}{2(1+\nu_{12})} + \frac{E_2}{2(1+\nu_{21})} \right] = \frac{1}{2} \left[\frac{E_1}{2(1+\nu_{12})} + \frac{E_1}{2\left(\frac{E_1}{E_2} + \nu_{12}\right)} \right]$$

$$G_{23} = \frac{1}{2} \left[\frac{E_2}{2(1+\nu_{23})} + \frac{E_3}{2(1+\nu_{23})} \right] = \frac{1}{2} \left[\frac{E_2}{2(1+\nu_{23})} + \frac{E_2}{2\left(\frac{E_3}{E_1} + \nu_{23}\right)} \right]$$

$$G_{13} = \frac{1}{2} \left[\frac{E_3}{2(1+\nu_{31})} + \frac{E_1}{2(1+\nu_{13})} \right] = \left[\frac{E_3}{2(1+\nu_{13})} + \frac{E_3}{2\left(\frac{E_3}{E_1} + \nu_{31}\right)} \right]$$
For isotropic cases: $E_1 = E_2 = E_3 = E$ $\nu_{12} = \nu_{13} = \nu_{23} = \nu_{21} = \nu_{31} = \nu_{32} = \nu$

| (1) Concrete | | |
|-----------------------|--|--|
| $\sigma_1 = \sigma_2$ | $v_1 = v_{23} = 0.2$ for any value of σ_3 up to 500 bar | |
| $\sigma_{1<}\sigma_2$ | $v_{13} > v_{23}$ | |
| $\sigma_{1}=0$ | $v_{13} = 0.2$ to 0.4 for any value of σ_2 | |
| | = 0.4 for up to σ_3 = 500 bar | |

 Table 3.3 Material properties of concrete, bovine, steel and composites

for 80°C temperature, the above values are increased by 35-50%

| $E_{\rm c}({\rm KN/mm^2})$ | 24 | 30 | 35 | 40 |
|----------------------------|-----------|-----------|-----------|-----------|
| v | 0.15-0.18 | 0.17-0.20 | 0.20-0.25 | 0.25-0.30 |

Alternatively

 $v = 0.2 + 0.6(\sigma_{2/}\sigma_{cu})^4 + 0.4(\sigma_{1/}\sigma_{cu})^4$

Where σ_1, σ_2 and σ_3 are the pressures/stresses along the three principal axes and σ_{cu} is the ultimate compressive strees of concrete

(2) Bovine material $E_1 = 11-18$ GPa: $E_2 = 11-19$ GPa; $E_3 = 17-20$ GPa $G_{12} = 3.6-7.22$ GPa; $G_{13} = 3.28-8.65$ GPa; $G_{23} = 8.285-8.58$ GPa $v_{12} = 0.285-0.58$: $v_{13} = 0.119-0.31$; $v_{23} = 0.142-0.31$ $v_{21} = 0.305-0.58$: $v_{31} = 0.315-0.46$; $v_{32} = 0.283-0.46$ (3) Steel E = 200 GN/m²; v = 0.3-0.33(4) Composite Hot-pressed silicone nitride (HPSN) versus tungsten carbide E = 320 GPa v = 0.26 E = 320 GPa V = 0.24

Carbon fibre (reinforced epoxy with 60% fibres by volume)

| | Longitudinal | Transverse |
|--|--------------|------------|
| Tensile strength (σ_{tu}) | 1750 MPa | 60 MPa |
| Compressive strength | 1300 MPa | _ |
| Tensile modulus (E_t) | 138 GPa | 9.1 GPa |
| Compressive modulus (E'_{c}) | 138 GPa | 9.1 GPa |
| Failure strain in tension $(\varepsilon_{tu})\%$ | 1.34 | 0.8 |
| Failure strain in compression (ε_{cu}) % | 0.85 | 2.9 |

Table 3.4 Material properties of additional composites

| | 1 1 1 | |
|--------------------------|--|---------------|
| Steel indenter | Versus | |
| $E = 200 \text{ GN/m}^2$ | | |
| v = 0.3 - 0.33 | \downarrow | |
| | (1) Plexiglass | |
| | $E = 3.435 \text{ GN/m}^2$ | |
| | v = 0.394 | |
| | (2) Laminate: thornel 300/5208 with fibres oriented | (0, +60, -60) |
| | $E_1 = 50 \text{ GN/m}^2$; $E_2 = 11.6 \text{ GN/m}^2$ | |
| | $G_{11} = 19 \text{ GN/m}^2$; $G_{12} = 4.0 \text{ GN/m}^2$ | |
| | $v_{11} = 0.31$ $v_{12} = 0.06$ | |

| (2) Aluminium and EB Da | (continued) | | | |
|--|--------------------------|--------------|--------------------|------------------------|
| (3) Aluminium and FRPs | DED D ³ | GERRA | CED D ³ | GEDDI |
| Aluminium $\Gamma(C) V(m^2)$ | BF RP" | GFRP | CFRP" | CFRPL |
| E(GN/m) | 707 | 7.0 | 70 | 190 |
| v 70 | /8./ | 7.0 | /0 | 180 |
| 0.5 | 0.52 | 0.30 | 0.30 | 0.28 |
| ^a Quasi-isotropic | | | | |
| ^o Random mat | | | | |
| Unidirectional | | | | |
| (4) Graphite/epoxy | | | | |
| (Web-stiffened foam sand | wich panels w | ith orthotro | pic facing an | d a number |
| of four equally embedded | stiffeners in a | a polyuretha | ne (PU) core | e) |
| $E_1 = 120.7 \text{ GN/m}^2; E_2 = 7.$ | .93 GN/m | | | |
| $G_{12} = G_{23} = G_{13} = 5.52 \text{ GN}$ | $/m^2$ | | | |
| $v_{12} = 0.30$ | | | | |
| Polyurethane foam | | | | |
| $E = 0.0431 \text{ GN/m}^2; G_2 = 0$ | $.017 \text{ GN/m}^2$; | v = 0.267 | | |
| (5) Boron/epoxy composite | 25 | | | |
| $E_1 = 219.8 \text{ GN/m}^2; E_2 = 2$ | $1.4 \text{GN/m}^2; v$ | =0.208 | | |
| $E_{p1} = 2.41 \text{ GN/m}^2; E_{p2} = 0$ | 0.04 GN/m^2 ; | | | |
| $G_{\rm p} = 0.008 \text{ GN/m}^2$; Pat pl | astic level | | | |
| $\sigma_{\rm yt} = 1.1 \ {\rm GN/m^2}$ | | | | |
| (6) Layers of woven roving | and chopped | strand mat | | |
| $E_1 = 14.5 \text{ GN/m}^2; \sigma_{yt} = 21$ | 5 N/mm^2 ; v = | 0.21 | | |
| (7) Other materials | | | | |
| | E_1 | E_2 | G | |
| Туре | (GN/m^2) | (GN/m^2) | (GN/m^2) | <i>v</i> ₁₂ |
| CSM/polyester | 8 | 8 | 3 | 0.32 |
| WR/polyester | 15 | 15 | 4 | 0.15 |
| Glass fibre/polyester | 25 | 25 | 4 | 0.17 |
| UD glass/polyester | 40 | 10 | 4 | 0.3 |
| UD Kevlar/epoxide | 76 | 8 | 3 | 0.34 |
| UD carbon/epoxide | 148 | 10 | 4 | 0.31 |
| GY70/epoxy(celion with | | | | |
| graphite fibre) | 102 | 7.0 | 4.14 | 0.318 |
| MODMORE II/epoxy | | | | |
| HMS/E (with graphite | | | | |
| fibres) | 76.8 | 9.6 | 5.83 | 0.305 |
| | | | | |
| T300/E (thornel 300/ | | | | |
| T300/E (thornel 300/ epoxy with graphite | | | | |
| T300/E (thornel 300/ epoxy with graphite fibres) | 54.86 | 12 | 5.83 | 0.30 |
| T300/E (thornel 300/ epoxy with graphite fibres) GL/E (glass/epoxy) | 54.86 30.3 | 12 149.9 | 5.83 5.84 | 0.30 0.32 |
| T300/E (thornel 300/ epoxy with graphite fibres) GL/E (glass/epoxy) Carbon fibre (60% | 54.86 30.3 | 12 149.9 | 5.83 5.84 | 0.30 0.32 |
| T300/E (thornel 300/ epoxy with graphite fibres) GL/E (glass/epoxy) Carbon fibre (60% volume) | 54.86 30.3 | 12 149.9 | 5.83 5.84 | 0.30 0.32 |
| T300/E (thornel 300/ epoxy with graphite fibres) GL/E (glass/epoxy) Carbon fibre (60% volume) Reinforced epoxy | 54.86 30.3 | 12 149.9 | 5.83 5.84 | 0.30 0.32 |

3.1 Introduction

| | Table 3.4 (continued) | |
|-----------------------------------|-----------------------|------------|
| | Longitudinal | Transverse |
| $E_1 (GN/m^2)$ | 140.0 | 9.00 |
| $E_{\rm c}({\rm GN/m^2})$ | 140.0 | 9.00 |
| $\sigma_{\rm tu} ({\rm GN/m^2})$ | 1.8 | 0.06 |
| $\sigma_{\rm cu} ({\rm GN/m^2})$ | 1.3 | 0.27 |
| V | 0.3 | 0.02 |

| (1) Brick mason | ry | | | |
|-----------------------|--------------------------------------|------------------------------|----------------|----------------------|
| Brick Strength | $f_{\rm b} = 20 - 70 \ {\rm N/mm^2}$ | $E = 300 f_{\rm b} - 2000$ | | |
| | $f_{\rm b}$ >70 N/mm ² | $E = 100 f_{\rm b} + 12,75$ | 0 | |
| | | Mortar mean | | |
| Brick Strength | | cube Strength | Wall thickness | Wall Strength |
| (MN/m ²) | Mortar | (MN/m ²) | (m²) | (MN/m ⁻) |
| 92 | 1:1:3 | 19.30 | 102.5 | 18.40 |
| 46 | 1:1:3 | 13.70 | 102.5 | 15.65 |
| 46 | 1:1:6 | 5.94 | 102.5 | 10.48 |
| (3) Soil/rock | | | | |
| | | $E = 10^2 \text{ MJ} / 2$ | N. | Density, ρ |
| | | $E \times 10$ MIN/m | v | (kg/m^3) |
| Fine sand | | 57.456 | 0.35 | |
| Silty clay | | 48.84 | 0.40 | |
| Silty sand | | 47.88 | 0.35 | |
| Plastic clay | | 3.56 | 0.40 | |
| Silt stone | | 8.4 | 0.30 | 2622 |
| Limestone | | 114.0 | 0.25 | 2671 |
| Alluvial clay | | 5.0 | 0.20 | |
| Clay (embankm | ent fill) | 20.0 | 0.20 | 1517 |
| Saturated soil | | 200.0 | 0.30 | |
| Jointed rock | | 150.0 | 0.25 | |
| Sandstone | | 255.0 | 0.11 | |
| For high plastic | ity, the frictional angle | $\mathfrak{G}_c' = 18^\circ$ | | |
| For low plastici | ty, the frictional angle | $\varphi_c' = 25^\circ$ | | |
| For rocks, $ø'_c$ ran | nges between 20° and 3 | 0° | | |
| The adhesion co | befficient c is around 1 | kN/m^2 | | |

Table 3.5 Material properties for brick and stone masonry and soil/rock

| Basic stresses and | moduli | | | | |
|------------------------|-----------------------------|----------------------------|--------------------------------|---------------|------------|
| <u>C</u> 4 | Bonding | Tension (\mathbf{N}^{1}) | Compress OL/mm ² | sion to grain | E_{\min} |
| Strength group | (N/mm) Parallel to grain | (IN/mm) | (N/mm) Parallel | Perpendicular | (IN/mm) |
| S_1 | 37.5 | 22.5 | 24.4 | 7.5 | 13,800 |
| S_2 | 30.0 | 18.0 | 20.0 | 6.0 | 11,900 |
| S_3 | 24.0 | 14.4 | 17.9 | 4.8 | 10,400 |
| S_4 | 18.7 | 11.2 | 15.5 | 3.7 | 9200 |
| S_5 | 15.0 | 9.0 | 13.3 | 3.0 | 7800 |
| Dry-grade stresses | and moduli | | | | |
| Grade/species | Bonding | Tension | Compress | sion to grain | E_{\min} |
| | (N/mm^2) | (N/mm^2) | (N/mm^2) | | (N/mm^2) |
| | Parallel to grain | | Parallel | Perpendicular | |
| SS/Douglas fir | 6.2 | 3.7 | 6.6 | 2.4 | 7000 |
| GS/Douglas fir | 4.4 | 2.6 | 5.6 | 2.1 | 6000 |
| SS/Redwood | 7.5 | 4.5 | 7.9 | 2.1 | 7000 |
| Whitewood | | | | | |
| GS/Corsican pine | 5.3 | 3.2 | 6.8 | 1.8 | 5000 |
| GS/European pine | 4.1 | 2.5 | 5.2 | 1.4 | 4500 |
| Plywood: all stress | es and moduli are | multiplied by the | he following | g factors: | |
| Grade/glued | Bonding | Tension | Compress | sion to grain | Emin |
| laminated | (N/mm^2) | (N/mm^2) | (N/mm^2) | 0 | (N/mm^2) |
| | Parallel to grain | | Parallel | Perpendicular | |
| LA/4 | 1.85 | 1.85 | 1.15 | 1.33 | 1.0 |
| LB/10 | 1.43 | 1.43 | 1.04 | 1.33 | 0.9 |
| LB/20 or more | 1.48 | 1.48 | | | |
| LC/10 | 0.98 | 0.98 | 0.92 | 1.33 | 0.8 |
| LC/20 or more | 1.11 | 1.11 | | | |
| | Permissible stresses | | | | |
| | 8 N/mm^2 | | _ | _ | 8700 |
| 12 mm ply thickness | 5 N/mm^2 | | - | _ | 7400 |

 Table 3.6
 Material properties of timber

If the stiffness matrix $[K_c]$ for typical elements is known from Eqs. (3.4) and (3.5) as

$$[\mathbf{K}_{c}] = \int_{vol} [\mathbf{B}]^{T} [\mathbf{D}] [\mathbf{B}] dVol$$
(3.6)

the composite stiffness matrix $[K_{TOT}]$, which includes the influence of liner and stud or any other material(s) in association, can be written as

$$[\mathbf{K}_{\text{TOT}}] = [\mathbf{K}_{\text{c}}] + [\mathbf{K}_{\text{l}}] + [\mathbf{K}_{\text{s}}]$$
(3.7)

where $[K_1]$ and $[K_s]$ are the liner and stud or connector matrices. If the initial and total load vectors on the liner/stud assembly and others are $[F_T]$ and $[R_T]$, respectively, then Eq. (3.4) is rewritten as

$$\{F\}^{e} + \{F_{T}\} - \{R_{T}\} = [K_{TOT}]\{x\}^{*}$$
(3.8)

The displacement $\{x\}^*$ is different from $(x\}$ in Eq. (3.4), since it now includes values for both unknown displacements and restrained linear boundaries. Hence $\{x\}^*$ is defined in matrix form as

$$\left\{\boldsymbol{x}\right\}_{x,y,z}^{*} = \begin{cases} x_{unx} \\ x_{uny} \\ x_{unz} \\ x_{bx} \\ x_{by} \\ x_{bz} \end{cases} = \begin{cases} x_{un} \\ x_{b} \end{cases}$$
(3.9)

where x_{un} and X_b are displacement values in unrestrained or unknown conditions and restrained conditions. Similarly, the values for $\{F_T\}$ and $\{R_T\}$ can also be written as

$$\{F_{\rm T}\} = \begin{cases} F_{\rm un} \\ F_{\rm b} \end{cases}_{x,y,z}$$

$$\{R_{\rm T}\} = \begin{cases} R_{\rm un} \\ R_{\rm b} \end{cases}_{x,y,z}$$
(3.10)

The quantities for the liner corresponding to unknown displacements can be written as

$$[K_{l}]\{x_{un}\}_{x,v,z} = \{F_{un}\}_{x,v,z}$$
(3.11)

The shear force τ acting on studs or any other type is evaluated as

$$\{\tau\} = [K_{\rm s}]\{x_{\rm un}\}_{x,y,z} \tag{3.12}$$

Table 3.7 gives the $[K_s]$ matrix modified to include the stiffness of the liner.

| $[K_b] = \pi dL$ | $\left[\left(l^2 E_{\rm h} + p E_{\rm v} + \gamma^2 E_\ell\right)\right]$ | $(lmE_{ m h}+pqE_{ m v}+\gamma sE_{\ell})\ (m^2E_{ m h}+q^2E_{ m v}+s^2E_{\ell})$ | $egin{array}{ll} (lnE_{ m h}+\gamma tE_{ m v})\ (mE_{ m h}+stE_{\ell})\ (n^2E_{ m h}+t^2E_{ m v}) \end{array}$ | $egin{array}{lll} (-PE_{ m h}-p^2E_{ m v}-\gamma^2E_\ell)\ (-lmE_{ m h}-pqE_{ m v}-\gamma sE_\ell)\ (-lmE_{ m h}-\gamma tE_{ m v}) \end{array}$ | $\begin{array}{l} (-lmE_{\rm h}-pqE_{\rm v}-\gamma sE_{\ell})\\ (-m^2E_{\rm h}-q^2E_{\rm v}-s^2E_{\ell})\\ (-mmE_{\rm h}-stE_{\ell})\end{array}$ | $egin{pmatrix} (-nE_{ m h}-\gamma tE_{ m v}) \ (-mmE_{ m h}-stE_{\ell}) \ (-m^2E_{ m h}-t^2E_{ m v}) \ \end{split}$ |
|--|---|--|--|---|--|---|
| 6×6 | symmetrical | | | $(l^2 E_{ m h} + p^2 E_{ m v} + \gamma^2 E_\ell)$ | $(lm E_{ m h}+pq E_{ m v}+\gamma s E_\ell) \ (m^2 E_{ m h}+q^2 E_{ m v}+s^2 E_\ell)$ | $egin{array}{l} (lnE_{ m h}+\gamma tE_{ m v})\ (mE_{ m h}+stE_{\ell})\ (m^2E_{ m h}+t^2E_{ m v}) \end{array}$ |
| Component $E_{\rm h} = \text{horizon}$ $E_{\rm v} = \text{vertical}$ $E_{\ell} = \text{longitue}$ | stiffnesses using springs tal stiffness stiffness linal stiffness | | | | | |
| $\{\Delta P^{\mathrm{e}}\}_{6	imes 1}=1$ | $tdL \begin{cases} -l\Delta\sigma_{\rm h} & -p\Delta\sigma_{\rm v} \\ -m\Delta\sigma_{\rm h} & -q\Delta\sigma_{\rm v} \\ -n\Delta\sigma_{\rm h} & -r\Delta\sigma_{\rm l} \\ l\Delta\sigma_{\rm h} & +p\Delta\sigma_{\rm v} \\ m\Delta\sigma_{\rm h} & +q\Delta\sigma_{\rm v} \\ n\Delta\sigma_{\rm h} & +r\Delta\sigma_{\rm l} \end{cases}$ | $\left. \begin{array}{c} -\gamma\Delta\sigma_{1}\\ -s\Delta\sigma_{1}\\ +\gamma\Delta\sigma_{1}\\ +s\Delta\sigma_{1} \end{array} \right\}$ | | | | |
| $\pi dL = \text{perin}$ | leter of the steel | | | | | |
| $\left[\begin{array}{c} l,m,n\\ p,q,\gamma\\ s,t \end{array} \right] = \epsilon$ | lirection cosines | | | | | |

Table 3.7 Stiffness matrix and load vector

3.2 Steps for Dynamic Non-linear Analysis

The solutions of Eqs. (3.6), (3.7), (3.8), (3.9), (3.10), (3.11) and (3.12) require a special treatment such as under any increment of dynamic loading, stresses, strains and plasticity are obtained in steel, concrete and composites such as the liner and its anchorages and other similar materials. An additional effort is needed to evaluate the rupture of the steel or other material when cracks develop, especially in concrete beneath the liner or its anchorages.

The dynamic coupled equations are needed to solve the impact/explosion problems and to assess the response history of the structure, using the time increment δt . If [M] is the mass and [C] and [K] are the damping and stiffness matrices, the equation of motion may be written in incremental form as

$$[M]\{\ddot{x}(t)\} + [C_{\rm in}]\{\dot{x}(t)\} + [K_{\rm in}]\{\delta(t)\} = \{R(t)\} + \{F_{\rm l}(t)\}$$
(3.13)

where $F_1(t)$ is the time-dependent load including impact/explosion load. If the load increment of $F_1(t)$ is $\delta P_n(t)$, where *n* is the *n*th load increment, then

$$P_n(t) = P_{n-1}(t) + P_n(t)$$
(3.13a)

and hence $\{R(t)\} = \{\delta P_n(t)\}$, which is the residual time-dependent load vector. The solution of Eq. (3.13) in terms of $t + \delta t$ for a δt increment becomes

$$[M]\{\ddot{x}(t+\delta t)\} + [C_{\rm in}]\{\dot{x}(t+\delta t)\} + [K_{\rm in}]\{\delta R(t+\delta t)\} + \{\delta P(t+\delta t)\}$$
(3.14)

where 'in' denotes initial effects by iteration using the stress approach; $\delta P(t + \delta t)$ represents the non-linearity during the time increment δt and is determined by

$$\{\sigma\} = [D]\{\varepsilon\} - \{\varepsilon_0\} + \{\sigma_0\}$$

$$(3.15)$$

The constitutive law is used with the initial stress and constant stiffness approaches throughout the non-linear and the dynamic iteration. For the iteration

$$\{x(t+\delta t)\}_{i} = [K_{\text{in}}]^{-1}\{R_{\text{TOT}}(t+\delta t)\}_{i}$$
(3.16)

The strains are determined using

$$\{\varepsilon(t+\delta t)\}_i = [B]\{x(t+\delta t)\}_i \tag{3.17}$$

where [B] is the strain displacement. The stresses are computed as

$$\{\sigma(t+\delta t)\}_i = [D]\{\varepsilon(t+\delta t)\}_i + \{\sigma_o(t+\delta t)\}_{i-1}$$
(3.18)

where $\{\sigma(t + \delta t)\}\$ is the total initial stress at the end of each iteration. All calculations for stresses and strains are performed at the Gauss points of all elements.

The initial stress vector is given by

$$\{\sigma_{o}(t+\delta t)\}_{i} = f\{\varepsilon(t+\delta t)\}_{i-1} - [D]\{\varepsilon(t+\delta t)\}_{i}$$
(3.19)

Using the principle of virtual work, the change of equilibrium and nodal loads $\{\delta P(t + \delta t)\}_i$ is calculated as

$$F_1(t+\delta t) = \{\delta P(t+\delta t)\}_{i\text{TOT}}$$
(3.20)

$$= \int_{-1}^{+1} \int_{-1}^{+1} \int_{-1}^{+1} [B]^{T''} \{\delta \sigma_o(t+\delta t)\}_i d\xi d\eta d\zeta$$

$$\sigma_o(t) = \{\sigma_o(t+\delta t)\}_i = 0$$

where $d\zeta$, $d\eta$ and $d\zeta$ are the local coordinates and T'' is the transpose. The integration is performed numerically at the Gauss points. The effect load vector $F_1(t)$ is given by

$$F_{1}(t + \delta t) = \{\delta P(t + \delta t)\}_{i \text{TOT}}$$

= $-[\delta C(t)in](\{x(t + \delta t)\}_{i} - \{x(t)\})$
 $- [\delta C(t + \delta t)]_{i}(\{x(t + \delta t)\}_{i} - [\delta K(t)_{in}])(\{x(t + \delta t)\}_{i} - \{x(t)\}_{i})$
 $- [\delta K(t + \delta t)]_{i}\{x(t + \delta t)\}_{i}$
(3.21)

The Von Mises criterion is used with the transitional factor f_{TR}^* to form the basis of the plastic state, such as shown in Fig. 3.2:

$$f_{\rm TR}^* = \frac{\sigma_y(t) - \sigma_{y-1}(t)}{\sigma(t + \delta t)_i - \sigma(t + \delta t)_{i-2}}$$
(3.22)

The elasto-plastic stress increment will be

$$\{\delta\sigma_i\} = [D]_{\rm ep}\sigma(t+\delta t)_{i-1}(1-f_{\rm TR}^*)\{\delta\varepsilon\}$$
(3.23)

If $\{\sigma(t + \delta t)\} < \sigma_y(t)$, it is an elastic limit and the process is repeated. The equivalent stress is calculated from the current stress state where stresses are drifted; they are corrected from the equivalent stress–strain curve.

The values of $[D]_{ep}$ and $[D]_p$ are derived using plastic stress/strain increments. In the elasto-plastic stage, the time-dependent yield function is f(t). It is assumed that the strain or stress increment is normal to the plastic potential $Q(\sigma, K)$. The plastic increment, for example, is given by





$$\delta \varepsilon \sigma (t + \delta t) p = \frac{\partial Q}{\partial \sigma} = \lambda b$$
 (3.24)

where $\lambda =$ proportionality constant >0

$$b \approx \frac{\partial Q}{\partial \sigma(t + \delta t)}$$

When f(t) = Q

$$\delta\varepsilon(t+\delta t)_{\rm p} = \lambda a$$
$$a = \frac{\partial f}{\partial\sigma(t+\delta t)}$$

Therefore,

$$df = [\partial f / \partial \sigma (t + \delta t)] \quad d\sigma (t + \delta t) + (\partial f / dK) dK$$
(3.25)

If A is the hardening plastic parameter, then

$$A = \frac{1}{\lambda} + \left(\frac{\partial f}{dK}\right) dK$$

An expression can easily be derived for the proportionality constant λ

$$\lambda = \frac{a^{T''} D\delta\varepsilon(t+\delta t)}{[A+a^{T''} Db]}$$
(3.26)

hence

$$\delta\varepsilon(t+\delta t)p=b\lambda$$

The value of the elasto-plastic matrix $[D]_{ep}$ is given by

$$[D]_{\rm ep} = D - \frac{Dba^{T''}Db}{[A + a^{T''}Db]}$$
(3.27)

The value of the plastic matrix $[D]_p$ is given by

$$[D]p = \frac{Dba^{T''}D}{[A+a^{T''}Db]}$$
(3.28)

where [D] is the compliance matrix for the elastic case. The elasto-plastic stress increment is given by

$$\{\delta\sigma_i\}_{t} = [D]_{ep}\{\sigma_i\}_{t}^{Y*}(1 - F_{TR}^*)\{\delta \in \}_{t}$$
(3.29)

For the sake of brevity, $\{\delta\sigma_i\}_t = \delta\sigma (t + \delta t)$ for the *i*th point or increment and other symbols are as given above. The total value becomes

$$\{\delta\sigma_i\}_{\text{TOT}} = \{\sigma_i\}_t^{Y*} + \{\delta \in\}_t$$
(3.30)

If $\{\sigma_i\}_t < \sigma_{yt}$ it is an elastic point and $\{\sigma_i\}_t = \{\sigma'_i\}_t$. The process is repeated. Looking at the plastic point in the previous iteration, it is necessary to check for

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unloading when $\sigma \ge \sigma_y$; the unloading will bring about the total stress $\{\delta\sigma_{i-1}\}_t + \{\delta\sigma'_i\}_i$, and set $\{\sigma_y\}_t = \{\delta\sigma_{i-1}\}_t$. Then loading at this point gives

$$\{\delta\sigma_i\} = [D]_{\rm ep}\{\sigma_{i-1}\}_{\rm t}\{\delta\in\}_{\rm t}$$
(3.31)

The total stress is then written as

$$\{\delta\sigma_i\}_{\text{TOT}} = \{\sigma_{i-1}\}_{t}\{\delta\sigma_i\}$$
(3.32)

Stresses are calculated using the elasto-plastic material matrix, which does not drift from the yield surfaces, as shown in Fig. 3.2. Stresses are corrected from the equivalent stress–strain curve by

$$\{\sigma_{\rm corr} = \{\sigma_{i-1}\}_{\rm t} + K\{\delta \in_{\rm P}\}_{\rm t}$$

$$(3.33)$$

where $\{\delta \in_{\mathbf{P}}\}_{t} = \sqrt{\frac{2}{3}} \{\sqrt{(\delta \varepsilon_{ij}^{p} \delta \varepsilon_{ij}^{p})}_{\mathbf{r}} =$ equivalent plastic strain increment. *K* is the strain-hardening parameter such that $\{\delta \in_{\mathbf{p}}\}_{t} = \lambda$. The equivalent stress is calculated from the current stress state as shown below:

$$\{\sigma_i\}_{\text{eq}} = f\{(\sigma_i)\}_{\text{t}} \tag{3.34}$$

the value of
$$\frac{\sigma_{\text{corr}}}{\sigma}$$
 is a factor (3.35)

Therefore the correct stress state on the yield surface is given by

$$\{\sigma_i = \text{factor} \times \{\sigma_i\}$$
(3.36)

A reference is made to Fig. 3.2 for evaluating this factor as f_{TR}^* .

3.2.1 Buckling State and Slip of Layers for Composite Sections

Within the above stages, there can be a possibility of plastic buckling of the liner or any embedded anchors or layers. The buckling matrix is developed so that at appropriate stages the layer/liner/anchor system is checked against buckling. The plastic buckling matrix is given below as

$$(K^i + \lambda_c K^i_G)F_T = 0 \tag{3.37}$$

where K^i is the elasto-plastic stiffness matrix as a function of the current state of plastic deformation using the above steps and K_G is the geometric stifness matrix:

$$\lambda_{\rm c} = 1 + E_{\rm ps} \tag{3.37a}$$

| $\left[T_{\varepsilon}''\right] =$ | $\begin{bmatrix} l_1^2 \\ l_2^2 \\ l_3^2 \\ 2l_1 l_2 \\ 2l_2 l_3 \\ 2l_1 l_3 \end{bmatrix}$ | $m_1^2 \\ m_2^2 \\ m_3^2 \\ 2m_1m_2 \\ 2m_2m_3 \\ 2m_1m_3$ | $n_1^2 \\ n_2^2 \\ n_3^2 \\ 2n_1n_2 \\ 2n_2n_3 \\ 2n_1n_3 \\ 2n_1n_3$ | $\begin{array}{c} l_1 m_1 \\ l_2 m_2 \\ l_3 m_3 \\ (l_1 m_2 + l_2 m_1) \\ (l_2 m_3 + l_3 m_2) \\ (l_1 m_3 + m_1 l_3) \end{array}$ | $\begin{array}{c} m_1 n_1 \\ m_2 n_2 \\ m_3 n_3 \\ (m_1 n_2 + m_2 n_1) \\ (m_2 n_3 + n_2 m_3) \\ (m_1 n_3 + m_3 n_1) \end{array}$ | $\begin{bmatrix} l_1n_1 \\ l_2n_2 \\ l_3n_3 \\ (l_1n_2 + l_2n_1) \\ (l_2n_3 + l_3n_2) \\ (l_1n_3 + n_1l_3) \end{bmatrix}$ |
|------------------------------------|---|---|---|---|---|---|
| $\left[T_{\sigma}''\right] =$ | $\begin{bmatrix} l_1^2 \\ l_2^2 \\ l_3^2 \\ l_1 l_2 \\ l_2 l_3 \\ l_1 l_3 \end{bmatrix}$ | $m_1^2 \ m_2^2 \ m_3^2 \ m_1 m_2 \ m_2 m_3 \ m_1 m_2 \ m_2 m_3 \ m_1 m_3$ | $n_1^2 \\ n_2^2 \\ n_3^2 \\ n_1 n_2 \\ n_2 n_3 \\ n_1 n_3$ | $\begin{array}{c} 2l_1m_1\\ 2l_2m_2\\ 2l_3m_3\\ (l_1m_2+l_2m_1)\\ (l_2m_3+l_3m_2)\\ (l_1m_3+l_3m_1)\end{array}$ | $\begin{array}{c} 2m_1n_1\\ 2m_2n_2\\ 2m_3n_3\\ (m_1n_2+n_1m_2)\\ (m_2n_3+n_2m_3)\\ (m_1n_3+m_3n_1)\end{array}$ | $ \begin{array}{c} 2l_1n_1 \\ 2l_2n_2 \\ 2l_3n_3 \\ (l_1n_2 + l_2n_1) \\ (l_2n_3 + l_3n_2) \\ (l_1n_3 + n_1l_3) \end{array} $ |

 Table 3.8
 T" transformation matrices

where E_{ps} represents accuracy parameters.

Where composite layers, liner and studs are involved, the incremental slips from the nodal displacements are assessed in the following manner:

$$\{\Delta S_i\}_{x,y,z} = [T'']\{d\delta_i\}$$
(3.38)

where S_i is a slip at node *i* and T'' is the transformation matrix given in Table 3.8. The total slip at iteration is given without subscripts as

$$\{S_i\} = \{S_{i-1}\} + \{S_i\}$$
(3.39)

The strains are computed as

$$\{\varepsilon_i\}t = \{\varepsilon_{i-1}\}t + \{\delta \in i\}t \tag{3.40}$$

Thes incremental stress { σ_B } between the studs and concrete or between any composite materials for the *i*th node can then be computed as

$$\{\delta\sigma_{\mathrm{Bi}}\}_{\mathrm{t}} = [Ks]\{\sigma_{\mathrm{B}i-1}\}_{\mathrm{t}}\{\delta S_i\}_{\mathrm{t}}$$
(3.41)

The total stresses are

$$\{\delta\sigma_{\mathrm{B}i}\}_{\mathrm{TOT}} =]\{\sigma_{\mathrm{B}i-1}\}_{\mathrm{t}} +]\{\delta\sigma_{\mathrm{B}i}\}_{\mathrm{t}}$$
(3.42)

If $|\delta S_i| > S_{\text{max}}$ the bond between the stud and the concrete or any composite material is broken and the pull-out occurs, i.e. $\{\sigma_B\} = 0$ and S_{max} has a value which is maximum. If $|\delta S_i| < S_{\text{max}}$ the value $\{S_i\}$ is calculated. The procedure is linked with the general finite element work discussed already in the non-linear dynamic cases for impact and explosion.

3.2.2 Strain Rate Effects Based on the Elastic–Viscoplastic Relationship for Earth Materials Under Impact and Explosion

It is assumed that for each dynamic loading increment, the strain rate ε_{ij} can be expressed as the sum of the elastic and viscoplastic components:

$$\left\{d\varepsilon_{ij}\right\}_{t} = \left\{d\varepsilon_{ij}\right\}_{e} + \left\{d\dot{\varepsilon}_{ij}\right\}_{vp}$$
(3.43)

Where the subscripts e and vp denote the elastic and viscoplastic components, respectively. The elastic strains are related to the stress rate σ_{ij} by

$$\{d\dot{\varepsilon}_{ij}\}_{\rm e} = \frac{1}{9K} \times \left(\frac{dJ_1}{dt}\right) \delta_{ij} + \frac{1}{2G} \times \frac{dS_{ij}}{dt}$$
(3.44)

where J_1 = deviatoric stress: first invariant; $S_{ij} = \{\sigma_{ij} \ \frac{1}{3} \ J_1 \delta_{ij}\}_t; \delta_{ij}$ = Knonecker delta; K = elastic bulk modulus; G = elastic shear modulus.

The shear modulus is expressed in terms of the invariant J'_2 , where

$$J_2' = \frac{1}{2} S_{ij} S_{ij} \tag{3.44a}$$

Then

$$K = \frac{K_i}{1 - K_1} [1 - K_1 e^{K_2 J_1}]$$
(3.44b)

$$G = \frac{G_i}{1 - G_1} [1 - G_1 e^{-G_2 J_2'}]$$
(3.44c)

where K_i , K_1 , G_i , G_1 , K_2 and G_2 are material constants. The values of J'_2 and S_3 are given below:

$$J_{2}' = \frac{1}{2}(S_{x}^{2} + S_{y}^{z} + S_{z}^{2}) + \tau_{xy}^{2} + \tau_{yz}^{2} + \tau_{zx}^{2} \text{ is the second variant}$$
(3.44d)

$$S_x = \sigma_x - \sigma_m, S_y = \sigma_y - \sigma_m, S_z = \sigma_z - \sigma_m$$
(3.44e)

The linear values of *K* and *G* are

$$K = \frac{E}{3(1-2\nu)}; \quad G = \frac{E}{2(1-2\nu)}$$
 (3.44f)

Tables 3.1 and 3.2 are used for variable properties of E and v.

The components of the viscoplastic strain rate are calculated using the above-mentioned plastic flow rule for rate-sensitive material:

$$\{\dot{\varepsilon}_{ij}\}_{\rm vp} = \gamma [f(\sigma_{\rm D}/B)\sigma_{\rm D}/\delta\sigma_{ij}]_{\rm t}$$
(3.45)

where γ = viscosity parameter:

$$f(\sigma_{\rm D}/B)_{\rm t} = f\left(\sigma_{\rm s} - \frac{\beta}{B}\right)$$

 $\sigma_{\rm s}$ = static yield stress; B = material parameter:

$$\beta = f^{-1} \left\{ \frac{1}{\gamma} \left[\frac{\frac{1}{3} \{ d\dot{\varepsilon}_{KK} \}_{vp} + (2\dot{e}^{-1})_{vp}^2}{(\partial \sigma_s / \partial J_1)^2 \frac{1}{2} ((\partial \sigma_s \partial J_2')^2)} \right] \right\}$$
(3.45a)

$$(\dot{e}^{-1})_{\rm vp} = \left[\frac{1}{2}d\dot{e}_{ij}d\dot{e}_{ij}\right]_{\rm vp}^{\frac{1}{2}}$$
 (3.45b)

and is the square root of the second invariant of the viscoplasic strain rate.

Using this bulk modulus approach for soils, the time-dependent stress–strain relation is given in Table 3.9. With reference to *rocks*, the failure strength of the rock is defined in exactly the same way as described earlier; the values for *E* and v will vary. Nevertheless, the various alternative failure models given in Table 3.10 for rocks are related in terms of strain rates by

$$\overline{M} = \frac{\sigma_{\rm dyn}}{\sigma_{\rm s}} = 1 + c \log \frac{\dot{\varepsilon}}{\dot{\varepsilon}_{\rm s}} \tag{3.46}$$

where $\sigma_{dyn} =$ dynamic stress; $\dot{\sigma}_s$ static stress; \dot{c} strain rate (dynamic); $\dot{c}_s =$ strain rate (static); c = constant.

Table 3.9 Bulk modulus model for earth

| $\left(\begin{array}{c} \delta\sigma_x\\ \delta\sigma_y\\ \delta\sigma_z\end{array}\right)$ | $\left[\begin{array}{c} (K + \frac{4}{3}G) \end{array} \right]$ | $(K - \frac{2}{3}G)$ $(K + \frac{4}{3}G)$ | $(K - \frac{2}{3}G)$ $(K - \frac{2}{3}G)$ $(K + \frac{4}{3}G)$ | 0 0 0 | 0 0 0 | $\begin{bmatrix} 0\\0\\0 \end{bmatrix}$ | $ \left(\begin{array}{c} \delta \epsilon_x \\ \delta \epsilon_y \\ \delta \epsilon_z \end{array}\right) $ |
|--|--|---|--|------------------------|--|--|---|
| $ \left(\begin{array}{c} \delta \tau_{xy} \\ \delta \tau_{yz} \\ \delta \tau_{zx} \end{array} \right)_{t} $ | | sym | | <i>G</i> ₁₂ | $\begin{array}{c} 0 \\ G_{23} \end{array}$ | $\begin{bmatrix} 0 \\ 0 \\ G_{13} \end{bmatrix}$ | $\left\{\begin{array}{c} \delta_{xy} \\ \delta_{yz} \\ \delta_{zx} \end{array}\right\}_{t}$ |

or in short $\{\delta\sigma\} = [D]\{\delta\varepsilon\}$

Where [D] is the required material matrix

$$G_{12} = G_{23} = G_{13} = G = G_e - \alpha \log \frac{J_2}{J_2^e}$$
 for $J_2 > J_2^e$
 $G = G_e$ for $J_2 \le J_2^e$

In the case where the soil/rock is orthotropic, the values of G_{12} , G_{23} and G_{13} are given as indicated in Table 3.2

(1) Sandstone $\tau = 1538 + \sigma \tan \phi \quad (1)$ where τ and σ = shear and compressive stresses, respectively $\phi = 29^{\circ}15'$ (2) Rupture of sandstone: Mohr failure envelope $\tau_{\rm max}/\sigma_{\rm cu} = 0.1 + 0.76 (\sigma_{\rm m}/\sigma_{\rm u})^{0.85}$ (2) where σ_{cu} is the uniaxial compressive stress at rupture under pure shear $\sigma_1 = -\sigma_3$ (3) Realistic rock including friction $\alpha = (\sigma_1 + \sigma_2 + \sigma_3) + (\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2 = K^*$ (3) where $\alpha = \sqrt{6 \tan \theta} / \sqrt{(9 + 12 \tan \theta)}$ $K^* = \sqrt{6c}/\sqrt{9+12\tan \theta}$ Ø = angle of friction c = cohesionA generalised Mohr coulomb criterion is written as $\tau^2 = \left[\sqrt{n+1} - 1\right] \left[\sigma_{\rm tu}^2 - \sigma \sigma_{\rm tu}\right] \quad (4)$ Where σ , t = normal stress and shear stress on the fractured plane σ_{tu} = uniaxial tensile strength $n = \sigma_{\rm cu}/\sigma$ = brittleness σ_{cu} = uniaxial compressive strength Equation (4) can be expressed in terms of σ'_m mean stress and σ_s the maximum shear stress by $\sigma_{\rm s} = \sigma_{\rm tu} - \sigma_{\rm m}$ for $\sigma_{\rm tu} > \sigma_{\rm mo} > \sigma_{\rm m}$ $\sigma_{\rm s} = \tau_{\rm o} \sqrt{\left[\left(1 - \sigma_{\rm m}/\sigma_{\rm tu}\right) - \left(\tau_{\rm o}/2\sigma_{\rm tu}\right)^2 \right]} \text{ for } \sigma_{\rm mo} < \sigma_{\rm m} \quad (5)$ where $\sigma_{\rm m}(\sigma_1 + \sigma_2)/2$, $\sigma_{\rm s} = (\sigma_1 - \sigma_2)/2$, $\sigma_{\rm mo} = \sigma_{\rm tu} - \tau_0^2 / \sigma_{\rm tu} \quad (6)$ $\tau_{\rm o} = [\sqrt{n+1} - 1]\sigma_{\rm tu}$ The stress state is assessed for $\sigma_{\rm m}$ and $\sigma_{\rm s}$ from the failure surface as $=\sigma_{\rm s}/\sigma_{\rm s(critical)} \ge 1$ representing the failure condition. If $a = \sigma_s / \sigma_{s(critical)}$, Eq. (5) is satisfied

The range of strain rate is $\dot{\varepsilon} = 10^{-5} \text{ S}^{-1}$. The dynamic failure criterion can then be written as

$$\sigma_{t}^{1} = \tau_{o}X_{3} + \sigma \left[\frac{\sigma_{cu}^{2}X_{1}^{2} - 4\tau_{o}^{2}X_{3}^{2}}{4\sigma_{cu}X_{1}\tau X_{3}} \right] \quad \text{for } \sigma \neq 0$$

$$\sigma_{t}^{2} = \tau_{0}^{2}X_{3}^{2} + \sigma \frac{[\tau_{o}^{2}X_{3}^{2} - \sigma_{tu}^{2}X_{2}^{2}]}{\sigma_{tu}X_{2}} - \sigma^{2} \text{ for } \sigma \neq 0 \qquad (3.47)$$

where

$$X_{1} = \frac{3}{40}\overline{M} + \frac{1}{25}\overline{M}^{2}$$

$$X^{2} = \frac{3}{100}\overline{M} + \frac{7}{1000}\overline{M}^{2}$$

$$X^{3} = \frac{1}{40}\overline{M} + \frac{1}{100}\overline{M}^{2}$$

$$\tau_{0} = \text{octahedral shear stress under static loads}$$

In the case of *brick material*, Khoo and Hendry relationships given below are used in the above failure models and strain rate simulations. The non-linear principal stress relationship (biaxial) is given by

$$\sigma_1 / \sigma_{\rm cu} = 1 + 2.91 (\sigma_2 / \sigma_{\rm c})^{0.805} \tag{3.48}$$

where σ_1 = major principal stress; σ_2 = minor principal stress; σ_{cu} = uniaxial compressive strength.

The brick-failure envelope with the mortar triaxial strength curve is given by the polynomials

$$\sigma_{\rm t}/\sigma_{\rm tu} = 09968 - 2.0264(\sigma/\sigma_{\rm cu}) + 1.2781(\sigma/\sigma_{\rm cu})^2 - 0.2487(\sigma/\sigma_{\rm cu})^2 \quad (3.49)$$

$$\sigma_3/\sigma_{\rm cu} = -0.1620(\sigma_1/\sigma_{\rm cu}) + 0.1126(\sigma_1/\sigma_{\rm cu})^2 - 0.0018(\sigma/\sigma_{\rm cu})^3$$
(3.50)

where σ/σ_{cu} = ratio of compressive strength; σ_t/σ_{tu} = ratio of tensile strength; $\sigma_t = \alpha \sigma_3$ where $\alpha = 0.15$ and 0.40 for mortars of 1:1/4:3 and 1:1:6, respectively.

3.2.3 Finite Element of Concrete Modelling

A number of modelling methods are available for simulation into the finite element method. On impact and explosion work, methods such as the edochronic, Ottoson and Blunt crack have been widely used. They are covered in this section. The bulk modulus model of Table 3.9 is reviewed to include cracking with and without aggregate interlocking. On the basis of the endochronic concept, which is widely reported the following equations apply:

$$\{\delta\sigma_{x,y,z}\}_{t} + \{\delta\sigma_{x,y,z}^{p}\}_{t} = [D_{T}^{*}]\{\varepsilon_{x,y,z}^{p}\}_{t}$$
(3.51)

where the superscript p denotes stresses in the plastic case. Table 3.11 gives details of uncracked and cracked cases for Eq. (3.51). When cracks in three directions are open the concrete loses its stiffness, then

$$[D_{\rm T}^*] = 0 \tag{3.52}$$

Stresses $\{\{\sigma_i\}_t\}$ ~ are checked against the cracking criteria. For example, if there is one crack normal to the *X*-direction, the concrete can no longer resist any tensile stress in that direction, then

$$\delta \sigma_x^* = 0$$

Table 3.11 Cracks using endochronic theory

| | | | | | | • | |
|---|------------------------------------|------------------------------|--|--|---|---|---|
| Uncracked matrix | | | | | | | |
| $ \left\{ \begin{array}{l} \delta \sigma_x + \delta \sigma_x^p \\ \delta \sigma_y + \delta \sigma_y^p \\ \delta \sigma_z + \delta \sigma_z^p \\ \delta \tau_{xy} + \delta \tau_{xy}^p \\ \delta \tau_{yz} + \delta \tau_{yz}^p \\ \delta \tau_{zx} + \delta \tau_{zx}^p \end{array} \right\}_{\rm t} =$ | D ₁₂ D ₂₁ | $D_{13} \\ D_{23} \\ D_{33}$ | $egin{array}{c} 0 \ 0 \ 0 \ eta^\prime D_{44} \end{array}$ | $egin{array}{c} 0 \ 0 \ 0 \ 0 \ eta \ eta \ b \ b \ 55 \ eta \ b \ b \ 55 \ eta \ b \ b \ b \ b \ b \ b \ b \ b \ b \ $ | $\begin{bmatrix} 0\\ 0\\ 0\\ 0\\ 0\\ \beta' D_{66} \end{bmatrix}$ | $\left\{\begin{array}{l} \delta\sigma_{x}\\ \delta\sigma_{y}\\ \delta\sigma_{z}\\ \delta\gamma_{xy}\\ \delta\gamma_{yz}\\ \delta\gamma_{yz}\\ \delta\gamma_{zx}\end{array}\right\}$ | ł |
| Where | | | | | | | |

where $D_{11} = D_{22} = D_{33} = K + \frac{4}{3}G$ $\beta = \text{aggregate inter locking} \approx \frac{1}{2}$ to $\frac{3}{4}$ $D_{12} = D_{13} = D_{23} = K - \frac{2}{3}G$ $D_{44} = G_{12} = \frac{1}{2} \left[\frac{E_1}{2(1+v_{12})} + \frac{E_2}{2(1+v_{21})} \right]$ $D_{55} = G_{23} = \frac{1}{2} \left[\frac{E_2}{2(1+v_{23})} + \frac{E_3}{2(1+v_{22})} \right]$ $D_{66} = G_{13} = \frac{1}{2} \left[\frac{E_3}{2(1+v_{31})} + \frac{E_1}{2(1+v_{13})} \right]$

The values of E and v are given in Tables 6.3, 6.4, 6.5 and 6.6

Cracked matrix

$$\sigma_{1} \text{-direction } [D]^{*} = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \left(D_{22} - \frac{D_{12}}{D_{11}}\right) & \left(D_{23} - \frac{D_{12}D_{12}}{D_{11}}\right) & 0 & 0 & 0 \\ 0 & \left(D_{23} - \frac{D_{31}D_{21}}{D_{11}}\right) & \left(D_{33} - \frac{D_{13}D_{13}}{D_{11}}\right) & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \beta'D_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & D_{55} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \beta'D_{66} \end{bmatrix}$$

$$\sigma_{2} \text{-direction } [D]^{*} = \begin{bmatrix} \left(D_{11} - \frac{D_{21}}{D_{22}}\right) & 0 & \left(D_{13} - \frac{D_{12}D_{23}}{D_{22}}\right) & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \beta'D_{66} \end{bmatrix}$$

$$\sigma_{3} \text{-direction } [D]^{*} = \begin{bmatrix} \left(D_{11} - \frac{D_{21}}{D_{22}}\right) & 0 & \left(D_{13} - \frac{D_{12}D_{23}}{D_{22}}\right) & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \beta'D_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & \beta'D_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \beta'D_{55} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & D_{66} \end{bmatrix}$$

then

$$D_{11}\delta\varepsilon_{x}^{*} + D_{12}\delta\varepsilon_{y}^{*} + D_{13}\delta\varepsilon_{z}^{*} = \delta\sigma_{x}^{p*}$$
$$\delta\varepsilon_{x}^{*} = \frac{\delta\sigma_{x}^{p*}}{D_{11}} - \frac{D_{12}}{D_{11}}\delta\varepsilon_{y}^{*} - \frac{D_{13}}{D_{11}}\delta\sigma_{y}^{*}$$
(3.53)

In a similar manner, examples for shear terms can be written as

$$\delta \tau_{xy}^* + \delta \tau_{yz}^{p*} = \beta' D_{44} \gamma_{xy}^*$$

$$\delta \tau_{yz}^* + \delta \tau_{yz}^{p*} = D_{55} \delta \gamma_{yz}^*$$

$$\delta \tau_{zx}^* + \delta \tau_{zx}^{p*} = \beta' D_{66} \delta \gamma_{zx}^*$$
(3.54)

3.2.3.1 Blunt Crack Band Propagation

The smeared crack concept, rather than the isolated sharp inter-element crack concept described above, is gaining ground. Here the element topology does change. The smeared crack band of a blunt front is that in which one can easily select cracks in any direction without paying a penalty, even if the crack direction is not truly known. Bazant et al. and Bangash introduced the equivalent strength and energy variation which are utilised for crack propagation once it is initiated within the element. The equivalent strength criterion is used for crack propagation by specifying an equivalent strength criterion is used for crack propagation by specifying an equivalent strength be propagated. The expression for the equivalent strength σ_{eq} is given (see Fig. 3.3) as

$$\sigma_{\rm eq} = C [EG_f / W(1 - 2 V \sigma_2^0 / \sigma_1^0)]^{1/2}$$
(3.55)

where C = a constant dependent on the choice of elements; E = elastic modulus; V = Poisson's ratio; $W = A/\delta \alpha = A/r \cos \alpha$; A = area of the element at the front.

The band length is specified as $a + \Delta a/2$

In the initial state prior to cracking, the strain energy U_0 is based on the principal stresses σ_2^0 , where σ_1^0 is the largest tensile stress. After cracking, of becomes 0 and $\sigma_2^1 = 0$. Which is used for the current value of U_1 . The change of strain energy $\delta U = U_0 - U_1$ is equated to the crack length $\Delta a \times G_f$, where U is the total strain energy in a cracked body and δU is the energy released by the structrure into the element which cracks. The crack direction within an arbitrary grid is given by

$$\theta_{\mathrm{A}} = \frac{1}{3} \left(\theta_{n-1} + \theta_n + \theta_{n+1} \right) \tag{3.56}$$



Fig. 3.3 Blunt crack propagation

where θ_A is the average crack direction, θ_{n-1} and θ_n are the cracking angles of the next to last cracked element and θ_{n-1} is the impending cracking angle of the element adjacent to the crack front. Since in the arbitrary grid the cracking direction is specified by the accumulated error of the cracked direction, the accumulated cracking error θ_E is given by

$$\theta_{\rm E} = \sum_{i}^{n} (\theta_{\rm Gi} - \theta_{\rm Ai}) \tag{3.57}$$

where *n* is the number of cracked elements and θ_G is the actual average crack propagation angle within each element. A better formulation by Gamborov and Karakoc, reported by Bangash, is given of the tangent shear modulus G^{CR} whenever cracking is initiated:

$$G^{\rm CR} = \frac{\sigma_{\rm nt}^{\rm c}}{\varepsilon_{\rm nn}^{\rm CR}} K \frac{1}{r(a_3 + a_4 \mid r \mid^3)}$$
(3.58)

or

$$G^{\rm CR} = \frac{\sigma_{\rm o}}{\varepsilon_{\rm nn}^{\rm CR}} K \{ 1 - [2(P/D_{\rm a})\varepsilon_{\rm nn}^{\rm CR}]^{1/2} \}$$

where

$$K = \frac{a_3 + 4a_4 |\gamma|^3 - 3a_3a_4\gamma^4}{(1 + a_4\gamma^4)^2}$$
(3.59)

and $a_{3,a_{4}}$ = coefficients as a function of the standard cylindrical strength f'_{c} ; τ_{0} = crack shear strength (ranging from 0.25 to 0.7 f'_{c}); D_{a} = maximum aggregate size (up to 4 mm); P_{c} = large percentage of crack asperities; $\gamma = \delta_{t}/\delta_{n}$; δ_{t} , δ_{n} crack displacements along the normal and tangential directions (Figs. 3.3 and 3.4).

Curves have been plotted showing a decrease in the value of G^{CR} when a crack opening linearly increases at increasing shear. A constitutive law in which a confinement stress within the rough crack model is given by

$$\sigma_{\rm nn}^{\rm c} = -a_1 a_2 \frac{\delta_{\rm t} \sigma_{\rm nt}^{\rm c}}{\left(\sigma_{\rm n}^2 + \sigma_{\rm t}^2\right)^q} \tag{3.60}$$

where σ_{nn}^{c} = interface normal stress; σ_{nt}^{c} = interface shear stress; a_1, a_2 = constant ($a_1, a_2 = 0.62$); q = a function of the crack opening; taken to be 0.25.

For different types of crack dilatancy δ_n/σ_{nt}^c (Fig. 3.3) the tangent shear modulus G^{CR} is plotted against the ratio *r* of the crack displacement. The value of σ_{nt}^c is given by

$$\sigma_{\rm nt}^{\rm c} = \tau_{\rm o} \left[1 - \sqrt{\left(\frac{2P}{D_a} \in_{\rm nn}^{\rm CR}\right)} \right] r \frac{a_3 + a_4 \mid r \mid^3}{1 + a_4 \gamma^4}, \quad r = \gamma_{\rm nt}^{\rm CR} / \varepsilon_{\rm nn}^{\rm CR} \tag{3.61}$$

where *p* is the crack spacing and CR is cracked concrete

$$\varepsilon_{nn}^{CR} = \delta_n / P = \text{strain against } \sigma_{nn}^{c}$$



Fig. 3.4 Crack displacement versus tangent shear modulus^{1.149}

The σ_{nn}^{c} values have been computed using points common to the curves of crack opening and constant confinement stress.

3.2.3.2 Ottoson Failure Model

The Ottoson four-parameter model has a smooth but convex surface with curved meridians determined by the constants a and b.

The analytical failure surface is defined by

$$f(I_1, J_2, J) = a \frac{J_2}{(f_c^{\prime})^2} + \lambda \frac{\sqrt{2}}{f_c^{\prime}} + b \frac{l}{f_c^{\prime}} - 1 = 0$$
(3.62)

where

 $I_1 = \sigma_x + \sigma_y + \sigma_z$ = the first invariant of the stress deviator tensor (3.62a)

$$J_2 = \text{the second invariant of stress deviator tensor}$$

= $\frac{1}{2} \left(S_x^2 + S_y^2 + S_z^2 \right) + \tau_{xy}^2 + \tau_{yz}^2 + \tau_{zx}^2$ (3.62b)

$$J = \cos 3\theta = 1.5\sqrt{3}(J_3/J_2) \tag{3.62c}$$

$$J_3$$
 = the third invariant of the stress deviator tensor

$$= S_x S_y S_z + 2\tau_{xy} \tau_{yz} \tau_{zx} - S_x \tau_{yz}^2 - S_y \tau_{zx}^2 - S_z \tau_{xy}^2$$
(3.62d)

$$S_x = \sigma_x - I_1/3$$

$$S_y = \sigma_y - I_1/3$$

$$S_z = \sigma_z - I_1/3$$

(3.62e)

 $\lambda = \lambda(\cos 3\theta) > 0$, *a* and *b* are constant

$$\lambda = K_1 \left(\frac{1}{3} \cos^{-1}(K_2 \cos 3\theta) \right) \quad \text{for } (\cos 3\theta) \le 0$$
$$\lambda = K_1 \cos\left(\frac{\pi}{3} - \frac{1}{3} \cos^{-1}(K_2 \cos 3\theta) \right) \quad \text{for}(\cos 3\theta) \le 0$$

 $k_1, k_2 a$ and b are material parameters $(0 \le K_2 \le 1)$ $f'_c =$ uniaxial compressive cylinder strength for concrete = $0.87\sigma_{cu}$ $\sigma_t =$ uniaxial tensile strength for concrete

Table 3.12 lists some of the relevant parameters.

The knowledge of the mechanical properties of concrete and the reinforcement (conventional and prestressing steel) at high strain rates is essential for rational application of materials in those constructions where impact and explosion loadings can be expected. The usual magnitude of the strain rate $(d\epsilon/dt) = \dot{\epsilon}$ for all concrete structures is of the order of 5×10^5 /s in the range of the ultimate load.

For reinforcement, the range is between 10^5 and 10^2 /s. Table 3.13 gives relevant data. Figure 3.5 gives experimental stress–strain relationships for reinforcement for various strain rates. The theoretical expression in Eq. (3.46) was used.



 Table 3.12
 Ottoson's failure model for concrete

| | Comparison | for the | four-p | arameter | model |
|--|------------|---------|--------|----------|-------|
|--|------------|---------|--------|----------|-------|

| | Fou | r-material Parameters | $s(k = \sigma_t / \sigma_c)$ | |
|------|--------|-----------------------|------------------------------|--------|
| Κ | а | b | k_1 | k2 |
| 0.08 | 1.8076 | 4.0962 | 14.4863 | 0.9914 |
| 0.10 | 1.2759 | 3.1962 | 11.7365 | 0.9801 |
| 0.12 | 0.9218 | 2.5969 | 9.9110 | 0.9647 |

| V | alues | of | the | func | tion | (k | $= \sigma_{t}$ | σ_{c} |) |
|---|-------|-----|-----|------|------|----|----------------|--------------|---|
| • | | ~ - | | | | | × 1/ | ~ (| |

| Κ | $\lambda_{ m t}$ | λ_{c} | $\lambda_{c}\lambda_{t}$ |
|------|------------------|---------------|--------------------------|
| 0.08 | 14.4925 | 7.7834 | 07378 |
| 0.1 | 11.7109 | 6.5315 | 0.5577 |
| 0.12 | 9.8720 | 5.6979 | 0.5772 |

(4)



 Table 3.12 (continued)

Determination of material parameters $(S_1, S_2, S_3, S_4 = \text{failure stresses})$ The following three failure states were represented: (1) Uniaxial compressive strength, $f_c'(\theta = 60^\circ)$, Uniaxial tensile strength, $\sigma_t (\theta = 0^\circ) = Kf_c'$ (2) Biaxial compressive strength, $\sigma_1 = \sigma_2 = -1.16\sigma_{\text{ci}}$; $\sigma_3 = 0$ ($\theta = 0^\circ$) (3) The triaxial state ($\xi/f_c', \rho/f_c'$) = (-5, 4) on the compressive meridian ($\theta = 60^\circ$)

| Table 3.13 | Strain rate | for concrete and | reinforcement |
|-------------|-------------|------------------|---------------|
| 1 able 5.15 | Sham ale | Tor concrete and | reimorcement |

| The relationship between the fracture strain $\varepsilon_{\rm f}$ and the strain rate ε is given by |
|--|
| $\varepsilon_{\rm t} = \dot{\alpha}^{1/3} \tag{1}$ |
| for plain concrete $\alpha = 206$; for reinforced concrete $\alpha = 220$. |
| Another expression given by DELFT for plain concrete is |
| $\varepsilon_t = 100 + 109\dot{\varepsilon}^{1/2} \tag{2}$ |
| In Eq. (1), for say $\dot{\epsilon}/s = 35$, the value of $\epsilon_{\rm f}$ for reinforced concrete will be 740×10^{-6} . |
| For $\dot{\epsilon}/s = 30$, the value of ϵ_f for plain concrete will be 650×10^{-6} . |
| For fibre-reinforced concrete, the influence of the strain rate upon the tensile strength for concrete is given by |
| $\sigma_{\rm t} = \alpha + \beta \log_{\rm e} \dot{\epsilon} \tag{3}$ |
| $\alpha = 0$ for no fibres, i.e. plain concrete |
| $\sigma = 1.7 + 0.0364 \log_e \dot{\varepsilon} \text{ for } 3\% \text{ fibres}$ |
| $\sigma = 1.87 + 0.0424 \log_e \dot{\epsilon}$ |

For low, intermediate and high strain rates, DELEFT gives an expression:

$$\sigma_t = \alpha + \beta N$$

where N is the number of fibres/reinforcements

| | Low | Intermediate | High |
|---|-----------------------|-----------------------|----------------------|
| α | 3.32 | 4.87 | 5.49 |
| β | 1.85×10^{-3} | 2.85×10^{-3} | 6.3×10^{-3} |

3.3 Ice/Snow Impact

| | | $G_{\rm t} = \alpha + \beta N$ | |
|---|-------|--------------------------------|--------|
| | Low | Intermediate | High |
| α | 12.72 | 22.90 | 29.200 |
| β | 0.12 | 0.18 | 0.211 |



800 Strain 700 rate ė(1/s) 600 Stress, σ (N/mm²) 500 1×10^{-1} 5×10⁻⁵ 400 300 200 100 0 0 5 10 15 20 Strain, ϵ (%)

Fig. 3.5 Stress-strain relationships for various strain rates

3.3 Ice/Snow Impact

Chapter 2 gives a thorough survey on data regarding the effect of ice floes. When floating ice sheets move under the influence of strong winds and currents, a seagoing vehicle or a semi-submersible will be subject to an impact given by

$$F_1(t) = F_{10}(t) + F'_1(t)$$
(3.63)

where $F_{10}(t)$ and $F'_1(t)$ $F'_1(t)$ are constants and fluctuating values of the ice impact force, respectively. The value of $F'_1(t)$ is given by

$$F_{\rm IO}(t) = S_1 S_2 S_3 f(\dot{\varepsilon}) TW \times h\sigma_{\rm c} \text{ (or } f_{\rm c}')$$
(3.64)

where S_1 = contact factor around the member during crushing; S_2 = shape factor S_f of the impactor; S_3 = temperature factor which is $(1 - 0.012T)/(1 - 0.012T_s)$ (T: 0.5°C> - 20°C) (T_s = -10°C; σ_c compressive strength of ice measured at a strain rate of 5 \times 10⁴/s which is $\dot{\varepsilon}_{0}$; W = transverse width of the member; h = ice sheet thickness

 $f(\dot{\epsilon}_{\rm o}) = (\dot{\epsilon}/\dot{\epsilon}_{\rm o})\gamma; \qquad \phi = \alpha_1 + \alpha_2 (h/w)^{1/2}$ (3.64a) $\dot{\epsilon} = \dot{x}/4 W$ where \dot{x} = ice flow velocity; γ = empirical coefficient dependent on strain rate; a_1, a_2 = factors dependent on the ice thickness/diameter ratio of a

Depending on the type of impact (direct or angular) and the stiffnesses of members and ice floes, the global equation of motion, (3.13), will be influenced by roll, pitch and yaw motions (θ_s, Φ_s, Ψ_h) and surge, sway and heave motions (θ_r, Φ_p, Ψ_y), respectively. Generally, the values of $\theta_r, \Phi_p, \Psi_y \theta_s, \Phi_s$ and Ψ_h range as shown below:

$$\theta_{\rm r} = -0.012 \text{ to } 0.04 \times 10^{-3} \text{ rad}; \ \theta_{\rm s} = -0.75 \text{ to } 6 \text{ m}$$

 $\Phi_{\rm p} = -0.012 \text{ to } 0.04 \times 10^{-3} \text{ rad}; \ \Psi_{\rm s} = -1.5 \text{ to } 3 \text{ m}$
 $\Psi_{\rm y} = -0.012 \text{ to } 0.04 \text{ rad}; \ \Psi_{\rm n} \approx \theta_{\rm s}$

3.4 Impact Due to Missiles, Impactors and Explosions: Contact Problem Solutions

Contact problems have been solved using Hallquis-contact method. Many similar methods are using the spring concept (given in Appendix A). In addition, at the time of impact constraints are imposed on global equations such as Eqs. (3.13), (3.14), (3.15), (3.16), (3.17), (3.18), (3.19), (3.20), and (3.21). Hallquist et al. developed a useful concept of *master* and *slave nodes* sliding on each other. As shown in Fig. 3.6, slave nodes are constrained to slide on master segments after impact occurs and must remain on a master segment until a tensile interface force develops. The zone in which a slave segment exists is called a *slave zone*. A separation between the slave and the master line is known as *void*. The following basic principles apply at the interface:

- (1) Update the location of each slave node by finding its closest master node or the one on which it lies.
- (2) For each master segment, find out the first slave zone that overlaps.
- (3) Show the existence of the tensile interface force.

Constraints are imposed on global equations by a transformation of the nodal displacement components of the slave nodes along the contact interface. Such a transformation of the displacement components of the slave nodes will eliminate their normal degrees of freedom and distribute their normal force components to the nearby master nodes. This is done using explicit time integration, as described later under solution procedures. Thereafter impact and release conditions are imposed. The slave and master nodes are shown in Fig. 3.6. Haliquist et al.^{3.40} gave a useful demonstration of the identification of the contact point, which is the point on the master segment to the slave node n_s and which finally becomes non-trivial. As shown in Fig. 3.6, when the master segment *t* is given the parametric representation and \hat{t} is the position vector

member.



Fig. 3.6 Hallquist contact method (modified by Bangash)

drawn to the slave node n_s , the contact point coordinate must satisfy the following equations:

$$\frac{\partial \hat{r}}{\partial \xi} (\xi_{\rm c}, \eta_{\rm c}) \times [\hat{t} - \hat{r}(\xi_{\rm c}, \eta_{\rm c})] = 0$$

$$\frac{\partial \hat{r}}{\partial \eta} (\xi_{\rm c}, \eta_{\rm c}) \times [\hat{t} - \hat{r}(\xi_{\rm c}, \eta_{\rm c})] = 0 \qquad (3.65)$$

where (ζ_c, η_c) are the coordinates on the master surface segment S_i . When penetration through the master segment S_i occurs the slave node n_s (containing its contact point) can be identified using the interforce vector f_s added, then

$$f_{\rm s} = -lK_i n_i \quad \text{if } l < 0 \tag{3.66}$$

to the degrees of freedom corresponding to $n_{\rm s}$ and

$$f_{\rm m}^{\,i} = N_i(\xi_{\rm c}, \eta_{\rm c}) f_{\rm s} \quad \text{if } l < 0$$
 (3.67)

where

$$l = \hat{n}_i [\hat{t} - \hat{r}(\xi_c, \eta_c)] < 0 \tag{3.67a}$$

A unit normal

$$\hat{n}_i = \hat{n}_i(\xi_c, \eta_c); \quad \hat{t}_i = \hat{n}_i \sum_{j=1}^n N_J(F_1)^j(t)$$
 (3.67b)

$$K_i = f_{\rm si} K_i A^2_i / V_i \tag{3.67c}$$

where $(F_1)^j(t) =$ impact at the *j*th node; $k_i =$ stiffness factor for mass segment S_i ; K_i , V_i , $A_i =$ bulk modulus, volume and face area, respectively; $F_{si} =$ scale factor normally defaulted to 0.10; $N_i = 1/4(1 + \xi \xi_i)(1 + \eta \eta_c)$ for a 4-node linear surface.

Bangash extended this useful analysis for others such as 8-noded and 12noded elements. On the basis of this theory and owing to the non-availability of the original computer source, a new sub-program CONTACT was written in association with the program ISOPAR. CONTACT is in three dimensions; the values of N_i for 8- and 12-noded elements are given in Table 3.14.

3.5 High Explosions

The pressure *P* is generally defined as a function of relative volume and internal energy. Assuming $F_1(t)$ is the final surface load, the pressure *P* must replace $F_1(t)$ in relevant equations by taking into consideration the surface volume on which it acts. All equations defining relevant detonation pressures *P* must first be evaluated. They are then first applied as stated, in Eqs. (3.13), (3.14), (3.15), (3.16), (3.17), (3.18), (3.19), (3.20), and (3.21).

The cause of explosions can be nuclear (air burst or underground). The pressures, which are time dependent, can then act as surface loads on the body of the element concerned or at nodal points of the element as concentrated loads derived on the basis of shape functions. It is essential to choose a proper time-aspect ratio as it will affect the type of solution procedure adopted. The interaction between the loads and the structure can be considered and the method shown in Section 3.5 must be included.

3.6 Spectrum Analysis

Spectrum analysis is an extension of the mode frequency analysis, with both base and force excitation options. The response spectrum table is generally used and includes displacements, velocities and accelerations. The force excitation is, in general, used for explosions and missile aircraft impact. The masses are assumed to be close to the reaction points on the finite element mesh rather than the master degrees of freedom. The base and forced excitations are given below. For the base excitation for wave

$$\gamma_i = \{\psi_i\}_R^{T'}[M]\{b\}$$
(3.68)

For the impact excitation

$$\gamma_i = \{\psi_i\}_R^{T'}[M]\{F_1(t)\}$$
(3.69)

| | Table 3.1 | 4 N , for 8- and 12-noded elements | |
|-------------------|--|---|--|
| | 2 | 6 6 7 7 7 7 7 7 7 7 7 7 7 7 7 | |
| Eight-noded membi | rane element | | |
| Node <i>i</i> | Shape functions $N_i(\xi,\eta)$ | | Derivatives |
| | | $\frac{\partial N_i}{\partial \xi}$ | $\frac{\partial \xi}{\partial \xi}$ |
| | $rac{1}{4}(1-ec{\xi})(1-\eta)(-ec{\xi}-\eta-1)$ | $rac{1}{4}(1-\eta)(2arepsilon+\eta)$ | $rac{1}{4}(1-arepsilon)(2\eta+arepsilon)$ |
| 2 | $rac{1}{2}(1-arepsilon^2)(1-\eta)$ | $-\xi(1-\eta)$ | $-\frac{1}{2}(1-\xi^2)$ |
| 3 | $rac{1}{4}(1+arsigma)(1-\eta)(arsigma-\eta-1)$ | $rac{1}{4}(1-\eta)(2\xi-\eta)$ | $rac{1}{4}(1+\xi)(2\eta-\xi)$ |
| 4 | $rac{1}{2}(1-\eta^2)(1+\xi)$ | $rac{1}{2}(1-\eta^2)$ | $-\eta(1+\xi)$ |
| 5 | $rac{1}{4}(1+arsigma)(1+\eta)(arsigma+\eta-1)$ | $rac{1}{4}(1+\eta)(2arepsilon+\eta)$ | $\frac{1}{4}(1+\xi)(2\eta+\xi)$ |
| 9 | $rac{1}{2}(1-\xi)(1+\eta^2)$ | $-\xi(1+\eta)$ | $rac{1}{2}(1-\xi^2)$ |
| 7 | $rac{1}{4}(1-arepsilon)(1+\eta)(-arepsilon+\eta-1)$ | $rac{1}{4}(1+\eta)(2\xi-\eta)$ | $rac{1}{4}(1-\xi)(2\eta-\xi)$ |
| 8 | $rac{1}{2}(1-\eta^2)(1-arepsilon)$ | $-rac{1}{2}(1-\eta^2)$ | $-\eta(1-\xi)$ |
| | | | |

Table 3.14 *N*, for 8- and 12-noded elements



where $\{\psi_i\}_{\mathbf{R}}$ = the slave degree-of-freedom vector mode; M = mass; $\{b\}$ = unit vector of the excitation direction; $\{F_1(t)\}$ = an input force vector due to impact and explosion.

The values of $\{\psi_i\}_{R}$ = are normalised and the reduced displacement is calculated from the eigenvector by using a mode coefficient $\{M\}$

$$\{x_i\} = [M_i]\{\psi\}_i \tag{3.70}$$

where $\{x\}_i$ = reduced displacement vector and $[M_i]$ = mode coefficient and where

(a) for velocity spectra

$$[M_i] = [\dot{x}_{si}]\{\gamma_i\}/\omega_i \tag{3.71}$$

where \dot{x}_{si} = spectral velocity for the *i*th mode; (b) for force spectra

$$[M_i] = [Fsi]\{\gamma\}/\omega^2 t \tag{3.72}$$

where F_{si} = spectral force for the *i*th mode; (c) caused by explosion *P* or impact $F_1(t)$

$$[M_i] = [\ddot{x}_{\rm si}]\{\gamma_i\}/\omega_i^2 \tag{3.73}$$

where \ddot{x}_{si} = spectral acceleration for the *i*th mode; (d)

$$[M_i] = [x_{\rm si}]\{\gamma\}/\omega_i^2 \tag{3.74}$$

 $\{x_i\}$ may be expanded to compute all the displacements, as in

$$\{x_{\gamma}\}_{i} = [K_{\gamma\prime\gamma\prime}]^{-1} [K_{\gamma\prime\gamma\prime}] \{x_{i}\} R$$
(3.75)

where $\{x'_{\gamma}\}_i$ = slave degree of freedom vector of mode *i*; $[K_{\gamma'\gamma'}][K_{\gamma'\gamma}]$ = submatrix parts; γ, γ' = retained and removed degrees of freedom.

The impact/explosion load is then equal to

$$\left[[K_{\gamma \gamma}] - [K_{\gamma \gamma}] [K_{\gamma \gamma'}]^{-1} [K_{\gamma' \gamma}] \right] \{ x_{\gamma} \} = \left[\{F_{\gamma}\} - [K_{\gamma \gamma'}] [K_{\gamma \gamma'}]^{-1} \{F_{\gamma'}\} \right]$$

or

$$[\overline{K}][\overline{\ddot{x}}] = \{\overline{F}_1(t)\}$$
(3.76)
where

$$[\overline{K}] = [K_{\gamma\gamma}] - [K_{\gamma\gamma'}] [K_{\gamma'\gamma'}]^{-1} [K_{\gamma'\gamma}]$$
(3.77)

$$\{\overline{F}_{1}(t)\} = \{F_{\gamma}\} - [K_{\gamma\gamma'}][K_{\gamma'\gamma'}]^{-1}\{F_{\gamma'}\}$$
(3.78)

$$\{\overline{x}\} = \{x_{\gamma}\}\tag{3.79}$$

and [K] and $\{F_1(t)\}\$ are generally known as the substructure stiffness matrix and the impact load vector, respectively.

3.7 Solution Procedures

Three types of solution procedures are available for impact and explosion analysis, namely time-domain, frequency-domain and modal analysis.

3.7.1 Time-Domain Analysis

The following steps are adopted using a direct implicit integration procedure

3.7.1.1 Initialisation

(1) The effective stiffness matrix is

$$[K_{\rm o}^*] = \left(\frac{6}{\tau^2}\right)[M] + \left(\frac{3}{\tau}\right)[C_{\rm o}] + [K_{\rm o}]$$
(3.80)

(2) Triangularise $[K_0^*]$

For each time step, calculate the displacement $\{x_{t+\tau}\}$

• Constant part of the effective load vector

$$\{R_{\tau}^{*} + \tau\} = \{R_{\tau}\} + \theta(\{R_{t+\delta t}\} - \{R_{t}\}) + \{F_{t}\} + [M] \times \left(\frac{6}{\tau^{2}}\right)\{x_{t}\} + \left(\frac{6}{\tau}\right)\{\dot{x}_{t}\} + 2\{\ddot{x}_{t}\} + [C_{o}]\left(\left(\frac{3}{\tau}\right)\{x_{t}\} + 2\{\dot{x}_{t}\} + \left(\frac{\tau}{2}\right)\{x_{t}\}\right)$$
(3.81)

- Initialisation, i = 0, $\{\delta F_{t \to t+t}^i\} = 0$
- Iteration
- (a) $i \rightarrow i+1$
- (b) Effective load vector $\{R_{t+\tau_{\text{TOT}}}^*\} = \{R_{t+\tau}^*\} + \{\delta F_{t\to t+\tau}^i\}$
- (c) Displacement $\{x_{t+\tau}^i\}[K_0^*]\{x_{t+\tau}^i\} = R_{t\to+\tau\text{TOT}}^{*i}$

3.7 Solution Procedures

(d) Velocity $\{\dot{x}_{t+\tau}^i\} + (\frac{3}{\tau})(\{x_{t+\tau}^i\}) - \{x_t\} - [\delta k_{t-\tau+\delta t}^i] - 2\{\dot{x}_t\} + (\frac{\tau}{2}\{\ddot{x}_t\})$

(e) Change of initial load vector caused by non-linear behaviour of the material =

$$\{\delta F_{t \to t+\tau}^{i}\} = - [\delta C_{o \to t}]\{\dot{x}_{t+\tau}^{i}\} - \{\dot{x}_{t}\}\omega - [\delta C_{t \to t+\tau}^{i}]\{\dot{x}_{t+\tau}^{i}\} \\ \times [\delta K_{o \to t}](\{x_{t+\tau}^{i}\} - \{X_{t}\}) - [\delta K_{t \to t+\delta t}^{i}]\{X_{t+\tau}^{i}\}$$
(3.82)

In fact, $\{\delta F_{t \to t+\tau}^i\}$ is calculated using the initial-stress method. (f) Iteration convergence

$$||\{\delta F_{l\to l+\tau}^{i}\} - \{\delta F_{l\to l+\tau}^{i-1}\}||/\{\delta F_{l\to l+\tau}^{i}\} < \text{tol} = 0.01$$
(3.83)

or, analogously, on stresses.

Calculation of Velocity and Acceleration

Calculate the new acceleration $\{\ddot{x}_{t+\delta t}\}$, velocity $\{\dot{x}_{t+\delta t}\}$, displacement $\{x_{t+\delta t}\}$ and initial load $\{F_{t+\delta t}\}$

$$\{\ddot{x}_{t+\delta_t}\} = \left(\frac{6}{\theta\tau^2}\right)(\{x_{t+\tau}\} - \{x_t\}) - \left(\frac{6}{\theta\tau}\right)\{\dot{x}_t\} + \left(1 - \left(\frac{3}{\theta}\right)\right) \quad (3.84)$$

$$\{\ddot{x}_t\}\{\dot{x}_{t+\delta t}\} = \{\dot{x}_t\} + \left(\frac{\tau}{2\theta}\right)\{\ddot{x}_t\} + \{\ddot{x}_{t+\delta t}\}$$
(3.85)

$$\{x_{t+\delta t}\} = \{x_t\} + \left(\frac{\tau}{\theta}\right)\{\dot{x}_t\} + \left(\frac{\tau^2}{6\theta_2}\right)(2\{\ddot{x}_t\} + \{\ddot{x}_{t+\delta t}\})$$
(3.86)

$$\{F_{t+\delta t}\} = \{F_t\} + \{\delta F_{t\to t+\tau}^i\}$$
(3.87)

Calculation by Quadratic Integration

When the velocity varies linearly and the acceleration is constant across the time interval, appropriate substitutions are made into Eq. (3.13), giving

$$[f_1[M] + f_2[C_t] + [K'_t]]\{x_t\} = \{F_1(t)\} + [M](f_3x_{t-1}) - f_4(x_{t-2}) + f_5(x_{t-3}) + [C](f_6\{x_{t-1}\} - f_7\{x_{t-2}\} + f_8\{x_{t-3}\})$$
(3.88)

where f_1 , f_2 are functions of time. This results in an implicit time integration procedure. The only unknown is $\{x_t\}$ at each time point and this is calculated in the same way as in static analysis. Equation (3.88) is then written as

$$\left(\frac{2}{\delta t_0 \delta t_0} [M] + \frac{\delta t_0 + \delta t_1}{\delta t_0 \delta t_0} [C] + [K'_t]\right) \{x_t\} \\
= \{F_1(t)\} + [M] \left(\frac{2}{\delta t_0 \delta t_1} \{x_{t-1}\} - \frac{2}{\delta t_1 \delta t_0} \{x_{t-2}\}\right) \qquad (3.89) \\
+ [C_t] \left(\frac{\delta t_0}{\delta t_0 \delta t_1} \{x_{t-1}\} - \frac{\delta t_0}{\delta t_0 \delta t_1} \{x_{t-2}\}\right)$$

where

 $\delta t_0 = t_0 - t_1$ and t_0 = time of current iteration $\delta t_1 = t_1 - t_2$ and t_1 time of previous iteration $\delta t_2 = t_2 - t_3$ and t_2 time before previous iteration $\delta t_2 = \delta t_0 - \delta t_1$ and $t_0 - t_2$ and t_3 = time before t_2

Calculation by Cubic Integration

Equation (3.88) becomes cubic and hence is written as

$$(f_{1}[M] + f_{2}[C_{t}] + [K'_{t}]\{x_{t}\})$$

$$= \{F_{1}(t)\} + [M](f_{3}\{x_{t-1}\} - f_{4}\{x_{t-2}\} + f_{5}\{x_{t-3}\}) \quad (3.90)$$

$$+ [C](f_{6}\{x_{t-1}\} - f_{7}\{x_{t-2}\} + f_{8}\{x_{t-s}\})$$

where f_1 to f_8 are functions of the time increments; these functions are derived by inverting a 4 × 4 matrix.

For clear-cut solutions, the size of the time step between adjacent iterations should not be more than a factor of 10 in non-linear cases and should not be reduced by more than a factor of 2 where plasticity exists.

3.7.2 Frequency-Domain Analysis

The original equation of motion is reproduced as

$$[M]{\ddot{x}} + [C]{\dot{x}} + [K]{x} = {J_F}{F}$$
(3.91)

where $\{J_F\}$ is a vector with all components zero except the last one, which is 1.

The terms [K] and [C] shall be frequency dependent. The value of $\{F\} = [K_N]\{x_s\}$ can be taken for solutions of rigid rock problems. If the excitation with frequency w assumes the form $e^{i\omega t}$ then

$$\dot{x} = i\omega x_{s'}; \quad \ddot{x}_s = -\omega^2 x_{s'}; \quad \{x\} = i\omega\{x\}$$

and $\{x\} = -\omega^2\{x\}$ (3.92)

Equation (3.91) can thus be written as

$$([K] + i\omega[C] - \omega^2[M])\{x\} = \{J_F\}K_n x_s$$
(3.93)

For a given value of w, a set of algebraic equations is solved using any numerical scheme. The displacement of a mass can be written as

$$\{x\} = ([K] + i\omega[C] - \omega^2[M])^1 \{JF\} K_n x_s$$
(3.94)

From displacements, accelerations, velocities, strains and stresses can be computed. The amplification function (AF) for each frequency x_1/x_s may be derived. Repeated solutions of Eq. (3.92) are necessary for a proper definition of this function. If the fast Fourier transform is used then AF must be tabulated at each frequency interval.

3.7.3 Runge–Kutta Method

It is an accurate method of time integration and is explicit in nature. Table 3.15 summarises this method. This method of higher order is a robust algorithm used to solve non-linear equations but may have problems which have discontinuous coefficients which take place spatially. Some coefficients change discontinuously as the load increases. Strain localisation will be difficult to produce in numerical simulations. Non-linear equations have bifurcation. The non-linear equation of stochastic elasto-plasticity is more suitable for finding the most unstable solution compared with the non-linear equation of deterministic elasto-plasty since the coefficients change continuously.

| Table 3.15 The Runge–Kutta method | |
|---|------------|
| $x^{n+1} = x^n + \frac{\delta t}{6} \left(f^{(1)} + 2f^{(2)} + 2f^{(3)} + f^{(4)} \right)$ | (3.95) (a) |
| where $f^{(1)} = f(x^n), f^{(2)} = f(x^n) + \frac{\delta t}{2} f^{(1)}$ | |
| $f^{(3)} = f(x^n) + \frac{\delta t}{2} f^{(2)}$ | |
| $f^{(4)} = f(x^n) + \delta t f^{(3)}$ | |
| Some computations are needed to calculate $f^{(1)}$ to $f^{(4)}$ | |
| f = kx | (3.95) (b) |

3.7.4 Keierleber Method

The author developed implicit with θ -operators covering linear, quadratic and cubic with θ -operators developed by Keierleber C.W. University of Nebraska (2003). The author found the Keierleber C.W. approach of these solution procedures extremely flexible and easily adaptable with both programs ISOPAR and F. BANG-2.

(a) Linear Implicit Method

$$\begin{cases} \ddot{x}_i + 1\\ \dot{x}_i + 1\\ x_i + 1 \end{cases} = [A] \begin{cases} \ddot{x}_i\\ \dot{x}_i\\ x_i \end{cases} + \{L\}(r_i\theta)$$
(3.96)

where

$$r_{i+\theta} = \frac{F_{i+\theta}}{m}, \{L\} = \begin{cases} \beta \\ \frac{\Delta t}{2}\beta \\ \frac{\Delta t^2}{6}\beta \end{cases}$$
(3.97)

$$[A] = \begin{bmatrix} \gamma\beta & \frac{1}{\Delta t}(\phi\beta) & \frac{1}{\Delta t^2}(-\omega^2\Delta t^2\beta) \\ \frac{\Delta t}{2}(1+\gamma\beta) & \frac{1}{2}(2+\phi\beta) & \frac{1}{2\Delta t}(-\omega^2\Delta t^2\beta) \\ \frac{\Delta t^2}{6}(2+\gamma\beta) & \frac{\Delta t}{6}(6+\phi\beta) & \frac{1}{6}(6-\omega^2\Delta t^2\beta) \end{bmatrix}$$
(3.98)

$$\beta = \frac{6}{6\theta + 6\xi\omega\theta^2\Delta t + \omega^2\theta^3\Delta t^2}$$
$$\gamma = \frac{6 + 6\theta - 12\xi\omega\theta\Delta t + 6\xi\omega\theta^2\Delta t - 3\omega^3\theta^2\Delta t^2 + \omega^2\theta^3\Delta t^2}{6}$$
$$\varphi = \omega^2\Delta r^2\theta + 2\xi\omega\Delta t$$
$$\beta = \frac{6}{6\theta + 6\xi\omega\theta^2\Delta t + \omega^2\theta^3\Delta t^2}$$

(b) Quadratic Implicit with θ Method Operators

$$\begin{cases} \ddot{x}_{i+1} \\ \dot{x}_{i+1} \\ x_{i+1} \end{cases} = [A] \begin{cases} \ddot{x}_i \\ \dot{x}_i \\ x_i \end{cases} + \{L\}(r_i\theta)$$
(3.99)

where

$$r_{i+\theta} = \frac{F_{i+\theta}}{m}, \{L\} = \begin{cases} \beta \\ 0 \\ \frac{5\Delta t}{12}\beta \\ \frac{\Delta t^2}{8}\beta \end{cases}$$
(3.100)

$$[A] = \begin{bmatrix} \gamma\beta & \rho\beta & \frac{1}{\Delta t}(\phi\beta) & \frac{1}{\Delta t}^{2}(-\omega^{2}\Delta t^{2}\beta) \\ 1 & 0 & 0 & 0 \\ \frac{\Delta t}{12}(8+5\gamma\beta) & \frac{\Delta t}{12}(-1+5\rho\beta) & \frac{1}{12}(12+5\phi\beta) & \frac{5}{12\Delta t}(-\omega^{2}\Delta t^{2}\beta) \\ \frac{\Delta t^{2}}{24}(10+3\gamma\beta) & \frac{\Delta t^{2}}{24}(-1+3\rho\beta) & \frac{\Delta t}{8}(8+\phi\beta) & \frac{1}{8}(-\omega^{2}\Delta t^{2}\beta) \end{bmatrix} (3.101)$$

$$\beta = \frac{24}{12(\theta + \theta^2) + 4\xi\omega\Delta t(3\theta^2 + 2\theta^3) + \omega^2\Delta t^2(2\theta^3 + \theta^4)}$$

$$\gamma = \frac{-12(1 - \theta^2) - 8\xi\omega\Delta t(3\theta - \theta^3) - \omega^2\Delta t^2(6\theta^2 - \theta^4)}{12}$$

$$\rho = \frac{12(\theta - \theta^2) - 4\xi\omega\Delta t(3\theta^2 - 2\theta^3) - \omega^2\Delta t^2(6\theta^2 - \theta^4)}{24}$$

(3.102)

$$\phi = -2\xi\omega\Delta t - \omega^2\Delta t^2\theta$$

(c) Cubic Implicit with θ Method Operators

$$\begin{cases} \ddot{a}_{i+1} \\ \ddot{a}_{i} \\ \ddot{a}_{i+1} \\ \ddot{a}_{i+1} \\ a_{i+1} \end{cases} = [\mathbf{A}] \begin{cases} \ddot{a}_{i} \\ \ddot{a}_{i+1} \\ \ddot{a}_{i+2} \\ \ddot{a}_{1} \\ a_{i+1} \end{cases} + \{L\}(r_{i}\theta)$$
(3.103)

where

$$r_{i+\theta} = \frac{F_{i+\theta}}{m}, \quad \{L\} = \begin{cases} \beta \\ 0 \\ \frac{3\Delta t}{8}\beta \\ \frac{19\Delta t^2}{180}\beta \end{cases}$$
(3.104)

Note: Keierleber Method

Keierleber C. W. developed a method of implicit method with θ opeators. The author developed linear implicit, quadratic implicit and cubic implicit all with θ operators. They are based on time integration approach. Plate 3.1 gives a summary of them.

3.7.5 Additional Solution Procedure

The following additional solution procedures are recommended. They are included in the programs ISOPAR and F. BANG-2.

3.7.6 Newton–Raphson Method

This concept benefits from the Taylor expression. Similar to the direct method given in Plate 3.1 and tabulated below, the Newton–Raphson as stated earlier can be viewed at for comparison: A reference is made to Plate 3.2. Additional solution procedures

| Direct integration method (Plate 3.1) | Newton-Raphson method (Fig. 3.7) |
|--|--|
| $\Psi(u) = Ku + F = 0 (3.105)$ | $\Psi(u) = Ku + F = 0$ |
| where $K = K(u)$ | $=\Psi[u^{n}] + [\frac{d\Psi}{du}]\{\Delta u^{n}\} = 0 (3.108)$ |
| $u_1 = -[K_0]^{-1} f$ where | with $\{u^{n+1}\} = \{u^n\} + \{\Delta u^n\}$ (3.109) |
| $K_{\rm o} = K(u_{\rm o}) \qquad (3.106)$ | |
| For <i>n</i> th iteration, one can write | In the above the derivative represents the |
| $u^n = [K^{n-1}]^{-1}.F (3.107)$ | tangential matrix |
| The process is terminated | The improved value u^{n+1} can be obtained as |
| when the error $e = u^n - u^{n-1}$ becomes | $\{\Delta u^n\} = -[k^n]_{T'}^{-1}\Psi^n$ |
| sufficiently small usually expressed in | $= -[K^n]_{T'}^{-1} \{F^n + F\}$ where T'' represents |
| terms of NORM | transpose (3.110) |



Plate 3.1 Direct method

3.7 Solution Procedures



Fig. 3.7 Newton-Raphion method

3.7.7 Modified Newton-Raphson Method

Since there is a difficulty of having to solve a completely new sytem of equations at each iteration an approximation can be introduced [(Fig. 3.8; Plate 3.2)]. This can be done to

$$[K]^{n}_{T''} = [K^{o}]_{T''}$$
(3.111)



Fig. 3.8 Modified Newton–raphion method

Plate 3.2 Large deflection of a column



and a simple solution known as 'resolution' of the same system of equations is repeatedly used.

3.7.7.1 Incremental Method

This method is elaborately explained in the text [(Fig. 3.9)]. It is realised that the solution for $\{u\}$ is known when the load term is zero. Once the starting point is known, it will be useful to study the *u* as *F* is incremented. For small increments of *F*, convergence is highly likely. For the loading process, the intermediate computed results would be useful information. Thus the method begins with



Fig. 3.9 Incremental method

$$\{F\}\{u\} + \{\lambda Fo\} = 0 \tag{3.112}$$

Differentiation is now needed. Assuming it is an exact differentiation, then

$$\frac{d\{F\}}{d\{u\}} \cdot \frac{d\{U\}}{d\{\lambda\}} + \{F_{o}\} = [K]_{T'} \frac{d\{u\}}{d\{\lambda\}} + \{F_{o}\} = 0$$
(3.113)

In simplified form

$$\frac{dU}{d\lambda} = -[K_{T''}\{U\}]^{-1}\{F_{o}\}$$
(3.114)

Here one can identify the tangential matrix. To simplify the equation such as the above one, Euler's method is used which states

$$\{U_{m+1}\} - \{U_m\} = -[K_{T''}]\{U_m\}^{-1}\{F_o\}\{\Delta\lambda - m\} = -[K_{T''}]^{-1}\{\Delta F_m\}$$
(3.115)

where

$$\lambda_{m+1} = \lambda_m + \Delta \lambda_m \tag{3.116}$$

or

$$F_{m+1} = F_m + \Delta F_m \tag{3.117}$$

Improved integration schemes in the text can be used.

3.8 Geometrically Non-linear Problems in Finite Element

3.8.1 Introduction

Geometrically non-linear problems are assumed to be those associated with large displacements and large strains. In the presence of large displacements, the structure subjected to static or dynamic loads alters shapes and hence changes distributions. Large displacements normally affect stress-strain relationship. Equilibrium equations are written for deformed geometry. In dynamic condition or under dynamic loading, the deformed geometry can be included in the dynamic non-linear equilibrium equations. The linear analysis forms the basis and there is no need to revise these equations. During deformation the conditions are displaced which are known as moving coordinates and they cause solution problems. In Plate 3.2, the stiffness matrix of AB changes to AC position and [K] is not constant. The matrix $[K]{\Delta U} = {\Delta R}$ where ${\Delta R}$ are the loads applied to the distorted nodes of the distorted elements and effectively are the arrayed *unbalanced* forces. The main idea is that for a typical

solution, procedures described in Section 3.8, the interactive solution, will always be looking for or seeking the configuration which conforms to or with $\{\Delta R\} = 0$. One way is to account for rigid body displacement where a distortion of the load axis x' is introduced and for example the distortion member angle φ can be written for element AB as nodes 1 and 2:

$$\phi = \tan^{-1} \frac{Y_{\rm L}}{x_{\rm L}} \tag{3.118}$$

If an element is distorted, it can also be expressed in the local coordinate system.

Various parameters are written as

$$\delta_{2} = L - L_{o} = \sqrt{x_{2}^{2} + y_{2}^{2} - L_{o}}$$

$$= \sqrt{(x_{o} + F_{4} - F_{1})^{2} + (y_{o} + \theta_{5} - \theta_{2})^{2} - L_{o}}$$
(3.119)

And θ_1 and θ_2 are evaluated as

$$\theta_1 = M_3 - (\phi - \phi_o) = M_3 - [\tan^{-1} \frac{Y_L}{x_L} - \theta_o]$$
 (3.120)

$$\theta_1 = M_6 - (\phi - \phi o) = M_6 - [\tan^{-1} \frac{Y_L}{x_L} - \theta_o]$$
 (3.121)

Forces $F_{G(1,2)}$ applied at nodes 1 and 2 by the distorted element are written in local coordinates

$$\{F_{G(1,2)}\} = [K]\{\delta\}$$
(3.122)

where

$$\delta = \begin{bmatrix} 0\\0\\\theta_1\\\delta_2\\0\\\theta_2 \end{bmatrix}$$
(3.123)

Several computer packages exist to solve geometrically distorted structures, mostly based on the following criteria (Fig. 3.10):

- 1. Establish initially local coordinates using local displacements
- 2. Compute element distortions in local coordinates
- 3. Establish [K] the stiffness matrix; $[K]{\delta}$ in local coordinates
- 4. Transfer [K] and $\{F_G\}$ to global coordinates



Fig. 3.10 Geometrically non-linear problems

- 5. The transfer technique is followed for all the distorted elements under new distributed loads. Repeat for all
- 6. Assemble global structural matrices $[K] = \sum [K]$ and $[R]_G = \sum \{F_G\}$
- 7. Compute the $\{\Delta R\}$, the unbalanced forces for the vector of the applied loads and $\{R\}$
- 8. Solve for the displacement increment $\{\Delta u\}$ from the structural equations $[K]\{\Delta u\} = \{\Delta R\}$
- 9. Add increments $\{\Delta u\}$ to global displacement $\{\delta\}$ accumulated in previous interactions.
- 10. Update estimate of the equilibrium configuration.
- 11. Apply convergence criteria given in the text.
- 12. When it does not converge go to step 1.

3.9 Finite Element Analysis of Explosion in Nuclear Facilities Using the Method of Explosive Factor

In order to stimulate detonation controlling of the release of chemical energy, a factor is needed to multiply the equations of high explosives given in books. The finite element method would require at the initial stage a lighting time t_{1l} for each element. Assuming the detonation velocity is v_D , the value of t_{1l} will be computed as follows:

Distance from the centre line of the detonation point to the centre of the element divided by v_D

The explosive factor f_{exp} between two points 1 and 2 will be

$$f_{\exp} = \{f_{1,\exp}, f_{2,\exp}\}$$

such that

$$f_{1,\exp} = \frac{2(t - t_{1l})v_{\rm D}}{3(v_{\rm e}/A_{\rm emax})} \quad \text{for } t > t_{1l}$$
(3.124)

$$= 0 \qquad \text{for } t \le t_{1l} \tag{3.125}$$

$$f_{2,\exp} = \frac{1 - v}{1 - v_{\rm oj}} \tag{3.126}$$

where $v_s =$ detonation velocity; A_e max maximum area on which detonation or burn occurs; t = current time; v_{cJ} Chapman-Jouguet relative volume; v = current volume.

The value of f_{exp} has several steps towards unity and according to Wilkins M.L.¹ spread the burn front over several elements.

After reaching unity, f_{exp} is held constant and if it exceeds 1, it is reset to 1. According to the author the high explosive material be have as an elastic perfectly plastic solids prior to detonation. Hence, it will be necessary to update the stress tensor to an elastic stress $*S_{ij}^{n+1}$ such that

$$* S_{ij}^{n+1} = S_{ij}^{n} + S_{ip}\Omega_{pj} + S_{jp}\Omega_{pi} + 2G\hat{\varepsilon}'_{ij} dt \qquad (3.127)$$

where G is the shear modulus and $\dot{\epsilon}'_{ij}$ is a deviatoric strain rate. The von Mises yield condition is given by

$$\phi = J_2 = \frac{\sigma_y^2}{3} \tag{3.128}$$

where the second stress invariant, J_2 , is defined in terms of the deviatoric stress components as

$$J_2 = \frac{1}{2} S_{ij} S_{ij} \tag{3.129}$$

and the yield stress is σ_y . If yielding has occurred, i.e. $\phi \ge 0$ the deviatoric trial stress is scaled to obtain the final deviatoric stress at time n+1:

For detailed investigation in this field a reference is made to the following publication by the author: '*Manual of Numerical Methods in Concrete*. Thomas Telford, London, 2001.'

The value of S_{ii}^{n+1} can be written as

$$S_{ij} = \frac{\sigma y}{\sqrt{3J_2}} S_{ij}^{n+1}$$
(3.130)

If $\phi \leq 0$ then

$$S_{ij}^{n+1} = S_{ij}^{n+1} \tag{3.131}$$

¹ [Wilkins M.L.,"Calulations of Elastic Plastic Flow," Meth, Comp. Phys. 3 (Academic Press), 211–263 (1964).]

Before detonation pressure is given by the expression

$$P^{n+1} = K(\frac{1}{y^{n+2}} - 1)$$

where *K* is the bulk modulus. Once the explosive material detonates

$$S_{ii}^{n+1} = 0 (3.132)$$

and the material behaves like a gas.

For practical application a reference is made to the author's book on *Explosion-Resistant Buildings*. Springer Verlag 2006.

3.9.1 Good Achievement of the Explosive Burn

It will be necessary to look into the following points in order to achieve good explosive burn:

- 1. Where the impact occurs, the FE mesh must be kept constant.
- 2. The characteristic element dimension must be found by checking all explosive elements for the largest diagonal.
- 3. The detonation points, if possible, must be within or at the boundary of the explosive.



Fig. 3.11 3D global mesh schemes of a tank and PWR nuclear power station

4. Check always the computed lighting time for the explosive material. The lighting time I program LS-DYNA is kept at a negative number. This is true in program BANG F-FIRE

The line of detonation must have sufficient number of detonation points in order to visualise the line of fire. Some of the global mesh schemes such as Tank and PWR power station are shown in Fig. 3.11.

3.10 Finite Element Method Schemes

Several finite element analysis packages are available together with their meshgenerating schemes. Although the subject is beyond the scope of this book, however the following packages are mentioned for the reader's in-depth studies:

Various mesh-generation schemes are available as front ended to various computer packages such as mentioned above. Plate 3.3 just shows a few of such examples. The following are known packages are listed below.



Fig. 3.12 3D mesh-generating schemes of nuclear structures



Plate 3.3 Finite Element Mesh Schemes for structures for nuclear facilities

| ANSYS | IDEAS |
|----------|-----------|
| ABACUS | OAYES |
| DYNA 3D | NASTRAN |
| ASAS | MARC |
| LUSAS | F. BANG |
| Ls DYANA | F. ISOPAR |

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Chapter 4 Steel Pressure Vessels for Nuclear Facilities

4.1 General Introduction

Steel pressure vessels have been used to contain reactor designed for various nuclear power facilities in the world. The dimensions, loadings and materials used are dependent on the type of reactor systems adopted in the nuclear facilities. Some are core left standing covered by radiation shielding or embedded in thick concrete walls and slabs. A typical reactor pressure vessel for PWR is shown in Figure 4.1. Table 4.1 indicates design limit stresses for various pressure parts. This chapter begins with the general design criteria for pressure vessels. These vessels are first treated as thin shell surfaces. The equations of equilibrium of the element shell of revolution have been established. Equations are derived for cylindrical shell surfaces of the vessel. Membrane solution of domical surfaces are given and they are tabulated for a comparative study. Spherical, conical and elliptical dome parts of the vessels have been examined. Step-by-step equations have been established with design examples. Since mostly these vessels in the current environment have Toro spherical domes surfaces, previous equations have been readjusted to cater for these types of surfaces.

A comprehensive accident analysis of PWR loss-of-coolant (LOCA) type accident is generally required. A 3D finite element technique given in Chapter 3 has been used to investigate this effect of thermal shock load causing partial or complete rupture of the vessels. Various results have been produced and they are plotted. Jet impingement forces on PWR steel vessel components have been carefully examined. The R6 method of structure mechanics is examined with failure diagram. At the end, the state-of-the-art software for 3D fracture mechanics simulation in the reactor vessel has been introduced, known as ZENCRACK. Finite element interfaces, mesh procedure, adaptive remeshing and load handling in fracture mechanics have been thoroughly explained and sample applications are given to demonstrate the ZENCRACK by Zentech International Ltd., London.



Fig. 4.1 Cut-away diagram showing the PWR steel vessel and internals (former CEGB Sizewell B inquiry). (From Bangash)^{3.3}

4.2 General Design Criteria for Pressure Vessels

4.2.1 Introduction

ASME provides necessary formulae to compute vessel sizes and membrane stresses of the vessel due to internal and external pressures; it leaves to the designer to carry out analytical procedures for computing stresses due to other loads including combinations of loads.

However, it is a general practice to provide detailed stress analysis for the vessel components outside the Code approved details using either the maximum-stress or the maximum-shear theory of failure and to select allowable stresses for design conditions other than normal operations or for computed stresses other than direct membrane or direct membrane plus primary bending Code stresses. CEGB R6 method based on fracture mechanics is highly recommended. This method later on has been thoroughly discussed in this chapter.

| | | Ta | ble 4.1 Design | n limit stresses for | pressure parts | | | |
|--|-------------------|--------------|-----------------|----------------------|----------------|-----------|--|---------|
| | COMBINAT | ION OF DI | ESIGN LOAD | S | | | | |
| | | | WIND OR | | LOCAL | THERMAL | MAXIMUM | |
| | DESIGN | VESSEL | SEISMIC | TEMPORARY | MECHANICAL | EXPANSION | ALLOWABLE | |
| DESIGN CONDITION | PRESSURE | WEIGHT | LOAD | OVERLOAD | LOAD | LOAD | STRESS | NOTES: |
| 1. Field erection | | × | × | | | | $1.2 S_a$ | 1 |
| 2. Operating | × | × | × | | | | S_a | 2, 5 |
| 3. Operating with thermal | × | × | × | | | × | $1.25(S_a + S_{atm})$ | 2, 3, 5 |
| expansion | | | | | | | | |
| 4. Short-term mechanical | × | × | | × | | | $1.33S_a < S_y$ | 2 |
| overload | | | | | | | | |
| 5. Short-term mechanical | × | × | | × | | × | $1.50(S_a + S_{\mathrm{atm}})$ | 7 |
| overload with thermal expansion | | | | | | | | |
| 6. Operating with local | × | × | × | | × | | $2S_a < S_v$ | 2, 5 |
| mechanical load (bending) | | | | | | | a | |
| 7. Hydrotest | test pressure | | | | | | $S_{\mathrm{atm}} \times \mathrm{test}$ factor | 4 |
| S_a = basic code allowable sti | ress value at de | sign metal t | emperature | | | | | |
| $S_{\text{atm}} = \text{basic code allowable}$ | stress value at a | atmospheric | : metal tempera | ture | | | | |
| Notes | | | | | | | | |

Computed stresses are based on the full uncorroded thickness.

2. Computed stresses are based on the corroded thickness.

- allowable stress range rather than using the shear theory of failure. The value $1.25(S_a + S_{atm})$ provides a safety margin against the possibility of fatigue due to localized stresses and other stress conditions (see Fig. 2.1). Obviously, stresses must be computed both with and without thermal expansion, since allowable 3. The criterion used here is the approach used in the ANSI B31.3 Petroleum Refinery Piping, that is, to limit the maximum calculated principal stress to the stresses are much smaller for conditions without thermal expansion. As an additional safety precaution, the computed stresses are usually based on the modulus of elasticity E at room temperature [8].
 - 4. Computed stresses are based on test thickness at test temperature. Since water pressure is a short-term condition, the allowable stresses for structural parts such as supports are frequently increased by a factor of 1.2. The upper limit of stress in the vessel shell during a hydrotest of pressure parts is not specified by the Code. However, it is a good engineering practice to limit the maximum membrane stress in any part of the vessel during a hydrotest to 80 percent of the yield strength. Thermal expansion stresses and local mechanical stresses will be absent and need not be considered.
- thousands. For cyclic conditions these allowable stresses would have to be substantially reduced and preferably a fatigue analysis made. Usually, in service the 5. This allowable stress limit is for statically stressed vessels. This means that the number of stress cycles applied during the life of vessel does not exceed several operating loads.are raised gradually up to their maximum values and maintained for some time and they are not reapplied often enough to make a fatigue analysis necessary.



Fig. 4.2 (a) The reactor vessel of a 4-loop PWR system (safety factors computed using the finite-element method). (b) Diagram showing sections from which the PWR vessel may be fabricated when sections are either rolled plate or forged material (*shaded parts* are common to both). (Courtesy of Marshall^{5.155}) (From Bangash^{3.3})

Table 4.1 gives the design limit stresses for the pressure parts of the steel vessel and they are kept as BENCH MARK for checking linear. Non-linear and fracture/cracking analysis based on computerized numerical methods such as finite element and boundary elements techniques. Basically the stresses, as they occur in the vessel shells, are divided into three distinct categories: primary, secondary and peak.

Primary stress is produced by steady mechanical loads, excluding discontinuity stresses or stress concentrations. Its main characteristic is that it is not

self-limiting. Primary stress is divided into two subcategories. It is imposed on the vessel by the equilibration of external and internal mechanical forces. Any yielding through the entire shell thickness will not distribute the stress, but will result in gross distortions, often carried to failure. General primary stress is divided into primary membrane stress and primary bending stress; the limit design method shows that a higher stress limit can be applied to the primary bending stress than to the primary membrane stress.

Local primary stress is produced by the design pressure alone or by other mechanical loads. It has some self-limiting characteristics. If the local primary *stress* exceeds the yield point of the material, the load is distributed and carried by other parts of the vessel.

The basic characteristic of *secondary stress* is that it is self-limiting. Minor yielding will reduce the forces causing excessive stresses. Secondary stress can be divided into membrane stress and bending stress, but both are controlled by the same limit stress intensities. Typical examples of secondary stress are thermal stresses and local bending stresses due to internal pressure at shell discontinuities.

Peak stress is the highest stress at some local point under consideration. In case of failure, peak stress does not generate any noticeable distortion, but it can be a source of fatigue cracks, stress-corrosion and delayed fractures. According to the shear theory of failure yielding in a member under loads begins if the maximum induced shear stress equals the yield shear stress developed in a test sample under simple tension. The maximum shear stress τ at the point under consideration equals one-half the largest algebraic difference between any two out of three principal stresses ($\sigma_1, \sigma_2, \sigma_3$) at that point. It occurs on each of two planes inclined 45° from these two principal stresses. For $\sigma_3 > \sigma_{2>} \sigma_1$, maximum $\tau = (\sigma_3 - \sigma_1)/2$. Twice the maximum shear stress τ is by definition the equivalent intensity combined stress or stress intensity.

There is a procedure for the computation of stress intesities.

- 1. The maximum stress intensity is computed on the basis of P_m , the sum of all primary membrane stress components which must not exceed a stress intensity equal to $\sigma_m \times k$ and k, a stress intensity factor ranges 1.0–1.2 for different load combinations such that when applied to $\sigma_m = \sigma_y$ or $\leq \frac{1}{3}\sigma_u$, while $\sigma_m =$ basic design stress value intension of the vessel materials.
- 2. Local membrane stress intensity. The maximum allowable stress intensity for S derived from σ_L stresses is $1.5\sigma_m$ times the factor k when applicable.
- 3. Primary membrane ($\sigma_{\rm m}$ or $\sigma_{\rm L}$) plus primary bending ($\sigma_{\rm b}$) stress intensity. The maximum stress intensity S based on $\sigma_{\rm m}$ or $\sigma_{\rm L}$ stresses plus the bending stress ($\sigma_{\rm b}$) is limited to $1.5\sigma_{\rm m}$ time the factor k when applicable.
- 4. Primary plus secondary stress intensity. The maximum stress intensity S as based on the primary or local membrane stresses plus the primary bending stress plus the secondary stress ($\sigma_{\rm m}$ or $\sigma_{\rm L} + \sigma_{\rm b} + \sum \tilde{Q}$) cannot exceed the

value of $3\sigma_m$. All stresses may be computed under operating conditions, usually less severe than the design conditions $(3\sigma_m \le 2\sigma_y)$

5. *Peak stress intensity*. If fatigue analysis is required for cyclic operating conditions, the maximum stress intensity *S* must be computed from the combined primary, secondary and peak stresses $(\sigma_{\rm m} \text{ or } \sigma_{\rm L} + \sigma_{\rm b} + \sum \tilde{Q} + \sum \tilde{F})$ under operating conditions. The allowable value $\sigma_{\rm a}$ for this peak stress intensity *S* is obtained by the methods of analysis for cyclic operations with the use of the fatigue curves.

The symbols below define various stresses:

 $\sigma_{\rm m}$ = sum of all general primary membrane stress components $\sigma_{\rm L}$ = sum of all local primary membrane stress components $\sigma_{\rm b}$ = sum of all primary bending stress components $\sum \tilde{Q}$ = sum of all secondary (membrane and bending) stress components $\sum \tilde{F}$ = sum of all peak stress components

Note: In ASME codes σ is defined as "S" but this symbol is adopted for uniformity for suitable computerized analysis as done elsewhere in the text.

4.3 Stress Analysis of Vessel Shell Components

4.3.1 Shape and Curvature

At any point of a shell surface there are two principal curvatures: $1/R_1$, and $1/R_2$. The Gaussian or *mean* curvature $1/R_1$, $1/R_2$ is used for classification.

- Synclastic or elliptical surfaces have $1/R_1R_2 > 0$, i.e. both curvatures are at the same sign. Examples are domes, elliptic paraboloids ('elpers').
- Anticlastic or hyperbolic surfaces with $1/R_1R_2<0$ are of the saddle type; curvatures at a point are of different sign. They are sensitive to the way they are supported and to various secondary effects, such as temperature, shrinkage.
- Some anticlastic surfaces can be generated by straight tines (ruled or warped surface): the *conoid* (one system of straight generators), the *hyperboloid* and the *hyperbolic paraboloid* ('Hypar') both with two systems of straight generators. They are easier to form than synclastic surfaces, but are subject to large displacements if free at the edges.
- Surfaces of *zero Gaussian curvature* i.e. *cylindrical shells* are probably most affected by the bending effect, and the membrane theory can give good approximation only in exceptional cases.
- *Folded plate structures* stripes of plate jointed at the edges are not really shells at all, but in functioning and in the way they can be treated are quite close to cylindrical shells. The edges of the dome shell of the reactor vessel will, sometimes, develop the shape of the folded plates.

Kind of surface

- *Developable surfaces* can be bent into other shapes without stretching e.g. cylindrical and conical shells.
- Non-developable surfaces, i.e. of double curvature.

4.3.2 Boundary and Edge Conditions

- Closed shells
- Open shells with various edge conditions:

Free for clamped continuous support Single supports Edge beams Ribs Ties and traverses

Boundary and edge conditions modify the behavior of the shell, due to disturbance or perturbations originating from the edges.

4.3.3 Generalized Analysis of Thin Shell Surfaces of the Reactor Vessels

4.3.3.1 Assumptions Made in the Theory of Elastic Thin Shells

- 1. Direct stresses perpendicular to the middle surface can be neglected.
- 2. Points on a normal distribution to the middle surface before the deformation will be on a straight line after the deformation has taken place.
- 3. This line will remain perpendicular to the deformed middle surface.
- 4. Displacements are small compared to the thickness of the shell.

Stress resultants of a shell of the reactor vessel:

A system of coordinates, i.e. x, y, is defined on the middle surface, so that the lines x = const meets lines y = const at right angles (Gaussian coordinates). The element is out from the shell along pairs of adjacent coordinates lines, and the cuts are made so that four sides of the element are normal to the middle surface. The coordinates z is measured positive inwards, x, y, z, from a right-handed triad.

(*Note:* Some writers define z positive outwards, which results in an interchange of x and y axes to preserve the right-hand rule).

Stress resultants are defined as *forces* (or bending moments) *per unit of length* as in plate theory. Figure 4.3 shows the shell element with the stresses. Figure 4.4 shows the membrane stress resultants. The tensile forces are positive, and the

Fig. 4.3 Membrane stresses



Fig. 4.4 Membrane stress resultants

figure shows positive shear forces N_{xy} and N_{yx} . Figure 4.5 shows the bending stress resultants, i.e. bending moments M_x , M_y , twisting moment M_{xy} , M_{yx} and transverse (radial) shear forces Q_x and Q_y .

The applied external forces revolved into components X, Y, Z in the directions for the *membrane stress resultants* are

Fig. 4.5 Bending stress resultants



$$N_{x} = \int_{\frac{-t}{2}}^{\frac{t}{2}} \sigma_{x} \left(1 - \frac{z}{r_{y}} \right) \mathrm{d}z; \quad N_{y} = \int_{\frac{-t}{2}}^{\frac{t}{2}} \sigma_{y} \left(1 - \frac{z}{r_{x}} \right) \mathrm{d}z$$
(4.1)

$$N_{xy} = \int_{\frac{z}{t}}^{\frac{t}{2}} \tau_{xy} \left(1 - \frac{z}{r_y} \right) dz; \quad N_{yx} = \int_{\frac{z}{t}}^{\frac{t}{2}} \tau_{yx} \left(1 - \frac{z}{r_x} \right) dz$$
(4.2)

The second terms in these expressions Z/r_y , Z/X are due to the trapezoidal form of the sides of the element: as the thickness *t* is small compared with the radii of curvature, these terms are omitted.

 $\tau_{xy} = \sigma_{yx}$ are complementary shear stresses, but shear forces N_{xy} and N_{yx} are only equal when $r_x = r_y$.

4.3.3.2 Assumptions of the Membrane Theory for Shells

The stresses are uniformly distributed over the thickness of the shell, from which it follows that $N_{xy} = N_{yx}$ (by dropping the second term τ_{yx} and τ_{xy} can be taken in front of the integration sign). The membrane stress resultants are therefore

- all the other six stress resultants are assumed to be zero;
- the three equations of equilibrium of forces are sufficient to determine the three unknowns, N_x , N_y and N_{xy} .

The requirements for the use of the membrane theory are

- 1. The middle surface must be continuous (no sudden changes of curvature).
- 2. No sudden changes of the thickness are allowed.
- 3. Reactions at the edges must be directed tangentially to the middle surface, and support arrangements must be made to allow this.

The geometry of a dome, as a shell of revolution, is shown in Fig. 4.6 and with notation in Figs. 4.7 and 4.8.

Fig. 4.6 Geometry of dome







Fig. 4.8 The membrane stress resultants and the load components

4.3.4 The Equations of Equilibrium of the Element of a Shell of Revolution

The equation for forces in the x direction (along tangent to a parallel circle) Geometry:

Tangents to meridians at A and B intersect at angle a (Fig. 4.9a)

$$r_2 \tan \phi d\alpha = AB = r d\theta$$

$$\mathrm{d}\alpha = \frac{r\mathrm{d}\theta}{r_2 \tan \phi}$$

But,

$$r = r_2 \sin \phi$$
$$d\alpha = d\theta \cos \phi$$

Required: component of $N_{\theta\phi}$, $R_{d\theta}$ in the x direction

$$2 \times N_{\theta \phi} r_1 \mathrm{d}\phi \sin\left(\frac{\mathrm{d}\alpha}{2}\right) = N_{\theta \phi} r_1 \mathrm{d}\phi \mathrm{d}\alpha$$



Fig. 4.9 (a) Tangents to meridian. (b) Equilibrium diagram. (c) Elements of meridian

But, $d\alpha = d\theta \cos \phi$

$$N_{\theta\phi}rd\theta + \frac{\partial N_{\theta\phi}}{\partial \phi}rd\theta d\phi - N_{\theta\phi}rd\theta + N_{\theta}r_{1}d\phi + \frac{\partial N_{\theta}}{\partial \theta}r_{1}d\phi d\theta - N_{\theta}r_{1}d\phi + N_{\theta}r_{1}d\phi d\theta \cos\phi + Xr_{1}d\phi rd\theta = 0$$

$$(4.3)$$



Fig. 4.10 Longitudinal forces

r = radius of curvature of parallel circle

 r_I = radius of curvature of meridian

 r_2 = length of normal to surface, to axis of rotation

 $r_1, r_2 =$ principal radii of curvature at A (Meusnier theorem)

$$AB = \mathrm{rd}\theta$$

$$AD = r_1 d\phi$$

Total forces acting on the sides of the element are shown in the figure as $AB \neq CD$. Coordinate axes are

- x = along tangent to parallel circle
- y = along tangent to meridian
- z = normal to the shell surface

And after reduction, as

$$\frac{\partial}{\partial \phi} \left(r N_{\phi \theta} \right) + r_1 \frac{\partial N_{\phi}}{\partial \phi} + r_1 N_{\phi \theta} \cos \phi + X r r_1 = 0 \tag{4.4}$$

The equation for forces in the *y* direction (along tangent to meridian).

Required: components of total force on AD and BC $N_{\theta}rd\phi$ has component along the radius of the parallel circle:

$$2N_{\theta}rd\phi\sin\left(\frac{\mathrm{d}\theta}{2}\right) = 2N_{\theta}r_{1}\mathrm{d}\phi\mathrm{d}\theta$$

Resolving this in the y and z directions:

Component in y direction $N_{\theta} r d\phi d\theta \cos \phi$ Component in z direction $N_{\theta} r_1 d\phi d\theta \sin \phi$

$$\frac{\partial}{\partial \phi} (rN_{\phi}) + r_1 \frac{\partial N_{\theta \phi}}{\partial \theta} + r_1 N_{\theta} \cos \phi + Yrr_1 = 0$$
(4.5)

The equation for forces in Z direction (i.e. normal to the middle surface of the shell):

Component due to N_{ϕ} in the Z direction:

$$N_{\phi} r \mathrm{d}\theta \sin\left(\frac{\mathrm{d}\phi}{2}\right) = N_{\phi} r_1 \mathrm{d}\theta \mathrm{d}\phi$$

Component due to N_{θ}

The complete equation of this equilibrium is

 $N_{\theta}r_{1}\mathrm{d}\phi\mathrm{d}\theta\sin\phi + N_{\phi}r\mathrm{d}\theta\mathrm{d}\phi + Zr_{1}r\mathrm{d}\theta\mathrm{d}\phi = 0$

4 Steel Pressure Vessels for Nuclear Facilities

where $r = r_2 \sin \phi$ and $r_1 = r_2 \sin \phi d\theta d\phi$

$$\frac{N_{\phi}}{r_2} + \frac{N_{\theta}}{r_2} + Z = 0 \tag{4.6}$$

Identity of cross shears

$$N_{\phi\theta} = N_{\theta\phi} \tag{4.7}$$

Equations (4.4), (4.5), (4.6) and (4.7) allow the calculation of the membrane forces of a shell of revolution, also for asymmetrical loading.

4.3.5 Shells of Revolution: Axisymmetric Loading

With loads symmetric about the vertical axis of rotation, Eqs. (4.4), (4.5), (4.6) and (4.7) simplify considerably

- 1. Stresses are independent of θ , and all partial derivatives with respect to θ disappear.
- 2. $N_{\phi\theta} = N_{\theta\phi} = 0$, otherwise they would produce asymmetrical deformation with respect to the vertical axis.
- 3. There is no variation of other stress resultants with θ .
- 4. The component *X* of the load must vanish; it would produce twist about the axis and shear deformation.

Therefore, Eq. (4.1) is identically satisfied and disappears. Hence, Eq. (4.5) simplifies to

$$\frac{\mathrm{d}}{\mathrm{d}\phi}\left(rN_{\phi}\right) + rN_{\theta}\cos\phi + Yrr_{1} = 0 \tag{4.8}$$

Eq. (4.6) is unchanged

$$\frac{N_{\phi}}{r_1} + \frac{N_{\theta}}{r_2} + Z = 0$$

The differential Eq. (4.8) and the common Eq. (4.6) are sufficient to determine meridian force N_{ϕ} and the hoop force N_{θ} for an axisymmetrically loaded shell of revolution.

Procedure in solving Eqs. (4.8) and (4.6)

From Eq. (4.6)

$$N_{\theta} = -Y_2 \left(Z + \frac{N_{\phi}}{r_1} \right) \tag{4.9a}$$

Substituting into Eq. (4.8) using $r = r_2 \sin \phi$, and multiplying the equation with $\sin \phi$ gives

$$\frac{\mathrm{d}(N_{\phi}r_{2}\sin\phi)}{\mathrm{d}\phi}\sin\phi + N_{\phi}r_{2}\sin\phi\cos\phi = -r_{1}r_{2}(Y\sin\phi + Z\cos\phi)\sin\phi$$

The left-curved side can be written as $d(N_{\phi}r_2\sin^2\phi)/d\phi$ hence

$$\frac{\mathrm{d}(N_{\phi}r\sin\phi)}{\mathrm{d}\phi} = -rr_1(Y\sin\phi + Z\cos\phi) \tag{4.9b}$$

The integration with ϕ is variable

$$N_{\phi} = -\frac{1}{r\sin\phi} \left[\int -rr_1 (Y\sin\phi + Z\cos\phi) d\phi + C \right]$$

where the constant C is found from boundary conditions. The hoop force is obtained later from Eq. (4.6).

The membrane forces of an axisymmetrically loaded dome can be obtained much faster and more directly. Instead of dealing with the equilibrium of the element of the shell, consider the equilibrium of the dome above a certain parallel circle.

If \overline{W} is the vertical resultant of the applied load and $2\pi r N_{\phi} \sin \phi$ is the total vertical component around the parallel circle of the meridian force N_{ϕ} , then

$$2\pi r N_{\phi} \sin \phi - \bar{W} = 0 \tag{4.10}$$

where $N_{\phi} = \overline{W}/(2\pi r \sin \phi)$.

The hoop force N_{θ} can now be calculated (see Fig. 4.9).

4.3.6 Cylindrical Shell Surfaces of the Vessel

4.3.6.1 Types of Cylindrical Shell Surfaces

Cylindrical shells — shells in which either the directrix or the generatrix is a straight line.

Membrane forces on the cylindrical shell part of the vessel under different loads are summarized in Table 4.2.



4.4 Membrane Solution of Domical Surfaces

As the solution of a 3D elasticity problem is tough, shell theory may be viewed as a 3D subset of elasticity valid for certain classes of structures. For this subset we shall develop appropriate kinematics, constitutive and equilibrium relations.

Now consider an element at the dome in the middle surface of the shell of revolution as shown in Fig. 4.11 where R is the radius of curvature of the parallel circle and a is the radius of curvature of the meridian.

The membrane stress, stress resultants and the load components can be designed as P_x , P_y , P_z The coordinate axes, as in Section 4.2.2, are

- x = along tangent to parallel circle
- y = along tangent to meridian
- z = normal to the shell surface

Equations of equilibrium of the element of a shell of revolution. As shown in Figs. 4.11, 4.12 and 4.13, the equations are given below. Equations of forces in the x direction.

Refer to Fig. 4.12: the tangents to meridians at A and B interact at an angle $d\theta$

$$AE = BE = a \tan \phi$$
$$AB = a \tan \phi d\theta \text{ and } AB = r \times \theta P \tag{4.11}$$

This required component of $N_{\theta\phi} \times ad\theta$ in the x direction is



Fig. 4.11 Side element equilibrium



Fig. 4.12 Curve on longitude



Fig. 4.13 Dome geometry

$$2 \times N_{\theta\phi} \times a \mathrm{d}\theta \sin\left(\frac{\mathrm{d}\alpha}{2}\right) = N_{\theta\phi} \times a \mathrm{d}\phi \mathrm{d}\theta = N_{\theta\phi} a \cos\phi \times \mathrm{d}\theta \mathrm{d}\phi = 0 \quad (4.12)$$

Therefore, the complete equation of equilibrium in the x direction is

$$\left(N_{\theta\phi} r \mathrm{d}\theta + \frac{\mathrm{d}N_{\theta\phi}}{\mathrm{d}\theta} \times r\theta \mathrm{d}\phi \right) - N_{\theta\phi} \cdot r \mathrm{d}\theta + \left(N_{\theta} \cdot a \mathrm{d}\phi + \frac{\mathrm{d}N_{\phi}}{\mathrm{d}\theta} \cdot a \mathrm{d}\theta \mathrm{d}\phi \right) - N_{\theta} \cdot a \mathrm{d}\phi + \left(N_{\phi} a \cos\phi \cdot \mathrm{d}\theta \mathrm{d}\phi \right) + P_{x} \cdot a \mathrm{d}\phi \cdot r \mathrm{d}\theta = 0$$

Divide all by $d\theta d\phi$ and the equation becomes

$$\frac{\mathrm{d}(N\phi\theta_{\cdot}r)}{\mathrm{d}\phi} + a.\frac{\mathrm{d}N_{\theta}}{\mathrm{d}\theta} + aN_{\theta\phi}.\cos\phi + P_{x}.ra = 0$$
(4.13)
Equation of forces in the v direction

Refer to Fig. 4.13 the total force on *AD* and *BC*, N_{θ} and $ad\phi$ has a component along the radius of the parallel circle:

$$2N_{\theta}a\mathrm{d}\phi\sin(\mathrm{d}\theta/2)\approx N_{\theta}\mathrm{d}\phi\mathrm{d}\theta$$

Resolving this in the *y* and *z* directions, one has Element in the *y* direction and is as follows:

$$N_{\theta}.ad\phi d\theta \cos\phi$$
 (4.14*a*)

Element in the *z* direction is as follows:

$$N_{\theta}.a\mathrm{d}\phi\mathrm{d}\theta\sin\phi$$
 (4.14*b*)

The complete equation of equilibrium in the *y* direction is as follows:

$$\begin{bmatrix} N_{\phi}rd\theta + d(N_{\phi})rd\theta \frac{d\phi}{d\phi} \end{bmatrix} - N_{\phi}rd\theta + \begin{bmatrix} N_{\theta\phi}ad\phi + \frac{d(N_{\theta\phi})}{d\theta}ad\phi d\theta \end{bmatrix} - N_{\theta\phi}ad\phi - N_{\theta}ad\phi d\theta \cos\phi + P_{y}ad\phi rd\theta = 0$$

Divide all by $d\theta d\phi$ we have

$$\frac{\mathrm{d}}{\mathrm{d}\theta}rN_{\phi} + a\frac{\mathrm{d}(N_{\theta\phi})}{\mathrm{d}\phi} - N_{\theta}a\cos\phi + P_{y}ra = 0$$
(4.15)

Equation of forces in the z direction

Required component of forces on AB and CD $N_{\phi}rd\theta$: component of $N_{\phi}rd\theta$ in the z direction is as follows:

$$2N_{\phi}r\mathrm{d}\theta\sin\left(\frac{\mathrm{d}\phi}{2}\right)\approx N_{\phi}r\mathrm{d}\theta\mathrm{d}\phi$$

Combining this with the component of z of $N_{\theta}ad\phi$ from (4.20a), the complete equation of equilibrium is as follows:

$$N_{\theta}ad\phi\sin\phi + N_{\phi}rd\theta d\phi + P_{z}rad\theta d\phi = 0$$

But $r = a \sin \phi$ therefore

$$\frac{1}{a(N_{\theta} + N_{\phi})} + P_z = 0 \tag{4.16}$$

Assuming that the stresses are uniformly distributed over the thickness of the shell:

$$N_{\theta} = N_{\phi\theta} \tag{4.17}$$

Equations (4.19) and (4.21), (4.22) and (4.23) allow the calculation of the membrane forces of a shell of revolution. Hence with loads symmetric about the vertical axis of rotation, these four equations simplify considerably:

- 1. Stresses are independent of ϕ and all partial derivatives with respect to ϕ disappear.
- 2. $N_{\theta\phi} = N_{\phi}\theta = 0$, otherwise they would produce asymmetrical deformation with respect to the vertical axis.
- 3. There is no variation of other stress resultants with θ .
- 4. The component *P* of the load must vanish; it would produce twist about the axis and shear deformation.

Therefore, (4.19) is identically satisfied and disappears. Hence, Eq. (4.21) becomes

$$\frac{\mathrm{d}}{\mathrm{d}\phi}(rN_{\phi}) - aN_{\theta}\cos\phi + P_{y}ra = 0 \tag{4.18}$$

Equation (4.22) remains the same:

$$\frac{1}{a(N_{\theta} + N_{\phi})} + P_z = 0$$

Therefore

$$N_{\theta} = -(P_z a + N_{\phi}) \tag{4.19}$$

For an axisymmetrically loaded dome, the meridional forces N_{ϕ} can be obtained much faster and directly by considering the equilibrium of the part of the dome above a certain parallel circle.

Then, if V is the vertical resultant of the applied load and $2\pi r N_{\phi} \sin \phi$ is the total vertical component around the parallel circle of the meridional force N_{ϕ}

$$2\pi r N_{\phi} \sin \phi + V = 0 \quad N_{\phi} = -\frac{V}{2\pi r \sin \phi}$$
(4.20)

Let W = weight per unit area. Surface area above parallel circle.

$$S_{\phi} = 2\pi a H = 2\pi a^2 (1 - \cos \phi)$$
 (4.21)

Therefore, the meridional force is as follows:

$$N_{\phi} = -W_a/(1+\cos\phi) \tag{4.22}$$

Therefore, the hoop force is as follows:

$$N_{\theta} = W_a (1 - \cos \phi - \cos^2 \phi) / (1 + \cos \phi)$$
(4.23)

The load on $rd\phi$ about the axis

$$= r \mathrm{d}\phi. 2\pi r \sin \phi w' (\phi - \phi_{\mathrm{o}}) \tag{4.24}$$

Total load is 0-1 about axis

$$W_u = 2\pi r^2 w'(\sin\phi_1 - \sin\phi_0) - \cos\phi_1(\phi_1 - \phi_0)$$

Determination of meridional thrust T and hoop force H

The reader is referred to Figs. 4.14, 4.15 and 4.16 for computing the value of T and H.



Fig. 4.14 Longitude and latitude of a spherical dome



Fig. 4.15 Meridional thrust and hoop or circumferential forces



Fig. 4.16 Forces in equilibrium

$$W_{u} = \text{sum of vertical componets } T$$

$$W_{u} = 2\pi r \sin \phi_{1} \times T \sin \phi_{1}$$

$$T = \frac{W_{u}}{2\pi r \sin^{2} \phi_{1}}$$
(4.24a)

If the dome is continuous along the circle of latitude through 1, a circular ring through that point is subjected to a unit radial force of $(T \times \cos \phi_1)$. Therefore

$$S = \text{ring tension} = (W_u \cos \phi_1) / (2\pi \times \sin \phi_1)$$
(4.25)

Total radial component

Length of arc $A - A' = (2T \times d\phi)/(2r \times d\phi) = T/r$ therefore,

$$H = -T + [w + w'(\phi_1 - \phi_o)] \times r \cos \phi_1 \tag{4.26}$$

4.4.1 Elliptical Dome-Shaped Surfaces of the Vessel

The following analysis is carried out for the elliptical dome (Fig. 4.17). Equation of ellipse

$$\frac{X^2}{a^2} + \frac{Y^2}{b^2} = 1 \tag{4.27}$$

where $X = a \sin \phi$ and $Y = b \cos \phi$. Consider a ring produced by rotating an element ds about the Y axis of the dome.

Fig. 4.17 Elliptical dome



$$ds = \sqrt{[(dx)^{2} + (dy)^{2}]} = \sqrt{[(a^{2}\cos^{2}\phi + b^{2}\sin^{2}\phi)]d\phi}$$
(4.28)

Weight of element ring is as follows

$$dw = 2\pi \times X \times W \times ds$$

= $2\pi \times w \times a^2 \sin \phi \sqrt{(1 - [((a^2 - b^2)/a^2)\sin^2 \phi] \times d\phi)}$ (4.29)

Let $k^2 = (a^2 - b^2)/a^2$ W_u = total load between points 0–1

$$W_u = dw = 2\pi \times a^2 w \left[\cos \phi (\sqrt{1 - k^2 \sin^2 \phi}) - \frac{1}{2} k (1 - k^2) \times \log k \cos \sqrt{(1 - k^2 \sin^2 \phi)} \right]$$

Let $\cos\phi = y/b = g$ and $\sin^2 \phi = 1 - \cos^2 \phi = 1 g^2$ Substitute into Eq. (4.35)

$$W = 2\pi \times a^2 w \left[\frac{1}{2} + \frac{1}{2} k(1 - k^2) \times \log(1 + k) - \frac{1}{2} g \left(\sqrt{1 - k^2(1 - g^2)} - \frac{1}{2} k(1 - k^2) \times \log k + \sqrt{1 - k^2(1 - g^2)} \right) \right]$$
(4.30)
= $(2\pi a^2 w) C$

where C is the quantity in the bracket.

4.4 Membrane Solution of Domical Surfaces

To find the meridional thrust

$$T = \frac{W}{2\pi \sin \phi x}$$

$$= \frac{2\pi \times a^2 wC}{2\pi \times a(\sqrt{(1 - g^2 \sin \phi)})}$$

$$= wCa^2 \sqrt{\frac{1 - k^2(1 - g^2)}{b(1 - g^2)}}$$

$$= \frac{wa^2}{b} \times \frac{CQ}{1 - g^2}$$
(4.31)

where $Q = \sqrt{1 - k^2(1 - g^2)}$

$$H = \frac{-Tx}{R\sin\phi} + \frac{wx\cos^2\phi}{\sin\phi}$$
$$= \frac{-wx^2}{2R\sin^2\phi} + \frac{wx\cos^2\phi}{\sin\phi}$$
$$= \frac{wa^2}{2b} \times \frac{2g^2 - 1}{O}$$
(4.32)

If the dome is continued along the circle of latitude through point 1, an edge member must be provided along that circle and that member is subjected to ring tension, S

$$S = \frac{Wa}{2\pi \times b} \times \frac{g}{\sqrt{1 - g_1}} \tag{4.33}$$

4.4.2 Torispherical Shell Surfaces of the Reactor Vessel Top Dome

The torispherical shell surface is formed when a toroidal segment is inserted between a spherical and a cylindrical cap. The dome surface is always used as well for the reactor vessel.

Main analysis

The geometry of this shell is shown in more detail in Fig. 4.18.

In terms of the radii of curvature of the sphere a_1 , the toroid a_3 and the cylinder a_2 , the meridional angle at the sphere—toroid junction is given by

$$\sin\phi_1 = \frac{a_2 - a_3}{a_1 - a_3} \tag{4.34}$$

In practice, the radius of the toroid is selected so as to provide smooth transitions at both ends.



Fig. 4.18 Torospherical shell geometry

To derive the membrane theory stress resultants, one again uses the overall equilibrium method. At a general section within the toroid, $\phi_1 < \phi < \pi/2$, the resultant axial load consists of two parts: P_I = the load on the spherical cap, and $P_2(\phi)$ = the load between ϕ_1 and ϕ on the toroid. For a uniform positive pressurep, the magnitude of the first force is the pressure multiplied by the projected base area of the cap.

Toroidal-shaped surfaces

$$P_1 = p\pi (a_1 \sin \phi_1)^2$$
 (4.35*a*)

For the second force, first compute the horizontal radius of the toroid

$$R_0 = (a_1 - a_3)\sin\phi_1 + a_3\sin\phi$$
(4.35b)

Whereupon the magnitude equals the pressure multiplied by the area of the projected annulus,

$$P_2(\phi) = p\pi [R_0^2 - (a_1 \sin \phi)^2]$$

= $p\pi [(a_1 - a_3)^2 \sin^2 \phi_1 + a_3^2 \sin^2 \phi + 2(a_1 - a_3)a_3 \sin \phi_1 \sin \phi - a_1^2 \sin^2 \phi_1]$

which reduces to

$$P_2(\phi) = p\pi a_3(\sin\phi - \sin\phi_1)[a_3(\sin\phi - \sin\phi_1) + 2a_1\sin\phi_1]$$
(4.35c)

Summing Eqs. (4.35a) and (4.35c)

$$P(\phi) = p\pi\bar{p}(\phi)$$

where,

$$\bar{p}(\phi) = (a_1 \sin \phi_1)^2 + a_3 (\sin \phi - \sin \phi_1) \\ \times [a_3 (\sin \phi - \sin \phi_1) + 2a_1 \sin \phi_1]$$
(4.35d)

$$N_{\phi} = \frac{1}{2\pi R_0 \sin \phi} \bar{p}(\phi)$$

$$= \frac{p\bar{p}(\phi)}{2[(a_1 - a_3)\sin \phi_1 + a_3\sin \phi]\sin \phi}$$
(4.36a)

To compute the circumferential stress resultant, the equation for N_{θ} is

$$N_{\theta} = R_{\theta} \left(p - \frac{N_{\phi}}{R_{\phi}} \right) \tag{4.37}$$

From Eq. (4.37) since $R_0 = R_0 \sin \phi$

$$R_{\theta} = \frac{a_2 - a_3}{\sin \phi} + a_3 = (a_1 - a_3) \frac{\sin \phi_1}{\sin \phi} + a_3$$
(4.38)

From Fig. 4.18

 $R_{\phi} = a_3$

Substituting (6.55a) and (6.56) into (6.55b) gives

$$N_{\theta} = p \left[\frac{(a_1 - a_3) \sin \phi_1 + a_3 \sin \phi}{\sin \phi} \right]$$

$$\times \left\{ 1 - \frac{\bar{Q}(\phi)}{2a_3 \sin \phi [(a_1 - a_3) \sin \phi_1 + a_3 \sin \phi]} \right\}$$
(4.39)

Equation (4.36a) and (4.39) constitute the membrane theory solution for the so-called toroidal knuckle portion of the torospherical head, called Toroidal Knuckle:

4.5 Nuclear Reactor: Accident Analysis

4.5.1 PWR Loss-of-Coolant Accident (LOCA)

4.5.1.1 Introduction to LOCA

The important steel reactor pressure vessel analysis is to check them against loss-of-coolant accident (LOCA), especially in PWR. A loss-of-coolant accident (LOCA) occurs as a result of a penetration to the main coolant boundary such that the primary circuit water is released through the break to the containment area, causing a rapid decrease in the pressure and temperature of the primary coolant Fig. 4.19. This will give an impact thermal shock load. The streamline break accident (SLBA) occurs as a result of a complete and partial rupture of a steam line inside the containment vessel. A rapid cool-down and depressurization of the primary circuit normally take place. In order to restore



Fig. 4.19 Finite-element mesh generation of the vessel (a) generalized vessel mesh. (b) Closure head—wall flange region. (From Bangash)

the reactor coolant pressure, a pressure loading unconnected with LOCA is required.

4.5.1.2 Description of the PWR Vessel and Its Materials

Figure 4.1 shows a typical PWR vessel for sizewell B. The vessel steel must possess high toughness and strength coupled with adequate weldability in thick sections, with generally low-alloy steels containing manganese, nickel and molybdenum. The material grade for plates is SA-533 B alloys, and SA-508 alloys for forging. Both must be in quenched and tempered conditions. The suitability of these steels rests on the mechanical properties such as yield stress, ultimate tensile strength, elongation to fracture and charpy impact energy affected by thermal aging, strain aging and neutron irradiation. The vessels are made out of thick-section plates of up to 360 mm or from ingots of over 200,000 kg. The ingots generally develop cavities of up to 3 mm in the *v*-segregation regions. These are healed by hot working processes. Both plates and forgings are welded. Figure 4.2 shows vessel fabrications.

Table 4.1 shows the data used in the 3D finite-element analysis. Figures 4.3 and 4.20 show the finite-element mesh generation scheme of the vessel, wall nozzles and closure heads. These are the important sections and locations in the reactor vessels from the point of view of fracture assessment. Figure 4.21a, b shows the pressure—time and temperature—time relationships. Figures 4.22–4.23 indicate various stresses in different zones due to a LOCA Table 4.3. The defect size in each region is checked using the R6 method of the former CEGB (UK) which is given in Tables 4.4–4.6.





Fig. 4.20 Finite-element mesh generation of (a) wail nozzles and (b) closure head. (From Bangash)



Fig. 4.21 Loss of load (without immediate reactor trip) (Westinghouse revision no 5). (a) Reactor coolant pressure and (b) temperature variations. (Courtesy of Marshall of U.K. AEA) (From Bangash)



Fig. 4.22 Belt-line reactor trip from full power. Time variation of hoop stress in vessel material from clad/vessel interface. 3DD: three-dimensional finite-element analysis (Bangash); M. Marshal^{5.155}; (From Bangash^{3.3})

4.5.1.3 Nuclear Containment Under Hydrogen Detonation

Hydrogen detonation has become an important issue after the Three-Mile-Island accident. The hydrogen burning occurred approximately 10 hours into the accident. The steam reacting with the Zircaloy cladding and the oxidation of the overheated steel vessel interiors created large quantities of hydrogen. This can also occur due to interaction of the molten core. In order to predict the wall pressures due to such detonations, non-linear gas dynamics equations for the entire volume of the containment vessel have to be solved. In the current analysis of the Sizewell B containment vessel, it is assumed that the wall pressure



Fig. 4.23 Secondary thermal stress at various durations: belt-line region. LOCA condition. 3DB: Bangash: M: Marshall.^{5,155} (From Bangash^{3,3})

 P_0 is proportional to the (containment pressure *P*. The vessel parameters are given in Table 4.1 and Figure 4.1. It is assumed that the detonation starts approximately at the mid-height of the containment vessel. The spherical shock front generated obliquely converges at the dome, causing a strong reflection around the apex. The containment finite-element mesh scheme is unchanged. Bond slip and shear slip for the reinforced elements are considered. The following additional input data have been included:

Figure 4.34 a, b shows the non dimensional relationship for the pressure $P/P_{\rm o}$ and $(t/R)v_{\rm so}$ for the Sizewell B vessel at the apex of the dome and at the mid-height. The parameters *R* is the radius of the containment vessel. Figures 4.35 to 4.37 illustrate the stress-time histories for the containment wall, dome springing and dome apex due to detonation.

E.4 Jet impingement forces on PWR steel vessel components

The safety of nuclear installations such as the pressure vessel and its piping systems requires strict measures. In the event of steel failure, the safety rules



Fig. 4.24 Time variation of hoop stress in vessel material from clad/vessel interface (belt-line loss of load). 3DB: Bangash; M: MarshalE^{5.155}(From Bangash^{3.3})

require the assessment of the jet impinging forces on the vessel nozzle areas. In the current analysis it was assumed that the transition from the cross-section of the discharging pipe to that of the outlet is abrupt. It is imperative to evaluate the structural behaviour under the jet impinging forces. The vessel chosen for this analysis was the Sizewell B PWR steel vessel. All parameters and finite-element mesh schemes are kept the same as in Figure 4.1. The following data is used:

At any height/diameter ration (z/D = z/737), the pressure ration $R_{p'} = p'T/P_w$ is computed, where p' is the saturation pressure at temperature T and P_w is the vessel pressure: z/D = 0.85, 0.95, 1, 2, 3, 4, 5 and $10: p'T/P_w$ ranges between 0 and 1 and there is a total of 20 times steps (t), with time interval;s pf 0.24 s.

The jet impinging force against $P'T/P_w$ for failure conditions is given in Figs. 4.28 and 4.29



Fig. 4.24 (a) Comparative study of results for the inside corner of an inlet nozzle. From Bangash^{3.3}



Fig. 4.25 Secondary thermal stresses at various durations for an inlet nozzle shell course large streamline break, M: Marshall,^{5.155} (From Bangash^{3.3})



Fig. 4.26 Inlet nozzle inside corner: reactor trip from full power. 3DB: Bangash: M: Marshall^{5.55} (From Bangash^{3.3})



Fig. 4.27 Inlet nozzle inside corner; loss of power, secondary thermal stresses. 3DB: Bangash; M: Marshall^{5.155} (From Bangash^{3.3})



Fig. 4.28 Inlet nozzle hoop stress plotted through the wall at the sections shown. Basic pressure 17.24 MPa (MN/m^2). 3DB: Bangash: M: Marshall^{5.155} (From Bangash^{3.3})



Fig. 4.29 Main hoop stress plotted through the wall at the sections shown. Basic pressure load of 17.24 MPa (MN/m^2). 3DB: Bangash: M: Marshall^{5.155} (From Bangash^{3.3})



Fig. 4.30 Axial and hoop stress plotted along the nozzle course and belt-line region for a large LOCA at 600 s. 3DB: Bangash: M: Marshall^{5.155} (From Bangash^{3.3})



Fig. 4.31 Axial and hoop stress plotted along the nozzle course and belt-line region for a large LOCA at 2000 s, 3DB: Bangash: M: Marshall^{5.155} (From Bangash^{3.3})



Fig. 4.32 Safety factors versus displacement (δ). (From Bangash^{3.3})



Fig. 4.33 Load factor versus defect size. 3DB: Bangash; M: Marshall^{5.155} (From Bangash^{3.3})



Fig. 4.34 (a) pressure at the mid-height; (b) pressure at the apex of the dome

ratio = RAT = q/RT_0

Material Liner: $\sigma_v = 390 \text{ MPa}$ Strain rate = 0.1/sPressures and shock front Detonation strength $q/\overline{R}T_0 = 17$ (base) and 23 (mid-height) where q = energy release/unit volume \overline{R} = gas constant = 8.31 kJ/kg-mole K T_0 = absolute temperature Shock front ν_{so} = shock wave velocity = 2000 m/s t = 0,50, 100, 200, 250, 300 μs (a) 3D F.E 400 failure 300 150 start at base RAT = 15 100 0 Stress (MN/m²) 300 (b) 30F.E at mid-height RAT = 25 250 200 150 - at mid-height RAT = 16 -100

Time, t (µs) Fig. 4.35 Stress histories at 40% of the cylinder, with variation of steel properities included: (a) inside hoop bars; (b) inside vertical bars; (c) seismic diagonal bars.

75

90

60

300

200

100

0

0

(C)

15

30

45

| Proposed parameters for | Sizewell D. | |
|--|---|----------------------------------|
| Vessel overall height | 13660 mm | |
| Inside diameter | 4394 mm | |
| Wall thickness opposite core | 215 mm | |
| Wall thickness at the flange | 500 mm | |
| Normal clad thickness | 6 mm | |
| Thickness of the dome top | 178 mm | |
| Thickness of the dome bottom | 127 mm | |
| Inside diameter of inlet nozzle | 700 mm | |
| Inside diameter of outlet nozzle | 737 mm | |
| Number of closure | 54 (each 1466 mm high) | |
| studs | (nut 268×203) | |
| | (washer 268×38) | |
| Studs | 173 mm | |
| Dry weight of the pressure vessel | 434.8×10 ³ Kg | |
| Normal operating pressure | 15.98 MPa | |
| Design pressure | 17.13 MPa | |
| Initial hydraulic pressure | 21.43 MPa | |
| Normal operating inlet temperature | 288°C | |
| Normal operating outlet temperature | 327°C | |
| Design temperature | 343°C | |
| No load temperature | 292°C | |
| Design life | 40 years at 80% load factor | |
| $E_{\rm s} = C \times E \times 10^5 {\rm MPa}$ | C varies with temperature | |
| (1) Material SA533B | C = 0.218, $Mn = 1.367$, $Ni = 0.547$, $Mo =$ | = 0.547, Si = 0.236, Cr = 0.074, |
| · · · · · | P = 0.009, S = 0.014 | |
| (weight per cent) | C=0.117 | |
| (2) Submerged arc- welding | C = 0.16, Mn = 2.20, Ni = 0, Mo = 0.6, S S = 0.035 | i = 0.05, Cr = 0, I = 0.025, |
| (electrode wire content) | C = 0.15 | |
| (3) Mechanical | Yield stress (N/mm ²) Ultimate tensile | Charpy test (minimum value) |
| properties | stress (N/mm ²) | |
| (a) SA533B plates | at 20°C 345 at 20°C 555 | |
| . – | at 400°C 280 at 400°C 520 | 34 J at 4.4°C flanges, shell |
| (b) SA508 forging | at 400° C 280 at 20° C 555 | rings and nozzles average or |
| | at 400°C 430 | values 150, 138, 100, |
| (c) Weld metal | 483 593 | respectively |

 Table 4.3 Vessel material properties and parameters

 Proposed parameters for Sizewell B:

| (d) | Stresses after 288°C | | |
|-------------|---------------------------------------|---|---|
| | irradiation unirradiated | These are given before from $3(a)$ to $3(c)$ Add 2% of the above values | |
| (e) | Fracture toughness of | | |
| (f) | plates Bonding | $K^{lc} = 106 \text{ N/mm}^2, \sqrt{m} = 153$ Yield = 900–1050 N/mm ² ; ultimate tens | ils stess = 1050 N/mm^2 ; |
| 1 | material | impact energy = $60.9-81.2 \text{ J}$ | Ultimata tancila strass |
| (4) M pr | echanical operties | Yield stress (N/mm ²) | (N/mm ²) Charpy test (minimum value) |
| (a) | SA533B plates | at 20°C 345 at 400°C 280 | at 20°C 555 at 400°C 520 34 J at 4.4°C at 20°C 555 at 400°C 430 flanges shell or rings and |
| (b) | SA508 forging | at 400°C 280 | nozzles 593 average values 150, 138, |
| (c) (d) | Weld metal Stresses after 288°C | 483 | 100, respectively |
| | irradiation unirradiated | These are given before from 3(a) to (3c) Add 2% of the above values | |
| (e) | Fracture toughness of | | |
| | plates | $K_{Ic} = 106 \text{ N/mm}^2, Vm = 153$ | |
| (f) | Bonding material | Yield = $900-1050 \text{ N/mm}^2$; ultimate tensi energy = $60.9-81.2 \text{ J}$ | le stress = 1050 N/mm; impact |

 Table 4.3 (continued)



 Table 4.4
 R6 method of fracture assessment

The failure assessment diagram for the R6 method (courtesy of CEGB, UK).

Figure represents $K_r - S_r$ diagram

$$K_r = S_r \left\{ \frac{8}{\pi^2} \log_e \sec\left(\frac{\pi}{2} S_r\right) \right\}^{-1/2}$$
(4.40)

$$K_r = K_r^{\rm P} / K_{\rm IC} \tag{4.41}$$

where K_r is a measure of how close the vessel is to linear clastic failure = 0.59 and K_1^p is the stress intensity factor due to σ stresses and is given by

$$K_{\rm I}^{\rm P} = Y \sigma \sqrt{\pi a} = 39.42 \,{\rm Mpa} \sqrt{{\rm m}}$$

where Y = magnification factor when applying unflaw stresses obtained to postulated flawed vessel; a Y value of 1.25 has been taken

 σ = applied stress

 $a = \operatorname{crack} \operatorname{height}$

 $K_{\rm IC}$ = fracture toughness, with a lower limit of 170 MPa \sqrt{m} at 288°C

Defect length 2C parallel to component surface

| Defect depth | S | distance between nearest edge of the defect and component surface |
|---------------|----|---|
| | | (normal distance) |
| Defect height | 2a | distance between nearest and the furthest extremities of a defect |

Defect height 2a distance between nearest and the furthest extremities of a defect normal of the surface (buried 2a, surface breaking a)



Fig. 4.36 Stress histories at hte dome springline, with variation of steel properties included: (a) inside hoop bars; (b) inside vertical bars; (c) seismic diagonal bars



Fig. 4.37 Strees histories 10° from the dome apex, with variation of steel properties included: (a) inside hoop bars; (b) inside meridional bars







Fig. 4.38 Measurements for jet impingement forces on a flat plate due to the discharge of saturated pressurized water from circular nozzles of different diameters

4.6 State-of-the-art Software for 3D Fracture Mechanics Simulation (ZENCRACK)

(Provided by R. Chandwani, Managing Director ZENTEC Corp. London). Zencrack is an advanced engineering analysis tool for 3D fracture mechanics assessment and crack growth simulation. The program uses finite element analysis to allow calculation of fracture mechanics parameters such as energy release rate and stress intensity factors. This is achieved by automatic generation of focused cracked meshes from uncracked finite element modules. A general mixed-mode crack growth capability allows non-planar crack growth prediction for fatigue and time-dependent load conditions via automated adaptive meshing techniques.

Overview

Zencrack provides flexibility with two levels of simulation capability -Standard and Professional.

For industries where static loading is important the Standard version can be used to evaluate stress intensity factors using energy release rate and nodal



| symbol | D (mm) | z/D |
|-------------------------|-----------|------|
| | 40 | 0.55 |
| * * | 40 | 0.50 |
| -00- R.F | 40 | 1.0 |
| - <u>A</u> - <u>A</u> - | 50 | 2.0 |
| ΦΦ | 40 | 3.0 |
| F.E -●-●- | 10 | 2.0 |
| -00- | 10 | 3.0 |

Fig. 4.39 $R'_{\rm p}$ versus $F_1(t)$

 Table 4.5
 Semi-elliptic surface breaking floor configuration: sample calculations
 For 0.1 < a/2c < 0.5 and $a/t \le 0.8$. When a/2c < 0.1 then c/w = a/t (extended crack). Therefore the S_r value is given by $S_{\rm r} = \{1/\bar{\sigma}(1-c/w)^2\}\{[\sigma_{\rm bc}/4 + \sigma_{\rm mc}(c/w)]\} + [(\sigma_{\rm bc}/4 + \sigma_{\rm mc}(c/w))^2 + \sigma_{\rm mc}^2(1-c/w)^2]^{1/2}$ (4.42)a/c13 if a = 70 mm: c = 210 mm 0.1 < 7/42 < 0.5 is satisfied $c/w = 2ac\pi/4t(2c+t) = 2(70)(210)\pi/4(216)(420+216) = 0.168$ (4.43) $\sigma bc = 6m/t^2 = 7.56/, MPa$ With $a/c\frac{1}{3}$. $\sigma_{\rm mc} = 171.5$ MPa, if a = 70 mm and c/w = 0.168 = area of flaw/area of rectangle. $S_{\rm r} = [7.56 \text{E}/4 + 175.5 \text{E}6(0.168)] + [(7.56 \text{E}6/4 + 171.5 \text{E}6(0.168)^2)]$ $+(171.5)^{2}(1-0.168)^{2}|^{1/2}/440E6(1-0.168)^{2}$ or $S_{\rm r} = 0.58$ and $K_{\rm I}^{\rm P} = Y \sigma_{\rm mc} \sqrt{\pi a} = 1.25(171.5 {\rm E6}) \sqrt{\pi (0.07)} = 100.53 \,{\rm MPa} \,\sqrt{{\rm m}}$ (4.44)where $K_{\rm r} = K_{\rm I}^{\rm P}/K_{\rm IC} = 100.53 {\rm E}6/170 {\rm E}6 = 0.59$ σ_{bc} = clastically calculated bending stress evaluated over the gross section containing the flaw

 σ_{mc} = clastically calculated tensile stress evaluated over the gross section containing the flaw



Table 4.6 Failure assessment of crack heights due to LOCA

Computed data: normal operating conditions, belt-line region S_r and K_r values for flaws normal to the hoop stress.

| Crack height | Effective ration | Calculate | Calculated values | |
|---------------|------------------|------------|-------------------|--|
| <i>a</i> (mm) | c/w | $S_{ m r}$ | $K_{ m r}$ | |
| 70 | 0.168 | 0.58 | 0.59 | |
| 90 | 0.234 | 0.70 | 0.67 | |
| 110 | 0.301 | 0.86 | 0.74 | |
| 130 | 0.371 | 1.10 | 0.81 | |

Normal operating conditions, belt-line region S_r and K_r values for flaws normal to hoop stress.

| Effective ratio | Calculate | ed values | |
|-----------------|--|---|---|
| c/w | $S_{ m r}$ | $K_{ m r}$ | |
| 0.168 | 0.25 | 0.23 | |
| 0.234 | 0.30 | 0.26 | |
| 0.301 | 0.38 | 0.29 | |
| 0.371 | 0.48 | 0.32 | |
| 0.440 | 0.64 | 0.34 | |
| 0.510 | 0.88 | 0.36 | |
| | Effective ratio c/w 0.168 0.234 0.301 0.371 0.440 0.510 | Effective ratioCalculate c/w S_r 0.1680.250.2340.300.3010.380.3710.480.4400.640.5100.88 | Effective ratioCalculated values c/w S_r K_r 0.1680.250.230.2340.300.260.3010.380.290.3710.480.320.4400.640.340.5100.880.36 |

displacement methods. For thermal transients, the instantaneous stress intensities may be evaluated through the transient to steady state conditions. Collapse analyses may be undertaken to allow, for example, generation of data for failure assessment diagrams.

The second level of capability is introduced through Zencrack Professional and provides a facility for 3D non-planar crack growth prediction for cases of fatigue and time-dependent loading. This includes several options for crack growth data definition and a flexible "load system" approach for defining complex load spectra.

4.6.1 Application Areas

ZENCRACK can be applied in any industry in which knowledge of crack behaviour, crack growth prediction and residual life calculation are important. Zencrack is relevant in many situations, e.g.

- Post-failure, forensic and accident investigations
- Parametric studies of different crack sizes in a component
- Leak before break studies
- Design of experiments
- Repair assessments
- Determination of inspection periods
- Determination of residual life
- Assessment of brittle-ductile failure using failure assessment diagrams

ZENCRACK takes an uncracked finite element mesh and inserts one or more user-specified cracks before submitting the model for analysis. Results are processed automatically and the mesh updated ready for the next finite element analysis of the advanced crack position.



4.6.2 Sample Applications

- Roller support including significant mode II and mode III effects and the use of crack face contact
- Crack at a bolt hole in an engine disk including temperate effects.



4.6.3 F.E. Interfaces

By interfacing to commercial finite element codes rather than using a proprietary finite element solution, Zencrack is able to take advantage of the many man-years of development within these codes and their associated pre and postprocessors.





4.6.4 A Typical Crack Growth Analysis Procedure

A typical crack growth analysis begins with a geometry model created in the user's pre-processor. This is meshed as an "uncracked model" in preparation for the insertion of the defect(s) by Zencrak. The insertion of the initial defect results in a cracked mesh ready for analysis in the interfaced finite element code. The analysis results are extracted for a fully automatic crack growth simulation in which re-meshing technologies allow the crack to be advanced through the structure. Typical results from an analysis include crack growth profiles and plots such as crack growth vs load cycles and stress intensity factor vs crack size. This is a useful method also when the vessel cracks under LOCA.

4.6.5 Meshing Procedure

The generation of 3D finite element models suitable for analysis of cracks requires special attention in and around the crack region where focused rings of hex elements are used. In addition, the initial crack front may be straight, a simple elliptic section, or a general curve in space.



To address these issues, Zencrack removes the onus of modelling the crack region from the analyst and requires instead that an uncracked mesh is supplied. A "crack-block" approach is then used to introduce one or more crack

fronts into the uncracked mesh. The term crack-block refers to a collection of brick elements stored as a unit cube. The arrangement of these noded brick elements in a user-supplied uncracked mesh by crack-blocks. During the mapping process to introduce the crack-blocks the user can control the size and shape of the generated crack-block. Crack-blocks can be connected together to form distinct crack fronts of the required size in the cracked mesh.

4.6.6 Adaptive Re-meshing

In a crack growth analysis the shape of the crack that develops is a function of the geometry, loading and material properties. The re-meshing of the crackblocks and if necessary the modification of the surrounding mesh that takes places automatically to allow the correct crack shape development in the structure. No assumptions are forced onto the developing crack shape – it is a consequence of the structure, loading and material. Any local mixed mode effects arising at the crack front are embodied in the stress and displacement solution and are handled during the growth and re-meshing procedure.

4.6.7 Load Handling

The loading requirements in a fracture mechanics analysis vary considerably depending upon the goal of the analysis. Some possible examples include:

- Parametric study of crack sizes to determine stress intensity factors
- Evaluation of j-integrals at multiple load increments in a non-linear analysis

Chapter 5 Concrete Reactor Pressure Vessels

This chapter attempts to review the state of the art of methods of analysis and design of the concrete reactor pressure vessels and their components. Existing vessels have been examined for elastic, inelastic and cracking conditions. The results obtained from the analysis given in this chapter and in the appendices are well collaborated with those available for the experimental tests on models and from site monitoring of similar structures of vessels. The text is provided with an up-to-date comprehensive bibliography.

5.1 Introduction

The state-of-the-art review of the prestressed concrete reactor vessels covers, in this chapter, historical development, the available methods of analysis and design procedures of vessels and their elements such as concrete, prestressing systems, conventional steel, vessel steel liner and anchorages including penetration liners. Each section is presented with a clear-cut discussion on its contents.

Several methods of analysis and design are described in detail. The author has, for the first time, presented detailed analyses based on Finite Element and Limit State concepts. A suite of computer programs has been developed by the author to evaluate the entire operational history, the inelastic and cracking conditions and the safety margins of the concrete vessels. The methods have been applied to existing vessels chosen built for gas-cooled reactors at Oldbury, Dungeness B, Hartlepool/Heysham and Fort St. Vrain. The results obtained from these analyses are in good agreement with those available from published data.

The analytical and design tools thus available in this text have made it possible to investigate fairly accurately the safety margins of other vessels adopted for pressurised water reactors (PWR), boiling water reactors (BWR) and fast breeder reactors (FBR).

Nomenclature

| $2h_I$ | internal height |
|------------|-----------------------------|
| R_1, R_E | internal and external radii |

| P_G | internal gas pressure |
|--|--|
| P_{GB} | boiler gas pressure |
| R_P | standpipe radius |
| R_B | radius of boiler/circulator |
| H_B | Height of boiler/circulator |
| ε'_{ps} | |
| $\left. \begin{array}{c} \varepsilon_{pc}^{\prime} \\ \varepsilon_{pb}^{e} \end{array} \right\}$ | circumferential strains at hinges |
| \bar{P}_{c} | total cap pressure |
| \overline{x}° | distance at which \bar{P}_c acts |
| F_V | total vertical prestressing load |
| F'_{V} | total modified vertical prestressing load |
| a | distance from the outside face of the vessel to F_V or F'_V |
| <i>R'</i> | distance from the centre line of the vessel |
| Xm Xh Xm | depths of compression hinge at top, bottom and at equator |
| Eng | $\varepsilon_{ro} + \varepsilon_{u}$ |
| Eco | concrete stress at the tendon level divided by E_C |
| - <i>се</i> Е., | average strain at the level of the tendon at ultimate conditions |
| x | neutral axis depth |
| d | depth of the section |
| ε_{pc} | effective prestressing strain after losses |
| ε ₀ | $\sqrt{\sigma}_{ m cm/5000}$ |
| σ_{cu} | concrete stress at ultimate |
| F_{bst}, F'_{bst} | longitudinal forces in tension and compression |
| | reinforcement |
| T_F | total force |
| F_{BL} | liner force |
| C_C | concrete force |
| b | average breadth $(R_E + R_t) \sin \theta$ |
| A'_{sh} | area of bonded steel in compression |
| σ_{vb} | yield stress of bonded steel |
| 2θ | angle of a segment |
| A_{Sb} | area of the bonded steel in tension |
| A_{SL} | area of the liner |
| σ_{yl} | yield steel of the liner |
| D_w | unit weight of concrete |
| $\sigma_{ii}^P, \sigma_{ii}^P$ | plastic stress and strain |
| f | stress function |
| dλ | constant of proportionality |
| С | factor in plasticity rule |
| E_t | tangent modulus |
| Ζ | coefficient for strain hardening |
| P_{HR} | total radial compression |
| P_{Hr} | radial compression $= P_{HR/2RE^{\sin\phi}}$ |
| \mathcal{E}_Z | strain profile at a particular position |

| K' | strength reduction factor from wire/strand bands or from |
|----------------------------|--|
| | the circumferential tendons |
| l_c | crack depth |
| ω_{th}, ω_{tb} | crack width top and bottom |
| \hat{X} | typical value of x_t or x_b |
| ω_{el} | longitudinal crack |
| ω_{eh} | horizontal crack |
| α_c | cap rotation factor |
| $\delta_{z}^{'}$ | deflection of cap at the yield zone |
| $n_{1,} n_{2}$ | concrete block parameters |
| β | measure of a distance |
| σ_t | tangential stress |
| Q | shear force |
| N | axial load |
| $	au_{RZ}$ | uniform or parabolic shear stress |
| Φ' | angle of frictional resistance for concrete |
| C' | apparent cohesion for concrete |
| X_1, X_2 | dimension on a cap plug |
| \overline{S} | terms for the uniform or parabolic shear stress |
| ε_{pp} | strain due to rigid plastic rotation of the barrel wall |
| E _{cpv} | strain due to rigid plastic rotation of the cap |
| E_o, E_s | Young's moduli for concrete and steel |
| ε_{pu} | strain of tendons or band in the circumferential direction |
| A_c | area of concrete |
| A_{sp} | area of prestressing steel |
| δ | displacement in a respective direction |
| Ζ | position of a hinge from equator |
| K_1, K_2, K_3 | coefficients |
| P_{w1}, P_{w2} | total pressure on various zones of the barrel wall |
| M_{HT}, M_{HR}, M_E | moments at top, bottom and equatorial hinges |
| A_{hp} | area of circumferential prestressing tendons or bends |
| n _b | number of boilers/circulators |
| m_{ϕ} | a plastic moment per unit length of the radial yield line |
| $P_{H\phi}$ | pressure due to circumferential tendons |
| H' | slope of the effective plastic stress |
| n | series of values or nth term |
| D_p | plasticity matrix |
| σ_{in} | initial stress |
| σ_{e-p} | clasto-plastic stage |
| σ_{TOT} | total stress |
| y (1) | yield |
| $\{\psi\}$ | residual force vector |
| α | alpha-constant used for acceleration |
| A [77]] | acceleration factor |
| $\lfloor T'' \rfloor$ | transformation matrix |

| ε _{cu} | ultimate or critical strain |
|---------------------------------|--|
| $\sigma_{cv}, \varepsilon_{cv}$ | stress and strain normal to the closed crack |
| τ | shear stress |
| τ_{cv} | shear stress on crack interface |
| tf | transfer stress |
| \hat{F} | transfer force |
| $\Delta \varepsilon_{su}$ | plastic strain in steel |
| $\Delta \varepsilon_s^p$ | plastic strain increment |
| X, Y, Z | global co-ordinates |
| p_i | shape function |
| ξ, η, ζ | local system co-ordinates |
| x_n, y_n, z_n | nodal co-ordinates |
| J | Jacobian |
| <i>u</i> , <i>v</i> , <i>w</i> | displacements |
| a_n | polynomial coefficients |
| [<i>c</i>] | matrix relating a_n and u |
| $\det[J]$ | determinant of a Jacobian |
| 3 | strain at any point |
| $[B_i]$ | matrix relating strains and displacements |
| σ | stress |
| δ | generalized displacement |
| δ^* | virtual displacements |
| $[S_{ijkl}]$ | material compliance tensor |
| W_e | external work done |
| U | internal energy |
| [K] | stiffness matrix |
| $\{F\}$ | nodal forces |
| $\{F_p^e\}$ | nodal forces at elastoplastic stages |
| \overline{f} | body forces and any other loads |
| $\{\hat{g}_{x,n}\}$ | vector containing the values of the body load at nodal pints |
| | in a given direction |
| R_i | residual load |
| L_F | loading function |
| S_H | the yield of work hardening function |

5.2 Historical Development, Existing Analyses and Scope of Research

5.2.1 General

The use of nuclear energy in the production of electrical power involves substantial structural systems comprised of pressure vessels that house the reactor. Most of the light water (LWR) and pressurised water reactors (PWR) in
operation at present are sheltered by two major structural units: the primary container which is a steel pressure vessel for holding the coolant systems pressure and a secondary container providing a second protective shield. An alternative to the use of liquid coolants is a pressurised gas system. The coolant in this case is either carbon dioxide or helium. The current British and French reactors, using these coolants, are called advanced gas-cooled reactors (AGR) and high-temperature gas-cooled reactors (HTR or HTGCR). Efficient operation of these nuclear power plants requires a large electrical output. This requirement calls for a large nuclear core space and much larger primary pressure vessels and supporting structures of sizeable dimensions. The inherent difficulties that would be involved in the fabrication and transportation of the pressure vessel steel units of the size necessary for such a reactor have led to the need for a more versatile type of structure. The vessel must, undoubtedly, be built on site and meet the serviceability and safety requirements. The solution adopted has been the use of prestressed concrete reactor vessels (PCRV).

One incentive for adopting PCRV is the economic advantages to be expected. These advantages arise, for example, from

- (a) the ability to contain large reactors with high pressures and temperatures;
- (b) simplification of plant layout;
- (c) the fact that a highly developed steel fabrication industry is not necessary.

Attractive features from a safety point of view include

- (a) physical isolation of the steel prestressing tendons and reinforcement from sources of heat and radiation and from the primary coolant;
- (b) the high degree of redundancy in the prestressing systems.

The shapes used, so far, for PCRVs have varied from a cylinder bounded by two inverted, non-prestressed, hemispherical domes, torospherical domes to spherical shells. The current trend in PCRV configuration is the use of thick-walled cylinders, the ends of which are closed by flat slabs known as caps. The boilers and circulators are either housed within the main cavity or within the thickness of the walls; the latter is known as a *multi-cavity-type vessel*. This study is concerned with such vessels also apart from other shapes.

The first application of prestressed concrete as a reactor vessel was in the Marcoule G-2 and G-3 installations in France. These are horizontally placed concrete cylinders with concave domes as caps. The vessel main cylinder is wrapped with prestressing cables describing an arc of 2700 which are finally anchored to prestressed concrete foundations under the vessel. The domes are not prestressed, resulting in a substantial loss of vessel volume. The standpipe and the control rod areas are badly situated for the charge machine. The French have recognised these limitations of the Marcoule vessels. However, in the meantime the requirements for high-quality steel and more rigorous inspections for both British and French reactor vessels have reawakened interest in concrete vessels. Consequently, in planning the construction of the EDF-3 reactor, the French designers decided to re-examine the application of prestressed concrete

to reactor vessels. The design selected provides a vessel with a cylindrical shape and with prestressing cables placed in layers parallel and perpendicular to the long axis of the vessel. Supplemental prestressing steel is also provided at the corners where the stress concentrations are high.

The British interest in concrete pressure vessels began with some experimental work done by the then General Electric Company and the Simon-Carves group on cylindrical vessels prestressed circumferentially by wire winding. Based on these tests and other tests carried out by the then United Kingdom Atomic Energy Authority (UKAEA), Waters and Barrett [1] published design studies for cylindrical and spherical vessels containing advanced gas-cooled reactors. They carried out a comparative study of steel and concrete pressure vessels and concluded that there were significant economic and technical attractions to adopting such vessels. They then presented a detailed design philosophy in which particular attention was paid to the short- and long-term effects of tendon loads on concrete, the premature failure of the liner and the optimum choice of the conventional reinforcement as an anti-crack steel. Apart from highlighting design and constructional problems, they suggested a list of research programmes. At a time when no suitable code of practice and no completely reliable mathematical tools existed for analysing and designing such structures, their recommendations prompted many UK firms with interests in nuclear technology to carry out research and development in this field. The first order placed by the then Central Electricity Generating Board (CEGB) was for the Oldbury Power Station. The then Nuclear Power Group (TNPG) proposed a vessel design that was a hybrid of the French Marcoule and EDF-3 concepts. The vessel is of cylindrical shape with flat top and bottom caps, and it utilises alternate layers of helical cables which wrap the vessel in reverse directions. These cables are anchored in groups in specially provided top and bottom galleries. Both longitudinal and lateral prestressing loads are produced from this single prestressing system.

By the time of completion of this vessel a great deal of knowledge had been gained from both the British and the French experience in this field. Another concept was under consideration at the CEGB, namely a spherical vessel containing the entire reactor internals. Owing to immediate requirements for more electrical output, the then CEGB gave the go-ahead to a group member of the British Nuclear Design Company to design and construct such a vessel for the Wylfa power plant. This vessel has a spherical inner surface and the prestressing is provided by a six-sided polyhedron made up of cables anchored to buttresses along the vessel circumference. Each tendon is laid perpendicular to the preceding one. Since the prestressing tendons in the Wylfa Nuclear Power Station are nearly straight, the possibility of large frictional effects is remote. The prestressing loads are uniform and this is partly due to its spherical shape. Compared with cylindrical vessels, the Wylfa spherical vessel effectively utilises the entire prestressing system, and the peak stressing is considerably less.

In the meantime, a number of variations on the French EDF-4 (now Bugey) reactor were under consideration. It was decided to have a vertical cylindrical

pressure envelope divided into two chambers: the upper one supports the reactor core while the lower one contains the boilers or heat exchangers. These affect the size of the internal cavity and the prestressing system. Complete data for these vessels were published by Marsh and Melese based on detailed literature surveys and the preliminary designs carried out by the Frankline Institute.

Both the Frankline Institute [2] and the Oak Ridge Laboratory [2] in the USA made a start on the research and development required for the Fort St. Vram high-temperature gas-cooled reactor. The choice was made of a cylinder with flat top and bottom caps. Both in the wall and in the cap the prestressing was by means of cables of variable curvature.

In the meantime, in the UK a great deal of experience was gained from the Oldbury and Wylfa vessels. Problems associated with the plant layout and the construction of the Wylfa vessel were such that the British designers had to rethink the use of cylindrical vessels. The then CEGB finally approved the cylindrical vessel of the Dungeness B Power Station using large tendons in the vertical and in the circumferential directions. The circumferential tendons are anchored on specially formed buttresses. This time, using a minimum number of large tendons, a greater concentration of forces has been achieved for the limited available space in the vessel.

However, the Oldbury contractors carried out optimisation studies on the UK HinkIey B and Hunterston B power stations. Slight changes in the vessel parameters were inevitable. This time true helices were adopted for the prestressing tendons rather than the 'barrelised' type adopted for the Oldbury vessel.

At this stage, the concept of multi-cavity vessels was under active consideration. Boilers and circulators occupied a large space within the main cavity. The dimensions of the main cavity were reduced by sheltering the boilers and circulators within the thickness of the wall. Burrow of Taylor Woodrow construction Ltd. reported on providing the wire-winding system for the circumferential_prestressing loads on the vessel, thus leaving the main vessel thicknesses for the large capacity longitudinal tendons only. Such a vessel was accepted for the AGR system adopted for both the Hartlepool and Heysham power stations. In the last few years substantial progress has been made in the development of such vessels and much experimental data have been produced from both model tests and on-the-spot measurement of the prototype vessel.

5.2.2 Problems Associated with Vessels

Although the multi-cavity vessel has much to offer, it is by no means an easy structure to model. Many designers and structural analysts have tried to tackle the various problems associated with these structures. In many cases they have claimed some achievements but for some reason they have not made them public. However, most are united on the design criteria for such vessels and these are

- (a) the vessel should be designed for elastic response to all possible combinations of loads during operation;
- (b) it must show a progressive mode of failure under increasing gas pressures with large deformation to warn against impending failure; and
- (c) the vessel must have an acceptable safety margin against failure.

In order to meet the above criteria satisfactorily, one has to first validate the performance of the individual components forming such structures. The major components are

- (a) concrete,
- (b) prestressing tendons,
- (c) the liner and other penetrations, and
- (d) bonded primary and secondary reinforcements or conventional steel.

The problems associated with each one of these are enormous. For example, a certain amount of evidence must be available to demonstrate that for shortand long-term loadings (under multiaxial compressive stresses) concrete can safely withstand higher compressive stresses than are generally acceptable under uniaxial loading. For all service load conditions, including startup and shutdown, both initially and at the end of the vessel's life, the stress–strain characteristics for the concrete should take account of the age, temperature and time under load. It is also considered that limited cracking may be accepted provided due regard is paid to any significant redistribution of the stresses which may arise, due to lack of integrity and leak tightness of the liner. Where local concentrations of stress occur, due to the presence of embedments or other discontinuities in the vessel geometry, these should be assessed individually. In such cases, due regard should be paid to the effects of increased creep rates or tensile cracking on the distribution of stresses in the vessel concrete and the influence which they may have on the strains in the vessel liner.

Stresses, strains, deflections and cracking in the vessel should be analysed for all relevant combinations of mechanical and thermal loads which can arise under normal service and ultimate conditions. In such cases the prestressing forces play a great part. The tendon forces adopted in each analysis should include allowances for the most severe effects of friction and loss of prestress. A proper method of analysis together with short- and long-term experimental tests is required to design tendon systems for cyclic loads produced by gas pressures. These requirements are translated in terms of range of stress or strain cycles in the steel liner, the concrete or the other components in the nuclear islands. Beyond the elastic range, the method of assessing the ultimate behaviour of prestressing tendons and their anchorages is very important for predicting a safety margin for the vessel. This, of course, depends on the time at which the incident occurs to the vessel and the rate of increased gas pressure and whether or not the tendons are grouted. The liner undoubtedly represents a vital safety element of the vessel. Indeed, it serves the fundamental purpose of forming an impervious barrier to the cooling gas. The reactor's operability depends on its integrity. The vessel will collapse, not at the ultimate collapse pressure coincident with the failure of the prestressing tendons but at the liner failure pressure which might be lower. This would require knowledge of the topology and magnitude of the cracking on the internal face of the concrete in contact with the liner. It would be necessary, therefore, to have a clear idea of the cracking mode of the vessel for increasing pressures up to the collapse pressure. Moreover, the liner integrity is also dependent upon the performance of the liner anchorages and cooling pipes, buckling stability and fatigue in general areas, the insulation and temperature distribution.

The choice and the distribution of the conventional bonded steel reinforcement in the vessel main areas and around the penetrations are extremely important should initial cracking occur due to moisture migration and unpredictable shrinkage and creep in concrete. The bonded steel reinforcement is needed in areas where extreme stresses under serviceability conditions cannot be avoided. Above all, the progressive failure of vessels depends on the amount and the distribution of such reinforcements.

Now turning to the vessel behaviour under extreme loads, it is necessary to provide some means of limiting the effect on the vessel of an excessive rise in internal operating pressure. The magnitude and rate of a postulated pressure rise can be determined only by reference to the characteristics of the particular reactor contained. It is common practice to provide automatic venting devices, such as safety valves, for this purpose. An alternative is to design the vessel so that it is self-venting by partial structural failure. It is generally recognised that this alternative cannot be relied upon at the present method of design/construction.

It is customary and advantageous to make provision to verify the state of the vessel. This may be done by installed instrumentation and/or by periodic inservice inspection. Such measures, which are taken in a manner appropriate to the particular situation, serve to verify the vessel integrity and to confirm the design criteria. However, this does not rule out the main problem of numerically assessing such design criteria. Under any circumstances the design philosophy is based on the recognition of two or more modes in the vessel response to increasing pressure, and this cannot be met by simple experimental models.

The design objective is to ensure that a particular response to the imposed load can be achieved in each mode and that this behaviour is consistent with the appropriate operational and predetermined fault conditions.

Over a range of pressures and temperatures, including normal operating conditions, the vessel will respond to short-term variations in pressure in an elastic manner. This facilitates machine analysis of stress and strain in the vessel. Long-term stresses and strains are affected by shrinkage and creep of the concrete, relaxation of tendons and possibly fatigue. In this range of response the effects of short- and long-term behaviour can be combined to demonstrate that stresses and strains are limited to acceptable values. Beyond the elastic range the response becomes increasingly inelastic and nonlinear. The vessel would not be expected to enter this phase except under the most severe overpressure fault conditions. In this phase the vessel is stable but may experience permanent damage. It is in this phase of vessel response that some limit states occur.

The ultimate load condition, in which the vessel is incapable of sustaining any further increase of internal pressure, is a further limit state. Evaluation of the ultimate load provides a measure of the factor of safety above design conditions.

5.2.3 Vessel Layouts and Finite Element Mesh Schemes

Typical layouts of the Dungeness B, Oldbury and HTGCR vessels are given in Figs. 5.1, 5.2 and 5.3, respectively. Figures 5.4, 5.5, 5.6 and 5.7 show the finite element mesh layout of the Dungeness B, Oldbury, Hartlepool and HTGCR vessels, respectively.

The mesh layouts take into consideration the vessel penetrations, prestressing configurations and other features such as the existence of buttresses, galleries and the liner plugs and cooling pipes.

5.2.4 Design Analysis

The objective of this analysis is to demonstrate that reactor vessels will meet both the serviceability and ultimate limit state conditions, taking into consideration the gas increasing pressure.

5.2.4.1 Service Conditions

Under service conditions it is important to know the technique and precision with which the vessel geometry can be reproduced by analytical means. A number of key loading cases are given below.

- (a) Initial prestressing loads: Analysis includes losses due to friction and elastic shortening and creep; this is to see that no abnormal stresses develop in the vessel concrete.
- (b) Proof test: In this analysis the vessel is tested at the commissioning stage for changes in strains and deflection due to proof pressure loading.
- (c) Normal operating conditions: This is intended to observe the vessel operating normally under extreme loads caused by the combination of prestress, design pressure and temperature gradient together with the effects of applicable environmental loadings. This can be at an early-life or late-life operating condition.



Fig. 5.1 Dungeness B vessel prestressing layout (plan)

- (d) Start-up and shut-down conditions: These are transient and quasi-transient conditions normally imposed on the steady conditions of normal operation. Together they reproduce the extremes of the early-life shut-down/start-up cycle. The late-life conditions are also examined by changing the material properties and temperature transient conditions.
- (e) Deviations from operating conditions: A number of inaccuracies arise from the simple treatment of loading cases; these mainly concern the effect of concrete creep on stresses, unloading and cooling effects on the vessel and the allowance for low-probability loadings arising from accident or fault conditions. Analyses are required of these uncertainties.



Plan showing typical clockwise and anti-clockwise helical tendons

Fig. 5.2 (a) Principal prestressing systems (patented) (*Note*: All dimensions in imperial units; 1 ft = 0.3048 m, 1 in. = 25.4 mm). (b) Model for Oldbury nuclear power station – layout of prestressing cables and cable profiles (*Note*: All dimensions in imperial units; 1 ft = 0.3048 m, 1 in. = 25.4 mm)

5 Concrete Reactor Pressure Vessels



Fig. 5.2 (continued)



Fig. 5.3 Vertical and circumferential prestressing precast channels

5.3 Ultimate Conditions

A validity analysis is required to check the mode of failure assumed or calculated or derived from the experimental tests. This analysis should cover cases such as the intact and ruptured liner, failure of local areas, the possibility of shear failure in top caps or at cavity/wall ligaments and cracks in hot spots (areas around cooling pipes).

5.4 Methods of Analysis

Many methods are available to designers. The most common [3–7] are based on the finite element, finite difference or dynamic relaxation, lumped parameter and limit state methods. This book gives earlier the step-by-step approach of the finite element method. In some service and fault conditions it is necessary to consider the influence of external hazards and environmental conditions. Major



Fig. 5.4 Finite element idealisation of Dungeness B vessel (*Note*: For clarity certain nodes are not shown)

external hazards are seismic disturbances, wind, missiles and aircraft crashes. These hazards are considered for the case of containment vessels.

5.5 Model Testing

The purpose of a model test is to verify the methods of analysis and to provide a visible physical demonstration of the adequacy of the design requirements. As described earlier, model tests have been carried out to verify the service and ultimate state behaviour of vessels and to assess prestressing, reinforcement and liner requirements. The scale chosen for a specific model depends on the objective of the test and on the reduction in size of important vessel components. For a complete vessel a suitable scale varies from 1:25 to 1: 10, and scales of 1:25 and 1:50 have been used for the investigation of the top slab behaviour. A large number of models for shear modes of failure have been tested with

Fig. 5.5 Finite element idealization of Oldbury vessel







Fig. 5.6 Prestressed concrete cylindrical multicavity reactor vessel (HTR) – three-dimensional finite element (first rough meshing)



Fig. 5.6 (a) Prestressed concrete cylindrical multi-cavity reactor vessel, HTR, Section with tendous and precast channels. Prepared by Bangash for 3D Analysis Based on Finite Element



Fig. 5.7 Prestressed concrete cylindrical 2D finite element pressure vessel

varying geometries, materials, prestressing loads, reinforcement and penetrations. Some pneumatic tests have been carried out using gas as the pressurising medium. Most of these tests produced progressive failures with sufficient means available for detecting the elastic limit, the onset of cracking and the failure mode. Many individual tests have been carried out to assess the integrity of the liners, penetrations, closures and thermal protection systems. The finite element analysis and constitutive model discussed earlier are applied to validate the proposed analysis.

5.6 Analysis of Results

(a) Dungeness B vessel: Figures 5.8 and 5.9 show gas pressure versus vessel deflection for the top cap. Here only 12 increments of pressure are plotted. For various pressures the trend in the incremental deflection is fairly regular and no abrupt change in the deflections between any two increments has been found. Finite element analysis using three concrete numerical models, namely the four-parameter, hypoelastic and endochronic models, has been carried out. Simultaneously the model has been analysed. Figure 5.10 shows the pressure-deflection relation for two areas of the barrel wall.

The experimental tests have been carried out on two pressure vessel models, namely that of Dungeness B and Oldbury, both cylindrical with top and bottom flat caps, with different prestressing systems, indicate different modes of failure. These will be the reference models of the limit state analysis which has been developed in the text and which will be finally provided by using 3D hybrid finite element analysis under increasing gas load pressure. The Oldbury will be given a detailed assessment later on in the text.

Most of the other ultimate load analyses of cylindrical PCRV follow general procedure as commented earlier.



Fig. 5.8 Deflection versus pressure: 4.14–8.28 MN/m²



Fig. 5.9 Deflection versus pressure: 4.14–8.28 MN/m²

The reported ultimate load analysis for Oldbury and Dungeness B vessels considers each vessel to be initially broken up into an open-ended cylinder and two end caps. The mechanisms of these initial break-ups, however, appear to be in disagreement with each other. For the Oldbury analysis, the cap was separated from the barrel wall by a plastic hinge at the junction of the cap and barrel (see Fig. 5.11). A shear-compression failure mechanism, on the other hand, was adopted for the Dungeness B analysis (see Fig. 5.12). Of even greater disparity between the two analyses were the mechanisms and modes of failure experiment adopted to predict the ultimate pressure or to prove that the ultimate load factor was higher than the adopted factors for the cap and the barrel. For the barrel wall, the Oldbury analysis apparently favoured the modes of failure through the formation of a plastic hinge at the mid-height of the barrel. This mode of failure has aroused considerable criticism. In particular, the mode of failure was pointed out by Morice [8] to be kinematically incompatible in a 3D vessel without extensive cracking. It is probably valid to assume that with extensive radial cracking along the barrel wall, the barrel wall would be divided into strips of equivalent prestressed concrete beams positioned in a cylindrical array by the circumferential prestressing or equivalent hooping cables. Under such a condition, assuming that the liner remained intact (a hypothetical assumption commonly used for convenience of analysis), the pressure force





would be entirely resisted by the prestressing system. The approach adopted in such a case is to consider the ultimate load analysis of the barrel on the basis of the rupturing strength of the tendons. The ultimate load analysis for the barrel of Dungeness B in fact adopted a similar approach with the exception that the membrane action of the wall of the barrel was taken into account. The tensile strength of the membrane and tendons, with due allowance for tendon efficiency, was checked in the analysis to be greater than the circumferential force associated with an internal pressure 2.5 times the design pressure.

Zudans and Tan [9] similarly used the simpler ultimate load analysis by assessing the ultimate strength of the cylinder solely on the strength of the prestressing tendons to resist the circumferential and axial components of the pressure force. A series of tests [10-14] have been carried out successfully on individual vessel components and scaled models. Some of them are worth mentioning. To crown all, the purpose of the model test is to verify the methods of analysis and to provide a visible physical demonstration of the adequacy of the design requirements. As described earlier, model tests have been carried out to verify service and ultimate state behaviour of the vessel [126], to assess prestressing and reinforcement and liner requirements [15]. The scale chosen for a specific model did depend on the objective of the test and on the reduction in size of important vessel components. For a complete vessel a suitable scale varied from 1:25 to 1:10, scales 1:25 and 1:50 have been used for the investigation of the top slab behaviour. A large number of models for shear modes of failure have been tested [13–15] with varying geometries, materials, prestressing loads, reinforcement and penetrations. Some tests have been carried out pneumatically using gas as the pressurising medium [13-15]. Most of these tests produced progressive failures with sufficient means available for detecting the elastic limit, the onset of cracking and the failure mode. Many individual tests have been carried out to assess the integrity of the liners, penetrations, closures and thermal protection systems [142–168].

5.7 Fundamental Elements of the Concrete Pressure Vessels

As stated earlier the major fundamental elements of the vessel are

- (a) Prestressing systems
- (b) The steel liner
- (c) The bonded reinforcement
- (d) The embedded elements
- (e) The concrete

5.7.1 Prestressing Systems

The layout of the prestressing system is dependent on the shape of the vessel. The safety characteristics of the vessel can only be claimed if the integrity of the prestressing tendon and achorage system is correctly established. Several tests [1–4, 6, 8–52] have been carried out to firmly establish the strength and deformation characteristics of these systems. These include reliable tests on cables, wires, anchorages and ducts. Both short- and long-term data have been obtained in stress–strain behaviour, losses and ultimate load-carrying capacity of longitudinal, circumferential, helical and radial tendons. The latest vessels built in the UK are provided with a wire-winding system in which the wires or strands are wound under tension into a steel-lined R.C. channel either formed in the vessel walls or made of precast concrete. The band comprises a series of layers of wire/strand anchored at both ends. In this way maximum circumferential pressures are exerted within a very limited area. The advantages of this system are fully discussed [200] in the literature.

In many vessels only unbonded systems have been adopted. This choice is based on a condition that all tendons must be inspected for defects including those due to corrosion. The advantages or disadvantages of bonded and unbonded tendons are fully discussed [200] by the author.

Figures 5.1, 5.2, 5.3, 5.4 and 5.5 show the prestressing systems adopted or recommended for the several existing and future vessels. Table 5.1 shows a summary of equations in case of wire-winding for obtaining axial, circumferential, radial and boundary pressures. Details and geometry of each vessel are given in several references [13–15].

Figures 5.2, 5.3, 5.4, 5.5 and 5.6 show typical layouts of prestressing systems for existing prestressed concrete vessels.



 Table 5.1 Circumferential prestre due to wire/strand winding

5.7.2 Liner

The liner in general is to protect concrete from excessive reactor temperatures and radiation developed from inside. It carries cooling pipes circulating water at suitable intervals. The liner is anchored to the concrete by means of plugs, etc. The details are given later on under a separate caption.

5.7.3 Bonded Reinforcement

Prestressing systems would be able to avoid completely a premature failure either in the primary zones or in local areas. Under such conditions greater emphasis can be laid on the control of cracking by using good quality bonded steel.

5.7.3.1 Primary and Secondary Reinforcement

Bonded reinforcements are divided into two main categories:

- i. Primary type: they reinforce radially, circumferentially and longitudinally the walls and caps, say, of a cylindrically shaped vessel.
- ii. Secondary type: these are mainly for local areas such as zones below anchorages, buttresses or wire/strand winding channels.

5.7.3.2 Factors Affecting the Quality and Layout of Bonded Reinforcements

Elastic, ultimate load and construction analyses, if properly carried out, do give sufficient information about the quantity and disposition of bonded reinforcement. Nevertheless they are not the only means of achieving the right objective. Several factors need to be considered prior to these analyses.

The shape of the vessel, whether spherical or cylindrical with flat, haunched or curved closures, is of importance.

The type and layout of a reactor system including boilers, circulators, standpipes and control rods and penetrations required for instrumentations and other equipment can also affect the reinforcements. Substantial changes in the layout and design would be necessary if boilers, circulators and their closures were located within the walls rather that in the annular space. The same is true of the manner in which standpipes and control rods are arranged in the caps.

Prestressing system layout is another factor which is to be considered in the conventional reinforcement design. Generally prestressing systems come first. The tendons will have to go into the vessel first and their positions are determined by analyses and practical requirements. Thus the bonded steel design layout will be dependent on how a typical vessel has been stressed. The layout and hence the design would be different if the vessel were stressed with a helical wire-winding system, tendons describing horizontal arcs and which are anchored on buttresses and finally a sequential cable system.

Other factors are the anchoring of liners, positioning of cooling pipes behind the liners, charge machine tract and tendon anchorage and their protection methods.

Vessel construction methods, which include the selection of lifts and bays and existing joints in between and methods of liner erection in relation to concrete pours, must be considered.

The final factors are material inherent properties which include the choice of reinforcement, its short- and long-term behaviour in the vessel under various combinations of loads, temperature, radiation and corrosion.

5.7.3.3 Choice of Bonded Reinforcement

Generally for thick concrete vessels the choice of bonded steel in the UK is based on its high tensile strength and its interaction with the concrete. In thick sections it most certainly gives a higher bond length and an improved degree of crack control. Several tests have been carried out on GK 60 deformed bars [218] or equivalent in Eurocodes. Bond tests carried out on the 50 mm dia. bars indicate that using these reinforcements no hooks are essentially required in the PCRV. Bars used in the UK vessels are 50 and 32 mm as primary reinforcements and 18 and 12 mm as secondary reinforcements.

5.7.3.4 Procedure for the Design of Bonded Reinforcement

The step-by-step procedure is recommended for the final disposition of primary and secondary reinforcements in the PCRV. The reactor layout and the influence runs on the effects on vessel and the allowance of low probability loadings arising from accident or fault conditions. Analyses are required to cover these uncertainties.

In certain zones such as embedded items areas would create where stresses in concrete are unacceptable; reinforcement may be arranged to reduce these stresses. Due to temperature hot spots may occur in concrete zones which could be unacceptable. The stresses could be high. By providing some of these local reinforcement will reduce stresses to acceptable values in concrete. The most appropriate technique is to use advance analytical means such as finite element. Stress trajectories with and without reinforcement could be developed. These stress trajectories would determine the sizes and the zones to which these reinforcement could form shapes. The extent of such reinforcement will have bond lengths between 24 and 48 diameters of the bar. Obviously these reinforcement would be evaluated under prestressing anchorages too to avoid cracks under stressing loads.

When the final layout is obtained for these bonded reinforcement, it will be necessary to include them in the hybrid finite element analysis, either placed on solid element nodes or within the concrete body linking them to the adjacent nodes of the solid elements. Alternatively, these reinforcement can be spread within the body of the solid elements. These methods are discussed in Chapter 3 under Finite Element Analysis.

5.7.4 Embedded Elements

Based on the vessel layout, certain components may be embedded to save vessel area for the reactor. These embedded elements such as shown in





Table 5.2 can produce stress concentration in areas quiet unacceptable. They should be thoroughly analysed using numerical techniques such as finite element.

5.7.5 The Concrete

A separate analysis is given on the behaviour of the reactor concrete in this chapter.

5.8 Ultimate Conditions

A validity analysis is required to check the mode of failure assumed or calculated or derived from the experimental tests. This analysis should cover cases such as the intactness and rupture of the liner, failure of local areas, the possibility of shear failure in top caps or at cavity/wall ligaments and cracks in hot spots (areas around cooling pipes) and computer subrouteries.

Several chapters give a list of analyses required for the vessels and their components. The ultimate limit state analysis is given in detail on the bases tests and carried out and discussed in Section 5.7.

5.9 Methods of Analysis

Many methods are available to the designers. The most common are [14, 15] based on the finite element, finite difference or dynamic relaxation lumped parameter and the limit state methods. Appendices A and B give the step-by-step approach of the finite element analysis, Chapter 3 and limited state method used for these vessels is given in this chapter. In some service and fault conditions it is required to consider the influence of external hazards and environmental conditions. Major external hazards are due to seismic disturbances, wind/local generated missiles and aircraft crashes. These are fully dealt with by a number of researchers or designers [231].

5.10 Analysis of Results

The linear, non-linear and cracking analyses mentioned earlier are useful to predict the operational and overload behaviours of the vessels. Four vessels, namely the Dungeness B, Oldbury, Hartepool and Fort St. Vrain have been analysed. Figures 5.13, 5.14, 5.15, 5.16, 5.17, 5.18, 5.19 and 5.20 give a summary of the load displacement relations, modes of cracking and failure and the safety margins. Cracks predicted by the finite element and limit state

Fig. 5.13 Oldbury prestressed concrete reactor pressure vessel



Fig. 5.14 Dungeness B prestressed concrete reactor vessel



Fig. 5.15 Hartlepool prestressed concrete reactor pressure vessel



Fig. 5.16 Fort St. Vrain prestressed concrete reactor vessel ($P_{\rm G} = 18 \text{ HN/m}^2$)



Fig. 5.17 Deflected shape. Sides of model - ulimate run

analyses for these vessels are compared with each other and wherever possible with those predicted by experimental tests. The comparative study shows that theoretical and experimental results are in good agreement.

In two such vessels conditions under normal operations, 2.5 P_{GD} and failure conditions are particularly examined – principal stresses are examined at suitable pressure increments right up to 2.5 P_{GD} and beyond. The complete plug failure occurred at 4:1 P_{GD} (13.5 MN/m²) and the top cap (of the Dungeness B) and the wall. It was the shear compression failure. At 2% ultimate strain in the tendons, the possible failure of longitudinal tendons, a group of circumferential tendons did fail. From this model testing, central core plug failure at the top cap (shear compression type) occurred at 13.8 MN/m². Two vertical tendons failed at 10.2 MN/m².

It is concluded that the failure of this vessel has occurred owing to the complete removal of the central core or plug in the top cap at a pressure



Fig. 5.18 Horizontal deflection of wall (ultimate pressure) - Oldbury vessel



Fig. 5.19 Vertical deflection of top cap (ultimate pressure) – Oldbury vessel

around four times the design pressure. The FE and the M analyses are in good agreement with each other and with most of the published data from the experimental tests. Throughout the vessel there is no premature failure of the liner.



Fig. 5.20 Presure-deflection curve of Oldbury vessel [418: experimental]

5.10.1 Oldbury Vessel

For the model test of the Oldbury vessel, gas pressure versus deflections is plotted in Figs. 5.18 and 5.19. The results from finite element analysis have been plotted for comparison in the same figures. Because of great variations in tendon layout, the pressure versus deflection curves are given but at a pressure of 4.825 MN/m^2 ($1.815P_{\text{GD}}$). This must have been produced even earlier in the model, since such a crack cannot suddenly appear at such a marginal pressure difference of $0.065P_{\text{GD}}$. The results from FE clearly indicate that there is a plastic zone appearing at the equator.

Raising the pressure to 5.32 MN/m^2 ($1.995P_{GD}$) FE indicates that the vessel top cap plastic zone has been abruptly increased and additional flexural cracks have emerged. The plastic zone in this case has reached the areas surrounding the central hole in the standpipe area and the prestressing galleries. Model tests show similar effects in the top cap. The results from M give two surface flexural cracks and various positions or locations. Therefore each curve takes into account the contribution it has received from the exact position of tendons, conventional steel and the liner in the original layout. In order to test these results, some of them are plotted in Fig. 5.20 along with those from the model tests (four tests) carried out by Eddie et al. and others. Both the horizontal and vertical deflections are in good agreement. However, in Fig. 5.21 although the computed axial strains are in good agreement with those measured on the prototype, the hoop or circumferential strains are wide apart. The only explanation that can be offered is the difference between the exact chosen tendon layout of the vessel parameters and that of the prototype.



Fig. 5.21 Hoop and axial strains at wall mid-height – Oldbury reactor vessel (conditions at ultimate pressure) (——, finite (five-parameter): ——O—, experimental)

The percentage difference is still within 5-8%. A further comparison is given in Fig. 5.21 which is based on the monitoring of the vessel's performance for a period of 10 years.

Figures 5.22 and 5.23 show plots for various principal stresses. It is interesting to note that in Fig. 5.24 the effect of removal of cracked concrete at 1.81 times the design pressure is shown. Figures 5.25 and 5.26 show the principal stresses at 2.5 times design pressure. No cracks have been observed for a pressure range of $2.66-3.75 \text{ MN/m}^2$. At a pressure of 3.99 MN/m^2 ($1.455P_{GD}$) a plastic zone in the top cap centre has been predicted by FE. Both FE and M show a plastic zone and a minor crack at the top haunch. Radial hair cracks together with a plastic zone have also been predicted by FE. However, M assumes a crack width at the equator and finally proves that it is the only crack that exists in the wall at this pressure.



Fig. 5.22 (a) Wall horizontal and vertical deflections. (b) Top slab horizontal and vertical deflections. (c) Circumferential stresses – operating conditions only (finite element analysis)

At a pressure of 4.665 MN/m^2 (1.75 P_{GD}), a wider and deeper plastic zone appeared (mark 6) in the top cap. It is interesting to note that the top haunch plastic zone has also been increased. In addition, a minor plastic zone has been predicted by FE at the bottom cap haunch. Moreover, at the upper part of the side wall a wider radial crack has occurred and this crack has also been confirmed by the model tests.

Both top and bottom haunch plastic zones of this vessel predicted by FE are fairly large. Here there is some disagreement between FE and M on the type of crack. The top haunch M results show both flexural and premature shear cracks. On the other hand, the results from FE clearly indicate the possibility of cracks caused by the principal tensile stresses caused by shear. However, there is an agreement between the two analyses on the initiation of flexural cracks in the bottom cap haunch. The magnitude of these cracks is not greater than 0.007 mm. Practically there is no change in the flexural crack. The bottom cap has an enlarged plastic zone.

Reports suggest that a horizontal-cum-radial crack has appeared above the circulator penetration, but the published data have not confirmed it. In the





barrel wall M shows flexural cracks in both radial and circumferential directions. Examination shows that cracks in radial directions do exist at pressures between 4.664 and 5.32 MN/m^2 . They have been superimposed for comparison. The results obtained from FE show plastic zones and surface cracks. Obviously there is a slight discrepancy. It seems that FE does not agree with M up to a pressure of 5.32 MN/m^2 for the creation of plastic zones or surface cracks. The difference is in the modelling of the layouts. No test data are available for this vessel or any other cylindrical vessels for such cracks appearing at 1.995 times the design pressure. However, there seems to be some agreement in this area at pressures above 5.32 MN/m^2 .

Carrying on in the same way, many failure zones have been developed at additional incremental pressures. As shown in Fig. 5.13 at $P_{\rm G}$, ultimate = 1197 MN/m² (4.5 $P_{\rm GD}$), both model tests and FE results are in agreement. The vessel top cap and top corner have been separated.

This failure mechanism is different from that predicted for the Dungeness B vessel, although they both have an identical shape and reactor system layout but with different prestressing system and gas design pressure.



5.10.2 High-Temperature Gas-Cooled Reactor Vessel (HTGCR)

Figure 5.22 and 5.23 show gas pressure versus deflection, and Figs. 5.24 and 5.25 show principal stresses at normal operation. Figures 5.26 and 5.27 show principal stresses at 2.5 times the design pressure. Although this vessel layout is different in many respects to that of the Hartlepool reactor, the stress flow in many areas is identical. The stress concentrations around the boilers and at the junction between the caps and the walls are similar in both cases. However, the quantities do differ. It is because of these and some dissimilar stress contours that the final failure modes in both vessels differ.

Figures 5.6 and 5.7 show 3D and 2D finite element mesh generation schemes of a prestressed concrete vessel designed for a high-temperature gas-cooled reactor. Both internal and external loads have been computed in accordance with the method given in Chapter 3. The program CREEP, which



Fig. 5.25 Minimum principal stress pressurisation after longterm shut-down showing effect of removal of cracked concrete (A)

Fig. 5.26 Maximam principal stresses at 2.5 P_{GD}





is a part of the program ISOPAR, gives results for when the vessel undergoes the effect of creep. First a normal operation condition (prestress + pressure + temperature) is considered. This vessel is analysed with and without creep. The axial, radial and circumferential stresses have been computed. The influence of creep when the Young's modulus is constant or variable is considerable. In some local areas, because of creep the stresses change significantly with passage of time. Figure 5.28 shows stresses at the top cap with and without creep for up to 20 years. Figure 5.28 shows the behaviour of the vessel under operating and thermal shut-down conditions with and without the influence of creep.

The vessel is then taken to elasto-plastic and cracking conditions. As discussed later on, the relationships between gas load, prestressing strains, and deflections and cracks with and without the influence of creep have been established. These results (Fig. 5.29) show that where the influence of creep is not considered, the load-carrying capacity is overestimated by as much as 25%. With creep, considerable changes were discovered in the cracking pattern of the vessel and the overstress conditions in local areas (standpipes and boiler/circulator penetrations).



Fig. 5.29 Maximum principal stresses at normal operation


Fig. 5.30 Pressure-deflection curve for top cap of HTGCR reactor vessel (— Experimental: —O—, FE (four-parameter); —•—, FE (five-parameter))

Ahmad has idealised the same vessel, as shown in Fig. 5.30. He has used the vessel bonded and unbonded and produced deformations (Figs. 5.30, 5.31, 5.32 and 5.33) for normal operation and for 40 years of creep. He has also produced a graph (Fig. 5.34) showing deformation for this vessel at various pressures. He has included creep in his analysis. This vessel has also been considered for elasto-plastic and cracking effects by Bangash. The deformation of the vessel at the cracking stage under the influence of creep and with the steel liner anchored to concrete is shown in Fig. 5.35.

The stress trajectories at normal operation and at 2.5 times design pressures can be obtained in the same manner as for vessels discussed previously. The vessel design pressure $P_{\rm GD}$ here is 5.68 MN/m². At a pressure of 7.48 MN/m² (1.315 $P_{\rm GD}$), this vessel's behaviour (Fig. 5.36) is identical to that of the Hartle-pool vessel. The only change is the plastic zone developed around the gas inlet duct under mark 6.

At a pressure of 9.28 MN/m^2 (1.635 P_{GD}) the behaviour of this vessel (Fig. 5.37) in most zones is identical to that of the Hartlepool vessel [423, papers H3/5, H5/3] and others. When the pressure was raised to 6 MN/m^2 the only difference is in the position of cracks (marks 11, 12 and 13) at the top haunch and the extent of the plastic zones (marks 7, 14, 20, 21 and 22). The crack sizes have not been predicted in the top cap. The bottom cap has been affected only at the bottom haunch. Both FE and M are in agreement in most areas, as shown in Fig. 5.37. Raising the pressure to 11.08 MN/m^2 (1.95 P_{GD}) there is a significant difference in the behaviour of this vessel (Fig. 5.38).



Fig. 5.31 Minimum principal stresses at normal operation

The HTGCR vessel failure mode is moving more towards flexural criteria than shear criteria. The initiation and propagation of cracks and their positions are very different. The reason is purely the dominant role that the barrel wall/ cap slenderness ratio has played in producing flexural cracks. In plan around the boiler and circulator penetrations and in the standpipe area, most of the plastic zones are identical.

At a pressure of 12.88 MN/m² (2.24 P_{GD}) the top cap mode (marks 46–53) is given in Fig. 5.39.

There is a similarity in the development of plastic zones between the two vessels in the bottom caps. In plan, the plastic patch zones are very similar between these two vessels. The only difference is the extent of cracks developed at the equator (mark 49) by FE. At this pressure in the top cap the plug failure (mark 60) is imminent. It is interesting to note that the crack sizes are identical in these zones. Another difference is in the sudden appearance of a plastic zone just above the gas inlet (mark 55) and a flexural crack in the circumferential direction in the top corner (mark 54) at the outside of the boiler penetration. There is also a slight shift in the position of the crack (mark 57) around the circulator. The crack widths have reached about 0.2 mm



Fig. 5.32 Stresses through top cap - at operating temperature and shut-down

in most places. In many places strains in the tendons and in the bands do not exceed 0.009.

Raising the pressure to 14.68 MN/m^2 (2.258 P_{GD}), sufficient flexural cracking in the barrel wall (Fig. 5.40) has occurred.

The nearest case that can be compared is the behaviour of the Hartlepool vessel under $2.5P_{GD}$. In the top cap, plastic zones have identical locations.

However, in the HTGCR vessel no internal cracking has been predicted by LS around the boiler and the circulator penetrations.

In plan, the plastic zones are quite similar. There is a change in the plastic zone around the boiler penetration between sections (3)–(3) and (4)–(4). In the top cap a plug failure under mark 69 has been initiated. The strain and crack widths in most places do not exceed 0.01% and 30 mm.

At a pressure of 16.48 MN/m^2 (2.81 P_{GD}) the behaviour of this vessel (Fig. 5.41) is identical in many respects to the behaviour of the Hartlepool vessel [418–431] for 2.82 P_{GD} . In plan, the cracks and plastic zones are very



Fig. 5.33 Maximum principal stresses at $2P_{GD}$



Fig. 5.34 Minimum principal stresses at $2P_{GD}$



Fig. 5.35 Stresses in top cap showing inflection of shut-down

similar in both cases. In both the top and bottom caps flexural cracks have been extended in depth. Not enough change is visible of the plug failure line in the top cap. In addition, the barrel (Figs. 5.41 and 5.42) wall cracks and the haunch cracks have advanced considerably. These flexural cracks are more pronounced than in the case of the Hartlepool vessel.

The circumferential prestressing bands have reached the ultimate strain of 1.5% and the cracks in *most places* are around 50 mm. When the pressure is raised to 18.28 MN/m^2 (3.2 IP_{GD}), Fig. 5.43a shows the positions of plastic zones between sections (1)–(1) and (2)–(2).

Additional flexural cracks have appeared in the top cap. It seems that the influence of cracks due to shear compression and plug failure has been minimised. At the equator (marks 115 and 116) a larger plastic *zone* has been



Fig. 5.36 Games point locations in the reactor vessel [262] (all dimensions in num)



Fig. 5.37 Deformations under normal operation and after 40 years of creep [262] – vessel type, perfectly bonded



Fig. 5.38 Deformations under normal operation and after 40 years of creep [262] – vessel type, bonded (with Ahmlink element)



Fig. 5.39 Deformations under normal operation and after 40 years of creep $\left[262\right]-vessel$ type, unbounded



Fig. 5.40 Deformed shapes at various pressures [262, 749] – vessel type, bonded vessel with Ahmlink element (—, —, deformed shape at 3.0; —, deformed shape at 3.3; —, deformed shape at 3.5; —, FE (four-parameter, Bangash); —• —, FE (five-parameter, Bangash))



Fig. 5.41 High-temperature gas-cooled reactor pressure vessel ($P_{\rm G}=7.48~{\rm MN/m^2}$) (see Fig. IX.118a for key)



Fig. 5.42 High-temperature gas-cooled reactor pressure vessel ($P_G = 11.08 \text{ MN/m}_2$) (see Fig. IX.118a for key)



Fig. 5.43 High-temperature gas-cooled reactor pressure vessel ($P_{\rm G}=9.28~{\rm MN/m^2}$) (see Fig. IX.118a for key)



Fig. 5.44 High-temperature gas-cooled reactor pressure vessel ($P_G = 12.88 \text{ MN/m}^2$) (see Fig. IX.118a for key)



Fig. 5.45 High-temperature gas-cooled reactor pressure vessel ($P_G = 14.68 \text{ MN/m}^2$) (see Fig. IX.118a for key)



Fig. 5.46 High-temperature gas-cooled reactor pressure vessel ($P_{\rm G}$ = 18.28 MN/m²) (see Fig. IX.118a for key)



Fig. 5.47 High-temperature gas-cooled reactor pressure vessel ($P_G = 16.48 \text{ MN/m}^2$) (see Fig. IX.118a for key)



Fig. 5.48 High-temperature gas-cooled reactor pressure vessel ($P_{\rm G} = 20.08 \text{ MN/m}^2$) (see Fig. IX.118a for key)



Fig. 5.49 High-temperature gas-cooled reactor pressure vessel and deflections

created. The bottom haunch crack (mark 117) position is another difference in the behaviour of these two vessels. The plastic zones also differ from those in the Hartlepool vessel. Their shapes and positions and crack sizes do not match. This again is due to the difference in the dominant role being played by the span/depth ratios. Longitudinal prestressing has failed and the crack sizes are approximately over 90 mm. Bonded reinforcement has yielded. Although there is sufficient yielding of the liner, it still has not failed.

At a pressure of 20.08 MN/m^2 (3.55 P_{GD}) both the top cap and the barrel wall have failed in flexure one after another. All cracks around the boilers and circulators have widened.

Circumferential cracks around the top haunch have joined the longitudinal cracks. The bottom cap has cracked but the various pieces are held together.

It is concluded that the vessel has failed due to the failure of a strand band at a pressure of $3.21P_{GD}$ and enough cracks have been produced in the top cap to define a premature fiexural failure intervening in the shear failure in the



Fig. 5.50 Dungeness B type vessel – temperature distribution

top cap. Fllexural failure has also occurred at several places in the barrel wall. Figure 5.43a,b gives additional cases for failure modes but these are not governing cases. Figure 5.44 gives the deflection and cracking history of this vessel.

5.11 Thermal Analysis of Vessels

Thermal analysis has been carried out for all vessels noted in this chapter. Figures 5.50, 5.51, 5.52 and 5.53 give the result of temperature distributions for the vessels. Where thermal loads are to be included in the overall analysis they are computed from these figures and are put at the respective nodes of the elements as concentrated loads or patch loads. Alternatively strains are evaluated from these temperatures and they are included in the finite element formulations as initial strains. Stress trajectories can be drawn for the temperature-only case on the lines given for vessels in normal operation – cases which in fact include temperature effects.

5.12 Concrete Failure Theories

Several concrete theories exist which can easily be simulated into the overall various failure stages of the vessels. A summary of the important ones are given in Table 5.3 for detailed derivations and applications, a reference is made to the authors' following books:



Fig. 5.51 Oldbury vessel – temperature distribution



Fig. 5.52 Temperature and Young's moduli at equator - HTGCR vessel

Manual of Numerical Methods in Concrete

"Modeling and Applications Validity by Experimental and Site Monitoring Data", Thomas Telford, London (1999).

Tables 5.4, 5.5 and 5.6 give derivations of equations for, respectively, fourparameter (OTTOSON) model, five-parameter model, Bulk shear moduli model and Endochronic cracking model, which have been used in the existing vessels to present the concrete failure. Reference is made to above reference by the author on other failure criteria including bulk and shear moduli and Endochronic cracking models.



5.13 The Contribution Made by the Steel Liner

Table 5.5 gives a brief on the analytical formulation of the steel liner which can easily be associated with the overall numerical modelling of the PCPV including the ultimate load and collapse conditions.

5.14 Prestressing Systems

Appendix C gives data on various prestressing systems.

5.15 Limit State Formulation

A reference is made to the future models (Fig. 5.11 for Oldbury and Fig. 5.12 for Dungeness); they definitely form the background for the development of the Limit State Analysis.

Several failure criteria [10–15] have been established from the experimental tests. Flexural failure is reported in the wall of the vessel. In the top cap both



Fig. 5.54 Vessel and its parameters

flexural and plug failures have been reported. The central plug normally consists of a perforated zone due to the location control rods or standpipes. When the resistance of the compressive area in this region is generally reduced, the outside perimeter of the standpipes develops a circumferential plane of weakness. Under gas-increasing pressure a complete punched-out failure of the central core of the cap has occurred. This is due to the force caused by internal gas pressure 1. Krupfer and Rusch $f(\sigma_{ij}) - A = 0 = \tau_{ocl} + Bp - A$ where $\tau_{oct} = (13\sigma_{ij}\sigma_{ij} - p^2)^{\frac{1}{3}} \quad i, j = 1, 2, 3$ $p = 13\sigma_{KK} \qquad K = 1, 2, 3$ $\frac{\partial f}{\partial \sigma_{ij}} = \sigma_{ij}(B\tau_{oct} - P)\delta_{ij}$

2. Ottosen Four-parameter model

 $f[(J_1, I_2)\cos 3\theta] = \frac{AI_2}{\sigma_y^2} + \lambda \frac{\sqrt{I_2}}{\sigma_y} + B \frac{J_1}{\sigma_y} - 1 = 0$

3. Argyris et al.

$$f\left(A\frac{J_1}{\sigma_c} + \left(B - C\cos 3\theta_c\right)\frac{\sqrt{J_2}}{\sigma_c} - 1\right) = 0$$

4. William et al.

(a)
$$(I_1, I_2, I_3) = 0$$
 $I_1 = \sigma_1 + \sigma_2 + \sigma_3; I_2 = \sigma_1 \sigma_2 + \sigma_2 \sigma_3 + \sigma_3 \sigma_1$
 $I_3 = \sigma_1 \sigma_2 \sigma_3$
(b) $\left(I\frac{1}{2_p}, I\frac{1}{2_c}\right) = 0$ $I_{2,c} = A_{01} + A_{11}J_1 + A_{22}J_1^2/\sigma_c$ tensile $\theta_c = 0$
 $I_{2,c} = B_{01} + B_{11}J_1 + B_{22}J_1^2/\sigma_i$ comp $\theta_i = 60^{\circ}$

5. Mohr's equations

$$\begin{split} f(z,r,\delta) &= 0 \qquad z = \frac{1}{\sqrt{3}} (\sigma_1 + \sigma_2 + \sigma_3) \\ &\qquad r = \frac{1}{\sqrt{3}} \sqrt{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_1 - \sigma_3)^2} \\ \cos \delta &= \sigma_1 + \sigma_2 - 2\sigma_3 / \sqrt{2} \sqrt{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_1 + \sigma_3)^2} \\ &\qquad \tau_{ect} = \frac{1}{\sqrt{3}} \gamma; \quad \sigma_0 = \frac{1}{\sqrt{3}} . z \end{split}$$

6. Launay et al.

 $f(\sigma^{**}-1)=0$

where

$$\begin{split} \sigma^{**} &= P^2 \left[\frac{\cos^2 \frac{3}{2} \theta_c}{P_c / J_1^2 / 3} + \frac{\sin^2 \frac{3}{2} \theta_c}{P_r J_1^2 / 3} \right]; P = \sqrt{2} P_c P_t / \sqrt{(P_t^2 + P_c^2) + (P_t^2 - P_c^2)} \cos 3\theta_c \\ \cos 3\theta_c &= \frac{3\sqrt{3}}{2} [I_3 / (I_2)^{\frac{3}{2}}]; I_3 = \frac{(\sigma_1^3 + \sigma_2^3 + \sigma_3^3)}{3} \\ 7. \text{ Bangash Y} \\ \text{Hypo-elastic theory} \\ f(\{\sigma\}, \{\varepsilon\}, \{\dot{\sigma}\}, \{\varepsilon\}) = 0 \\ d\sigma_{ij} = D_r(\sigma_{ij}) d\varepsilon_{Kl} \qquad \delta = \text{Kronecker delta} \\ D_r = \text{ Material property tensor} \\ &= (A_0 + A_{11}\sigma_{rr})\delta_{ij}\delta Kt + 12(A_{02} - 2A_{11}\sigma_{rr})(\delta_{iK}\delta_{ji} - \delta_{jK} - \delta_{il}) \\ &+ A_{13}(\sigma_{ij}\delta_{Kl} + \sigma_{Kl}\delta_{ij}) + 12A_{14}(\sigma_{jK}\delta_{il} + \sigma_{jl}\delta_{Kl} + \sigma_{il}\delta_{ij}) \\ \end{split}$$

 $d\sigma_{ij} = A_{01}\dot{\varepsilon}_{kk}\delta_{ij} + A_{02}\dot{\varepsilon}_{ij} + A_{11}\dot{\varepsilon}_{kk}\delta_{ij}$ $-2A_{11}\sigma_{kk}\dot{\varepsilon}_{ij}+A_{13}(\sigma_{ij}\dot{\varepsilon}_{kk}+\sigma_{k1}\dot{\varepsilon}_{k1}\delta_{ij})$ $+ A_{14}(\sigma_{ik}\dot{\varepsilon}_{ik} + \sigma_{ik}\dot{\varepsilon}_{ik})$

where δ 's are Kroneckler deltas and A's are various hydrostatic constants to be determined by experiments

 $K_{11} = A_{01} + A_{02} - A_{11}J_1 + 2(A_{13} + A_{14})\sigma_1$ K_{22} , K_{33} have all the terms of K_{11} except σ_1 is changed to σ_2 for K_{22} and σ_3 for K_{33} $\begin{aligned} & K_{44} = (A_{02} - 2A_{11}J_1) + A_{14}(J_1 - \sigma_1) \\ & K_{55} = (A_{02} - 2A_{11}J_1) + A_{14}(J_1 - \sigma_2) \\ & K_{66} = (A_{02} - 2A_{11}J_1) + A_{14}(J_1 - \sigma_3) \\ & K_{12} = (A_{01} + A_{11}J_1) + A_{13}(\sigma_1 + \sigma_2) = R + A_{13}(\sigma_1 + \sigma_2) \end{aligned}$ $K_{13} = R + A_{13}(\sigma_1 + \sigma_3)$ $K_{23} = R + A_{13}(\sigma_2 + \sigma_3)$ $K_{21} = R + A_{13}(\sigma_2 + \sigma_1)$ where $R = \dot{A}_{01} + A_{11}J_1$ $K_{31} = R + A_{13}(\sigma_3 + \sigma_1)$ $K_{32} = R + A_{13}(\sigma_3 + \sigma_2)$

The determinant in () after expansion leads to

$$\begin{bmatrix} (A_{02} - 2A_{11}j_1) \left\{ -3A_{13}^2 \left(2J_2 - \frac{J^3}{3} \right) + [3A_{01} + A_{02} + (A_{11} + 2A_{13})J_1] \right\} \\ + 2A_{14} \left\{ (A_{02} - 2A_{11}J_1)^2 J_1 + 2(A_{02} - 2A_{11}J_1)J_1(A_{01} + A_{11}J_1) \\ + (2J_{1/3}^2 - (J_2 - J_{1/3}^3))[A_{14}(A_{01} + A_{11}J_1) + (A_{02} + 2A_{11}J_1)(A_{13} + 2A_{14})] \\ + \left(\left(J_{3/3} - J_1 \left(J_2 - \frac{J_1^3}{3} \right) \right) \right) / 2 \right) [2A_{14} + (6A_{13} + 2A_{14}) + 6A_{13}^2] \\ - A_{13}^2 [J_{1/3}^3 + J_1(J_2 - J_{1/3}^3) - J_3] \right\} \right] \times [(A_{02} - 2A_{11}J_1)A_{14}(J_1 - \sigma_1)] \\ \times [(A_{02} - 2A_{14}J_1) + A_{14}(J_1 - \sigma_2)][(A_{02} - 2A_{11}J_1) + A_{14}(J_1 - \sigma_3)] = 0 \\ \text{for } \sigma_3 > \sigma_1 \text{ or } \sigma_2 \\ \end{bmatrix}$$

 $A_{01} + \frac{1}{2}A_{02} + (2A_{13} + A_{14})$

The inclination of the strain path for $d\varepsilon$ is given as

$$dx' = \tan^{-1} \frac{1}{\sqrt{3}} \frac{(dep_1 - dep_2) + dep_1 - dep_3)}{(dep_2 - dep_3)}$$

7. Sulkand shear moduli noddle

8. Endochronic cracking model

9. Fifth para model

Table 5.4 Four-parameter model

An analytical failure model in which four parameters are included has been developed by Ottoson. This failure surface is described already. The same chain rule of partial differentiation is applied. The gradient $\{\partial f/\partial \sigma\}$ is given by Bangash:

$$\begin{aligned} c &= \frac{\partial f}{\partial \sigma} = \frac{\partial f}{\partial l_{1}} \frac{\partial l_{1}}{\partial \sigma} + \frac{\partial f}{\partial l_{2}} \frac{\partial J_{2}}{\partial \sigma} + \frac{\partial f}{\partial \cos 3\theta} \frac{\partial \cos 3\theta}{\partial \sigma} \\ a_{1}c_{1} + a_{2}c_{2} + a_{3}c_{3} \qquad (5.1) \\ a_{1} &= \frac{\partial f}{\partial l_{2}} = \frac{B}{f_{c}^{l}} \\ a_{2} &= \frac{\partial f}{\partial l_{2}} = \frac{\partial}{\partial l_{2}} \frac{AJ_{2}}{f_{c}^{2}} + \frac{\partial}{\partial l_{2}} \frac{\lambda J_{2}^{1/2}}{f_{c}^{2}} = \frac{A}{f_{c}^{l}} + \frac{\partial}{\partial l_{2}} \frac{\lambda J_{1}^{1/2}}{f_{c}^{2}} \\ \frac{\partial}{\partial J_{2}} \frac{\lambda J_{2}^{1/2}}{f_{c}^{2}} &= \frac{\lambda}{f_{c}} \frac{1}{2} J^{-1/2} + \frac{J^{1/2}}{f_{c}^{l}} \frac{\partial(\lambda)}{\partial J_{2}} \qquad (5.2) \\ \frac{\partial(\lambda)}{\partial J_{2}} &= \frac{\partial}{\partial J_{2}} \left\{ K_{1} \cos \left[\frac{1}{3} \cos^{-1} \left(K \frac{3\sqrt{3}}{2} \frac{\sqrt{3}}{3/J_{2}^{2}} \right) \right] \right\} \qquad (5.3) \\ \text{where} \\ \cos 3\theta &\leq 0 = -K_{1} \sin(P) \frac{1}{3} \frac{-1}{\sqrt{1-t^{2}}} K_{2} \left(\frac{3}{2} \right) \sqrt{3} J_{3} \left(-\frac{3}{2} \right) J_{2}^{-6/2} \\ -K_{1} \sin(P) \frac{1}{3J} \left(K_{2} \frac{3\sqrt{3}}{2} \frac{\sqrt{3}}{3/J_{2}^{2}} \right) \frac{1}{\sqrt{1-t^{2}}} \left(+\frac{3}{2} \right) \\ -K_{1} \frac{t}{\sqrt{1-t^{2}}} \sin(P) \frac{1}{2J} &= -\frac{K_{1}}{2J} \frac{t}{\sqrt{1-t^{2}}} \sin(P) \\ t &= K_{2} \frac{3\sqrt{3}}{2} \frac{J_{3}}{3/J_{2}^{2}} \\ \frac{\partial(\lambda)}{\partial J_{2}} &= \frac{\partial}{\partial J_{2}} \left\{ K_{1} \cos \left[\frac{\pi}{3} - \frac{1}{3} \cos^{-1} \left(K_{2} \frac{3\sqrt{3}}{2} \frac{J_{3}}{3/J_{2}^{2}} \right) \right] \right\} \cos \theta \leq 0 \\ &= K_{1} (-\sin P) \left[-\frac{1}{3} \frac{(-1)}{\sqrt{1-t^{2}}} \left(-K_{2} \frac{3\sqrt{3}}{2} J_{3} \right) \left(-\frac{3}{2} \right) J_{2}^{-6/2} \right] \\ &= -\frac{K_{1}}{T} (-\sin P) \left[\frac{1}{3} \frac{t}{\sqrt{1-t^{2}}} \left(-\frac{3}{2} \right) \right] \frac{-K}{2J} (\sin P) \frac{t}{\sqrt{1-t^{2}}} \quad (5.4) \\ \text{From this equation} \\ a_{2} &= \frac{A}{f_{c}^{2}} + \frac{1}{J_{2}^{1/2} f_{c}^{2}} \left\{ \lambda - K_{1} \sin \left[\frac{1}{3} \cos^{-1} \left(K_{2} \frac{3\sqrt{3}}{2} \frac{J_{3}}{J_{2}^{3}} \right) \right] \right\}$$

$$\frac{A}{f_{c}^{2}} - \frac{1}{2f_{2}^{1/2}f_{c}^{t}} \left\{ \lambda - K_{1} \sin\left[\frac{\pi}{3}\frac{1}{3}\cos^{-1}\left(K_{2}\frac{3\sqrt{3}}{2}\frac{J_{3}}{J_{2}^{3/2}}\right)\right] \frac{t}{\sqrt{1-t^{2}}} \right\}$$
(5.5)

$$a_{3} = \frac{\partial}{\partial\cos 3\phi} \left(\lambda \frac{f_{2}^{1/2}}{f_{c}}\right) \quad \cos 3\theta \ge 0 \quad (5.6)$$

$$\frac{f_{2}^{1/2}}{f_{c}}\frac{1}{3}K_{1} \sin\left[\frac{1}{3}\cos^{-1}(K_{2}\cos 3\theta)\right] \frac{K_{2}}{\sqrt{1-t^{2}}}$$

$$= \frac{1}{3}\frac{K_{1}K_{2}J_{2}^{1/2}}{3\sqrt{t}-t^{2}f_{c}}\sin\left[\frac{1}{3}\cos^{-1}(K_{2}\cos 3\theta)\right] \quad \cos \theta \ge 0 \quad (5.7)$$

$$a_{3} = \frac{K_{1}K_{2}J_{2}^{1/2}}{3\sqrt{1-t^{2}f_{c}}}\sin\left[\frac{\pi}{3} - \frac{1}{3}\cos^{-1}(-K_{2}\cos 3\theta)\right]\cos 3\theta \ge 0$$

where $t = K_{2}\cos 3\theta$

$$J_{2} = \left[\frac{1}{2}(S_{x}^{2} + S_{y}^{2} + S_{z}^{2}) + \tau_{xy}^{2} + \tau_{yz}^{2} + \tau_{zx}^{2}\right]$$

The values of c_{1}, c_{2}, c_{3} are as follows:

$$\begin{split} C_1 &= \frac{\partial I_1}{\partial [\sigma]} = \begin{cases} 1\\ 1\\ 1\\ 0\\ 0\\ 0 \end{cases} \\ C_2 &= \frac{\partial I_2}{\partial [\sigma]} = \frac{\partial I_2}{\partial S_2} \frac{\partial S_2}{\partial [\sigma]} + \frac{\partial I_2}{\partial S_2} \frac{\partial S_2}{\partial [\sigma]} + \frac{\partial I_2}{\partial S_2} \frac{\partial T_2}{\partial [\sigma]} + \frac{\partial I_2}{\partial T_{zz}} \frac{\partial T_{zy}}{\partial [\sigma]} + 22 \begin{cases} 0\\ 0\\ 0\\ 0\\ 0\\ 0 \end{cases} \\ (5.8) \end{cases} \\ \text{or} \\ C_2 &= \begin{cases} \frac{1}{3} (2S_x - S_y - S_z) \\ \frac{1}{3} (2S_x - S_x - S_y) \\ 2T_{yy} \\ 2T_{yy} \\ 2T_{yy} \\ 2T_{yy} \end{cases} \\ (5.9) \\ 2T_{yy} \\ 2T_{yy} \\ 2T_{yz} \\ 2T_{zx} \end{cases} \\ (5.9) \\ C_3 &= \frac{\cos 3\theta}{\partial J_3} = \frac{\cos 3\theta}{\partial J_3} \frac{\partial I_3}{\partial [\sigma]} + \frac{\cos 3\theta}{\partial J_2} \frac{\partial I_3}{\partial [\sigma]} \\ (5.11) \\ \text{From Eq. (5.11)} \\ \text{From Eq. (5.11)} \\ \frac{\cos 3\theta}{\partial J_3} = \frac{3J_2^{3}}{2J_2^{3/2}} \frac{\cos 3\theta}{\partial J_2} = \left(\frac{3J_2^{3}}{2}J_3\right) \left(\frac{-3/2}{J_2^{3/2}}\right) = -\frac{9}{4} \sqrt{3} \frac{J_2^{5/2}}{J_2^{5/2}} \\ (5.12) \\ \text{Now} \\ J_3 &= \left[S_x S_y S_z + 2\tau_{xy} \tau_{yz} \tau_{zx} - S_y \tau_{xy}^2 - S_y \tau_{yz}^2 - S_z \tau_{zx}^2 \right] \\ \frac{\partial I_3}{\partial S_x} = \frac{\partial I_3}{\partial \sigma} + \frac{\partial J_3}{\partial S_y} \frac{\partial S_y}{\partial \sigma} + \frac{\partial J_3}{\partial S_y} \frac{\partial S_y}{\partial \sigma} + \frac{\partial J_3}{\partial S_y} \frac{\partial T_y}{\partial \sigma} \\ (5.14) \\ \frac{\partial J_3}{\partial S_x} = \frac{1}{3} \left(\frac{-1}{-1} \\ 0\\ 0\\ 0 \\ 0 \\ \end{array} \right), \quad \frac{\partial S_y}{\partial \sigma} &= \frac{1}{3} \left(\frac{-1}{2} \\ -1\\ 0\\ 0\\ 0 \\ 0 \\ \end{array} \right), \quad \frac{\partial S_y}{\partial \sigma} &= \frac{1}{3} \left(\frac{-1}{-1} \\ -1\\ 0\\ 0\\ 0 \\ 0 \\ \end{array} \right), \quad \frac{\partial I_3}{\partial T_y} &= 2\tau_{xy} \tau_{zx} - 2S_z \tau_{xy}, \\ \frac{\partial I_3}{\partial T_y} &= 2\tau_{xy} \tau_{zx} - 2S_y \tau_{xz} \\ (5.16) \end{aligned}$$

$$\begin{split} \frac{\partial \tau_{xy}}{\partial \{\sigma\}} &= \begin{cases} 0\\0\\1\\0\\0 \end{cases}, \quad \frac{\partial \tau_{yz}}{\partial \{\sigma\}} &= \begin{cases} 0\\0\\0\\1\\0 \end{cases}, \quad \frac{\partial \tau_{zx}}{\partial \{\sigma\}} &= \begin{cases} 0\\0\\0\\0\\1\\0 \end{cases}, \quad \frac{\partial \tau_{zx}}{\partial \{\sigma\}} &= \begin{cases} 0\\0\\0\\0\\0\\1 \end{cases} \end{cases} (5.17) \\ \left. \frac{1}{3} \left[2(S_y S_z - \tau_{yz}^2) - (S_x S_z - \tau_{xz}^2) - (S_x S_y - \tau_{xy}^2) \right] \\ \frac{1}{3} \left[-(S_y S_z - \tau_{yz}^2) + 2(S_x S_z - \tau_{xz}^2) - (S_x S_y - \tau_{xy}^2) \right] \\ \frac{1}{3} \left[-(S_y S_z - \tau_{yz}^2) - 2(S_x S_z - \tau_{xz}^2) - (S_x S_y - \tau_{xy}^2) \right] \\ \frac{1}{3} \left[-(S_y S_z - \tau_{yz}^2) - 2(S_x S_z - \tau_{xz}^2) + (S_x S_y - \tau_{xy}^2) \right] \\ \frac{2(\tau_{yz} \tau_{zx} - S_z \tau_{xy})}{2(\tau_{xy} \tau_{zx} - S_x \tau_{yz})} \\ 2(\tau_{xy} \tau_{yz} - S_y \tau_{xz}) \end{cases} \end{split}$$

Equation (5.18) is further simplified as

$$\frac{\partial J_{x}}{\partial \{\sigma\}} = \begin{cases} \frac{1}{3} \left[2S_{y}S_{z} - S_{x}S_{z} - S_{x}S_{y} - 2\tau_{yz}^{2} + \tau_{xz}^{2} + \tau_{xy}^{2} \right] \\ \frac{1}{3} \left[2S_{x}S_{z} - S_{y}S_{z} - S_{x}S_{y} - 2\tau_{xz}^{2} + \tau_{yz}^{2} + \tau_{xy}^{2} \right] \\ \frac{1}{3} \left[2S_{x}S_{y} - S_{y}S_{z} - S_{x}S_{z} - 2\tau_{xy}^{2} + \tau_{yz}^{2} + \tau_{zx}^{2} \right] \\ \frac{2(\tau_{yz}\tau_{zx} - S_{z}\tau_{xy})}{2(\tau_{xy}\tau_{zx} - S_{x}\tau_{yz})} \\ \frac{2(\tau_{xy}\tau_{zx} - S_{x}\tau_{yz})}{2(\tau_{xy}\tau_{zx} - S_{y}\tau_{xz})} \end{cases}$$
(5.19)

From the flow rule of normality principle, the following relationship exists between the plastic strain increment and the plastic stress increment:

$$d\{\varepsilon\} = \lambda \frac{\partial f}{\partial \{\sigma\}} \qquad (5.20)$$

This equation can be interpreted as requiring the normality of the plastic strain increment vector to yield the surface in the hyper-space of *n* stress dimensions. As before $d\lambda$ is the proportionality constant.

For stress increments of infinitesimal size, the change of strain can be divided into elastic and plastic parts, thus (as before)

$$d\{\varepsilon\} = d\{\varepsilon\}_{\varepsilon} + d\{\varepsilon\}_{p} \qquad (5.21)$$

The elastic increment of stress and strain is related to an isotropic material property matrix [D] by

$$d\{\varepsilon\}_{\varepsilon} = [D]^{-1}d\{\sigma\} \qquad (5.22)$$

From Equation (5.20) - (5.22) the following equation is established:

$$d\{\varepsilon\} = [D]^{-1}d\{\sigma\} + d\lambda \left\{\frac{\partial f}{\partial\{\sigma\}}\right\}$$
(5.23)

The function stresses, on differentiation, can be written as

$$df = \frac{\partial f}{\partial \sigma_1} d\sigma_1 + \frac{\partial f}{\partial \sigma_2} d\sigma_2 + \ldots + 0 = \left\{ \frac{\partial f}{\partial \{\sigma\}} \right\}^{T''} d\{\sigma\}$$
(5.24)

Equation (5.24) together with (5.25) can be written in matrix form as

$$d\{\varepsilon\} = [D]_{\varepsilon p}^{-1} d\{\sigma\} \qquad (5.25)$$

$$\begin{cases} d\varepsilon_{x} \\ d\varepsilon_{y} \\ d\varepsilon_{z} \\ d\gamma_{xy} \\ d\gamma_{yz} \\ d\gamma_{zx} \\ 0 \end{cases} = \begin{bmatrix} [2pt] & & \frac{\partial f}{\partial \sigma_{x}} \\ & & [D]^{-1} & & \frac{\partial f}{\partial \sigma_{z}} \\ & & & \frac{\partial f}{\partial \tau_{xy}} \\ & & & \frac{\partial f}{\partial \tau_{xy}} \\ & & & & \frac{\partial f}{\partial \tau_{yz}} \\ \frac{\partial f}{\partial \sigma_{x}} & & \frac{\partial f}{\partial \sigma_{y}} & \frac{\partial f}{\partial \sigma_{z}} & \frac{\partial f}{\partial \tau_{xy}} & \frac{\partial f}{\partial \tau_{zx}} \\ \frac{\partial f}{\partial \sigma_{x}} & & \frac{\partial f}{\partial \sigma_{y}} & \frac{\partial f}{\partial \sigma_{z}} & \frac{\partial f}{\partial \tau_{xy}} & \frac{\partial f}{\partial \tau_{xx}} & 0 \end{bmatrix} \begin{pmatrix} d\sigma_{x} \\ d\sigma_{y} \\ d\sigma_{z} \\ d\tau_{xy} \\ d\tau_{yz} \\ d\lambda \end{pmatrix}$$
(5.26)

Inversion of the above matrix $[D]^{[-1]}$ will give stresses

$$d\{\sigma\} = [D]_{\epsilon p} d\{\varepsilon\} \qquad (5.27)$$

The explicit form of the elasto-plastic material matrix $[D]_{sp}$ is given by

$$[D]_{\epsilon p} = [D] - [D] \left\{ \frac{\partial f}{\partial \sigma_x} \right\} \left\{ \frac{\partial f}{\partial \sigma_x} \right\}^T [D] \left\{ \frac{\partial f}{\partial \sigma_x} \right\}^T [D] \left\{ \frac{\partial f}{\partial \sigma_x} \right\}^{-1}$$
(5.28)

The value of $(\partial f/\partial_{\sigma_x})$ has been evaluated above. The rest of the procedure using finite element is described in Chapter 3.

Table 5.5 Five-parameter model

A full description of this model is given which predicts failure. The same failure surface in terms of tensile and compressive meridians is well defined. The average normal stress σ_a is given by

$$\rho(\sigma_{a}, \theta) = \frac{(c+t)}{v}$$
(5.29)

$$c = 2(\rho_{c}^{3} - \rho_{c}\rho_{t}^{2})\cos\theta$$

$$t = (2\rho_{c}\rho_{c} - \rho_{c}^{2})[\alpha_{1}'' + 5\rho_{c}^{2} - 4\rho_{c}\rho_{c}]^{1/2}$$

$$v = \alpha_{1}'' + (\rho_{c} - 2\rho_{c})^{2}$$

The chain rule of differentiation is used in order to evaluate the gradient $\partial f / \partial \sigma_{ij}$

$$\frac{\partial f}{\partial \sigma_{ij}} = \frac{\partial f}{\partial p} \frac{\partial p}{\partial \sigma_a} \frac{\partial \sigma_a}{\partial \sigma_{ij}} + \frac{\partial f}{\partial p} \frac{\partial p}{\partial \theta} \frac{\partial \theta}{\partial \sigma_{ij}} + \frac{\partial f}{\partial \tau_a} \frac{\partial \tau_a}{\partial \sigma_{ij}}$$
(5.30)

Values for the terms in (5.30) are given below:

$$\frac{\partial f}{\partial p} = \frac{-\tau_a}{f_c} \frac{1}{\rho^2} \qquad (5.31a)$$

where
$$\partial \rho = 1 \left[\left(\partial c \right) \left(\partial t \right) \right] = \left(c + t \right) \partial y = (5.21b)$$

$$\begin{aligned} \frac{\partial \sigma_{a}}{\partial \sigma_{a}} &= \frac{1}{v} \left[\left(\frac{\partial \sigma_{a}}{\partial \sigma_{a}} \right) \left(\frac{\partial \sigma_{a}}{\partial \sigma_{a}} \right) \right] - (c+t) \frac{\partial \sigma_{a}}{\partial \sigma_{a}} & (5.31b) \\ \frac{\partial c}{\partial \sigma_{a}} &= 2 \cos \theta \left[\left(3\rho_{c}^{2} - \rho_{t}^{2} \right) \frac{d\rho_{c}}{d\sigma_{a}} - 2\rho_{c}\rho_{t} \frac{dt}{d\sigma_{a}} \right] \\ \frac{\partial t}{\partial \rho_{a}} &= \left[2\rho_{c} \frac{d\rho_{t}}{d\sigma_{a}} + 2(\rho_{t} - \rho_{c}) \frac{d\rho_{c}}{d\sigma_{a}} \right] [\alpha_{1}^{\prime\prime} + 5\rho_{t}^{2} - 4\rho_{c}\rho_{t}]^{1/2} \\ + \frac{(2\rho_{c}\rho_{t} - \rho_{c}^{2}) \left[(+10\rho_{t} - 8\rho_{t} \cos^{2} \theta - 4\rho_{c}) \frac{d\rho_{t}}{d\sigma_{a}} + (8\rho_{c} \cos^{2} \theta - 4\rho_{c}) \frac{d\rho_{c}}{d\sigma_{a}} \right] \\ \frac{\partial v}{\partial \sigma_{a}} &= \left(8\rho_{t} \sin^{2} \theta - 4\rho_{c} \right) \frac{d\rho_{t}}{d\sigma_{a}} + \left(8\rho_{c} \cos^{2} \theta + 2\rho_{c} - 4\rho_{t} \right) \frac{d\rho_{c}}{d\sigma_{a}} \quad (5.31c) \end{aligned}$$

From Eq. (5.30) the vectors $\rho_{\rm c}$ and $\rho_{\rm t}$ are evaluated.

In Eq. (3.31e) $d\rho_{\rm c}/d_{\sigma_{\rm a}}$ is taken as

$$\frac{d\rho_{\rm c}}{d\sigma_{\rm a}} = \sqrt{5b_1} + \frac{2\sqrt{5b_2\sigma_{\rm a}}}{f} \qquad (5.31f)$$

Similarly

 $\frac{d\rho_{\rm t}}{d\sigma_{\rm a}} = \sqrt{5a_1} + \frac{2\sqrt{5a_2}\sigma_{\rm a}}{f}$

The value of the term $\partial_{\sigma_a}/\partial_{\sigma_{ii}}$ is already known and equal to $1/3S_{ii}$.

Once the gradient is known the elasto-plstic formulation described in Chapter 3 can be adopted.

Table 5.6 Non-linear bond linkage element

The Ahmlink element procedure described in \sim i4—I can easily be included in the finite element analysis by adopting the following steps:

(a) Calculate the incremental slip from the nodal displacements:

 $\{\triangle S_i\} = [T'']\{\triangle U_i\} \qquad (5.32)$

where $[T^n j$ is the transformation matrix and $\{\sim L,\}$ are the element nodal displacements. The total slip at iteration *i* is calculated as

$$\{S_i\} = \{S_{i-1}\} + \{\triangle S_i\}$$
(5.33)

(b) Calculate the incremental stress based on the bond stress at iteration i - I:

$$\{\triangle \sigma_{\mathbf{b}i}\} = [E_{\mathbf{b}}^{\mathsf{t}}]\{\sigma_{\mathbf{b}i-1}\}\{\triangle S_i\} \tag{5.34}$$

Total stress is equal to

 $\{\sigma_{\mathbf{b}}i\}_{\mathrm{TOT}} = \{\sigma_{\mathbf{b}i-1}\} + \{\triangle\sigma_{\mathbf{b}i}\}$ (5.35)

- (c) Check the state of the bond, i.e. whether the bond is broken or not, and calculate the stress accordingly.
- If $IS \sim > S_{max}$, set flag 'sat = I, i.e. bond is broken. At this point, the bond stress is instantaneously dropped to zero, i.e. $\{u_5\} = 0.0$, where $\{S_{max}\}$ is the maximum slip allowed.
- If JS~~ < S~, calculate the bond stress which is compatible with the slip, S~. This is obtained by linear interpolation of a nonline r ~ond—slip curve. The curve is simulated by multi-linear lines. Figure V ~ gives the scheme for the linear interpolation. Let {o~,} be the bond stress compatible with the slip S. The difference between {ab.} and {o~} is treated as initial stress and this may be converted into nodal loads on the structure under consideration.



 $\{\triangle \sigma_{\mathrm{D}}\} = \{\sigma_{\mathrm{b}i}\} - \{\sigma_{\mathrm{b}}^r\} \qquad (5.36)$

The correct stress is written as

 $\{\sigma_{\mathrm{b}i}\}_{\mathrm{cor}} = \{\sigma_{\mathrm{b}i}\} - \{\triangle\sigma_{\mathrm{D}}\} \qquad (5.37)$

(d) Total internal equivalent loads and residuals are calculated as

 $\{F\}_{\text{internal}} = \pi dL[T]^{T'}\{\sigma_{bi}\} \quad \{R\} = \{F\}_{\text{external}} - \{F\}_{\text{internal}}$ (5.38)

The rest of the procedure is the same as for the other above cases.

 Table 5.7 Analytical formulation of the steel liner

 $[K]_{\text{TOT}} \{\delta\}^* + \{F_{\text{T}}\} - \{R_{\text{T}}\} = 0$ where $[K]_{\text{TOT}} = [K_{\text{I}}] + [K_{\text{a}}]$

$$\{\delta\}^* = \left\{\begin{array}{c} \delta_{\mathrm{un}} \\ \delta_{\mathrm{b}} \end{array}\right\}; \ \{F_{\mathrm{T}}\} = \left\{\begin{array}{c} F_{\mathrm{un}} \\ F_{\mathrm{b}} \end{array}\right\}; \ \{R_{\mathrm{T}}\} = \left\{\begin{array}{c} R_{\mathrm{un}} \\ R_{\mathrm{b}} \end{array}\right\};$$

 $[K_{\text{TOT}}]$ = total stiffness matrix, $[K_i]$ = liner stiffness matrix, $\{K_j\}$ = a stud stiffness matrix, $\{F_T\}$ total initial load vector, $R \sim$ } = total external load vector

= quantities corresponding to unknown displacement = quantities corresponding to restrained boundaries

$$[K]_{,,J} \{\sim 5 \sim, \} + \sim = 0$$

$$\{c\} = [B] \{b4$$

$$\sim cr\} = [D] (\sim\} - \{e \sim\})$$

$$= \text{ anchor shear forces}$$

$$F_{un} = \int_{r} [B]^{T} [D] \{\varepsilon_{0}\} dv = [B]^{T} [D] \{\varepsilon_{0}\} \det[J] d\xi d\eta d\zeta$$

The plastic buckling matrix is given by

$$(K + \lambda K_{\rm G})F_{\rm T} = 0$$

where

K = elasto-plastic stiffness matrix as a function of the current state of plastic deformation $K_G =$ initial stress geometric stiffness matrix.

The determinant $|K + \lambda K_G| = 0$

The essential equation is characteristically triangularised for the *i*th loading step as

 $(K^i + \lambda_{\epsilon} K^i_G) F^i_T = 0$ $\lambda_c = 1 + E_{ps} E_{ps}$ - accuracy parameter

| $\sigma_1 - \text{Direction } [D]^* =$ | $\begin{bmatrix} 0 & 0 \\ 0 & \left(D_{22} - \frac{D_{12}^2}{D_{11}}\right) \\ 0 & \left(D_{23} - \frac{D_{31}D_2}{D_{11}}\right) \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$ | $ \begin{pmatrix} 0 \\ D_{23} - \frac{D_{18}D_{12}}{D_{11}} \\ D_{33} - \frac{D_{13}D_{13}}{D_{11}} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} $ | $\begin{matrix} 0\\ 0\\ 0\\ \beta' D_{44}\\ 0\\ 0\\ 0\end{matrix}$ | $\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ D_{55} \\ 0 \\ \beta \end{array}$ | $\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0' D_{66} \end{bmatrix}$ |
|--|--|--|---|--|--|
| σ_2 – Direction $[D]^* =$ | $\begin{bmatrix} \left(D_{11} - \frac{D_{21}}{D_{22}}\right) \\ 0 \\ \left(D_{31} - \frac{D_{21}D_{32}}{D_{22}}\right) \\ 0 \\ 0 \\ 0 \end{bmatrix}$ | $\begin{array}{lll} 0 & \left(D_{13} - \frac{D_{12}D_{23}}{D_{22}}\right) \\ 0 & 0 \\ 0 & \left(D_{33} - \frac{D_{23}^2}{D_{22}}\right) \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{array}$ | $egin{array}{c} 0 \\ 0 \\ 0 \\ \beta' D_{44} \\ 0 \\ 0 \end{array}$ | $\begin{matrix} 0\\ 0\\ 0\\ 0\\ \beta' D_{55}\\ 0\end{matrix}$ | $\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ D_{66} \end{bmatrix}$ |
| σ_3 – Direction $[D]^* =$ | $\begin{bmatrix} \left(D_{11} - \frac{D_{13}^2}{D_{33}}\right) \\ \left(D_{21} - \frac{D_{31}D_{32}}{D_{33}}\right) \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$ | $ \begin{pmatrix} D_{12} - \frac{D_{13}D_{23}}{D_{23}} \end{pmatrix} & 0 \\ \begin{pmatrix} D_{22} - \frac{D_{23}D_{23}}{D_{33}} \end{pmatrix} & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{pmatrix} $ | $egin{array}{c} 0 \\ 0 \\ D_{44} \\ 0 \end{array}$ | $\begin{array}{ccc} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ \beta' D_{55} & 0 \end{array}$ | |

Table 5.8 Material matrices typical cracks in one, two, three directions

exceeding the vertical components of the shear resistance and normal stress on the inclined failure surface of the core. The vessel is assumed to deform. Several flexural and shear modes are considered. Cracks are assumed to develop at different positions in the wall and the cap. Strains, stresses and crack widths are computed under each mode. Several concrete strength criteria are included for comparison. Each failure mode is judged against the following criteria:

- (a) exceeding the minimum rupturing strength of the tendons,
- (b) exceeding concrete strength under complex loads,
- (c) limiting crack sizes affecting the integrity of the vessel,
- (d) rupturing strength of the liner crossing the crack. Any one of these cases, if reached, will define the failure of the vessel. The gas pressure that causes these is treated to have a minimum value.

5.15.1 Analysis of Flexural Failure

Generally the symmetry dictates and it is also evident from the experimental test [10–15] that one hinge should form at the equator and the position of any haunch hinge is determined by considering the equilibrium of the mechanism with various assumed hinge positions at the junction of the cap and the wall. Figure 5.28 shows a slice of the vessel between the two radial yield lines. The

internal height of the main cavity is $2H_i$. The internal and external radii are R_I and $R_{\rm E}$, respectively. For distinction the main cavity is subject to the internal gas pressure P_{G} and where boilers or circulators exist in the vessel walls the internal gas pressure is denoted by P_{GB} . As before the top cap standpipes/ control rods are shown as each having a diameter of $2R_{\rm p}$. Where boilers/ circulators exist, the diameter of each boiler is denoted by $2R_{\rm B}$ with an assumed pressurised height $H_{\rm B}$ above or below the equator. Let $\varepsilon'_{\rm ps}$, $\varepsilon'_{\rm pc}$, $\varepsilon^{\rm e}_{\rm pc}$ be the circumferential strain at the hinge at any distance Z, the circumferential strain at the top of the cap and the circumferential strain at the equator, respectively. The total cap pressure \bar{P}_{c} acts at a distance X from the central line of the vessel. The total vertical prestressing load $F_{\rm v}$ or $F'_{\rm v}$ defined earlier acts at a centroid at a distance 'a' from the outside face of the vessel or R' from the central line of the vessel. Under incremental pressure or during deformation, all the above parameters do vary, particularly the magnitude of the pressure and prestressing loads and their centroids for specific values of strains and deformations. As the vessel deforms and cracks are propagating, the depth of the compression block at the hinge such as $x_{\rm p}$, $x_{\rm b}$ and $x_{\rm w}$ changes. It is essential to assume the shape of the compressive block before developing the equilibrium equations defining various incremental stages and ultimate conditions.

5.15.1.1 Concrete Stress Block

For the ultimate limit state conditions, the stress block given in Fig. 5.28 is adopted. The general flexural theory may be modified to include tendon strain $\varepsilon_{\rm pb}$ at ultimate conditions which is made up of the two parts, namely $\varepsilon_{\rm ps}$, the effective tendon prestress after losses as dictated earlier, and the additional strains $\varepsilon_{\rm pa} = \varepsilon_{\rm ce} + \varepsilon_{\rm u}$, as shown later on. The value of $\varepsilon_{\rm ce} = (1/E_{\rm c})x$ the concrete prestress at the tendon level and the value of $\varepsilon_{\rm u}$ is the average concrete strain at the level of the tendon at ultimate conditions. This of course is true for a bonded tendon. For an unbonded tendon $\varepsilon_{\rm pa}$ is always less than the algebraic sum of $\varepsilon_{\rm ce}$ and $\varepsilon_{\rm u}$. In general $\varepsilon_{\rm pa}$ is written as

$$\varepsilon_{\rm pa} = m_1 \varepsilon_{\rm e} + m_2 \varepsilon_{\rm u} \tag{5.39}$$

For bonded tendon in the vessel $m_1 = m_2 = 1$. In the examples chosen where unbonded tendons are used, the values of m_1 and m_2 are assumed to be 0.5 and 0.25, respectively, as are normally assumed for heavy beams and slabs.

5.15.1.2 Barrel Wall

For the limit state flexural analysis of the barrel wall, Fig. 5.28 shows one-half of the barrel wall. The equations of equilibrium of forces on the wall have been computed and are given below. The axial force F'_v on segment 2θ is then related as

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$$f_{v}' = \frac{\theta}{\pi} \left[A_{\rm sp} E_{\varepsilon} \left[\varepsilon_{\rm p\varepsilon} + \frac{\pi p_{\rm G} (R_{\rm I}^{2} + n_{\rm o} R_{\rm B}^{2})}{E_{\rm c} A_{\rm c} + E_{\rm s} A_{\rm sp}} \right] \right]$$
(5.40)
+
$$\frac{R_{\rm E} (\varepsilon_{\rm po}^{\varepsilon} - \varepsilon_{\rm ps}') R_{\rm E} - R_{\rm I} - \frac{2(F_{\rm o} + T_{\rm F})}{0.45\sigma_{\rm cu}(R_{\rm E} + R_{\rm I})\sin\theta}}{Z(H_{\rm I} + d)}$$
+
$$\frac{R_{\rm E} (\varepsilon_{\rm pc}^{\varepsilon} - \varepsilon_{\rm ps}') \left(a - \frac{(F_{\rm o} + T_{\rm F})}{0.45\sigma_{\rm cu}(R_{\rm E} + R_{\rm I})\sin\theta} \right)}{(H_{\rm I} + d)(H_{\rm I} - d - z)}$$
+
$$D_{\rm W} \pi (R_{E}^{2} - R_{\rm I}^{2}) - \pi P_{\rm G} (R_{\rm I}^{2} + n_{\rm b} R_{\rm B}^{2})$$

Since F'_1 is a function of P_G for iterative solutions on the computer, it will be convenient to separate constant terms from the F'_1 and P_0 dependent terms.

$F'_{\rm V}$ Dependent Terms

$$\begin{split} 1 + \frac{\theta}{\pi} A_{\rm sp} E_{\rm s} \bigg[\frac{R_{\rm E}(\varepsilon_{\rm pc}^* - \varepsilon_{\rm ps}')}{Z(H_1 + d)} \bigg\{ \frac{1}{0.225\sigma_{\rm cu}(R_{\rm E} + R_1)\sin\theta} \bigg\} + \frac{R_{\rm E}(\varepsilon_{\rm pc} - \varepsilon_{\rm ps}')}{(H_1 + d)(H_1 - d - Z)} \\ + \bigg\{ \frac{1}{0.45\sigma_{\rm cu}(R_E + R_1)\sin\theta} \bigg\} \bigg] \end{split}$$

or

$$K_{1} = \left[1 + \frac{R_{\rm E}\frac{\theta}{\pi}A_{\rm sp}E_{\rm s}}{(\sigma_{\rm cu}(R_{\rm E} + R_{\rm 1})\sin\theta)(H_{\rm 1} + d)} \left\{\frac{\varepsilon_{\rm pb}^{\epsilon} - \varepsilon_{\rm ps}'}{0.225Z} + \frac{\varepsilon_{\rm pc}^{*} - \varepsilon_{\rm ps}'}{0.45(H_{\rm 1} + dZ)}\right\}\right]$$
(5.41)

Equation (5.41) is common for all the vessels.

P_G Dependent Terms

$$\frac{\theta}{\pi} \left[A_{\rm sp} E_s \frac{\pi (R_{\rm I}^2 + n_{\rm b} R_{\rm B}^2)}{E_{\rm c} A_{\rm c} + E_{\rm s} A_{\rm sp}} - \pi (R_{\rm I}^2 + n_{\rm b} R_{\rm B}^2) \right]$$
(5.42)

or

$$K_{2} = \theta (R_{1}^{2} + n_{b}R_{B}^{2}) \left[\frac{A_{sp}.E_{s}}{E_{c}.A_{c} - E_{s}A_{sp}} - 1 \right]$$
(5.42a)

Equation (5.42a) can be used directly for the HTGCR and Hartlepool vessels. For the Dungeness B and Oldbury vessels, equation (5.42a) is reduced to

$$K_2 = -\theta \cdot R_1^2 \left(\frac{E_c A_c \cdot E_{sp}}{E_c A_c + E_s A_{sp}} \right)$$
(5.43)

Constant Terms

$$K_{3} = \frac{\theta A_{\rm sp} E_{s}}{\pi} \left[\varepsilon_{\rm ps} + \frac{R_{E}}{(H_{1} + d)} \begin{cases} (\varepsilon_{\rm pc}^{\varepsilon} - \varepsilon_{\rm ps}^{\prime}) \left(R_{\rm E} + R_{1} \frac{T_{\rm F}}{0.225\sigma_{\rm cu}(R_{\rm E} + R_{1})\sin\theta} \right) \\ Z \end{cases} + \frac{R_{\rm E} (\varepsilon_{\rm pc}^{\epsilon} - \varepsilon_{\rm ps}^{\prime}) \left(a - \frac{T_{\rm F}}{0.45\sigma_{\rm cu}(R_{\rm E} + R_{1})\sin\theta} \right) \\ (H_{1} - d - Z) \end{cases} \right\} \right] + D_{\rm w} (R_{\rm E}^{2} + R_{1}^{2})$$

where

$$\sigma_{\rm pb} = (\varepsilon_{\rm ps} + \varepsilon_{\rm l} + \varepsilon_{\rm pp} + \varepsilon_{\rm cpv}) \times E_{\rm s}$$
(5.45)

It is initially assumed that, $\sigma_{pb} \leq pu \dots$ where $pu \dots$ the circumferential strain when the circumferential bands or tendons yield.

Evaluation of Strain and Stresses

(a) $\varepsilon_{\rm ps}$ stress in tendons/ $E_{\rm s}$

(b)
$$\varepsilon_{\rm l} = \frac{[(P_{\rm G}\pi R_{\rm l}^2) + n_{\rm b}\pi (P_{GB})\pi R_{\rm B}^2]}{E_{\rm c}}.A_{\rm c} + E_{\rm s}.A_{\rm sp}$$
 (5.46)

where $A_{\rm c} = \pi \left(R_{\rm E}^2 - R_1^2 - n_{\rm b} - \pi R_{\rm B}^2 \right)$ $A_{\rm sp} =$ area prestressing steel

(c) ε_{pp} and ε_{cpt} . Figure J.4 shows the top half of the barrel wall in a rotated position. Line A - A is centroid of the vertical tendon. Various displacements are related which are given below:

$$\frac{\delta_{\epsilon}}{(R_{\rm E} - F_{\rm I} - t - x_{\rm t})} = \frac{\delta_{\rm T}}{(t - x_{\rm w})} = \frac{R_E(\varepsilon_{\rm pb}^{\epsilon} - \varepsilon_{\rm ps}')}{Z}$$
(5.47)

Therefore

$$\delta_{\varepsilon} + \delta_{\mathrm{T}} = \frac{R_{\mathrm{E}}(\varepsilon_{\mathrm{pb}}^{e} - \varepsilon_{\mathrm{ps}}')}{Z} \{ R_{\mathrm{E}} - R_{\mathrm{l}} - t - x_{\mathrm{t}} + t - x_{\mathrm{w}} \}$$
(5.48)

Hence

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$$\varepsilon_{\rm pp} = \frac{\delta_e + \delta_{\rm T}}{H_1 + d} \tag{5.49}$$

where δ_e and δ_T are defined in Fig. 1.4 and thickness of the cap.

Then

$$\varepsilon_{\rm cpo} = \frac{\delta'}{H_1 + d} = \frac{R_{\rm E}(\varepsilon_{\rm pc} - \varepsilon'_{\rm ps})(a - x_{\rm t})}{(H_1 + d)(H_1 - d - Z)}$$
(5.50)

where *a* is the distance from the outside face to the centroid of the vertical tendons.

 ε_{ps} = strain at transferless losses including those due to creep effect.

 ε_l = elastic strain due to gas pressure, ε_{pp} strain due to rigid plastic rotation of the barrel, ε_{cpt} strain due to rigid plastic rotation of the cap. The general equation for F' in the abbreviated form is now given by

$$F_{\rm v}' = \frac{K_2}{K_1} P_{\rm G} \frac{K_3}{K_1} \tag{5.50}$$

Now the pressure P_0 to hold forces due to prestressing tendons, bonded steel reinforcement, liner steel and concrete for specified values of Z, ε_{pc}^e and ε_{ps}' can be found by taking first moments about the haunch hinge zone at Z. Referring to the previous equations, the equating moments are

$$\overline{P}_{w1} \text{ or } \overline{P}_{w2}\left(Z - \frac{H_1}{2}\right) + P_{GB} \cdot 2R_B Z (2 \sin \theta) \frac{Z}{2} = M_{HT} \text{ or } M_{HB} + M_E + \sum_{z_B < z} (T(Z - Z_B)) + \sum \left((A_{sb} + \sigma_{yb} + A_{SL} \sigma_{yl}) \frac{Z^2}{2} \right)$$
(5.51)

In this case $P_{08} = P_0$, the second term on the left-hand side of equation (~is zero for the Oldbury and the Dungeness *B* vessels. The value of *T*, the radial component of force from the circumferential tendons or bands, is given by

$$T = \sigma_{\rm ps} \times A_{\rm hp} \times 2\sin \theta$$

$$\overline{P}_{w1} \text{ or } \overline{P}_{w2} = P_{\rm G}(2R_{\rm I}\sin \theta.H_{\rm I})$$
(5.52)

The expression for the moment M derived earlier is now the hinge moment $M_{\rm HT}$ or $M_{\rm HB}$ and $M_{\rm E}$ depending on the respective positions. Substituting equation (~~T into the above equations the following relationship between gas pressure and hinge moment is obtained:

$$M_{\rm HT} \text{ or } M_{\rm HB} + M_{\rm E} = C_{\rm c}(d_1 - \overline{x}) + F_{\rm bst}'(d_1 - d') - \left[\frac{K_2}{K_1}P_{\rm G} + \frac{K_3}{K_1}\right](d_e - e)$$
(5.53)
= $\left(\frac{K_2}{K_1}P_{\rm G} + \frac{K_3}{K_1}\right)(d_1 - d_e + e - \overline{x}) + T_{\rm F}(d_1 - \overline{x}) + F_{\rm bst}'(\overline{x} - d')$

Now take the same segment 2θ representing the top and bottom cap. For computer simulation procedure the segmental angle is given a new rotation 2ϕ which will differentiate between the barrel wall rotation and the cap rotation and will also assess distinctly the compatibility between them. Hence for both the top and the bottom caps the segmental angle $2\phi = 2\theta$ is retained throughout in the calculations.

The cap is subject to disturbing forces and moments due to gas pressures. The restoring forces and moments are due to

- (a) vertical compression of longitudinal prestressing tendons, bonded reinforcement and the liner causing a yield line moment *m*, of the transverse yield lines per unit length;
- (b) radial compression due to circumferential prestress, bonded reinforcement and the internal pressure acting on the barrel wall.

The equilibrium equations can be established by taking moments about a line passing through the centroid of the longitudinal tendons. This is the point about which $M_{\rm HT}$ and $M_{\rm R_{,,}}$ have previously been calculated. Similar to the barrel wall the equilibrium equation for the caps can be derived.

Total pressure P_c (Fig. 1.4)

$$P_{\rm G}\pi R_{\rm I}^2 \cdot \frac{2\phi}{2\pi} + P_{\rm GB}n_{\rm b}\pi R_{\rm B}^2 \frac{2\phi}{2\pi}$$

$$P_{\rm G}\phi R_{\rm I}^2 + P_{\rm GB}n_{\rm b}\phi R_{\rm B}^2$$
(5.54)

The centroid \bar{X} has already been evaluated earlier. The relationship between circumferential tendon forces $T_{\rm H}$ and P_0 given for various cases can now be easily derived. This pressure $\bar{P}_{\rm G}$ is required to maintain the cap in equilibrium for specified values of Z, t and

As the cap is divided into radial and transverse yield lines, they have their individual plastic moments which help in restoring the cap to equilibrium. Let m_{ϕ} be the plastic moment per unit length of the radial yield lines. The total length of any two radial lines is $(2RE-n_p2R_p)$ where *n*, is the number of penetrations each having a radius R_p crossing the yield lines. Similarly m_r is the plastic moment of the transverse yield lines per unit length with a total length of this type of yield line $2(R_E-a)$. In addition there is a pressure $P_{A\phi}$ due to circumferential tendons. The equilibrium equations can therefore be written as

$$\begin{split} \phi P_{\rm G}(R_I^2 + n_{\rm b}R_{\rm B}^2) \left(R_{\phi} - a - \frac{2}{3}R_{\rm I}\frac{\sin\phi}{\phi} \right) \\ &= D_{\rm w}R_{\rm B}^3\sin\phi \left(1 - a - \frac{\sin\phi}{\phi} \right) \\ &+ \left(\frac{K_2}{K_1}P_{\rm G} + \frac{K_3}{K_1} \right)(a) + T_{\rm F}(d_1 - \overline{x}) + F_{\rm bst}'(\overline{x} - d') \end{split}$$
(5.55)

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$$+2(R_{\rm E} - n_{\rm p}R_{\rm p}\sin\varphi) \left[\sum_{Z_{\rm B=1}}^{n} \left\{ (A_{\rm hp}'E_{\rm s}\varepsilon_{z}K') - P_{\rm G}(2n_{\rm b}R_{\rm B})H_{\rm 1} + d - (H_{\rm I}R_{\rm I}) \right. \\ \left. +2\bar{A}_{\rm sb}\sigma_{yb}(d_{\rm 1} - \overline{x}) + A_{\rm sb}''\sigma_{\rm scy}(d_{\rm 1} - d') \right\} \\ \left. -2\sin\varphi \left\{ \sum_{Z_{\rm B<1}}(T_{\rm H}) + \overline{A}_{\rm sb}\sigma_{yb}Z \right\} \left(H_{\rm 1} + \frac{d}{2} - Z \right) \right. \\ \left. +\sum_{Z_{\rm B<1}} \left((T_{\rm H})(H_{\rm 1} + \frac{d}{2} - Z_{\rm B}) \right) \right] \\ \left. +2\sin\varphi P_{\rm G}(R_{\rm I}H_{\rm I} + 2R_{\rm B}Z) \left(H_{\rm 1} + \frac{d}{2} - Z \right) \right.$$

$$\left. +2R_{\rm B}(H_{\rm B} - Z) \left(H_{\rm 1} + \frac{d}{2} - \frac{H_{\rm B} - Z}{2} - Z \right) \right.$$
(5.56)

The above term $P_{H\phi}(e)$ is evaluated which is a moment of the radial forces about the centre line of the cap. These are due to shear forces at the hinge at Z and circumferential tendons and any other pressure forces acting above the position Z of the hinge. Using Figs. 5.29 and 5.30 the breakdown of these forces and moments is given below:

(a) Circumferential prestresses below the hinge $Z_b \leq Z$

$$M_1 = -2\sin\phi \sum_{Z_{B(5.57)$$

(b) Circumferential prestresses below the hinge $Z_b > Z$

$$M_2 = -2\sin\phi \sum_{Z_{\rm B}< Z}^n (T_{\rm H}) \left(H_1 + \frac{d}{2} - Z\right)$$
(5.58)

(c) Boiler pressure $P_{\text{GB}} Z_{\text{b}} \leq Z$

$$M_{3} = +\sin\phi P_{\rm GB} 2R_{\rm B} \left(H_{1} + \frac{d}{2} - Z\right)$$
(5.59)

(d) Boiler pressure $P_{\text{GB}} Z_{\text{b}} \ge Z$

$$M_4 = +2\sin\phi P_{\rm GB} 2R_{\rm B} (H_{\rm B} - Z) \left(H_1 + \frac{d}{2} - \frac{H_{\rm B} - Z}{2} - Z\right)$$
(5.60)

(e) Gas internal pressure $P_{\rm G}$

$$M_{5} = 2\sin\phi P_{\rm G}R_{\rm I}H_{\rm I}\left(H_{1} + \frac{d}{2} - Z\right)$$
(5.61)

(f) Bonded reinforcement T_{ϕ}

$$M_6 = 2\sin\phi \bar{A}_{\rm sb}\sigma_{\rm yb}Z\left(H_1 + \frac{d}{2} - Z\right)$$
(5.62)

5.15.1.3 Crack Sizes

The major cracks are as follws:

- Horizontal cracks at haunch w_{th} and w_{bh}
- Longitudinal and horizontal cracks wel and weh
- Substituting *t*, *l* and *e* represent a top, bottom and equator of the vessel. Before computing the crack width, the barrel wall and the cap rotation α_B and α_c , respectively, are evaluated. The relevant strain used for these rotations are ε_{po}^e , ε'_{ps} and ε_{pc}

$$\alpha_{\rm B} = \left(\varepsilon_{\rm pb}^e - \varepsilon_{\rm ps}'\right) R_{\rm E} Z \tag{5.63}$$

$$\alpha_{\rm c} = \left(\varepsilon_{\rm pb}^e - \varepsilon_{\rm ps}'\right) R_{\rm E} / (H_1 + d - Z) \tag{5.64}$$

Next the depth of the crack is evaluated. From the geometry (Fig. 5.28) it is easy to compare the crack depth l_c given by

$$l_{\rm c} = \left[(R_{\rm E} - R_{\rm I} - \hat{x})^2 + (Z - H_{\rm I})^2 \right]^{1/2}$$
(5.65)

where \hat{x} is a typical value for x_t or x_b . Then crack width

$$w_{\rm th} \, {\rm or} \, W_{\rm tb} = (\alpha_{\rm B} + \alpha_{\rm c}) . l_{\rm c} = \frac{R_{\rm E}}{(H_1 + d - Z)} \bigg\{ (\varepsilon_{\rm pb}^e - \varepsilon_{\rm ps}') \frac{H_1 + d - Z}{Z} + (\varepsilon_{\rm pc} - \varepsilon_{\rm ps}') \bigg\}_{(5.66)}$$
$$x [(R_{\rm E} - R_I - \hat{x})^2 + (Z - H_I)^2]^{1/2}$$

The longitudinal crack width at the equator w_{el} is computed as

$$W_e = 2\pi R_{\rm E} (\varepsilon_{\rm pb}^e - \varepsilon_{\rm ps}') \frac{2\sin\theta}{2\pi}$$
(5.67)

The horizontal crack width at the equator w_{eh} is computed as
$$W_{eh} = R_{\rm E} \left(\varepsilon_{\rm pb}^e - \varepsilon_{\rm ps}' \right) \left[\frac{H_1 + d}{H_1 + d - Z} \right]$$
(5.68)

5.15.1.4 Additional Mechanisms in Caps

Once the vessel starts developing tensile cracks, only aggregate interlock friction and bonded steel reinforcement prevents the formation of one large crack. In zones where the reinforcement is not sufficient additional cracks form in the cap area vertically [10–15] near the haunch and at the standpipe perimeter (central plug) due to cap fixture-cum-shear. Under pure flexural conditions, the additional hinges form in the cap, say, at any distance $2R_E\beta$ as shown in Fig. 5.55. It is assumed that lateral restraint is provided to the cap due to barrel and cap circumferential prestressing and no vertical translation occurs between the hinge and the external boundary or rim of the cap. This assumption demands that analysis should include the effect on the compressive membrane action of this partial restraint against lateral displacement at the rim and the radial strain in the plane of the cap. The radial strain σ_7 is assumed to be the algebraic sum of Σ_c , the creep strain Σ_s , the shrinkage strain and Σ_e the elastic strain.

The total radial strain $\varepsilon_T = \varepsilon_c + \varepsilon_s + \varepsilon_e$ is assumed to be constant since elastic or membrane forces due to these are constant. Because of the value of C_T , the middle portion *BC* between the yield and cracked zone will be reduced by $2R_E\varepsilon_T(1-2\beta)$. This will cause an outward lateral displacement \ddot{o}_0 at the haunch boundaries *A* and *B* or *C* and *D* as shown in Fig. 5.55 owing to the same c_7 the dimensions *AB* or *CD* will decrease *AB* by $2R_E\beta(1-2\beta)$. Hence due to the total movement caused by ε_T and δ_0 , the final reduced dimension *R'* will become

$$R' = [2R_{\rm E}(\beta + \varepsilon_T(1 - 2\beta) + \delta_o)] \sec \alpha_{\rm c}$$
(5.69)

where α_c is the cap rotation. -

Let the distances to the neutral axes from the compressed faces of the concrete at the sagging and hogging conditions be the two values of x, i.e. x_1 and x_2 . These values of x_1 and x_2 can be evaluated in the same way as before. Due to the inclusion of membrane forces, the value of x may not be equal to x_1 or x_2 , during incremental deformation. Assume $x_1 = n_1 d$ and $x_2 = n_2 d$, (Fig. 5.56). The equations for n_1 and n_2 , F_e , M_e are written as

$$(1 - n_2)d\tan\alpha_{\rm c} + 2R_{\rm E}(1 - \varepsilon).\beta n_1 d\tan\alpha_{\rm c}$$
(5.70)



Fig. 5.55 Collapse mechanism

Fig. 5.56 Portion of a YIELD SECTION



From Eqs. (5.69) and (5.70)

$$1 - (n_1 + n_2) = \frac{\left[2R_{\rm E}\beta + 2R_{\rm E}\varepsilon_{\rm T}(1 - 2\beta) + \delta_{\rm o}\right] - 2R_{\rm E}(\beta - \varepsilon\beta)\cos\alpha_{\rm c}}{d\sin\alpha_{\rm c}}$$

or

$$n_{1} + n_{2} = 1 - \frac{2R_{E}\{\beta - \varepsilon_{T}(1 - 2\beta) - (\beta - \varepsilon_{T})\cos\alpha_{c}\} + \delta_{o}}{d\sin\alpha_{c}}$$

$$= 1 - \frac{R_{E}\{\sin^{2}\frac{\alpha_{c}}{2} + \beta\epsilon\cos\alpha_{c} + \varepsilon_{T}(1 - 2\beta)\} + \delta_{o}}{d\sin\alpha_{c}}$$
(5.71)

For membrane forces α_c and ϵ_T are very small values therefore it is assumed that

$$\sin \alpha_{\rm c} = 2 \sin \frac{\alpha_c}{2} = \delta_z' / \beta(2R_E) \tag{5.72}$$

where δ'_z is the deflection of the cap at yield zone. Hence Eq. (5.71) is written as

$$n_1 + n_2 = 1 - \left\{ \frac{\delta'_z}{2d} + \frac{4R_{\rm E}^2\beta}{(d)(\delta'_z)} \varepsilon_{\rm T}\beta + \varepsilon_{\rm T} - 2\beta\varepsilon_{\rm T} + \frac{\delta_o}{2R_{\rm E}} \right\}$$
(5.73)

If the crack occurs around the standpipe perimeter or the central plug the hinges at *B* and *C* will be at equal distance from *A* and *D*, respectively. In that case equation (5.73) is modified by replacing $(\varepsilon_T - 2\beta_{\varepsilon T} + \frac{\delta_0}{2R_E})$ with $(\varepsilon_T + \frac{\delta_0}{2R_E})$. Proceeding as above Eq. (B. 8 l) then assumes the following form:

$$n_1 + n_2 = 1 - \left\{ \frac{\delta'_z}{2d} + \frac{4R_{\rm E}\beta}{(d)(\delta'_z)} \left(\varepsilon_T + \frac{\delta_o}{2R_{\rm E}} \right) \right\}$$
(5.74)

The equilibrium of horizontal forces acting on zone AB

$$F_{\varepsilon} = F_2'$$

or

$$C_{\rm c} + T_{\phi}' - T_{\rm F} = C_{\rm c}' + T_{\phi} - T_{\rm F}'$$
(5.75)

Therefore

$$n_2 - n_1 = \frac{T_{\rm F}' - T_{\rm F} - T_{\phi} + T_{\phi}'}{0.45\sigma_{\rm co}.d}$$
(5.76)

$$n_{1} = \frac{1}{4d} \left[2d - \delta_{z}' - \frac{\left(\varepsilon_{\rm T} + \frac{\delta_{o}}{2R_{\rm E}}\right) \cdot 4R_{\rm E}^{2}\beta}{\delta_{z}'} - \frac{T_{\rm F}' - T_{\rm F} - T_{\phi} + T_{\phi}'}{0.225\sigma_{\rm cu}} \right] \quad (5.77)$$

$$n_{2} = \frac{1}{4d} \left[2d - \delta_{z}' - \frac{\left(\varepsilon_{T} + \frac{\delta_{o}}{2R_{E}}\right) \cdot 4R_{E}^{2}\beta}{\delta_{z}'} + \frac{T_{F}' + T_{F} - T_{\phi} + T_{\phi}'}{0.225\sigma_{cu}} \right]$$
(5.78)

Equations (5.77) and (5.78) indicate that the values of n_1 and n_2 do differ as stated earlier and the term $(\varepsilon_T + (\delta_0/2R_E))$ in the same equations merely signifies the reduction in the depth to the neutral axis at the cracked sections. For the sagging part of the cracked section, the forces C_c , T'_{ϕ} and T_F are statically equivalent to the membrane force F_e at mid-depth. Hence

$$F_{\varepsilon} = C_{\rm c} + T_{\phi}' - T_{\rm F} = 0.45\sigma_{\rm cu}.n_1d + T_{\phi}' - T_F.$$
(5.78)

Various values in Eq. (5.78) have already been defined. The moment M caused by these forces is computed as

$$M_{\varepsilon} = 0.45\sigma_{\rm cu}n_1d\left(\frac{1}{2}d - K_3.x\right) + T'_{\phi}\left(\frac{1}{2}d - d'\right) + T_F\left(d_1 - \frac{1}{2}d\right)$$

= 0.45\sigma_{\rm cu}n_1d\left(\frac{1}{2}d - K_3n_1d\right) + T'_{\phi}\left(\frac{1}{2}d - d'\right) + T_F\left(d_1 - \frac{1}{2}d\right)(5.79)

where K_3 is already defined.

The moment M_e then replaces all the terms in the previous equations, except the terms $F_v(d_e - e)$ or $F_v a$ respectively. Wherever necessary, equations are similarly adjusted to include the above terms. For Hogging moment M'_e for yield or cracked sections is similar to equation 5.79 and can be computed by replacing n_1 by n_2 . The summation of moments for, say, *AB* or *CD* portions due to the above stress resultants at one end for a segment of 2ϕ will be given by

$$\begin{split} \sum M &= M_c + M'_e - F_e \cdot \delta'_z \\ &= 0.45\sigma_{\rm cu} \bigg\{ \frac{1}{2} d^2 (1 - K_3) + \frac{1}{4} \delta'_z \cdot d(2K_3 - 3) \\ &+ R_{\rm E}^2 \beta \varepsilon_T (1 - K_3 + 2K_3 d - d) + \frac{1}{(8d)} (\delta'_z)^4 (2 - K_3)] \\ &- 16K_3 \varepsilon_I^2 \beta^2 R_E^4 \bigg\} (2\sin \phi) - \frac{K_3}{0.9\sigma_{\rm cu}} (T'T_{\rm F} - T_{\phi} T'_{\phi})^2 (2\sin \phi) \\ &+ T_{\phi} \bigg(\frac{1}{2} d - d_{\rm c} - \frac{\delta'_z}{2} \bigg) (2\sin \phi) + T'_{\phi} \bigg(\frac{1}{2} d - d' - \frac{\delta'_z}{2} \bigg) (2\sin \phi) \\ &+ T_{\rm F} \bigg(d_1 - \frac{1}{2} d + \frac{\delta'_z}{2} \bigg) (2\sin \phi) \\ &+ T_{\rm F} \bigg(d_1 - \frac{1}{2} d + \frac{\delta'_z}{2} \bigg) (2\sin \phi) \end{split}$$
(5.80)

From the barrel wall rotation caused by the eccentric prestressing about the haunch hinge the moment value is

$$M_{\rm pB} = 2F_{\rm v}\left(e + \overline{x} - \frac{d}{2}\right) = 2\sin\phi\left(\frac{K_2}{K_1} \cdot P_{\rm G} + \frac{K_3}{K_1}\right)\left(e + \overline{x} - \frac{d}{2}\right) \tag{5.81}$$

This term is algebraically added to Eq. (5.82). Hence $M_{\rm HT}$, $M_{\rm HB}$ of previous equations are written in an abbreviated form as

$$M_{\rm HT} \text{ or } M_{\rm HB} = \sum M + M_{\rm PB} \tag{5.82}$$

The new values of $M_{\rm HT}$, $M_{\rm H}$ from Eq.(5.83) are then used and the intermediate equations are similarly adjusted accordingly for the redevelopment of the interaction equation.

5.15.1.5 Load Variation Due Radial Prestressing in Caps

In the Oldbury vessel a slight variation to the above equations is necessary for computing forces and moments. As stated in both the top and bottom caps of the Oldbury vessel the tendons are arranged horizontally in layers which form a square mesh in plan view. As shown in Figs. 5.55 and 5.56 both top and bottom caps are divided into slices. Equations are modified to include the term

$$\sum_{i=1}^{n} (P_{hi}.\mathbf{Y}_i + F_{vi}.R_i).$$

The final equation is then written as

$$\begin{split} \phi P_{\rm G} R_{\rm I}^2 (R_E - a - \frac{2}{3} R_I \frac{\sin \phi}{\phi} &= D_w R_E^3 \sin \phi \left(1 - a - \frac{\sin \phi}{\phi} \right) + \left(\frac{K_2}{K_1} P_{\rm G} + \frac{K_3}{K_1} \right) (a) \\ &+ T_F (d_1 - \overline{x}) + F_{\rm bst}' (\overline{x} + d') \end{split}$$

$$\pm \sum_{i=1}^{n} (P_{Hi}.Y + F_{vi}.R_i) + 2(R_E - n_p R_p \sin \phi)$$

$$\times \left[\sum_{Z_B=1}^{n} \left\{ (A'_{hp} E_s \varepsilon_z K') + P_G H_I R_I + 2A'_{sb} \sigma_{yb} (d_1 - \overline{x}) + A''_{sb} \sigma_{scy} (d_1 - d') \right\} \right]$$

(The term $(-n_p R_p \sin \phi)$ is zero from bottom cap)

$$-2\sin\phi\left\{\sum_{Z_{B}Z}T_{H}\left(H_{1}+\frac{d}{2}-Z_{B}\right)+2\sin\phi P_{G}-(R_{I}H_{I})\left(H_{1}+\frac{d}{2}-Z\right).$$
(5.83)

Equation (5.84) can then be recalled as an independent sub-routine in a computer program in solving this specific case.

Ultimate Limit State of Shear Analysis

Basic concept: The failure of concrete under complex loading has been adequately discussed in the references. In this section a further explanation is required regarding the so-called 'shear failure' under gas increasing pressure.

The concept of shear failure in thick sections of brittle material such as concrete is obscure and in many instances it could be misleading. One clear concept is that concrete failure can easily be put to the test if it is assumed that it is governed by the principal tensile and compressive stress caused by the so-called 'shear'. The problem with this simple concept is the limitation on these stresses. In the prestressed concrete reactor vessels due to variations in loading conditions these principal stresses at any time at any point may vary from biaxial and triaxial compression to compression—tension—tension in any combination. These instant changes can bring about any kind of failure. For example, it may be pure flexural-cumnominal shear failure or principal tensile or compressive failure or by the so-called shear compression failure or in any combination of these. It must be borne in mind that the type of failure is directly related to the vessel overall layout. Before discussing the individual sample examples, it is necessary to know what the above-mentioned terms are and what effect they have on the prestressed concrete vessels.

(a) Flexural-cum-Nominal Shear

As evident from previous discussions, flexural failure occurs by the formation of principal tensile or bending cracks followed by the crushing of the compressive zone. This may have been preceded by the yielding or breaking of steel in the vessel. In zones where nominal shear governs, the failure will take place along planes parallel to the direction of the applied loads. In some zones a certain magnitude of shear resistance is provided side by side with the flexural failure case.

(b) Principal Tensile Failure

Failure can take place by inclined principal tensile cracks produced by inclined principal tensile stresses in zones of larger shear. These cracks can spread rapidly through the section across the compression zone. Unless conventional steel reinforcements are present in such zones, an internal redistribution of forces is not possible.

(c) Principal Compressive Failure

Depending upon the low span/depth ratio, there is a possibility for the vessel components, like a short deep beam, to fail directly in compression as a tied arch or truss.

(d) Shear Compressive Failure

This term is normally associated with shorter deeper beams. Failure takes place when the compression zone, after its reduction in size due to cracking, fails under combined action of triaxial compression and shear stresses. This failure type can happen at principal tensile cracks. The limitation to this shear compression is that the average compressive stress in the concrete has only been found at failure in pure flexure. As it is based on extreme concrete fibre reaching its limiting strain it is possible that 'shear' failure can occur on an inclined plane near the centre of a compression zone. In the vessel the haunch hinge is under a multiaxial state of stress due to prestressing bonded steel, liner and penetrations. This zone will in that case resist shear compression failure.

However, principal stresses and consequently the cracks they cause, may appear in a number of different positions depending upon the relative magnitudes of loads, moments and 'shear' carried by the section. Significant differences occur among isolated cap tests and full model tests. Reported ultimate load tests for Oldbury and Bungeness B vessels consider each vessel to be initially broken up into an open-ended cylinder and two end slabs. The mechanisms of this initial break-up, however, appear to be in disagreement with each other. For the Oldbury analysis, the slab was separated from the barrel by a plastic hinge at the junction of the slab and barrel.

A shear-compression failure mechanism on the other hand was adopted for the Dungeness B vessel analysis. Of even greater disparity between the two analyses were the mechanisms and modes of failure adopted to predict the ultimate pressure or to prove that the ultimate load factor was higher than the adopted factors for the slab and the barrel. For the barrel, the Oldbury analysis apparently favoured the modes of failure through the formation of a plastic hinge at the mid-height of the barrel. For Hartlepool (20 g, 24Aa, 24Ae) the one-tenth scale model tests carried out gave flexural cracking in top cap but with isolated cap tests plug failure similar to the Dungeness B has been observed which is claimed to be due to shear compression and inclined tensile cracking phenomena. Other tests have reported either flexural or shear plug failure.

Shear in Barrel Wall and Caps

The present analysis is based on gas increasing pressure and progressive incremental deformation. Any of the above-mentioned 'shear' failure conditions caused by the net difference of the instantaneous inward and outward vessel forces can be automatically handled provided sufficient mathematical tools and iterative techniques are available. A separate analysis is required for both the barrel wall and the caps. Concrete failure criteria have been discussed previously. Some of the concrete strength theories discussed in this chapter are reproduced in the following order:

- (a) Mohr's theory based on octahedral shear and normal stresses.
- (b) Biaxial compression state.
- (c) Combined compression-tension state.
- (d) Empirical for shear derived from actual vessel data using hypo-elastic concept.

Any one of the above is associated with a straight line and parabolic stress variation. The above equations can be arranged so that they can be linked up with those of the ultimate limit state of flexure for both wall and caps. For each incremental deformation of the vessel, these equations can be tested for any premature 'shear failure' intervening flexural failure.

Barrel 'Shear'

The shear forces at any position of the hinge $Z \ge Z_B$ for each vessel incremental deformation can be found by resolving inward forces due to prestressing liner and bonded reinforcement and outward radial forces due to gas pressures from the main cavity with and without gas pressures in the boiler penetrations. The net force divided by the area of the concrete at that position is the shear stress.

Cap 'Shear'

The elastic analyses of many vessels indicate that everywhere except at the centre of the cap the circumferential tensile stresses are greater than the radial stresses and they cause flexural mode of failure by breaking up the cap into a series of wedges with their apices at the centre of the cap. In addition to this mode of failure the resistance of the compressive area in the standpipe region is generally reduced and it finally develops a circumferential plane of weakness at the outside perimeter of the standpipes. The Dungeness B model tests show a complete punched-out failure of the central core of the cap. Failure has occurred when the force due to the internal gas pressure P_G exceeded the vertical components of the shear resistance and normal stress on the inclined failure surface of the core. Figure 5.30 shows the equilibrium forces on the central core having sloping surfaces. The normal force and the shear force components are represented by N and Q. It is assumed that they act on single straight lines of intersection between the failure surface and the radial plane of the cap. The angle of failure y is considered as the rupture angle corresponding to the minimum pressure required to punch out the core. At the point of sliding the shear resistance on the failure surface is dependent on the normal stress. Once the relationship between the shear resistance and the normal stress is established then it is not difficult to determine the failure pressure for the core. As indicated in this case the distances x_1 and x_2 which are the inner and outer radii of the central core are dependent on the angle y. Let Z_c be the vertical distance from the top of the cap to any point on the sloping surface at a horizontal distance R_x from the circumferential plane of weakness as shown in Fig. 5.31. The radial forces $\bar{P}_{H\phi}$ are known from previous equations. Let the shear stress in the $R_x - Z_c$ plane be τ_{RZ} and the radial thrust on the inner core be \bar{P}_{Hi} , the minimum value of which is $\bar{P}_{H\phi}$. The upper value of \bar{P}_{Hi} is given from Fig. 5.31 as

$$\overline{P}_{Hi} = \frac{R_E}{R_x} \cdot \overline{P}_{H\phi} + \left(\frac{R_E}{R_x} - 1\right) \sigma_t$$
(5.84)

where σ_t is the tangential stress along the crack taken right through the thickness of the ring and is not less than $T_{H}/(R_E - R_I) (R_E + R_I) \sin \phi \sigma_t$ can also be the concrete tensile stress. The forces on the central core are shown in Fig. 5.31 and when they are resolved vertically

 P_{Gx} = the total pressure on the core diameter

$$x_1 = Q \sin \gamma - N \cos \gamma. \tag{5.85}$$

For simplification it is assumed that the shear and normal stresses acting at the inclined surface at distance (R_x, Z_c) from the top of the central core are of the octahedral type and are denoted, as before, by τ_0 and σ_0 , respectively. The above forces can then be written as

$$P_{Gx} = \pi (x_2 - d \cot \gamma)^2 \cdot P_G$$

$$Q = \int_{x_{2-d \cot \gamma}}^{x_2} \tau_o \cdot R_x \sec \gamma dR_x$$

$$N = 2\pi \int_{x_{2-d \cot \gamma}}^{x_2} \sigma_o R_x \sec \gamma \cdot dR_x$$
(5.86)

Substituting Eq. (5.86) into Eq. (5.85) those stresses are related to the internal gas pressure

$$P_G = \frac{2}{\left(x_{2-d \cot \gamma}\right)^2}$$

$$\int_{x_{2-d \cot \gamma}}^{x_2} (\tau_o \tan \gamma - \sigma_o) R_x dR_x$$
(5.87)

The equilibrium equation in the radial direction (Fig. 5.31) is given by

$$\sigma_o \sin \gamma + \tau_o \cos \gamma = \overline{P}_{Hi} \sin \gamma - \tau_{RZ} \cos \gamma.$$
(5.88)

Campbell–Allen et al. suggest straight line and parabolic stress variations for the shear stress τ_0 influenced by concrete strength and maximum aggregate size. As stated previously at the point of sliding the relationship between τ_0 and σ_0 can be written using different concepts. Campbell–Allen et al. suggests Mohr envelops. For straight line stress variation

$$\tau_{\rm o} = C' + \sigma_{\rm o} \tan \phi' \tag{5.89}$$

where *C*' is apparent cohesion for concrete, ϕ' is the angle of frictional resistance for concrete. In terms of parameters largely dependent on the concrete strength and the aggregate size, Campbell–Allen et al.^{20d} suggest an expression

$$\frac{\tau_n}{f'_c} = A(\sigma_n / f'_c + F_t / f'_c)^k$$
(5.90)

where τ_n is the limiting shear resistance

 σ_n normal stress on failure surface f'_c unconfined concrete compressive strength f_t the uniaxial tensile strength of concrete A, K parameters.

In this section $\tau_n = \tau_0$, $\sigma_n = \sigma_0$, K = K', $f_t = \sigma_t$ have been adopted and therefore Eq. (5.90) can be rewritten as

$$\tau_o = B' (\sigma_o + \sigma_t)^k \tag{5.91}$$

where

$$B' = \frac{A f_c'}{\left(f_c'\right)^k}.$$
 (5.92)

Now in addition to the above relationship τ_o , equations for shear reproduced below are considered for τ_o

Biaxial State of Stress

$$\tau_o = -\sqrt{2} \left(\frac{R_C - 1}{2R_C - 1} \right) \left(\sigma_o + \frac{1}{3} \sigma_o \right)$$
(5.93)

where R_c = biaxial strength/uniaxial strength of concrete.

Combined Compression Tension

$$\tau_o = -\sqrt{2} \left(\frac{L}{3} + \frac{2}{3} L_4 \right) \tag{5.94}$$

where

$$L_3 = \frac{1 - R_t}{1 + R_t}; \quad L_4 = \frac{R_t}{1 + R_t}$$

Hypoelastic Concept

$$\frac{\sigma_3}{\sigma_c} = -0.053 - 0.92 \left(\frac{\tau_0}{\sigma_c}\right)^{1.35}$$
(5.95)

From Equations (5.89) and (5.95) any one of the value of τ_0 can be considered during the vessel incremental deformation or gas increasing pressure. Case (A) $\tau_0 = C' + \sigma_0 \tan \phi'$

Substituting τ_0 from Eq. (5.98) into Eq. (5.88), Eq. (5.88) becomes

$$\sigma_{\rm o} = \frac{1}{\sin\gamma + \cos\gamma \tan\phi'} \left\{ \overline{P}_{Hi} \sin\gamma - \tau_{RZ} \cos\gamma - A' \cos\gamma \right\}$$
(5.96)

Substituting τ_0 and σ_0 into Eq. (5.87) then Eq. (5.87) is rewritten as

$$(x_{2} - d\cot\gamma)^{2}P_{G} + 2\int_{x_{2-d\cot\gamma}}^{x_{2}} \frac{\tau_{Rz}\cos\gamma(\tan\phi'\tan\gamma-1)}{(\sin\gamma+\tan\phi'\cos\gamma)}R_{x}d.R_{x}$$

$$= 2\int_{x_{2-d\cot\gamma}}^{x_{2}} \frac{\overline{P}_{Hi}\sin\gamma(\tan\phi'\tan\gamma-1)}{(\sin\gamma+\tan\phi'\cos\gamma)}R_{x}d.R_{x}$$

$$+ 2c'\int_{x_{2-d\cot\gamma}}^{x_{2}} \left[\tan\gamma - \frac{\cos\gamma(\tan\phi'\tan\gamma-1)}{\sin\gamma+\tan\phi'\cos\gamma}R_{x}d.R_{x}\right]$$
(5.97)

The value of \bar{P}_{Hi} is linear to those of P_{HQ} and τ_{RZ} and can be assumed to vary linearly with P_G , the internal gas pressure. The left-hand side of Eq. (5.97) involves τ_{Rz} values and the integral on the left-hand side can be solved for two different shear stress distributions.

Case (A): Uniform Shear Stress T_{Rz}

The value $\tau_{Rz} = (\frac{1}{2d}) P_G R_x$ is substituted in the integral part of the left-hand side of Eq. (5.64) and is finally itegrated

$$l.h.s = (x_2 - d \cot \gamma)^2 \cdot P_G + \frac{\cos \gamma (\tan \phi' \tan \gamma - 1)}{(\sin \gamma + \tan \phi' \cos \gamma)} \left[\frac{R_x^3}{3} \right]_{x_{2-d \cot \gamma}}^{x_2}$$
$$= (x_2 - d \cot \gamma)^2 + \frac{P_G \cos^2 \gamma (\tan \phi' \tan \gamma - 1)}{\sin \gamma (\sin \gamma + \tan \phi' \cos \gamma)}$$
$$(x_2^2 - x_2 d \cot \gamma - 0.334 \cot^2 \gamma) = P_G(\hat{\alpha}\hat{k})$$
(5.98)

where $\hat{\alpha}\hat{k}$ are the terms of Eq. (5.98) in the bracket after $P_{\rm G}$ is taken outside the bracket.

Now the right-hand side of Eq. (5.97) is evaluated. This is written as:

$$r.h.s = \overline{P}_{Hi} \frac{\sin\gamma(\tan\phi'\tan\gamma-1)}{(\sin\gamma+\tan\phi'\cos\gamma)} (2x_2d - d^2\cot\gamma)$$
(5.99)
+ $C' \left[\tan\gamma - \frac{\cos\gamma(\tan\phi'\tan\gamma-1)}{(\sin\gamma+\tan\phi'\cos\gamma)} \right] (2x_2d - d^2\cot\gamma)$

In Eq. (5.99) \bar{P}_{Hi} may have two values. One is

$$\overline{P}_{Hi} = \overline{P}_{H\phi} \tag{5.100}$$

The other is given by Eq. (5.84) when σ_0 is compressive \bar{P}_{Hi} must always be related as

$$\overline{P}_{Hi} \ge \cot \gamma (\tau_{Rz} + C') \tag{5.101}$$

where τ_{Rz} has a uniform or a parabolic shape.

Subject to modification given by Eq. (5.100) and equation (5.84) the gas minimum vertical pressure component $P_{\rm G}$ of the cap causing the parameter 'shear' failure is given by

$$\overline{P}_{\rm G} = {\rm Eq.}(5.100)/(\hat{\alpha}\hat{K}). \tag{5.102}$$

The value of γ in the above equations will then be the rupture angle.

Case (B) $\tau_{\rm o} = B' (\sigma_{\rm o} + \sigma_{\rm t})^k$

Using the parabolic stress variations, the value of

$$\tau_{Rz} = \frac{3P_G R_x Z_c (d - Z_c)}{d^3}.$$
 (5.103)

The value of τ_{Rz} when substituted in the integral part of the left-hand side of Eq. (5.97) gives another expression very similar to Eq. (5.98):

$$l.h.s = (x_2 - d\cot\gamma)^2 P_G + \frac{P_G \cos^2\gamma(\tan\phi'\tan\gamma - 1)}{\sin\gamma(\sin\gamma + \tan\phi'\cos\gamma)}$$
$$[x_2^2 - x_2d\cot\gamma - 0.3d^2\cot^2\gamma]$$
(5.104)

The difference between Eqs. (5.98) and (5.104) is very small and therefore hardly affects the ultimate pressure of the cap. Equation (5.104) is written in an abbreviated form as

$$1.h.s = P_G(\hat{a}_1 \hat{k}_1). \tag{5.105}$$

Now substituting $\tau_0 = B'(\sigma_0 + \sigma_t)^k$ into Eq. (5.88) the equilibrium equation is written as

$$\sigma_{\rm o} \sin \gamma + B' (\sigma_{\rm o} + \sigma_{\rm t})^k \cos \gamma = \overline{P}_{Hi} \sin \gamma - \tau_{Tz} \cos \gamma \qquad (5.106)$$

For a parabolic variation Eq. (5.105) is further written as

$$\sigma_{\rm o}\sin\gamma + B'(\sigma_{\rm o} + \sigma_{\rm t})^k\cos\gamma = \overline{P}_{Hi}\sin\gamma - \frac{3P_G R_x Z_c(d - Z_c)}{d^3}\cos\gamma. \quad (5.107)$$

From Eq. (5.106)

$$\sigma_{\rm o} = \overline{P}_{Hi} - B' (\sigma_{\rm o} + \sigma_{\rm t})^k + \frac{3P_G R_x Z_{\rm c} (d - Z_c)}{d^3} \cot \gamma$$
(5.108)

Substituing σ_{o} and σ_{t} into Eq. (5.87)

$$P_G = \frac{2}{\left(x_2 - d\cot\gamma\right)^2} \int_{x_2 - H\cot\gamma}^{x_2} \left[B'(\sigma_0 + \sigma_1)^k \tan(-\sigma_0)R_x dR_x\right]$$

$$=\frac{1}{\left(x_2-d\cot\gamma\right)^2}\left[B'(\sigma_0+\sigma_t)^k\tan\gamma-\sigma_0(2x_2d\cot\gamma-d^2\cot^2\gamma)\right] \quad (5.109)$$

Since binomial terms exist in Eq. (5.109), the solution depends upon the variables such as $\sigma_0^2 \ge \sigma_t^2$.

Case (C) Biaxial Compression State

Equation (5.86) is utilised for the value of τ_0 , hence the same equation is written as

$$\sigma_{\rm o}\sin\gamma + \left[C_1\left(\sigma_{\rm o} + \frac{1}{3}\sigma_{\rm o}\right)\right]\cos\gamma = \overline{P}_{Hi}\sin\gamma - \tau_{RZ}\cos\gamma \qquad (5.110)$$

where

$$C_1 = \sqrt{2L_1} - \frac{\sqrt{2}(R_c - 1)}{2R_c - 1}.$$

Therefore

$$\sigma_{\rm o} = \frac{1}{= (C_1 \cos \gamma + \sin \gamma)} \left[\overline{P}_{Hi} \sin \gamma - \tau_{Rz} \cos \gamma - \frac{1}{3} C_1 \sigma_{\rm c} \cos \gamma \right].$$
(5.111)

The value of P_{G} is computed as

$$P_{\rm G} = \frac{2}{(x_2 - d\cot\gamma)^2} \int_{x_{2-d\cot\gamma}}^{x_2} \left[C_1 \left(\sigma_{\rm o} + \frac{1}{3} \sigma_{\rm o} \right) - \sigma_{\rm o} \right] R_x dR_x \qquad (5.112)$$

or

$$P_{G}(x_{2} - d\cot\gamma)^{2}$$

$$= \left\{ \left[+\frac{1}{3}C_{1}\sigma_{c}d\cot\gamma(2x_{2} - d\cot\gamma) \right] + \frac{(c_{1} - 1)}{c_{1}\cos\gamma + \sin\gamma} \left[\overline{P}_{Hi}\sin\gamma - \tau_{RZ}\cos\gamma - \frac{1}{3}c_{1}\sigma_{c}\cos\gamma \right] \right\}.$$
(5.113)

(i) For a case of uniform shear stress distribution

$$\tau_{RZ} = \frac{1}{2} \frac{P_G R_x}{d}.$$

$$P_G = \frac{\overline{S}_1}{\left\{S_2 + \frac{(C_1 - 1)}{2d} R_x \cdot \overline{S}_3\right\}}.$$
(5.114)

(ii) For a case of parabolic stress distribution

$$\tau_{RZ} = \frac{3P_G R_x Z_c (d - Z_c)}{d^3}$$

$$P_G = \frac{\overline{S}_1}{\left\{ \overline{S}_2 + \frac{3(C_1 - 1)(Z_c (d - Z_c))}{d} \cdot R_x \cdot \overline{S}_3 \right\}}$$
(5.115)

where

$$\overline{S}_{1} = \left\{ \frac{1}{3} C_{1} \sigma_{c} d\cot\gamma (2X_{2} - d\cot\gamma) + \frac{(C_{1} - 1)}{C_{1}\cos\gamma + \sin\gamma} \times \left[\overline{P}_{Hi} \cdot \sin\gamma - \frac{1}{3} C_{1} \sigma_{c} \cos\gamma \right] \right\}$$

$$\overline{S}_{2} = (x_{2} - d\cot\gamma)^{2} \qquad (5.116)$$

$$\overline{S}_{3} = \frac{\cos\gamma}{(C_{1}\cos\gamma + \sin\gamma)}$$

Case (D): Combined Compression-tension State

$$+\tau_{\rm o} = +\sqrt{2} \left(\frac{L}{3} + \frac{2}{3} L_4 \right) \tag{5.117}$$

where

$$L_3 = \frac{1 - R_{\rm t}}{1 + R_{\rm t}}$$
 and $L_4 = \frac{R_{\rm t}}{1 + R_{\rm t}}$

Substituting Eq. (5.117) into Eq. (5.88) the same equation is written as

$$\sigma_{\rm o}\sin\gamma + \sqrt{2}\left(L_3 + \frac{2}{3}L_4\right)\cos\gamma = \overline{P}_{Hi}\sin\gamma - \tau_{RZ}\cos\gamma$$

or

$$\sigma_{\rm o} = \overline{P}_{Hi} - \tau_{RZ} \cot \gamma - \sqrt{2} \left(L_3 + \frac{2}{3} L_4 \right) \cot \gamma.$$
 (5.118)

Similarly Eq. (5.118) is substituted in Eq. (5.87) and the value of P_G is arrived at in the following manner:

$$P_G(x_2 - d\cot\gamma)^2 = \left\{ \sqrt{2} \left(L_3 + \frac{2}{3} L_4 \right) \left(\frac{1}{\sin\gamma\cos\gamma} \right) - \overline{P}_{Hi} + \tau_{RZ}\cot\gamma \right\}$$
(5.119)
$$\left[2X_2 d\cot\gamma - d^2\cot^2\gamma \right].$$

Putting τ_{RZ} terms on the left-hand side

$$P_{G}(X_{2} - d\cot\gamma)^{2} - \tau_{RZ}(2x_{2}d\cot^{2}\gamma - d^{2}\cot^{3}\gamma)$$

$$= \left\{\sqrt{2}\left(L_{3} + \frac{2}{3}L_{4}\right)\left(\frac{1}{\sin\gamma\cos\gamma}\right) - \overline{P}_{Hi}\right\}$$

$$(5.120)$$

$$(2X_{2}d\cot\gamma - d^{2}\cot^{3}\gamma).$$

(i) For a uniform shear stress distribution

$$\tau_{RZ} = \frac{1}{2} \frac{P_G \cdot R_x}{d}$$

$$P_G = \frac{\bar{S}_4}{\bar{S}_2 + \frac{1}{2}\bar{S}_5 \cdot R_x}.$$
(5.121)

(ii) For a parabolic shear stress distribution

$$\tau_{RZ} = \frac{3P_G R_x Z_c (d - Z_c)}{d^3}$$

$$P_G = \frac{\bar{S}_4}{\bar{S}_2 + \frac{3Z_c (d - Z_c)}{d^2} \bar{S}_5 \cdot R_x}$$
(5.122)

where

$$\bar{S}_4 = (2X_2d\cot\gamma - d^2\cot^2\gamma) \left\{ \sqrt{2} \left(L_3 + \frac{2}{3}L_4 \right) \left(\frac{1}{\sin\gamma\cos\gamma} \right) - \bar{P}_{Hi} \right\}$$

$$\bar{S}_5 = (2X_2 - \cot^2\gamma - d\cot^3\gamma).$$
(5.123)

Case (*E*) τ_o *Value from the Hypo-elastic Analysis*

From the hypo-elastic approach discussed earlier the expression for the deviatoric stresses arrived at is

$$\frac{\sigma_3}{\sigma_{\rm c}} = -0.053 - 0.92 \left(\frac{\tau_{\rm o}}{\sigma_{\rm c}}\right)^{1.35}.$$
(5.124)

Adopting the same convention

$$\left(\frac{\tau_{\rm o}}{\sigma_{\rm c}}\right)^{1.35} = 1.09 \frac{\sigma_3}{\sigma_{\rm c}} + 0.058$$

$$\tau_{\rm o} = \sigma_{\rm c}^{1.35} \sqrt{1.09 \frac{\sigma_3}{\sigma_{\rm c}} + 0.058}.$$
(5.125)

In the analysis σ_3 could also be σ_1 and σ_3 whichever is the higher compressive stress. Substituting Eq. (5.125)

$$\sigma_{\rm o} = \bar{P_{Hi}} - \tau_{RZ} \cot \gamma - \left\{ \sigma_{\rm c}^{1.35} \sqrt{1.09\sigma_3/\sigma_{\rm c} + 0.058} \right\} \cot \gamma \qquad (5.126)$$

Now the value of P_G is calculated on the lines suggested above

$$P_{G} = \frac{2}{(X_{2} - d\cot\gamma)^{2}} \int_{x_{2} - d\cot\gamma}^{x_{2}} \left\{ \left(\sigma_{c}^{1.35} \sqrt{\frac{1.09\sigma_{3}}{\sigma_{c}}} + 0.058 \right) \tan\gamma - \sigma_{o} \right\} R_{x} dR_{x} (5.127)$$

or

$$P_G(\bar{S}_2) = \left\{ (\bar{S}_6) \left(\frac{1}{\sin \gamma \cos \gamma} \right) + \tau_{RZ} \cot \gamma - \bar{P}_{Hi} \right\} (2X_2 d \cot \gamma - d^2 \cot^2 \gamma) (5.128)$$

(i) For a uniform shear distribution

$$\tau_{RZ} = \frac{1}{2} P_G \frac{R_x}{d}$$

$$P_G = \frac{\bar{S}_7}{(\bar{S}_2 - \frac{1}{2}\bar{S}_5.R_x)}$$
(5.129)

(ii) For a parabolic shear distribution

$$\tau_{RZ} = \frac{3P_G R_x Z_c (d - Z_c)}{d^3}$$

$$P_G = \frac{\bar{S}_7}{\bar{S}_2 = \frac{3Z_c (d - Z_c)}{d^2} . \bar{S}_5 . R_x}$$
(5.130)

where

$$\bar{S}_7 = \left\{ (\bar{S}_6) \left(\frac{1}{\sin \gamma \cos \gamma} \right) - \bar{P}_{Hi} \right\} (2X_2 d \cot \gamma - d^2 \cot^2 \gamma)$$

$$\bar{S}_6 = {}^{1.39} \sqrt{(1.09\sigma_3/\sigma_c + 0.058)} . (\sigma_c)$$
(5.131)

$$\pm \sum_{i=1}^{n} (P_{Hi} \cdot y_i + F_{vi} \cdot R_i) + 2(R_E - n_p R_p \sin \phi)$$
$$\times \left[\sum_{Z_B=1}^{n} \left\{ (A'_{hp} E_s \varepsilon_Z K') + P_G H_I R_I + 2A'_{sb} \sigma_{yb} (d_1 - \dot{x}) A''_{sb} \sigma_{scy} (d_1 - d') \right\} \right]$$

The barrel walls are constructed on top of bottom caps in lift and bays generally not exceeding 2 m. During this process it is impossible to avoid a congestion of embedded components. In these regions it is difficult to achieve a full compaction of concrete and hence the possibility of using high workability concrete mixes, secondary grouting procedures and super-plasticising admixtures cannot be ruled out. Individual bays in the walls and top caps are kept free of 4harp discontinuities. Around all embedded components including cooling pipes, aggregates with low coefficients of expansion and low long-term shrinkage are adopted. The sequence of concrete casting is chosen which is conductive to acceptable distributions of tensile strain as and when the vessel concrete cools.

5.16 Quality Assurance and Control

Quality assurance in any applied science and engineering project is an essential task. It is a disciplined approach in the provision of systems and components of nuclear power plants. The main objectives for the vessel are to ensure that each part of the vessel manufacture is assembled, inspected, tested and operated strictly in accordance with the performance requirements, reliability and safety codes and the designers' intent. The quality control is those quality assurance actions which provide a means to control measure and monitor the characteristics of the vessel throughout its life. The quality assurance in practice embodies formal documentation and procedures:

- (a) Design control.
- (b) Instructions, procedures and drawings.
- (c) Identification and control of special monitoring processes including material equipment, inspection and test control.
- (d) Operating and maintenance manual.
- (e) Quality performance records of liners, penetrations, closure members, prestressing system, reinforcement and concrete under mechanical, thermal and creep loading effects.
- (f) Records to monitor and control the instrumentation of the vessels. Types of instruments embedded are the strain, stress, deformation and temperature and crack gauges which determine the general behaviour of the vessel. Other special instruments load cells for monitoring prestress level; moisture gauges and gas detectors for concrete and the liner, respectively, need quality performance and control.
- (g) Periodic checks for mechanical damage, variation of pressures around the cooling circuits and the safety valve accumulation pressure insulation and the difference between test and operating temperature are all part of surveillance and quality control.

5.17 Conclusions

In this chapter a step-by-step review of the literature pertaining to the analysis, design and model testing of the prestressed concrete reactor pressure vessel is given. The author has looked in some detail at methods of analysing the operational and overload behaviour of these vessels. Vessel component designs are given together with a relevant design data of some of the existing vessels. The methods of analysis discussed provide tools which could prove useful in the future development and monitoring of the existing vessels. The comparative study of analytical and model analysis validates the design and overload performance of these vessels fairly accurately. An emphasis is given on the monitoring and quality assurance of these vessels. Since any vessel has not completed its life, many more predictions in future will be made using site monitoring data. Using these analyses and in the light of new available data, the exact operational and overload performances can be safely predicted on the lines suggested earlier.

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Chapter 6 A Complete Manual Design Analysis of Concrete Containment Vessel (Building) Using American Practices and Codes

6.1 Introduction

A comprehensive analysis is related to these structures has been given in this text: Design loads, material properties and other design specifications and parameters have been thoroughly explained. In this chapter, preliminary design calculation for the containment based on limits state concept are given using U.S Regulations and codes. One typical case of BELLEFONTENUCLEAR PLANT of the TVA is considered. Design calculations for other kinds of PWR shall be carried out on the same line using new design parameters and guide-lines. For detailed analysis a reference is made to the following comprehensive paper by author.

'Containment Vessel Design And Practice' -Annals of Nuclear energy. Pergamon Press Ltd., Vol1.No. 2, pp. 107–181(1982)

The geometry and other parameters are based on the information given by the TVA(USA). They have been taken into consideration. The drawings given by TVA are gracefully recorded. The author took a great pain to interpret the data given in Imperial units and then convert them using SI units. The calculations carried out seems to be a final check o the TVAdesign and in conformity to the safely analysis demanded by the NUCLEAR Regulatory Commission (NCR) of the USA and the additional work based on local requirements of the TVA. Based on the requisite guidelines (N4-50-D702) the design of the annulus and auxiliary structures is included. Both the barrel walls and the dome have been designed as prestressed concrete structures integrated fully. Hence a complete manual design makes this entire chapter extremely useful prior to.

6.2 Geometry And Design Parameters Adopted by the TVA

Figures 6.1 and 6.2 show the vertical presentation and plan of the containment which are self explanatory as far as the geometry is concerned.

Secondary Containment. This category I reinforced concrete structures consists of a cylinder wall having a 162 ft, (49.37 m), inside diameter which is



Fig. 6.1 Vertical presentation (with compliments from TVA)

capped with a ring girder and a 18-in., (457 mm), thick circular dome. The base of the cylinder wall is 2'6", (0.725 m), thick at EL. 620.0 where it is anchored into an extension of the tendon gallery top slab. The wall decreases in thickness linearly from EL. 620.0 to EL. 635.0 where the wall is 18 in., (457 mm), thick. The 18 in., (457 mm), thick cylinder extends above EL. 635.0 approximately 237 ft, 72.214 m, to the ring girder. The top inside face of the dome is approximately 280 ft, (85.34 m), above the EL. 62.0 base slab.

elevations

Note 'C'. The typical dome tendon spacing is 978 mm measure horiz: the final prestressing force for each tendon group is 5453.25 KN/m.

Purpose of this structure is to minimize off-site radiation dosage which might occur during certain atmospheric conditions. The structure also serves to protect the mechanical and electrical systems, which pass through the annulus enroute to the Auxiliary Building, from catastrophic effects of earthquake, tornado, and flood.





Fig. 6.2 (continued)



Fig. 6.2 (continued)



Fig. 6.2 (continued)

The TVA structure has been sealed with PVC seals to prevent ingress of water at construction joints below El 625.0. PVC seals shall also be provided across the expansion joints at the bottom slabs and the exterior walls of the Auxiliary Building. The seals into exterior walls shall extend to EI 646.5.

All doors and openings connecting the secondary containment and the Auxiliary Building have been sealed to maintain a vacuum pressure in the annulus between the primary and secondary containment.

Where this structure supports slabs in the annulus, care has be taken to insure minimum resistance from these slabs by the use of expansion joints between the cylinder wall and the slabs. In addition, low friction bearing pads have been used under the slab support steel at the steel brackets on the primary containment wall to insure that there is essentially no interaction between the primary and secondary containment.

Where the walls and slabs from the Auxiliary Building intersect the secondary containment, fiberous glass joint filler material has been used to separate the structures to allow for seismic movement. The material is intended to be held in place by the concrete pouring pressure. This material will provide adequate sealing in areas that are subjected to low pressure purging.

6.2.1 Annular Structures

6.2.1.1 El 666.0 Shield Slab

This 2-ft (0.61 m) thick slab extends from the refuelling transfer tube compartment slab at approximately the 90^{0} azimuth around the annulus past 0° stopping at the 300° azimuth. Its basic function is to provide radiation shielding for personnel working in the annulus above El 646.0. The slab support steel has been connected to steel brackets on the secondary and primary containment walls. The slab support steel will be free to slide on low friction bearing pads at the steel support bracket on the primary containment wall. Openings have been made in this floor to allow purging underneath. The openings have been located so that someone walking on the 646.0 floor level will not be exposed, to a radiation stream.

6.2.1.2 Barrier Wall

This wail is located at the 0° azimuth and extends from El 620.0 to El 646.0 levels.

The barrier is designed to protect redundant electrical systems that are required for safe shutdown from the effects of fire, pipe jets, and missiles. The barrier shall have a minimum thickness of 2 ft. (0.61 m).

The barrier has been separated from the primary and secondary containment structures by expansion joints to allow free movement of each structure during earthquake. The barrier has been connected to the El 64.6.0 slab.

6.2.1.3 Primary Shield Door

This 3-ft thick concrete door is approximately 25'-5'' (7.8 m) wide and 24'-6'' (7.47 m) high. It is located at the equipment hatch in the primary containment at the 270° azimuth. The basic function of the door is to provide radiation and tornado borne missile shielding for the equipment hatch opening.

6.2.1.4 Primary Shield Door Support

This structure is located under the equipment access hatch at the 270° azimuth. It consists of a wall, two columns, two beams, and a thin slab. The wall provides door support during normal plant operation. The 300-kip (1334 KN) door is mounted on a rail and opens toward a decreasing azimuth providing access to the primary containment during maintenance operations. A long beam supported by one column provides door support in the open position. The

remaining beam and column allow the door to be moved slightly toward an increasing azimuth to allow for wheel maintenance. The thin slab provides a working surface for door operation and maintenance.

6.2.1.5 Compartment Around the Fuel Transfer Tube

This structure serves primarily as shielding against radioactivity around the refuelling transfer tube. It consists of two side walls and a top slab. The walls and slab are separated from the secondary and primary containments by an expansion joint to allow independent movement of these structures during earthquake. The top slab is concrete plug which can be removed to inspect the transfer tube.

6.2.2 Tendon Gallery and Annulus Maintenance Access

This structure is located at the 214° azimuth, it consists of a vertical shaft extending from grade at El 646.0 down to the horizontal passageways which enter the annulus at El 620.0 and the tendon gallery at El 606.5, respectively.

Steel ladders with safety devices shall extend between horizontal levels and the shafts can serve as a work access to the tendon gallery during tendon installation. After tendon installation a removable structural steel floor at El 620.0 has been installed to provide access to the annulus. The annulus access can be used to bring in the tendon jacks during surveillance testing. The surveillance tests will be performed at one year intervals for the first three years of plant life and at five year intervals thereafter. The annulus access can also serve as the maintenance access for servicing various mechanical systems located in the annulus.

Due to the infrequent use of the access structure, the top cover slab at El 646.25 has been bolted into place and will have lifting eyes such that it can be removed with a small mobile hoist.

The removable floor at El 620.0 shall have a man-hatch to provide access to the tendon gallery for inspection purposes. If it becomes necessary to take large tools or parts into the tendon gallery, the steel floor at El 620.0 may be lifted out to grade.

This structure has been connected to the tendon gallery by construction joints below El 620.0. Above El 620.0, an expansion joint shall be used, to allow independent, movement of this structure and the secondary containment during earthquake.

6.2.3 Applicable Design References

- 1. Bellefonte PSAR
- 2. Concrete Design Standards, Parts II and III ACI 1972. (Revised 2006)

6.2 Geometry And Design Parameters Adopted by the TVA

- 3. General Criteria for Design of Civil Structures (N4-50-D702)
- 4. Civil Design Branch report, "Dynamic Earthquake Analysis of Secondary Containment Structure and Response Spectra for the Attached Equipment - Bellefonte Nuclear Plant (1972) (Revised 1985)
- 5. OEDC Quality Assurance Manual (1972) (Revised 2007)
- 6. American Concrete Institute (ACI) (Revised 2008)
 - ACl 315-65- Manual of Standard Practice of Detailing Reinforced Concrete Structures
 - ACI 318-71- Building Code Requirements for Reinforced Concrete
 - ACI 347-68- Recommended Practice for Concrete Formwork
 - ACI 305-72- Recommended Practice for Hot Weather Concreting
 - ACI 211.1-70 Recommended Practice for Selecting Proportions for Concrete
 - ACI 6114-73- Recommended Practice for Measuring, Mixing, and Placing Concrete
- 7. American Society for Testing and Materials-1972 ASTM Standards (Revised 2008)
- 8. American Society of Civil Engineers (ASCE), Paper No. 3269, "Wind Forces on Structures" (1969)
- 9. Code of Federal Regulations, Title 29, Chapter XVII "Occupational Safety and Health Standards"
- 10. NRC Regulatory Guides
 - No. 1.10 "Mechanical (Cadweld) Splices in Reinforcing Bars of Category I Concrete Structures"
 - No. 1.55 Concrete Placement in Category I Structures
- 11. TVA Construction Specifications
 - G-2 TVA General Construction Specification for Plain and Reinforced Concrete
 - G-30 TVA General Construction Specification Fly Ash for Use as an Admixture in Concrete (1972) (Revised 2007)
 - G-32 TVA General Construction Specification Bolt Anchors Set in Hardened Concrete (1972) (Revised 2007)
- "TVA Report on Wind Analysis of Sequoyah Shield Building," by R.G. Domer and B. C. Giordano(1972) (Revised 2007
- "THERMCYL Thermal Stresses in Reinforced Concrete Cylinders," by R. G. Domer and R. C. Giordano available at TVA (1973)
- "Design of Structures for Missile Impact," Bechtel Power Corporation Report BC-Top-9 (1972)
- 15. Bangash M.Y.H. Shock, Impact & Explosion -Springer Verlag, Heidelberg 2008.
- Bangash M.Y.H. Manual of Numerical Methods in Concrete -Thomas Telford, London (2003)
- 17. Bangash M.Y.H. Earthquake Resistant Buildings-Analysis and Design Springer Verlag, Heidelberg 2010

6.2.4 General Design Requirements and Loads Used by TVA. For Calculations

6.2.4.1 Load Symbols and Definitions

- D = dead load of structure and equipment plus any other permanent loads excluding soil and hydrostatic pressure. An allowance is also made for future permanent loads.
- $-E^* = 1/2$ safe shutdown earthquake resulting from horizontal rock acceleration of 0.09 g (0.09 g vertical).
- *E = safe shutdown earthquake resulting from horizontal rock acceleration of 0.18 g (0.18 g vertical).
- -L = live loads (loads which vary in intensity and occurrence) including movable equipment, soil and hydrostatic pressure loads.
- $-L_c$ = construction live loads (greater than normal operating live loads of a temporary or unusual nature) which occur during construction.
- R_a = pipe reactions under thermal conditions generated by the postulated pipe break and. including R_0 .
- $-R_0$ = pipe reactions during normal operating or shutdown conditions, based on the most critical transient or steady state conditions.
- $-T_a$ = thermal loads due to temperature differences under accident conditions,
- $-T_0$ = thermal loads due to temperature differences under normal operating or shutdown conditions, based on the most critical transient or steady state condition.
- U = required ultimate load capacity of structures.
- -W = wind load as defined
- $-W_t$ = tornado loadings including missiles as defined in the General Design Criteria.
- Y_j = jet impingement equivalent static load on a structure generated by the postulated break including an appropriate dynamic factor,
- $Y_{\rm m}$ = missile impact equivalent static load on a structure generated by or during the postulated break, pipe whipping, including an appropriate dynamic factor.
- Y_r = equivalent static load on the structure generated by the reaction of the broken high-energy pipe during the postulated break including an appropriate dynamic factor.

In determining an appropriate equivalent static load for Y_{j} , Y_m and Y_r , elasto-plastic behaviour may be assumed with appropriate ductility ratios and as long as excessive deflections will not result in loss of function.

6.2.5 Earthquake Loads

Earthquake effects on these concrete structures shall be determined by using the appropriate structural response prepared by the Civil Engineering Branch of the TVA or any other organisations.

6.2.6 Temperature Loads (Concrete Members)

The surface temperature and the gradient through the concrete members for normal operation and accident conditions shall be calculated by the Nuclear Systems Engineering Group of the Mechanical Engineering Branch. These gradients will be used with the THERMCYL computer program or a similar method to compute the thermal stresses. Currently many advanced computer programs are being used. Program ISOPAR or any other 3D-hybrid F.E. Nonlinear Computer Program.

6.2.7 Jet Loads and Pipe Restraint Loads

Restraints for steam and other systems piping will be located by the Bellefonte Project Mechanical Design Sections and the Civil Engineering Branch will evaluate the design criteria for determining loads.

Jet forces on the structure from accidental pipe breaks shall be calculated by the following formulas:

- -F = 1.26 K PA for steam or flashing liquid
- -F = 2.0 K PA for subcooled nonflashing liquid
- -F = total force for flexural design or shear design
- P = maximum operating pressure
- -A =internal area of pipe
- -K = dynamic load factor for flexure, peripheral shear, and diagonal tension.

Pressures for piping systems shall be obtained from the Project Mechanical Design Sections.

Three types of pipe breaks shall be postulated and are defined below:

- Circumferential rupture. This type of pipe break exists when a pipe breaks circumferentially and the ends at the break displace laterally such that a full diameter jet from each broken end is possible.
- Longitudinal split. The area of this type of break is equal to the internal crosssectional area of the pipe and is two inside diameters long. The shape may be assumed to be a narrow rectangle, circular, or elliptical for analyses purposes.
- Through-wall leakage cracks are not postulated in high energy piping systems, except where these lines are routed in the vicinity of vital electrical equipment. Fluid flow from a through-wall leakage crack may be based on a circular opening with an area equal to an equivalent rectangular opening of one-half the pipe inside diameter in length and one-half the wall thickness in width and oriented parallel to the pipe flow axis.
- A jet shall be assumed to expand 10 degrees each direction from the sides of the break for purposes of determining an impact area. The load F shall be assumed to act uniformly over the impact area.

When designing for jet forces, local yielding is permitted which will reduce the dynamic effects of the force on the structures. The dynamic load factor, K, shall be determined by using a ductility ratio $(Y_{\rm m}/Y_{\rm el})$ as described in Structural Dynamics by J. M. Biggs, 1961, pp. 69–81 and 222–223 or elsewhere.

- $-Y_{\rm m}$ = maximum permissible deflection of the structure
- $-Y_{el}$ = deflection of the structure at yield strain of the reinforcing steel

 $Y_{\rm rn}$ and $Y_{\rm el}$ shall be determined by moment rotation concepts as outlined in "Limit Design for Structural Concrete," Journal of the PCA Research and Development Laboratories, May 1959, p. 14–23.

6.2.8 Load Combinations

The load combinations used by the TVA are identical to ones recommended in Chapter 2. Table 6.1 gives a brief on load combinations and load factors for secondary containment, the following special live loads have been adopted with appropriate load factors as given in table 6.1.

6.2.9 Secondary Containment

6.2.9.1 Special Live Loads

The following loads shall be treated as live loads using the appropriate load factors as given in Table 6.1. Snow. The structure shall be designed for a 20 psf (0.958KN/m^2) snow load on the dome.

| Table 0.1 Eoud Combinations and Eoud Tactors | |
|--|---|
| 1. Normal operating | $U = 1.14D + 1.7L + 1.3T_0 + 1.3R_0$ |
| 2. Seismic operating | $U = 1.14D + 1.7L + 1.9E + 1.3T_0 + 1.3R_0$ |
| 2a. Dead and seismic | U = 1.2D + 1.9E |
| 3. Normal wind | $U = 1.4D + 1.7L + 1.7W + 1.3T_0 + 1.3R_0$ |
| 3a. Dead and wind | U = 1.2D + 1.7W |
| 11. Extreme seismic | $U = D + L + T_0 + R_0 + E'$ |
| 5. Extreme wind | $U = D + L + T_0 + R_0 + W_t$ |
| 6. Extreme accident | $U = D + L + T_{\rm a} + R_{\rm a}$ |
| 7. Seismic/accident | $U = D + L + T_{a} + R_{a} + 1.25E + Y_{r} + Y_{j} + Y_{m}$ |
| 8. Extreme seismic/accident | $U = D + L + T_{a} + R_{a} + E' + Y_{r} + Y_{j} + Y_{m}$ |
| 9. Temporal7 construction | $U = 1.4D + 1.4L_{\rm c}$ |
| 10. Probable maximum flood | U = D + L |

 Table 6.1
 Load Combinations and Load Factors

Notes:

1. All components that constitute these structures shall be designed to resist all applicable loading combinations.

With the exception of the load factors given in Table 6.1, this structure shall be designed in accordance with the ultimate strength design provision of ACI 318-71.

- 2. In combinations 6, 7, and 8, the maximum values of T_a , R_a , Y_j , Y_r , and Y_m ' including an appropriate dynamic factor shall be used unless a time history analysis is performed to justify otherwise.
- 3. For combinations 7 and 8, local stresses due to the concentrated loads Y_r , Y_j , and Y_m , may exceed the allowable provided there will be no loss of function of any safety-related system.
- 4. Where *L* reduces the effects of other loads it shall be taken as the minimum possible value.
- 5. In addition to the above, combination 1 will also be designed for temperature and shrinkage, in place of 1.3 T_0 , using TVA "Concrete Standards for Temperature and Shrinkage Reinforcement" as the criteria.

<u>Water</u>. Water pressure shall be assumed outside the Auxiliary Building to El 625.0 for design purposes. The dynamic effect on the water due to earthquake shall be considered in accordance with N4-50-D702.

<u>Earth.</u> Design for soil pressure shall be based on soil backfiled to El 646.0 in all areas that are not adjacent to the Auxiliary Building. Surcharge on the soil surface shall be 200 psf (9.58 KN/m^2) except where larger surface loads are known to exist, The dynamic effect on the earth due to earthquake shall be considered.

<u>Vacuum.</u> The structure shall he designed to resist a theoretical vacuum of 5.2 psf (0.2491 KN/m^2) during normal operation with a design value of 10.4 psf (0.477 KN/m^2) to allow for marginal error.

6.2.10 Annular Structures

6.2.10.1 El 646.0 Shield Slab

Since no equipment is supported by this floor it shall be designed for a 100 psf (4.79 KN/m^2) live load.

Analysis may be done by considering the floor as a simple span in the circumferential direction, Temperature and shrinkage steel shall be placed in the radial direction.

6.2.10.2 Barrier Wall

Analysis of this wall may be done by conventional methods.

6.2.10.3 Primary Shield Door

This door shall be designed to withstand the stresses produced by the credible tornado-borne missiles listed in the General Criteria for Design of Civil Structures, N14-50-D702. For further design considerations by others see Shield Door at Equipment Access Hatch Criteria, N4-MAD740C.

6.2.10.4 Primary Shield Door Support

This structure shall be designed to carry the moving door load, plus a 100 psf (4.79 KN/m^2) live load on the slab outside the door area. The wall shall be designed to take the vertical load that could possibly occur during the removal of a steam generator. A horizontal load of 5% of the weight shall be assumed to occur simultaneously with the vertical load on the wall.

This structure shall be analyzed by a conventional frame analysis taking account of moment distribution, flexibility and stiffness methods.

6.2.10.5 Compartment Around the Fuel Transfer Tube

The top slab shall be designed for a 100 psf (4.79 KN/m^2) live load.

6.2.11 Geometrical Analysis

6.2.11.1 Elliptical Dome of The Reactor Containment

General

Developmental Analysis and computer Program exist in this text in Chapter 3. In addition the formulation under this section has been provided by the TVA.

Geometric Analysis of Elliptical Dome

By concentric circles method, points on the elliptical curve of minor axis "b" and major axis "a" can be located graphically as followed:

Standard elliptic EQ

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} \tag{6.1}$$

From figure

$$x = a\sin\phi \tag{6.1a}$$

$$y = b\sin\phi \tag{6.1b}$$

For x - 14 and y - 5



Fig. 6.3 Concentric circles for elliptical curve development

Elliptical dome

$$a = 67.5'(20.574 m)$$

 $b = 39.75'(12.116 m)$

Method of Obtaining Arc Length of A Elliptical Curve



Fig. 6.4 Method of obtaining arc length of a elliptical curve For length of a plane curve:

$$L_A^B = \int_A^B \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx \tag{6.2}$$

Equation of an ellipse can be written as

$$y^2 = b^2 - \frac{b^2 x^2}{a^2} \tag{6.2a}$$
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Taking derivative

$$2ydy = -\frac{2b^2}{a^2} \times dx$$
$$\frac{dy}{dx} = -\frac{b^2x}{ya^2}$$
$$\left(\frac{dy}{dx}\right)^2 = \left(\frac{b^2x}{ya^2}\right)^2 = \frac{b^4x^2}{y^2a^4} = \frac{b^4x^2}{\left(b^2 - b^2\frac{x^2}{a^2}\right)a^4} = \frac{b^2x^2}{a^4 - a^2x^2}$$
(6.2b)

Substituting

$$L_{A}^{B} = \int_{A}^{B} \sqrt{1 + \frac{b^{2}x^{2}}{a^{4} - a^{2}x^{2}}} dx$$

=
$$\int_{A}^{B} \sqrt{1 + \frac{a^{4} - a^{2}x^{2} + b^{2}x^{2}}{a^{4} - a^{2}x^{2}}} dx$$
 (6.2c)

Letting $x = a \sin \phi$

$$\mathrm{d}x = a\cos\phi d\phi$$

$$L_{A}^{B} = \int_{A}^{B} \sqrt{\frac{a^{4} - a^{2}(a\sin\phi)^{2} + b^{2}(a\sin\phi)^{2}}{a^{4} - a^{2}(a\sin\phi)^{2}}} (a\cos\phi d\phi)$$
(6.2d)

$$L_{A}^{B} = \int_{A}^{B} \sqrt{\frac{a^{4} + (b^{2}a^{2} - a^{4})\sin^{2}\emptyset}{a^{4}(1 - \sin^{2}\emptyset)}} a\cos\phi d\phi$$
(6.2e)

Since

$$a = 67.5'(20.574 m)$$

$$b = 39.75'(12.118 m)$$

$$b = .58889a$$

$$b^{2} = .34679a^{2}$$

$$L_{A}^{B} = \int_{A}^{B} \sqrt{\frac{a^{4} + (.34679a^{4} - a^{4})\sin^{2}\phi}{a^{4}(\cos^{2}\phi)}} a \cos\phi d\phi$$

$$= \int_{A}^{B} \sqrt{\frac{a^{4}(1 - .65321\sin^{2}\phi}{a^{4}\cos^{2}\phi}} a \cos\phi d\phi$$

$$a \int_{A}^{B} \sqrt{1 - .65321\sin^{2}\phi} d\phi$$

$$L_{A}^{B} = aE_{1}$$

(6.2f)

where

$$E_1 = \int_0^{\pi/2} \sqrt{1 - 0.65321 \sin^2 \phi}; \, \mathrm{d}\phi \tag{6.2g}$$

and

$$\frac{\sqrt{a^2 - b^2}}{a} = k$$

$$k = 0.65321$$

$$k = \sqrt{0.65321} = 0.80821$$

$$\sin \theta = k$$

$$\theta = \sin^{-1}k = \sin^{-1}(0.80821) = 53^{\circ}55'$$

$$use \ \theta = 54^{\circ}$$

Using CRC table (table269 page) $\theta = 53^{\circ}55'\theta = 90^{\circ}$ Handbook $E_1 = 1.2681$ One quarter length of an ellipse

$$L_0^{\pi/2} = aE_1 = 67.5 \times 1.2681$$

 $L = 85.59675 \text{ft} \approx 85.6 \text{ ft}(26.06 \text{ m})$

By approximation

$$L = \frac{2\pi}{4} \sqrt{\frac{a^2 + b^2}{2}} = 87 \text{ ft} (26.5176 \text{ m})$$

Table 6.2 is prepared for the elliptical dome (CRC Math tables @ $E_1 \theta = 54^{\circ}$ and using interpolation.

Dome with Portions of Elliptical, Spherical and Others

General. Here analysis is presented where various segments of ellipse.

Geometrical Analysis.

Let

$$l_{\rm e} = \text{length of elliptical portion}$$

 $l_{\rm s} = \text{length of spherical portion}$
 $l_{\rm r} = \text{length of remaining portion}$
 $L_{\text{Total}} = l_e + l_s + l_r$
(6.3)

| | Table 6.2 ϕ vers | us θ values of E_1 | $\theta = 54^{\circ}$ | |
|---------|------------------------------|-----------------------------|---------------------------------|--|
| ф | $\frac{b=54}{F}$ | ф | $\frac{\theta = 54^{\circ}}{E}$ | |
| φ | 0175 | φ 16 | 7502 | |
| 2 | .0175 | 40 | .7502 | |
| 2 | .0349 | 4/ | .7043 | |
| 5 1 | .0323 | 40 | .7702 | |
| 4 5 | .0090 | 49 50 | ./922 | |
| 5 | .0072 | 50 | .8000 | |
| 0 | .1040 | 52 | .819/ | |
| 0 | .1220 | 52 | .0332 | |
| 0 | .1393 | 55 | .040/ | |
| 9 10 | .1300 | 54 | .8000 | |
| 10 | .1/39 | 33 57 | .8/30 | |
| 11 | .1912 | 30 57 | .8800 | |
| 12 | .2084 | 5/ | .8988 | |
| 13 | .2230 | 58 | .9116 | |
| 14 | .2427 | 59 | .9243 | |
| 15 | .2598 | 60 | .9367 | |
| 16 | .2/69 | 61 | .9492 | |
| 17 | .2939 | 62 | .9614 | |
| 18 | .3108 | 63 | .9736 | |
| 19 | .3277 | 64 | .9856 | |
| 20 | .3445 | 65 | .9973 | |
| 21 | .3612 | 66 | 1.0093 | |
| 22 | .3779 | 67 | 1.0210 | |
| 23 | .3945 | 68 | 1.0326 | |
| 24 | .4110 | 69 | 1.0441 | |
| 25 | .4274 | 70 | 1.0555 | |
| 26 | .4439 | 71 | 1.0668 | |
| 27 | .4601 | 72 | 1.0780 | |
| 28 | .4763 | 73 | 1.0891 | |
| 29 | .4924 | 74 | 1.1001 | |
| 30 | .5084 | 75 | 1.1110 | |
| 31 | .5243 | 76 | 1.1221 | |
| 32 | .5401 | 77 | 1.1326 | |
| 33 | .5558 | 78 | 1.1433 | |
| 34 | .5714 | 79 | 1.1540 | |
| 35 | .5870 | 80 | 1.1646 | |
| 36 | .6024 | 81 | 1.1750 | |
| 37 | .6177 | 82 | 1.1856 | |
| 38 | .6329 | 83 | 1.1960 | |
| 39 | .6479 | 84 | 1.2064 | |
| 40 | .6629 | 85 | 1.2167 | |
| 41 | .6777 | 86 | 1.2254 | |
| 42 | .6925 | 87 | 1.2373 | |
| 43 | .7071 | 88 | 1.2475 | |
| 44 | .7216 | 89 | 1.2578 | |

45

.7360

90

1.2681

With reference to calculation "length of Elliptical Dome", by DQL on 3-10-72.

$$l_{eA}^{B} = aE_{1} = aE_{1B} - aE_{1A} = a(E_{1B} - E_{1A})$$
(6.3a)

$$E = \int_0^0 \sqrt{1 - k^2 \sin^2 \phi} d\phi$$

$$k = \frac{\sqrt{a^2 - b^2}}{a} = \frac{\sqrt{69.125^2 - 41.375^2}}{69.125} = \frac{\sqrt{3066.375}}{69.125}$$
(6.3b)

$$k = \frac{55.37485}{69.125} = 0.8011 \tag{6.3c}$$

Limit
$$A = 90^{\circ} - \tan^{-1} \left(\frac{40'}{41.375' - 7.64'} \right)$$

 $\phi = A = 90^{\circ} - 49.857 = 40.143^{\circ}$

Limit $B = \phi = 90^{\circ}$

At
$$\phi = 40.143^{\circ}, E_{1A} \approx .666$$

At $\phi = 90^{\circ}, E_{1B} = 1.275$ (6.3d)

$$l_{eA}^{\ B} = (69.125)(1.275 - 0.666) = (69.125)(.609) = 42.097'(12.831 m)$$
 (6.3e)

 $\theta = \sin^{-1} k = 53^{\circ} 14$

$$l_{s} = \frac{\pi R}{180^{\circ}}(\theta_{3}) = \frac{(3.1416)(102.33)}{180^{\circ}}(12.8815^{\circ}) = 23.02'(7.165 m)$$
$$l_{s} = \frac{R' - 60'}{\cos \theta_{4}}$$
(6.3f)

Where

 $\mathbf{R}' = \text{distance from } \pounds \text{ of dome to external edge of ring girder}$ (6.3g)

$$=\frac{72.5'-60'}{\cos(35.8975)}=\frac{12.50'}{0.8101}=15.43'(4.7031\ m)$$
(6.3h)

$$L_T = 42.100' + 23.02' + 15.43' = 80.55'(24.552 m)$$

Compute Elev. of Anchorage Point on Ring Girder:

$$h = \sqrt{(15.43)^2 - (12.50)^2} = 9.05'(2.7858 m)$$

$$E_1 = 871.44 - 9.05 = 862.39 = Anch.elev.$$
(6.3i)

6.2.11.2 Equations of Curvature for Elliptical Dome at specific Location

Figure 6.5 gives the curvature phenomenon of the elliptical dome at specific location.

Ellipsoid at right has the equation

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

where

$$|x| \le a, |y| \le b, |z| \le c$$

If a plane x-z cut through the ellipsoid @ y = 0, then the equation reduced to:

$$\frac{x^2}{a^2} + \frac{z^2}{c^2} = 1 \tag{6.4}$$

which is the equation of ellipse.

Further, if the plane x - z cuts through the ellipsoid @ y = y, where $y_1 < b$, then the equation of an ellipsoid becomes:

$$\frac{x^2}{a^2} + \frac{y_1^2}{b^2} + \frac{z^2}{c^2} = 1$$

$$\therefore \frac{y_1^2}{b^2}$$

$$= constant$$
(6.4.1)



Fig. 6.5 A curvature at specific location of the elliptical domes. (a) Curvature is xyz. (b) Plan

6.2 Geometry And Design Parameters Adopted by the TVA

$$\frac{x^2}{a^2} + \frac{z^2}{c^2} = 1 - \frac{y_1^2}{b^2}$$
(6.4.2)

or
$$\frac{x^2}{a^2(1-\frac{y_1^2}{b^2})} + \frac{z^2}{c^2(1-\frac{y_1^2}{b^2})} = 1$$
 (6.4.3)

Reference to Fig. 6.5b section A1 - A1 cut the ellipsoid at Y' = 0 then the section has the equation of the form:

$$\frac{x_1^2}{a^2} + \frac{z^2}{c^2} = 1.0$$

Let

$$a = 69.125'(21.069 m)$$

$$c = 41.375'(12.61 m)$$

$$x_1 = 40.0'(12.192 m)$$

Then

$$z^{2} = \frac{a^{2}c^{2} - c^{2}x^{-2}}{a^{2}}$$
$$z^{2} = \frac{69.125)^{2}(41.375)^{2} - (41.375)^{2}(40)^{2}}{(69.125)^{2}}$$
$$z = 33.7441$$
ft(10.285 m)

Let section A2 - A2 cut the ellipsoid @ $y_1 = 26.25'$, the section has an equation:

$$\frac{x_2^2}{a^2(1-\frac{y_1^2}{b^2})} + \frac{z^2}{c^2(1-\frac{y_1^2}{b^2})} = 1$$
(6.4.4)

where

$$x_2 = \sqrt{(40)^2 - (26.25)^2} = \sqrt{910.9375} = 30.1817(9.2 m)$$

b = 69.125'(21.069 m)

Solve for

$$\frac{x_2^2}{a^2 \left(1 - \frac{y_1^2}{b^2}\right)} = \frac{910.9375}{(69.125)^2 \left(1 - \frac{26.25^2}{69.125^2}\right)} = \frac{910.9375}{(69.125)^2 (1 - 14421)} = .2228$$

$$c^{2}\left(1 - \frac{y_{1}^{2}}{b^{2}}\right) = (41.375)^{2}(1 - .14421) = (41375)^{2}(.8558) = 1465.0$$
$$0.2228 + \frac{z^{2}}{1465.04} = 1.0$$
$$z^{2} = (1 - .2228)(1465.04)$$
$$z^{2} = (9.7772)(1465.04) = 1138.6290$$
$$z = 33.7435(10.285 m)$$

Radius of curvature of section A2 - A2: Major axis $a = \sqrt{(69.125)^2 - (26.25)^2} = \sqrt{4089.2031} = 63.95(19.492 m)$ Major axis: Previously where $x^2 = 30.1871$:

$$0.2228 + \frac{z^2}{1465.04} = 1.0$$

where $x^2 = 0$

$$z^2 = 1465.04$$

 $c = z = \sqrt{1465.04} = 38.28'(11.67 \text{ m})$

Find radius of curvature @ pt. z = 33.7441

$$a = 63.95'(19.442 m)$$

$$c = 38.28'(11.69 m)$$

$$x_2 = 30.1817'(9.2 m)$$

$$z = 33.7435'(10.28 m)$$

$$R_{2} = \text{ radius of curvature } = \frac{(a^{4}z^{2} + c^{4}x_{2}^{2})^{1/2}}{c^{2}}$$
$$= \frac{[(63.95)^{4}(33.7441)^{2} + (38.28)^{4}(30.1817)^{2}]^{1/2}}{(38.28)^{2}} = 98.8930'(30.1426 \text{ m})$$

Radius of Curvature @ pt. $x^2 = 0, z = 38.28'(11.668 m)$

$$R_2 = \frac{\left[(63.95)^4 (38.28)^2 + 0\right]^{1/2}}{(38.28)^2} = 106.834'(32.563 m)$$

Angle formed by C.G. Tendon with respect to the Horizontal Axis of section -A2:

$$x_{2} = \sqrt{60^{2} - 26.25^{2}} = \sqrt{2910.9375} = 53.953(16.4449 \ m)$$

$$\cos \theta_{2} = \frac{53.9531'}{98.893'} = .54539$$

$$\theta_{2} = 56^{\circ} - 57'$$

$$\theta_{4} = 90^{\circ} - (56^{\circ} - 56' - 00)$$

$$\theta_{4} = 33^{\circ} - 04'$$

$$\sin \theta_{1} = \frac{30.1817'}{98.893'} = .3052$$

$$\theta_{1} = 17.77^{\circ} = 17^{\circ} - 46' - 13$$



$$\theta_3 = 90^\circ - (\theta_2 + \theta_1)$$

$$\theta_3 = 90^\circ - (56^\circ - 57' - 00 + 17^\circ - 46' - 13)$$

$$\theta_3 = 90^\circ - (74^\circ - 43' - 13) = 15^\circ - 14'$$

Length of Tendon of Section A2-A2:

$$l_{eA}^{\ B} = a(E_B - E_A)$$

Knowing that

$$a = 63.95'(19.492 m)$$

$$b = c = 38.28'(11.07 m)$$

$$k = \frac{\sqrt{a^2 - b^2}}{a} = \frac{\sqrt{(63.95)^2 - (38.28)^2}}{63.95}$$

$$k = .8011. \ \theta = \sin^{-1}(.8011) = 53.75^{\circ}$$

Limit $A = \phi = 90^{\circ} - \tan^{-1}\left(\frac{30.1817}{33.7441}\right) = 90^{\circ} - \tan^{-1}(0.8944)$ = 90° - 41.8° = 48°11′24

$$E_A \approx 0.7823$$

 $\text{Limit } B = \phi = 90^{\circ}$

$$E_B = 1.2750$$

$$l_{eA}^{B} = 63.95(12.750 - .7820) = 63.95(.4930) = 31.53'$$

$$l_s = \frac{\pi R_2 \theta_3}{180^\circ} = \frac{(3.1416)(98.893)(15.2777)}{180^\circ} = 26.37'(8.038 m)$$

$$l_r = \frac{12.65'}{\cos \theta_4} = \frac{12.63'}{\cos(33^\circ 030)} = \frac{12.5}{.838195} = 16.86'(4.9577 m)$$

$$L_T = 31.53' + 26.37' + 16.26' = 74.16'(22.604 m)$$

6.2.11.3 A Spheroid Equation

Similar to ellipsoid a spheroid has an equation of the form. A reference is made to Fig. 6.5d.

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

where $a = b = c = r, x^2 + y^2 + z^2 = r^2$



Fig. 6.5d Plan for spheroid

At any section where $y = y_1 = constant$ Now

$$x^{2} = y_{1}^{2} + z^{2} = r^{2}$$
$$x^{2} + z^{2} = (r^{2} - y_{1}^{2})$$

Which is an equation of a circle

$$x_3 = \sqrt{(60)^2 - (52.5)^2} = \sqrt{843.75} = 29.0473'(8.85362m)$$



Fig. 6.5 (e) Section A2 – A2

We have

$$x_3^2 + z^2 = (r^2 - y_1^2)$$

$$r = R_2 = 102.33'(31.190 \text{ m})$$

$$y_1 = 52.50'(16.002 \text{ m})$$

$$z^2 = (102.33)^2 - (52.5)^2 - (29.0473)^2$$

$$z = \sqrt{6871.433} = 82.8941'(25.266 \text{ m})$$

where $x_3 = 0$

$$z^{2} = 102.33^{2} = 52.5^{2} = 7715.178'$$

$$z = \sqrt{7715.178} = 87.836'(26.6273 m)$$

Radius of curvature @ $x_3 = 0, z = 87.836'(26.6273 \text{ m})$

$$R_2 = \frac{\left[(29.0473)^4 (87.836)^2 + (29.0473)^4 (0)\right]^{1/2}}{(29.0473)^2} = 87.836' (26.6273 \, m)$$

Radius of curvature @ $x_3 = 29.0473, z = 82.8941$

$$R_2 = \frac{\left[(29.0473)^4 (82.8941)^2 + (29.0473)^4 (29.0473)^2\right]^{1/2}}{(29.0473)^2} = 87.836'(26.6273 \text{ m})$$

Angle formed by C.G.Tendon with respect to Horizontal Axis of section A3-A3:

$$\cos \theta_2 = \frac{29.0473'}{87.836'} = .3307$$
$$\theta_2 = 10^\circ - 41' - 39''$$
$$\theta_4 = 90^\circ - (70^\circ - 41' - 18'')$$
$$\theta_4 = 19^\circ - 18' - 21''$$

6.2.11.4 Length of the Tendon of Section A3–A3 (DQL)

$$l_e = 0$$

$$l_s = \frac{\pi R_2 \theta_4}{180^\circ} = \frac{3.1416 \times 87.836 \times 19.306}{180^\circ} = 29.60 ft$$

$$l_r = \frac{20.95}{\cos \theta_4} = \frac{20.95}{\cos(19.312)} = 22.20'$$

$$L_T = 29.60 + 22.20 = 51.80 ft (15.79 \text{ m})$$

Similarly this distance can be computed through out.

6.2.11.5 Coordinates for the Tendon Length (DQL) section A3–A3 used possibly for the Infinite Element mesh scheme

Method used

Starting from £ of dome, determine coordinates x,y with respect to the origin of the elliptical curve at L = 18''(457 mm)

$$L = aE_1$$
$$E_1 = \frac{L}{a} = \frac{18''}{67.5 \times 12}$$
$$E_1 = .0222$$

Interpolating

$$\phi = 1.270^{\circ}$$

$$\sin \phi = \sin(1.2701)^{\circ} = 0.2217$$

$$x = a \sin \theta = (67.5)(.02217)$$

$$x = 1.4965'(0.456133m)$$

$$x = 17.9577''$$

$$y = \sqrt{b^2 - \frac{b^2 x^2}{a^2}} = \sqrt{(39.75)^2 - \frac{(39.75)^2(1.4965)^2}{(67.5)^2}}$$

$$39.74022ft = 476.88275'' *$$

Again $\phi R type y = b \cos \phi = 39.75 \cos(1.2701) = 39.74165 ft(12.113255 m)$

476.89982"* checked.

6.2.11.6 TVA Response Curve for Containments Plates No. 6.1–6.3 Were Decided by he TVA Preliminary Earthquake Response Curves



Plate No. 6.1 TVA vessel elevation versus bending moment



Plate No. 6.2 Elevation versus vertical loads. Ground Acceleration $0.18 \text{ G} = r_g$



Plate No. 6.3 Load versus elevation. Ground Acceleration = $0.09 \text{ G}_{1/2}$ safe shutdown

6.3 Design Calculations for Containment Structures

6.3.1 General Criteria

A great deal of substance available in this text to design both primary and secondary containments. The geometry material and loading are always dominant. The decision based on a number of variables has to be made regarding the usage of prestressed or reinforced concrete or perhaps both many primary and secondary containments have been designed in concrete using conventional steel reinforcement and prestressing system to resist loads. Here typical design parameters and prestressing systems adopted for the TVA Containment have been given. Any other geometry and design criteria for a typical vessel of a country must be adopted keeping in mind the methodology given in theses preliminary calculations adopted by the Tennessee Valley Authority (TVA). These calculations give a fair assessment of the containment prior to subjecting it to a more sophisticated analysis such as the dynamic finite element analysis involving the three dimensional behaviour under seismic impact, explosion and hurricane loadings in any combinations. These calculations cover both the dome and the walls of the TVA containments. Whatever criteria have been used, the calculation follow the TVA guidelines. Any changes needed for other containments must follow that country's codified methods. The author acknowledges the TVA support on the design calculations.

6.3.2 Types of Prestress Losses

| Type of Loss | Value |
|--|---|
| 1. Seating of anchorage | None (see comments 1 below) |
| 2. Elastic shortening of concrete, in./in. | (see comment 2 below) |
| 3. Creep strain of concrete, in./in. per psi | 0.20×10^{-6} |
| 4. Shrinkage strain of concrete, in./in. | 100×10^{-6} |
| 5. Relaxation of prestressing steel, psi | $8\% of 0.65 for 12,500 psi(8625 MN/m^2)$ |
| 6. Friction losses | $k = 0.0003, \mu = 0.13$ |

6.3.2.1 Comments on Types of Losses

- 1. There will be no allowance needed for seating losses in the end anchorage, since no slippage occurs in the anchorage during the transfer of the tendon force to the structure. In addition, the tendon force will be measured by making a life off reading after the anchorage has been seated.
- 2. The elastic shortening of the concrete due to the stressing of subsequent tendons results in a strain changes is considered in determining the effective force of a typical tendon. The average value of strain loss in the tendons is

determined by taking one –half the stress in the concrete under initial prestress and dividing it by the modulus of elasticity of the concrete(50×10^6 psi).

- 3. The above assumed values for the friction factors are somewhat larger than the factors measured on full-scale friction tests on the similar projects; however, the listed values are based on those used in similar containments.
- 4. Prior to the actual tensioning operation of the containment structures, friction tests will be performed to determined the actual friction factors and stressing data will then be revised as necessary.

6.3.3 Primary Containment Structures

6.3.3.1 Vertical Prestressing Losses (A)

a) Shrinkage losses

$$\Delta f_g = E. \in = (29 \times 10^3 \text{ksi})(100 \times 10^{-6}) = 2.90 \text{ ksi} = (20 \text{ } MN/\text{m}^2)$$

b) Steel relaxation losses

$$\Delta_1 f_g = 12,500 \, psi(86.2MN/m^2)$$

c) sum of creep + shrinkage + relaxation

 $6.54 + 2.9 + 12.5 = 21.94 \text{ ksi}(151.28 \text{ MN/m}^2)$ Final $F = 0.7 fc_{\text{pu}} - 21.94 = 146.06 \text{ ksi}(1007 \text{ MN/m}^2)$

NOTE: These are losses may not be recovered by prestressing $0.7 f_s$

```
Initial prestress f_{in} = f_f = 146.06(1007MN/m^2)

creep = 6.54(45MN/m^2)

Shrinkage = 2.90(19.99 MN/m^2)

1/2(Relaxation) = 6.23 ksi

Total 161.73 ksi(1115 MN/m<sup>2</sup>)
```

d) Dome prestressing

Tendon at 26' - 2''(7.9748 m) from the £ dome

| Segment | L | KL | α | μ.α | $KL + \mu \alpha$ | $e^{-(KL+\mu\alpha)}$ | Тx |
|---------|------------------|---------|------|-------|-------------------|-----------------------|-------|
| A | 0 | 0 | 0 | 0 | 0 | 1 | 1.0 |
| AB | 16.26'(4.96 m) | .00487 | 0. | 0 | .00487 | $.995\pm$ | 0.995 |
| BC | 626.37'(8.376 m) | .00791' | .268 | .0348 | .0427 | .958 | 0.954 |
| CD | 31.53'(9.610 m) | .00945 | .306 | .0394 | .0489 | .952 | 0.907 |

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$$\alpha_{BC} = \frac{L_{SC}}{R} = \frac{26.37'}{98.89'} = 0.268$$
$$\alpha_{CD} = \frac{L_{CD}}{R_{AVG}} = \frac{31.53'}{\underline{106.83' + 98.89'}} = .306$$

| Segment | L | KL | α | μ.α | $KL + \mu \alpha$ | $e^{-(KL+\mu\alpha)}$ | Тx |
|---------|-------|--------|-------|--------|-------------------|-----------------------|-------|
| A | 0 | 0 | 0 | 0 | 0 | 1 | 1.0' |
| AB | 22.2 | .00666 | 0' | 0 | .00666 | .9935 | 0.994 |
| | 29.60 | .00888 | | | .00888 | .992 | 0.992 |
| BC | 29.61 | .00888 | 0.337 | 0.0438 | .0527 | .949 | 0.994 |
| | 22.20 | .00666 | | | .0505 | .951 | 0.943 |
| CD | NO | | | | | | |

$$T_o = \frac{T_x}{.907} = 1.103 \therefore \text{ Frictionloss} = 10.3\%$$

$$\alpha_{BC} = 29.60' = 0.337'$$

$$T_0 = \frac{T_x}{943} = 1.060^{\circ}$$
 : Friction Loss = 6.0%

6.3.3.2 Layout of the Containment Dome Assumptions

The flat portion of the DOME-RING-GIRDER will be assumed to be 10'-3" (3.1242 m) wide in order to satisfy anchorage requirement. Therefore, the X-Y coordinates of points "A" are

$$X_A = 72.5 - 10.25 = 62.25(18.974 \text{ m})$$

 $Y_A = 903.5 - 879.0 = 24.5(7.4676 \text{ m})$

6.3.3.3 Computations

Equation for roof

$$\frac{X^2}{(70.5)^2} + \frac{Y^2}{(42.75)^2} = 1$$
$$Y^2 = (42.75)^2 \frac{(42.75)^2}{(70.5)^2} X^2$$



Fig. 6.6 Equipment hatch geometry

Slope to the curve above @ any point can be forced by determining the derivative.

$$y = \sqrt{(42.75)^2 \frac{(42.75)^2}{(70.5)^2} X^2}$$
$$Y = (1827.56 - 0.3677 X^2) \frac{1}{2}$$

Defining $U = 1827.56 - 0.3677X^2$

6.3.3.4 Layout of Containment Dome Verifiction of Tangent Purpose

To verify the point of Tangency of the Dome-Ring-girder Intersection for final design notes.

Data

The roof of primary containment is in the form of an ellipse from \pounds R.B to the point of tangency in question. The equation is :

$$\frac{x^2}{(70.5)^2} = \frac{y^2}{(42.74)^2} = 1$$

Info. On Sketch Fig 6.6(a) primary containment dome



Fig. 6.6 (a) Dome verification for tangency (dome ring order)

Then

$$y = (U)^{1/2}$$

$$\frac{dy}{dx} = 1/2(U)^{1/2} \frac{d}{dx}$$

$$\frac{dy}{dx} = 1/2(1827.56 - 0.3677x^2)^{1/2} \cdot \frac{d}{dx}(1827.56 - 0.3677x^2)$$

$$\frac{dy}{dx} = 1/2(1827.56 - 0.3677x^2)^{1/2}(-0.7354x)$$

With above equation the Slope @ several points will be calculated Trail # 1

$$x'' + 10.25' = 27.5'$$

$$x = 72.5 - 27.5 = 45.0'(13.176 m)$$

$$\frac{dy}{dx} = 1/2(1827.56 - 0.3677(45)^2)^{1/2} \cdot (-0.7354 \times 45)$$

$$= (0.0151936561)(-0.7354)(45)$$

$$Slope = -0.5028036615$$

$$when x + 10.25 = 27.5'$$

The rectangular coordinates for the assumed point of tangency can be found by solving the equation of ellipse.

$$\frac{(45)^2}{(70.5)^2} + \frac{y^2}{(42.75)^2} = 1$$

y = 32.91'(10.031 m)
x = 45.00'(13.716 m)

From equation of straight line

$$Slope = m = \frac{y_2 - y_1}{x_2 - x_1}$$

Slope of trail # 1

$$Slope = \frac{32.91 - 24.5}{45.0 - 62.25} = \frac{8.41}{17.25} = 0.487536$$
$$0.487536\phi = 0.50280$$

Trail # 2

 \therefore Try point of tengancy @ 27.0'

$$x = 72.5 - 27.0 = 45.5'$$

$$\frac{dy}{dx} = 1/2(1827.56 \times 0.3677(45.5)^2)^{1/2} \cdot (-0.7354 \times 45.5)$$

$$= (0.0153117341)(-0.7354)(45.5)$$

Slope = -0.512341

Rectangular coordinates for assumed point of tangency.

$$x = 45.5(13.8684 m)$$
$$y = 32.66(9.9538 m)$$

The equation for straight line

$$Slope = \frac{32.66 - 24.5}{45.3 - 62.2} = \frac{8.16}{-16.75} = 0.48716$$
$$0.48716\phi = 0.512341$$

Trail # 3

$$x'' + 10.25 = 28.5 feet x = 72.5 - 28.5 = 44.0 \frac{dy}{dx} = 1/2 (1827.56 - 0.3677(44^2)^{-1/2} \times (-0.7354)(44) = (0.014969198)(-0.7354)(44) Slope = -0.4843663801 When x + 10.25 = 28.5 ft$$

6.3 Design Calculations for Containment Structures

Solving equation of ellipse when

$$x = 44'.0(13.4112 \text{ m})$$

 $y = 33'.402(10.181 \text{ m})$

From straight line equation

Slope
$$= \frac{33.402 - 24.5}{44.0 - 62.25} = \frac{8.902}{16} = 0.48778081$$

Slope of ellipse \approx Slope of line
 $0.48436638 \approx 0.4877808$

Summary

: Tangent point to the ellipse is 28.5 ft from edge of any girder x = 18.25(5.5626 m)

6.3.3.5 Dome Layout & Design C.G. of Tendon

Elliptical curvature of C.G. ends at 40' - 0'' (12.19m) from £ of Dome. Equation of Ellipse, $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ For C.G. of Tendon

$$a = 67.5' + 1.625' = 69.125' (21.069 \text{ m})$$

 $b = 39.750' + 1.625' = 41.375' (1.986 \text{ m})$

From Ron Howerton's oliveHi program, With x = 40' y = 33.74' + 849.00' = 882.74'(26.9059 m)

(Elev: of transition from elliptical to circular curve) E1 = 882.747'[26.9059 m]

Radius of curvature R_2 of elliptical dome @ y = 40' = 102' - 4''[31.1432 m]

$$R_2 = \frac{(a^4y^2 + b^4x^2)^{1/2}}{b^2}$$

$$a = 69.125(21.0693 \text{ m})$$

$$b = 41.375(12.611 \text{ m})$$

$$x = 40'$$

$$y = 33.74'$$

| x | Y | y (approx) |
|----|---------|--------------------|
| 5 | 39.6408 | 39' - 8'' |
| 6 | 39.5926 | 39' - 7'' |
| 7 | 39.5357 | $39' - 6^{1/2''}$ |
| 8 | 39.4698 | $39' - 5^{1/2''}$ |
| 9 | 39.3951 | 39' - 4" |
| 10 | 39.3114 | 39' - 3'' |
| 12 | 39.1169 | 39' - 1'' |
| 14 | 38.8858 | $38' - 10^{1/2''}$ |
| 16 | 38.6174 | 38' - 8'' |
| 18 | 38.3108 | 38' - 4'' |
| 20 | 37.9631 | $38' - 11^{1/2''}$ |
| 22 | 37.5800 | 37' - 6'' |
| 24 | 37.1532 | 37' - 2'' |
| 26 | 36.6836 | 36' - 8" |
| 28 | 36.1697 | 36' - 2'' |
| 30 | 35.6083 | 35' - 7" |
| 32 | 35.0005 | 35' - 0'' |
| 34 | 34.3405 | 34' - 4'' |
| 36 | 33.6264 | 33' - 8" |
| 40 | 32.0187 | 32' - 0'' |
| 42 | 31.1204 | $31' - 1^{1/2''}$ |
| 44 | 30.1471 | 30' - 2'' |
| 46 | 29.0937 | 29' - 1'' |
| 48 | 27.9511 | 28' - 0'' |
| 50 | 26.7037 | $26' - 8^{1/2''}$ |
| 52 | 25.3492 | 25' - 4'' |
| 54 | 23.8554 | 23' - 10'' |
| 56 | 22.1993 | 22' - 2'' |
| 58 | 20.3411 | 20' - 4'' |
| 60 | 18.2104 | $18' - 2^{1/2''}$ |
| 62 | 16.7274 | 15' - 9'' |
| 63 | 14.2831 | $14' - 3^{1/2''}$ |
| 64 | 12.6482 | 12' - 8'' |
| 65 | 10.72 | 10' - 9'' |

Table 6.3 Table of Offsets For Eliptical Roof of Reactor Containment Table .14711 Imperial units X 0.3048 = (m)





Fig. 6.7 Alternative II: layers touching in middle



Fig. 6.8 Present case

Refer to Sketch on sheet 1 dated 6-6-72

$$\sin \theta_1 = 40.00' = .39089221$$
$$\theta_1 = 23^{\circ}00'36'$$

$$Ao = \sqrt{(102.33')^2 - (40)^2} = 94.18826 \text{ or } 94.19$$
$$\cos \theta_2 = \frac{60'}{102.33'} = .58633831$$
$$\theta_2 = 54^\circ \ 06' 09'$$
$$CD = \sqrt{(102.33)^2 - (60)^2} = 82.89408 = 82.89$$
$$\theta_3 = 90^\circ - (\theta_1 + \theta_2)$$
$$\theta_3 = 12^\circ 53' 15'$$

E1 of Transition from elliptical to cir. cure -AO

882.74 - 94.191 = 788.55

E1 of centre of spherical curve +CD

$$788.55 + 82.89 = 871.44$$



Fig. 6.9 Bar locations and dimensions

Eleve: of Transition from spherical to conical curve= E1 871.44

$$\theta_4 = 90^\circ - \theta_2 = 90^\circ - 54^\circ 06' \, 09'$$

 $\theta_4 = 35^\circ 53' 51'$



Fig. 6.10 Length of dome Reactor Bldg. Dome Length of Tendon

$$AN_{1} = R \sin \theta_{1}$$

$$\sin \theta_{1} = \frac{26.25'}{72.50} = .36206$$

$$\theta_{1} = 21^{\circ}13'36'$$

$$N_{1}P_{1} = Rvers \theta_{1}$$

$$vers \theta_{1} = 1 - \cos \theta$$

$$= 2 \sin^{2} 1/2\theta_{1}$$

$$\frac{\theta}{2} = 10^{\circ}36'48'$$

$$\sin \frac{\theta}{2} = 0.18418$$

$$N_{1}P_{1} = R(2 \sin^{2} 1/2\theta_{1})$$

$$= 72.50(2)(.18418)^{2}$$

$$= 4.91872'(1.5m)$$

$$P_{1}S_{1} = 72.50' - 4.91872 = 67.58128'(20.599 m)$$

$$X = 67.58128' - 53.2531 = 13.6282'(4.15388 m)$$

$$l_{r} = \frac{13.63}{\cos \theta_{4}}$$

6.3.3.6 Reactor Bldg – Dome Length of Tendon



Fig. 6.11 Length of tendon

$$AN_{1} = R \sin \theta_{1}$$

$$\sin \theta = \frac{52.50}{72.50} = 0.72413$$

$$\theta_{1} = 46^{\circ}23'48'$$

$$N_{1}P_{1} = R(2 \sin^{2} 1/2 \theta_{1})$$

$$1/2 \ \theta_{1} = 23^{\circ}11'54''$$

$$N_{1}P_{1} = 72.50(2)(.39391)^{2}$$

$$\sin 1/2 \ \theta = 0.39391$$

$$N_{1}P_{1} = 22.4980$$

$$P_{1}S_{1} = 72.50 - 22.4980 = 50.0011$$

$$X = 50.001 - 29.0473 = 20.9530 = 20.95'$$

6.3.3.7 Dome Layout Horizental Measure

Purpose

To determine the proper spacing of Dome Tendons to obtain Equal Areas of NO Prestress in Ring Girder Region size of Dome from Bulds.

Known Data

41N711

Computations

Assuming the tendon groups divide section in red into 12 equal parts; therefore Each segment is $360^{\circ} \div 12$ or 30° from each sketch pg $2\theta_2 - \theta_2 = 30^{\circ}$ And $\theta_2 + \theta_2 = 30^{\circ}$ Or $2\theta_2 = 30^{\circ}$

$$\theta_2 = 15^{\circ}$$

$$\therefore \theta_1 - 15^{\circ} = 30^{\circ} \quad \theta_1 = 45^{\circ}$$

from sketch cos $\theta_1 = X/72.5$
$$X = 72.5 \times \cos 45^{\circ} = 51.26524 ft$$

Say 51'-3" checks value used (ok)

6.3.3.8 Vertical Prestress Calculations

To determine the required vertical prestress force necessary to withstand load cases of design criteria and to comply with BELLEPONTE PSAR.

Assumptions

- 1- Critical section for vertical Tendons is 2t base of wall (EL620.0)
- 2- Concrete is not counted on to resist tendon
- 3- Liner is always in compression.
- 4- Force in reinforcement balances the force in liner.
- 5- At accident tendon elongation increases stress in the Tendon.
- 6- According to latest AEC guidelines earthquakes must be considered to occur in three directions simultaneously the effects of the earthquakes must be computed by taken the square root of the sum of the square of the maximum responses at a particular point caused by each of the three components of motion (two orthogonal horizontal motions and one vertical motion).

Explanation

In order to determine the max. (F) force to be resisted by vertical prestress. The three motions will be combined as

$$E^* = \sqrt{(V)^2 + (H_N - S)^2 + (H_E - W)^2}$$

But when $H_N - E$ is max. $H_E - W$

:
$$E^* = \sqrt{(V)^2 + (H)^2 + O^2}$$



Fig. 6.12 Force resisted by vertical stress

Vertical Prestress Calculations Computations

A-Controlling Load Case. Vertical free body Notation:

> F = final prestress forceDL = dead = live loadE = load due to earthquake



Fig. 6.13 Controlling load

P = presure load RL = force in liner RS = force in reinf. steel # Cases or bar number – American Practice

From previous calculations it has been determined that load cases 8 and 9 of design critical control vertical Prestress.

#8 - 1.00 + 1.0L + 1.0F + 1.25P + 1.0R + 1.0Ta + 1.25E#9 - 1.00 + 1.0L + 1.0F + 1.0P + 1.0Ta + 1.0Ra + 1.0Rs + 1.0E

Note:

1.0Ro, 1.0R, 1.0Ra, are small loads that will be considered to act only locally. These loads are not axists metrical and most be handled separately. Therefore, they will be ignored for prestress determination $1.0T_2$ will 20 be ?

1- LOAD CASE # 8

From free body sheet 2 to balance vertical forces (see assumption 4)

$$1.0F + 1.0D = 1.25P + 1.25E$$

: Dead load, Pressure and Earthquake must be determined.

2- DEAD LOAD (1.0D)

1.0D is made of wall and Dome weight 1.0wall : 229.4m weight = (229.4)(3.54)(0.150 k/ft) = 120.23 k/ft = 1754.64KN/m

2 Dome. Surface of Dome Forms ∂ one-half Oblate spheroid with $\partial i = 67.5 bi = 39.75$ from Ref.#6 pg17, formula for surface area.

$$S = 2\pi\partial^{2} + \pi \frac{b^{2}}{\epsilon} \ln \frac{1+\epsilon}{1-\epsilon}$$

where ϵ eccentricity $= \sqrt{\frac{a^{2}-b^{2}}{a}}$
 $\therefore \epsilon = \frac{\sqrt{(67.5)^{2}-(39.75)^{2}}}{67.5} = \frac{\sqrt{2976.19}}{67.5} = 0.8082$
 $S = 2\pi(67.5)^{2} + \pi \frac{(39.75)^{2}}{0.8082} \ln \frac{1.8082}{0.1918}$
 $S = 28,627.76 + 13,778.59 = 42406.35$

Dome inside surface area = 1/2 S

$$S_{\rm Ai} = 21,203.17 ft^2 (1969.84 \,{\rm m}^2)$$

Out side sur face $\partial = 70.5'$ b = 42.75'

$$\in = \frac{\sqrt{(70.5)^2 - (42.75)^2}}{70.5} = 0.79517$$

$$S = 2\pi (70.5)^2 + \pi \frac{(42.75)^2}{0.79517} \ln = \frac{1.79517}{0.2048}$$

$$S = 31,229.0 + 15,673.35 = 46902.35$$

$$SA_o = 23,451.176 ft^2 (2178.69 \text{ m}^2)$$

6.3.3.9 Vertical Prestress Calculations

: Average Surface ∂ rea

$$\frac{SAi + SAo}{2} = \frac{21,203.17 + 23,451.18}{2} = 22,327.175 ft^2 (2072.36 \text{ m}^2)$$

Weight of dome = (22,327.175 ft²)(3.0)(0.15 k/ft³)
 $W_D = 10,047.23 k(44.690 MN)$
Weight per foot = 10,047.23/2 π (69.25) = 23.09 k/ft(336.975KN/m)

3 Ring Girder. Volume of ring girder will be determined by sealing from sketch sh.6

Using plain meter the Un- shaded area of sheet #6 has been established as 14.8 ft^2

$$\therefore W_{RG} = 148ft^2 \times o.15 k/ft^3 = 22.2 k(98.75KN)$$

$$a - 1.0D = W_W + W_D + W_{RG}$$

$$= 120.23 + 2.09 + 22.2 = 165.52 k/ft(2415.60 \text{ KN/m})$$

$$b - \text{pressure}(1.0P)$$

Design accident pressure = 50.0 psi(0.345 MN/m^2)

Uplift from pressure

$$p = 50^{\#} / \Box'' \times \frac{144 \Box''}{ft^2} \times \frac{1^k}{1000^{\#}} \times \pi (67.5)^2 . (\pi) (138.5)^2$$
$$p = 236.86 \text{ k/ft say } 237 \text{ k/ft } (50.4773 \text{ MN/m})$$

6.3.3.10 New Earthquake Response

For SSE

$$P_{AE} = 204.0 \times 10^{2} k$$
$$ME = 44.8 \times 10^{5} k - 4$$
$$E = \sqrt{\left[\frac{204.0 \times 10^{2}}{1523}\right]^{2} + \left[\frac{44.3 \times 10^{5} k - 4 \times 69.35}{3,653.332}\right]^{2}}$$
$$= \sqrt{179.4157 + 7209.1912} = \sqrt{7388.6089}$$
$$E = 85.9570 \text{ k/ft} \times 3.5 = 300.25 \text{ k/ft} (4.382 \text{ MN/m})$$
$$1.25E = 1.25 \times 30025 = 376.06 \text{ k/ft} (5.4884 \text{ MN/m})$$

For SSE

$$P_{AE} = 313.0 \times 10^{2} \text{kips}$$

$$ME = 67.2 \times 10^{2} \text{kips} - \text{ft}$$

$$TE = \sqrt{\left(\frac{313.0 \times 10^{2} \text{kips}}{1523 \text{ ft}^{2}}\right)^{2} + \left(\frac{67.2 \times 10^{5} \text{kips} - \text{ft} \times 69.25}{3653.832}\right)^{2}}$$

$$= \sqrt{422.37 + 16222.068} = \sqrt{16643.05}$$

$$= 129.01 \text{ k/ft}^{2} (6.167 \text{ MN/m}^{2})$$

$$E' = 129.01 \text{ k/ft}^{2} \times 3.5 \text{ ft} = 45153 \text{ k/ft}$$

$$1.0E = 451.53 \text{ k/ft}$$

Case#8

$$1.0F + 1.0D = 1.25P + 1.25E$$

$$1.0F = 296.52 + 376.06 - 165.52$$

$$= 506.79 \text{ k/ft}$$

Case#9

$$1.0F = 1.0P + 1.oE' - 1.0D$$

= 236.86 + 451.53 - 165.52
1.0F = 522.87 k/ft

:. Load case#9 controls design conclusion.

Present prestress force of 530 k/ft (7734.82 KN/m) is more than 523 k/ft reqd. by controlling load CASE.

:. From pressure
$$1.0P = 236.86 \approx 237 \text{ k/ft} (3.459 \text{ MN/m})$$

 $1.25P = 296.25 \text{ k/ft} (4.234 \text{ MN/m})$
 $1.50P = 355.5 \text{ k/ft} (5.2 \text{ MN/m})$

6.3.3.11 Earthquake Forces -1.0E and 1.0E'

The effect of three component earthquake must be considered according to AEC. This will be done by taking the square root of the sum of the squares of each component. From Bending Moment pressure distribution may uplift occurs over a 90° quadrant and is constant @ H_{max} .

$$\sigma_E = \sqrt{\left(\frac{P_{AE}}{A_W}\right)^2 + \left(\frac{M_E \cdot C}{I}\right)^2 + (0)^2}$$

where

 P_{AE} = vertical load from earthquake.

 M_E = bending moment from horizental component.

 A_W = moment of inertia of cylinder.

C =radius top of wall

Thus,

$$A_W = \pi (r_0^2 - r_i^2) = \pi ((71)^2 - (67.5)^2) = \pi (484.75)$$

$$A_W = 1522.89 \text{ say } 1523 \text{ ft}^2$$

$$I = \pi / 64 [d_o^4 - d_i^4] = \pi / 64 [142^4 - (135)^4]$$

$$= 3,653.882 \text{ ft}^4$$

$$c = 67.5 + 3.5/2 = 9.25 \text{ ft}$$

1. 1/2 Safe- Shutdown Earthquake

From R&D spectrum see sheet # 9 and 10

$$P_{AE} = 2.215 \times 10^{4} \text{kip}$$

$$M_{E} = 47.5 \times 10^{5} \text{kip/ft}$$

$$\sigma_{E} = \sqrt{\left(\frac{2.215 \times 10^{4}}{15.23}\right)^{2} + \left(\frac{4.75 \times 10^{6} \times 69.25'}{3653882}\right)^{2}}$$
$$\sigma_E = \sqrt{8315.0} = 91.19 \text{ k/ft}^2$$
$$E = (91.19 \text{ k/ft}^2)(3.5ft) = 319.15 \text{ k/ft}$$
$$1.25E = 398.94 \text{ k/ft}(5.8354 \text{ MN/m})$$

2. Safe Shutdown Earthquake

From

$$P_{AE} = 3.13 \times 10^{4} kip$$

$$M_{E} = 66.0 \times 10^{5} kipft$$

$$\sigma_{E} = \sqrt{\left(\frac{3.13 \times 10^{4} k}{15.23 \text{ft}^{2}}\right)^{2} + \left(\frac{66.0 \times 10^{5} \text{k.ft.} 69.25}{3.653882 \text{ft}^{2}}\right) + 0}$$

$$= \sqrt{(20.55 \text{k/ft})^{2} + (125.09)^{2}}$$

$$= \sqrt{1606.81}$$

$$\sigma_{E} = 126.77 \text{k/ft}^{2}$$

$$E' = 126.77 \text{k/ft}^{2} \times 3.5 ft = 443.68 \text{k/ft}$$

$$.0E' = 443.68 \text{k/ft} (6.5 \text{MN/m})$$

LOAD CASE 8 Required Prestress

$$1.0F + 1.0D = 1.25P + 1.25E$$

 $1.0F + 165.52 = 296.25 + 398.94$
 $1.0F = 529.67 k/ft (7.76MN/m)$

II LOAD CASE 9

1

From free body $5\lambda.2$ statics gives 1.0F + 1.0D = 1.0P + 1.0ESubstituting values from proceeding pages

> 1.0F + 165.52 = 236.86 k/ft + 443.68 k/ft 1.0F = 515.2 k/ft(7.546 MN/m) $1.0F_3 > 1.0F_9 \therefore \text{ load case eight controls}$ $\therefore \text{Reqd vertical prestress} = 529.67 \text{ k/ft}$ Say 530 k/ft (7.765 MN/m)

Note: This force is reduced by 64 k/ft(0.9rMN/m) over original estimated values. Calculations must be made to optimize the amount of prestress

provided to reduce reinf steel necessary to withstand sheer. Fin al prestress @Accident = 502 k/ft. manufacturers supply 564 k/ft the reserve prestress $F_{TR} = 62 \text{ k/ft}$ @accident use have

62 ×
$$\frac{151.3}{144.3}$$
 = 65k/ft(0.9523 MN/m)
∴ F_{TR} = 65k/ft (0.9523 MN/m)

B. Required Final Prestress

From sheet # 13 the required force is 530 k/ft however the prestress force may be reduced because of Tendon Elongation. Since tendon elongation depends of final stress in tendon, an estimate of this will be made and the reserved @later time.

Based on preliminary Cale by EGB & NP (see reference $\phi = 1$) and calculation by sergeant & Lundy the final stress is 144.9 ksi and @accident fs = 151.3

The estimated final prestress

$$F_F = 530 \,\mathrm{k/ft} \times \frac{144.9}{151.3} = 506 \,\mathrm{k/ft}(7.4134 \,\mathrm{MN/m})$$

C. INITIAL PRESTRESS

In order to estimate losses an initial prestress force must be determined. However initial prestress and losses are interdependent.

From previous calculations the primary containment under different loading it has been determined that the initial stress in tendons is approx $161.8ksi(1115.6MN/m^2)$

and final stress is approx $144.9ksi(999MN/m^2)$

$$F_t = \frac{506 \, k}{\text{ft}} \times \frac{161.8 \text{ksi}}{144.9 \text{ksi}} = 564.9 \text{k/ft}$$

565 k/ft(8.28MN/m)

Check of Initial concrete stress.

$$f_{CI} = \frac{F_I + DL}{AW} = \frac{565 + 165.32}{(12)(42)} = \frac{730.52 \, k/ft}{504 \, k/ft}$$
$$F_{CI} = 1440 \, \text{psi} < = 0.3fc = (0.3)(5500)$$
$$F_{CI} = 1440 \, \text{psi} < 1650 \, \text{psi} \therefore ok$$
$$9.93 \, \text{MN/m}^2 < 11.38 \, \text{MN/m}^2$$

Summary

The final prestress force @ Accident = 530 k/ft (7.765 MN/m). The estimated final prestress before accident = 506 kft (7.4134 MN/m).

6.3.3.12 Vertical Prestress Losses Purpose Of Computations

To determine the prestress losses for vertical Tendons in order to compute the required prestress force for design.

Data

$$E_c = 5.0 \times 10^{\epsilon}, E_c = 29 \times 10^6 psi, n = \frac{29}{5} 5.8$$
$$f'_c = 5500 \text{ psi}, E_{px} = 240 \text{ ksi}(1659 MN/m^2), f_{py} = 192 \text{ ksi}(1327 \text{ MN/m}^2)$$

Assumptions

Final prestress and losses are interdependent therefore ∂ value for final prestress will be estimated and losses will be calculated. Then the process will be repeated to see if changes are required for final prestress.

Assume final prestress of 506 k/ft.

Computations

1-CREEP LOSSES From PSAR, Creep strain of concrete = 0.20×10^6 Assuming $F_{TF} = 506 \text{k/ft}$ Initial prestress $\approx 506 \left(\frac{161.8}{144.9}\right) = 565.02 \text{k/ft} = (8.28 \text{MN/m})$ Concrete stress due to Fi

$$f_a = \frac{565 \text{k/ft}}{12 \times 41.75} = 1128 \text{ psi}(7.78 \text{ MN/m}^2)$$

Strain change in concrete

$$\Delta E_c = (1.128)(0.20 \times 10^{6\%}) = 2.26 \times 10^{-4}$$

Steel stress change

$$\Delta f_s = (29 \times 10^3) \times (2.26 \times 10^{-4}) = 6.54 \, \text{ksi}(45.1 \, \text{MN/m}^2)$$

6.3 Design Calculations for Containment Structures

5. Losses Due to Elastic Shortening

Elastic shortening will be calculated according to procedure

$$\Delta fs = \frac{n \times F_0}{Ac \times 2}$$

Where: F_0/A_C = initial concrete stress from prestress

$$n = E_S/E_C$$

Assuming $fo = 1128 \operatorname{psi}(fo = 565 \mathrm{k/ft})$

$$\Delta fs = \frac{(5.8)(1.128)}{2} = 3.27 \, ksi(22.547 MN/m^2)$$

:. In order for tendon stress @anchorage to equal 168 ksi the tendon must

be ANCHORED

$$F_S = 168 + 3.27 = 171.27 \, ksi(1181 MN/m^2)$$

6. Friction Loss

From Ref# 5 the loss due to friction is 11.2%

:. An increase in stress of 11.2% in necessary to overcome friction loss. 11.2% of 171.27 ksi = 19.18 + 171.27 = 190.45 \approx 191 ksi(13.7 MN/m²) 151 < 0.8 f_{pg} = 192 ksi(1324 MN/m²)(OK)

Therefore friction and elastic shortening may be overcome by over stressing.

Purpose of Computations

To recalculate the friction loss sustained by vertical Tendons from Tendon Gallery Base Slab to Ring Girder Anchorage. This loss is necessary for calculation of required vertical prestress.

Data

Dimensions from Design (SEE sheet 3 for copy portion of this DRG)

 $K = 0.0003 \quad wobble \ coefficient \\ \mu = 0.13 \qquad curvature \ coefficient \\ \} \ PSAR \ 3.8.1.4.1.6$

Assumptions

Friction ignore for average Tendon will be calculated and used. Deflected Tendons will be considered separate due to insure the additional losses do not alter design. For straight portion of Tendon have wobble friction loss and curved portion has both wobble curvature.

Primary Containment Structure Computations

1. Equation of Friction Loss

The ring girder has curvature in it. Equation from *Ael EQ friction loss*

$$P_S = P_x e^{(KL + \mu x)}$$

Where:

 $P_{S} = \text{force} @ \text{Jacx } G END$ $P_{Y} = \text{Force} @ \text{paint of question}$ e = natural log base k = wobble friction loss coefficient. L = length of strand being considered. $\mu = \text{curvature friction coefficient.}$ $\alpha = \text{angle change for strand.}$

and $k = 0.0003 \,\mu = 0.13$ 2. Loss Calculations

See sheet 3 for sketch and segment numbering. Segment + BC is only segment with curvature $\alpha = 11^{\circ}30' = 0.2007$, $L = R.\alpha = (30')(0.2007) = 6.021$ ft Then $11^{\circ}30' = \Delta EL/30$

$$\Delta EL = 6.104 \, \text{ft} 855 = 861.10 \, \text{ft} (262.463 \, \text{m})$$

| Segment | L | KL | α | μ.α | $KL + \mu \alpha$ | $e^{-(KL+\mu x)}$ | Tx |
|---------|--------|----------|--------|--------|-------------------|-------------------|----------|
| A | 0 | 0 | 0 | 0 | 0 | 1.0 | 1.0 |
| AB | 12.52' | 0.003756 | 0 | 0 | 0.003756 | 0.99625 | 0.99625 |
| BC | 6.021' | 0.001806 | 0.2007 | 0.0261 | 0.027897 | 0.972488 | 0.968841 |
| CD | 248.5 | 0.07455 | 0 | 0 | 0.07455 | 0.928161 | 0.89924 |

3. Table Losses

$$P_x = 0.89924' P_S$$
$$P_S = \frac{1}{0.89924}. P_X = 1.11205 P_X$$

 \therefore To obtain Required Jacking Force (or stress) the desired force must be increased 11.2%.

Conclusions

1. Vertical Friction Loss for Average Tendon is 11.2%

| | Condition | Prestressing Force |
|---------|--|-------------------------------------|
| Initial | Jacking | 498 k/ft(7.2962 MN/m ²) |
| | Anchorage | 436 k/ft(6.388 MN/m ²) |
| | Design $F_S = (161.8 ksi)$ | 420 k/ft(6.1536 MN/m ²) |
| Final | Before Tendon elongation @ accident $(f_{1} - 143.0 km)$ | 373 k/ft(5.465 MN/m ²) |
| | $(f_S = 143.9 \text{ kst})$ After tendon elongation after accident $(f_S = 152.7 \text{ kst})$ | 396 k/ft(5.802 MN/m ²) |

Summary of Forces

6.3.4 Dome Prestressing: Description of Tendon Arrangement

Dome tendons are arranged in three groups, each group related 60° apart. Tendon in each group run in vertical planes parallel with vertical plane thru £ of tendon group. Spacing of tendons in each group is approximately 42" and spacing is begun at approx: 52'-6" from of roof.

There will be three layers of Tendons, are in each of the three directions.

Each group of Tendons will take 1/1.5 times the required prestressing force. For check on this see roof plane on sheet 2. Red cross hatching indicates areas where 2 groups of tendons are anchored. Single red lines indicates where only one group of tendons are anchored.

Each anchor zone is divided into 12 equal areas. $\frac{1}{2}$ of these areas have one tendons group anchored where each group will take 1/12 of the prestressing force. Also $\frac{1}{2}$ the anchor areas where 2 groups of tending area will take 1/6 of the prestressing force with each direction contributing 1/12.

Summing 12 increments around circumference of dome.

$$6 \times 1/6 = 1.0$$

 $6 \times 1/12 = 0.5$
 $1.0 + 0.5 = 1.5$

1.5 times required prestressing of force is furnished by all the tendons, therefore the computed prestress force will be divided 1.5 to act read prestress Assumption and Criteria for design.

- (1) All computations for prestressing requirements will be based upon the centre of gravity of the dome tendons.
- (2) The tensile stress in the prestressing tendons exert a normal force on dome which depends on the radius of curvature of the tendons. Tendons will have a different curvature which will result in Normal forces that vary through out the dome.
- (3) Since the Tendons are placed in three different directions, the normal forces will have to be computed in each direction for certain critical points in dome. Each critical point will have three "normal" forces acting. These forces will have to be summed vertically to obtain a resultant force. Liberal sketches will be provided to locate these critical points.
- (4) Final prestressing force in Dome will be based on the resultant effect of the above mentioned "Normal" forces.
- (5) Dome Tendons are anchored at different angles (in relation to a horizontal plane). At least every other tendon will be anchored on a different angle at ring due to the fact that:
 - (a) The curvature of the dome is constantly changing at location of each Tendon.
 - (b) With 3 layers of tendons, each layer has to emerge from ring girder at different elevation. Therefore, an average angle of emergence thru the ring girder will be used to determine the horizontal and vertical components of the prestressing force at the ring girder.
- (6) When all prestressing forces have been determined, they will used in a computer analysis of the containment wall and dome to arrive at stresses and deformations in the structure.

6.3.5 Dome Vertical Components

6.3.5.1 Statics

Total Uplift Force on Dome Must be Balanced by Vertical Component of Dome Prestressing Force.

$$\left[\sum F_V = 0\right] P = F \times \text{circum} + W_{\text{DOME}}$$
$$W_{\text{DOME}} = (\text{vol. of Dome}) \times (150 \text{ ibs/ft}^3)$$
$$\text{Volume} = \text{Area} \times 3.0'$$
$$\text{Area} \cong (80.6)(2\pi)(35) = 17,700$$



Fig. 6.14 Uplift force on Dome

Volume =
$$3 \times 17,700 = 53100 ft^3$$

WGT = $53100 \times 0.150 = 7960 - 10,047$ KN (*actual*)
 $P \approx (0.075 k)(144)(\pi)(67.5)^2 = 154,500$ k
 $F(k/1)(\pi)(135) \sin 35.9^\circ = 154.500 - 7960 = 146,540$
 $249F = 146,540$
 $F = 588 k/1 \pm (8.615 MN/m) \pm$

Prestressing provided 593 k/z (8.69 MN/m).

6.3.6 Dome Prestressing Elliptical Dome

For design accident pressure $P = 50 psi(344.75 KN/m^2)$

$$P = 50 \, psi \times 144^{in^2} / ft^2 = 7.20 \, k / ft (0.1055 \, \text{MN/m})$$

Dead load = $0.15 \, k / ft^3 (3.0 ft) = 0.45 \, k / ft$
 $1.5p = 1.5 \times 7.20 = 10.80 ksf (48.04 KN)$

Critical Design Case for Dome = 1.5P + 1.0TA + 1.0DDead load subtracts from pressure load since pressure is an un lift force.

:. Net load on dome =
$$1.5P - D$$

= $10.80 - 0.45$
= $10.35ksf(46.04 \text{ KN})$

Max.meridional force at
$$\tau$$
 dome N ϕ = pa2
N ϕ = 10.35 k/ft = (67.5)2 = 593 k/ft
2(39.75')

:. Prestress force $=\frac{593^{K1}}{1.5} = 396 k/ft(5.802 MN/m)$ *Assume that compressive force in liner due to thermal loads in resisted by tendon.

6.3.6.1 Elliptical Dome

Meridional force @ 55 from \oint dome (this is where dome begins transition to thickened section and where one layer of Tendons begin)

$$N\phi @55' = \frac{p \cdot \gamma_2}{2}$$

$$\gamma_2 = \frac{\alpha^2}{(\alpha^2 \sin^2 \phi + b^2 \cos^2 \phi)^{1/2}}$$

$$\tan \phi = \frac{55'}{110} = 0.5 \quad \phi = 26.5^{\circ}$$

$$\sin 26.5^{\circ} = 0.4446 \quad \sin^2 = 0.199$$

$$\cos 26.5^{\circ} = 0.895 \quad \cos^2 = 0.800$$

$$\gamma_2 = \frac{(67.5)^2}{[67.5^2(0.199 + 39.75^2(0.800)]^{\frac{1}{2}}}$$

$$\gamma_2 = \frac{4560}{(905 + 1265)^{\frac{1}{2}}} = 97.8 ft(29.81 \text{ m})$$

Meri: force $N\phi = \frac{P_{\gamma_2}}{2} = \frac{10.35 \times 97.85 \text{ft}}{2} = 506 \text{ k/m}(7.413 \text{ MN/m})$
For $\phi = 13^{\circ}$

$$\sin 13^{\circ} = 0.225 \quad \sin^{2} = 0.0507$$
$$\cos 13^{\circ} = 0.974 \quad \cos^{2} = 0.948$$
$$\gamma_{2} = \frac{4560}{(231 + 1500)^{\frac{1}{2}}} = 109.2 \text{ft} (32.285 \text{ m})$$

Meridional: force will be; $N_{\phi O} = \frac{p.\gamma_2}{2} = \frac{10.35(109.2)}{2} = 567 k^2/ft(8.6433 \text{ MN/m})$ From the preceding computation, we see that the meridional force increases. The dome is all reached for check, approx: radius of curvature for upper part of dome = 102'-3'' and consider as spherical dome.

* $Min N\phi$ @ top of dome $\frac{ag}{2} 1/2(10.35)102.25') = 530 \text{ k/ft}(.765 \text{ MN/m})$ $\sin\phi = 55 \text{ft}/102.25' = 0.557 \quad \phi = 32.4^{\circ}$ $N\phi = @55' = \frac{ag}{1 = \cos\phi} = \frac{102.25 ft(10.35 \text{ k/ft})}{1 + \cos 32.4}$ $N\phi@55' = 575 k/ft(8.4243 MN/m) \text{ max}$.

Tendons become tangent to curvature of dome at this point (see sheet 7) $\therefore Prestress force = \frac{575 k/ft}{1.5} = 383 k/i \approx 396$ Therefore, we will extrime to use elliptical dame for our englasis

Therefore, we will continue to use elliptical dome for our analysis. Note:

The final prestress can be reduced Since @ accident condition tendon elongates and stress is increasing.

Final prestress force $=\frac{593 k/ft}{1.5} = 396 k/ft(5.80MN/m)$

For spherical dome minimum meridional stress occurs at Top while for an elliptical dome, may meridional stress may be occur at Top.

Based on this assumption of Tendon elongation at accident; the final force before accident.

$$\left(\frac{593 k}{N}\right) \left(\frac{\text{final stress befor eaccident}}{\text{finl stress before accident} \times (\Delta f_z) \text{aacident}}\right)$$

At accident condition, concrete compressing stress diminishes to zero

Before accident =
$$f_c = \frac{539}{(12)(35.75)} = 1.385 \, \text{ksi} \left(4.55 \, \text{KN/m}^2 \right)$$

and

$$f_c = \frac{f_i}{\epsilon_c} = \frac{1.385}{4.55 \times 10^6} = 0.000304$$

At accident $\in_c -0$

 $\Delta f_s = 29 \times 10^6 \times 0.000304 = 8.8 \,\mathrm{ksi}.$

Final tendon stress before accident = 140.35;

final tendon strees after accident = 140.35 + 8.8 = 148.35

Thus

Final force before @ accident =
$$\frac{593 k}{ft} \frac{40.35}{148.35}$$

= $593 k/ft \left(\frac{40.36}{148.35}\right) \left(\frac{143.9}{152.7}\right)$
= $560 k/ft (8.205 MN/m)$

and

Final stress force
$$=\frac{560}{1.5}=373 k/ft (4.484 MN/m)$$

Friction Losses Assmptions

- (1) Tendons stressed from both ends
- (2) From sketch of sheet 2 of Dome prestressing

Calculation dated 2-24-72, will take three critical locations in dome for computing normal force acting on dome from prestress. This analysis will require computation of friction losses for the following Tendon locations.

(A) Tendon passing through £ dome

(B) Tendon @ 26'3" from £dome

(C) Tendon @ 52'6'' from £ dome.

(3) Use C.G of Tendon for all computations.

(A) Tendon Passing through \pounds dome Ac1 Code equation from Friction Loss

$$T_0 = T_x e^{(KL + \mu x)}$$

 $T_0 =$ Force at jacking and.

 $T_x =$ Force at any point

K = Wobble coefficient.

L = Length of prestressing strand being considered.

 α = angle change for strand being considered.

From PSAR, pg. 40:

$$K = 0.0003$$

 $\mu = 0.13$



Fig. 6.15 Frictional losses in dome

| Segment | L | K.L | α | $\mu.\alpha$ | $KL + \mu \alpha$ | $e^{-(KL-\mu\alpha)}$ | T_x |
|---------|--------|--------|-------|--------------|-------------------|-----------------------|-------|
| A | 0 | 0 | 0 | 0 | 0 | 1 | 1.0 |
| AB | 15.43′ | .00463 | 0 | 0 | .00463 | 0.995 | 0.995 |
| BC | 23.02' | .00690 | 0.224 | .291 | .0360 | 0.965 | 0.960 |
| CD | 42.10' | .01262 | 0.387 | .0503 | .0629 | 0.939 | 0.900 |

$$T_X = \frac{T_0}{e^{(KL+\mu\alpha)}} \alpha_{BC} = \frac{L_{BC}}{R} = \frac{23.02}{102.33}$$

$$T_X = T_0 e^{-(KL+\mu\alpha)} \alpha_{BC} = 0.224 \text{ radians}$$

$$T_X = T_0(0.900) \quad \alpha_{CD} = \frac{L_{CD}}{R_{Avg}} = \frac{42.10}{\frac{115.49' + 102.3}{2}}$$

$$T_0 = \frac{T_X}{0.900} = 1.11T_X \alpha_{CD} = 0.387 \text{ radians}$$

$$\therefore \text{ Friction loss} = 11.1\%$$

Elastic Shortening Loss

Final prestress force = 560 kip/ft(8.205 MN/m)Initial prestress;

$$F_{ct} \cong 560 \,\text{k/ft} \times (160.1 \,\text{kbi}) \cong 630 \,\text{k/ft}(9.2306 \,\text{MN/m})$$
(142.2)
$$\therefore F_{ci} = \frac{630}{(13'')(36.75'')} = 1470 \text{psi}$$

$$\therefore$$
 Assume initial prestress = 1500 psi(10.3425 MN/m²)

Avg. elastic shortening $(\Delta fs)_{Avg} = \frac{nfci}{2} = \frac{6.38(1500)}{2} = 4.81 \text{ksi/ft} (0.705 \text{ MN/m})$

Creep Loss

$$\Delta \in_{c} = (1500 \text{ psi})(0.25 \times 10^{-6} \text{in./in./psi}) = 0.000375$$
$$\Delta f_{s} = \Delta \in_{c} \times E_{s} = 0.000375(29 \times 10^{6})$$
$$\Delta f_{s_{\text{creep}}} = 10.90 \text{ ksi}(75.16 \text{ MN/m}^{2})$$

Tendon Relayation Loss

 $\Delta F_S = 12.50 \ ksi (86.2 \text{MN}/\text{m}^2)$

Shrinkage Loss

$$\Delta f_s = \in_{sh} E_s$$

$$\Delta f_s = (100 \times 10^{-6})(29 \times 10^6) = 2.9 \text{ ksi}(20 \text{ MN/m}^2)$$

Summary of losses Avg elastic shortening = 4.8 ksi(0.705 MN/m)Creep = 10.90Shrinkage = 2.90Tendon relavation = 12.50AVG friction loss = $\frac{1}{2(11.1\% + 6.0\%)} = 85\%$ Friction loss at 26'3 from the dome = 10.3%

:. use 10.3% for all friction losses since at least $\frac{1}{2}$ of all tendons will have 1.3 11.1% friction losses. (Note: friction losses in domes are small enough to be compensated for by overstressing to $0.80 f'_5(0.8 \times 240 \text{ ksi})$ Maximum jacking stress = 0.80% fsa = $0.80(280 \text{ ksi}) = 192 \text{ ksi}(2.813 \text{ MN/m}^2)$

Then max. initial stress available at while overstressing $=\frac{192}{1.103} = 174.07$ ksi < 180

:.O.K

or $=\frac{0.813}{1.103}=2.55$ MN/m² < 2.6372

Average initial tendon stress at achoring $= 0.70f'_s = 168 \text{ ksi}(2.4614 \text{ MN/m}^2)$ Max initial allow tendon stress at enchoring $= 0.75f'_s = 180 \text{ ksi}(2.6372 \text{ MN/m}^2)$ Avg elastic shortening = 4.8 ksi

Therefore initial force stress in first stressed tendon at enchoring 168 + 4.8 = 172.8ksi < 174 *O.K* Total elastic shortening = -9.6Stress in first stressed tendon = $163.2 ksi(2.391MN/m^2)$ Stress in last stressed tendon = $172.8 ksi(2.52173MN/m^2)$ \therefore Avg initial stress in tendons an anchoring (at completion of stressing) = $168 ksi(2.4614 \text{ MN/m}^2)$ Avg final prestress = $168 - 26.3 = 143.7(2.1054 \text{ MN/m}^2)$

6.3.6.2 Initial Stress for Design

Final stress = 141.7 ksi(2.0761)Creep loss = 10.90 ksi(0.160)Shrinkage loss = 2.90 ksi(0.0426)1/2 Relax loss = 6.30 ksi(0.0425)Total = 161.8 ksi(2.3705)

Summary of Dome Prestressing Forces

(A) STRESS LEVELS

(1) Maximum jacking stress = $192 \text{ ksi}(2.813 \text{ MN/m}^2)$

(2) Initial tendon stress at anchorage = $172.8 \text{ ksi}(2.53173 \text{ MN/m}^2)$

(3) Average initial stress in tendon at anchorage $= 168 \text{ ksi}(2.4614 \text{ MN/m}^2)$ (4) Final tendon stress = $143.70 \text{ ksi}(2.1054 \text{ MN/m}^2)$

(B) FORCES

- (1) Final tendon force = 373 k/ft(5.4648 MN/m)
- (2) Initial tendon force at anchorage = $373 \times \frac{172.8}{141.70} = 454 \text{ k/ft}(6.65155\text{MN/m})$ (3) Average initial force at anchorage = $373 \times \frac{168}{147.7} = 436 \text{ k/ft}(6.388 \text{ MN/m})$
- (4) Jacking Force = $373 \times \frac{192}{147.7} = 506 k/\text{ft} (7.4134 \text{ MN/m})$

NOTE: Effecting meridional force in dome considering three layers of tendon S = 1.5 times.



Fig. 6.16 Plan of dome

Dome Prestressing Tendon Normal Forces.

Scale1 = 40'0

Compute approx. spacing of tendons based on 186' - 1/4 wires per tendon.

$$Spacing = \frac{186 \text{ wires} \times 0.0471^{B} /_{\text{wires}} \times 143.90 \text{ k} / B''}{373 \text{ k/ft}} = 42'' (1067 \text{ mm})$$

For 170 wires Tendon.

$$Speg = \frac{170}{186} \times 42 = 38.6C/C(980.6 \text{ mm})$$

Assume 42"(1067 mm) spacing between Tendons measured in horizontal plane.

(1007 mm)42'' spacing will equire approx 31 Tendons in each group, 3 groups = $\frac{\text{tendons table}}{93}$

Due to the fact that the curvature in the Tendons gets sharper (i.e. radius of curvature) as the tendons become further from \pounds dome and the normal forces that the Tendon experts on the dome increases as the Tendons becomes more remote form the \pounds of dome, then we will design on the following basis:

- (1) Complete forces on dome assuming constant tending spacing in horizontal plane.
- (2) Adjust spacing as necessary to achieve uniform prestress.

Point 1 on Dome (£ of dome at Apex)

$$N = \frac{F}{R}$$

where

N = normal force exerted in a direction from prestress Tendon.

F = force in prestressing tendon.

R = radius of curvature of tendon.

From sketch on sheet. The three groups of tendons in the dome are labelled directions "A", "B"&"C".

Critical points are labelled 1, 2, 3, etc. For point 1

$$NA = NB = NC = \frac{373}{115.49} = 3.23 \text{ kip/ft}$$

 $\therefore N_i \text{ total} = 3 \times 3.23 = 9.69 \text{ kip/ft}(0.1242 \text{ MN/m})$

Check normal force at 1.5P accident condition

$$N_T = 9.69 \text{ kip/ft} \times \frac{396 \text{ kip/ft}}{373 \text{ kip/ft}} = 10.30 \text{ ksf}(13 .955 \text{KNm})$$

Dead load roof = $\frac{0.45}{10.75}$
 $1.5p \text{ load} = 10.80 \text{ ksfi}(14.63 \text{ KNm})$
 $\approx 10.75 \text{ ksf prestress load}(14.56 \text{ KNm})$

Check Average Initial Prestress Force

Average initial prestress = 436 kip/ft

$$N_T = \frac{436}{115.49} \times 3 = 11.33 \text{ kip/ft}$$

 $D.L = 0.45 \text{ kip/ft}$
Total load = 11.78 kip/ft

Meridional force in dome

$$N_{\phi o} = \frac{P_{ver}}{2} = \frac{11.78 \times 115.5}{2}$$

 $N_{\phi o} = 687 \, k/ft$

Initial conc. stress;

 $f_{ct} = \frac{687.000}{12 \times 35 - 75} = 1602 \text{ psi}(11.0538 \text{ MN/m}^2) < 1650 \text{ psi}(11.2585 \text{ MN/m}^2)$ ∴ ok Maximum allowable initial stress = $0.3fc' = 0.3(5500) = 1602 \text{ psi}(11.2585 \text{ MN/m}^2)$

Point 2 on Dome

(1 k/ft = 12.81734KN/m)

Consider forces in vertical plane along a radial line from \pounds dome. (This will give *X*&*Y* Components of forces only *Z* Components will cancel out).

"A" direction $\rightarrow NA = \frac{373}{87.8'} = 4.25 \text{ kip/ft}$ "B" direction $\rightarrow NB = \frac{373}{102.33} = 3.64 \text{ kip/ft}$ "C" direction $\rightarrow NC = \frac{373}{87.8} = 4.25 \text{ kip/ft}$

Computer Vector Components in X&Y Plane

"A" direction $F_{AY} = 4.25 \cos 19.31^{\circ} = -4.01^{K}$ $F_{AX} = 4.25 \sin 1931^{\circ}(\cos 60^{\circ}) = 0.71^{K}$ "B" direction $F_{BY} = 3.64 \cdot \cos 35.90^{\circ} = -2.96^{K}$ $F_{BX} = 3,64 \sin 35.90^{\circ} = 2.14^{K}$ "C" direction $F_{CY} = F_{AY} = -4.01^{k}$ $F_{CX} = F_{AX} = 0.71^{k}$

Resultants:

$$F_{RY} = 4.01^{k/1} + 2.96^{k/1} + 4.01^{k/1} = 10.98 \text{ k/ft}$$

$$F_{RX} = 0.71 + 2.14 + 0.71 = 3.56 \text{ k/ft}$$

$$F_R = \sqrt{(10.98)^2 + (3.56)^2} = 22.56 \text{ k/ft}$$

$$\tan \theta (\text{angle from vertical}) = \frac{3.56}{10.96} = 0.324$$

$$N_A = \frac{373^{\frac{k}{3}}}{87.8'} = 2.25^{k/ft}$$
$$N_B = \frac{373^{\frac{k}{3}}}{98.9'} = 3.78^{k/ft}$$
$$N_C = \frac{373}{98.9} = 3.78^{k/ft}$$



Compute vector components in Y-Y plane along radial line

"A" direction =
$$F_{AY} = -4.25 \text{ k/ft}$$

 $F_{AX} = 0$
"B" direction = $F_{SY} = 3.78 \cos 27^\circ = -3.36 \text{ k/ft}$
 $F_{BX} = 3.78 \sin 27^\circ (\cos 30^\circ) = 1.49 \text{ k/ft}$
C direction = $F_{CY} = F_{BY} = -3.36 \text{ k/ft}$
 $F_{CX} = F_{BX} = 1.49 \text{ k/ft}$

Dome Prestressing Tendon Normal Forces Resultants

$$F_{RY} = 4.25 + 3.36 + 3.36 = 10.97^{k/ft}$$

$$F_{RX} = 0 + 1.49 + 1.49 = 2.98^{k/ft}$$

$$F_R = \sqrt{(10.97)^2 (2.98)^2}$$

$$= 11.36 k/ft$$









For "A" and "C" Directions @26.25' from ∮ Dome Properties of ellipse;

$$a = 63.95$$

$$b = 38.28$$

$$x = 115.17$$

Y ISOPAR EEO = 37.1'
Y(from olliveti program) = 37.2'
ISOPAR EEO = 163.978
 γ_z (from olliveti program) = 164.92'
sin $\theta_1 = \frac{15.17}{104.92} = 0.45 \,\theta_1 = 8.3^0$

For "B" directions @ 30.35' from ∮ dome properties of ellipse

$$a = 69.125'$$

$$b = 41.375'$$

$$x = 30.35$$

$$\therefore Y = 37.2'$$

$$\sin \theta_1 = \frac{30.35}{108.18} = 0.279 \ \theta_1 = 16.2^0$$

"A" and "C" direction

$$N_A = N_C = \frac{373^{\frac{k}{7}}}{104.92'} = 3.56^{k/ft}$$
$$N_B = \frac{373^{\frac{k}{7}}}{108.18'} = 3.45^{k/ft}$$

Compute Vector Components in X-Y Plane Along Radial Line "A" direction

$$F_{AY} = 3.56^{k} (\cos 8.3^{0}) = 3.52^{k/ft}$$

$$F_{AX} = 3.56 (\cos 8.3^{0}) (\cos 60^{0}) = 0.26^{k/ft}$$

"B" direction

$$F_{BY} = 3.45(\cos 16.2^{\circ}) = 3.31^{k/ft}$$

 $F_{BX} = 3.45(\sin 16.2^{\circ}) = 0.96^{k/ft}$

"C" direction



Fig. 6.17(c) Resolution of forces

$$F_{RY} = 3.52 + 3.31 + 3.52$$

$$F_{RY} = 10.35^{k/1}$$

$$F_{RX} = 0.26 + 0.96 + 0.26$$

$$F_{RY} = 1.48^{k/1}$$

$$F_R = \sqrt{(10.35)^2 + (1.48)^2}$$

$$= 10.43^{k/1}$$

$$\tan \theta = \frac{1.48}{10.35} 1.43$$

$$\theta = 8.15^{\circ}$$

Vector Diagram Check Point 5 on Done

Fig. 6.17(d) X value X['] value in A, B, C Directions.

$$\sin 30^{0} = \frac{X}{26.25'}$$
$$X = 13.125$$
$$X' = 26.25 \cos 30^{0} = 22.7'$$



Properties of Ellipse in "B" and "C" Directions

Major Axis
$$a = \sqrt{(69.125)^2 - (13.125)^2}$$

 $a = 67.9'$
 $b = 40.5'$
 $x = 22.7'$
 $y = 38.28'$
 r_z (from ollivetti Prog) = 109.97'
sin $\theta_1 = \frac{22.7'}{109.97} = 0.2065$
 $\theta_1 = 11.9^\circ$

Properties of Ellipse in "A" Direction

$$a = 63.95'$$

$$b = 38.28'$$

$$x = 0$$

$$y = 38.28$$

$$r_z(\text{from ollivetti Prog.}) = 106.83'$$

Normal forces = $N_A = \frac{373 k/1}{106.83'} = 3.49 k/ft$

$$N_B = N_C = \frac{373 k/1}{109.95} = 3.40 k/ft$$

Vector components along Radial Line

"A" Direction

$$F_{RY} = 3.49 \, k/ft$$
$$F_{RX} = 0$$

"B" Direction

$$F_{BY} = 3.40 \, k/1(\cos 11.9^\circ) = 3.33 \, k/ft$$
$$F_{BX} = 3.40 \sin 11.9^\circ 1(\cos 30^\circ) = 0.61 \, k/ft$$

"C" Direction

$$F_{CY} = 3.33 \, k/ft$$

 $F_{CX} = 0.61 \, k/ft$



$$F_R = \sqrt{(10.13)^2 + (1.22)^2}$$

 $F_R = 10.22 \, k/ft$

Point 6 on Dome

For estimation purposes the curvature in "B" & "C" will be assumed to be the same as for point 3

$$N_A = 0$$

$$N_B = \frac{373}{98.9} = 3.78 \, k/ft$$

$$N_C = \frac{373}{98.9} = 3.78 \, k/ft$$

Vector Components in X - Y Plane

"B" Direction

$$F_{BY} = 3.78 \cos 27^\circ = -3.36 \text{k/ft}$$

 $F_{BX} = 3.78 \sin 27^\circ = +1.49 \text{k/ft}$

"C" Direction

$$F_{CY} = -3.36$$

$$F_{CX} = 1.49$$

$$F_{RY} = 6.72 \, k/ft$$

$$F_{RX} = 2.98$$

$$F_r = \sqrt{(6.72)^2 + (2.98)^2}$$

$$= 7.35 \, k/ft$$

$$\tan \theta = \frac{2.98}{6.72} = 23.9150^\circ$$

Dome Prestressing Tendon Normal Forces Key 1 k/ft = 12.81734 KN/m 1ft = 0.3048

| POINT | Fry (k/ft) | Frx (k/ft) | Angle from vert. to resultant F _e | Fr (k/ ft ²) | Fr and accident 396/ 373X Fry(k/ft) |
|-------|---------------|---------------|---|-----------------------------|--|
| 1 | 9.69 | 0 | 0 | 9.69 | 10.29 |
| 2 | 10.98 | 3.56 | 18° | 11.56 | 12.27 |
| 3 | 10.97 | 2.98 | 15.2° | 11.36 | 12.06 |
| 4 | 10.35 | 1.48 | 8.15° | 10.43 | 11.07 |
| 5 | 10.15 | 1.22 | 6.85° | 10.22 | 10.85 |
| 6 | 6.72 | 2.98 | 23.92° | 7.35 | 7.80 |

Summary of tendon normal forces

Summary of forces

| Initial | Condition | Prestressing Force |
|---------|--|--------------------|
| | Jacking | 973' kip/ft |
| | Anchorage | 875 kip/ft |
| | Design ($fs = 154.2^{ksi}$) | 781 kip/ft |
| Final | Before Tendon elongation @ accident (fs 135.7 ksi) | 687 kip/ft |
| | After Tendon elongation due to accident ($fs = 144.2^{ksi}$) | 729 kip/ft |

Prestress Losses

Sources Of Design Information

| Reference No. | Reference | Page No. |
|------------------|--|-------------|
| 1 | Bellefonte Nuclear Plant, Preliminary Safety Report | |
| 2 | Design of Prestressed Concrete Structures, Second Edition T.Y. Lin | |
| 3 | Building Code Requirements for Reinforced Concrete (ACI 313 – 71) | |
| 4a | Preliminary Calculations "Hoop Tendon - Prestress Loss" EGB | |
| 4b | "Reactor Containment – Friction Loss in Horz: Tendon RWH | |
| 5 | Bellefonte N.P Design Criteria | |

6.4 Primary Containment Hoop Prestress

6.4.1 1- Prestress Losses

6.4.1.1 1- Friction Losses

PC1 Code equation for friction loss.

$$T_o = T_x e^{(kl+\mu\alpha)}$$
$$T_x = T_o e^{(kl+\mu\alpha)}$$

Notation

 T_o = steel stress (force) at jacking end T_x = steel stress (force) at any point x. k = friction wobble coefficient per foot of prestressing steel. L' = length of prestressing *steel being considered*. μ = friction curvature coefficient. α = Total angular change of prestressing steel profile in radians from jacking end to any

Given

k = 0.0003

 $\mu = 0.13$

For straight portion of Tendon use wobble only. For curved portion of Tendon use wobble and curve friction. When post tensioning from both sides, only half of the Tendon length is substituted for L'.

6.4.2 Prestress Losses

key 1ft = $0.3048 \text{ m} 1 \text{ k} = 6.895 \text{ MN/m}^2$

Let $T_0 = 1^{kip}$

Assume jacking from both ends

| | 3 0 | | | | |
|---------|--------|---------------|-------------------|-----------------------|-------------|
| Segment | L(ft) | $\alpha(rad)$ | $kl + \mu \alpha$ | $e^{-(kl-\mu\alpha)}$ | $T_x(kips)$ |
| D | 0.0 | 0 | 0.0 | 1 | 1.0 |
| DC | 15.25 | 0 | 0.004575 | 0.9954 | 0.9954 |
| BC | 101.04 | 1.44 | 0.218 | 0.804 | 0.800 |

@ mid point of Tendon point B

$$T_x = 0.800 T_0$$

 $T_x = T_x/0.800 = 1.25 T_x$

Friction loss = 25.07

- @ point D T_x = T₀ = 0.8 f_{su} = 0.8 (240 ksi) = 192 ksi
- @ point B mid point of Tendon.

$$T_x = 0.8 (T_0) = 0.8 (192^{ksi}) = 153.6^{ksi}$$

6.4.3 Prestress Losses

6.4.3.1 2- Elastic Shortening

$$\begin{split} (\varDelta ts)_{AVG} &= \frac{f_{ci}}{2E_C} \\ \varDelta f_{sAVG} &= E_S(\varDelta ts)_{AVG}(\varDelta ts)_{AVG} = \text{average value of strain loss in tendons} \\ \text{due to elastic shortening.} \\ f_{ci} &= \text{initial concrete prestress.} \\ E_C &= \text{modulus of elasticity of concrete.} \\ E_S &= \text{modulus of elasticity of steel} \\ \varDelta f_{sAVG} &= \text{average value of steel prestress loss due to elastic shoetening.} \\ f_{ei} &= 1.600 \text{ ksi} \\ (\varDelta ts)_{AVG} &= \frac{1.600}{2(5,000)} = 0.00016 \text{ in./in.} \\ \varDelta f_{sAVG} &= (29,000)(0.00016) = 4.64 \text{ ksi} \end{split}$$

6.4.4 Prestress Losses

6.4.5 3- Creep Loss

 $\Delta tc = tc f ci$ $\Delta ts = \Delta tc$ $\Delta fs = \Delta ts Es$

Notation

 $\Delta tc = \text{strain in concrete due to creep } (in./in.)$ tc = unit strain in concrete due to creep (in./in./psi) fci = initial concrete prestress (psi). $\Delta ts = \text{strain in steel due to creep } (in./in.)$ Es = modulus of elasticity of steel(ksi) $\Delta fs = \text{loss of prestress in steel due to creep } (ksi)$ $tc = 0.20\Delta \times 10^{-6}in./in./psi$ $fci = 1600 \, psi(\text{estimated}) \text{Actual} = 1.558 \, \text{psi}$ $\Delta tc = (0.000002)(1600) = 0.00032 \, in./in.$ $\Delta ts = \Delta tc = 0.00032 \, in./in.$ $\Delta fs = (0.00032)(29000 \, ksi)$ $\Delta fs = 9.280 ksi$

6.4.6 Prestress Losses

6.4.6.1 4- Shrinkage Loss

 $\Delta ts = \Delta ki \\ \Delta fs = Es \Delta ts$

Notation

 Δtc = strain in concrete due to concrete shrinkage (in./in.) Δts = loss of strain in steel due to concrete shrinkage (*in./in.*) Es = modulus of Elasticity of steel (ksi) Δfs = loss of prestress in steel Tendon due to concrete shrinkage (ksi) Δtc = 100 × 10⁻⁶(in./in.) Δfs = (29.000 × 0.0001) = 2.9 ksi Δfs = 2.9 ksi

6.4.6.2 5- Tendon Relaxation Loss

 $\Delta fs = 0.08(0.65f \text{ su})$ or $\Delta fs = 12.5 \text{ ksi}$

Notation

 $\Delta fs = loss$ of prestress in tendon due to tendon relaxation (ksi)

fsu = ultimate strength (ksi) $\Delta fs = 0.08(0.65)(240 \text{ ksi})$ = 12.48 ksi

: Use $\Delta fs = 12.5$ ksi

6.4.7 Prestress Loss

6.4.7.1 Summary of Losses

- 1. Friction losses = 25.0%
- 2. Average Elastic Shortening =4.64 ksi
- 3. Creep Loss = 9.28 ksi
- 4. Shrinkage loss = 2.90 ksi
- 5. Tendon Relaxation = 12.50 ksi

Total losses due to Creep, Shrinkage and tendon relaxation = 9.28 + 2.90 + 12.50 = 24.68ksi

6.4.7.2 Primary Containment

Hoop Prestress

Prestress Losses Tendon 1

> $t_x = 0.9954$ $\Delta fs = 0.0046(192 \, ksi)$ = 0.883 ksi .0941∴ $T_X \approx 191 \, ksi$

Average initial tendon stress @ anchoring = $70\% f_{sci}$ = 0.7/2nd = 168 ksi

For Tendon 1 use anchorage stress equal to 168 ksi plus average value of Elastic Shortening @ anchorage f_s Tendon 1 = 168 ksi + 4.64 ksi = 172.64 ksi @ critical section use f_s tendon 1 = 173 ksi.

Tendon 2

Friction Losses in Tendon @ critical Section using PC1 code Equation for Friction Loss

 $T_{o} = T_{X}e^{(KL'+\mu\alpha)}$ $T_{X} = T_{o}e^{(KL+\mu\alpha)}$ Angle between P + B and critical section = 74°52′ = 131 radians = 1.27 $L' = 70.17 \times 1.31 = 92′$ $KL' = \mu \alpha = (0.0003)(92) + (0.13)(1.31) = 0.1976$ $e^{-(KL'+\mu\alpha)=0.821°}$ $T_{X} = (0.821)(0.995)T_{o} = 0.817T_{o}$

:. For Tendon 2 $f_s = (0.817)(192) = 156.9ksi$ atcritical section. Average Initial Prestress

Average prestress (elastic shortening) = $\frac{tendon1+tendon2}{2}$ = $\frac{173+156.9}{2}$ = 164.95ksi Average Elastic Shortening Loss = 4.64 ksi \therefore Average initial prestress = 164.95 - 4.64 = 160.31 ksi

Average Final Prestress @ Critical Section

To obtain avg. final prestress @ critical section, subtract the losses due to creep shrinkage and tendon relaxation from avg. initial prestress.

Loss due to creep, shrinkage and tendon relaxation = 24.68^{ksi} Average initial prestress = 160.36 ksi Losses = 24.68 ksi Avg = Final Prestress = 135.68 ksi

Stress At 1/4 Point (0°) of Tendon

 $f_{s_{\text{tandon# 2}}} = f_{s_{\text{tandon# 2}}} \Rightarrow average f_s = f_{s_{\text{tandon# 1}}}$

Tendon#1

 $\begin{array}{l} \gamma = 70.17' \\ \alpha = 37^{\circ}.26' = 0.6533 \, RADIONS \\ l = 45.84' \\ k = 0.0003 \\ \mu = 0.13 \end{array}$

$$\begin{split} kl + \mu & \alpha = 0.0003(45.84') + 1.13(0.6533) = 0.09865\\ e^{-(kl + \mu \alpha)} &= 0.90606\\ T_x = 0.906 \ T_o(0.998)\\ f_s = 0.906(197) = 173.95 \, \text{ksi} \end{split}$$

Average f_s @ critical section: $\frac{191+156.75}{2} = 173.87 ksi$ Conclusion

Average stress at 1/4 point of Tendon is only slightly larger than average stress at critical section.

Initial Tendon Stresses Jacking Prestress

Jacking prestress = 0.8fsuJacking prestress = 0.8fsu= 192^{ksi}

Anchorage prestress

Av. initial tendon = $0.70f \, su$ stress@anchoring = $0.70(240) = 168^{ksi}$

Achoring Prestress = Avg:initial tendon stress @ anchoring plus avg = value of elastic shortenig

= 168' + 4.64'ksi

= 172.64′ksi

Initial Stress for Design

To obtain initial stress for design add the losses due to Creep, shrinkage, and 1/2 tendon relaxation loss due to the Avg: Final Prestress

Creep Loss = 9.28 ksi Shrinkage Loss = 2.90 ksi $\frac{1}{2}$ Tendon relaxation loss = 6.25 ksi Av. final prestress $\frac{135.68}{154.11 \text{ ksi}}$ Initial stress for Design = 154.11 ksi

Final Prestress Force Sketch

Notes:

- (1) Controlling load case is Equation T in PSAR pg.
- (2) Earthquake load has no effect on required hoop prestress.
- (3) NO principal stress check is required for this case.
- (4) Temp: analysis calculations by NP 2-1-72 are ok. For Hoop direction.



6.4.7.3 Final Prestress Force

Design Assumptions

- (1) Concrete is not counted on to resist tension.
- (2) Liner load (L) and reinforced steel force (R_s) exactly balance; $R_s = L$

This is reasonable and conservative. As the cylinder expands due to pressure, the value of R_s increases; while the value of L decreases. At some value of cylinder deformation R_s and L are equal and opposite. Further deformation leads to Rs becoming greater than L, As $L \rightarrow 0$.

Loading:

 $p = 50 \text{psi} \quad P_{\text{Design}} = P_d = 1.5P = 1.5(50)$ $P_d = 75 \text{ psi}$ $P_d.D_o = (0.75 \text{ k/in.}^2)(144 \text{in}^2/\text{ft}^2)(135 \text{ ft})$ $P_d.D_o = 1459 \text{ K/ft}$ from $\sum F_{11} = 0 \quad 2F = P_d.D_o = 1458 \text{ K/ft}$ F = 729 k/ft from $\Sigma F_{11} = 0.2F = P_d \cdot D_o = 1458 \text{ ft } F = 729 \text{ } k/\text{ft}$ This is the final prestressing force neglecting tendon elongation @accident. The 'final' force @ accident + (As sargent & Lundy specify it) would be: $F_{\text{final}} = F(\text{final stress before Ave/final stress before accident} + (\Delta f_s) \text{ accident})$

Before accident $f_e = \frac{F}{Area} = \frac{729}{12(41.75)} \approx 1.455^{ksi}$ Close approximation $\in_c \cong$ concrete strain (in./in.) $f_c \cong \text{concrete stress (ksi)}$ $E \cong$ modulus of elasticity (ksi) $\epsilon_c = \frac{f_c}{E_c} = \frac{1.455^{\text{ksi}}}{5000 \text{ksi}} = 0.00291 \text{ in./in.}$ At accident \in_{c} goes to zero $\Delta f_s = \text{increase in steel stress}(ksi)$ $E_s =$ modulus of elasticity of steel (ksi) $\Delta f_s = E_s$ (increase in steel strain which is equal to the loss of conc : strain) $\Delta f_s = E_s t_c = 29000^{ksi} (0.000291)$ $\Delta f_s = 8.439^{ksi}$ Final tendon stress before accident = 135.68ksi Final tendon stress after accident = Final before accident + $\Delta f_s = 135.68 + 8.349 = 144.12$ ksi Final prestress Force = 729, (135.68) = 686.31 k/ft

Initial Forces

Jaking force = $\frac{\text{Jacking tendon stress}}{\text{Avg}: \text{final prestress}}$ (final prestress force) = $\frac{192^{ksi}}{135.68}$ (678 k/ft) = 972.17 k/ft

For Jacking Force use 973 kip/ft Anchorage Force

> Anchorage forec $= \frac{\text{Avg:initial tendon stress@anchoring}}{\text{Avg final prestres}} (\text{final prestress force})$ $= \frac{172.64}{135.68}$ 687 k/ft 874.14 k/ft

For anchorage force use 875 kip/ft Initial Forces for Design

Initial force design
= (finalforce @ accident)
$$\frac{(\text{initial stress for design})}{\text{Avg}: \text{ final prestress}}$$

= (678) $\frac{154.11}{135.68}$
= $\frac{780.32 k}{ft}$

:. For initial force for design use 781.0k/ft

$$f_{sci}$$
 = concrete stress = $\frac{P}{\text{area}} = \frac{780.5}{12 \times 41.75}$
= 1.558 ksi < f_c allowable = 0.30 f_i = 1650 ksi

Estimated min spacing for stoop tendons

$$S_{\min} \cong \min \text{ spacing}$$

$$S_m = \frac{(\text{area of tendon})(\text{Av}: \text{ final prestress})}{\text{final prestress force (a) acci}}$$

$$= \frac{(170 \text{ wries})(0.00491B''/\text{wire})(135.68 \text{ ksi})}{687 \text{ k/ft}}$$

$$S_m = 1.6485ft = 19.78in$$

Equipment Hatch Tendon layout (horizontal)

Tendon 1(T₁) Radius = 20' $a'_1 = x'_1 = 20 \sin 20^\circ = 6.84'$ Avc length = $\frac{\pi(20)(20)}{180} = 6.98'$ $\dot{b}_1 = \dot{y}_1 = 20(20^2x'_1) = 1.21'$ $b_2 = y_2 = 11.375' - 2\dot{y}_1 = 8.96'$ $a_2 = x_2 = \frac{42'}{\tan 20^\circ} = 24.62'$ $2x_1 + x_2 = 38.30$

The straight portion of the tendon is an ellipse but for simplicity the length is assumed to be $(a_2^2 + b_2^2)^{1/2}$

 a_2 is an arc length OK Tendon 2 (T₂)

$$2a_1 + a_2 = 38.30''$$

$$2b_1 + b_2 = 11.375' - 2.625 = 8.750$$

Let $\theta = 14.806^{\circ}$

 $a_1 = 20 \sin \theta = 5.111$ radius = 20'Arc length $= = \pi (20)\theta = 5.168$



Fig. 6.19 Horizontal tendon layout for equipment hatch

$$b_{1} = 20 - (2\theta^{2} - a_{1}^{2})^{\frac{1}{2}} = 0.644$$

$$b_{1} = 8.75 - 2b_{1} = 7.422$$

$$a_{2} = \frac{b_{2}}{\tan \theta} = 28.078$$

$$2a_{1} + a_{2} = 38 - 30$$

$$2c_{1} + c_{2} = x - y_{1}$$

$$a_{1} = R \sin \phi \quad b_{1} = R \sin \theta_{2}$$

$$Arc_{1} = \frac{\pi R \theta_{1}}{180} \quad Arc_{2} = \frac{\pi R \theta_{2}}{180}$$

$$c_{1} = R - (R^{2} - a_{1}^{2})^{\frac{1}{2}} \quad d_{1} = (R^{2} - b_{1}^{2})^{\frac{1}{2}}$$

$$c_{2} = x - y - 2c_{1} \quad d_{2} = x - y_{2} - 2d_{1}$$

$$a_{2} = \frac{c_{2}}{\tan \theta_{1}} \quad b_{2} = \frac{d_{2}}{\tan \theta_{2}}$$

Solve for θ_1 by trial and error. 2R; = 38.3 sin θ_2 + (2 $R_i - x_i - y_i$) $a_2\theta_2$

let $\phi_1 = 16.16^{\circ}$ $R = 21(T_3)$ let $\phi_2 = 11.857^{\circ}(T_4)$ $2a_1 + a_2 = 39.30$ $2b_1 + b_2 = 38.30$ $2c_1 + c_2 = 9.375'$ $2d_1 + d_2 = 7.125'$ $a_1 = 21 \sin \theta_1 = 5.845$ $b_1 = 21 \sin \theta_2 = 4.315$ Arc $= \frac{\pi 2 \phi \theta_1}{180} = 5.923$ Arc $= \frac{\pi 21\theta}{180} = 4.346$ $c_1 = 21 - (21^2 + a_1^2)^{\frac{1}{2}} = 8.30$ $d_1 = 21 - (21^2 + b_1^2)^{\frac{1}{2}} = 0.448$ $c_2 = 9.735' - 2c_1 = 7.716$ $d_2 = 7.125 - 2d_1 = 6.229$ $a_2 = \frac{c}{\tan \phi_1} = 24.426$ $b_2 = \frac{d_2}{\tan \phi_2}$





 $2b_2 + b_2 = 38.289 Ok$ $2a_2 + a_2 = 34.316 Ok$

6.4.7.4 Equipment Hatch

Tendon Layout (Horizental) Deflected Tendon

| Tendon | R | θ_i | a_{1i} | a_{2i} | c_{1i} | C_{2i} | $A_{\rm rc}$ | Α | X | у |
|--------|-----|------------|----------|----------|----------|----------|--------------|--------|-------|--------|
| T1 | 20' | 20° | 6.84 | 24.62 | 1.21 | 8.96 | 6.98 | 26.200 | 11.75 | 0.375 |
| T2 | 20' | 14.806 | 5.111 | 22.078 | 0.661 | 7.422 | 5.163 | 29.042 | 11.75 | 2.625 |
| Т3 | 21' | 16.16 | 5.845 | 26.226 | 0.830 | 7.716 | 5.923 | 27.721 | 12.75 | 3.375 |
| T4 | 21' | 11.875 | 4.315 | 29.668 | 0.448 | 6.229 | 4.346 | 30.315 | 12.75 | 5.625 |
| T5 | 22' | 12.41 | 4.728 | 28.844 | 0.514 | 4.097 | 4.765 | 29.134 | 13.75 | 6.375 |
| T6 | 22' | 8.306 | 3.178 | 33.523 | 0.231 | 4.894 | 3.189 | 33.878 | 13.75 | 8.625 |
| T7 | 23' | 8.789 | 3.514 | 31.271 | 0.270 | 4.835 | 3.528 | 31.643 | 14.75 | 9.375 |
| T8 | 23' | 4.917 | 1.971 | 34.357 | .085 | 2.956 | 1.974 | 34.484 | 4.75 | 11.625 |
| Т9 | 24' | 53.47 | 2.236 | 33.928 | o.104 | 3.166 | 2.240 | 33.976 | 15.75 | 12.375 |
| T10 | 24' | 1.715 | 0.718 | 36.855 | .011 | 1.103 | 0.718 | 36.872 | 15.75 | 14.625 |
| T11 | 25' | 2.107 | 0.919 | 36.455 | .017 | 1.341 | 0.919 | 36.480 | 16.75 | 15.375 |

Purpose

To determine the curvature and radii of the deflected tendons occurred the equipment hatch.

Data

See drawing 41N711-A for size of equipment hatch and tendon size and spacing.

Assumptions

- 1- Tendons deflected along the circular curve on the developed elevation
- 2- Maximum angle of deflection of 70°
- 3- Centreline of tendon assumed 1'-0" from the edge of hatch sleeve.

References

- 1- Dwgs 41N711-1 thru-4
- 2- Calculation by HRT "Equipment" Hatch Tendon layout 11-9.72
- 3- Olivetti program by Rw Hanorton "Tendon Deflection"

Discussion

Due to cross found in HRTS calculations (Equp: Hatch Tendon Layout) the following will be a revised set of calculations.

Calculations

Tendon 1 Radius = 20', $x_1 = 20 \sin 20^\circ = 20(0.342^\circ 02) = 6.24'$ Using Pyth's theorem to find y_1 ..

$$y_1 = 20 - (20^2 - x_1^2)^{1/2} = 20 - 18.79 = 1.21'$$

$$y_2 = 12' - 4\frac{1''}{2} - 2y_1 = 12' - 0.375' - 2.42' = 9.21'$$

From *AAEC*

$$X_2 = \frac{y_2}{\tan 20^\circ} = \frac{9.21}{0.363} = 25.3'$$

$$2x_1 + x_2 = 13.68 + 25.3 = 38.98' \text{say } 39'$$

$$Arc \text{ Length} = \frac{\pi(20)(20)}{180} = 6.98'$$

| Loading | N_{ϕ}' | $N_{	heta}'$ | $N_{\phi 	heta}'$ |
|--|---|---|-------------------|
| w/unit area of surface per m ² of surface Normal $\downarrow \downarrow $ | $-\frac{wr_01-\cos^3 d\phi}{3\sin^2 d\phi\cos^2 d\phi}$ | $\frac{wr_0 2 - 3\cos^2 \partial \phi + \cos^2 \partial \phi}{3\sin^2 \partial \phi}$ | 0 |
| <i>p</i> /unit area of projection | $-\frac{\rho r_0}{2\cos d\phi}$ | $-\frac{pr_0}{2}\cos\partial\phi$ | 0 |

 Table 6.4
 Membrane forces in parabolic domes

6.5 Computer Program NIZAM

A typical computer program, NAZAM, is developed for the spherical dome shape made in reinforced concrete. With small changes incorporated, the same dome can be analysed in any material, provided correct data can be included. The NAZAM listing is given below.

Computer program: NAZAM listings

```
С
   *
      TITLE: COMPUTER AID ANALYSIS OF THIN SHELLS
С
        : Dr. Y. BANGASH
   С
    * The original program was modified by NIZAM of Malaysia,
С
С
    * under the supervision of Y. Bangash.
С
   С
           COMPUTER PROGRAM FOR CASE STUDIES
С
   *
           _____
С
   * THIS IS A PROGRAM TO FIND OUT THE MERIDIAN
   * FORCES, THE HOOP FORCES AND RING TENSION ACTING
С
                                           *
С
   * ON EACH SECTION OF THE SPHERICAL DOME DUE TO ITS
С
   * DEAD LOAD AND IMPOSED LOAD.
                                           *
    С
С
С
    С
    =
                   * NOTATIONS *
                                           =
С
    =
                                           =
С
           OK UNIFORMLY DISTRIBUTED LIVE LOAD
С
    =
           GK UNIFORMLY DISTRIBUTED DEAD LOAD
                                          =
С
          TY THICKNESS OF THE DOME
С
          HI RISE AT POINT 1
    _
С
          HO RISE AT POINT 0
    =
С
          A LENGTH OF LATITUDE AT POINT 1
   =
                                           =
С
          B LENGTH OF LATITUDE AT POINT 0
    =
С
   =
                                           =
С
С
```

```
С
С
      REAL LY, LX, X, Y, AS, ASR, BAR, SP
С
3000 WRITE (6, 10)
      FORMAT (1X, 'INPUT THE SPAN UNI FORMLY
      DISTRIBUTED LIVE LOAD')
      READ (5, *) QK
      WRITE (6, 15)
15
      FORMAT (/, 1X, 'INPUT THE DEAD LOAD')
      READ (5, *) GK
      WRITE (6, 20)
     FORMAT (/, 1X, 'INPUT THE THICKNESS OF THE DOME')
20
      READ (5, *) T
      WRITE (6, 30)
30
      FORMAT (/, 1X, 'INPUT THE SINO')
      READ (5, *) SINO
      WRITE (6, 40)
      FORMAT (/, 1X, 'INPUT SIN1')
40
      READ (5, *) SIN1
      PRINT*, 'SP=', SP
      IF (ASR.GE.141.AND.ASR.LE.226.AND.SP.GE.125.AND.SP.LE.200)
            GO TO 25
      *
      IF (ASR.GE.226.AND.ASR.LE.355.AND.SP.GE.150.AND.SP.LE.200)
           GO TO 27
      *
      IF (ASR.GE.392.AND.ASR.LE.532.AND.SP.GE.150.AND.SP.LE.200)
      *
            GO TO 29
      IF (ASR.GE.565.AND.ASR.LE.904.AND.SP.GE.125.AND.SP.LE.200)
      *
            GO TO 31
      IF (ASR.GE.1005.AND.ASR.LE.1340.AND.SP.GE.150.AND.SP.LE.200)
      *
            GO TO 33
      IF (ASR.GE.1571.AND.ASR.LE.2094.AND.SP.GE.150.AND.SP.LE.200)
           GO TO 35
      *
      IF (ASR.GE.2454.AND.ASR.LE.2805.AND.SP.GE.175.AND.SP.LE.200)
            GO TO 3740
      *
      WRITE (6,500)
500
     FORMAT(/,16X, 'HALTED IN REINFORCEMENT')
      STOP
      PRINT*, 'BAR=6'
25
      RETURN
     PRINT*, 'BAR=8'
27
      RETURN
      PRINT*, 'BAR=10'
29
      RETURN
     PRINT*, 'BAR=12'
31
      RETURN
      PRINT*, 'BAR=16'
33
      RETURN
35
     PRINT*, 'BAR=22'
      RETURN
      PRINT*, 'BAR=25'
37
      RETURN
      END
```

6.5 Computer Program NIZAM

| c | * SUBROUTINE TO FIND MOMENT COEFFICIENT | * |
|-----|---|------|
| C | *************************************** | *** |
| C | | |
| 0 | SUBROUTINE TABL12 (LY.LX.X.Y) | |
| | TF(RATTO.GT.3.0) GOTO 160 | |
| | F(RATTO, EO, 3.0) GOTO 81 | |
| | F(RATTO, GE. 2.5) GOTO 82 | |
| | IF (RATTO.GE.2.0) GOTO 83 | |
| | IF (RATTO.GE.1.8) GOTO 84 | |
| | IF(RATIO.GE.1.5) GOTO 85 | |
| | IF(RATIO.GE.1.4) GOTO 86 | |
| | IF(RATIO.GE.1.3) GOTO 87 | |
| | IF(RATIO.GE.1.2) GOTO 88 | |
| | IF(RATIO.GE.1.1) GOTO 89 | |
| | IF(RATIO.GE.1.0) GOTO 90 | |
| 81 | X=0.124 | |
| | Y=0.014 | |
| | RETURN | |
| 82 | X=0.122 | |
| | Y=0.020 | |
| | RETURN | |
| 83 | X=0.118 | |
| | Y=0.029 | |
| | RETURN | |
| 84 | X=0.113 | |
| | Y=0.037 | |
| | RETURN | |
| 85 | X=0.104 | |
| | Y=0.046 | |
| | RETURN | |
| 86 | X=0.099 | |
| | Y=0.051 | |
| | RETURN | |
| 87 | X=0.093 | |
| | Y=0.055 | |
| 0.0 | RETURN | |
| 88 | X=0.084 | |
| | Y=0.059 | |
| 0.0 | KETUKN | |
| 89 | X=0.061 | |
| | | |
| 0.0 | KEIUKN V-0.062 | |
| 90 | X-0.062 | |
| | | |
| 160 | WRITE (6 170) | |
| 170 | FORMAT(// 16X SLAB TOO NARROW - DESTEN AS ONE WAY SDANNIN | C1 \ |
| 1/0 | RETURN | J) |
| | END | |
| | | |
6.6 Conoidal dome's surfaces

A conoidal dome is analysed in this section. The dome can be of any material but the geometry of this surface is different from the spherical surface. Using Figure 6.1 the radius of the circle of latitude for the conoidal dome is, $r \sin \phi - r'$.

Consider the conoidal dome shown in Figure 6.17, say, between a plane of latitute through points 0 and 1.

Length of element = $r \times d\phi$

Area of element rotated about axis = $r d\phi \times 2\pi (r \sin \phi - r')$ Tatal surface area 4, of doma is:

Total surface area A, of dome is:

$$A = \int_{\phi_0}^{\phi_1} r \, d\phi \times 2\pi (r \sin \phi - r')$$

= $2\pi r^2 (\cos \phi_0 - \cos \phi_1) - 2\pi r r' (\phi_1 - \phi_0)$ (6.33)

Assuming a uniform distributed load (M, W) for all elements

Total load between points 1 and 0 is:

$$W_u = 2\pi r^2 W(\cos\phi_0 - \cos\phi_1) - 2\pi r W(\phi_1 - \phi_0)$$
(6.34)

To find the meridional thrust T Substituter $\sin \phi_1 - r' \operatorname{forr} \sin \phi$. Then

$$W = 2\pi (r \sin \phi_1 - r')$$

$$T = W/(2\pi (r \sin \phi_1 - r') \sin \phi_1)$$
(6.35)



Fig. 6.17(f) Conoidal dome

To find the hoop force H

$$T/r + H/(r\sin\phi_1 - r') \times \sin\phi_1 - [W + W'(\phi_1 - \phi_0)]\cos\phi_1 = 0$$
$$H = \frac{r\sin\phi_1 - r'}{r\sin\phi_1} [-T + [W + W'(\phi_1 - \phi_0)]r\cos\phi_1$$

If the dome is continuous along the circle of latitude through 1, a circular ring through that point is subjected to a unit radial force of $T \times \cos \phi_1$. Therefore

$$S \text{ (ring tension)} = \frac{W_u \times \cos \phi_1}{2\pi \times \sin \phi_1} \tag{6.36}$$

Three examples are included to analyse a conical surface. They are based on:

Example 6.2 –Conical tent under surface or dead weight Example 6.3 –Conical tent under uniform load WExample 6.4 –Conical umbrella roof supported on a central column.

Another example (Example 6.5) is given on a truncated conical dome type tent. General solutions are incorporated. By introducing specific data the same shape can be incorporated for any material such as plastic, glass, fabric, concrete and steel/aluminum. Table 6.5 gives other cases under different loads for conical and truncated conical dome shapes.

Example 6 Conical dome tent

The conical dome tent (Fig. 6.18) is generally used for roofs and closures for storage structures and temporary dwellings.

Conical tent under selfweight of deadweight For the analysis the value of r_1 is α and

$$r_0 = r_e \sin \phi = r_2 \cos \alpha$$

where α is the semi-angle at the apex *C*.

$$W = \text{Load} = \int_0^y 2\pi r_0 w \, dy = \pi w y^2 \sin \alpha$$
 (6.37)

| Туре | Loading | Resultant components | N_{ϕ} | N_{θ} | T_{θ} |
|------|---------|---|---|---|--------------|
| 1 | p_s | $w \mathrm{d}s \sin \alpha = p_s$ | $\frac{\omega_{\alpha}}{2S} \frac{L^2 - S^2}{\sin \alpha}$ | $-\omega \mathrm{d}s\cos\alpha\cot\alpha$ | 0 |
| 2 | p_t | $w \mathrm{d}t \cos \alpha = p_t$ $p_s = w_L \sin \alpha \cos \alpha$ | $\omega_L \frac{L^2 - S^2}{2S} \cot \alpha$ | $-\omega_L S \cos^2 \alpha \cot \alpha$ | 0 |
| 3 | p_t | $p_t = -\omega \cos^2 \alpha$ $p_t = -p \sin \alpha \cos \theta$ | $p[L^2 - S^2] \frac{(1/3)S^2 - (1/2S)\sin^2 \alpha}{\cos \alpha / \cos \theta}$ | $p \frac{L^2 - S^2}{3S^2} \sin \theta$ | |

 Table 6.5
 Conical and truncated conical dome shapes

Fig. 6.18 Conical dome tent



$$N_{\phi} = -\frac{w_y}{2\cos\alpha} \tag{6.38}$$

$$N_{\theta} = -w_{v} \sin \alpha \cos \alpha \tag{6.39}$$

Example 6 Conical dome tent under uniform load w

(Figs. 6.19 and 6.20)

Let the vertical distance be represented by 'z'. The total load w_z and stress resultants N_{ϕ} and N_{θ} are computed as given below:

$$A = \text{Surface Area}$$
$$= 2\pi \int_0^h z \tan \alpha \sec \alpha \, dz$$
$$= \pi h^2 \tan \alpha \sec \alpha$$
(6.40)

V =Volume

$$V = \pi \int_0^h z^2 \tan^2 \alpha dz \tag{6.41a}$$

$$=\frac{\pi}{3}h^2\tan^2\alpha \tag{6.41b}$$

$$w_z = w\pi z^2 \tan \alpha \sec \alpha$$

$$\phi = (90^\circ - \alpha)$$
(6.41c)

6.6 Conoidal dome's surfaces





$$N_{\phi} = -\frac{w_z}{2\pi r_2 \sin^2 \phi} = -\frac{w\pi z^2 \tan \alpha \sec \alpha}{2\pi r \cos \alpha}$$

$$= -\frac{w_z^2 \tan \alpha \sec \alpha}{2z \tan \alpha \cos \alpha} = -\frac{1}{2} w_z \sec^2 \alpha$$

$$N_{\theta} = -r_2 w \sin \alpha = -w_z \tan^2 \alpha$$
(6.41e)

Example 6.4 Conical umbrella roof supported on a central column

The analysis of the conical umbrella roof is shown in Figure 6.21. The roof is subjected to a uniform load w/unit area. The stress resultants are computed together with load between parallel circles.

The load on the surface between parallel circles A-A and B-B, i.e. on surface below z''

$$W_{AB} = w\pi (h^2 - z^2) \tan \alpha \sec \alpha \tag{6.41f}$$

Equilibrium of vertical forces at level A-A gives

$$N_{\phi} \cos \alpha 2\pi z \tan \alpha = W_{AB} \tag{6.41g}$$

$$N_{\phi} = \frac{w(h^2 - z^2)\sec^2\alpha}{2z}$$
(tensile) (6.41h)

with $R_2 = Z \tan \alpha \sec \alpha$

$$N_{\theta} = -w_Z \tan^2 \alpha; \quad N_{\phi} \to \alpha \text{ as}Z \text{ tends to zero.}$$
 (6.41i)

This indicates that membrane theory is inadequate since bending moments a brought into play.





Fig. 6.21 Conical umbrella roof supported on a central column



 $N_{\phi} \cos \alpha$ = the value of the vertical force in ϕ direction.

$$\bigwedge_{\phi}^{N_{\phi}} \bigwedge_{\phi}^{N_{\phi}} \cos \alpha$$
(6.43)

 N_{ϕ} and $N_{\phi} \cos \alpha =$ two components in ϕ direction.

$$r_2 z \tan \alpha \sec \alpha$$
 (6.44)

 $r_2 z \tan \alpha \sec \alpha =$ the inclined component.

Truncated conical dome

The conical dome is truncated at a length S_0 , and obviously the values of N_{ϕ} and N_{θ} will be affected. The generalized equation for N_{ϕ} and N_{θ} for a full length is given by

| | | Table 6 | .6 Truncated conical d | omes | |
|-------|------------------------------|-------------------------------------|---|--|---------------------------------------|
| T | T 1' | Resultant | 37 | 37 | T |
| I ype | Loading | components | N_{ϕ} | N_{θ} | 1 |
| 1 | w/unit area | $w\mathrm{d}s\sin\alpha=p_S$ | $-w_{\rm d}\frac{S^2-S_0^2}{2R}\frac{L}{\sin\alpha}$ | $-w_{\mathrm{d}S}\cos\alpha\cot\alpha$ | 0 |
| | | $-w d \cos \alpha = p_r$ | . 2 . 2 | | |
| 2 | <i>p</i> /unit area | $p_S = w_L \sin \alpha \cos \alpha$ | $-w_L \frac{\sin^2 - S_0^2}{2S} \cot \alpha$ | $-w_{LS}\cos^2\alpha\cot\alpha$ | _ |
| | | $p_1 = -w_L \cos^2 \alpha$ | | | |
| 3 | <i>p_r</i> /radius | $p_r = p \sin \alpha \cos \theta$ | $-\frac{p_S S}{3} \left[\cos \alpha - \frac{1}{3 \cos \alpha} \right]$ | $-p_S \cos \alpha \cos \theta$ | $-\frac{p_S^2-S_0^2}{3S^2}\sin\theta$ |
| | | | $-\frac{S_0^2}{S^2}\left(\cos\alpha-\frac{1}{\cos\alpha}\right)$ | | |
| | | | $-\left(\frac{S_0^3}{S_0}\frac{2}{3\cos\alpha}\right)\right]\cos\theta$ | | |
| 4 | p_w /unit | $S_{0} = 0$ | $-p_w \frac{S_0}{S} \frac{1}{\sin \alpha}$ | _ | 0 |
| | area | | $\frac{p_w}{2\pi S \sin \alpha \cos \alpha}$ | - | $\frac{pL^2 - S^2}{2S^2}\sin\theta$ |



Fig. 6.22 Truncated shapes

$$N_{\phi} = -\frac{1}{S} \left[\frac{wS^2}{2\sin\alpha} + \operatorname{const} C \right]$$
(6.45)

$$N_{\theta} = -wS\cos\alpha\cot\alpha \tag{6.46}$$

Table 6.5 gives a good description of a truncated conical dome. Table 6.6 shows other loading cases for conical roofs and truncated domes.

Example 6 Truncated conical dome type tent

Data: Uniform load W (excluding at the top of the opening= 2.394 kN/m^2 .

Uniform load (daylight lantern = 0.035 kN/m)

Determine the stress resultants and the compressive stress for the truncated conical dome.

$$N_{\phi} = -\frac{1}{S} \left[\frac{wS^2}{2\sin\alpha} + C \right]$$

For a truncated conical shell for a sloping length of S_0

$$N_S = 0$$
 at $S_0 0 = -\frac{1}{S_0} \left[\frac{w S_0^2}{2 \sin \alpha} + C \right]$

or

$$C = -\frac{wS_0^2}{2\sin\alpha}$$
$$N_{\phi} = \frac{w(S^2 - S_0^2)}{2S\sin\alpha}; \quad N_{\theta} = -wS\cos\alpha\cot\alpha$$

Determination of α and S_0

$$\tan \alpha = \frac{3.66}{\left(\frac{15.24}{2} - \frac{3.04}{2}\right)} = 0.6 \quad \therefore \alpha = 30^{\circ} 58'$$

Sloping length $S = \sqrt{(3.66^2 + 6.1^2)} = 7.114 \,\mathrm{m}$

$$\therefore \frac{7.114}{7.114 + S_0} = \frac{6.1}{7.62}$$
$$S_0 = 1.773 \,\mathrm{m}$$

Forces due to dead weight $N_{\theta} = -wS \cos \alpha \cot \alpha = -1.368S$ For $S = S_0 = 1.773 \text{ m}$ $N_{\theta} = -2.426 \text{ kN/m}$ S = 7.114 m $N_{\theta} = -9.732 \text{ kN/m}$

$$N_{\phi} = -2.394 \frac{S^2 - (1.773)^2}{2S} \left(\frac{1}{0.5145}\right) = \frac{2.33(S^2 - 3.144)}{S}$$

For $S = S_0 = 1.773 \text{ m}$; $N_{\phi} = 0$ S = 7.114 m; $N_{\phi} = -2.33 \frac{(7.104)^2 - 3.144}{3.114}$

 $= -15.546 \, kN/m$

Forces due to uniform vertical load at top edge

$$N_{\phi} = -w' \cdot \frac{1}{\sin \alpha} \cdot \frac{1.773}{S} \\ = -0.0035 \times \frac{1.773}{S} \times \frac{1}{0.5145} \\ = \frac{-0.0121}{S}$$

For $S = S_0 = 1.773$; $N_{\phi} = -0.0068 \text{ kN/m}$ S = 7.114; $N_{\phi} = -0.0027 \text{ kN/m}$

Total $N_{\phi(\text{max})} = (-0.0027) + (-15.546) = 15.5487 \,\text{kN/m}^2$

Max. compressive stress
$$=\frac{15.5487}{0.075 \times 1} = 207.316 \text{ kN/m}^2$$

= 0.207316 N/mm²

Computer program: Conoidal domes

```
С
С
       TITLE: COMPUTER AID ANALYSIS OF THIN SHELLS
                                                 *
С
         : Dr. Y. BANGASH
    С
С
    * Assisted by NIZAM of Malaysia
С
    *******
С
С
    * THIS IS A PROGRAM TO FIND OUT THE MERIDIAN
С
    * FORCES, THE HOOP FORCES AND RING TENSION ACTING
С
    * ON EACH SECTION OF THE CONOIDAL DOME DUE TO ITS
С
    * DEAD LOAD AND IMPOSED LOAD.
С
    С
С
С
    _____
С
    =
                      * NOTATIONS *
                                                  _
С
    -
С
        GK UNIFORMLY DISTRIBUTED LIVE LOAD
    =
С
       QK UNIFORMLY DISTRIBUTED DEAD LOAD
    =
                                                  _
С
        TX THICKNESS OF THE DOME
    =
С
         R THE RADIUS OF CURVATURE
    _
С
    =
         R1 DISTANCE FROM AXIS OF ROTATION
                                                  =
С
      X(I) LENGTH OF LATITUDE AT POINT I
    =
                                                  _
С
    = AE(I) AREA BETWEEN POINT 1 AND I
С
        WC COLLAR LOAD
    =
                                                  =
С
    = WU(I) TOTAL LOAD BETWEEN POINT 1 AND I
                                                  =
С
    = T(I) MERIDIONAL THRUST AT POINT I
                                                  =
С
    = TS(I) STRESS DUE TO MERIDIONAL THRUST AT POINT I
С
      H(I) HOOP FORCE AT POINT I
    =
                                                  =
С
    = HS(I) STRESS DUE TO HOOP FORCE AT POINT I
                                                  =
С
    = S(I) RING TENSION AT POINT I
                                                  =
С
        SC COMPRESSION IN EDGE MEMBER AT THE OPENING
    =
С
    = SN(I) SIN ANGLE AT POINT 0
С
    = CS(I) COSINE ANGLE AT POINT 0
                                                  _
С
    = PIE(I) ANGLE AT POINT 0 IN RADIAN
                                                  =
С
    = SN(I) SIN ANGLE AT POINT 1
С
    = CS(I) COSINE ANGLE AT POINT 1
                                                  =
С
    = PIE(I) ANGLE AT 1 IN RADIAN
                                                  =
С
    _____
С
С
    REAL QK, GK, WC, TX, R, R1, Q1, PI, SC
    REAL X(1:6), Y(1:6), Z(1:6), SN(1:6), CS(1:6), PIE(1:6),
    REAL S(1:6), AE(1:6), WU(1:6), T(1:6), TS(1:6), H(1:6)
    REAL HS(1:6), XB(1:6)
3000 WRITE(6, 10)
    FORMAT (1X, 'INPUT THE UNIFORMLY DISTRIBUTED LIVE LOAD')
10
    READ(5, *) QK
    WRITE(6, 15)
15
    FORMAT(/, 1X, 'INPUT THE DEAD LOAD')
    READ(5, *) GK
```

| | WRITE(6, 17) |
|-------|---|
| 17 | FORMAT(/, 1X, 'INPUT COLLAR LOAD') |
| | READ(5. *) WC |
| | WPTTF(6, 20) |
| 20 | EODMAT(/ 1Y) TNDUT THE THEORNESS OF THE DOME() |
| 20 | FORMAI(/, IX, 'INPUT THE THICKNESS OF THE DOME') |
| | READ(5, $*$) TX |
| | WRITE(6, 50) |
| 50 | FORMAT (/, 1X, `INPUT THE RADIUS OF THE CURVATURE') |
| | READ(5, *) R |
| | WRITE(6, 60) |
| 60 | FORMAT (/, 1X, 'INPUT DISTANCE FROM THE AXIS OF ROTATION') |
| | READ(5, *) R1 |
| | METTE(6, 70) |
| 70 | WAIIE(0, 70) |
| 70 | FORMAI(/, IX, INPUT THE LENGTH ALONG THE X-AXIS) |
| | READ(5, $*$) X(1), X(2), X(3), X(4), X(5), X(6) |
| | DO 80 I=1,6 |
| | XB(I) = R1 + X(I) |
| 80 | CONTINUEDO 81 I=1,6 |
| | Y(I)=SQRT((R**2)-(X(I)**2)) |
| 81 | CONTINUE |
| | 01=2400 |
| | PT=3.142 |
| | DO 90 T=1.6 |
| | Z(T) = SORT((Y(T) * 2) + ((R1 + Y(T)) * 2)) |
| 90 | CONTINIT |
| 90 | CONTINUE DO 100 I-1 C |
| | D = 100 = 1.76 |
| 100 | SN(1) = (R1 + X(1)) / Z(1) |
| 100 | CONTINUE |
| | DO 100 1=1,6 |
| | CS(I) = Y(I) / Z(I) |
| 110 | CONTINUE |
| | DO 120 I=1,6 |
| | PIE(I)=ASIN(SN(I)) |
| 120 | CONTINUE |
| | DO 130 I=1,6 |
| | AE (T) = 2* PT* R** 2* (CS (1) - CS (T)) - 2* PT* R* R1* (PTE (T) - PTE (1)) |
| 130 | CONTINUE |
| 100 | DO 1/0 T=1.6 |
| | $\operatorname{HII}(T) = \operatorname{Ar}(T) * (\operatorname{CR}(\operatorname{AR}) + \operatorname{HIC} 2 * \operatorname{DT} * \operatorname{V}(T) + (\operatorname{CR}) * (\operatorname{DTR}(T) - \operatorname{DTR}(T))$ |
| 140 | WU(1)-AE(1)~(GATQA)+WC~2~P1~A(1)+(QATGA)~(P1E(1)-P1E(1)) |
| 140 | CONTINUE |
| C | SC=COMPRESSION IN EDGE MEMBER AT OPENING |
| | $SC = (WC^* 2^* P1^* (R1 + X(1))^* CS(1)) / (2^* P1^* SN(1))$ |
| С | T1=MERIDIONAL THRUST AT POINT 1 |
| | DO 150 I=1,6 |
| | T(I)=WU(I)/((2*PI)*(R*SN(I)-R1)*SN(I)) |
| 150 | CONTINUE |
| С | |
| С | TS1=STRESS AT POINT 1 DUE TO MERIDIONAL THRUST |
| - | DO 160 T=1.6 |
| | T = T T |
| 160 | |
| T 0 0 | CONTINUE |
| C | |
| C | TO FIND THE HOOP FORCE |

```
С
      H1=HOOP FORCE AT POINT 1
      DO 170 I=1.6
      H(I) = ((R*SN(I) - R1) / (R*SN(I)))*(-T(I) + (GK+QK)*R*CS(I))
170
      CONTINUE
С
С
      HS1=STRESS DUE TO HOOP FORCE
      DO 180 I=1,6
      HS(I) = H(I) / TX
180
      CONTINUE
С
С
      S1=RING TENSION IN EDGE MEMBER
      DO 190 I=1,6
      S(I) = (WU(I) * CS(I)) / (2* PI* SN(I))
190
      CONTINUE
С
      PRINT 191
      PRINT 192
     FORMAT(///,31X, 'OUTPUT RESULTS')
191
     FORMAT(31X, '**********')
192
      WRITE(6,200) XB(1), XB(2), XB(3), XB(4), XB(5), XB(6)
200
      FORMAT(//,1X, 'POINTS',1X,F7.3,4X,F7.2,4X,F7.2,4X,
      * F7.2,4X,F7.2,4X,F7.2)
      WRITE (6,210) AE (1), AE (2), AE (3), AE (4), AE (5), AE (6)
      FORMAT(/,1X, 'AREA', 5X, F7.2, 4X, F7.2, 4X, F7.2, 4X, F7.2, 4X,
210
      * F7.2,3X,F8.2)
      WRITE(6,220) WU(1),WU(2),WU(3),WU(4),WU(5),WU(6)
220
      FORMAT(/,1X, 'WEIGHT',2X,F8.2,3X,F8.2,3X,F8.2,3X,F8.2,3X,
      * F8.2,3X,F8.2)
      WRITE(6,230) T(1),T(2),T(3),T(4),T(5),T(6)
230
      FORMAT(/, 1X, 'THRUST', 2X, F8.2, 3X, F8.2, 3X, F8.2, 3X, F8.2, 3X,
      * F8.2,3X,F8.2)
      WRITE(6,240) TS(1), TS(2), TS(3), TS(4), TS(5), TS(6)
      FORMAT(/,1X, 'TSTRESS',1X,F8.2,3X,F8.2,3X,F8.2,3X,F8.2,3X,
240
      * F8.2,3X,F8.2)
      WRITE(6,250) H(1), H(2), H(3), H(4), H(5), H(6)
250
      FORMAT(/,1X, 'HOOP',4X,F8.2,3X,F8.2,3X,F8.2,3X,F8.2,3X,
      * F8.2,3X,F8.2)
      WRITE (6,260) HS (1), HS (2), HS (3), HS (4), HS (5), HS (6)
260
      FORMAT(/,1X, 'HSTRESS',1X,F8.2,3X,F8.2,3X,F8.2,3X,F8.2,3X,
      * F8.2,3X,F8.2)
      WRITE(6,270) S(1), S(2), S(3), S(4), S(5), S(6)
      FORMAT(/,1X, 'RING',4X,F8.2,3X,F8.2,3X,F8.2,3X,F8.2,3X,
270
      * F8.2,3X,F8.2)
      WRITE(6,280) SC
280
      FORMAT(/,1X, 'COMPRESSION IN EDGE MEMBER AT
      * OPENING =', 1X, F10.2)
      END
```

Elliptical dome-shaped surfaces

The following analysis is carried out for the elliptical dome (Fig. 6.23). Equation of ellipse:

$$\frac{X^2}{a^2} + \frac{Y^2}{b^2} = 1$$

where $X = a \sin \phi$ and $Y = b \cos \phi$. Consider a ring produced by rotating an element ds about the Y axis of the dome.

$$ds = \sqrt{\left[(dx)^2 + (dy)^2 \right]}$$
$$= \sqrt{\left[(a^2 \cos^2 \phi + b^2 \sin^2 \phi) \right]} d\phi$$

Weight of element ring is

$$dw = 2\pi \times X \times W \times ds$$

= $2\pi \times w \times a^2 \sin \phi \sqrt{(1 - [((a^2 - b^2)/a^2) \sin^2 \phi]} \times d\phi$ (6.47)



Fig. 6.23 Elliptical dome

Let $K^2 = (a^2 - b^2)/a^2$

 W_u = Total load between points 0–1

$$W_u = \mathrm{d}w = 2\pi \times a^2 w \left[\cos \phi (\sqrt{(1 - k^2 \sin^2 \phi)} - \frac{1}{2}k(1 - k^2) \times \log k \cos \sqrt{(1 - k^2 \sin^2 \phi)}) \right]$$

Let $\cos \phi = y/b = g$ and $\sin^2 \phi = 1 - \cos^2 \phi = 1 g^2$. Substitute into Eq. (6.47):

$$W = 2\pi \times a^2 w \left[\frac{1}{2} + \frac{1}{2} k(1 - k^2) \times \log(1 + k) - \frac{1}{2} g \left(\sqrt{(1 - k^2(1 - g^2))} - \frac{1}{2} k(1 - k^2) \times \log g k + \sqrt{(1 - k^2(1 - g^2))} \right) \right]$$
(6.48)
$$= (2\pi a^2 w) C$$

where C is the quantity in the bracket.

To find the meridional thrust

$$T = \frac{W}{2\pi \sin \phi x}$$

$$= \frac{2\pi \times a^2 wC}{2\pi \times a(\sqrt{(1 - g^2 \sin \phi)})}$$

$$= wCa^2 \sqrt{\frac{1 - k^2(1 - g^2)}{b(1 - g^2)}}$$

$$= \frac{wa^2}{b} \times \frac{cQ}{1 - g^2}$$
(6.49)

where $Q = \sqrt{1 - k^2(1 - g^2)}$.

| surfaces | |
|------------|--|
| Elliptical | |
| Table 6.7 | |

| Sys | tem | Loading | Ns | N_{ϕ} $	au$ |
|---------|--|--|---|---|
| (↓ + g) | $\eta = a^{2}\cos^{2}\phi + b^{2}\sin^{2}\phi$ | $p_y = -p_E \cos \phi$ $p_z = p_E \sin \phi$ | $-p_E \frac{s}{2}(l-s) \times \frac{3a^2b^2 - \eta^2}{a^2b^{2}\eta^{1/2}} \sin\phi$ | $-p_{E}a^{2}b^{2} \frac{\sin \phi}{\eta^{3/2}} - p_{E}\left(\frac{1}{2} - s\right)\frac{2a^{2} + (a^{2} - b^{2})\sin^{2}\phi}{\eta}\cos^{2}\phi$ |
| (q) | | $p_y = -p_S \sin \phi \cos \phi$ $p_z = p_S \sin^2 \phi$ | $\begin{array}{l} -p_{S} & \frac{3s(l-s)}{2a^{2}b^{2}\eta^{1/2}} \\ \times [b^{2}(a^{2}\cos^{2}\phi-b^{2}\sin^{2}\phi) \\ + 2\eta^{2}(\sin^{2}\phi-\cos^{2}\phi)] \end{array}$ | $-\rho_{\rm S}a^2b^2\frac{\sin^2\phi}{\eta^{3/2}} \rho_{\rm S}\left(\frac{1}{2}-s\right)\frac{3\sin\phi\cos\phi}{\eta}(b^2-2\eta)$ |
| (c) | | $\phi \cos \phi$ | $\begin{array}{l} -p_W \frac{s}{2} \frac{(l-s)\cos \phi}{a^2 b^{2\eta} ^{1/2}} [\eta^2 + 3\eta \\ \times (b^2 - a^2 (l-3\sin^2 \phi) \\ -6(b^2 - a^2)^2 \sin^2 \phi) \end{array}$ | $-p_W a^2 b^2 \frac{\cos \phi}{\eta^{3/2}} p_W \left(\frac{1}{2} - s\right) 3 \frac{b^2 - a^2}{\eta} \\ \times (1 + \cos^2 \phi) \sin \phi$ |
| (p) | $\frac{1}{a} = \varepsilon$ | $p_{X} = p_{E} \cos \theta$ $p_{Z} = p_{E} \cos \theta$ | $-\frac{p_{\rm E}}{2} \frac{\sqrt{a^2 t g^2 \theta + b^2}}{a^2 \sin \theta t g \theta} \\ \times \left[a^2 - \frac{a^2 b^2 \sqrt{1 + t g^2 \theta}}{b^2 + a^2 t g^2 \theta}\right]$ | $\begin{split} p_{E} \Big[\frac{(b^2 + a^2 \operatorname{tg}^2 \theta)^{3/2}}{2\operatorname{tg}^2 \theta \sqrt{1 + \operatorname{tg}^2 \theta}} \\ \times \left(\frac{1}{\operatorname{ea}^2} \ln \frac{(1 + \varepsilon) \sqrt{b^2 + a^2 \operatorname{tg}^2 \theta}}{b(\varepsilon + \sqrt{1 + \operatorname{tg}^2 \theta})} \right) \end{split} $ |
| | | | $+ \frac{b^2}{\epsilon} \ln \frac{(1+\epsilon)\sqrt{b^2 + a^2 t q^2 \theta}}{b(\epsilon + \sqrt{1 + t q^2 \theta})} \Big]$ | $+\frac{1}{b^2} - \frac{\sqrt{1+tg^2\theta}}{b^2 + a^2tg^2\theta} \bigg) - \frac{a^2}{\sqrt{b^2 + a^2tg^2\theta}} \bigg]$ |
| (e) | esellipse | $p_{\rm x} = p_{\rm S} \sin \theta \cos \theta$ $p_{\rm z} = p_{\rm S} \cos^2 \theta$ | $-\frac{p_{\rm S}}{2}\frac{a^2\sqrt{1+tg^2\theta}}{\sqrt{b^2+a^2tg^2\theta}}$ | $-\frac{p_S}{2}\frac{a^2}{b^2}\frac{b^2-a^2\mathrm{tg}^2\theta}{\sqrt{b^2+a^2\mathrm{tg}^2}\theta\sqrt{1+\mathrm{tg}^2\theta}} 0$ |
| (£) | | $b_z = b_z$ | $-p \frac{a^2}{2} \frac{1}{\sqrt{b^2 + (a^2 - b^2) \sin^2 \theta}}$ | $-p \frac{a^2}{2b^2} \frac{b^2 - (a^2 - b^2) \sin^2\theta}{\sqrt{b^2 + (a^2 - b^2) \sin^2\theta}} 0$ |

To find the hoop force

$$H = \frac{-Tx}{R\sin\phi} + \frac{wx\cos^2\phi}{\sin\phi}$$
$$= \frac{-wx^2}{2R\sin^2\phi} + \frac{wx\cos^2\phi}{\sin\phi}$$
$$= \left(\frac{wa^2}{2b}\right) \times \frac{2g^2 - 1}{Q}$$
(6.50)

If the dome is continued along the circle of latitude through point 1, an edge memb must be provided along that circle and that member is subjected to ring tension,

$$S = \frac{Wa}{2\pi \times b} \times \frac{g}{\sqrt{(1-g_1)}} \tag{6.51}$$

Example 6 shows a typical example for elliptical dome surfaces, and Table 6.7 give certain specific cases for elliptical shell surfaces.

Torospherical shell surfaces

The torospherical shell surface is formed when a toroidal segment is inserted between a spherical and a cylindrical cap.

Main analysis

The geometry of this shell is shown in more detail in Figure 6.24.

In terms of the radii of curvature of the sphere a_1 , the toroid a_3 , and the cylinder a_2 , the meridional angle at the sphere–toroid junction is given by

$$\sin\phi_1 = \frac{a_2 - a_3}{a_1 - a_3} \tag{6.52}$$

In practice, the radius of the toroid is selected so as to provide smooth transitions at both ends.

To derive the membrane theory stress resultants, one again uses the overall equilibrium method. At a general section within the toroid, $\phi_1 < \phi < \pi/2$, the resultant axial load consists of two parts: P_1 = the load on the spherical cap, and $P_2(\phi)$ = the load between ϕ_1 and ϕ on the toroid. For a uniform positive pressure p, the magnitude of the first force is the pressure multiplied by the projected base area of the cap.

Toroidal-shaped surfaces

$$P_1 = p\pi (a_1 \sin \phi_1)^2$$
 (6.53)

For the second force, first compute the horizontal radius of the toroid

$$R_0(\phi) = (a_1 - a_3)\sin\phi_1 + a_3\sin\phi \tag{6.53a}$$

where upon the magnitude equals the pressure multiplied by the area of the projected annulus,

$$P_{2}(\phi) = p\pi [R_{0}^{2} - (a_{1}\sin\phi)^{2}]$$

= $p\pi [(a_{1} - a_{3})^{2}\sin^{2}\phi_{1} + a_{3}^{2}\sin^{2}\phi + 2(a_{1} - a_{3})a_{3}\sin\phi_{1}\sin\phi - a_{1}^{2}\sin^{2}\phi_{1}]$

which reduces to

$$P_2(\phi) = p\pi a_3(\sin\phi - \sin\phi_1)[a_3(\sin\phi - \sin\phi_1) + 2a_1\sin\phi_1]$$
(6.53b)

Summing Eqs. (6.53a) and (6.53c)

$$P(\phi) = p\pi\bar{p}(\phi) \tag{6.53c}$$

where,

$$\bar{p}(\phi) = (a_1 \sin \phi_1)^2 + a_3 (\sin \phi - \sin \phi_1) \\ \times [a_3 (\sin \phi - \sin \phi_1) + 2a_1 \sin \phi_1]$$
(6.54)

$$N_{\phi} = \frac{1}{2\pi R_0 \sin \phi} \bar{p}(\phi)$$

$$= \frac{p\bar{p}(\phi)}{2[(a_1 - a_3)\sin \phi_1 + a_3\sin \phi]\sin \phi}$$
(6.55)

To compute the circumferential stress resultant, the equation for N_{θ} is

$$N_{\theta} = R_{\theta} \left(p - \frac{N_{\phi}}{R_{\phi}} \right) \tag{6.56}$$

From Eq. (6.53b), since $R_0 = R_\theta \sin \phi$,

$$R_{\theta} = \frac{a_2 - a_3}{\sin \phi} + a_3 = (a_1 - a_3) \frac{\sin \phi_1}{\sin \phi} + a_3 \tag{6.57}$$

From Figure 6.24

$$R_{\phi} = a_3$$

Substituting Eqs. (6.55a) and (6.56) into Eq. (6.55b) gives

$$N_{\theta} = p \left[\frac{(a_1 - a_3) \sin \phi_1 + a_3 \sin \phi}{\sin \phi} \right] \\ \times \left\{ 1 - \frac{\bar{Q}(\phi)}{2a_3 \sin \phi [(a_1 - a_3) \sin \phi_1 + a_3 \sin \phi]} \right\}$$
(6.58)

Equations (6.5) and (6.7) constitute the membrane theory solution for the called toroidal knuckle portion of the torospherical head.

Toroidal knuckle:

$$Z^2 + R^2 - 95.7574Z - 126.72R + 5234.9519 = 0$$

Cylindrical segment:

$$R - 96.1 = 0 \tag{6.59}$$

Table 6.8 gives some cases of a toroidal shell surface under load.

Example 6.6 Toroidal shell shapes

Referring to Figure 6.24, and allowing for the wall thickness h = 5 mm, the geometrical properties are

$$a_1 = 4392 \text{ mm}; \quad a_2 = 2441 \text{ mm}; \quad a_3 = 823 \text{ mm}$$



Fig. 6.24 Torospherical shell geometry

| System | Loading | N _θ | N _¢ | Т |
|--------------------|---|--|---|---|
| (a) \uparrow | $ p_x = p_E \sin \theta p_z = p_E \cos \theta R = 2p_E^{\pi} \left(r\theta_0 \sin \theta_0 - 2 \sin^2 \frac{\theta_0}{2} \right) $ | $-p_E r \frac{1 - \cos \theta + \theta \sin \theta_0}{\sin \theta (\sin \theta + \sin \theta_0)}$ | $-p_{E'}\left[\cos\theta - \frac{1-\cos\theta}{\sin^{2}\theta} + \sin\theta_{0}\left(\operatorname{ctg}\theta - \frac{\theta}{\sin^{2}\theta}\right)\right]$ | 0 |
| | $p_x = p_S \sin \theta \cos \theta$ $p_z = p_S \cos^2 \theta$ $R = p_S \pi r^2 \sin^2 \theta_0$ | $-p_{S} \frac{r}{2} \frac{\sin \theta + 2 \sin \theta_{0}}{\sin \theta + \sin \theta_{0}}$ | $-p_{S}\frac{r}{2}(\cos 2\theta - 2\sin \theta \sin \theta_{0})$ | 0 |
| Ring axis does not | bisect the cross-section | Photos and the second s | For the direction of the load components $p_{\rm X}, p_{\rm Z}$ and of the unit normal forces N_{θ}, N_{ϕ} | ò |
| (c) | | $-p_E \frac{Rr(\theta - \theta_0) + r^2 (\cos \theta_0 - \cos \theta)}{(R + r \sin \theta) \sin \theta}$ | $-\frac{p_E}{\sin \theta} \left[(R + r \sin \theta) \cos \theta - R(\theta - \theta_0) - r(\cos \theta_0 - \cos \theta) \right]$ | 0 |
| | $p_x = p_E \sin \theta$ $p_z = p_E \cos \theta$ | For $\theta_0 = -\theta$ $-\rho_E \frac{Rr\theta + r^2 (1 - \cos \theta)}{(R + r \sin \theta) \sin \theta}$ | $ \begin{array}{l} (\text{symmetrical cross-section}) \\ - \frac{P_E}{\sin \theta} \ [(R + r \sin \theta) \cos \theta \\ - R\theta - r(1 - \cos \theta)] \end{array} \end{array} $ | 0 |
| | $p_z = \gamma(h - r\cos\theta)$ | $-\frac{\gamma r}{(R+r\sin\theta)\sin\theta} \left[-Rh(\sin\theta_0) - \sin\theta_0 + \frac{h}{2}(\cos^2\theta_0 - \cos^2\theta) + \frac{Rr}{2}(\sin\theta_0\cos\theta_0 - \sin\theta\cos\theta) + \frac{Rr}{3}(\cos^3\theta_0 - \cos^3\theta) - \theta + \theta_0) - \frac{r^2}{3}(\cos^3\theta_0 - \cos^3\theta)\right]$ | $\begin{aligned} &-\frac{\gamma}{\sin^2\theta} \left[(h - r\cos\theta)(R + r\sin\theta) \right. \\ &\times \sin\theta + Rh(\sin\theta_0 - \sin\theta) \\ &-\frac{rh}{2} \left(\cos^2\theta_0 - \cos^2\theta \right) - \frac{Rr}{2} \\ &\times \left(\sin\theta_0\cos\theta_0 - \sin\theta\cos\theta \right) \\ &-\theta + \theta_0 \right) + \frac{r^2}{3} \left(\cos^3\theta_0 - \cos^3\theta \right) \right] \end{aligned}$ | 0 |
| | | For $\theta_0 = -\theta$ $-\frac{\gamma r}{(R + r \sin \theta) \sin \theta} \left[Rh \sin \theta + \frac{rh}{2} \sin^2 \theta - \frac{Rr}{2} (\sin \theta \cos \theta + \theta) - \frac{r^2}{3} (1 - \cos^3 \theta)\right]$ | $P_{1} (symmetrical cross-section)$ $-\frac{\gamma}{\sin^{2}\theta} \left[\frac{r\hbar}{2} \sin^{2}\theta - \frac{Rr}{2} (\sin \theta \cos \theta - \theta) - r^{2} (\cos \theta \sin^{2}\theta - \frac{1 - \cos^{3}\theta}{3}) \right]$ | 0 |
| (e) | <i>P_z</i> = <i>P</i> | $-\frac{p}{2(R+r\sin\theta)\sin\theta} [(R+r\sin\theta)^2 - (R+r\sin\theta)^2] - (R+r\sin\theta)^2]$ $-\frac{pr}{2}\frac{2R+r\sin\theta}{R+r\sin\theta}$ For $\theta_0 = -\theta_1$ | $-\frac{p}{2\sin^2\theta}[2R\sin\theta_0 + r(\sin^2\theta_0 + \sin^2\theta)]$ (symmetrical cross-section) $-\frac{p_r}{2}$ | 0 |
| (f) | Edge load p _L | $-\rho_L \frac{R+r\sin\theta_0}{(R+r\sin\theta)\sin\theta}$ | $\frac{p_L}{r} \frac{R+r\sin\theta_0}{\sin^2\theta}$ | 0 |

Table 6.8 Toroid shell

as shown in Figure 6.25, so that from Eq. (6.58)

$$\sin\phi_1 = \frac{2441 - 823}{4392 - 823} = 0.45205 \tag{6.60}$$

and

 $\phi_1 = 26.88^{\circ}.$

The equation of the meridian was established with the origin set at the pole, and the resulting equations are as follows:

Spherical cap:

$$Z^2 + R^2 - 345.8Z = 0 \tag{6.61}$$

$$\bar{p}(\phi) = \text{Eq.} (6.54b)$$
 (6.62)

$$P(\phi) = p\pi\bar{p}(\phi) \tag{6.63}$$

The values of N_{ϕ} and N_{θ} can now be computed, as in other domical shapes.

Reference is made to Table 6.8 and Eqs. (6.55a) and (6.57) for evaluation of these values.

Example 6 Elliptical dome

The reinforced concrete dome shown in Figure 6.25 is an ellipsoid of revolution about the minor axis. The dome carries a vertical live load of 2.5 kN/m^2 on plan. Calculate the meridional and hoop forces and stresses for zones C1, 2 and 3 and



Fig. 6.25 Test specimen middle surface geometry



Fig. 6.26 Elliptical dome surface

draw the hoop stress diagram for one-half of the dome. Calculate the areas of reinforcement at points C1, 2, 3 and B. Use the following data: Density of concrete= 2400 kg/m^3

$$\begin{split} N_{\phi} &= \text{meridional thrust from the live load} = \frac{2.5a^2}{2b}Q = 1.25\frac{a^2}{b}Q \\ N_{\theta} &= \text{hoop force} = 1.25\frac{a^2}{b}\left(\frac{2(y/b)^2 - 1}{Q}\right) \\ \text{Total meridional thrust} &= N_{\phi} + N_{\phi,1} = \bar{T} \\ \text{Total hoop thrust} &= N_{\theta} + N_{\theta,1} = \bar{H} \end{split}$$

Allowing no tension in the concrete (compressive stress in the reinforcement steel = 125 N/mm^2)

$$A_{\rm S} = \frac{H}{125} = \frac{700}{125} \times 10^3 = 5600 \,{\rm mm^2/m}$$

0.2% concrete sectional area for temperature and shrinkage

$$= 5610 + 200 \times 1000 \times \frac{0.2}{100}$$
$$= 6000 \text{ mm}^2/\text{m in the latitude direction}$$

and

$$400 \,\mathrm{mm^2/m}$$
 in the meridional directions

List of reinforcement for various zones:

| g | 0 | 0.2 | 0.6 | 0.8 | 1.0 | |
|--------------|------|------|------|-----|-----|---------------------------------|
| N_{ϕ} | 400 | 400 | 400 | 400 | 400 | meridional (mm ² /m) |
| N_{θ} | 6000 | 4600 | 1088 | 400 | 400 | latitude |

Self weight $W_D = 2400 \times 9.81 \times 10^{-3} \times 0.2 = 4.71 \text{ kN/m}^2$ Stresses at the end of minor axis: $N_{\phi} = N_{\theta} = Wa^2/2b$ for both live and dead loads is:

> $4.71 \times (25.5)^{2} + \frac{2.5 \times (25.5)^{2}}{20} = 235 \text{ kN/m}$ Stresses = $\frac{235}{0.2} = 1175 \text{ kN/m}^{2}$ = 1.175 N/mm²

Computer program: analysis of thin shells

```
* TITLE: COMPUTER AID ANALYSIS OF THIN SHELLS
С
    * TUTOR: Dr. Y. BANGASH
С
    С
С
С
    С
С
    * THIS IS A PROGRAM TO FIND OUT THE MERIDIAN FORCES,
С
    * THE HOOP FORCES AND RING TENSION ACTING ON
С
    * EACH SECTION OF THE ELLIPTICAL DOME DUE TO ITS
                                                *
С
    * DEAD LOAD AND IMPOSED LOAD.
    ******
С
С
С
С
   С
                     * NOTATION *
С
                                                _
    = QK UNIFORMLY DISTRIBUTED LIVE LOAD
С
                                                =
С
    = GK UNIFORMLY DISTRIBUTED DEAD LOAD
                                                _
С
    = TX THICKNESS OF THE DOME
                                                =
С
    = B HALF HEIGHT OF THE DOME
                                                =
С
    = AX HALF LENGTH OF THE DOME
                                                =
С
    = R RADIUS OF CURVATURE
                                                _
С
    = H HOOP FORCE DUE TO LIVE LOAD
С
    = H1 HOOP FORCE DUE TO DEAD LOAD
С
    = HBAR TOTAL HOOP FORCE
                                                =
С
   = DELTH STRESS DUE TO HOOP FORCE
                                                =
С
   = T1 MERIDIONAL THRUST DUE TO DEAD LOAD
                                                =
С
    = T2 MERIDIONAL THRUST DUE TO LIVE LOAD F
                                                =
```

Elliptical dome-shaped surfaces

= TBAR TOTAL MERIDIONAL STRESS С _ С = DELTT STRESS DUE TO MERIDIONAL THRUST = С _____ С REAL G(1:6), C(1:6), O(1:6), A(1:6), WU(1:6), TBAR(1:6) REAL DELTT(1:6), HBAR(1:6), DELTH(1:6), Y(1:6), H(1:6), T(1:6 REAL E(1:6), F(1:6), O, Z, Q1, PI, K, H1(1:6), T1(1:6) REAL QK, GK, TX, B, AX, R 3000 WRITE(6, 10) 10 FORMAT(1X, 'INPUT THE UNIFORMLY DISTRIBUTED LIVE LOAD') READ(5, *) OKWRITE(6, 14) FORMAT(/, 1X, 'INPUT THE DEAD LOAD')READ(5, *) GK 14 WRITE(6, 18) 18 FORMAT(/, 1X, 'INPUT THE THICKNESS OF THE DOME') READ(5, *) TX WRITE(6, 22) FORMAT(/, 1X, 'INPUT THE HALF HEIGHT OF THE DOME') 22 READ(5, *) BWRITE(6, 26) 2.6 FORMAT(/, 1X, 'INPUT THE HALF LENGTH OF THE DOME') READ(5, *) AXWRITE(6, 29) 29 FORMAT(/, 1X, 'INPUT THE RADIUS OF THE CURVATURE') READ(5, *) R WRITE(6, 31) FORMAT(/, 1X, 'INPUT THE VALUE OF Y') 31 READ(5, *) Y(1), Y(2), Y(3), Y(4), Y(5), Y(6) DO 33 I=1,6 G(I) = Y(I) / B33 CONTINUE 01=2400 PI=3.142 K=SORT ((AX**2-B**2)/(AX**2)) DO 40 I=1,6 Q(I)=SQRT(1-(K**2)**(1-G(I)**2)) 40 CONTINUE DO 41 I=1,6 E(I) = (-0.5*G(I)*Q(I))41 CONTINUE DO 42 I=1,6 $F(I) = ((1-K^**2) / (2^*K)) * LOG(K^*G(I) + Q(I))$ CONTINUE 42 0 = 1 $Z = (-0.5) - (1 - K^* 2) / (2^* K) * LOG(K+0)$ DO 43 I=1,6 C(I) = E(I) - F(I) - Z43 CONTINUE W=QK + GK DO 44 I=1,6 A(I) = (2*PI*AX**2)*C(I)44 CONTINUE

```
DO 45 I=1,6
      WU(I) = W^* A(I)
      CONTINUE
45
С
С
     TO FIND THE HOOP FORCE
С
      H = HOOP FORCE DUE TO THE LIVE LOAD, QK
      DO 46 I=1,6
      H(I) = (QK^*AX^{**}2/B)^*(G(I) - C(I)/(1 - G(I)^{**}2)/Q(I))
      CONTINUE
46
      H1 = HOOP FORCE DUE TO DEAD LOAD, GK
С
      DO 47 I=1,6
      H1(I) = (GK*AX**2) / (2*B)*(2*G(I)**2-1) / O(I)
47
     CONTINUE
      HBAR = TOTAL HOOP FORCE
С
      DO 48 I=1,6
      HBAR(I) = H(I) + H1(I)
48
      CONTINUE
С
      TO FIND THE STRESS DUE TO HOOP FORCE, DELTH
      DO 49 I=1,6
      DELTH(I) = HBAR(I) / (TX*1000)
49
      CONTINUE
С
С
С
      TO FIND THE MERIDIONAL THRUST
С
      T=MERIDIONAL THRUST DUE TO DEAD LOAD, GK
      DO 50 I=1, GT(I) = (GK*C(I)*Q(I)*AX**2) / ((1-G(I)**2)*B)
50
     CONTINUE
      T1=MERIDIONAL THRUST DUE TO LIVE LOAD, QK
С
      DO 51 I=1,6
      T1(I) = (QK*Q(I)*AX**2) / (B*2)
51
      CONTINUE
С
      TBAR = TOTAL MERIDIONAL THRUST
      DO 52 I=1,6
      TBAR(I) = T(I) + T1(I)
52
      CONTINUE
      TO FIND STRESSES DUE TO MERIDIONAL THRUST, DELTT
С
      DO 53 I=1,6
      DELTT(I) = TBAR(I) / (TX*1000)
      CONTINUE
53
С
С
      PRINT 55
      PRINT 56
     FORMAT(///,2X, '*SHELL DIMENSION (m)*')
55
56
      FORMAT(/,2X, 'THICKNESS',8X, 'HALF HEIGHT', 6X,
      * 'HALF LENGTH', 6X, 'RADIUS')WRITE(6,57) TX, B, AX, R
57
      FORMAT(/, 3X, F7.2, 9X, F7.2, 9X, F7.2, 9X, F7.2)
      PRINT 58
58
     FORMAT(//, 31X, 'OUTPUT RESULTS')
      PRINT 59
     FORMAT(31X, `************')
59
     WRITE(6,60) G(1),G(2),G(3),G(4),G(5),G(6)
60
     FORMAT(//,1X, 'G=Y/B',6X,F4.3,7X,F4.3,7X,F4.3,7X,F4.3,
```

| Execut | tion begins |
|--------|---|
| 140 | FORMAT (/,1X, 'DELTH',3X,F7.2,4X,F7.2,4X,F7.2,4X,F7.2, *4X,F7.2,4X,F7.2)END |
| | <pre>wRITE(6,140) DELTH(1), DELTH(2), DELTH(3), DELTH(4), * DELTH(5), DELTH(6)</pre> |
| 130 | FORMAT (/, 1X, `HBAR', 4X, F7.2, 4X, F7.2, 4X, F7.2, 4X, F7.2, 4X, F7.2, 4X, F7.2, |
| | <pre>^ 44, F /. 2, 44, F /. 2) WRITE(6,130) HBAR(1), HBAR(2), HBAR(3), HBAR(4), HBAR(5), * HBAR(6)</pre> |
| 120 | * DELTT (5), DELTT (6) FORMAT (/,1X, `DELTT', 3X, F7.2, 4X, F7.2, 4X, F7.2, 4X, F7.2, * 4X, F7.2, 4X, F7.2) |
| | *4X,F7.2,4X,F7.2) WRITE(6,120) DELTT(1),DELTT(2),DELTT(3),DELTT(4), |
| 110 | WRITE (6,110) TBAR (1), TBAR (2), TBAR (3), TBAR (4), TBAR (5), * TBAR (6) FORMAT (/,1X, 'TBAR',4X,F7.2,4X,F7.2,4X,F7.2,4X,F7.2, |
| 100 | WRITE(6,100) WU(1),WU(2),WU(3),WU(4),WU(5),WU(6) FORMAT(/,1X, 'WEIGHT',1X,F8.2,3X,F8.2,3X,F8.2,3X, *F8.2.3X,F8.2.4X,F7.2) |
| 96 | WRITE (6,96) A (1), A (2), A (3), A (4), A (5), A (6) FORMAT (/, 1X, 'AREA', 4X, F7.2, 4X, F7.2, 4X, F7.2, 4X, F7.2, *4X, F7.2, 4X, F7.2) |
| 84 | <pre>*F1.2,4X,F1.2) WRITE(6,84) Q(1),Q(2),Q(3),Q(4),Q(5),Q(6) FORMAT(/,1X, 'Q',7X,F7.2,4X,F7.2,4X,F7.2,4X,F7.2,4X,F7.2,4X,</pre> |
| 72 | *7X,F4.3,7X,F4.3) WRITE(6,72) C(1),C(2),C(3),C(4),C(5),C(6) FORMAT(/,1X,`C',7X,F7.2,4X,F7.2,4X,F7.2,4X,F7.2,4X, |

INPUT THE UNIFORMLY DISTRIBUTED LIVE LOAD ? 2.25 INPUT THE DEAD LOAD ? 1.5 INPUT COLLAR LOAD ? 10 INPUT THE THICKNESS OF THE DOME ? 0.2 INPUT THE RADIUS OF THE CURVATURE ? 50

```
INPUT DISTANCE FROM THE AXIS OF ROTATION
                                           MORE... IBMA
?
10
INPUT THE LENGTH ALONG THE X-AXIS
?
0, 10, 20, 30, 40, 50
OUTPUT RESULTS
*****
POINTS 10.00 20.00 30.00 40.00 50.00 60.00
       0.00 262.68 1059.98 2448.77 4704.97 11089.70
AREA
WEIGHT
        0.00 1614.16 5233.17 11070.29 20160.35
44733.53
                                               177.97
                               98.26
THRUST 0.00 76.38 87.45
                                       113.81
TSTRESS 0.00 381.88 437.26 491.29
                                       569.04
                                                889.83
MORE... IBMA
       -3.64
              45.77
                      44.07
                               24.62
HOOP
                                       -13.30
                                               -142.37
HSTRESS -18.21 228.87 220.36
                              123.08
                                       -66.48 -711.86
       0.00 629.20 1272.09 1761.66 1924.92
RING
                                                 0.00
COMPRESSION IN EDGE MEMBER AT OPENING = 500.00
Execution begins....
INPUT THE SPAN UNIFORMLY DISTRIBUTED LIVE LOAD
?
291.0
INPUT THE DEAD LOAD
?
0
INPUT THE THICKNESS OF THE DOME
?
1.2
INPUT SIN
0
?
0
INPUT SIN
1
?
1INPUT THE RADIUS OF CURVATURE
?
55.5
```

Elliptical dome-shaped surfaces

```
INPUT COSO
?
1
INPUT COS1
?
0
MERIDIONAL THRUST = 5631950.00 KN/M
HOOP FORCE = 8075.00 KN/M
```

Execution begins....

```
INPUT THE SPAN UNIFORMLY DISTRIBUTED LIVE LOAD
?
344.75
INPUT THE DEAD LOAD
?
0
INPUT THE THICKNESS OF THE DOME
?
1.37
INPUT SINO
2
0
INPUT SIN1
?
1
INPUT THE RADIUS OF CURVATURE
?
22.71
INPUT COSO
?
1
INPUT COS1
?
0
MERIDIONAL THRUST = 7829.3 KN/M
HOOP FORCE = 3924.63 KN/M
ASR = 15048.8 MM**2/M
BAR = 25
```

Chapter 7 Concrete Containment Subject to Aircraft Crashes and Seismic Effects and Over Pressurisation

7.1 Introduction

A comprehensive analysis of the containment using numerical techniques has been given in this text. More examples are given in the authors' following book: *'Shock, Impact and Explosion'*, Springer, Heidelberg (2009). First, the Belle Fonte vessel given in chapter 6 is taken with respective design parameter.

Secondly, this time Size well B containment vessel (Fig. 7.1) is taken as an example. Figures 7.2, 7.3, 7.4 and 7.5 show typical reinforcement system. Figure 7.6 shows a secondary dome provided to protect the primary containment from the external hazards and public from the internal hazards.

The same containment is taken as an example to assess its behaviours in the seismic environments and an overpressurisation. Results obtained are clearly established in the form of acceleration. Time historys, displacement and stress-states and acceleration spectra.

7.2 Aircraft Impact/Crashes on Containment

The design and analysis of containment vessel to withstand the effect of an aircraft crash or impact involves many complex parameters, including loadings and durations. Bangash has produced modified force-time impact functions for various aircrafts, and these are shown in Fig 7.6. First, the Belle Fonte vessel parameters discussed earlier were chosen for the analysis. The impact point is chosen to be the apex of the vessel and at the junction of the dome and the cylinder. Results are produced in the form of the acceleration-time histories, displacement and stress states for selected times and acceleration response spectra. Newmark Wilson θ direct integration methods are used for the analysis. Crack propagation and linear and non-linear displacements for four aircrafts are shown in Figs. 7.7 and 7.8a. The impact zones are shown in Fig. 7.9. Table 7.1 shows comparative results for penetrations and perforations based on both empirical and finite element analysis for a number of aircraft impact loads. The endochronic model is used throughout the analysis. A similar analysis was carried out for the Size well B vessel using load-time functions for the F-16



Fig. 7.1 Sizewell B power station reactor building – sectional elevation on north/south centre line (with compliments of CEGB, UK)

aircraft. 'Post-mortem' of the vessel is shown in Fig. 7.10. The load-displacement as a function of time is given in Fig. 7.8. For this analysis the vessel foundations are assumed to be consisting of strings at different directions with parameters given in general by Table 7.2. The springs represent the soil behaviour when aircraft crashes occur as part of the integrated system. In reality a proper soil structure interaction analysis would have given accurate assessment of vessel behaviour. This analysis is avoided due to costs. The application of the soil-structure interaction analysis is more appropriate and is cost-effective in case seismic analysis of such vessels is carried out.

7.2.1 Aircraft Impact Using Finite Element and Ultimate Limit State Analysis

A reference is made to the finite element and ultimate state analysis given in this text and the author books stated in section 7.2. These analyses are not repeated



Fig. 7.2 Post-tensioning loads -- circumferential tendons

and are avoided due to space limitation. A non-linear finite element model is given in Fig. 7.11 for the Sizewell B containment vessel parameters given in Fig. 7.3. Both finite element and ultimate limit state analysis stated earlier are compared and plotted in Figs. 7.12 and 7.13 while assuming different boundary conditions. For convenience the results are plotted on the containment outside face. The containment is also analysed when it is integrated with other ancillary buildings. The impact zone is assumed on the visible part of the containment outside the ancillary building shown in Fig. 7.10. Throughout the analytical work the impacting aircraft was assumed as F-16 multirole combat aircraft for which the parameters are given. The post-mortem of the containment vessel is given in Fig. 7.14 for the final disaster scenario. Throughout this analysis the following data were maintained and used:

- No. of vessel solid elements 1005 isoparametic type, 20 noded.
- Vessel material properties are stated earlier with bonded steel and tendon indicated in Figs. 7.3, and 7.4 placed either on solid nodes or in the body of the element. Total 5000 elements are taken as measured and compared.
- The aircraft elements/variable with the total element numbering 500,000 solid elements.



Fig. 7.3 Sizewell B dimensional layout

- The gap or contact elements were provided for the interaction and integrated analysis adopted at suitable places to be 9500 elements.
- Program ISOPAR conveniently checked by ANSYS took the total time 3¹/₄h to produce the disaster scenario. Stresses, displacements and strains were obtained. Cracks were produced together with plasticity indices and zones.
- A four-parameter crack theory was considered for the concrete failure.
- Mostly tendons ruptured or deformed with visible plastic zone.
- Similar time dependent displacements have been produced.



Fig. 7.4 Developed elevation (section-right) showing tendon layout $0^{\circ}-180^{\circ}$ (all dimensions in mm except reduced level) (courtesy of CEGB and Sizewell Task force)



Fig. 7.5 Arrangement of longitudinal and circumferential tendons (all dimensions in mm) (EGB and Sizewell B Task force, 2001) with compliments)



Fig. 7.6 Force–Time function

• A comparative study of the finite element analysis and the limit state approach of this containment has been carried out. Figures 7.7 and 7.8 and the results are in good agreement.

Note: For more detailed analysis the reader is referred to the author's available books on

- 1. Explosion Resistant Buildings
- 2. Shock, Impact & Explosions Springer Verlag 2001, 2005 respectively Hiedelberg, Germany





(c) Displacement-time relationship using a Tornado aircraft

Fig. 7.7 A comparative study of displacement-time relations and post-mortem of containment vessel



Fig. 7.8 Linear and non-linear displacement as a function of time

7.3 Seismic Analysis for PWR/BWR

A non-linear dynamic analysis was carried out for the containment vessel. A direct approach was adopted in which the whole system (containment/soil/ bedrock) was modelled and analysed in the time domain using finite elements. Inertia forces were reproduced by distributed masses by involving consistent matrices. In general the equation of motion contain a mass matrix (M), damping matrix (C) and a stiffness matrix (K). The excitation is taken in the form of a base motion. As shown in Figs. 7.15 and 7.16, 20-noded isoparametric elements together with line and panel elements representing concrete, prestressing tendons and reinforcement and steel liner are used to model the structure and the supporting medium. This method allows treatment of non-linear behaviour and material properties which are adjusted at each step. Special care is exercised in using the numerical integration procedure together with time steps in order to achieve stability in the solution. In the stiffness matrix of the evaluation of the vessel, the four-parmeter model is considered. The cracking cases are evaluated using the endochronic cracking model. Table 7.3 shows the foundation parameter for impact and seismic problems. Figure 7.16a and b indicates damage scenarios of the PWR containment of BelleFonte NPS with and without seismic devices.



Fig. 7.8 (a) Impact on the dome for various aircraft

The Program ISOPAR has been written to perform seismic analysis incorporating the effects of circumferential cracking. The program uses numerical integration rather than the method of normal modes. The cracks were obtained when the overall stiffness of the vessel was no longer constant but was a function of the shearing stresses in the vessel.

The equation of motion was solved using the Wilson and Newmark θ methods. The convergence criterion for ending the iterations was 0.0001.

The size of the time step (t) is critical for obtaining accuracy and rapid iteration convergence (optimum t = 0.0025s).

Stiffness changes will occur while giving some time steps. A typical subroutine that keeps track of where each crack is on the hysteresis loop is shown in Figs. 7.17 and 7.18 and makes in the crack stiffness when necessary. A time step is repeated only when stiffness changes from line to line. This is because the high velocities which occur during the unloading from certain lines can cause the


Fig. 7.9 Post-mortem of the containment vessel

crack tip to go far below these specified slips at certain points, which causes the loop to grow much wider than originally specified. Shear crack relation for a typical containment is given in Fig. 7.18. These techniques are given in this text with exclusive details.

At time t, one of the cracks is at the positions marked on a line by the hysteresis loop. At time $(t + \Delta t)$, a certain point can be missed by a significant

| | Depth of penetration (m) Thickness for no perforation (m) | | | | | | Finite element Thickness ^a /displacement (mm) | |
|------------------------|--|-------------|--------|------------|--------|------------|---|------------------------|
| | | | | | | | | |
| Aircraft [speed (mph)] | IRS | HN- NDRC | ACE | DF- BRL | BRL | DF- ACE | Depth of penetration (m) | Thickness ^b |
| MRCA | 2.0 | 3.1 | 2.5 | 1.57 | 1.59 | 2.5 | 1.80 | 3.0 |
| | [2.59] | [3.75] | [2.85] | [2.30] | [2.75] | [2.95] | (55 max) | _ |
| Phantom RF- 4E | 1.85 | 2.90 | 2.25 | 1.25 | 1.35 | 2.10 | 1.55 | 2.35 |
| [482] | [2.50] | [3.70] | [3.00] | [2.00] | [1.75] | [2.75] | (55 max) | _ |
| Phantom (C) | 1.75 | 2.80 | 2.15 | 1.10 | 1.35 | 2.0 | 1.55 | 2.35 |
| [F482] | [2.50] | [3.50] | [2.85] | [1.75] | [1.75] | [2.75] | (60 max) | _ |
| Boeing 707-320 (E) | 1.80 | 2.75 | 2.00 | 1.20 | 1.50 | 2.0 | 1.10 | 2.00 |
| [730] | [2.50] | [3.25] | [2.75] | [1.75] | [2.0] | [2.75] | (55 max) | _ |
| Boeing 747 | 2.0 | 3.0 | 2.30 | 1.55 | 1.85 | 2.30 | 1.90 | 2.75 |
| [250] | [2.50] | [3.75] | [2.85] | [2.30] | [2.50] | [2.85] | (65 max) | - |
| FB-11 (CH) | 2.0 | 2.50 | 2.00 | 1.05 | 1.35 | 1.75 | 1.25 | 2.30 |
| [200] | [2.50] | [3.75] | [2.75] | [2.00] | [2.00] | [2.25] | (45 max) | _ |
| Mirage | 1.75 | 2.85 | 2.20 | 1.25 | 1.50 | 2.50 | 1.45 | 2.35 |
| [470] | [2.75] | [3.75] | [3.00] | [2.00] | [2.20] | [3.00] | (40 max) | _ |
| Mig-23 | 1.2 | 1.8 | 2.2 | 1.0 | 1.0 | 2.1 | 1.80 | 2.85 |
| [480] | [1.6] | [5.0] | [6.0] | [3.0] | [1.15] | [3.10] | (45 max) | _ |

Table 7.1 Aircraft impact load versus comparative vessel thickness

^aAll thicknesses mentioned under finite element are computed thicknesses ^bFor wide perforation

| Fable 7.2 | Foundation | parameters | (major | data) | ļ |
|-----------|------------|------------|--------|-------|---|
|-----------|------------|------------|--------|-------|---|

Foundation radius R = 24.86 mFoundation thickness $t_f = 3.76 \text{ m}$ Seismic shear force = 1822.52 kN/mUplift from vertical earthquake component = 470 kN/mTangent shear from earthquake = 1272.96 kN/m $K_u = \text{translational spring constant} = \frac{32(1-v)GR_o}{(7-8v)}$ $K_z = \text{vertical constant} = \frac{4GR}{3(1-v)}$ $K_t = \text{torsional spring constant} = \frac{8GR_0^3}{3(1-v)}$ $K_t = \text{torsional spring constant} = \frac{16GR^3}{3}$ v = 0.14 $\beta' = 0.5$ Material damping 8% for the soil and 2% for the vessel



Fig. 7.10 Finite element mesh scheme for PWR reactor vessel integrated with other buildings

amount. The program at this point goes back to time t and refines the time step and computes the shear stress and crack displacement with the new refined time step. If the shear stress is not within a specified limit then the time step is refined further and the process is repeated until the specified limits are met. The same process is performed for the stiffness change from time to time.

The changing of hysteresis loops due to cycling is shown in Figs. 7.16 and 7.17. All cracks start on the cycle1 line. Once a shear stress is exceeded, unloading starts and proceeds along a line parallel to the dotted line A–B. The second cycle is reached when A–B intercepts a line. This process continues.

The circumferential (horizontal) and longitudinal (vertical) cracks in the vessel have a significant effect on the dynamic response of the vessel due to



Fig. 7.11 Stress distribution on dome



Fig. 7.12 Stress on the barrel wall



Fig. 7.13 Final disaster scenario

the SSE. The important design parameters which are affected are the liner distortion and the maximum shear stress in the concrete vessel.

Current design criteria specify that the nuclear containment vessel must be able to withstand the simultaneous occurrence of a LOCA with strong (SSE) earthquake motions. The internal pressure creates tensile stresses in both the longitudinal and circumferential directions, while the earthquake causes inertia forces which in turn cause shearing stresses and bearing stresses in the vessels. These stresses cause forces which must be transferred across horizontal and vertical cracks. The crack patterns, crack width and spacing are computed. Crack widths vary between 0.25 and 0.38 mm.

To predict failure mechanisms and to establish the seismic safety margin of a structure, the most severe earthquake which possibly could occur at the site is applied. For this extreme loading case pounding will often occur. Extensive non-linear analyses have to be performed. Pounding introduces impact loads which have to be superimposed on those caused by the ground acceleration itself. While, in general, the structure can withstand the latter, if sufficient ductility is provided, the former loads often introduce stress and displacement distributions not envisaged in the original design. When these impact loads from pounding are too high, the structural system has to be modified to reduce the response [6]. This can be achieved, e.g. by 'tuning' the two involved structures by introducing a spring-dashpot system between them or using Hallquist contact elements.

The shearing stiffness of the cracks due to aggregate interlock affects the shear stress distribution in the containment vessel after immediate short-term internal pressurisation.



Fig. 7.14 Non-linear model

During an earthquake, the stresses caused by inertia forces do cause the crack width to change. Where the crack was too narrow over the whole of some portion of its circumference, it results in alteration in the shear stress distributions. Computer results show that for a total unbonded length at the crack of 64 mm the change in crack width is small compared to the initial crack width. Therefore the shear stress distribution is not significantly altered from the



Fig. 7.15 Finite elements for the Bellefonte vessel: (a) with seismic devices and (b) without seismic devices

| Conventional steel | |
|--|--|
| σ_y = yield strength | 451.6 MN/m ² |
| $E_p = 0.1E$ | |
| Liner 6–12 mm thickness | |
| Coefficient of linear expansion | $10 \ \mu M/m^{\circ}C$ |
| Thermal conductivity | 41.6 W/m°C |
| ε_{cu} -ultimate strain for concrete 0.0035 | $200 \times 10^3 \text{ MN/m}^2$ |
| E (steel) | |
| E (concrete)–short term | $38 \times 10^3 \text{ MN/m}^2$; $34 \times 10^3 \text{ MN/m}^2$ |
| Long term | $20.7 \times 10^3 \text{ MN/m}^2$ |
| (soft zones) | 0.74E |
| $E_{\rm p}$ -plastic modulus | 0.476 <i>E</i> |
| Poisson's ratio | 0.15 (concrete) |
| | 0.3 (steel) |
| Coefficient of thermal expansion of concrete | $10 \times 10^{-6} / ^{\circ}C$; $12 \times 10^{-6} / ^{\circ}C(*)$ |
| Short-term specific creep | $1830 \times 10^{-9} \text{ MN/m}^{2^{\circ}}C$ |
| Long-term specific creep | $2407 \times 10^{-9} \text{ MN/m}^{2^{\circ}}C$ |
| Minimum crushing strength at 28 days | 41.7 MN/m^2 |
| Rigid target | |
| Steel and alloys | |
| $m_a = 127.5 { m Mg}$ | |
| $m_a = 38.6 \text{Mg}$ included in m_a | |
| $\varepsilon_y = 2 \times 10^{-3}; \varepsilon_r = 5 \times 10^{-2}$ | |
| Deformable target | |
| Impact area = 37.2 m^2 ; 38 m^2 and 25 m^2 | |
| Sizewell B parameter | |
| R_1 | 22.5 m |
| d (wall) | 2.5 m |
| <i>R</i> (outer dome) | 22.860 m |
| d (dome) | 1500 mm spherical shape |
| $D + F + 1.5P + T_a$ | |
| $D + F + 1.25P_a + T_a + 1.25E$ | |
| $D + F + P_a + T_a + E$ | |
| D-dead load; F-prestressing loads; | $P_{\rm a}$ -local pressure; |
| $T_{\rm a}$ -local temperature load; <i>E</i> -seismic (OBE) load; | E'-siesmic (SSE) |
| $P_a = 50 \text{ psig } (345 \text{ kN/m}^2);$ | design accident temperature 271°F |
| $E = 0.05 g; E = 0.11 g \text{ and } 0.17; \rightarrow$ | Time 100 |
| <i>E''</i> (SSE) uplift 6.9 MN/m; | $f_{cu} = 41.3 \text{ MN}/\text{m}^2$ |
| E(OBE) = uplift 4.7 MN/m | |
| $\mu = 0.14; K = 0.0003$ for friction; | tendon losses 21 % |

 Table 7.3 Parameters, design loads and stresses

Note: For detailed 3D hybrid analysis with and without seismic devices using finite element, the reader is referred to the author main text on "Earthquake Resistant Buildings" published by Springer Verlag, Heidelberg in 2010.



Fig. 7.16 Shear stress versus slip

sinusoidal distribution. The vertical cracks present may effectively decrease the flexural and shear stiffnesses of the containment vessel.

Figure 7.20 shows a mass displacement–time relation for the containment. Figure 7.21 shows response spectra under various conditions and at the top and bottom of the vessel. The control motion is specified at the free surface of the soil deposit.

The curves show the motion specified at bedrock and at the foundation level, respectively. Figure 7.16 shows a 'post-mortem' of the Bellefonte containment at X, Y = 200 gals and Z = 50 gals. Throughout the vessel excitation the damping for the vessel was 2% and that of the soil was 8%.

7.3.1 Mutual Pounding of Containment Building with Auxiliary Building–The Pushover Analysis

7.3.1.1 Introduction

The seismic response of a structure which, in addition to earthquake loading, is subjected to the impact force resulting from pounding by an adjacent containment



Fig. 7.17 Shear stress versus horizontal slip

Building located is determined. At first, simple models are used to examine the characteristics of the pounding phenomenon. The pounding structure is modelled as a non-linear DOF system and the neighbouring containment building is represented by an impact-spring-dashpot mechanism. Parametric studies, varying the structural parameters, are performed both for steady-state and transient excitations. Finally, the pounding of a typical reactor building by an adjacent auxiliary building during an earthquake is analysed using a simple DOF system and a very detailed dynamic model. The stresses and in-structure response spectra are compared to those for the case in which no pounding occurs.

The gap size between adjacent structures or between adjoining structural units can turn out to be too small in an actual earthquake in which plastic displacements of the soil and of the structure develop, as it is customary to design the structure, and thus also the gap size, for a moderate earthquake, assuming elastic behaviour. The problem of insufficient gap size can also arise when retrofitting nuclear power plants for increased seismic requirements can occur.



Fig. 7.18 Shear - crack relation



Fig. 7.19 Mass displacement - time relation for typical containment structure



Fig. 7.20 Containment vessel response spectrum (---, measured; --, non-linear; -•-, linear)

$$|K|_{\text{Element}} = \frac{1}{\det} \begin{bmatrix} \left(\frac{L}{EI} + C\right) & -\left(\frac{L^2}{2EI} + B\right) & -\left(\frac{L}{EI} + C\right) & \left(B - \frac{L^2}{2EI} - CL\right) \\ -\left(\frac{L^2}{2EI} + B\right) & \left(\frac{L^3}{3EI} + \frac{L}{GA_S} + \frac{N}{K_C} + A\right) & \left(\frac{L^2}{2EI} + B\right) & \left(\frac{L^3}{6EI} + BL - \frac{L}{GA_S} - \frac{N}{K_C} - A\right) \\ -\left(\frac{L}{LI} + C\right) & \left(\frac{L^2}{2EI} + B\right) & \left(\frac{L}{EI} + B\right) & \left(\frac{L^2}{2EI} + B\right) \\ \left(B - \frac{L^2}{2EI} - CL\right) & \left(\frac{L^3}{6EI} + BL - \frac{L}{GA_S} - \frac{N}{K_C} - A\right) & \left(\frac{L^2}{2EI} + B\right) & \left(\frac{L^3}{3EI} + \frac{L}{GA_S} + \frac{N}{K_C} + A\right) \end{bmatrix}$$

$$A = \left(\frac{1}{I} - \frac{1}{I}\right) \frac{L^{2}L_{u}}{E} \sum_{i=1}^{N} \left(\frac{2i-1}{2N}\right)^{2} \qquad B = \left(\frac{1}{I_{c}} - \frac{1}{I}\right) \frac{LL_{u}}{E} \sum_{i=1}^{N} \left(\frac{2i-1}{2N}\right) \qquad C = \left(\frac{1}{I_{c}} - \frac{1}{I}\right) \frac{NL_{u}}{E}$$
$$\det = \frac{L^{4}}{12E^{2}I^{2}} + \frac{L}{EI} \left(\frac{L}{GA_{S}} + \frac{N}{K_{c}}\right) + \frac{AL}{EI} + C \left(\frac{L^{3}}{3EI} + \frac{L}{GA_{S}} + \frac{N}{K_{c}} + A\right) - \frac{BL^{2}}{EI} - B^{2}$$

GLOBAL STIFFNESS MATRIX

$$K_{ii} = \frac{EI_i}{1+4\lambda_i} \begin{bmatrix} \frac{-12}{L_i^3} & -\frac{6}{L_i^2} \\ -\frac{6}{L_i^2} & \frac{4}{L_i}(1+\lambda_i) \end{bmatrix} \quad K'_{ii} = \frac{EI_i}{1+4\lambda_i} \begin{bmatrix} \frac{12}{L_i^3} & \frac{6}{L_i^2} \\ \frac{6}{L_i^2} & \frac{4}{L_i}(1+\lambda_i) \end{bmatrix}$$
$$K_{ij} = \frac{EI_i}{1+4\lambda_i} \begin{bmatrix} -\frac{12}{L_i^3} & -\frac{6}{L_i^2} \\ \frac{6}{L_i^2} & \frac{2}{L_i}(1-2\lambda_i) \end{bmatrix} \quad M_{ij} = K_{ij}^{T''}$$
$$[K_E] = \frac{EI}{1+4\lambda} \begin{bmatrix} \frac{12}{L^3} & -\frac{6}{L^2} & -\frac{12}{L^3} & -\frac{6}{L^2} \\ -\frac{6}{L^2} & \frac{4}{L}(1+\lambda) & \frac{6}{L^2} & \frac{2}{L}(1-2\lambda) \\ -\frac{12}{L^3} & \frac{6}{L^2} & \frac{12}{L^3} & \frac{6}{L^2} \\ -\frac{6}{L^2} & \frac{2}{L}(1-2\lambda) & \frac{6}{L^2} & \frac{4}{L}(1+\lambda) \end{bmatrix}$$

$$\lambda = \frac{3EI}{L^3} \frac{L}{A_S G}$$
$$u_1 \theta_1 \quad u_2 \theta_2 \quad u_3 \theta_3 \quad u_4 \theta_4 \quad u_5 \theta_5 \quad u_f \phi_f$$

$$\begin{bmatrix} K_{11} & K_{12} & 0 & 0 & 0 & 0 \\ K_{21} & K'_{11} + K_{22} & K_{23} & 0 & 0 & 0 \\ 0 & K_{32} & K'_{22} + K_{33} & K_{34} & 0 & 0 \\ 0 & 0 & K_{34} & K'_{33} + K_{44} & K_{45} & 0 \\ 0 & 0 & 0 & K_{54} & K'_{44} + K_{55} & K_{5f} \\ 0 & 0 & 0 & 0 & K_{f5} & K'_{55} + K_{ff} \end{bmatrix}$$

$$K_{ff} = \begin{bmatrix} K_u & 0\\ 0 & K_\phi \end{bmatrix} \quad K_{5f} = \frac{EI}{1+4\lambda_5} \begin{bmatrix} -\frac{12}{h_5^2} & -\frac{6}{h_5^2}\\ \frac{6}{h_5^2} & \frac{2}{h_5}(1-2\lambda_5) \end{bmatrix}$$
$$K_{f5} = K_{5f}^{T''}$$

$$F_i(t_k) = M_{1i}, [u_{1i}, (t_k) - u_{ni}] = M_{II}, i[u_{ni}, -u_{IIi}, (t_k)]$$
(7.1)

$$F_i(t'_k) = M_{1i}, [u_{ni}, -u_{Ii}(t'_k)] = M_{\Pi i}, [u_{\Pi i}, (t'_k) - u_{ni}]$$
(7.2)

Hence

$$\bar{e} = [\dot{u}_{\mathrm{II}i}, (t'_k) - u_{\mathrm{I}i}, (t'_k)] / [u_{\mathrm{I}i}, (t_k) - u_{\mathrm{II}i}, (t_k)] = F_1(t'_k) / F(t_k)$$
(7.3)

In terms of this coefficient, the final velocities are as follows:

$$\dot{u}_{\mathrm{II},1}(t'_{k}) = \dot{u}_{\mathrm{I},t}(t_{k}) - (1+\bar{e})[M_{\mathrm{II}i}\dot{u}_{\mathrm{II}i}(t_{k}) - M_{\mathrm{II}i}\dot{u}_{\mathrm{II}i}(t_{k})]/(M_{\mathrm{I}i} + M_{\mathrm{II}i})$$
(7.4)

$$\dot{u}_{\mathrm{II}i}(t'_{k}) = \dot{u}_{\mathrm{II}i}(t_{k}) + (1+\bar{e})[M_{\mathrm{II}i}\dot{u}_{\mathrm{I}i}(t_{k}) - M_{\mathrm{I}i}\dot{u}_{\mathrm{II}i}(t_{k})]/(M_{\mathrm{I}i} + M_{\mathrm{II}i})$$
(7.5)

The loss of kinetic energy is given as

$$\mathrm{KE}(\mathrm{loss}) = \frac{1}{2} \left[\frac{(M_{\mathrm{I}i} M_{\mathrm{II}i})}{(M_{\mathrm{I}i} + M_{\mathrm{II}i})} \right] (1 - 2^2) (\dot{u}_{\mathrm{I}i}(t_k) - \dot{u}_{\mathrm{II}_i}(t_k))^2$$
(7.6)

The energy loss vanishes when the impact is on elastic build-up. It means $\bar{e} = 1$, the kinetic energy loss will become

$$KE(loss) = \frac{1}{2} \left[\frac{(M_{Ii}M_{IIi})}{(M_{Ii} + M_{IIi})} \right] (\dot{u}_{Ii}(t_k) - \dot{u}_{IIi}(t_k))^2$$
(7.7)
$$(\bar{e} = 0)$$

For completely plastic ($\bar{e} = 0$), since there is no coupling existing between pair of the floors of the build-up. Equations (7.1), (7.2), (7.3), (7.4), (7.5), (7.6), (7.7), (7.12), (7.13), (7.14), (7.15), and (7.16) can be applied to any pair of floors in the two or with one conventional type building and one reactor vessel buildings whenever they come into comtact. Equations (7.11), (7.12), (7.13), and (7.14) and can be summed up as Eqs. (7.11) and (7.12) without the value of [*F*] on the right-hand side. Equation (7.13) stays as it is. However

$$\{\bar{e}\dot{u}_{\rm I}(t_k)\} = \{\dot{u}_{\rm I}(t'_k) - \{\dot{u}_{\rm I}(t_k)\}\}$$
(7.8)

$$\{\bar{e}\dot{u}_{\rm II}(t_k)\} = \{\dot{u}_{\rm II}(t'_k) - \{\dot{u}_{\rm II}(t_k)\}\}$$
(7.9)

$$(t_k \le t < t_{k+1}; k = 1, 2, 3, \dots, e_1 = 0)$$
(7.10)

where (t_k) and (t_{k+1}) are instants corresponding to two successive different states of contacts and Eqs. (7.3) and (7.9) represent the incremental velocities of buildings I and II at time (t_k) , respectively. The velocities $\dot{u}_I(t'_k)$ and $\dot{u}_{IIi}(t'_k)$ after the collision cannot be evaluated from Eqs. (7.1), (7.2), (7.3), (7.4), (7.5), and (7.6). The response of the entire system can be useful between the limits given in Eq. (7.10).

7.3.1.2 Problem Formulation for Publisher Analysis

A containment building and nuclear auxiliary building exist and they are shown in Plate 8.1. Both structures are named as follows:

Nuclear Containment Building \rightarrow I

Auxiliary Lab Building \rightarrow II

7 Concrete Containment Subject to Aircraft Crashes

Both structures are modelled by discrete MDOF systems with concentrated masses. The adjacent masses at the same height are considered as *Contact Impact Case*. One can imagine each pair of masses vibrating initially along the line joining their centres and finally colliding head-on and moving along the same straight line, joining their centres, without rotation after collision which can be treated as inelastic such that the local energy absorption methodologies during impact will be taken into account. Two separate dynamic equations of equilibrium are written for buildings I and II, taking into consideration the geometric compatibility conditions: looking at Plate 7.1, the equations are written as

$$[M_{\rm I}]\{\ddot{u}\}_{\rm I} + [C_{\rm I}]\{\dot{u}\}_{\rm I} + [k_{\rm I}]\{u\}_{\rm I} = -[M_{I}][I]\ddot{x}_{g} - \{F\}$$
(7.11)

$$[M_{\rm II}]\{\ddot{u}\}_{\rm II} + [C_{\rm II}]\{\dot{u}\}_{\rm II} + [k_{\rm II}]\{u\}_{\rm II} = -[M_{II}][I]\ddot{x}_g - \{F\}$$
(7.12)

$$\{u\}_{\rm I} - \{u\}_{\rm II} \le \{\bar{e}\} \tag{7.13}$$

$$\{F\} \ge \{0\} \tag{7.14}$$

in which the displacement, velocity and acceleration column vector, respectively. are relative to the structures base; [M] = structure diagonal mass matrix; [C] = damping matrix; [K] = the structure stiffness matrix; \ddot{x}_g represents the acceleration of support motion and $\{I\}$ is the influence coefficient column vector and = the initial distance between each pair of spheres and $\{F\} =$ the impulsive forces developed between them during collision; $\{0\} =$ zero column vector. The subscripts I and II represent buildings I and II, respectively. Note since the whole system has now turned to be a series of zones, the problem of determining the motion of restrained buildings after collision from the motion before collision can be solved independently between each pair of zones, having masses. For those not in touch, all kinematical terms remain constant. For those which are in contact the liner impulse momentum law to the normal velocities of colliding zones yields in terms of common normal velocity $u_{n,i}$ at the end of approach, called the Goldsmith approach:

$$M_{\mathrm{I},i}u_{\mathrm{I},i}(t_k) + M_{\mathrm{II},i}u_{\mathrm{II},i}(t_k) = M_{\mathrm{I},i}u_{\mathrm{I},i}(t'_k) + M_{\mathrm{II},i}u_{\mathrm{II},i}(t'_k) = u_{n,i}$$
(7.15)

or

$$u_{n,i} = [M_{\mathrm{I},i}u_{\mathrm{I},i}(t_k) + M_{\mathrm{II},i}u_{\mathrm{II},i}(t_k)]/(M_{\mathrm{I},i} + M_{\mathrm{I},i})(M_{\mathrm{I},i} + M_{\mathrm{II},i})$$
(7.16)

where t_k = instant time when an impact occurs,

 t'_k = instant time when an impact ends.

The normal impact force is $F_i(t_k)$ and $F_i(t'_k)$ for the approach and restitution periods.



Plate 7.1 Mutual pounding of adjacent structures during earthquakes

Auxiliary Buildings

The adjacent building associated with the containment structure is shown in Plate 7.1. Various stiffness matrices are given in Plates 7.2, 7.3 and 7.4 which have been used in the program ISOPAR with input shown in Plate 7.1.

Analysis of Results

Pounding occurs between the two adjacent structures when the displacement of containment 1 (relative to the ground \ddot{X}_g) exceeds that of the frame at c of the auxiliary building by the value of the gap size \bar{e} . The impact spring stiffness K_e becomes equal to the force required for a unit rotation of half of the length of





(b) 3D 2% damping (reactor containment combined) with tuning







Plate 7.4 Frequency acceleration time relations: (a) $\bar{e} = 0$, $\bar{e} = 17$ m and (b) when $\bar{e} > 17$ m





the frame ($K_{ea} = 306 \text{ N/m}$). The impact damping coefficient C_{ea} can be determined at point C. $C_{ea} = 61.8 \text{ MN/m}$ was found. The spring stiffness K_{er} was found to be 2.75 GN/m structure. K_e was evaluated as 2.51 GN/m. The value of C_e was 7.12 MN/m. Two modes are taken as typical example and they are 2.4 and 4.78 HZ with respective damping ratios of the associated module motion as 0.0693 and 0.0710.

The maximum relative displacement of point B and point C based on nonlinear calculations for $\bar{e} = 17m$ between the two structures is given in graphical form as shown in Plate 7.2. They give relative displacement time history. The impact force time history is shown in Plate 7.3. The total acceleration time and frequency relations are summarised in Plate 7.5.

For greater understanding of the analysis a reference is made to the authors' following book.

Earthquake Resistant Buildings – Analysis and Design (*With and Without Seismic Devices*) Springer Verlag 2009.

7.4 Data for Program ISOPAR–NLFEA

Table 7.4 gives data for the two structures (structure 1 and structure 2) for program ISOPAR–NLFEA. The theory behind the seismic analysis is clearly established in the text.

7.5 Containment Overpressurisation and Blowdown

7.5.1 General Introduction

This section deals with the dynamic loadings of overpressurisation and pressure suspension in containment due to pressure fluctuations which are induced during blowdown as a result of steam condensation in the suspension pod. In the later cases regarding blowdown two experiments have been conducted: one on Brunsbuttle Power Plant (Germany in 1974) and the other one at Marviken Power Plant (Sweden in 1972–1973). A comprehensive paper on blowdown has been published:

"Dynamic Loading of the Containment During Blow Down: Reviews of Experimental Data from Marviken and Brunsbuttle"

J. Kadlec and R.A. Muller. *Nuclear Engineering and Design*, vol. 38P, 143–158(1976) published by North-Holland Publishing Company, Amsterdam, Holland.

The reader is referred to this paper. The details are not mentioned in this text.

The containment overpressurisation analysis has been carried out using program ISOPAR and results obtained are fully collaborated with the 1/6

| 1. Vessel parameters and auxiliary building dimensions as | | | |
|--|---|--|--|
| stated in Plate 8.1 | | | |
| 2. Containment vessel data | | | |
| Concrete solid elements 20 noded | $2500/\text{sector of } 22\frac{1^{\circ}}{2} - 2 \text{ deep}$ | | |
| Isoparametric type: \rightarrow | 30,000 nodes | | |
| Plastic elements: | | | |
| 8-noded isoparametric 1000 elements/sector of $22\frac{1^{\circ}}{2} - 1$ depth | | | |
| Representing liner or membrane | 8000 nodes | | |
| Prestressing elements 4 noded | 5000 | | |
| Isoparametric | 20,000 nodes/sector of $22\frac{1^{\circ}}{2}$ | | |
| Total embedded or on surface | 2000/sector elements | | |
| Bond elements | 20,000 | | |
| Bar elements: 4 noded | | | |
| Isoparametric | 60,000 nodes/sector of $22\frac{1^{\circ}}{2}$ | | |
| $P_{\rm g}$ = containment vessel internal pressure | \geq 344.75 KN/m ² | | |
| Material parameters are given in Chapter 2 | | | |
| The failure of concrete and cracking criteria | | | |
| there in | | | |
| $\omega_{\rm g} = {\rm natural \ frequency} = 15.7 \ {\rm rad/s}$ | | | |
| 3. Building data | | | |
| Line elements | | | |
| Nodes 4-noded ISOPAR | | | |
| The rest of data visible in Plate .1 | | | |
| Each storey mass $\geq 5.52 \times 10^8$ kg | | | |
| Storey stiffness calculated = $5.404 \times 10^8 \text{ KN/m}$ | | | |
| When VED is considered | 100 total used | | |
| Total number | = 30 | | |
| $\gamma = \text{scale factors}$ | =100 | | |
| $\eta = loss factor$ | =1.12 | | |
| $\xi_g = $ soil damping ratio | = 0.61 | | |
| $5_{\rm w}$ = white noise input data | = 1.0 g | | |
| k = each brace | ≯ storey stiffness | | |
| α weighting ratio | =4.120 | | |
| $E_{\rm s} = 200 {\rm GN/m^2}; \sigma_y = f_{yt} = 460 {\rm N/mm^2} {\rm considered}$ | | | |
| Plate elements | = 500/floor, edge nodes are linked | | |
| 10 bond elements | | | |
| 4. Seismic data | | | |
| \dot{u} velocity: 50 cm/s; | | | |
| <i>ü</i> acceleration | | | |
| X- direction | 200 gal | | |
| Y- direction | 200 gal | | |
| Z- direction | 50 gal | | |
| D = maximum drift = 2% | | | |
| $\bar{e} = \text{gap maintained} = 17 \text{ m} = d$ | | | |
| $\ddot{x}_g =$ ground acceleration as shown | | | |

 Table 7.4
 Data from program ISOPAR–NLFEA

Plate 8.1 For undamped vibration $c = c_e = 0$ $\frac{\tilde{e}}{u_{g0}} \neq 5$ for $\xi = 0$ $\omega_g/\omega \neq 1.8$ computer program limitation Test case I. One-sided impact $K=4, \xi = 0.05$ e - coefficient of restriction = 0e - pounding and impact distance 0–17 m

scale R C model containment test results by Lawrence Livermore laboratory and many others.

7.5.2 Containment Overpressurisation

A 1/6 th scale R C model (Figs. 7.20 and 7.21) has been designed for a design pressure of 317 KN/m^2 . The reinforcement layouts are shown in Figs. 7.22 and 7.23. A pre-test analysis has been carried out using the program ISOPAR. The endochronic model representing the failure of concrete along with cracking criteria indicated in the text has been adopted.

The results are compared with others in Figs. 7.24, 7.25, 7.26 and 7.27 using the 3D finite element analysis with non-linear dynamic solutions. The mesh scheme for this technique for a model is shown in Fig. 7.28. The final model is shown in Fig. 7.29 and some cracks and their zones are indicated in a portion of wall in Fig. 7.30.

The Sizewell B model provided by then CEGB was overpressurised. Figure 7.33(a) gives the displacement pattern. The vessel model failed at 3.15 times the design pressure by rupturing reinforcements crossing the developed cracks. The model is of the type indicated in Figs. 7.30 and 7.31. The post-mortem of the Sizewell B containment model with crack patterns is shown in Fig. 7.31.

For the Lawrence Livermore model, the pressure -displacements are collaborated well with the experimental and theoretical models. They are summarised in Figs. 7.24, 7.25, 7.26, 7.27, 7.28, 7.29, 7.30, 7.31. Thus, these results validate the analytical work and computer program ISOPAR-NLFEA.

Concrete structures are equal to 30 GPa, 0.2, 2.5 Mg/m³ and 0.07, respectively. The horizontal earthquake excitation is represented by the input–time history of Fig. 16, scaled to a maximum acceleration of 0.3 g. No vertical or rotational input components are considered. The structures of the plant are constructed on a deep firm soil layer whose (uniform) material properties, compatible with the strain level of the prescribed earthquake, are as follows:



Fig. 7.21 Schematic of the 1/6th scale reinforced concrete containment model elevation view (Courtesy of Lawrence Livermore, USA)

Dynamic shear modulus = 0.6 GPa, Poisson's ratio = 0.4, density = 2.4 Mg/ m³ and coefficient of hysteretic damping = 0.05.

The dynamic model is also shown schematically in Fig. 7.21. The auxiliary building is indicated on the right-hand side of this figure. It is assumed that only the roof slab of the structure, which is hardened for aircraft impact, hits the reactor building during the earthquake. To extend the scope of this investigation, the gap size *e* is varied. For the purpose of this analysis, where primarily the response of the reactor building is of concern, the auxiliary building is adequately represented by a simple frame with one (horizontal) degree of freedom. The dimensions of the roof slab (length 72 m, width = 30 m, thickness 1.2 m) result in a mass ma = 6.48 Gg of this 1-DOF system. Assuming a representative natural frequency of 3.50 Hz, a stiffness coefficient k_a is calculated as 3.13 GN/m. A damping ratio of 0.07 determines the damping coefficient $C_a = 20.0$ MN s/m. The axisymmetric reactor-shield building is modelled with 32 curved higher-order isoparametric frusta in the meridional direction. Inasmuch as (in this investigation) the results are calculated on the outer shield building only, the







Fig. 7.23 Comparative study $-(-\cdots, SNL; -, NIL; --, SERD; -\Box -, CEGB; -\bigcirc -, EPRI; ---, BNL; -\Box -, ENEA; ---, ANL; \bullet - \bullet, CEA; -\triangle -, GRS; -\bullet -, Bangash) (Courtesy of Lawrence Livermore, USA)$



Fig. 7.24 Comparative study – 2 (see Fig. 7.26 for key) (Courtesy of Lawrence Livermore, USA)



Fig. 7.25 Comparative study – 3 (see Fig. 7.26 for key) (Courtesy of Lawrence Livermore, USA)



Fig. 7.26 Comparative study – 4 (see Fig. 7.26 for key)



Fig. 7.27 One-sixth scale RC containment - finite element mesh



Fig. 7.28 Containment vessel final mode [1006; ISOPAR]



Fig. 7.29 Major crack zones [1006](denotes zero tensile stress; denotes crushing; denotes radial vertical cracking)



Fig. 7.30 Cracked containment

Fig. 7.31 Sizewell B overpressurisation analysis – final mode



internal structures and the base are modelled as a rigid body. In the circumferential direction, the standard Fourier expansion method is used. It is assumed that the impact force from the frame acts horizontally on an area on the middle surface of the shell equal to 3 m in the meridional times 12 m in the circumferential direction at point B. This evenly distributed load is decomposed circumferentially into 16 Fourier terms. For each harmonic, 297 dynamic degrees of freedom result for the reactor building. Structural damping of 0.07 times the critical value is selected. The impedance function of the soil, modelled as a visco-elastic half space, is approximated as being frequently independent. The corresponding springs and dashpot are shown schematically in Fig. 7.20.

In addition to this quite elaborate analysis, referred to as the 'rigorous' solution further on, the pounding structures are also represented as a twodegree-of-freedom (2-DOF) system (Fig. 7.21). The properties of the first structure are associated with the response of the reactor building in the first mode of the first harmonic (fundamental mode). The corresponding frequency equals 2.30 Hz. Using this mode shape as the shape function, the generalised mass $m_1 = 53.1$ Gg and the generalised stiffness $k_1 = 11.1$ GN/m are calculated. The corresponding damping coefficient $C_1 = 107$ MNs/m. The modelling of the second structure in Fig. 7.22 is identical to that of the frame in Fig. 7.20 ($m_2 = m_a, k_2 = k_a, C_2 = C_a$).

Chapter 8 Bonded Reinforcement in the Concrete Reactor Pressure and Containment Vessels

8.1 Introduction to the Main Philosophy

The quantity and disposition of main bonded reinforcement in the Hunterston— 'B' P C P V is taken as a typical case study. In this chapter covering only main and local bonded reinforcement are covered. An attempt has been made to discover the need and function of main bonded steel in the prestressed concrete cylindrical pressure vessel. The same is adhered to the containment vessel. At present there is no established method available to determine the amount of such steel needed in the vessel and to adjudge its performance during working and overload conditions of the vessel.

The elastic analysis carried out for the vessel hardly suggests the need of such reinforcement apart from where maximum stress concentrations occur. The present ultimate load analysis for the vessel needs very little help (about 10%) to develop along with prestressing tendons and the liner steel a full assumed ultimate strength of the vessel. In both these stages, namely elastic and ultimate load, certain assumptions are adopted, the truth of which is yet to be discovered. Moreover, many other factors are unknown about the vessel behaviour including those from creep, shrinkage, construction and general accidents. All of them individually as well as in combination will create infinite number of cracks in the body of the vessel, thereby causing a premature failure of the vessel before ultimate load is reached. Greater emphasis is therefore laid on these factors in this report and it is maintained that cracks developing due to above causes must be controlled by bonded steel and they should also be sufficient in quantity so that a rise of pressure would lead a progressive increase in depth of cracks incipient or already present under working conditions. More research work is recommended for the accurate assessment of the bonded steel quantities. Local areas with and without penetrations obviously require special analysis such as finite element to assess whether or not unacceptable stresses and cracks are present. Those areas need to offset them. These analyses obviously act as a scanning processes.

8.1.1 General Rules for the Disposition of the Main Bonded Reinforcement in the Pressure or Containment Vessels

The following general rules are taken into account for the disposition of main bonded reinforcement.

8.1.1.1 Disposition Type-1

The behaviour of the vessel must be thoroughly studied under working and overload conditions prior to the assessment of bonded steel. Sufficient bonded steel is provided in areas of maximum stress concentration under working conditions and is gradually reduced for economic reasons to areas of low tensile or high compressive stresses. Where cracks are predicted at pressure above design value, bonded steel provided there must be sufficient to effectively control the initiation and propagation of these cracks.

8.1.1.2 Disposition Type-2

Sufficient strain must be developed in the vessel due to cracking to enable the prestressing tendons, bonded steel and liner to develop their full assumed ultimate strength, i.e., the number of cracks times the average crack width must be equal to the additional elongation necessary to bring tendons up to 90% GUTS.

8.1.1.3 Disposition Type-3

Bonded reinforcement in all areas must be sufficient to accept, without failure, the tensile load transferred to it during vessel cracking. In general, a minimum percentage of steel based on the area of cross-section of the vessel (in this case not more than 0.3%) should be investigated for ultimate load reasons and then distributed in proportion on the outside and inside faces of the vessel.

8.1.1.4 Disposition Type-4

In assessing the contribution of bonded reinforcement to the ultimate strength of the vessel due consideration shall be given to the stress–strain curve of the steel concerned. The stress allowed in the bonded steel shall not exceed that corresponding to a strain of 1%. The minimum average strain in bonded steel shall be given by dividing crack width by crack spacing from a well-distributed crack pattern formed in the vessel.
8.1.2 Choice of Main Bonded Reinforcement

The choice of main bonded reinforcement is based on its high tensile strength and interaction between it and concrete, resulting in higher bond length and an improved degree of crack control. A considerable experimental work has been carried out by research on steel bars such as GK 60 deformed bars in close cooperation with the manufacturers. Experience of design companies with this material in the past suggests to use $GK + 60 \ 1\frac{4''}{4}$ dia. (31 mm) bar as main bonded reinforcement steel. It develops a stress of 60,000 psi at 0.2% strain and has an ultimate strength of about 100,000 psi (735 MN/m²) at minimum guaranteed elongation of 14%. The low carbon content (comparable to mild steel) of GK 60 reinforcing bar simplifies welding in local areas and can expect to carry the full tensile strength of the bar. Bond tests carried out on G.K 60 according to BS8110 of EC-2 indicate that where an end slip of 0.001'' occurs its bond strength exceeds a plain bar by more than twice the 40% suggested by B8110 of EC-2 and with initial end slip, the anchorage value increases continuously up to the maximum value. This suggests that by using this type of reinforcement, no hooks are required in the vessel concrete.

All main bonded reinforcement shown on vessel drawings cannot be less than $1\frac{1''}{4}$ dia. (31mm) high tensile GK + 60 bar. Minimum requirement of bonded steel in different areas of the vessel is, therefore, based on the properties of GK + 60 bar or similar. For other types approved by authorities, special tests shall be carried out.

8.1.2.1 Choice of the Minimum Percentage of Main Bonded Reinforcement

The phrase 'Percentage of Bonded Reinforcement' is ambiguous in many existing vessels; nevertheless, minimum percentage of steel based on cross-sectional area of the vessel is still regarded as the basis of design quantity in the vessel with some variations depending upon different requirements, discussed elsewhere. The minimum percentage of bonded GK 60 reinforcement steel for pure tensile case is shown in Fig. 8.1. This figure is obtained on a simple basis of assuming concrete failure stress of 300 psi (2.07 MN/m²) with a steel stress of 90,000 psi (620 MN/m²). The figure becomes 0.46% if corresponding steel stress is assumed to be 60,000 psi. (441 MN/m²). The research on other containments inclusive WYLFA vessel indicated that the steel is likely to rupture following the formation of primary cracks if the amount is greater than 0.2% of the cross-sectional area of concrete. Therefore 0.2% steel is considered as minimum steel to be placed in any cross-section of the vessel concrete.

In Hunterston 'B', a desirable assumption is made that the bonded reinforcement is capable of maintaining a strain of 100 micro-strain throughout the vessel in order to assist in the formation of a well-disposed crack pattern, hence a strain of 100×10^{-6} can be propagated if the percentage reinforcement is of the order

$$\frac{250}{90,000} \times 100 = 0.277\%$$
 of concrete area

- - -



Fig. 8.1 Disposition of main bonded reinforcement in the vessel

This value is found experimentally in case of WYLFA. A conservative value of 0.3% of the area of cross-section is allowed for ultimate load purpose. As indicated in the general rules the obvious choice is that this should be distributed in a proportion 0.2% on outer face of the vessel and 0.1% at the liner. Being a conservative choice, this selection is kept in areas of the vessel where maximum hinges or cracks occur at ultimate load. The reason of not putting the whole amount of 0.3% on the outside face comes from the fact that it would be difficult in practice to fix steel and pour concrete in the congested outer face area of the vessel. Areas outside the predicted maximum crack zones are reinforced with 0.15% (approx.) of the area of cross-section of the vessel (refer to Fig. 8.1c, d). To limit cracking, should any occur under pressure test conditions, 0.05% of bonded steel is provided near the inner face in a similar manner to the outer layer. Therefore away from the critical areas of crack formation at ultimate load, the choice of minimum bonded steel is always 0.15% on outside face and 0.05% near the inner face. It is of interest to note the following additional points regarding the requirements of minimum steel.

8.1.2.2 Disposition Requirement Type-1

Bonded reinforcement is considered up until now to control tensile stresses in the concrete of the vessel. In fact, concrete is subjected to both tensile and flexure effects. The flexural stresses arise from the temperature cross fall through the vessel barrel. As a pure flexural member (refer to Fig. 8.1), the estimate is that only one-half of steel areas mentioned above would be necessary. Since the conditions in the vessel are partly between these two cases, it is justifiable to take 0.2% bonded steel, made up of 0.15 and 0.05% on the outer and inner faces, respectively, as discussed earlier.

8.1.2.3 Disposition Requirement Type-2

In actual vessel tensile stresses up to 500 or 600 psi $(3.45-9.14 \text{ MN/m}^2)$ will exist at the outer face of vessel concrete during working conditions for 15° C temperature cross fall.

This is based on a fact that smaller cracks have already been initiated at construction joints or any other areas of low tensile strength and at areas of maximum stress concentrations. These cases are very difficult to analyse, hence engineering judgement is required to assess the amount of steel in areas under these worse effects on top of above requirements.

8.1.2.4 Disposition Requirement Type-3

'Anti-crack steel' is necessary to be placed as splay bars in the haunch area of the vessel to control major cracks predicted at ultimate load. Preferential cracking at this position is possible due to stress concentration and will already be existing in order to bring about premature failure before the development of a

major crack. 'Anti-crack steel' helps to a greater extent, if placed as close to the liner as possible, in contributing along with horizontal and vertical bars towards controlling these cracks.

8.1.2.5 Design of Main Bonded Steel

General Vessel Analysis

As explained earlier, it is expected that concrete adjacent to the outer face of the vessel will lose moisture at a greater rate than in the general body of concrete. This moisture gradient causes differential shrinkage and tensile stresses are introduced in the outer face of the vessel. In addition to these, tensile stresses due to differential cooling strains are introduced in the vessel together with stresses due to stress concentration, constructional stresses and thermal gradient stresses. The overall tensile stress value between 500 and 600 psi is taken on the outside face of the vessel. It is also noted that a tensile stress of 500 psi (3.45 MN/m²) is permitted on the outside face due to temperature cross fall of 15° C at working conditions. For preliminary design, areas outside haunch and equator, carrying bonded steel, are designed on the basis of Fig. 8.2 (a, b). At equator and at the haunch Fig. 8.2 (c, d), has been considered in order to arrive at the quantity of bonded steel. Figure.8.2 shown in calculation I is maintained for preliminary design and is selected after careful study of the vessel behaviour during working conditions.

A special case around the haunch due to local effects with and without fillet is taken to check the steel in that area. Figure. 8.3 in calculation I represents the principal tensile stresses around haunch both with and without fillet. These values are taken from computer program for prestress plus proof pressure case. Four different cases are analysed both across the barrel wall and the cap with and without principal compressive stresses.

As shown in Section 8.2.1.2, a barrel wall is analysed as a in infinite cylinder for combined loading of hoop prestress, temperature and design pressure with the following limitation:

+
$$[f_{t0} + f_{p10} + f_{p20}] \le f_s = +500 \text{ psi (outside tension)}$$
 (8.1)

$$-\left[f_{\text{ti}} + f_{p2i}\right] \leq f_{\text{c}} = -2200 \text{ psi (inside compression)}$$
(8.2)

Refer to Fig. 8.4 where

 $f_{\rm ti}$ = hoop stress on inside due to temperature;

 f_{p10} = hoop stress on inside due to internal pressure;

 f_{p20} = hoop stress on inside due to external pressure;

 f_{p2i} = hoop stress on inside due to external pressure.



Fig. 8.2 General criteria for nominal main bonded reinforcement

The results tabulated indicate that the stresses are well within the limiting cases. Hence reinforcement design based on 500 psi tension allowed for 15°C temperature cross fall on the outer face is safe. It is of interest to note that compressive stress on the inside face of the vessel due to above combination of loads is well within the allowable compressive stress, i.e. 2200 psi for Hunterston 'B' concrete mix of 5400 psi cube strength at 28 days.





8.1 Introduction to the Main Philosophy

Fig. 8.4 Cylindrical part



Figure 8.5 shows from zero tensile stress to 500 psi tension for various internal pressures and ratios of inside and outside radii, i.e. wall thicknesses. This is based on a simple formula:

$$P_{1} = \left(f_{t} + 0.45f_{c}'\right)\frac{\frac{1-a^{2}}{b^{2}}}{\frac{1+a^{2}}{b^{2}}}$$
(8.3)

All these notations are defined in Fig. 8.5. It is interesting to note that tension in concrete becomes more significant for internal pressure only when it is reaching ultimate load somewhere halfway; 500 psi (3.45 MN/m^2) tension is hardly reached for a ratio of approximately 1 between internal and external radii. Thus the choice of 500 psi is conservative if no temperature is considered as in the case of ultimate load. This graph covers various barrel wall thicknesses and will be useful for future reports on bonded reinforcement. In Section 8.2.1.3, a good attempt has been made to analyse the cap for the design pressure plus temperature. By assuming the cap fixed all round circumferentially with certain elastic fixity (n=0.5) in vertical direction due to scattering positions of the vertical tendons, it is assumed that the steel does not reach yield point under design pressure and that the principal problem of the plastic design of two-way reinforced cap is represented by the determination of their redistribution factor values. The cap is transformed into a mechanism shown in Fig. 8.6. The 'minimum re-distribution criterion' is established for a given design pressure and cap dimensions.

Bending stress in the cap is found to be insignificant and the caps arc too thick to develop bending under design pressure. However, on top of it, direct stresses due to temperature $(339 \text{ psi} (3.34 \text{ MN/m}^2) \text{ tension on})$



Fig. 8.5 Graphs showing variations of internal pressure and concrete tensile stress for a given strength of concrete

outside and 131 psi (0.904 MN/m²) compression on inside) taken from computer program as a worse case gave the total area of steel necessary to be 1.1565 in². (10.04 cm²) based on 16.3" to standpipes, 21" dia. GK + 60 bars are required on outside face of the cap, which is less than what is required from conditions established in Fig. 8.5 and for the 'Ultimate Load Analysis'. In general the bonded steel 5-layers of $1\frac{1}{4}$ " (30 mm) dia. bars on the outside face is more than sufficient. This is justified later on under 'Quantity and Spacing of Bonded Steel'.

Taking a segment of the cap between the centres of two boilers and by means of virtual work method, the cap reinforcement is analysed at the edge of standpipe area and at the inside of the barrel wall, i.e. at the junction between the cap and the wall, subject to external hoop prestress and ultimate gas pressure. The amount of steel thus required is

3.47in.² or
$$3 - 1\frac{1''}{4}$$
 dia bars at 16.3" c/c

In SI system (3T30 @ 415 mm) centres or 3T30 – 415 centres





As mentioned earlier, the minimum steel is between 0.25 and 0.3% 5-layers of $1\frac{1''}{4}$ dia. (30mm) bars on the outside are given for the 'Ultimate Load Analysis' and 3D Finite Element Analysis.

In Section 8.2.1.5, with a given cap reinforcement shown in Figs. 8.1 and Table 8.1 computer results from 'Finite Element Analysis' are taken to check the cap for shear and principal stresses. In Fig. 8.8 the loads are shown (combined loading from vertical and hoop prestress and internal ultimate pressure). Random values arc taken from the program ISOPAR and stresses



Fig. 8.7 Cap reinforcement at ultimate load

are checked at the edge and at the predicted failure plane. Principal tension is 135 psi (0.923 MN/m^2) at the failure plane which is close to allowable value and the cap is not necessary to be reinforced in that area. On the other hand at the edge nominal barrel shear is 21 psi. Reinforcement in this area is sufficient to look after any effect due to shear or principal stresses.

| Area | rea Description of reinforcement bars | | | | |
|------|--|--|--|--|--|
| A | $1\frac{1''}{4}$ dia. bars in 3 layers at 10'' crs. both ways | | | | |
| В | $1\frac{1}{4}$ dia. bars in 2 layers at 10" crs. both ways | | | | |
| С | $1\frac{1}{4}$ dia. bars in single layer at 10" crs. both ways | | | | |
| D | $1\frac{i''}{4}$ dia. bars in 2 layers between boilers (circumferential) | | | | |
| | $1\frac{i}{4}$ dia. bars in 3 layers at 10" crs. (radial) | | | | |
| E | $1\frac{1}{4}$ dia. bars in 5 layers at $16\frac{1}{4}$ crs. both ways | | | | |
| | $1\frac{i''}{4}$ dia. bars in 5 layers at $16\frac{i''}{4}$ crs. (orthogonal grid) | | | | |
| F | $1\frac{1}{4}$ dia. bars in 2 layers at $16\frac{1}{4}$ crs. both ways | | | | |
| | $1\frac{1''}{4}$ dia. bars in 5 layers at $16\frac{1''}{4}$ crs. (orthogonal grid) | | | | |
| G | $1\frac{1''}{4}$ dia. bars in 3 layers at $16\frac{1''}{4}$ crs. both ways | | | | |
| | $1\frac{1''}{4}$ dia. bars in 3 layers at $16\frac{1''}{4}$ crs. (orthogonal grid) | | | | |
| Н | $1\frac{1''}{4}$ dia. bars in 4 layers at $16\frac{1''}{4}$ crs. both ways | | | | |
| | $1\frac{1''}{4}$ dia. bars in 4 layers at $16\frac{1''}{4}$ crs. (orthogonal grid) | | | | |
| J | $1\frac{11}{4}$ dia. bars in 3 layers at 10" crs. (vertical) | | | | |
| | $1\frac{1''}{4}$ dia. bars in 2 layers at 20'' crs. (horizontal) | | | | |
| K | $1\frac{11}{4}$ dia. bars in 2 layers at 10" crs. (vertical) | | | | |
| _ | $1\frac{11'}{4}$ dia. bars in 2 layers at 20'' crs. (horizontal) | | | | |
| L | $1\frac{11}{4}$ dia. bars in single layer at 11 crs. | | | | |
| | $1\frac{1''}{4}$ dia. bars in single layer at 11'' crs. (orthogonal grid) | | | | |
| М | $1\frac{17}{4}$ dia. bars in 2 layers at 11" crs. both ways | | | | |
| NT. | $1\frac{11}{4}$ dia. bars in 2 layers at 11'' crs. (orthogonal grid) | | | | |
| N | $1\frac{17}{4}$ dia. bars in 3 layers at 11" crs. both ways | | | | |
| D | $1\frac{17}{4}$ dia. bars in 3 layers at 11'' crs. (orthogonal grid) | | | | |
| Р | $1\frac{1}{4}$ dia. splay bars in 3 layers with $1\frac{1}{4}$ dia spacer. | | | | |
| D | bars in 2 layers $1/\sqrt{1-1}$ and $1/\sqrt{1-1}$ bars | | | | |
| K | $1\frac{1}{4}$ dia. bars in 4 layers at $12^{\prime\prime}$ crs. both ways | | | | |
| C | $1\frac{4}{4}$ dia. bars in 4 layers at $12''$ crs. (orthogonal grid) | | | | |
| 2 | $1\frac{1}{4}$ dia. bars in 6 layers at 12" crs. (circumferential) | | | | |
| | $1\frac{1}{4}$ uia. bars in 0.12° layers (radial) | | | | |

Table 8.1 Location of Main Bonded Reinforcement (key: 1 ft = 0.3098 m, 1 in = 25.4 mm)

Note: This should be read in conjunction with Fig. 8.1 *Note*: $1\frac{1''}{4}$ in metric T-30m.s. All GK. 60 bar

8.1.3 Crack Distribution and Control Analyses of the Vessel

Various crack distributions shall be summarised in a separate section and indicates distribution of stresses between cracks of a well-disposed crack pattern of the wall. Figure 8.9 can be drawn in which the embedment and tension areas in the barrel wall are defined. Main bonded steel in these areas is defined on the basis of a single bar embedded in vessel concrete which would span a certain crack width and also between two cracks of a well-disposed crack pattern as indicated earlier. As the strain in main bonded steel varies from maximum at the crack to a reduced value in between the two cracks, it becomes necessary to know the minimum average strain in the bonded steel.



The minimum value is defined as

$$\frac{W}{L}$$
 (8.4)

where W is the width of crack; L the average crack spacings. 'W' and 'L' both depend on the shape of the vessel, bonded steel and the way the internal forces are distributed in the vessel. Moreover, construction joints, local stress concentrations and thermal stresses will be additional factors to assist in the formation of these cracks.

In the uncracked part of the vessel concrete, tie strain assumed is 100 microstrain. Therefore, the average strain in the bonded steel is

$$100 \text{ mirco} - \text{ strain} + \frac{W}{L} \tag{8.5}$$

Various theories gave different values of 'W' and 'L' and they are tabulated in Section 8.2.1.2.

The average values are taken as W = 0.05'' (1.27'' mm);

$$L = 30''(762 \,\mathrm{mm}).$$

As the pressure increases more and more cracks are formed and the value of 'L' will be reduced. It is necessary therefore to limit the size of the cracks by providing sufficient bonded reinforcement. The size of the crack is limited to 0.3 mm (0.0118") and the number of G.K + 60 bars of $1\frac{1}{4}$ " dia. required to do so

load



Fig. 8.9 Embedment and tension areas location in the barrel

is 3. This condition is applied only near the equator and at the haunch. In all other areas it is taken for granted that at a stress of 60,000 psi in a bar, a crack width of 0.05" (1.27 mm) can be expected. Thus in the whole vessel the minimum number of bars necessary to be placed for obvious reasons of these cracks is to be $2-1\frac{11}{4}$ dia. G.K. + 60 type. They are shown in Figs. 8.1 and Table 8.1 of this chapter. This matches very well with the reasons discussed earlier.

In an axisymmetric vessel the cracks in the longitudinal direction in the barrel and radial direction in the top cap will in theory be infinite in number. In nonaxisymmetric vessel such as in the Hunterston 'B' containing boiler pods, the number of these cracks is assumed at ultimate load to be limited by the number of weak sections. Since peak bending moments occur because of loading and inter-restraint, between cap and wall, the meridional cracks will be bounded by a few major cracks in the haunch region and near the equator. These cracks at ultimate load are tabulated in Section 8.2.1.3. The results are taken from 'Ultimate Load Analysis' and the crack pattern in this case is shown in Fig. 8.11. These cracks vary from 1.8" (38 mm) to 3.6" (91.5 mm). Also in Section 8.2.1.4 crack formulation at ultimate load corresponding to liner failure strain is evaluated for stud spacings of $8\frac{1''}{4}$ (205 mm) and 9'' (235 mm). The crack width that a liner can span comes out to be 1.57" (40 mm), corresponding to 28% liner steel strain and 14% GK +60 bar. However, the crack sizes are compatible. Thus a common figure of 2'' (50 mm) crack width is taken at ultimate load. This is checked by the 3D Finite Element whether or not the bars lie matching the solid element nodes.

It is assumed that smaller crack developed in major crack zones is progressively increased to 2 inch (50 mm) width at ultimate load and it is necessary to check the bursting stress in the bar and the bond length required at that stage, in Section 8.2.1.5, analysis is carried out to check the minimum GK-60 inch bond length of steel provided in the vessel. Previous research indicates that at ultimate load $1\frac{1}{2}$ (40 mm) dia. GK + 60 bar can span over 2'' (50 mm) crack for a stress differential of 40,000 psi. Thus, at ultimate load conditions 2 no. $1\frac{11}{4}$ (30 mm) dia bars will still be a reasonable number to control the crack. The number of bars from Brice theory in this area comes out to be 3. Thus, in major crack zones, this number is maintained in either direction as shown in Fig. 8.1 and Table 8.1.

8.1.4 Quantity and Spacings of Bonded Steel

The disposition of main bonded reinforcement shown in Fig. 8.1 clearly shows a change of the amount of bonded steel from one zone to another. All these zones are named and are given reasonable dimensions. Quantities and spacings of bonded steel in these zones are based on design requirements, as discussed earlier.

As a general rule, outer skin and inner skin bonded steel are taken to be 2layers at 10'' (250 mm) c/c and single layers at 10'' c/c both ways, respectively. Departure from this general rule in some areas is based on certain requirements to be met at working and overload conditions.

In the top and bottom caps, the number of layers and spacings vary but the quantity of steel necessary is kept more or less the same. In top cap standpipe area, the bar spacings are rearranged to fit between standpipes while at the inside face of the bottom cap, the spacings are limited by the grout holes. These bars are placed in orthogonal grid. All radial and circumferential bars in top and bottom caps are fitted in between the tendons and hence their spacings are not constant. In order to adjust the minimum requirement of 3 layers at 16.3" (415 mm) c/c or 2 layers at 10" (250 mm) c/c, the number of bars is increased. Additional reinforcement is shown in the caps around boiler pods in order to meet ultimate load requirements.

All bars have been given full bond lengths. Various lap lengths given in the vessel have been worked out from the construction programme of lifts and bays.

After the final arrangement of bonded steel, each zone is further checked on the basis of the following limitation:

$$\mu \times f_{sf} \ge t_{ca} \tag{8.6}$$

where

 μ is the bond steel ratio; f_{SF} the rupture stress of bond steel; t_{ca} the tensile stress of concrete.

8.2 Calculation 1

8.2.1 General Criteria for Nominal Main Bonded Reinforcement

8.2.1.1 General Problems

It may be expected that concrete adjacent to the outer surface of the 'vessel' will lose moisture at a greater rate than in the general body of the vessel. This moisture gradient through the thickness of the vessel will cause differential drying shrinkage and the tensile stresses, hence, are introduced in the outer surface of the vessel. These stresses are effectively controlled by means of bonded reinforcement.

In Additional to these tensile stresses, some random tensile stresses are introduced due to differential cooling strains which cannot be covered by analysis; constructional stresses locked in, local stress concentration and thermal gradient stresses are some more to be considered while assessing the amount of reinforcement.

For preliminary disposition of main bonded reinforcement, it is necessary to study carefully the 'vessel' behaviour during elastic and ultimate load conditions and a proposed construction technique. After careful study of the 'vessel', general criterion for main bonded reinforcement is established. This criterion is indicated in Fig. 8.2. It covers preliminary requirements for general 'vessel' areas and specific haunch and equatorial regions. A tensile stress of 1500 lb/m² (3.45 MN/m²) at working conditions, worse case of 600 psi (4.15 MN/m²) at ultimate load is also considered.

Check on reinforcement around haunch based on stress concentration figures (principal tensile stresses) with and without fillets is also made, taking zones across the barrel wall and the cap. Four different cases shown in Fig. 8.3 have been taken for analysis, with and without principal compression. These are the stresses for proof pressure case from elastic analysis carried out on computer using program ISOPAR or equivalent.

8.2.1.2 Prestress, Temperature and Design Pressure

After selecting and locating reinforcement in the barrel, various areas are checked for combined loading of prestress, temperature and pressure.

$$\rho = \text{radius}$$

$$a = \text{internal radius} = 21 - 6'(6.5532 \text{ m})$$

$$b = \text{external radius} = 42' - 16'' \text{ (excluding channel shutters)}$$

$$p_1 = \text{internal pressure} = 644 \text{ psi design pressure}$$

$$p_2 = \text{external pressure due to circumferential prestress} = (700 \text{ psi average})$$

$$T_x = \text{temperature cross fall} = 15^{\circ}\text{C}$$

$$\alpha = \text{thermal coefficient} = 9.2 \times 10^{-6}$$

$$E_c = 5 \times 10^6 \text{psi} \left(34,500 \text{ MN/m}^2 \right)$$

$$f_c = \text{Permissible working compressive stress} = 200 \text{ psi (p/s + pressure)}$$

$$f_s = \text{Permissible working tensile stress} = 500 \text{ psi}$$

$$f_t = \text{hoop stress due to temperature cross fall}$$

$$f_{p1} = \text{hoop stress due to internal pressure}$$

$$v = \text{Poisson's ratio} = 0.15$$

$$f_{ti} = \text{hoop stress on inside due to temperature}$$

$$f_{p2}^{-} = \text{hoop stress on inside due to temperature}$$

$$f_{p1}^{-} = \text{hoop stress on inside due to temperature}$$

All other suffixes 'i' and 'o' are for inside and outside, respectively.

General Cases

$$f(\text{hoop}) = \frac{p_1 a^2 - p_2 b^2 + \left(\frac{a^2 b^2}{\rho^2}\right)(p_1 - p_2)}{(b^2 + a^2)} + \text{compressive tensile compression (8.7)}$$

$$f(\text{radial}) = \frac{p_2 b^2 - p_1 a^2 + \left(\frac{a^2 b^2}{\rho^2}\right)(p_1 - p_2)}{(b^2 - a^2)}$$
(8.8)

(a) Internal pressure only

$$f_{p_1} = \frac{a^2 p_1}{b^2 - a^2} \left(1 + \frac{b^2}{\rho^2} \right)$$
(8.9)

8.2 Calculation 1

(b) External pressure only

$$f_{p_2} = \frac{-b^2 p_2}{b^2 - a^2} \left(1 + \frac{a^2}{\rho^2} \right)$$
(8.10)

(c) Temperature cross fall

$$f_{\rm t} = \frac{E_{\rm c} \alpha T_x}{2(1-v) \log_{\rm c} b/a} \left[1 - \log_{\rm c} \frac{b}{\rho} - \frac{a^2}{b^2 - a^2} \left(1 + \frac{b^2}{\rho^2} \right) \log_{\rm c} b/a \right] \quad (8.11)$$

Limiting Cases

+
$$|f_{to} + f_{p_1o} + f_{p_2o}| \le +f_s = +500 \operatorname{psi}(\mathrm{MN/m}^2)$$
 (8.12)

$$-\left|f_{\text{ti}} + f_{p_{2}i}\right| \le -f_{\text{c}} = -2200 \operatorname{psi}\left(-15.18 \operatorname{MN/m}^{2}\right)$$
(8.13)

| | p_1 | | p_2 | p_2 | |
|------------|-------------|------------|-------------|------------|--|
| | f_{p_1} i | f_{p_1o} | $f_{p_2 i}$ | f_{p_2o} | |
| psi | + 11.15 | + 473 | - 1918 | - 1215 | |
| (MN/m^2) | (+7.94) | (+3.28) | (-13.235) | (-8.384) | |
| | | | | | |

| | $f_{ m ti}$ | $f_{ m to}$ |
|------------|-------------|-------------|
| psi | -219 | +1090 |
| (MN/m^2) | (-1.511) | (+7.5215) |

Applying Limiting Cases

$$1090 + 473 + (-1215) = 348 < 500 = 3.45 \text{ MN/m}^2$$

 $- 1918 - 219 = -2137 < -2200 = -15.18 \text{ MN/m}^2$

~

OK

Minimum reinforcement $2 - 21\frac{1}{4}\phi$ bars at 10 c/c is required. In some areas such as near the haunch, additional reinforcement is introduced for the reason indicated elsewhere in this chapter.

8.2.1.3 Plastic Design of Caps Under Symmetrical Working Loads

Notation

a = radius of cap periphery

b = radius of a load surface

 g_s = permanent load uniformly distributed on a unit area

 $G_{s'}G$ = over load and design lond

$$G_{s'}G \gamma_g = 1$$

 $L_{\rm M}, L_{\rm G}, L_{\rm P}$ = virtual works of plastic moments, design permanent load and design gas load, respectively

 M_{1a} = absolute value of the negative unit elastic radial moment on the cap periphery

 M_{p_1}, M_{p_2} = positive unit plastic radial and annual moments, respectively

 M_{p_1a}, M_{p_2a} = absolute values of the negative unit plastic radial and annular moments in the slab periphery

p = gas load distribution on a unit area or on a unit length of a certain circle of the cap

 $P_{s'}p_1 =$ stand pipe and design loads respectively

$$(P_{\rm u} = \gamma_{\rm p} p_{\rm s})$$

 P_1 = total gas load corresponding to the attainment of the design yield point is only one point of the steel reinforcement

$$\gamma = \text{redistribution factor} = \frac{G + P_U}{G + P_1}$$

 γ_a = redistribution factor for $P_1 = P_s$

 $U_{10}, U_{20}, U_{1a} =$ coefficient of unit elastic moments produced by total permanent load

 $\gamma_{\rm S}, \gamma_{\rm P}$ = overload factor of permanent and gas loads, respectively

 $\eta = \text{elastic fixity of the cap periphery} = 0.5$ in this case

 $= M_{1a}/a$ bsolute value of unit elastic moment on the peiphery of a perfectly fixed ended slab

$$K_{\rm s} = rac{P_{\rm s}}{G}; \quad K_{\rm l} = rac{P_{\rm l}}{G}; \quad K_{\rm u} = rac{P_{u}}{G}; \quad \beta = b/a$$

 $\rho_1 g$ = radius corresponding to the circle defined by all the zero points of the diagram of the elastic moments produced by the permanent load, exclusively, assuming rigid fixity of the cap periphery

 $\rho_1 p$ = same as for $\rho_1 g$ except the load is gas load

 ρ_1 = approximate true radius of the circle defined by all zero points of the diagram of the elastic negative radial moments produced by the loads, assuming an elastic fixity of the slab periphery.

8.2.1.4 The General Plastic Equilibrium Equation for Reinforcement

Let θ be the virtual angular displacement of the plastic mechanism (Fig. 8.6). In this case the virtual work principle gives the following plastic equilibrium equation:

$$L_{\rm M} + L_{\rm G} + L_{\rm P} = 0 \tag{8.14}$$

The virtual work of the plastic moments acting along all the yield lines after rearranging becomes

$$L_{\rm M} = 2\pi [RMP_1 + aM_{p1a} + (a - R)M_{p2}]\theta = L_{\rm G} + L_{\rm P}$$
(8.15)

For obtaining a unique solution of the plastic moments MP_1 , M_{Pa} and M_{P2} satisfying the above equation, supplementary equations are necessary.

The criterion for solving the problem of the plastic design of two-way reinforced cap is the 'minimum redistribution criterion'. In the case of a fixed ended circular cap subjected to a symmetrical pressure load, the most stressed points are its centre and the unit elastic radial and annular moments are maxima. Let

$$M_{10} = U_{10}G + v_{10}P \tag{8.16}$$

$$M_{20} = U_{20}G + v_{20}P \tag{8.17}$$

$$M_{1a} = U_{1a}G + v_{1a}P \tag{8.18}$$

be the values of the unit elastic moments at these points. Taking into account both the definition of the plastic moment and the redistribution criterion

$$M_{10} = M_{p1}$$

 $M_{20} = M_{p1}$ and $p = p_1$
 $M_{1a} = M_{p1a}$

On the other hand, the elastic analysis of symmetrically loaded reinforced concrete cap shows

$$M_{10} = M_{20}$$
 (a)

Therefore

$$v_{10} = v_{20}$$
 (b)
 $u_{10} = v_{20}$ (c)

Hence

$$M_{p1} = M_{p2} \quad (d)$$

Therefore

$$2\pi a (M_{p2} + M_{p1a})\theta = L_{\rm G} + L_{\rm P}$$
(8.19)

The sum

$$L_{\rm G} + L_{\rm p} = \text{maximum if } \mathbf{R} = 0 \tag{8.20}$$

Hence the actual plastic mechanism of the cap subjected to symmetrical pressure loads

$$L_{\rm G} = 2\pi U_l G\theta \tag{8.21a}$$

$$L_{\rm P} = 2\pi v_l P_{\rm u} \theta \tag{8.21b}$$

From the above consideration, the maximum value of ρ_1 is

$$P_1 = \frac{(U_l - U_{20} - U_{1a})G + v_1 P_u}{v_{20} + v_{1a}}$$
(8.22)

Therefore,

 $\gamma =$ Expression for redistribution factor becomes

$$\frac{G+P_u}{G+P_1} = \frac{(v_{20}+v_{1a})(1+K_u)}{U_L - U_{20} - U_{1a} + v_{20} + v_{1a} + v_l K_u}$$
(8.23)

$$G = \pi a^2 g; \ L_G \frac{1}{3} a G \phi; \ U_e = \frac{1}{6\pi}$$
 (8.24)

$$P_{\rm v} = \pi \beta^2 a^2 p_u; \, v_e = \frac{3 - 2\beta}{6\pi} \tag{8.25}$$

$$u_{20} = \frac{19 - 2\eta}{96\pi}; \ v_{1a} = \frac{\eta}{8\pi}$$
(8.26)

$$v_{20} = \frac{24 - 5\beta^2 - 28\ln\beta - 12\eta(2 - \beta^2)}{96\pi}$$
(8.27)

$$v_{10} = \frac{\eta (2 - \beta^2)}{8\pi}$$
(8.28)

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8.2 Calculation 1

Final value for ' γ '

$$\gamma = \frac{\left(24 - 5\beta^2 - 28\ln\beta\right)(1 + K_{\rm u})}{21 - 5\beta^2 - 28\ln\beta + 16(3 - 2\beta)K_{\rm u}} \tag{8.29}$$

Taking the expression p_1 by using the general expression of the redistribution factor

$$p_1 = -\left(1 - \frac{1}{\gamma}\right)G + \frac{P_u}{\gamma} \tag{8.30}$$

$$M_{p1} = M_{p2} = \left[u_{20} - v_{20}\left(1 - \frac{1}{\gamma}\right)\right]G + \frac{v_{20}}{\gamma}P_u$$
(8.31)

$$M_{p1a} = \left[u_{1a} - v_{1a}\left(1 - \frac{1}{\gamma}\right)\right]G + \frac{v_{1a}}{\gamma}P_U$$
(8.32)

The above plastic moments become that the actual redistribution factor corresponding to the loads 'G' and 'P_U' are equal to γ_a . In this case a partial redistribution of internal forces takes place under the action of loads G and P_U and also $P_1 = P_s$

Therefore

$$M_{p1} = M_{p2} = u_{20}G + v_{20}P_{\rm s} \tag{8.33}$$

$$M_{P_{2a}} = u_{1a}G + v_{1a}P_s \tag{8.34}$$

Position of the Zero Points

$$P_1 = (1 - \eta)a + \eta \frac{\rho_1 g + K_1 \rho_{1p}}{1 + K_1}$$
(8.35)

(a) When $\gamma < \gamma_a$

$$K_1 = \frac{1+ku}{\gamma} - 1$$

(b) When $\gamma \geq \gamma_a$

$$K_1 = K_s$$

The absolute values of the negative radial moments decrease from the periphery to the centre of the cap. Obviously, the maximum absolute value of these moments corresponds to the cap periphery. For particular purposes it is first necessary to obtain the position of the zero point of the elastic negative radial moment. Subsequently, the fulfilment of the condition is obtained when radial steel reinforcement is placed along the length of the above-mentioned moment diagram so that the intensity of this reinforcement is the same at all points and equal to the corresponding radial plastic moment $M_{P_{2n}}$. It is clear that this is on the safe side.

Total effective dia =
$$(43' - 0) + 40' = 83' - 0$$
 (25.3 m)

Ignoring channel shutters approximate C.G of tendon from outside = 150'' (3.810 m)

effective
$$2a = 58' - 0$$
 and $a = 29' - 0 = 883.82$ cm
 $2b = 43' - 0$ and $b = 21' - 6'' = 655.32$ cm

 η = elastic fixity degree of the cap periphery = 0.5(worse condition)

Value of g_s

The value of g_s is the built-in stresses, i.e. construction stresses. They vary from 100 psi to a very negligible amount. These stresses are usually ignored. The amount of 10 psi (0.069 MN/m²) is taken for *a* circle of the cap.

$$g_{\rm s} = 0.703 \, {\rm kg/cm^2} = 10 \, {\rm Psi} \left(0.069 \, {\rm MN/m^2} \right)$$

 $p_{\rm s} = 45 \, {\rm kg/cm^2} = 644 \, {\rm Psi} \left(4.443 {\rm MN/m^2} \right)$

 $\gamma_8 = 1.0 - no overload factor$

 $\gamma_p = 1.15$ – overload factor for proof pressure

design value of $G_{\rm s} = \pi a^2 g_{\rm s} = 2.207(883.92)^2$

$$= 172 \times 10^{4} \text{kg} \left(15.627 \text{ MN/m}^{2} \right) = G$$

$$P_{s} = \pi b^{2} p_{s} = 6 \times 10^{7} \text{ kg} (545.13 \text{ MN})$$

$$P_{U} = \gamma_{p} P_{s} = 6.9 \times 10^{7} \text{ kg} (629.91 \text{ MN})$$

$$K_{s} = \frac{P_{s}}{G} = \frac{6 \times 10^{7}}{1.72 \times 10^{6}} = 39.4$$

$$K_{U} = \frac{P_{U}}{G} = \frac{6.9 \times 10^{7}}{1.72 \times 10^{6}} = 40.1$$

$$\gamma_{a} = \frac{1 + k_{u}}{1 + k_{s}} = \frac{41.1}{40.4} = 1.02$$

$$R = \frac{b}{100} = \frac{21.5}{1.5} = 0.741 (\text{from Fig. 8 6d})$$

$$\beta = \frac{\beta}{a} = \frac{21.5}{29} = 0.741$$
(from Fig. 8.6d)
 $\gamma > \gamma_{a}, \quad \gamma = 1.22$

8.2 Calculation 1

$$U_{20} = \frac{19 - 2\eta}{96\pi} = 0.0425$$

$$v_{1a} = \frac{\eta}{8\pi} = 0.0199$$

$$v_{20} = \frac{24 - 5\beta^2 - 28 \ln \beta - 12\eta (2 - \beta^2)}{96\pi}$$

= 0.04

$$v_{1a} = \frac{\eta (2 - \beta^2)}{8\pi} = 0.0289$$

For $\gamma > \gamma_a$

$$\begin{split} M_{p1} &= M_{p2} = \left[U_{20} - v_{20} \left(1 - \frac{1}{\gamma} \right) \right] G + \frac{v_{20}}{\gamma} \rho_u \\ &= \left[0.0425 - 0.04 \left(1 - \frac{1}{1.22} \right) \right] 1.72 \times 10^6 + \left[0.0328 \times 6.9 \times 10^7 \right] \\ &= 0.0072 \times 1.72 \times 10^6 + 0.22632 \times 10^7 \\ &= 0.12384 \times 10^5 + 0.22632 \times 10^7 \\ &= 2,275,584 \, \text{kg cm} \left(20.675 \, \text{MN cm} \right) \\ M_{p1a} &= \left[U_{1a} - v_{1a} \left(1 - \frac{1}{\gamma} \right) \right] G + \frac{v_{1a}}{\gamma} \rho_u \\ &= \left[0.0199 - 0.0289 \left(1 - \frac{1}{1.22} \right) \right] 1.72 \times 10^6 + \left[\frac{0.0199}{1.22} \times 6.9 \times 10^7 \right] \\ &= 0.01468 \times 1.72 \times 10^6 + 0.11247 \times 10^7 \\ &= 0.25250 \times 10^5 + 0.11247 \times 10^7 \\ &= 1,149,950 \, \text{kg cm} \left(10.448 \, \text{MN cm} \right) \\ f_c &= \frac{1}{3} \times 5400 = 1800 \, \text{psi} = 126.54 \, \text{kg cm}^2 \\ f_t &= \frac{1900 \, \text{kg}}{\text{cm}^2} ; \frac{f_t}{f_c} = \frac{1900}{126.54} = 15 = \gamma_1 \end{split}$$

$$\eta_{1} = \text{neutral axis factor} = \frac{m}{m + \gamma_{1}} = 0.5$$

$$a = 1 - \frac{\eta_{1}}{3} = 1 - \frac{0.5}{3} = 0.833$$

$$Q = \frac{1}{2} f_{c} \eta_{1} a = \frac{1}{2} \times 126.54 \times 0.5 \times 0.833 = 26.4$$

$$M = Qbd^{2} = 26.4 \times 1 \times (648.64)^{2}$$

$$= 26.4 \times 1 \times 42 \times 10^{4}$$

$$= 1108.8 \times 10^{4} \text{ kg cm}$$

$$11.088 \times 10^{6} \text{ kg cm}$$

$$> 2.275584 \times 10^{6} \text{ kg cm} (20.875 \text{MNcm})$$

Also > 1.149950×10^{6} kg cm (10.448MNcm) Thus at working load the bending stress is not very significant:

$$\alpha = 0.01 \times af_{t} = 16.112$$

$$\alpha d = 1.0368 \times 10^{4}$$

$$A_{t} = \frac{M(\text{kg m})}{\alpha d} = 2.19 \text{ cm}^{2}/m = 0.107 \text{ m}^{2}/\text{ft}$$

Less than minimum

Maximum tensile stress in the cap on outside surface taken from 'Dynamic Relaxation Program' closed to edge = 339 psi with corresponding compression stress of 131 psi. Therefore combinated of these with 'Design Pressure' shall give the required minimum reinforcement in top and bottom caps

$$f_{s} = 131; \frac{f_{t}}{m} = 339; f_{t} = 5085$$

$$\eta_{1} = 0.315; l_{a} = 0.895$$

$$Q = \frac{1}{2}(131)(0.315)(0.895) = 18.5$$

$$Qbd^{2} = 18.5 \times 12 \times (210)^{2} = (222)(44, 100)$$

$$\alpha = l_{a}f_{t} = 4560$$

$$A_{s} = \frac{222 \times 44, 100}{4560 \times 210} = 1.06 \text{ in.}^{2}/\text{ft}$$

Since the steel owing to proof pressure is negligible, the following amount of steel by direct ratio of proof pressure and design pressure will be close to reality:

$$A_{\rm t} = 0.0965 \,\text{in}^2/\text{ft}$$
$$A_{\rm T} = \text{total steel} = 1.1565$$

Area based on 16.3" c/c (415 mm c/c) spacings

No. bars $= \frac{16.3}{12} \times 1.565 \times \frac{1}{1.227} = \frac{1.57}{1.227} = 1.28$ bars

Minimum steel

2 no.1 $\frac{1''}{4}Q$ bars (2 - 30 mm HTS) <5 no.1 $\frac{1''}{4}Q$ bars (5 - 30 mm HTS) Based on 600 psi (tension).

Note: Check this for ultimate load by combining ultimate pressure and hoop prestressing.

8.2.1.5 Cap Reinforcement at Ultimate Load with Penetration

Yield Line at Edge of Standpipe Area

Refer to Fig. 8.7 Approx. no. of standpipes crossing a radius=9 O.D of standpipes = 12" (300 mm)

(1/2'' thickness)

Ligament $1\frac{1''}{2}$ and spacing c/c of stand pipes = 16.3'' (415 mm)

replacing 12" concete by1 steel compensation $=\frac{1\times35,000}{12\times4000}$ = 0.73 take 0.5 for safety reasons equivalant concrete on radius = $186 - \frac{1}{2} \times 9 \times 12 = 132$ Let *m* be the resisting moment/inch around circumference

Area $= \frac{1}{2} \times 186 \times 145.8 = 13,600$

Total gas pressure $= 13,600 pF_s$

For gas cooled reactor p = pressure 644 psi, $F_s =$ safety factor 3 for cap

external work = 13,600 pF_s $\frac{\Delta}{3}$

internal work = $\frac{145.8}{186}m\Delta$

Thus equating work

 $m = 11.1 \times 10^6$ Ib in./in.

Average pressure over top $9' - 0 \operatorname{cap} = 966 \operatorname{psi} (5.665 \operatorname{MN/m}^2)$ (based on 77 t/in.²). Similarly for containment $p = 50 \operatorname{psi}$. similar calculations are carried out.

Average pressure over bottom 9' - 0 cap = 722 psi (4.2341 MN/m^2)

$$d = 118''$$

$$l_{a} = 118 - \frac{d_{1}}{2}$$

$$f_{c} d_{1} l_{a} = 11.1 \times 10^{6}$$
Concrete stress 4000 × $\frac{132}{186} = 2800$ psi $\frac{1}{d_{c}}$

$$2800d_{1} \left(118 - \frac{d_{1}}{2}\right) = 11.1 \times 10^{6}$$

Therefore

$$d_1 = 39.75''$$

Lever arm for P_1 is $l_{a1} = (216 - 19.875 + 21) = 175.125''$

 $M_1 = 966(108 - 21) \times 175.125 = 14.72 \times 10^6$ (lbin)

Lever arm for P_2 is $l_{a2} = 108 - 19.875 = 88.125''$

$$M_2 = 772 \times 108 \times 88.125 = 7.44 \times 10^6$$
 (lbin)

$$M_1 + M_2 = 25.16 \times 10^6 > 11.1 \times 10^6$$

No reinforcement is required in this area. Yield Line at the Inside of Barrel Wall

> equivalent area = $258 - \frac{1}{2} \times 9 \times 12 = 204$ in² area of the element = $\frac{1}{2} \times 258 \times 203 = 26187$ in².

Similarly equating external and internal works

$$26187pF_{\rm s}\frac{\Delta}{3} = \frac{203}{258}m\Delta$$

 $m = 11,100; \ pF_{\rm s} = 11,100 \times 1932 = 21.4452 \times 10^{6} \, {\rm lbin/in.}$
 $d = 118'', \text{ concrete stress} = 205/258 \times 4000 = 3180 \, {\rm psi}$

8.2 Calculation 1

Similarly

$$3180d_1\left(118 - \frac{d_1}{2}\right) = 21.4452 \times 10^6$$

$$d_1 = 97.39''$$

$$M_1 = \frac{146.31}{175.125} \times 14.72 \times 10^6 = 12.3 \times 10^6 \text{ lbin/in.}$$

$$M_2 = \frac{108 - 48.698}{88.125} \times 7.44 \times 10^6 = 5 \times 10^6 \text{ lbin/in.}$$

$$M_1 + M_2 = 17.3 \times 10^6 < 21.4452 \times 10^6 \text{ lbin/in.}$$

Bonded reinforcement is required.

Assume bonded reinforcement on top and bottom faces

External work =
$$8729 \times 1932\Delta = 16.85 \times 10^{6}\Delta$$

Internal work = $0.786m\Delta + 2 \times 0.786m'\Delta$
m due to prestress = 17.3×10^{6} psi

(assuming load can be transferred to ring beam – cracked but not separated)

$$16.85 \times 10^6 = 0.786 \times 17.3 \times 10^6 + 1.572m'$$

Therefore $m' = 20.6 \times 10^6$

$$A_{\rm st} = \frac{20.6 \times 10^6}{\left(210 - \frac{97.39}{2}\right) \times 6000} = 0.213 \text{ in.}^2/\text{in.}$$

total no bars = $\frac{2.56}{1.227} \approx 2$

In standpipe area from this total effect

$$= \frac{16.3}{12} \times 2.556 = 3.47 \text{ in.}^2 \text{ or } 2.84 \text{ bars}$$

say 3 - 1 $\frac{1''}{4}$ \phi bars G. K. 60 + (minimum requirement)

Elsewhere in the cap -2 no. $1\frac{1}{4}$ \phibars G.K. 60+placed at 12''c/c (305 mm c/c) Same as before.

Note: Area of steel in particular zones should be increased if spacings required are more than 12° c/c or of varied nature.

8.2.1.6 Shear and Principal Stresses in Cap at Ultimate Load

Data

SF = shear force at the hinge

$$H = \text{cap thickness} = 216''$$

 $A = \text{area of concrete } t_c = \frac{\theta}{\pi} \left[\pi R_E^2 - \pi R I^2 - \pi R D^2 \right] = 26841 \text{ in.}^2$

Where

$$\theta = \text{ half symmetrical angle}$$
 (8.36)

RE, RI = external and internal radii
$$D$$
 = boiler diameter

$$n_{\phi} = \frac{\text{radial force on the element of cap}}{(2R_{\rm E} - DP)\sin\theta}$$
 (8.37)

 t_{ϕ} = yield force of cap reinforcement per inch ACT × FYS (8.38)

$$\tau_{b} = \text{shear stress in the barrel} = \frac{SF}{A}$$

$$\tau_{xy} = \text{nominal shear at } \theta_{1} - \theta_{1} \text{ edge plane}$$

$$= \frac{P \times 2\pi R I^{2}}{H \times 2\pi R_{I}} = \frac{RI}{2H}P = 0.597P \text{ psi}$$

$$\sigma_{x} = \text{nominal compression} = \frac{n_{\phi} + t_{\phi}}{H}$$

$$\sigma = \text{principal stresses (psi)}$$

(8.40)

The following table shows various values at $\theta_1 - \theta_1$ of shear and principal stress derived based on data available from ultimate load program IBM140:

AT Plane $\theta_1 - \theta_1$

| EEH | $\rho_{\rm cap}$ | ρ_{barrel} | SF at X | τ | n_{ϕ} | t_{Φ} | σ_x |
|----------|------------------|--------------------------|----------------------|--|---|------------|-------------------------------------|
| 0.016 | 1885 | 1610 | -1,374,839 | -21 | 138,394 | 76,663 | 996 psi 6.8724 MN/m ² |
| | | | | | | | |
| | | τ_{xy} | $\frac{\sigma_x}{2}$ | $\sqrt{\left(\frac{\sigma}{2}\right)}$ | $\left(\frac{x}{2}\right)^2 \left(\tau_{xy}\right)^2$ | σ_1 | σ_2 |
| psi | | 961 | 498 | ± 10 | 82 | +153 | 0 -534 |
| MN/m^2 | | 6.631 | 3.436 | ±7.4 | 66 | 10.56 | -3.685 |

At plane $\theta_2 - \theta_2$

$$z = R + H \cot \theta$$
$$Z - R$$

where
$$\cot\theta = \frac{Z - R}{H}$$
 (8.41)

$$\tan 2\theta = \frac{2\tan\theta}{1-\tan^2\theta} = \frac{2H(Z-R)}{(Z-R)^2 - H^2}$$
$$\alpha = \theta \tan 2\alpha = \frac{2\tau}{\sigma} = \frac{PR}{2H} = \frac{PR}{n_{\phi}}$$
$$\frac{2H(Z-R)}{(Z-R)^2 - H^2} = \frac{P_sR}{n_{\phi}}$$
(8.42)

Rearranging, the cubic equation becomes

$$PR^{3} - 2\rho ZR^{2} + R[\rho(Z^{2} - H^{2}) + 2Hn_{\phi}] - 2HZn_{\phi} = 0$$

Taking random value from computer program

$$H = 216; Z = 250.5; n_{\phi} - 163,676.96$$
$$P = -1885.5532$$

The cubic equation reduces to

$$R^3 - 501R^2 - 2.14 \times 10^4 R + 0.84 \times 10^7 = 0$$

Transforming into the form

$$x^{3} - px \pm q = 0$$

Putting $x = y - \frac{b}{3a} = y - 167$

cubic equation becomes

$$y^3 - y(10.5 \times 10^4) - 34.9 \times 10^4 = 0$$

The only applicable root + $\sqrt{(4p/3)}\cos(\theta + 240^\circ)$ where $\cos 3\theta = \sqrt{27q^2/4p^2}$

when
$$4p^3 > 27q^2$$

 $4p^3 = +4630.5 \times 10^{12}$
 $27q^2 = +32,886 \times 10^8$
 $\cos 3\theta \approx o$
 $\theta \approx 30^\circ$
 $R = 167 +$

$$\tan \alpha = \frac{216}{83.5} = 2.584, \ \alpha \approx 60^{\circ}$$
$$\sigma_x = 845$$
$$F = \frac{845}{2} \pm \frac{1}{2} \sqrt{(845)^2 + 4(730)^2} = 422.5 \pm 55.75$$
$$F_1 = +980 \text{ psi}$$
$$F_2 = -135 \text{ psi not critical}$$

The vale of θ as 60° is established from computer program and lab tests. *Ratios, Coefficients*

$$\mu = \frac{A_{\rm s}}{bd} (\text{bending}); \frac{A_{\rm S}}{A_{\rm b}} (\text{tension})$$

m = modular ratio

$$v = \frac{p}{ACT}$$

$$K_{\rm B}, K_{\rm R}, K_{\rm W} = {\rm coefficients}$$

 α_s , α_c = coefficient of thermal expansion of steel and concrete respectively

$$K_1, C_1, C_2, C_3 = \text{coefficients}$$

 $a = \sqrt{\frac{A_b}{n}}$
 $\lambda = \frac{a}{\phi}$

8.2.1.7 Bending Area (Circular)

- (a) Two consecutive cracks and a section in between having a constant bending moment
- (b) At each crack where $t_c = 0$ the maximum stress is attained in the reinforcement and its magnitude is

$$f_{\rm SF} = \frac{M}{A_{\rm s}J} \tag{8.43}$$

8.2 Calculation 1

Moving away from cracks, the bond between concrete and steel is brought into play; the reinforcement transfers an increasing proportion of the total tensile force to the concrete. The maximum stress in concrete is reached at $x = \frac{L}{2}$ and cracking takes place if this value $t_c = t_{ca}$. Thus two extreme values are achieved for the distance between the cracks

$$t_{\rm c} < t_{\rm ca} - L$$
 maximum distance

$$t_{\rm c} = t_{\rm ca}$$
 at $\frac{L}{2}$ maximum distance $x = \frac{L}{2}$
Average mean spacing $L_{\rm a} = 0.75L$ (8.44)

At Section 8.2.1.10, total tensile force is carried by partly:

- (a) Reinforcement $f_s A_s$
- (b) Bond between steel and concrete is

$$p\int_0^x f_{\rm b}\left(F\left(\frac{x}{L}\right)\right)dx$$

where

$$f_{\rm bx} = f_{\rm b} F \left(\frac{x}{L}\right) \tag{8.45}$$

Denoting the distribution bond stress along distance between cracks as shown in Fig. 10.10

$$f_{\rm SF}A_{\rm s} = f_{\rm s}A_{\rm s}p \int_0^x f_{\rm b}F\left(\frac{x}{l}\right)dx \tag{8.45a}$$

or

$$f_{\rm s} = f_{\rm SF} - \frac{p}{A_{\rm s}} \int_0^x F\left(\frac{x}{l}\right) dx \tag{8.45b}$$

For constant moment domain

$$M_{\rm A} = M_{\rm B} = f_{\rm SF}A_{\rm s}y = M_{\rm x} = f_{\rm s}A_{\rm s}J + t_{\rm c}z_{\rm c}$$

Together with Eq. (8.45b)

$$t_{\rm c} = \frac{pf_{\rm b}J}{z_{\rm c}} \int_0^x F\left(\frac{x}{l}\right) dx \tag{8.45c}$$

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$$t_{\rm ca} = \frac{pf_{\rm b}JL}{z_{\rm c}} \int_0^{\frac{1}{2}} F\left(\frac{x}{l}\right) d\left(\frac{x}{l}\right)$$
(8.45d)

$$L = \frac{1}{\int_0^{\frac{1}{2}} F\left(\frac{x}{l}\right) d\left(\frac{x}{l}\right)} \frac{1}{p} \frac{z_c}{J} \frac{t_{ca}}{f_b}$$
(8.45e)

$$=C_1 \frac{1}{p} \frac{z_c}{J} \frac{t_{ca}}{f_b}$$
(8.45f)

where

$$\frac{1}{C_1} = \int_0^{1/2} F\left(\frac{x}{l}\right) d\left(\frac{x}{l}\right)$$
(8.45g)

Referring to the assumption regarding the functions F(x/l) shown in Fig. 8.10

at $x = 0.5L t_{c} = t_{ca}$

$$C_{1} = 2 \text{ for } F\left(\frac{x}{l}\right) = 1 \text{ in Brice theory} C_{1} = \pi \text{ for } F\left(\frac{x}{l}\right) = 1 \text{ in Saligers theory} C_{1} = 4 \text{ for } F\left(\frac{x}{l}\right) = 1 \text{ in Wastlund theory}$$

$$\left. \left. \right\}$$

$$(8.45h)$$

Crack Width

Width of cracks denotes elongation in net value between steel and concrete, i.e. the total slip between them, or

$$w = 2 \int_0^{L/2} s dx$$
 (8.46a)

where $s = (e_s - e_c)$ per unit length

$$=\frac{f_{\rm s}}{E_{\rm s}} - \left(\frac{t_{\rm c}}{E_{\rm s}} - e_{\rm sh}\right) \pm T(\alpha_{\rm s} - \alpha_{\rm c}) \tag{8.46b}$$

taking into consideration the influences of shrinkage and temperature variation of $\pm T$. Introducing the modular m

$$s = \frac{f_{\rm s} - mtc}{E_{\rm s}} + e_{\rm sh} \pm T(\alpha_{\rm s} - \alpha_{\rm c})$$
(8.46c)

8.2 Calculation 1

Using Eq. (8.46a)

$$w = 2 \int_0^{L/2} \frac{1}{E} (f_{\rm s} - mtc) dx + 2 \int_0^{L/2} \{e_{\rm sh} \pm T(\alpha_{\rm s} - \alpha_{\rm c})\} dx \qquad (8.46d)$$

Substituting for f_s and t_c from Eqs. (8.45b) and (8.45c) respectively, and after rearranging terms:

$$w = \frac{2}{E_{\rm s}} \int_0^{L/2} \left[f_{\rm SF} - 2 \frac{pL f_{\rm b} J}{z_{\rm c}} \left\{ m + \frac{z_{\rm c}}{JA_{\rm s}} \right\} \int_0^x F\left(\frac{x}{l}\right) dx \right] dx$$

$$+ L \{ e_{\rm sh} \pm T(\alpha_{\rm s} - \alpha_{\rm c}) \}$$
(8.47)

$$= \frac{L}{E_{\rm s}} \left[f_{\rm SF} - 2 \frac{p L f_{\rm b} J}{z_{\rm c}} \left(m + \frac{z_{\rm c}}{J A_{\rm s}} \right) \int \int_{0}^{1/2} F\left(\frac{x}{L}\right) d\left(\frac{x}{L}\right) d\left(\frac{x}{L}\right) \right]$$

$$+ L \{ e_{\rm sh} \pm T(\alpha_{\rm s} - \alpha_{\rm c}) \}$$
(8.48)

With the aid of Eqs. (8.45d) and (8.45)

$$w = \frac{L}{E_{\rm s}} \left[f_{\rm SF} - t_{\rm ca} \left(m + \frac{z_{\rm c}}{JA_{\rm s}} \right) 2C_1 \int \int_0^{1/2} F\left(\frac{x}{L}\right) d\left(\frac{x}{L}\right) d\left(\frac{x}{L}\right) \right]$$

$$+ L \{ e_{\rm sh} \pm T(\alpha_{\rm s} - \alpha_{\rm c}) \}$$
(8.49)

or more compactly

$$w = \frac{L}{E_{\rm s}} \left[f_{\rm SF} - C_2 t_{\rm ca} \left(m + \frac{z_{\rm c}}{JA_{\rm s}} \right) \right] + L \{ e_{\rm sh} \pm T(\alpha_{\rm s} - \alpha_{\rm c}) \}$$
(8.50)

where

$$C_2 = 2C_1 \int_0^{1/2} \int_0^{1/2} F\left(\frac{x}{L}\right) d\left(\frac{x}{L}\right) d\left(\frac{x}{L}\right)$$
(8.51)

For bond distribution shown in Fig. 8.10

$$C_{2} = \frac{1}{2} \text{ in Brice theory}
C_{2} = \frac{1}{2} \text{ in Saligers theory}
C_{2} = \frac{1}{3} \text{ in Wastlund theory}$$

$$(8.52)$$

Neglecting the elastic deformation in concrete (i.e. m=0) and the shrinkage and temperature effects

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$$w = \frac{L}{E_{\rm s}} \left[f_{\rm SF} - C_2 t_{\rm ca} \left(m + \frac{z_{\rm c}}{JA_{\rm s}} \right) \right] \tag{8.53}$$

where L is given by Eqs. (8.45e) and (8.45f).

Direct Tension Area

These equations are taken by Watstien and Parsons. In Fig. 8.9a the embedment area Ab = abcd = 2d'b when under direct tension having a large depth *D*, consisting of two flanges each of area Ab = 2d'b as shown in Fig. 8.9c:

$$z_{\rm c} = 2Ab \frac{D^2}{4} \frac{2}{D} = A_b D \tag{8.54a}$$

$$J = Ab\frac{D^2}{2} \left/ A_b \frac{D}{2} = D \right.$$
(8.54b)

or

$$f_{\rm c} = JA_b \tag{8.54c}$$

Substituting these values in Eqs.(8.45c), (8.45d), (8.45e) and (8.45f) and expressing

$$\frac{A_{\rm s}}{A_{\rm b}} = \mu \text{ and } \frac{p}{A_{\rm s}} = \frac{4}{\Phi}$$

$$t_{\rm c} = \frac{pf_{\rm b}J}{z_{\rm c}} \int_{0}^{x} F\left(\frac{x}{l}\right) dx = p \frac{f_{\rm b}}{A_{\rm b}} \int_{0}^{x} F\left(\frac{x}{l}\right) d\left(\frac{x}{L}\right) \tag{8.55}$$

$$t_{\rm ca} = \frac{pf_{\rm b}JL}{z_{\rm c}} \int_{0}^{1/2} F\left(\frac{x}{l}\right) d\left(\frac{x}{L}\right) = \frac{p}{A_{\rm s}} \frac{A_{\rm s}}{A_{\rm b}} f_{\rm b} L \int_{0}^{1/2} F\left(\frac{x}{l}\right) d\left(\frac{x}{L}\right) \tag{8.56}$$

$$l = 4 \frac{\mu}{\Phi} f_{\rm b} \int_{0}^{1/2} F\left(\frac{x}{l}\right) d\left(\frac{x}{L}\right) \tag{8.56}$$

$$L = C_{1} \frac{1}{p} \frac{Z_{\rm c}}{J} \frac{t_{\rm ca}}{f_{\rm b}} = C_{1} \frac{1}{p} \frac{A_{\rm s}}{A_{\rm s}} A_{b} \frac{t_{\rm ca}}{f_{\rm b}} \tag{8.57}$$

$$= \frac{C_{1}}{4} \frac{\phi}{\mu} \frac{t_{\rm ca}}{f_{\rm b}} = C_{3} \frac{\phi}{\mu} \frac{t_{\rm ca}}{f_{\rm b}}$$

in which

$$C_3 = \frac{C_1}{4}$$
 (8.57a)

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In a similar manner Eq. (8.50) transforms into

$$W = \frac{L}{E_{\rm s}} \left[f_{\rm SF} - C_2 t_{\rm ca} \left(m + \frac{1}{\mu} \right) \right] + L \{ e_{\rm sh} \pm T(\alpha_{\rm s} - \alpha_c) \}$$
(8.58)

The similar expression comparable to Eq. (8.58) is

$$w = \frac{L}{E_{\rm s}} f_{\rm SF} - C_2 \frac{t_{\rm ca}}{\mu}$$
(8.59)

For practical reasons, a considerable amount of simplification is achieved by neglecting the term $C_2 \frac{l_{ca}}{\mu}$ in Eq. (8.59). The assumption is on the same side:

$$w = L \frac{f_{\rm sp}}{E_{\rm s}} = C_3 \frac{f_{\rm SF}}{E_{\rm s}} \frac{t_{\rm ca}}{f_{\rm b}} \frac{\Phi}{\mu}$$
(8.60a)

[It seems that the limitation of stresses f_{sf} and t_{ca} may sometimes be necessary to restrict the width of cracking. Reduction in crack.]

Width is also based on f_b which in turn is dependent on bar surface. GK 60 is more effective in this respect.

Writing in different ways

$$w = c \frac{t_{\rm ca}}{f_{\rm b}} \frac{\Phi}{\mu} f_{\rm SF} \tag{8.61a}$$

Equation (8.53a) can be written as

$$w = A \frac{\Phi}{\mu} f_{\rm SF} \tag{8.61b}$$

where

$$A = C_3 \frac{t_{\rm ca}}{E_{\rm s} f_{\rm b}}$$

The following are various theories taking into consideration various formulae for f_b or f_{bx}

8.2.1.8 Brice Theory

Bond between steel and concrete is essentially a frictional force and the elastic plastic strains in concrete are negligible compared to those in reinforcement. This force is uniform:

$$f_{\rm bx} = f_{\rm b} = \frac{2 \, KB}{1 + 3 \frac{l_{\rm s}}{l_{\rm c}}} \tag{8.62a}$$

KB for GK 60 = 1.6

 l_s , l_c = the sum of bar diameters and the sum of thickness of concrete traversed by a line of possible cracking whose last two non-coincident sides are normal to the face of concrete.

The line of possible cracking should be so chosen that it encounters the largest number of bars and minimum of concrete, i.e l_s/l_c is as large as possible. In Fig. 8.9b the contour of cracking may be abcde or abfg or gfhi.

When the bars are fairly uniformly distributed over the embedment area. Brice suggests that the area Ab may be assumed to be made up of as many square areas as the number of bars with the bar embedded in the centre of each of these elemental areas.

In such a case

$$a^{2} = \frac{Ab}{n}$$

$$l = n\phi$$

$$l = na - n\phi$$

$$\lambda = \frac{a}{\phi}$$
(8.63)

Therefore

$$1 + 3\frac{l_{\rm s}}{l_{\rm c}} = 1 + \frac{3p}{a - \phi} = \frac{\lambda + 2}{\lambda - 1}$$

Expression (8.47a) reduces to

$$f_{bx} = f_b = 2KBt_{ca}\frac{\lambda - 1}{\lambda + 2}$$
i.e. $F(x/L) = 1; C_1 = 2.0; C_2 = \frac{1}{2}$ and $C_3 = \frac{1}{2}$
(8.63a)

As given earlier by Eqs. (8.61b), (8.52) and (8.50) substitution of C_1 , C_2 and C_3 in the appropriate expression of the above general theory gives results in Table 8.2.

Theoretically, flexural cracks will not occur so long as the applied moment $M < M_c$ but accidental cracks can nevertheless take place. Brice assumes that in the circumstance the bars behave as if they were fixed in concrete on either side of the crack and proposes a simple formula for limiting the stresses in steel in relation to the width of cracks.

The variation of f_s in this theory is shown in Fig. 8.9a from which the average stress in steel f_{sa} can be computed as:
8.2 Calculation 1

$$f_{\rm sa} = f_{\rm SF} - \frac{p}{4A_{\rm s}}Lf_{\rm b} = f_{\rm SF} - \frac{f_{\rm b}L}{\phi}$$
 (8.63b)

Therefore, the crack width on $L_a(0.75L)$ is

$$w_{\rm a} = \frac{0.75L}{E_{\rm s}} (f_{\rm SF} - 0.75 \frac{L}{\Phi} f_{\rm b})$$
 (8.63c)

Substituting *L* from Eq. (8.8b)

$$w_{\rm a} = \frac{0.75L}{E_{\rm s}} \left(f_{\rm SF} - 0.75 \frac{L}{\phi} f_{\rm b} \right)$$
 (8.63d)

reduces to

$$0.75 \frac{L}{\phi} f_{\rm b} = 0.75 C_1 \frac{1}{p} \frac{z_{\rm c}}{J} t_{\rm ca}$$
(8.63e)

 $0.75 \frac{L}{\Phi} f_{\rm b} = 0.75 C_1 \frac{1}{p}$ With $c = 2, \frac{A_s}{p} = \frac{\Phi}{4}; M_{\rm c} = t_{\rm ca} z_{\rm c}; M_{\rm f} = f_{\rm SF} A_{\rm s} J$ Therefore

$$0.75\frac{L}{\Phi}f_{\rm b} = 0.75 \times 2 \times \frac{r}{p\Phi}\frac{A_{\rm s}f_{\rm SF}z_{\rm c}}{A_{\rm s}f_{\rm SF}J}t_{\rm ca} = \frac{3}{8}f_{\rm SF}\frac{M_{\rm c}}{M_{\rm f}}$$
(8.63f)

and

$$0.75L = \frac{\Phi}{f_{\rm b}} f_{\rm SF} \left\{ \frac{3}{8} \frac{M_{\rm c}}{M_{\rm f}} \right\}$$

| | e | 5 |
|----------------|---|---|
| | General theory | |
| Quantity | Flexure $C_1 = 2; C_2 = 0.5$ | Tension $C_2 = 0.5; C_3 = 0.5$ |
| $f_{\rm bx}$ | | $f_{\rm bx} = f_{\rm b} = 2KBt_{\rm ca} \frac{1}{1+3\frac{\hbar}{2}} = 2KBt_{\rm ca} \frac{\lambda-1}{\lambda+2}$ |
| t _c | $\frac{pf_{\rm b}Jx}{Z_{\rm c}}$ | $\frac{pf_{\rm bx}}{Ab} = \frac{4\mu}{\phi} f_{\rm bx}$ |
| fs | $f_{\rm SF} - \frac{p}{A_s} f_{\rm bx} = f_{\rm SF} = \frac{4\mu}{\Phi} f_{\rm bx} \text{ from } 0 - \frac{1}{2}$ $f_{\rm SF} - \frac{p}{A_s} f_{\rm bx} = f_{\rm SF} = \frac{4\mu}{\Phi} f_{\rm bx} \text{ from } 0 - L$ | |
| L | $\frac{\phi}{4KB}\frac{z_c}{J}\left(1+3\frac{l_s}{l_c}\right)$ | $\frac{\Phi}{4KB}\frac{1}{\mu}\left(1+3\frac{l_s}{l_c}\right)$ |
| W | $L/E_s \left\{ f_{\rm SF} - \frac{t_{\rm ca}}{2} \frac{z_{\rm c}}{JA_{\rm s}} \right\}$ | $L/E_s \left\{ f_{\rm SF} - \frac{t_{\rm ca}}{2\mu} \right\}$ |
| | Simplified solution | n |
| f_{bx} | As above | |
| W | $\frac{1}{2}\frac{\Phi}{\mu}\frac{f_{\rm sc}}{f_{\rm b}}\frac{f_{\rm sF}}{E_{\rm s}} = \frac{\Phi}{4\mu}\frac{1}{KB}\frac{\lambda+2}{\lambda-1}\frac{f_{\rm sF}}{E_{\rm s}}$ | |

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$$E_{\rm s}W_{\rm a} = \frac{\Phi}{f_{\rm b}}f_{\rm SF}^2 \left[\left\{ \frac{3}{8}\frac{M_{\rm c}}{M_{\rm f}} \right\} \left\{ 1 - \frac{3}{8}\frac{M_{\rm c}}{M_{\rm f}} \right\} \right] = \frac{\Phi}{f_{\rm b}}f_{\rm SF}^2 P \qquad (8.64a)$$

in which

$$P = \frac{3}{8} \frac{M_{\rm c}}{M_{\rm f}} \left(1 - \frac{M_{\rm c}}{M_{\rm f}} \right) \tag{8.65}$$

When $w_a = 0$ there will be no cracking when either $M_c = 0$, i.e. $t_{ca} = 0$ or $1 - \frac{3}{8} \frac{M_c}{M_f} = 0$

i.e.
$$M_{\rm c} = 2.67 M_{\rm f}$$
 (8.65a)

Since $t_{ca} > 0M_c = 2.67M_f$ can be attained if reinforcement is provided.

On the other hand w_a attains the maximum magnitude when p is the largest which is easily determined. Thus putting

$$\frac{3}{8} \frac{M_{\rm c}}{M_{\rm f}} = y$$

$$P = Y(1 - Y) = Y - Y^2$$
(8.66)

8.2.1.9 Summary of Crack Distribution Theories

Notation

(A) Stresses

 $t_{\rm c}$ =tensile stress in concrete at any section

 t_{ca} =tensile strength of concrete

 f_{su}, f_{pr} =crushing strength of cubes and prisms, respectively

 $f_{\rm s}$ =tensile stress in steel at any section

 $f_{\rm sp}$ =tensile stress in steel across a crack

 $f_{\rm b}$ =maximum value of bond stress between concrete and steel

 $f_{\rm ba}$ =average bond stress

 f_{bx} =bond stress at any section at a distance X from a crack

 $E_{\rm s}$ =modulus of elasticity of steel

(B) Strains

 $e_{\rm c}e_{\rm s}$ =strain in concrete and steel, respectively

 $e_{\rm sh} = {\rm shrinkage of concrete/unit length}$

s = slip of steel per unit length

(C) Dimensions and section properties

b =width of tension zone

d, h =effective and overall depth, respectively, in a section

d' =cover to the centre of tensile reinforcement d = h - d'

 $z_{\rm c}$ =sectional modulus of concrete section

J = lever armAb =embedment area of concrete $A_{\rm ct}$ = area of concrete in tension zone $A_{\rm d}$ =area of tension reinforcement in one direction per foot length (width) $A_{\rm t}$ =active stretched area of concrete = 12 (2 d' + Q) ϕ =diameter of reinforcing bar $A_{\rm s}$ = area of reinforcement = $\frac{n\pi\phi^2}{4}$ for 'n' bars *p* =perimeter of reinforcing bars = $n\pi\phi$ for '*n*' bars $l_{\rm s}, l_{\rm c} =$ explained L =maximum distance between cracks L_a =average (mean) distance between cracks w = maximum width of cracks w_a =average width of cracks T =temperature S = spacing of bars (D) Moments M = moment

 $M_{\rm f}$ =moment at a crack

 $M_{\rm c}$ =moment of resistance of concrete above $t_{\rm ca}z_{\rm c}$

Setting dp/dy = 0

$$T - \frac{1}{2} \cdot P = 0.25$$

Then

$$E_{\rm s}w_{\rm a} = \frac{\Phi f_{\rm SF}^2}{4f_{\rm b}} \tag{8.67}$$

Limiting value for stress in steel is given by

$$f_{\rm SF}^2 \le 4 \frac{E_{\rm s} w_{\rm a} f_{\rm b}}{\Phi}$$
$$\le 8 E_{\rm s} \frac{\lambda - 1}{\lambda + 2} K_{\rm S} \frac{w_{\rm a}}{\Phi} t_{\rm ca}$$

8.2.1.10 Saliger's Theory

In this theory the bond stress distribution in the form of sine curve (Fig. 8.10) is defined by

$$f_{\rm bx} = f_{\rm b} \sin \frac{2\pi x}{L} \tag{8.68}$$

Saliger takes into consideration elastic strain in concrete and uses the following value for stresses and modular ratio

$$t_{ca} - \frac{f_{pr}}{4.4} \text{ kg/cm}^2 \text{ flexure } E_s = 29,000 \text{ kg/cm}^2$$
$$t_{ca} - \frac{f_{pr}}{12} \text{ kg/cm}^2 \text{ tension } m = 8.8 \text{ flexure}$$
$$\frac{f_{pr}}{3} to \frac{f_{pr}}{4} \text{ for deformed bars } m = 24 \text{ tension}$$

with $C_3 = \frac{\pi}{4}$ as given by Eq (8.9b).

Then from Eq. (8.44a)

$$w = \frac{\pi f_{SF} t_{ca} \Phi}{4 E_s f_b \mu}$$
(8.69)

8.2.1.11 Rüsh's Theory

In this theory the crack width is expressed as

$$w = \frac{K_{\rm R}}{v} f_{\rm SF} \tag{8.70a}$$

$K_{\rm R}$ – coefficient

The value of w is easily transformed to the general form of Eq. (8.44b) by relating v to u

$$v = \frac{p}{A_{\rm ct}} = \frac{p}{A_{\rm ct}} \frac{A_{\rm s}}{A_{\rm s}} \frac{A_{\rm b}}{A_{\rm s}}$$
$$= \frac{4\mu}{\Phi} \frac{A_{\rm b}}{A_{\rm ct}}$$

v=0 percent age bond between concrete and steel denoted by the ratio of the bond area to the area in the tension zone abcd in Fig. 8.9d i.e.

$$v = \frac{p}{A_{\rm ct}}$$

and

$$w = \frac{K_{\rm R}}{4} \frac{A_{\rm o}}{A_{\rm ct}} \frac{\Phi}{\mu} f_{\rm SF} = \frac{K_{\rm R}}{2} \frac{\Phi}{\mu} f_{\rm SF}$$
(8.70b)

 $K_{\rm R} = 0.10 - 0.14 \times 10^{-6}$ for the type similar to GK 60

8.2.1.12 Efsen and Krenchel Theory

 $A_{\rm b} = {\rm gross}$ area of concrete

Net area = $(A_b = n\frac{\pi}{4}b^2) = AN$

Part of the load transferred to the concrete by bond stress $= \pi \phi A_t = AN(f_s) = A_b f_s$

 $f_{\rm b}$ maximum bond stress

$$A_{b} = Cf_{b}\frac{L}{2}$$

$$f_{m} = \frac{1}{2}\pi\phi = A_{b}f_{SF}$$

$$L = \frac{2Eb}{\pi\phi} \times \frac{f_{SF}}{f_{m}} = 2\beta \frac{f_{SF}}{f_{m}}$$
(8.70c)

W from this work was found out by Henshuholt to be 0.05 mm for total elongation of 120 cm prism.

Ratio between mean values w_m/L_a is independent of bar type and of the concrete cross-section and practically only dependent on the reinforcing bar stress

 $\frac{w_{\rm m}}{L_{\rm a}}$ and $f_{\rm SF}$ are plotted as shown in Fig. 8.10a;

 \tilde{f}_{SF}^{a} between 2000 and 4000 kg/cm².

$$w_{\rm m} = L_{\rm d} \frac{f_{\rm SF} - 600}{2 \times 10^6}$$

$$\tan \theta = \frac{\rm stress}{\rm strain} = 2 \times 10^6 \text{ kg/cm}^2$$
(8.70d)

For

$$\frac{w_{\rm m}}{L_{\rm a}} = (f_{\rm SF} - 600)\cot\theta$$

 $f_{\rm SF} > \frac{2500 \, \rm kg}{\rm cm^2}$ $L_{\rm a}$ practically is independent of the steel stress

Crack spacing for $f_{\rm SF} = 3000 \text{ kg/cm}^2 (42,600 \text{ lb/m}^2)$

$$\beta = \frac{A_b}{\pi \Phi}$$

$$L_a = K_1 + K_1 p$$
(8.70e)

Variation K_1 , K_2 with f_{SF} shown in Fig. 8.10b

$$L_{\rm a} = 3 + 0.63\beta \tag{8.70f}$$

Crack width L can also be computed directly from

$$w_{\rm m} = 0.03 + 3.6\beta \frac{f_{\rm SF} - 800}{10^6}$$

 $w = 1.1\beta \frac{f_{\rm SF}}{10^6} (\text{mm})$ Refer to Fig. 8.12c



8.2.1.13 Wastlund, Jonsson and Osterman Theory

 t_{ca}

The investigation deals with flexure only. The maximum value of the bond stresses assumed to occur at the edges of the cracks is expressed as

$$f_{\rm b} = k t_{\rm ca} \sqrt{\frac{w}{\Phi}}$$

$$= \frac{f_{\rm cu}}{10}; K \text{ coefficient}$$
(8.71)

8.2 Calculation 1

The distribution of bond stress gives

$$f_{\rm bx} = \left(1 - \frac{2x}{L}\right) K t_{\rm ca} \sqrt{\frac{w}{\Phi}}$$
(8.72)

Elastic strains in concrete is taken for m = 10

$$w(\text{flexure only}) = k_{w} \phi \left[\frac{z_{c} f_{\text{SF}}}{A_{s} J E_{s}} \right]^{2/3}$$
(8.73)

 $K_{\rm w} = 0.1$

For transformation of Eq. (8.73) to the case of direct tension, using Eq. (8.54c)

$$\frac{Z_{\rm c}}{A_{\rm s}J} = \frac{A_{\rm b}}{A_{\rm s}} = 100u$$
(8.74)
Therefore $w = K_{\rm w} \phi \left[\frac{100 f_{\rm SF}}{\mu E_{\rm s}}\right]^{\frac{2}{3}}$

$$= 100 \frac{K_{\rm R}}{E_{\rm s}} \sqrt{K_{\rm R}} \sqrt{\frac{w}{\phi}} f_{\rm SF} \frac{\phi}{\mu}$$

Generalised expression

$$A_{\rm w} = 100 \frac{K_{\rm R}}{E_{\rm s}} \sqrt{\frac{w}{\phi}} K_{\rm R} \tag{8.74a}$$

For GK 60 bars $\sqrt{w/\phi} = 14$

Summary of Results

Table 8.3 summarises various crack width and spacings based on the above theories.

To limit the crack to 0.3 mm 3 no. $GK60 + bars 1\frac{1}{4}\phi$ are required in the embedded area on the tension side. Usually in RC structures, hair crack size permissible with ordinary reinforcement having tensile strength of 20,000 psi is 0.15 mm. With the type of reinforcement provided in p.v and with the size of structure like pressure vessel, crack size at working permissible is assumed to be 0.3 mm. Therefore where greater tension in concrete is to be expected on the outside surface or haunches, the minimum number of bars <3.

Lower average strain in

Bonded steel =
$$100 \times 10^{-6} + \frac{w}{L}$$
 (8.75)

| | | | | 1 0 | |
|-----------------------------------|----------------------------|------------------------------|--|---|--|
| Method of analysis | Crack width (w) (mm) | Crack spacing (L) (mm) | GK60+ Minimum reinforcement embedded | Stress assumed in GK60 bar | Tensile stress developed in concrete |
| Brice | 1.59 | 1130 | | | |
| Saliger | 1.85 | 990 | | | .= |
| Rüsch | 1.96 | 930 | ar | .sı | sd (|
| Efsen and Krenchel | 1.815 | 1005 | $\frac{1}{2}$ $1\frac{1}{4}'' \phi 30 \text{mm} \phi$ $\frac{1}{2}$ or T30 only | ⁶ (415) 8 MN/m ² | ⁸ (345) ¹ MN/m ² |
| Wastlund, Jonsson, Osterman | 1.90 | 710 | SII | 09 | 50 |
| Maximum cra | ack spacing = | = 30'' (750 mm | 1) | | |
| Maximum cra | ack width $= 0$ | .05" (1.25 mn | n) | | |

Table 8.3 Summary of crack width and crack spacing

8.2.1.14 Crack Formation at Ultimate Load Corresponding to Liner Failure Strain

Maximum crack width the liner can span is estimated for a failure strain of 25%. A stress–strain curve for the AGR liner is not yet available after aging and irradiation. In this analysis, a typical mild stress–strain curve is used and is assumed that the stress–strain curve in bending tension is similar to that in direct tension.

Studs spacing are fixed from buckling analysis and neglecting elastic strains and friction, a crack width is determined for ultimate pressure. The results are summarised in the following pages. The ultimate capacity of studs is investigated according to C P 117 and results established by 'Nelson Studs' of USA.

8.2.1.15 Crack Widths at Ultimate Load Case

Combination of vertical prestress, hoop prestress and ultimate pressure. *Data*

HL = internal height from equator to the underside of the cap

- $H = \operatorname{cap}$ thickness
- $2\theta = angle of segment$
- RE = external dia
- RI = internal dia

X = position of hinge for equator

EEH = hoop strain at equator

ECH = hoop strain at cap

EOH = hoop strain at hinge

l =length of crack

D =boiler dia

 $\gamma =$ depth of compression block



Fig. 8.11 Deformation pattern of vessel

The general patterns are shown for various cracks in Fig. 8.11.

CWL = longitudinal crack width at equator

$$= 2\sin\theta RI (EEH - EOH)$$
(8.76)

CWH = horizontal crack at haunch

$$= \left[(\text{EEH} - \text{EOH}) \frac{\text{RE}}{X} + \frac{(\text{ESH} - \text{EOH})\text{RE}}{(\text{HL} + H - X)} \right] \times L$$
(8.77)

where

$$l = \sqrt{(RE - RI - Y)^{2} + (X - HL)^{2}}$$

CWE horizontal crack at equator

$$= \frac{2RE(EEH - EOH)}{X} \left[RE - RI - Y\frac{RE}{RI} \right]$$
(8.78)

For 1610 psi ultimate pressure, Table 8.4 shows the estimated crack width.

| | 1 | |
|------|----------------------------|--------------------------|
| | IBM 1401 programcalculated | IBM 7094 programcomputer |
| Туре | values | values from ISOPAR |
| CWL | 1.8 in. (46 mm) | 2.1 in. (54 mm) |
| CWH | 2.8 in. (70 mm) | 2.3 in. (58 mm) |
| CWE | | 3.6 in. (92 mm) |

Table 8.4 A comparative study of cracks



Fig. 8.12 Crack formation at ultimate load corresponding to linear failure strain

Crack formation ultimate load corresponding to liner failure strain is shown in Fig. 8.12.

Data

```
x_1 = square pitch of studs (assumed) = 9" and 1/8"

t = liner thickness = 3/4"

\mu = coefficient of friction = 0.4 (assumed)
```

- $\rho_{\rm s}$ = shear loading on studs (between 12.75 and 14.3 t)
- $P = \text{transverse pressure} = 1610 \text{ lb/in}^2$,
- n = number of pitches

 $(f_x)x =$ stress in the liner at distance X from crack

$$=\frac{(f_x)_{x=0}x_1t - \mu x_1px - [np_s]^{(2n-1)\frac{x_1}{2} < x < (2n+1)\frac{x_1}{2}}}{tx_1}$$
(8.79)

for
$$(2n-1)\frac{x_1}{2} < x < (2n+1)\frac{x_1}{2}$$
 (8.79a)

$$(f_x)_{x=0} \text{ in tension } = 55,000 \frac{\text{lb}}{\text{in}^2} (380 \text{ MN/m}^2) (\in_x)_{x=0} = 12\% \text{ corresponding strain} f_b = \frac{M}{Z} = \frac{P\Delta^2 x_1}{12} \frac{6}{x_1 t^2} = \frac{p\Delta^2 x}{2t^2}$$
(8.80)

Assuming this, since stress-strain curve is not linear

$$f_u = \text{limiting stress} = 60,000 \text{ psi} (415 \text{ MN/m}^2)$$

Failure strain 25-28% (25% taken)

$$(f_x)_x = 55,000 - 855x - n(4220)$$
lb/in², (8.81)

$$\in_{x} = \left[\frac{f_{x} - 36,000}{58,000}\right]^{1.633} \tag{8.82}$$

$$\Delta x = 2 \int_0^{4.5} t_x dx + 2 \int_{4.5}^{13.5} \epsilon_x dx = 1.8'' (\text{crack width})$$

$$f_b = \frac{1610(1.8)^2}{2 \times (0.75)^2} = 4650 \text{ lb/in}^2.$$
(8.83)

From Fig 8.12c

$$(f_x)_{x=0} + f_b < 6000$$

55,000 + 4650 = 59,650 < 60,000

The liner in this case takes $\Delta x = 1.8''$ (47 mm), take as 50 mm

shear
$$\frac{1610}{0.75} = 2280 \text{ lb/in}^2 \cdot \langle (f_x)_{x=0} \text{ and } f_b$$



Considering 25% strain

Ratio proportion

$$\Delta x > \left[25x - \frac{2.89x^2}{2} \right]_0^{4.5} \left\{ \frac{1}{100} \times 2 \right\}$$
$$\Delta x > 0.847 \times 2$$

i.e. $\Delta x > 1.694$ (hence 1.8 is equivalent reasonable) With 14.3 value of ρ_s for $x_1 = 8\frac{1}{8}''$ (207mm)

$$\Delta x = 2 \int_0^{4.0625} \epsilon_x \, dx + 2 \int_{4.0625}^{12.1875} \epsilon_x \, dx = 1.35'' (4.29 \text{ mm}) (\text{crack width})$$

Note: The value of the 14.3 t from standard tests on anchors by Nelson company on 5/8'' size studs. If 12.7 tons anchor value is taken, the value of Δx will reach about 2''.

If idealised stress–strain curve is used with friction stress in x-direction = f_x

$$w_u \rightarrow f_y t \text{ or } f_u t$$
 $x_1 = 8\frac{1''}{8} (207 \text{ mm})$
 $f_x = [w_u - \mu Px] \times \frac{1}{t}$
 $x_{1/2} = p_1 = \text{Half spacing} = 4.0625$
 $\in_x = \frac{f_x}{E}$

$$\Delta x = 2 \int_0^{p_1} \frac{1}{Et} (w_u - \mu P x) dx \qquad E = 27.9 \times 10^6 \, lb/in.^2$$
$$= \frac{2}{Et} \left[w_u P_1 - \frac{\mu P P_1^2}{2} \right] \qquad w_u = 60,000 \times 0.75 = 45,000(311 \text{MN/m}^2)$$
$$= 0.17'' \text{(crack width)}$$

The most valuable consideration is friction factor. However, idealised stress–strain curve is definitely meaningless and also in this case exact value of E cannot be correctly determined.

The liner is more ductile than either prestressing strand or GK60 bar, having elongation twice that of GK60 and therefore an average crack width of 1.57 in. over which the liner can span before failure against 25% strain is a reasonable assessment. To prove this, it is proposed that further tests on liner should be carried out.

Crack width = 1.57 in. (40. mm)

8.2.1.16 Analysis of a Single Bar Spanning a Crack at Ultimate Load

Major cracks are formed due to the stress in concrete exceeding the permissible stress in tension. Concrete on the edge of crack and to a distance *x* on either side of it will become progressively ineffective in transmitting the force from the reinforcement to the body of concrete with the increase of the force in steel up to the ultimate load.

It is assumed that the concrete adjoining the crack will fail in the manner shown in Fig. 8.13a, c.

Area of truncated cone on which spalling is assumed to take place:

$$A = \pi sa = \frac{\pi x}{\cos \theta} (\gamma + \phi) \tag{8.84}$$

where $a = (\gamma + \phi)$

Tensile force in concrete developed on the plane of weakness just before cracking = force of difference in the bar.

Let concrete fail in tension when the tensile stress along the plane of failure is 'f' ie. stress in concrete in the direction of reinforcement = $f \cos \theta$

Tensile force in concrete on the area of conical plane of weakness just before spalling occurs

 $= T = Af_t \sec \theta \rightarrow \text{comonent of the force parallel to the bar } Af_t \quad (8.85)$

For 'x' bar length change of force

$$f_b = \frac{\pi}{4} \phi^2 (f_{SF} = f_y)$$
(8.86)

For maximum crack width say 2" with $\gamma = x \tan \theta$



(c)

Λ

Fig. 8.13 Analysis based on a single bar spanning a crack at ultimate load

Therefore, for GK60 bars equating these forces

$$\frac{\pi x}{\cos \theta} (x \tan \theta + \phi) f_t = \frac{\pi}{4} \phi^2 (100,000 - 60,000) \text{ from Fig. 8.15b}$$
(8.86a)
$$x^2 \tan \theta + x\phi - 10,000 \frac{\phi^2}{f_t} \cos \theta = 0$$
$$f_t = 500 \text{ psi at ultimate}$$

$$\phi = 1 \frac{1''}{4} size \ 6 - k - 60 \text{ bar}$$

$$x^{2} \tan \theta + 1.25x - 31.25 \cos \theta = 0$$
for $\theta = 45^{\circ}$

$$x^{2} + 1.25x - 22.1 = 0$$

$$x = 4.2''$$

For $\theta = 0$ along the length of bar

$$x = \frac{31.25}{1.25}25''$$

The assumptions are as follows:

- (a) No external compression at right angle to the bar.
- (b) Effect of mechanical anchorage is ignored.
- (c) Failure occurs in a single bar, i.e. all bars fail over maximum crack width.

The value of x = 2.5'' bond length on both sides is just about all right. Assume still the stress distribution in bar at ultimate load is as shown in Fig. 8.13 having a bond length of 60'' (1500 mm) minimum on both sides of the crack, i.e.

minimum bond length = 5' - 0(1.524 m)

The final bond stress is

$$\frac{60}{\cos \theta} (60 \tan \theta + \phi) f_t = \phi^2 / 4 (f_{sf} - 60, 000)$$

$$\theta = 0, \phi = 1.25$$

$$60 f_t = \phi / 4 [40, 000]$$

$$f_t = 0.00521 \times 40,000$$
(8.87)

= 208.4 psi > allowable bond stress 180 psi

Conclusion

minimum bond length = 5' - 0 (1.52 hm)

Maximum crack width = 2''(50 mm)

 $1\frac{1}{2}$ GK 60 + can span a crack of 2''(50 mm) and hence one bar $1\frac{1'}{4}(30 \text{ mm})\phi$ GK 60 is considered a minimum requirement for a crack of 2'' size anywhere in vessel:

$$\frac{\text{stress at bond distance}}{A_{s} = x - \text{sectional area}} x = 60$$

The force in the tensile reinforcement at a distance x = 60'' from the crack

$$F = f_{\rm SF} - p/A_s \int_0^{x=60} f_{\rm bdx} \qquad p - \text{perimeter}$$
(8.88)

Bending moment is constant and before cracking starts, it is taken up partly by the steel and partly by concrete.

$$f = 100,000 - 4/\phi f_b.x$$

$$= 100,000 - 4/1.25 \times 208 \times 4 \times 60$$

$$\approx 60,000 \text{ psi o.k.}$$
(8.89)

Take an average crack width at ultimate load = 2'' = 50 mm.

Since all theories are giving identical results, for example, Brice theory is taken into consideration:

$$L - \text{between boilers} = 391.179''$$

$$W \max = A \frac{\Phi}{\mu} f_{SF} \text{ where } A = \frac{C_3 \times t_{ca}}{E_s f_b} \qquad (8.90)$$

$$C_3 = \frac{1}{2}; E_s(\text{assumed}) = 30 \times 10^6 \text{ psi} = 2.12 \times 10^4 \text{ kg/mm}^2$$

$$t_{ca} = 42.2 \text{ kg/cm}^2 (\text{max})$$

$$f_b = \text{bond stress (max)}$$

$$14.65 = 2 \times 1.6 \times 42.2 \left(\frac{\lambda - 1}{\lambda + 2}\right)$$

$$\left(\frac{\lambda - 1}{\lambda + 2}\right) = \frac{14.65}{135} = 0.1085$$

$$\lambda = 1.365$$

$$f_{b_{(\text{max})}} = 208.4 \text{ psi} \approx 14.65 \text{ kg/cm}^2$$

taking 60" bond length as discussed above.

Notation

w,
$$\phi - mm; \mu - \%; f_b, t_{ca} - kg/cm^2; f_{sf}, E_s - kg/mm^2$$

$$A = \frac{1}{2} \times \frac{42.2}{2.12 \times 10^4 \times 14.65} = 0.68 \times 10^{-4}$$

Therefore,

$$50.8 = w_{\text{max}} = 0.68 \times 10^{-4} \frac{\Phi}{\mu} f_{\text{SF}}$$
$$= 0.68 \times 10^{-4} \times \frac{\Phi}{\mu} 42.2$$
$$\frac{\Phi}{\mu} = \frac{50.8 \times 10^{-2}}{0.287}$$
$$\Phi = 31.8 \text{ mm}$$
$$\mu = 0.00018\%$$

assumed embedded area = $1.365 \times 31.8 = 43.3$

Therefore

% area of steel = $0.0018 \times 43.3 = 0.08\%$ (minimum through out)

Assuming if 3 bars are used

area of steel =
$$0.25\%$$

Taking 12×240 embedded area across the barrel thickness (excluding shutters)

steel area =
$$2880 \times 0.0018 = 5.184 \text{ in}^2$$

using
$$1\frac{1''}{4}\phi GK60$$
 bars, area = 1.227 in²

total bars $=\frac{5.184}{1.227} = 4.23$ bars (based on 60,000 psi yield strength)

Since crack size of approx. 2''(50 mm) is developed at ultimate load plastic range is considered for steel.

No.bars =
$$\frac{60,000}{90,000} \times \frac{5.184}{1.227} \approx 3$$
 bars GK601 $\frac{1''}{4}$ ϕ in metric 3T30

Therefore, where crack sizes are 2''(50 mm) width, 3 no.1 $\frac{1''}{4}$ ϕ GK60 bars should be embedded, giving minimum 50''(1270 mm) length on either side.

Chapter 9 Concrete Nuclear Shelters

9.1 Introduction

There is increasing current concern about safety from nuclear hazards, including nuclear blasts and radiation. There will be greater involvement in protecting people against such hazards. A nuclear shelter is just one of many ideas to protect and shield a person from the effects of nuclear explosions. These structures can range from a deep buried rigid structure to a concrete framed box covered with soil.

The vast quantities of nuclear energy released by detonation are distributed approximately in the following way:

Blast and shock wave: 45% Light and heat radiation: 35% Initial nuclear radiation: 5% Residual radiation: 15%

Secondary effects such as flooding and soil liquefaction are also considered in the overall safety analysis of shelters. Factors which affect the response of shelters to air blast are the following:

- (a) strength and mass
- (b) structural layout
- (c) ductility

The airburst from an atom bomb propagates through the atmosphere to great distance with minimum energy losses. On the other hand, in an underground burst much of the energy is absorbed in cratering and melting of the ground. A burst occurring above 30,000 m is known as an airburst provided the fireball at maximum brilliance does not touch the surface of the earth. If it touches, it becomes a 'surface burst'. These cases together with their loading conditions are described in this section. A typical concrete shelter design for a six-person family is chosen for finite element analysis using the five-parameter constitutive law. Analytical results show agreement with those provided by the various codes.

9.2 Characteristics of the Blast Wave in Air

Most of the material damage from an airburst (nuclear weapon) is caused mainly by the shock (or blast) wave which accompanies the explosion. The majority of structures will suffer some damage from air blast when the overpressure in the blast wave, i.e. the excess over atmospheric pressure (101.3 kN/m² at sea level), is about 3.5 kN/m^2 or more. The distance to which this overpressure level will extend depends on the yield of the explosion and on the height of the burst.

A difference in air pressure acting on separate surfaces of a structure produces a force on that structure; the size of these forces is dependent on the difference between ambient air pressure and the overpressure. The maximum value of overpressure, known as the peak overpressure, occurs at the front of the blast wave.

As the blast wave travels in the air away from its source, the overpressure at the front steadily decreases, and the pressure behind the front falls off in a regular manner. After a short time, when the shock front has travelled a certain distance from the fireball, the pressure behind the front drops below that of the surrounding atmosphere and a so-called 'negative phase' of the blast wave forms, as given in Fig. 9.1.

For the curves marked t_1 to t_4 the pressure in the blast wave has not fallen below atmospheric pressure, but on the curve t_5 it is seen that at some distance behind the shock front the overpressure is below that of the original atmosphere so that an 'underpressure' exists.

During the negative (rarefaction or Suction) phase a partial vacuum is produced and the air is sucked in, instead of being pushed away, as it is when the overpressure is positive.

The peak values of the underpressure are generally small compared with the peak overpressures, the former having a maximum value of 27.5 kN/m^2 below the



Distance from explosion (m)

Fig. 9.1 Variation of overpressure with distance at successive times





ambient pressure. With increasing distance from the explosion, both peak values decrease, the positive more rapidly than the negative, but they do not approach equality until the peak pressures have decayed to a very low level (Fig. 9.2).

For a short interval after the detonation, point 1, there will be no increase in pressure since it takes the blast wave some time to travel the distance from the point of explosion to the given location. Point 2 indicates the time of arrival of the shock front; a strong wind commences to blow away from the explosion. This is often referred to as a 'transient' wind, as its velocity decreases fairly rapidly with time.

Following the arrival of the shock front the pressure falls rapidly, and at the time corresponding to point 3 it is the same as that of the original atmosphere. Although the overpressure is now zero, the wind will continue in the same direction for a short time. The interval from points 2 to 3 (roughly 2–4 s for a 1 megaton explosion) represents the passage of the positive (or compression) phase of the blast wave. It is during this interval that most of the destructive action of the airburst will be experienced.

As the pressure in the blast wave continues to decrease, it sinks below that of the surrounding atmosphere. In the time interval from point 3 to point 5, which may be several seconds, the negative (or suction) phase of the blast wave passes the given location. For most of this period the transient wind blows towards the explosion. As the negative phase passes, the pressure at first decreases below ambient and then increases towards that of the ambient atmosphere which is reached at the time represented by point 5. The blast wind has then effectively ceased and thedirect destructive action of the airblast is over.

9.2.1 Dynamic Pressure

Although the destructive effects of the blast wave are usually related to values of the peak overpressure, there is another quantity of equivalent importance called the 'dynamic pressure'.

The dynamic pressure is proportional to the square of the wind velocity and to the density of the air behind the shock front. For very strong shocks the dynamic pressure is larger than the overpressure but below 480 kN/m² (4.7 atmospheres) overpressure at sea level; the dynamic pressure is smaller. The

peak overpressure dynamic pressure decreases with increasing distance from the explosion centre, although at a different rate.

Some indication of the corresponding values of peak overpressure, peak dynamic pressure and maximum blast wind velocity for an ideal shock front in air at sea level are given in Table 9.1.

| Peak overpressure, KN/M ² | Peak dynamic pressure, KN/M ² | Maximum wind velocity, |
|--------------------------------------|--|------------------------|
| (atoms) | (atoms) | Km/h |
| 1378 (13.78) | 2274 (22.74) | 3347 |
| 1034 (10.34) | 1537 (15.37) | 2860 |
| 689 (6.89) | 848 (8.48) | 2275 |
| 496 (4.96) | 551 (5.51) | 1883 |
| 345 (3.45) | 275 (2.75) | 1512 |
| 207 (2.07) | 110 (1.10) | 1078 |
| 138 (1.38) | 55 (0.55) | 756 |
| 69 (0.69) | 15 (0.14) | 467 |
| 34 (0.34) | 5 (0.05) | 257 |
| 14 (0.14) | 0.7 (0.007) | 97 |

 Table 9.1
 Overpressure, dynamic pressure, and wind velocities, in air at sea level for an ideal shock front

When the shock front reaches a given point, both the overpressure and the dynamic pressure increase almost immediately from zero to their maximum values and then decrease. The dynamic pressure (and wind velocity) will fall to zero some what later than the overpressure because of the momentum of the air in motion behind the shock front, but for the purposes of estimating damage the difference is not significant. During the negative (suction) phase of the blast wave the dynamic pressure is very small and acts in the opposite direction.

9.2.2 Arrival Time and Duration

There is a finite time interval required for the blast wave to move out from the explosion centre to any particular location. This time interval is dependent upon the energy yield of the explosion and the distance involved. At 1.6 km from a 1 megaton burst, the arrival time would be about 4 s. Initially, the velocity of the shock front is quite high, many times the speed of sound, but as the blast wave progresses outwards, so it slows down as the pressure at the front weakens. Finally, at long ranges, the blast wave becomes essentially a sound wave and its velocity approaches ambient sound velocity.

The positive phase duration is shortest at close ranges and increases as the blast wave moves outwards. At 1.6 km from a 1 megaton explosion, the duration of the positive phase of the blast is about 2 s. The period of time over which the positive dynamic pressure is effective may be taken as essentially the positive phase of the overpressure.



Fig. 9.3 Variation of overpressure with time at fixed location

9.2.3 Reflection of the Blast Wave at a Surface

When the incident blast wave from an explosion in air (Fig. 9.3) strikes a more dense medium, such as the Earth's surface, either land or water, it is reflected.

When such reflection occurs, an object precisely at the surface will experience a pressure increase, since the reflected wave is formed instantaneously the value of the overpressure thus experienced at the surface is generally considered to be entirely a reflected pressure. In the region near ground zero, this total reflected overpressure will be more than twice the value of the peak overpressure of incident blast wave.

There are two important destructive aspects of the blast wave involved reflection:

- (i) Only a single pressure increase is experienced in the Mach region below the triple point as compared to the separate incident and reflected waves region of regular reflection.
- (ii) (a) Since the Mach stem is nearly vertical, the accompanying blast wave travelling in a horizontal direction at the surface.
 - (b) The transient winds are approximately parallel to the ground, thus, the Mach region, the blast forces on aboveground structures other objects are directed nearly horizontally, so that vertical surfaces are loaded more intensely than horizontal surfaces.

9.2.4 Blast from a Surface Burst

In a surface explosion, the front of the blast wave in air is hemispherical in (Fig. 9.4), there is no region of regular reflection, and all objects and on the



Fig. 9.4 Blast wave from a contact burst

structures on the surface, even close to ground zero, are subjected to air blast similar to the Mach region below the triple point of an airburst.

The diameter of the rupture zone D_r is 1.5 D_a ; the overall diameter, including the D_D is $2D_a$; and the height of the lip H_t is $0.25H_a$.

The dependence of crater radius and crater depth upon the depth of burst for a 1 kiloton explosion in dry soil is shown in Fig. 9.5. Also shown are the range of ... dimensions possible from a surface burst to the approximate maximum for an



Fig. 9.5 Crater versus yield (courtesy of US Airforce)

underground burst, for any explosion energy yield from 1 kiloton to 10 megatons. Therefore a 1 megaton blast wave front may be assumed to be vertical for most structures, with both overpressure and dynamic pressure decaying at different rates behind the blast wave as previously stated.

All the above descriptions are based on an ideal blast wave in ideal atmospheric conditions: unfortunately, nothing is perfect, especially meteorological conditions, which can greatly alter the expected performances of explosions, either increasing them or decreasing them.

9.2.5 Ground Shock from Air Blast

Another aspect of the blast wave problem is the possible effect of an airburst on underground structures as a result of the transfer of some of the blast wave energy into the ground. A minor oscillation of the surface is experienced and a ground shock is produced. The strength of the shock at any point is determined by the overpressure in the blast wave immediately above it. For large overpressures with long-positive phase duration, the shock will penetrate some distance into ground; but blast waves which are weaker and of shorter duration are attenuated more rapidly. The major principal stress in the soil will be nearly vertical and about equal in magnitude to the air blast overpressure.

For high airbursts where relatively large blast pressures are not expected at ground level, the effects of ground shock induced by the air blast will be negligible, but if the overpressure at the surface is large there may be damage to buried structures. However, even if the structure is strong enough to withstand the effect of the ground shock, the sharp jolt resulting from the impact of the shock front can cause injury to occupants and damage to loose equipment.

9.2.6 Technical Aspects of a Blast Wave

The basic relationships among the properties of a blast wave having a sharp front at which there is a sudden pressure discontinuity, i.e. a true shock front, are given in Tables 9.2–9.5 and Fig. 9.5 respectively.

9.2.7 Air Blast Loading and Target Response

The behaviour of an object or structure exposed to the blast wave from a nuclear explosion may be considered under two main headings.

- 1. Loading, the forces which result from the action of that pressure.
- 2. Response or distortion of the structure due to the particular loading.

 $p_{\rm do}$ = peak dynamic pressure $U_{\rm o}$ = velocity of the shock front $p_{\rm s}$ = overpressure at time t = time after detonation of yield 'v' $t_{\rm dd}$ = delayed time (dynamic) t_{dp} = duration of dynamic overpressure $U_{0}[U_{s} = 1117 \times \sqrt{1 + 6p_{s0}/7p_{0}}]$ $p_{\rm o}$ = atmospheric pressure = 14.7 $p_{\rm r}$ = reflected pressure = $2p_{\rm o}\left(\frac{102.9+4p_{\rm so}}{102.9+p_{\rm so}}\right)$ $t_{\rm c}$ = clearing time of the reflection effect = 3x height of the reflecting surface above ground/ U_0 Scaling laws (for two bombs) $R_{2} = \tilde{R}_{1} (y_{2}/y_{1})^{1/3}$ $t_{dd} = t_{dp} (y_{2}/y_{1})^{1/3}$ R, R_1, R_2 = radii or distances from explosions Reference should be made to Fig. IX. 163 for other details Additional loadings $\frac{p_{so}}{p_o} = 3.2 \times 10^6 R^{-3} \sqrt{1 - \left(\frac{R}{87}\right)^2 \times \left(\frac{800 + R}{800}\right)}$ time in seconds = $t_{dp} = (y)^{1/3} \left\{ \frac{180[1+(0.01R)^3]^{1/2}}{1+(R/40)\sqrt[6]{1+(R/285)^5\sqrt[6]{1+0.0002R}}} \right\}$

$$IMt: Pso = 20lbf/in^2 \rightarrow 7100ft$$
$$\frac{1}{2}Mt: \frac{R_2}{7100} = \left(\frac{0.5}{1}\right)^2$$

Therefore

$$R_1 = 5650 \, \text{ft}$$

(Note: 1ft = 0.3048 m.)

As a general rule, response may be taken to be synonymous with damage, since permanent distortion of a sufficient amount will impair the usefulness of a structure.

Direct damage to structures attributable to air blast can take various forms; the blast may deflect structural steel frames, collapse roofs, dish-in walls, shatter panels and break windows.

9.2.7.1 Loading

(a) Diffraction Loading

When the front of an air blast wave strikes the face of a building, reflection occurs. As a result the overpressure builds up rapidly to at least twice that in the incident wave front; the actual pressure attained is determined by various factors, such as the peak overpressure of the incident wave and the angle between the direction of motion of the wave and the face of the building. As the wave front moves forward, the reflected overpressure on the face drops

| Distance from ground zero kilometer miles 1 | Peak overpres | sure kpa (psi) | Windspeed, r | n/s (mph) | Arrival | time (s) | Duratic | n (s) |
|---|---------------|----------------|--------------|------------|---------|----------|---------|-------|
| | Mt | 10 Mt | 1 Mt | 10 Mt | 1 Mt | 10 Mt | 1 Mt | 10 Mt |
| 1 (0.6) 98 | 980 (140) | 4200 (600) | 980 (2200) | | 0.9 | | 0.9 | 1 |
| 2 (1.25) 2(| 200 (29) | 1050 (150) | 400 (900) | 980 (2200) | 4 | 1.8 | 1.8 | 7 |
| 3 (1.9) 15 | [30 (18) | 380 (54) | 180 (400) | 805 (1800) | 9 | 4.7 | 2.3 | 2.4 |
| 4 (2.5) 65 | 53 (12) | 220 (31) | 128 (285) | 490 (1100) | 9 | 8 | 2.6 | 3.7 |
| 5 (3.1) 5(| 56 (8) | 170 (24) | 106 (238) | 277 (620) | 12 | 11 | 2.8 | 4.2 |
| 6 (3.8) 42 | 12 (6) | 135 (19) | 81(182) | 200 (450) | 14 | 12.5 | ŝ | 4.7 |
| 7 (4.4) 35 | 33 (4.7) | 110 (16) | 69 (155) | 170 (380) | 18 | 16 | 3.2 | 5 |
| 8 (5) 27 | 27 (3.8) | 90 (13) | 56 (125) | 143 (320) | 22 | 18 | 3.4 | 5.3 |
| 9 (5.6) 24 | 24 (3.4) | 77 (11) | 48 (108) | 125 (280) | 26 | 20 | 3.5 | 5.5 |
| 10 (6.2) 21 | 21(3) | 63 (9) | 40 (90) | 114 (255) | 28 | 22 | 3.6 | 5.9 |
| 12 (7.5) 15 | 15 (2.2) | 46 (6.5) | 31 (70) | 96 (215) | 31 | 30 | 3.7 | 6.3 |
| 15 (9.4) 11 | [0 (1.5) | 34 (4.8) | 24 (53) | 72 (160) | 45 | 38 | 3.8 | 6.7 |
| 20 (12.5) 7 | 7 (1) | 22 (3.3) | 17 (37) | 46 (103) | 5.9 | 53 | 4 | 7.5 |
| 25 (16) 5 | 5 (0.75) | 15 (2.2) | 9 (20) | 32 (72) | 70 | 67 | 4.2 | 7.8 |

| | Shallow buried | | |
|-----------------|----------------|------------------|-------------|
| Member | In dry ground | High water level | Surface |
| Roof and floors | $P_{\rm so}$ | P _{so} | Pso |
| Walls | $0.5P_{so}$ | P _{so} | $2.3P_{so}$ |

 Table 9.4
 Blast loads on shallow buried surface shelters

 $P_{\rm so} = {\rm overpressure}$

Dead loads, soil and water loads should be added to the blast loads given above.

| Table 9.5 Generalised data in relation to loads |
|--|
| 1-megatonburst at a distance of 1.6 km (1 mile) from ground zero |
| Velocity of shock front 0.500 m |
| Ductility ratio $\mu = 5$ |
| Maximum allowable time $= 0.15$ s |
| Where applicable, drag coefficients: roof $= -0.4$, wall $= +0.9$ |
| Yield strength of steel reinforcement = $410 \text{ or } 425 \text{ N/mm}^2$ |
| $f_{\rm cu}$ (dynamic) = 1.25 $f_{\rm cu}$ (static) |
| P_{y} (dynamic) = 1.10 P_{y} (static) |
| Main reinforcement $\neq 0.25\%$ bd (b = width of section, d = effective depth of section) |
| Secondary reinforcement $\neq 0.15 bd$ |
| The ultimate shear stress $\neq 0.04 f_{cu}$ |
| The dynamic shear stress for mild steel $\geq 1.172 \text{ N/mm}^2$ |
| Bolts should be black bolts to BS 4190 |
| Allowable dynamic stresses: |
| Bolts: tension 275 N/mm ² |
| shear 170 N/mm ² |
| bearing 410 |
| Welds: tension/compression 274 N/m ² |
| Shear 170 N/mm ² |
| |

rapidly to that produced by the blast wave without reflection, plus an added drag force due to the wind (dynamic) pressure. At the same time the air pressure wave bends or 'diffracts' around the structure so that the structure is eventually engulfed by the blast (Fig. 9.7) and approximately the same pressure is exerted on the side walls and the roof.

The front wall, however, is still subject to wind pressure, although the back wall is shielded from it.

The pressure differential between the front and back faces will have its maximum value when the blast wave has not yet completely surrounded the structure. In this case, such a pressure differential will produce a lateral (or translational) force, tending to cause the structure to deflect and thus move bodily, usually in the same direction as the blast wave. This force is known as the 'diffraction loading' because it operates while the blast wave is being diffracted around the structure. The extent and nature of the actual motion will depend upon the size, shape and weight of the structure, and how firmly it is attached to the ground.

When the blast wave has engulfed the structure, the pressure differential is small, and the loading is almost entirely due to the drag pressure exerted on the front face.





The actual pressures on all faces of the structure are in excess of the ambient atmospheric pressure and will remain so, although decreasing steadily, until the positive phase of the blast wave has ended, thus the diffraction loading on a structure without openings is eventually replaced by an inwardly directed pressure.

The damage caused during the diffraction stage will be determined by the magnitude of the loading and by its duration. The loading is related to the peak overpressure in the blast wave and this consequently is an important factor. If the structure under consideration has no openings, as has been assumed for this discussion, the duration of the diffraction loading will be very roughly the time required by the wave front to move from the front to the back of the building, although wind loading will continue for a longer period.

If the building exposed to the blast wave has openings, or if it has Windows, panels, light sidings or doors which fail in a very short space of time, there will



Fig. 9.7 Stages in diffraction (plan view) without openings (Courtesy of US Department of Defence and Atomic Energy Commission)

be a rapid equalisation of pressure between the inside and the outside of the structure. This will tend to reduce the pressure differential while diffraction is taking place. The diffraction loading on the structure as a whole will thus be decreased, although the loading on interior walls and partitions will be greater than for essentially closed structures. Furthermore, if the building has many Openings after the diffraction stage, the subsequent squeezing (crushing) action, due to the pressure being higher outside than inside, will not occur.

9.2.7.2 Loading Due to Drag

During the whole of the overpressure positive phase, a structure will be subjected to the dynamic pressure loading or drag loading caused by transient winds behind the blast wave front. Like the diffraction loading, the drag loading, especially in the Mach region, is equivalent to a lateral (air translational) force acting upon the structure.

9.2.7.3 Loading Versus Structural Characteristics

There are basically two types of building when considering blast wave loading:

- (1) Diffraction type
- (2) Drag type

As these names imply, in a nuclear explosion, the former would be affected mainly by diffraction loading and the latter by drag loading. While it is true that some structures will respond mainly to diffraction forces and others mainly to drag forces, all such buildings will respond to both types of loading.

A diffraction type building is one that is primarily sensitive to the peak overpressure in the shock wave, e.g. reinforced concrete buildings with small window area and large wall-bearing structures.

When the pressures on different areas of a structure are quickly equalised, because of its small size, the characteristics of the structure or the rapid formation of numerous openings by the action of blast, the diffraction forces operate for a very short time. The response of the structure is then mainly due to the dynamic pressures (or drag forces) of the blast wind, e.g. for telephone poles, radio and television transmitter towers, and tall chimneys.

9.3 Introduction to Codified Design

This section is devoted to the analysis and design of reinforced concrete nuclear shelters. Calculations are given for a particular study using both the British and American codes. Details are also given in this section regarding the Swedish Civil Defence Administration Code.

9.3.1 US Code Ultimate Strength Theory: General Formulae

Figure 9.8 shows cracking, crushing and disengagement cases recommended in successive ACI building codes.

9.3.1.1 General Equation: Ultimate Static Moment Capacity

Cross-Section Type I

(1) The ultimate unit resisting moment M_u of a rectangular section of width b, with tension reinforcement only, is given by

$$M_{\rm u} = (A_{\rm s} f_{\rm s}/b)(d - a/2) \tag{9.1}$$

where A_s = area of tension reinforcement within the width b

- $f_{\rm s}$ = static design stress for reinforcement
- d = distance from the extreme compression fibre to the centroid of tension reinforcement
- a = depth of equivalent rectangular block $= A_s f_s / 0.85 b f'_e$
- b = width of compression face

 f'_e = static ultimate compressive strength of concrete.

The reinforcement ratio p is defined as

$$p = A_{\rm s}/bd \tag{9.2}$$



Fig. 9.8 Reinforced concrete cross-section

(2) To ensure against sudden compression failures, p must not exceed 0.75 of the ratio $P_{\rm b}$, which produces balanced conditions at ultimate strength and is given by

$$P_{\rm b} = (0.85K_1 f_{\rm o}'/f_{\rm s})[87\,000/(87\,000 + f_{\rm s})] \tag{9.3}$$

where $K_1 = 0.85$ for ft up to 4000 psi and is reduced by 0.05 for each 1000 psi in excess of 4000 psi.

(3) For a rectangular section of width b with compression reinforcement, the ultimate unit resisting moment is

$$M_{\rm u} = \left[\left(A_{\rm s} - A_{\rm s}^{'} \right) f_{\rm s} / b \right] (d - a/2) + \left(A_{\rm s}^{'} f_{\rm s} / b \right) \left(d - d^{'} \right)$$
(9.4)

where A'_{s} = area of compression reinforcement with in the width b,

d' = distance from the extreme compression fibre to the centroid of compression reinforcement,

| Pressure design range | Reinforcement | Two-way elements | One-way elements |
|-----------------------|---------------|--|--|
| Intermediate | Main | $A_{\rm s} = 0.0025bd$ | $A_{\rm s} = 0.0025bd$ |
| and low | Other | $A_{\rm s} = 0.0018bd$ | $A_{\rm s} + A_{\rm s}^{'} = 0.0020 b T_c$ |
| High | Main | $A_{\rm s} = A_{\rm s}^{'} = 0.0025 b d_c$ | $A_{\rm s} = A_{\rm s}^{'} = 0.0025 b d_c$ |
| | Other | $A_{\rm s} = A_{\rm s}^{'} = 0.0018bd_{c}^{*}$ | $A_{\rm s} = A_{\rm s}^{'} = 0.0018 b d_c^{*}$ |

Table 9.6 Reinforcement for one-and two-way elements

*But not less than $A_s/4$ used in the main direction (see Fig. 9.9 for coefficients)

a = depth of the equivalent rectangular stress block:

$$(A_{\rm s} - A_{\rm s}')f_{\rm s}/0.85bf_{\rm c}'$$
 (9.4*a*)

The minimum area flexural reinforcement is given in Table 9.6.

9.3.1.2 Ultimate Static Shear Capacity

Diagonal Tension

(1) The ultimate shear stress v_u as a measure of diagonal tension, is computed for type I sections from

$$v_{\rm u} = V_{\rm u}/bd \tag{9.5}$$

and for type II and III sections from

$$v_{\rm u} = V_{\rm u}/bd_{\rm c} \tag{9.6}$$

where V_u is the total shear on a width b at the section a distance d (type I) or d_c (type II and III) from the face of the support. The shear at sections between the face of the support and the section d or d_c therefor need not be considered critical.

(2) The shear stress permitted on an unreinforced web is limited to

$$v_{\rm c} = \phi \left[1.9\sqrt{f_{\rm c}'} + 2500p \right] \le 2.28\phi \sqrt{f_{\rm c}'}$$
(9.7)

where ϕ is the capacity reduction factor and is equal to 0.85 for all sections.

(3) When the ultimate shear capacity $v_u > v_c$ shear reinforcement must be provided. When stirrups are used, they should be provided for a distance *d* beyond the point theoretically required, and between the face of the support and the cross-section at a distance *d*. The required area for stirrups for type I cross-sections is calculated using

$$A_{\rm v} = [(v_{\rm u} - v_{\rm c})b_{\rm s}s_{\rm s}]/[\phi f_{\rm s}(\sin\alpha + \cos\alpha)]$$
(9.8)

while for cross-sections conforming to types I, II and III, the required area of lacing reinforcement is calculated and shown in Fig. 9.10.

$$A_{\rm v} = [(v_{\rm u} - v_{\rm c})b_{\rm l}s_{\rm l}]/[\phi f_{\rm s}(\sin\alpha + \cos\alpha)]$$
(9.9)



Fig. 9.9 Coefficient for the moments of inertia of cracked sections with tension reinforcement only (courtesy of ACI)



Fig. 9.10 Designs of lacings: (a) vertical and (b) horizontal

where A_v = total area of stirrups or lacing reinforcement in tension within a width b_s, b_l and distance s_s or s_l

 $(v_u - v_c)$ excess shear stress

- $b_{\rm s}$ = width of concrete strip in which the diagonal tension stresses are resisted by stirrups of area $A_{\rm v}$
- b_1 = width of concrete strip in which the diagonal tension stresses are resisted by lacing of area
- $s_s = spacing$ of stirrups in the direction parallel to the longitudinal reinforcement
- s_1 = spacing of lacing in the direction parallel to the longitudinal reinforcement
- α = angle formed by the plane of the stirrups or lacing and the plane of the longitudinal reinforcement

The excess shear stress $v_u - v_c$ is as follows.

| Limits | Excess shear stress $v_u - v_c$ stirrups | Lacing |
|---|--|---------------------------|
| $v_{\rm u} \leq v_{\rm c}$ | 0 | ν _c |
| $\upsilon_c\!<\!\upsilon_u\leq 2\upsilon_c$ | $v_u - v_c$ | υ _c |
| $v_u > 2v_c$ | $v_u - v_c$ | $\upsilon_u - \upsilon_c$ |

The ultimate shear stress v_u must not exceed $10\phi\sqrt{f_c}$ in sections using stirrups. In sections using lacing there is no restriction on v_u because of the continuity provided by this type of shear reinforcement.

Wherever stirrups are required $(v_u > v_s)$, the area A_v should not be less than 0.0015*bs*_s and for type III rectangular sections of width *b*:

$$M_{\rm u} = A_{\rm s} f_{\rm s} d_{\rm c}/b \tag{9.10}$$

where A_s = area of tension or compression reinforcement within the width *b*;

 $d_{\rm c}$ = distance between the centroids of the compression and the tension reinforcement

The reinforcement ratios p and p' are given by

$$p = p' = A_{\rm s}/bd \tag{9.11}$$

The reinforcement ratio p' is given by

$$p' = A'_s/bd \tag{9.12}$$

Equation (9.11) is valid only when the compression steel reaches the value f_s at ultimate stress, and this condition is satisfied when

$$p - p' \ge 0.85 K_1 \frac{f_c'd'}{f_s d} \left(\frac{87000}{87000 - f_s}\right)$$
(9.13)

Cross-Section Types II and III.

(1) The ultimate unit resisting moment of type II.

9.3.1.3 Modulus of Elasticity

Concrete.

The modulus of elasticity of concrete, E_c , is given by

$$E_{\rm c} = w^{15} 33 \sqrt{f_{\rm c}'} \mathrm{psi} \tag{9.14}$$

The value of w, the unit weight of concrete, lies between 90 and 155 lb/ft^2 .

Reinforcing Steel.

The modulus of elasticity of reinforcing steel, E_s , is

$$E_{\rm s} = 30 \times 10^6 \rm psi \tag{9.15}$$

Modular Ratio.

The modular ratio, n, is given by

$$n = E_{\rm s}/E_{\rm c} \tag{9.16}$$

and may be taken as the nearest whole number.

9.3.1.4 Moment of Inertia

The average moment of inertia, I_a , to be used in calculating the deflection is

$$l_{\rm a} = (l_{\rm g} + l_{\rm c})/2 \tag{9.17}$$

where I_g is the moment of inertia of the gross concrete cross-section of width b about its centroid (neglecting steel areas) and is equal to

$$l_{\rm g} = bT_{\rm c}^3/12 \tag{9.18}$$
and l_c is the moment of inertia of the cracked concrete section of width *b* considering the compression concrete area and steel areas transformed into equivalent concrete areas and computed about the centroid of the transformed section. l_c is calculated from

$$l_{\rm c} = Fbd^3 \tag{9.19}$$

The coefficient F varies as the modular ratio n and the amount of reinforcement used. For sections with tension reinforcement only, F is given in Fig. 9.9.

9.4 Design of a Concrete Nuclear Shelter Against Explosion and Other Loads Based on the Home Office Manual

Figure 9.11 shows a typical layout of a domestic nuclear shelter for a family of six.



Fig. 9.11 Domestic nuclear shelter: general arrangement

9.4.1 Basic Data (Home Office Code)

For a 1 Mt ground burst at a distance of 1.6 km from ground zero:

Ductility ratio, μ : 5 Main reinforcement $\neq 0.25\% bd$ Secondary reinforcement $\geq 0.15\% bd$ Ultimate shear stress $\geq 0.04 f_{cu}$ Dynamic shear stress (mild steel) $\geq 172 \text{ N/mm}^2$ Protective factor: 4000 Concrete f_{cu} (static): 30 N/mm² (grade 30) Concrete f_{cu} (dynamic): 1.5f $f_{cu} = 37.5 \text{ N/mm}^2$ Reinforcement f_{cu} (static): 420 N/mm² Reinforcement f_{cu} (dynamic): 1.10 = 462 N/mm² Young's modulus, E_c : 20 GN/m² Young's modulus, E_s : 200 GN/m² Clear span: 3 m Slab thickness: 300 mm (with minimum cover 50) Blast load: 0.17 N/mm², $F_1(t) = P_{do}$

9.4.2 Additional Data for Designs Based on US Codes

Dynamic increase factors (DIF) Concrete compression 1.25 diagonal tension 1.00 direct shear 1.10 Reinforcement: bending 1.10 1.00 shear Dynamic stresses: concrete f_{c}' (cylindrical strength) = 0.87 f_{cu} $= 3000 \text{ lb/in}^2 \text{ (psi)}$ $= 60000 \text{ lb/in}^2 \text{ (psi)}$ concrete $f_{\rm v}$ (static)

$$R_{\rm m} = r_{\rm u} = \left(\frac{1}{1 - \frac{1}{2\mu}}\right) F_1(t) = 1.1 F_1(t) = 0.187 \,{\rm N/mm^2}$$
 (9.20)

Deadload of concrete plus soil = 0.014 N/mm^2

$$r_{\rm u} = 0.187 + 0.014 = 0.201 \, {\rm N/mm^2}$$

For a two-way slab

$$M_u = r_u - L^2 / 16 = 0.201(3000)^2 / 16 = 11,3062.5 N mm/mm$$

300 mm thick slab

T16—200 bars; $A_s = 1005 \frac{mm^2}{m}$: d = 300 - 50 - 8 = 242

$$z = d - (0.84 f_{yd} A_s / f_{cu} (dyn))$$

= 242 - (0.84(462)(1005)10⁻³/37.5)
= 231.58 mm

Note: Later on, based on finiteelement analysis, the T20-200 bars adopted were checked

Area of the roof = 9 m² = A_t ; $\sqrt{A_t} = 3m$

$$H - x = 2.7 - 0.3 = 24 \text{ or } 3.4 - 0.3 = 3.1$$

 $\sqrt{(A_t)(H - X)} = 1.25 \text{ and } 0.97$

Weight of overhead material = 1340 kg/m^2 R = 0.025% (roof contribution)

$$PF = \frac{100}{(R + G_T)}$$
$$= \frac{100}{(0.025 + 0)}$$
$$= 4000 \text{ (safe)}$$

where $G_{\rm T}$ is the percentage wall contribution, ignored in the worst case. Figure 9.12 gives structural details of the reinforced concrete shelter.

Steel blast doors

Clear opening 800 mm \times 1200 mm.

 $F_1(t) = P_{do} = 2.3P_{so} = 2.3(0.17) = 0.39 \text{ N/mm}^2$ $r_u = 1.1 F_1(t) = 0.43 \text{ N/mm}^2$ $M_u \text{ (simply supported) } 0.43(800)^2/8 = 34,400 \text{ N/mm}$

20 mm thick steel door

$$z = bd^2/4 = 1(20^2)/4 = 100 \text{ mm}^2$$

Also $z_p = M_u/1.1(265) = 118 \text{ mm}^2$

Calculated thickness of steel doors = (118/100)20 = 23.625 mm A 25 mm thick door was adopted.

The thickness of the glass door may have to be increased for protection against radiation fall-out. One possibility is a steel-concrete sandwich construction. One possible steel door design is given in Fig. 9.13 or z = 0.95(242)= 229.9 mm ≈ 230 mm

Walls: 300 mm thick

Blast load on walls $= p_{do} \times 05 = 0.085 \text{ N/mm}^2$ $r_u = 1.1 F_1(t) = 1.1(p_{do}) = 0.0935 \text{ N/mm}^2$ Total (including soil) $= 0.0935 + 0.08 = 0.1735 \text{ N/mm}^2$



Fig. 9.12 Domestic nuclear shelter (reinforcement concrete): detail



Fig. 9.13 Design of steel blast doors. (a) Elevation; (b) vertical section; (c) door location; (d) horizontal section: structural details

Two-way slab

$$M_{\rm u} = r_{\rm u}L^2/16 = 0.1735(2700)^2/16 = 79\,050.941$$

Both walls (2700 mm
and 3400 mm)
$$M_{\rm u} = \left[(3400)^2/(2700)^2 \right] (79\,050.94)$$
$$= 125\,353.75\,\rm N\,\,mm/mm\,\,(adopted)$$

$$M_{\rm u} = 125\,353.75 = A_{\rm s}(230)(462)$$

 $A_{\rm s} = 1.18\,\,{\rm mm^2/mm} = 1180\,{\rm mm^2/m}$

adopted T20–200 (in some critical areas T20–100 and T25–100) Shaft wall bars: T12–200 links T16-300 U-bars Minimum steel:

Main → $0.25\% \times 1 \times 242 = 0.605 \text{ mm}^2/\text{mm} (605 \text{ mm}^2/\text{m})$ $1005 \text{ mm}^2/\text{m} > 605(\text{T16} - 200) \text{ adopted}$

Secondary $\rightarrow 0.15\% \times 1 \times 242 = 0.363 \text{ mm}^2/\text{mm} (363 \text{ mm}^2/\text{m})$ (T16–200 or 300) adopted

Shear: allowable shear = $0.04 f_{cu} = 1.2 \text{ N/mm}^2$

shear =
$$r_u[(L/2 - d)/d]$$

= $(2700/2 - 242)/2700$
= $0.41 < 1.2 N/mm^2$ (safe)
or = $(\frac{3400}{2} - 242)/3400$
= $0.43 < 1.2 N/mm^2$

Protective factor (PF) in the middle of the shelter and at 0.25–0.30 m above the floor level.

9.5 Design of a Nuclear Shelter Based on the US Codes

9.5.1 Introduction

Many codes in the USA have empirical equations which are based on imperial units. The reader is given the conversions in SI units. However, the bulk of the calculations given here are based on imperial units (conversion factors shown below).

Conversion factors

 $1 \text{ ft} = 0.3048 \text{ m}; 1 \text{ lb/ft}^2 = 47.88 \text{ N/mm}^2$ $1 \text{ lb}f = 4.448 \text{ N}; 1 \text{ lb/ft}^2 = 16.02 \text{ kg/mm}^2$ 1 lbin = 0.113 Nm; 1 kg = 9.806 N; $1 \text{ lb/in}^2 = 6895 \text{ N/mm}^2 1 \text{ in} = 25.4 \text{ mm}$ Dynamic stresses Concrete: Comp — 1.25(3000) = 3750 psi Diagonal tension — 1.00(3000) = 3000 psi Direct shear — 1.10(0.18) (3000) = 600 psi Reinforcement: Bending — 1.10(60,000) = 66,000 psi Shear — 1.10(60,000) = 60,000 psi since f'_c = 3000 psi and f_y (static) = 60,000 psi.

9.5.2 Wall Design

Figure 9.14 shows a one-way slab fully restrained at the supports.

Wall thickness $(T_c) = 300 \text{ mm} (12 \text{ in})$ (see Fig. 9.14).

The US recommended covers are 0.75 in. and 1.5 in. (37 mm) rather than 50 mm (adopted by the Home Office, in the UK).

For a negative moment, d = 12 - 1.5 - 0.3125 = 10.1875 in. (assuming # 5 bars). For a positive moment, d = 12 - 0.750.3125 = 10.935 in.

$$A_{\rm s} = 0.0025 \times 12 \times 10.935 = 0.328 \, in.^2/{\rm ft}$$



Fig. 9.14 Wall analysis and design

#5 bars at 11 in (275 mm), $A_s = 0.34 > 0.328 \text{ in.}^2$ the wall blast load $= 0.085 \text{ N/mm}^2 = 12.33 \text{ lb/in}^2$. The ultimate moment is given by

$$M_{\rm u} = (A_{\rm s} f_{\rm yd}/b)(d-a/2)$$

where $a = A_s f_{yd}/0.85 bft(dyn) = 0.586$ in.

```
b = 12 in.
```

$$M_{\rm u}(\text{positive}) = M'_{\rm p} = 19900 \text{ in.} - 1\text{b/in.}$$
$$M_{\rm u}(\text{negative}) = M'_{\rm N} = 18500 \text{ in.} - 1\text{b/in.}$$
$$\text{E}_{\rm c} \text{ for concrete} = D^{1.5} \{33\sqrt{f_{\rm c}'}\}$$
$$= (150 \text{ lb/in}^3)^{1.5} \times 33(3000)^2$$
$$= 3.32 \times 106 \text{ psi}$$

 $\rho = D = \text{density of concrete} = 150 \text{ lb/in.}^3(23.6 \text{ kN/m}^3)$ $E_s \text{ for steel} = 30 \times 10^6 \text{ psi} (200 \text{ GN/m}^2)$ $n = E_s/E_c = 9.03$

Average moment of inertia for a 1 in. strip.

$$\begin{split} &l_{\rm g} \; ({\rm gross}) = bT_c^3/12 = 144 \; {\rm in.}^4 \\ &T_c \; ({\rm thickness \; of \; the \; wall}) = d \\ &d \; ({\rm average}) = 10.5625 \; {\rm in.} \\ &p \; ({\rm average}) = A_{\rm s}/bd = 0.00268 = \rho_s \\ &l \; ({\rm cracked \; section}) \; {\rm using \; Fig. \; 2.1} \\ &F' = 0.0175; I_{\rm cracked} = I_c = F'bd^3 = 20.6 \; {\rm in.}^4 \\ &I_a = {\rm average \; moment \; of \; inerita \; = \frac{I_{\rm g}+I_c}{2} = 82.3 \; {\rm in.}^4 \\ &Elastic \; (K_{\rm e}) \; {\rm and \; elasto \; - \; plasto \; (K_{\rm ep}) \; stiffness} \\ &K_{\rm e} = (384E_{\rm c}I_{\rm a})/bL^4 = 244 \; {\rm lb/in.}^3; \quad b = 1 \\ &K_{\rm ep} = 384E_{\rm c}I_{\rm a})/5bL^4 = 48.8 \; {\rm lb/in.}^3 \end{split}$$

Elastic and elasto-plastic deflection

$$\delta_e = X_e = r_e/K_e = 10.71/244 = 0.0439$$
 in.
 $\delta_{ep} = X_p - X_c = (r_u - r_e)/K_{ep} = 0.084$ in.
 $X_p = 0.1279$ in.

Equivalent elastic deflection and stiffness

$$X_{\rm E} = X_e + X_p(1 - r_e/r_u)$$

= 0.0793 in
 $K_{\rm E} = r_u/X_{\rm E} = 1.86.8 \, {\rm lb/in}^3$

Load-mass factors and effective mass Fig. 9.14 gives

| $K_{\rm LM}$ | Range |
|--------------|----------------|
| 0.77 | elastic |
| 0.78 | Elasto-plastic |
| 0.66 | Plastic |
| | |

 K_{LM} (elastic and elasto-plastic) = 0.78 (average) K_{LM} (elastic and plastic) = 0.72 (average)

 $M = \rho T_c/g = 150 \times 1 \times 10^6/32.3(1728)$ = 2700 lb - ms²/in.³

 $M_{\text{effetive}} = K_{\text{LM}} \times M = 1944\text{lb} - \text{ms}^2/\text{in.}^3$ Natural period = $T_{\text{N}} = 2\pi \sqrt{(M_e/K_e)} = 20.3 \,\text{ms}$

Where $g = 32.2 \text{ft/s}^2$; $k_{\text{E}} = 186.8$

Response chart parameters Reference is made to Fig. 9.15

Peak pressure B = 12.33 psi Peak resistance r = 14.81 psi The chart $B/r_u = 0.8325 \rightarrow T/T_N = 28/20.3 = 1.38$ $X_m/X_E = 1.50$ as this is < 3 the section is safe

The corresponding $t_{\rm m}/T_{\rm N} = 0.50 \rightarrow t_{\rm m}/t_o = t_{\rm m}/T$ = $(t_{\rm m}/T_{\rm N})/(T/T_{\rm N}) = 0.50/1.38$ = 0.3623

This lies within the range $3.0 > t_m/t_o > 0.1$, hence the response is satisfactory. *Diagonal tension at a distance d from the support*

$$v_u = r_u[(L/2) - d_e]/d_e = 14.81(72 - 10.1875)/10.1875$$

= 89.9 psi

The allowable shear stress, v_c , is given by

$$v_{\rm c} = \phi [1.9 \sqrt{f_{\rm c}' + 2500p}] \le 2.28 \phi \sqrt{f_{\rm c}'}$$

(Where $\phi = 0.85$)

 $v_c = 94.4$ psi, as this is > 89.9 psi, OK with no stirrups

Ultimate shear

$$V_s = r_u L/2.0 = 14.81 \times 144/2.0 = 1066 \, lb/in$$



Fig. 9.15 Maximum response of simple spring-mass system (LU.S Corpe of Engineer, Washington DC)

Allowable shear

$$V_{\rm d} = 0.18 f_{\rm c}(dyn) {\rm bd} = 6050 {\rm lb/in} > 1066 {\rm lb/in}$$

Hence the 300 mm (12 in.) wall designed against the same blast load in both codes (British and US) is safe. The roof slab can be checked in the same way as for the gas explosion, described earlier in the text.

9.6 Lacing Bars

Design of lacing bars

Where lacing bars are needed, the following calculations will help in the design of nuclear shelters. The lacings can be in both the vertical and horizontal directions.

Vertical lacing bars

The wall thickness is kept the same. Data: $d_1 = 10$ in. $s_1 = 22$ in. no of bars = 6; $D_0 = 0.75$ in.

$$d_l = 21 + 1.13 + 2 + 0.75 = 24\,88\,\text{in}.$$

$$Re = 3D_o$$
for $S_1/d_1 = 0.884$

$$(2R_e + D_o)/d_l = 7D_o/d_l = 0.211$$

 L_1 is measured along the centre line of the lacing bar between points *a* and *b*.

$$L_{l} = \frac{s_{l} - (2R_{l} + D_{o})\sin\alpha}{\cos\alpha} + \pi (2R_{l} + D_{o})\left(\frac{\alpha}{180}\right)$$
(9.21)

$$\cos\alpha = \frac{-2B(1 - B) \pm \sqrt{\left\{2B(1 - B)^{2} - 4(1 - B)^{2} + A^{2}\right](B^{2} - A^{2})}}{[2(1 - B)^{2} + A^{2}]}$$

$$A = \frac{s_{l}}{d_{l}} \text{ and } B = \frac{2R + D_{o}}{d_{l}}$$

$$\alpha = 51.5^{\circ}$$

$$A_{v} = (v_{uv} - v_{c})b_{l}S_{l}/\Phi f_{s}(\sin\alpha + \cos\alpha) = 0.378 \text{ in}^{2}.$$
(9.22)

$$A_{v\min} = 0.0015 \ b_{l}s_{l} = 0.330 \text{ in}^{2}.; no. \text{ of bars} = 6; A_{s} = 0.44 \text{ in}^{2}. OK$$

Horizontal lacing bars

No. of bars 6; $D_0 = 0.75$ in.

$$d_{\rm l} = 21.0 + 1.13 + 0.7522.8$$
 in
 $R_{\rm lmin} = 3D_{\rm o}$

for $s_1 d_1 = 20/22.88 = 0.874$

$$(2R_e + D_o)/d_1 = 7D_o/d_1 = 0.229$$

 $A_v = 0.339 in^2.$

 $A_{v\min} = 0.0015 \ b_{1}s_{1} = 0.0015 \times 11 \times 20 = 0.330 \ \text{in}^{2}\text{no of bars} = 6; \ A_{s} = 0.44 \ \text{in}^{2}.$

Still OK.

Additional reinforcement details from the British code are given in Figs. 9.18 and 9.24.

When a ring forced concrete element is subject to a blast load, the element deflects far beyond the stage of well-defined cracking until:

- (1) The strain energy of the element is developed sufficiently to balance the kinetic energy created by the applied load when it comes to rest.
- (2) Fragmentation of the concrete element results in either its partial or total collapse.

For the development of the available energy of the concrete elements, it is necessary to make changes in the reinforcement layouts and details. Each



Fig. 9.16 Length of lacing bar



Fig. 9.17 Lacing reinforcement

element is reinforced symmetrically. The reinforcement and the intervening concrete are laced together, as shown in Figs. 9.16 find 9.17 with continuous bent diagonal bars. This system offers forces which will contribute to the integrity of the protective element. Where structural elements are located outside the immediate high blast intensity, they should be designed without lacing. All other types are given in Figs. 9.18, 9.19, 9.20, 9.21 and 9.22.



Fig. 9.18 Typical laced wall



Fig. 9.19 Typical details for splicing of lacing bars: (a) splice pattern; (b) lacing splice



Fig. 9.20 Typical detail at intersection of two continuous walls



Fig. 9.21 Flextural reinforcement in lacing

9.7 Finite Element Analysis

A 3D isoparametric, finite-element analysis has been carried out by Bangash. Figure 9.25 shows the finite-element mesh scheme for a dynamic model for a nuclear shelter. Figure 9.26 gives the relationships between pressure and time. The results are given in Fig. 9.27.

9.7.1 The Swedish Design and Details

The Swedish code TB78E provides novel details of the nuclear shelter. They are presented here by courtesy of the Civil Defence Administration of Sweden. Figures 9.28 and 9.29 show structural details of a roof slab and sectional details illustrating various reinforcements.

9.8 Damage Classification

Damage to structures or objects above ground can be divided into three categories:



Fig. 9.22 Typical detail at intersection of continuous and discontinuous walls

- Severe damage: A degree of damage that precludes further ijse of the structure or object for its intended purpose, without essentially complete reconstruction. For a structure or building, collapse is generally implied.
- Moderate damage: A degree of damage to principal members that precludes effective use of the structure or object for its intended purpose, unless major repairs are made.
- Slight damage: A degree of damage to buildings resulting in broken windows, slight damage to roofing and cladding, blowing down of light interior partitions and slight cracking of certain walls in buildings.



Fig. 9.23 Reinforcement through section



Fig. 9.24 Section B–B through shelter



Fig. 9.25 Dynamic model for a nuclear shelter



Fig. 9.26 Relationships between pressures and time



Fig. 9.27 Typical results from the finite-element analysis



Fig. 9.28 Structural details - I Swedish code TB78E





detail sections

Fig. 9.29 Structural details - II Swedish code TB78E



Fig. 9.30a Stress trajectories/cracking



Fig. 9.30b Principal stresses for a nuclear shelter (all stresses are maximum principal stresses)

9.9 Blast Loads and Stesses

Table 9.2 and Fig. 9.10 give a summary of the blast loads generated from a bomb burst. Table 9.5 gives generalised data, including allowable stresses used later on in the analysis.

Based on HMSO reports, American Defence Agency carried out limit state analysis for a six-person domestic shelter, as given in Figs. 9.11a and 9.12b. This was designed for a 1 megaton weapon yield, for which the data are given in Table 9.3. For shallow shelters Table 9.4 indicates the blast loads.

9.10 Finite Element Analysis of a Domestic Nuclear Shelter

Figure 9.30 shows a typical finite element mesh for the dynamic analysis of this shelter. Again 20-noded elements representing concrete in the walls and slabs with smeared reinforcements are used to analyse the shelter resistance against a 1 megaton weapon yield. The dynamic pressure p_{do} is applied in the form of nodal loads. Time duration is included corresponding to the specific values of $p_{\rm do}$. The dynamic finite-element analysis together with cracking is given in Chapter 6, and the numerical model for the material law developed for the five-parameter case has been adopted. The program ISOPAR is modified to include the blast loads. The total number of increments considered is 12. The structure is yielded, cracked and crushed in vulnerable areas when assumed to be placed above ground. The same structure is placed underground with 0.5 m overburden. The stress trajectories are plotted. Figures 9.30a shows the cracking of the structure when placed above ground. Figure 9.30b shows the stresses and partial cracking when placed underground. The safety factor for the structure is 3.1 when placed underground and the protection factor based on the HMSO reports [639 - 640] is 4000. The shelter received no damage above ground for $\frac{1}{2}$ Mt yield at a ground zero distance of 20,000 m.

Chapter 10 Elemental Design Analysis for Auxillary Structures Associated with Nuclear Facilities

10.1 General Introduction

In this chapter design calculations are given for auxiliary structures associated with nuclear facilities. They are divided into three parts. Part A deals with the design analysis of steel elements using steel Euorcode EC-3. Part B deals with the design analysis of concrete elements based on Eurocode EC-2. Parts C is developed entirely based on the design of a nuclear laboratory. It is assumed that the dimensions and thicknesses of various elements are in accordance with the nuclear requirements and have satisfied the radioactive and the radiation parameters normally adopted by the respective experts. Any necessary changes and alterations needed must be adhered to the demands imposed by those experts. Part C can only claim on the structural design analysis of the structural elements of the nuclear laboratory, using British Codes such as BS 8110, BS 5950 and other codes.

PART A DESIGN ANALYSIS OF STEEL ELEMENTS FOR AUXILLARY STRUCTURES OF NUCLEAR FACILITIES BASED ON EC-3

10.2 Background to Eurocode EC-3

NV1993-1-1 Eurocode-3. Design of Steel Structures: Part 1.1. General Rules and Rules for Buildings (EC-3) gives general rules for design of all types steel structures. In principle this code covers both ultimate and serviceability limit states. Safety factors are applied to loading (actions) and resistances. The National Application Documents (NAD) have been prepared by the authorities in various CEN member countries including United Kingdom. The U.K version which is followed adds rules for lying forces or actions etc. from BS5950 Part 1. In order to minimise any difficulty that those engineers who are already familiar with BS5950 Part 1 may find in switching to EC-3, many of the EC-3 provisions have been recast into tables and charts to improve their useability. The system of symbols used in EC-3 is at level of sophestication above that used in BS5950 Part 1. Majority of symbols are found quite familiar. The parametric comparisons are as follows:

| Parameter | Symbols (BS5950) | Symbols (EC-3) |
|--|------------------|-----------------|
| Axial force | F | Ν |
| Elastic section modulus | Z | Wel |
| Plastic section modulus | S | W _{pl} |
| Radius of gyration | r | i |
| Conventions of Member Axes | | |
| (a) Definition of longitudinal Axis of a member | ZZ | XX |
| (b) Major Axis of cross-section | XX | YY |
| (c) Minor Axis of cross-section | YY | ZZ |
| Values of γ_m | | |
| (a) When failure is by Plastic yielding | | Ϋмо |
| (b) When failure is by any type of buckling | | ŶMI |
| (c) When failure occurs by any net section at bolt holes | | γ <i>M2</i> |
| | | |

On the analysis side both elastic and plastic methods are allowed. In case of plastic global analysis either rigid plastic or elasto-plastic methods are used in EC-3.

Imperfections

The adverse effects of imperfections are allowed in EC-3. Frame imperfections are included in the global or individual member's analysis.

Classification of cross-section

The main purpose is to identify the extent to which its resistance is modified by the propensity of its compression elements for local buckling which depends on width-to-thickness b/t ratio of the steel elements and upon the patterns of stresses and levels of strains imposed on them.

Various classes

- Class 1:- For plastic global analysis the usage of cross-sections with large rotation capacity, at least at the plastic hinge location. The b/t ratios are efficiently stocky to permit the necessary substantial deformations without local buckling.
- Class 2:- Most rolled sections have b/t values of sufficiently stocky for the cross-section to reach M_{pl} and they are termed Class-2 or compact sections. Here some strain hardening occurs and some limited rotation is possible before falling part of the curve drops (rotation capacity) below M_{pl} .
- Class 3:- Here semi-compact section is envisaged for the section. The values b/t are less. The maximum moment reaches the elastic resistance moment M_{el} but falls short of the M_{pl} , the plastic resistance moment.

Class 4:- In this class, the slender cross-section, the maximum moment is governed by local buckling and occurs at a value less than the elastic moment of resistance. In this case the stress at the extreme fibres reach the yield strength. $f'_y < f_y$

In BS5950 classes 1, 2, 3, 4 as comparison representing plastic, compact, semi-compact and slender classifications, are replaced by the above classes. The principles are the same for classifications.

10.2.1 Axially Loaded Members: Definitions and Formulae

(a) Section properties

Shear lag effects when for outstanding flange elements

$$c \le Lo/20 \tag{10.1}$$

$$b \le Lo/10 \tag{10.2}$$

If they are exceeded, the effective breadth specified in EC-3 should be used.

10.2.2 Tension Members

(a) The design tension resistance is smaller than $N_{pl.Rd}$, the design plastic resistance of the gross area. In this case f_y = yield strength of with γ_{M0} = 1.05 shall be used. The design ultimate resistance of the net area = 0.9 × ultimate tensile strength f_u with γ_{M2} = 1.2.

 $N_{u:Rd} \neq N_{Pl:Rd}$ and can be achieved inductile behaviour as

$$\frac{0.9A_{net}}{A} \ge \begin{cases} f_y \\ f_u \end{cases} \begin{cases} \frac{\gamma_{M2}}{\gamma_{M0}} \end{cases}$$
(10.3)

10.2.3 Compression Members

They shall be designed both for cross-section resistance and buckling resistance. All classes 1, 2, 3 shall be considered. For class 4 sections, the additional moment due to the eccentricity of the centroidal axes of the effective section should be allowed for.

10.2.4 Buckling Resistance

Calculated values of the compressive strength, similar to BS5950 Part 1, in EC-3 are calculated according to various slenderness ratio $\lambda = \frac{\text{buckling length}}{\text{radius of gyration}}$. The

compressive strengths are tabulated against values of $\sqrt[3]{\beta_A}$ in Table 5.14 (a) and (b) for Fe 430 and Fe 510 steels, respectively. Where

> $\beta_A = 1$ for classes 1, 2, 3 cross sections $\beta_A = A_{eff}/A$ for class 4 cross sections

10.3 Beams

The yield strength in shear = $f_v/\sqrt{3}$ which is a plastic shear resistance. Comparing with BS5950 which is 0.6 f_v , the EC-3 takes sometime a lower value of $0.577 f_v$ for a rolled section W_{pl} , the plastic modulus, is used for class 1 or 2 while W_{el} , the elastic modulus is used for class 3, each with γ_{M0} for class 4 cross-section W_{el} and W_{eff} , the effective cross-section with γ_{M1} are both used.

The beams should be checked for the following:

(a) Moment of resistance for cross-section with high shear

(b) Effect of transverse forces on moment of resistance

(c) Lateral torsional buckling

The methods are explained in the examples associated with this part.

10.4 Shear Buckling

Tables and clauses related to shear buckling are given in Section 5.5.6 of the code. This is needed for which the shear failure mode is a consequence of buckling rather than yielding. "Simple post critical method" is a prominant one. Interaction of moment resistance and shear buckling is an important phenomenon which needs full checking. The following relations are to be noted

 $m_{\rm sd} = \max$ value of moment $\leq M_{f:\rm Rd}$, the plastic moment resitance (10.4)

due to two flanges alone

 $v_{sd} = \max$ value of shear $\leq V_{ba \cdot Rd}$, the design shear buckling. (10.5)

10.5 Axially Loaded Member

The following processes are to be noted:

| • • | $Clause 5 \in 1.2$ |
|---|------------------------------|
| (a) A vial force and banding with law sheer | Clause 5.0.1.2 |
| (a) Axial force and bending with low shear | Clause 5.6.1.3 |
| (b) Axial force and bending with high shear | Clause 5.0.1.5 |
| (b) Akhar foree and bending with high shear] | Clause 5.6.1.4 to 5.6.1.5(3) |

 (c) Buckling resistance with combined bending and axial tension and with combined bending and axial compression tacking into consideration major axis bending and minor axis bending.
 Clauses 5.6.3.2 to 5.6.3.4(4)

10.6 Resistance of Webs to Transverse Compression Forces

(a) Crushing resistance
(b) Crippling resistance
(c) Buckling resistance
(d) The choice of transverse stiffness
(e) Flange induced buckling

Note. All these are thoroughly explained in the design examples using various formulae in the EC-3.

10.6.1 WE10.1

A steel beam of Fig. 10.1 has an effective span of 6.5 m fully restrained along length. At one end its simply supported and at the other end is supported by a roller. The beam shall be designed in F_e430 steel (S275) based on EC-3. The followings are unfactored loads:- loads (udl) $g_{kl} + G_{kl} = 15.0$ KN + 41 KN, $q_{kl} + Q_{kl} = 35$ KN + 45KN



Fig. 10.1 A simply supported steel beam (with permanent and variable loads)

Solution:

Factored loads Stiffness bearing length at supports = 50 and 75 mm at concentrated load

- (a) Permanent $g_{dl} = \gamma_G g_{kl} = 20.25 \text{ KN/m}$ distributed concentrated load = $\gamma_Q G_{kl} = 55.35 \text{ KN/m}$ - distributed g_{dl} (total) = 73 KN/m G_{dl} (total) = 122.85
- (b) Variable $q_d = \gamma_Q q_{dl} = 52.55 \text{ KN/m}$ conentrated load $Q_{dl} = \gamma_Q Q_{kl} = 67.5 \text{ KN}$

Trial section and material properties

 $533 \times 210 \times 92UB$ $t_1 = 533.1 \text{ mm}; b = 209.3 \text{ mm}$ $t_w = 10.2 \text{ mm}; t_f = 15.6 \text{ mm}$ $d = 476.5 \text{ mm}; A_v = 58.1 \text{ cm}^2$ $A = 118 \text{ cm}^3; W_{ely} = 2076 \text{ cm}^3$ $W_{Pl.y} = 2366 \text{ cm}^3; c/t_f = 6.71$ $I_y = 55390 \text{ cm}^4; d/t_w = 46.7$ $t \le 40 \text{ mm} \text{ Grade } F_e 430 \text{ (S275)}$ $F_y = 275 \text{ N/mm}^2; F_u = 430 \text{ N/mm}^2$



(b) Bending moment diagram

Classification:-I-section-rolled section = $\frac{c}{t_f} \le 9.2$ Flange :- class I type Web subject to bending when NA @ mid depth For selected item $\frac{d}{t_w} = 46.7$ For I class web $\frac{d}{t_w} \le 66.6$ Section is class I (i) Shear resistance of crossection

 $V_{\rm sd}$ = shear force at x - section $\geq V_{pl,Rd}$

$$V_{pl,Rd} = \frac{AV}{\gamma_{M0}} \left[\frac{f_y}{\sqrt{3}} \right]$$

= $\frac{58.1 \times 10^2}{1.05} \left[\frac{275}{\sqrt{3}} \right] \times 10^{-3} = 879 \text{KN}$
 $V_{\text{sd}} (298.075 \text{KN}) < V_{pl,Rd} = 879 \text{KN } OK$

Hence $533 \times 210 \times 92UB$ is O.K. for shear resistance.

(ii) Moment resistance at x-section
 Coexisting shear force V_{sd} ≤ 0.5V_{pl,Rd}, then the moment of resistance cannot be reduced by shear
 M_{c.Rd} = ^{W_{pl,yfy}}/_{Tmo} for class 1 or 2 section = 620 KNm
 Maximum moment is calculated as 585 < 620 KNm</p>
 The section 533 × 210 × 92UB is sufficient.

(iii) Beam for lateral torsional buckling (LTB) Since it is fully restrained in lateral direction it will not be affected by lateral torsional buckling.

(iv) Shear buckling

For steel grade Fe 430 (s = 275) $\frac{d}{t_w} > 63.8$ For the section $\frac{d}{t_w} = 46.7 < 63.8$ No check is needed.

(v) Resistance of web to transverse forces

The unstiffened web to forces applied to a flange is governed by crushing resistance or by crippling resistance or by buckling resistance. Here stiff bearing length can be taken into consideration.

 S_s = bearing at supports = 50 mm

 S_{ms} = bearing at midspan = 75 mm

Crushing resistance $R_{y.Rd}$ on the web.

At support

$$R_{y.Rd} = (S_s + S_y) \frac{t_w f_{yw}}{\gamma_{m1}}$$

$$S_{y} = t_{f} \left[\frac{b_{f}}{t_{w}} \right]^{0.5} \left[\frac{f_{yf}}{f_{yw}} \right]^{0.5} \left[1 - \left\{ \frac{\gamma_{mo} \sigma_{fE.d}}{f_{yf}} \right\}^{2} \right]^{0.5}$$
$$= 15.6 \left[\frac{20.93}{10.35} \right]^{0.5} \left[\frac{275}{275} \right]^{0.5} [1,0]$$

70.67 mm

$$R_{y.Rd} = (50 + 70.67) \frac{10.2 \times 275}{1.05 \times 10^3} = 322KN$$

But

$$V_{\rm sd} = 298.675 < R_{v.Rd} = 322KN$$

The section is OK

- (1) At mid span Concentrated load = 122.85KN
- (2) Crippling resistance

At supports

$$R_{a.Rd} = 0.5t_{w}^{2} (Ef_{yw})^{0.5} \left[\left\{ \frac{t_{f}}{t_{w}} \right\}^{0.5} + 3\left\{ \frac{t_{u}}{t_{f}} \right\} \left\{ \frac{s_{s}}{d} \right\} \right] \frac{1}{\gamma_{m1}}$$

But $\left\{\frac{s_s}{d}\right\} \le 0.2$ At support $s_s = 50 \, mm$ $\frac{s_s}{d} = \frac{50}{476.5} = 0.105 < 0.2$

$$\gamma_{m1} = 1.05 \quad E = 210 \quad \times \quad 10^3 \ N/mm^2$$

 $R_{a.Rd} = 543 KN$

Maximum Design shear force $V_{sd} = 298.675KN < R_{a.Rd} = 543KN$ The section is O.K At mis span For $S_{sm} = 75mm R_{a.Rd} = 583KN$ And $V_{sd} = 61.425KN < R_{a.Rd} = 583KN$ The web has sufficient crippling resistance When the beam is subject to bending moment, then

$$\frac{F_{sd}}{R_{a.Rd}} + \frac{M_{sd}}{M_{c.Rd}} \le 1.5$$
$$\frac{122.85}{583} + \frac{585}{620} = 1.154 < 1.5 O.K$$

Buckling Resistance At supports:

$$h = 533.1 \text{mm}$$

$$a = 0 \text{ mm}$$

$$b_{\text{eff}} = \frac{1}{2} [h^2 + s_s^2]^{0.5} + a + \frac{s_s}{2}$$

$$= 292.7 \text{ mm} < 535.4 \text{ mm}$$

The buckling resistance of the web $R_{b.Rd} = \frac{B_A f_{cA}}{\gamma m_2}$

$$\beta_{\rm A} = 1, \ A = b_{\rm eff} \times t_w = 2986 \,\rm{mm}^2$$

 $\gamma_{M1} = 1.05, \ \lambda = \frac{2.58}{t_w} = 116.8$
 $f_c = 104 \,\rm{N/mm}^2$

$$R_{b.Rd} = 300 \,\mathrm{KN} > V_{\mathrm{sd}} = 298.675 \,O.K$$

The buckling resistance is sufficient laterally. Serviceability limit state

$$\begin{aligned} \gamma_G &= 1.0, \gamma_Q = 1.0\\ g_d &= 1.0 \times 15 = 15 \,\mathrm{KN/m} \quad (\mathrm{dead})\\ q_d &= 1 \times 35 = 35 \,\mathrm{KN/m} \quad (\mathrm{imposed}) \end{aligned}$$

Concentrated loads

$$G_d = 1.0 \times 41 = 41 KN; Q_d = 1 \times 45 = 45 KN$$

 δ_2 – deflection due to variable load

$$=\frac{5}{384}\left[\frac{q_d L^4}{EI}\right]\left[\frac{1}{48}\left(\frac{Q_d L^3}{EI}\right)\right]$$

 $I = I_y = 553.3 \times 10^6 \,\mathrm{mm^4}; \ E = 210 \times \frac{10^3 \,N}{\mathrm{mm^2}}$

 $\delta_2 = 9.21 \,\mathrm{mm}$

$$\delta_2(\text{limiting}) = \frac{L}{20} = 26 \,\text{mm}$$

$$\delta_2 < \delta_2$$
(limiting) deflection O.K

Hence the section

$$533 \times 210 \times 92UB, Fe(430)S = 275 O.K$$

10.6.2 WE10.2

In the Section 10.6.1, the beam is laterally restrained at the ends only and as a result the span is increased to 90 m.

 g_d = characteristic load 24.2 KN/m (permanent) inclusive γ_G = 1.35 q_d = characteristic variable load = 30 KN/m inclusive γ_Q = 1.5

No concentrated load exists. Design basis EC3 Solution

Total u.d.1 = 54.2 KN/m material grade Fe 430 Shear force = 243 KN γ_{mo} = 1.05

BM diagram parabolic with maximum ordinate = 550 KNm Section $610 \times 305 \times 149 UB$ (Fe430) and s275 Class I section; h = 609.6 mm; b = 304.8 mm, $t_w = 11.9$ mm

 $t_f = 19.7 \text{ mm}, d = 537.2 \text{ mm}; A_v = 79 \text{ cm}^2$ $A = 190 \text{ cm}^2, c/t_f = 7.74; d/t_w = 45.1$ $w_{pl.y} = 4575 \text{ cm}^3, w_{el.y} = 4093 \text{ cm}^3$ $I_y = 124700 \text{ cm}^4; i_{LT} = 7.75 \text{ cm}; a_{LT} = 201 \text{ cm}$ $t \le 40 \text{ mm}; f_v = 275 \text{ N/mm}^2; f_u = 430 \text{ N/mm}^2$

Shear resistance plastic

$$V_{pl.Rd} = \frac{A_V}{\gamma_{M0}} \left\{ \frac{f_y}{\sqrt{3}} \right\} = 1195 \text{ KN}$$
$$V_{sd} = 243 \text{ KN} < V_{pl.Rd} = 1195 \text{ KN}. \text{ O.K section sufficient}$$

Moment resistance applied shear force

$$M_{c.Rd} = \frac{W_{pl.yfy}}{\gamma_{mo}} = 1198 \text{ KNm } 0.5 V_{pl.Rd} = 59.7 > 243$$
$$> M_{sd} = 550 \text{ KNm } O.K. \text{ Section sufficient}$$

Lateral Torsional Buckling (LTB)

Class I rolled I section For loading support:-

$$\left[\frac{k}{c_1}\right]^{0.5} . L = 0.94 = 8460 > 0.35i_{LT} = 2713 \ O.K$$
$$M_{y.sd} \le M_{b.Rd} = \frac{B_w f_b w_{pl,y}}{\gamma_{M1}}$$
$$f_b = \text{bending strength} = \lambda_{LT} \sqrt{B_w}$$

where λ_{LT} = spenderness Equivalent

$$= \frac{\left[\frac{k}{c_1}\right]^{0.5}}{i_{LT}} \bigg/ \left\{ 1 + \frac{\left(\frac{L}{a_{LT}}\right)^z}{25.66} \right\}^{0.25} = 94.5$$

 $M_{b.Rd}$ = buckling resistance moment

$$=\frac{B_w f_b w_{pl.y}}{\gamma_{m1}} = 723.3 KNm > M_{sd} 550 KNm$$

OK for sufficient resistance. Shear Buckling

$$\frac{d}{t_w} > 63.8 \text{ and } \frac{d}{t_w} \text{(chosen section)}$$
$$= 45.1 < 63.8$$

Shear buckling not needed.

Example 10.1 gives a method for checking resistance of the web to transverse forces.

Section 610 × 305 × 149*UB Fe*430,(*S*275) O.K

10.6.3 WE10.3

The ground floor steel column assumed pinned at top and bottom has total length 6.0 m. From the top floors the column receives a total load of 2500KN axially only. Design is steel column based on EC3 of material properties Fe430 (s275, $f_y = 275N/\text{mm}^2$; $f_u = 430 \text{ N/mm}^2$. Show that the column 365 × 368 × 129*UC* class 3 section is adequate for load 2300KN (factor load) *Solution*

$$h = 355.6; \ b = 368.3 \text{ mm}; \ t_w = 10.7 \text{ mm}; \ t_f = 17.5 \text{ mm}; \ d = 290.2 \text{ mm}$$
$$A_v = 43.5 \text{ cm}^2; \ A = 165 \text{ cm}^2; \ i_y = 15.6 \text{ cm}^2; \ i_z = 9.39 \text{ cm}; \ c/t_f = 10.5 \ d/t_w = 27.1 \text{ mm}$$
$$\gamma_{M0} = 1.05; \ \gamma_{M1} = 1.05$$

Compressive Resistance

 $N_{sd} \le N_{c.Rd} = \frac{Af_y}{\gamma_{Mo}}$ class 3 section $N_{c.Rd}$ = design compressive resistance = 4321 $KN > N_{sd}$ = 2300 KN

Section OK against compression.

Buckling Resistance

$$N_{sd} \le N_{c.Rd} = \frac{\beta_{\rm A} f_y A}{\gamma_{M1}}$$

Buckling about *YY* axis $l_y = 1 \times 6000 = 6000$ mm Buckling about *ZZ* axis $l_z = 1 \times 6000 = 6000$ mm

Hence

$$\lambda_y = \frac{l_y}{i_y} = 38.5 < 180$$

 $\lambda_z = \frac{l_z}{i_z} = 63.9 < 180$

The buckling about *YY* axis and $\frac{h}{b} = 0.966 < 1.2$ curve 'b' Table 5.14

 $\beta_A = 1.0 \lambda_y \sqrt{\beta_A} = 38.5 \text{ and } t \le 40 \text{ mm}$ $f_c = 249.5 N/\text{mm}^2$ $N_{b,y,Rd} = 3921 \text{ KN} > 2300 \text{ KN}$

Buckling about ZZ axis

$$\frac{h}{b} = 0.966$$
$$\beta_A = 1.0 t \le 40 \text{ mm}$$
$$\lambda_z \sqrt{\beta_A} = 63.9, f_c = 193 \text{N/mm}^2$$

The design buckling resistance @ZZ axis

$$N_{b.z.Rd} = 3033 \,\mathrm{KN} > N_{sd} = 2700 \,\mathrm{KN}$$

Section 356 × 368 × 129UC Fe430 (S275) O.K



Fig. 10.2 Axially load column with pinned end

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Fig. 10.3 Steel column under axial load and biaxial moment

PART B DESIGN ANALYSIS OF CONCRETE ELEMENTS FOR AUXILARY STRUCTURES OF NUCLEAR FACILITIES BASED ON EC-2

10.7 A Brief of Systematic EC-2 Design

Suitable dimensions for b and d can be decided by a few trial calculations as follows

1. For no compression reinforcement

$$K = M/bd^2 f_{ck} < K_{bal} \tag{10.6}$$

where

$$K_{bal} = 0.167 \, for \, f_{ck} \le C50 \tag{10.7}$$
With compression reinforcement it can be shown that

$$M/bd^2 f_{ck} < 8/f_{ck} \tag{10.8}$$

approximately, if the area of bending reinforcement is not to be excessive.

- 2. The maximum design shear force $V_{Ed,\max}$ should not be greater than 0.1 $8b_w$ $d(1-f_{ck}/250)f_{ck}$. To avoid congested shear reinforcement, $V_{Ed,\max}$ preferably be somewhat closer to half (or less) of the maximum allowed.
- 3. The span-effective depth ratio for spans not exceeding 7 m should be within the basic values given of the code. For spans greater than 7 m the basic ratios are multiplied by 7/span.
- 4. The overall depth of the beam is given by

$$h = d + cover + t \tag{10.9}$$

where t = estimated distance from the outside of the link to the centre of the tension bars, see Fig. 10.4. For example with nominal sized 12 mm links and one layer of 32 mm tension bars, t = 28 mm approximately. It will, in fact, be slightly larger than this with deformed bars as they have a larger overall dimension than the nominal bar size.

5. Calculate

$$z = d \left[0.5 + \sqrt{0.25 - \frac{K}{1.134}} \right]$$
(10.10)

6. Calculate

$$A_s = \frac{M}{0.87 f_{ykz}} \tag{10.11}$$

7. Check that the area of steel provided is within the maximum and minimum limit required.



Fig. 10.4 Beam dimensions

10.7.1 Rectangular Sections with Tension and Compression Reinforcement with Moment Redistribution Applied (Based on the UK Annex to EC2)

The steps in the design are

8. Calculate

$$X_{bal} \le (\delta - 0.4)d\tag{10.12}$$

9. Calculate

$$K = M/bd^2 f_{ck} \tag{10.13}$$

10. Take K_{bal} from Table 7.1 or alternatively calculate

$$K_{bal} = 0.454(\delta - 0.4) - 0.182(\delta - 0.4)^2 \text{ for } f_{ck} \le C50$$
(10.14)

If $K > K_{bal}$, compression steel is required.

11. Calculate the area of compression steel from

$$A'_{s} = \frac{(K - K_{bal})f_{ck}bd^{2}}{f_{sc}(d - d')}$$
(10.15)

where f_{sc} is the stress in the compression steel

If $d'/x \le 0.38$ the compression steel has yielded and $f_{sc} = 0.87 f_{yk}$ If $\frac{d'}{x} > 0.38$ then the strain ε_{sc} in the compressive steel must be calculated from the proportions of the strain diagram and $f_{sc} = E_s \varepsilon_{sc} = 200 \times 10^3 \varepsilon_{sc}$

12. Calculate the area of tension steel from

$$A_{s} = \frac{K_{bal}f_{ck}bd^{2}}{0.87f_{vkz}} + A'_{s}\frac{f_{sc}}{0.87f_{vk}}$$
(10.16)

where $z = d - 0.8 X_{bal}/2$

13. Check Eq. 7.5 for the areas of steel required and the areas provided that

$$\left(A_{s.prov}' - A_{s.req}'\right) \ge \left(A_{s.prov} - A_{s.req}\right) \tag{10.17}$$

This is to ensure that the depth of the neutral axis has not exceeded the maximum value of X_{bal} by providing an over-excess of tensile reinforcement.

10.7.2 Design of Shear

The theory and design requirements for shear have been covered in EC3 and the relevant design equations were derived based on the requirements of EC2 using the variable strut inclination method.

The shear reinforcement will usually take the form of vertical links or a combination of links and bent-up bars. Shear reinforcement may not be required in very minor beams such as door or window lintels with short spans of less than say 1.5 m and light loads.

The following notation is used in the equations for the shear design

- A_{sw} = the cross-sectional area of the two legs of the stirrup
- s = the spacing of the stirrups
- z = the lever arm between the upper and lower chord members of the analogous truss
- f_{ywd} = the design yield strength of the stirrup reinforcement
- f_{vk} = the characteristic strength of the stirrup reinforcement
- V_{Ed} = the shear force due to the actions at the ultimate limit state
- V_{wd} = the shear force in the stirrup
- $V_{rd.s}$ = the shear resistance of the stirrups
- $V_{Rd,max}$ = the maximum design value of the shear which can be resisted by the concrete strut

10.7.3 Vertical Stirrups or Links

The procedure for designing the shear links is as follows

- 14. Calculate the ultimate design shear forces V_{Ed} along the beam's span.
- 15. Check the crushing strength $V_{Rd.max}$ of the concrete diagonal strut at the section of maximum shear, usually at the face of the beam support.

For most cases the angle of inclination of the strut is $\theta = 22^{\circ}$, with $\cot \theta = 2.5$ and $\tan \theta = 0.4$ so that from Eq. 5.6:

$$V_{Rd.max} = 0.1\,24b_w d\,\left(1 - f_{ck}/250\right)f_{ck} \tag{10.18}$$

and if $V_{Rd,max} \ge V_{Ed}$ then go to step (16) with $\theta = 22^{\circ}$ and $\cot \theta = 2.5$, but if $V_{Rd,max} < V_{Ed}$ then $\theta > 22^{\circ}$ and θ must be calculated from Eq. 10.18 as VEd 1

$$\theta = 0.5 \sin^{-1} \left\{ \frac{V_{Ed}}{0.18 b_w df_{ck} (1 - f_{ck}/250)} \right\} \le 45^{\circ}$$

16. The shear links required can be calculated from Eq. 10.19

$$\frac{A_{sw}}{s} = \frac{V_{Ed}}{0.78 df_{yk} \cot \theta}$$
(10.19)

where A_{sw} is the cross-sectional area of the legs of the stirrups ($2 \times \pi \phi^2/4$ for single stirrups)

For a predominately uniformly distributed load the shear V_{Ed} should be taken at a distance *d* from the face of the support and the shear reinforcement should continue to the face of the support.

17. Calculate the minimum links required by EC2 from

$$\frac{A_{sw,min}}{s} = \frac{0.08f_{ck}^{0.5}b_w}{f_{yk}}$$
(10.20)

and the shear resistance for the links actually specified

$$V_{min} = \frac{A_{sw}}{s} \times 0.78d f_{yk} \cot\theta \tag{10.21}$$

This value should be marked on the shear force envelope to show the extent of these links.

18. Calculate the additional longitudinal tensile force caused by the shear force

$$\Delta F_{td} = 0.5 V_{Ed} \cot\theta \tag{10.22}$$

This additional tensile force increases the curtailment length of the tension bars. The minimum spacing of the links is governed by the requirements of placing and compacting the concrete and should not normally be less than about 80 mm. EC2 gives the following guidance on the maximum link spacing:

(a) Maximum longitudinal spacing between shear links in a series of links

$$S_{1,max}0.75d(1+\cot\alpha)$$

where α is the inclination of the shear reinforcement to the longitudinal axis of the beam.

(b) Maximum transverse spacing between legs in a series of shear links

$$S_{b,max} = 0.75d \ (\le 600 \ mm)$$

Types of links or stirrups are shown in Fig. 7.15. The open links are usually used in the span of the beam with longitudinal steel consisting of top hanger bars and bottom tensile reinforcement. The closed links are used to enclose

top and bottom reinforcement such as that near to the supports. Multiple links are used when there are high shear forces to be resisted.

10.7.4 Floor Slab with Different and Boundary Conditions

After evaluating moments, the rest of the procedures given in the EC3 shall be followed.

10.7.5 Short and Slender Columns in Reinforced Concrete

10.7.5.1 Slenderness Ratio of a Column

The slenderness ratio of a column bent by an axis is given by

$$\lambda = \frac{l_o}{L^\circ} = \frac{l_o}{\sqrt{I/A^\circ}} \tag{10.23}$$

where $l_o =$ effective height of the column

i = radius of gyration about an axis

I = second momment of inertia

A = the cross - sectional area of the

 l_o the effective height , based on EC2 gives two formulae:

$$l_o = 0.5 l \sqrt{\left(1 + \frac{k_1}{0.45 + k_1}\right) \left(1 + \frac{k_2}{0.45 + k_2}\right)} (\text{braced members})$$
(10.24)

$$l_o = l \sqrt{1 + 10 \frac{k_1 k_2}{k_1 + k_2}} \tag{10.25}$$

and

$$l_o = l \left(1 + \frac{k_1}{1 + k_1} \right) \left(1 + \frac{k_2}{1 + k_2} \right)$$
(10.26)

The values k_1 and k_2 are respectively relative flexibilities and rotations. The restraints at ends 1 and 2 of the columns respectively do exist.

At each end k_1 and k_2 can be taken as

$$k = \frac{\text{column stiffness}}{\sum \text{ beamstiffness}} = \frac{\left(\frac{EI}{T}\right)_{\text{column}}}{\sum 2\left(\frac{EI}{T}\right)_{\text{beam}}} = \frac{\left(\frac{I}{T}\right)_{\text{column}}}{\sum 2\left(\frac{I}{T}\right)_{\text{beam}}}$$
(10.27)

A typical column is a symmetrical frame with spans of approximately equal length, k_1 and k_2 can be calculated as

$$k_1 = k_2 = k \frac{\left(\frac{I}{l}\right)_{\text{column}}}{\sum 2\left(\frac{I}{l}\right)_{\text{beam}}} = \frac{\left(\frac{I}{l}\right)_{\text{column}}}{2 \times 2\left(\frac{I}{l}\right)_{\text{beam}}} = \frac{I\left(\frac{I}{l}\right)_{\text{column}}}{4\left(\frac{I}{l}\right)_{\text{beam}}}$$
(10.28)

The EC2 places an upper limit on a slenderness ratio of a single member below which second-order effects can be ignored.

$$\lambda_{\text{limit}} = 20 \times A \times B \times C / \sqrt{n} \tag{10.29}$$

$$A = 1/(1 + 0.2\phi_{\rm ef}); B = \sqrt{1 + 2w}; \ c = 1.7 - \gamma_m$$
(10.30)

The following conditions apply to the value of C:

- (a) If the end moments M_{01} and M_{02} give rise to tension on the same side of the column r_m should be taken as positive from which it follows that $C \le 1.7$.
- (b) If the converse to (a) is true, i.e the column is in a state of double curvature, then r_m should be taken as negative from which it follows that C > 1.7.
- (c) For braced members in which the first-order moments arise only from transverse loads or imperfections; *C* can be taken as 0.7.
- (d) For unbraced members, C can be taken as 0.7.

For an unbraced column an approximation to the limiting value of λ will be given by

$$\lambda_{\text{limit}} = 20 \times A \times B \times C/_{\sqrt{n}} = 20 \times 0.7 \times 1.1 \times 0.7/\sqrt{N_{ED}/(A_s f_{cd})}$$
$$= 10.8/\sqrt{N_{ED}/(A_s f_{cd})}$$
(10.31)

The limiting value of λ for a braced column will depend on the relative value of the column's end moments that will normally act in the same clockwise or anti-clockwise direction as in case (b) above. If these moments are of approximately equal value then, $r_m = -1, C = 1.7 + 1 = 2.7$ and a typical approximate limit on λ will be given by

$$\lambda_{\text{limit}} = 20 \times A \times B \times C/_{\sqrt{n}} = 20 \times 0.7 \times 1.1 \times 0.7/\sqrt{N_{ED}/(A_s f_{cd})}$$

= 41.6/\sqrt{N_{ED}/(A_s f_{cd})} (10.32)

Alternatively for a braced column the minimum limiting value of λ will be given by taking C 1.7. Hence

$$\lambda_{\text{limit}} = 20 \times A \times B \times C/_{\sqrt{n}} = 20 \times 0.7 \times 1.1 \times 0.7/\sqrt{N_{ED}/(A_s f_{cd})}$$
$$= 26.2/\sqrt{N_{ED}/(A_s f_{cd})}$$
(10.33)

If the actual slenderness ratio is less than the calculated value of λ_{limit} then the column can be treated as short. Otherwise the column must be treated as a slender one and the second-order effects must be accounted for in the design of the column.

10.7.6 WE.10.5

A simply supported beam of an effective span of 6.0 m is subject to permanent load $g_k = 60KN/m$ inclusive self-weight and variable load q_k of 18KN/m. Design this beam taking into consideration $f_{ck} = 30 N/mm^2$; $f_{yk} = 500 N/mm^2$

Solution

Ultimate loading and maximum moment Ultimate load $w_u = (1.35g_k + 1.5q_k)kN/m$

$$= (1.35 \times 60 + 1.5 \times 18) = 108 KN/m$$

Maximum design moment $M = \frac{w_{ij}L^2}{8} = \frac{108 \times 6.0^2}{8} = 486$ kNm Bending reinforcement

$$K = \frac{M}{bd^2 f_{ck}} = \frac{486 \times 10^6}{300 \times 540^2 \times 30} = 0.185 > k_{bal} = 0.167$$

Therefore compression reinforcement, A'_s is required.

$$d'/d = \frac{50}{540} = 0.092 < 0.171$$
 therefore $f_{sc} = 0.87 f_{yk}$

Compression steel

$$A'_{s} = \frac{(k - k_{bal})bd^{2}f_{ck}}{f_{sc}(d' - d)}$$
$$= \frac{(0.185 - 0.167) \times 30 \times 300 \times 540^{2}}{0.87 \times 500(540 - 50)} = 222 \text{mm}^{2}$$

Provide H16 bars, $A'_z = 402 \text{ mm}^2$ Tension steel, $A_s = \frac{0.167bd^2 f_{ck}}{0.87 f_{ykz}} + A'_s$ $I_a = 0.82$ therefore of steel as

$$A_s = \frac{0.167 \times 30 \times 300 \times 540^2}{0.87 \times 500 \times (0.82 \times 540)} + 222$$
$$= 2275 + 222 = 2497 \,\mathrm{mm}^2$$

Provide 2NOH32 bars and 2NOH25 bars, area 2592 mm², 100 $A_s/bd =$ 1.6 > 0.15.

Two bars are curtailed near the support. Tension bars shall be anchored over the support.

Span-effective depth ratio

$$\rho = 100A_{sreq}/bd = (100 \times 2497)/(300 \times 540) = 1.54\%$$

 $A_s = 2$ NOH32 and 2NOH25 steel $A'_s = 2$ NOH16

From Table 6.10 or Fig. 6.3 basic span-effective depth ratio = 14Modification for steel area is provided as

Modified ratio = $14.0 \times \frac{2592}{2497} = 14.5$ Span-effective depth ratio provided = $\frac{6000}{540} = 11.1 <$ allowable upper limit O.K

10.7.7 WE10.6

A simply supported T-beam 600 mm (Fig. 10.4(b)) flange width and overall height 580 mm with a 6 m span is subjected to the design ultimately distributed load of 40 KN/m. As shown in Fig. 10.5, the beam has flange thickness of 150 mm and web thickness is 250 mm. Using $f_{ck} = 25 N/mm^2$ and $f_{vk} = 500$ N/mm^2 design the beam based on EC2

Solution

$$B.M_{\rm max} = \frac{40 \times 6^2}{8}$$
$$= 180 \,\rm KNm$$

Longitudinal reinforcement

$$\frac{M}{b_f d^2 f_{cx}} = \frac{180 \times 6^2}{600 \times 530^2 \times 25} = 0.0273$$

$$l_a = 0.95$$

$$z = \text{lever arms} = l_a d = 0.95 \times 530 = 503 \text{ mm}$$

$$s = \text{depth of stress block} = 2(d - z) = 54 \text{ mm} < b_f = 150 \text{ mm}$$

$$A_s = \frac{M}{0.87 f_{ykz}} = \frac{180 \times 6^2}{0.87 \times 500 \times 503} = 823 \text{ mm}^2$$

Provision: 2 No. H25 bars; $A_s = 982 \text{ mm}^2$ For these bars

$$\frac{100A_s}{b_w d} = \frac{100 \times 982}{250 \times 530} = 0.74\% > 0.13\%$$

Transverse steel in the flange



Fig. 10.4(a) Simply supported T beam



Fig. 10.4(b) T-section

Fig. 10.5 Type of shear link



Using the code Section 5.14

$$\Delta x = 0.5 \frac{L}{2} = \frac{6000}{4} = 1500 \,\mathrm{mm}$$

 $\Delta M = \text{change in moments over distance } \Delta x = \frac{L}{4} \text{ from moment}$ $= \frac{w_u L}{2} \times \frac{L}{4} - \frac{w_u L}{8} \cdot \frac{L}{8} = \frac{3 \times 40 \times 6^2}{32} = 135 \text{ KNm}$

The change in the longitudinal force ΔF at the flange web interface is

$$=\frac{\Delta M}{(d-h_f/2)}\left[\frac{(b_f-b_w)/2}{b_f}\right]=87\mathrm{KN}$$

 V_{Ed} = Longitudinal shear

$$Stress = \frac{\Delta F_d}{h_f \times \Delta x} = \frac{87 \times 10^3}{150 \times 1500} = 0.4 \text{ N/mm}^2$$

Check the concrete steel strength

To prevent crushing of the compressive steel in the flange

$$V_{Ed} \le \frac{0.6((1 - f_{ck})/250)f_{ck}}{1.5(\cot\theta_f + \tan\theta_f)}$$

Note:- moments are sagging-compression steel in the flange



 $\leq 5.4N/mm^2 > 0.43N/mm^2$

And the concrete strength has sufficient strength for flange in tension θ is $45^{\circ} > 38.6^{\circ}$.

Limits for $\theta f 26.5^\circ \le \theta f \le 45^\circ$ take $\theta f = 26.5^\circ$ mini.

Transverse steel

Transverse shear reinforcement required if

 $v_{Ed} \ge 0.27 f_{ctk} = 1.85 \text{N/mm}^2$ for 25 grade of concrete $0.27 f_{ck} = 0.49 \text{N/mm}^2 > 0.43 \text{ N/mm}^2$

Transverse reinforcement *Not Needed* A minimum are 0.13%

 $A_{sf} = 0.1bh_f/100 = 0.13 \times 1000 \times 150/100 = 195 \,\mathrm{mm}^2/\mathrm{m}$

Provide $H10@300 = 262 \text{ mm}^2/\text{m}$

Reinforcement



(c) Reinforcement details

Fig. 10.7

10.7.8 WE10.7

A simply supported slab, spanning 5 m as an effective span is to be designed using EC2. The following data are taken:

1. Floor finishes + ceiling loads = 1KN/m², basic span/depth = 0.19

2. Variable load = $3KN/m^2$ Characteristic material properties: $f_{ck} = 25N/mm^2$; $f_{yk} = 500N/m^2$ Class × c1 exposure cover = 25 mm (c25/30) l = 25%

Solution

Slab depth = span/depth = 27 take 40% more Minimum depth = span/27 × correction factor c.f

$$=\frac{5000}{27} \times c.f = 185.6/c.f$$

Since the span < 7 m; c.f = 1.0Overall depth of the slab = 185.6 + 25 + 5 = 215.6 mmTake initially the slab 200 mm on trial basis with d = 170 mmSelf-weight = $200 \times 25 \times 10^{-3} = 5 \text{ KN/m}^2$ Total permanent load = $1 + 5 = 6 \text{ KN/m}^2$ Ultimate load parameter width of the slab = $(1.35g_k + 1.5q_k)$ (5.0) = $(1.35 \times 6 + 1.5 \times 3) (5.0) = 63.0 \text{ KN}$ M = ultimate moment = $63 \times 5/8 = 39.375 \text{ KNm}$

$$\frac{M}{bd^2 f_{ck}} = \frac{39.375}{1000} \times (170)^2 \times 25 = 0.054$$

Code:- $l_a = 0.96$ adopt upper limit = 0.95; $z = \text{lever arm } l_a \text{d} = 0.95 \times 170$ = 161 mm $A_s = \text{area of steel} = M/0.87 f_{ykz} = 562 \text{ mm}^2$ Provide H12-150; $A_s = 754 \text{ mm}^2$ Check span-depth ratio = $\frac{100(562)}{1000(170)} = 0.33 > 0.13\% \text{ min}$ Code: span/depth = 32 while actual span/depth = $\frac{5000}{170} = 29.41$ Hence the chosen depth is OK. Shear at the face of the support v_{Ed}

shear
$$v_{Ed} = \frac{61.7}{2} \left[\frac{2.25 - 0.5 \times 0.3}{2.25} \right] = 28.79 \text{ KN}$$

 $P_1 = \frac{100 \times 754}{1000 \times 170} = 0.44$
 $v_{R.dc} = v_{R,dc} bd, \quad V_{R,dc} = 0.55 \text{ around}, \quad \rho_1 = 0.4 \text{ no adjustment}$
 $= 0.55 \times 1000 \times 170 = 0.935 \text{ KN}$



Fig. 10.8 A simply supported slab

Enchorage length = $40\phi = 40 \times 12 = 480 \text{ mm}$ Distributed steel = $0.13bd = 0.13 \times 1000 \times 170 = 221 \text{ mm}^2/\text{m}$ Provided H12–300:- $A'_s = 377 \text{mm}^2/\text{m} > 22 \text{ mm}^2/\text{m}$ The slab reinforcements are shown in Fig. 10.8.

10.7.9 WE10.8

Assuming the column is in a braced frame using EC2 and the following data: Ultimate axial load = 1279KN; column = 400×300

 λ_{yy} = heighest slenderness ratio; beam of the frame 300×500 $f_{ex} = 25 \text{ N/mm}^2$; hcolumn = 3 m; $l_{\text{beam}} = 4 \text{ m}$; $l_o = 0.59 \times 3.0 = 1.77 \text{ m}$

Solution

$$I_{col} = 400 \times 300^{2}/12 = 9 \times 10^{8} \text{mm}^{4}$$

$$l_{beam} = 300 \times 500^{3}/12 = 31.25 \times 10^{8} \text{mm}^{4}$$

$$k_{1} = k_{2} = \frac{\frac{I_{col}}{l_{col}}}{\sum \left(\frac{21_{beam}}{l_{beam}}\right)} = \frac{\frac{40 \times 10^{8}}{3} \times 10^{8}}{\frac{2(2 \times 3.12 \times 10^{8})}{4} \times 10^{3}} = 0.96$$

$$\lambda = \frac{l_{o}}{i} = 20.4$$

$$i = \text{radius of gyration} = \sqrt{\frac{bh^{3}/12}{bh}}$$

$$= 86.6 \text{ mm}$$

$$\lambda_{Lrm} = limited \ slenderness \ ratio = \sqrt{\frac{26.2}{\{N_{Ed}/A_{c}, f_{cd}\}}}$$

 $f_{cd} = \frac{25}{1.5} = 16.67$ Hence $\lambda_{Lim} = 26.2\sqrt{\left\{\frac{1279}{400 \times 300 \times 16.67}\right\}} = 32.8 > 20.4 = \lambda$ The column is short since $\lambda_{Lim} > \lambda$.

10.7.10 WE10.9

A slender column 450 × 350 mm cross-section is subject to an ultimate load of 1650 KN and end moments at A = 65 KNm and at B = 10 KNm as shown in Fig. 10.9. The double curvature exist about y-y axis. Use the following data and EC2 design requirements, check the sufficient reinforcement are catered for $l_{ey} = 6.75$ m; $l_{ez} = 7.5$ m; $f_{yk} = 500$ N/mm²; $\phi_{eff} = creep$ ratio = 0.87. Solution

Solution

$$e_{ob} = \frac{MB}{N_{Ed}} = = 6.06 \,\mathrm{mm};$$

 $e_{oA} = \frac{MA}{N_{Ed}} = \frac{-65 \times 10^3}{1650} = -40.0 \text{ mm} \text{ (column bent in double base curvature)}$

Limiting slenderness ratio

$$A = \frac{1}{(1+0.2\phi_{eff})} = 0.85$$

$$B = \text{the default value 1.1}$$

$$C = 1.7 - \frac{M_{oB}}{M_{oA}} = 1.7 - \frac{10}{65} = 1.854$$

$$\lambda_{Lim} = [20 \times A \times B \times C] / \sqrt{n}$$

$$[20 \times A \times B \times C] / \sqrt{N_{Ed} / A_c f_{cd}}$$



Fig. 10.9 Axial load with two acting moments

$$\frac{20(0.85)(1.1)\times1.854}{\sqrt{\frac{1650\times10^3}{300\times450\times0.567\times25}}}$$

 $\lambda_{\text{Lim}} = 43.71;$
Actual slenderness ratio
 $\lambda_y = \frac{l_{ey}}{l_z} = \frac{6.75}{0.3} \times 3.46 = 77.85 > 43.71$
 $\lambda_z = \frac{l_{ex}}{l_z} = \frac{7.5}{0.45} \times 3.46 = 61.35 > 31.19$

The column is parallel to be slender and λ_y is critical. Equivalent eccentricities = e

$$0.6e_{oA} + 0.4e_{oB} = 0.6(40) + 0.4(-6.06)$$

= 24.0 - 2.424 = 21.576 mm
$$0.4e_{oA} + 0.6 = 0.4(40) = 16 \text{ mm}$$

Hence v =accidental eccentricity $= \frac{1}{200}$

$$e_{eq} = v \frac{l_{ey}}{2} = 16.88 \text{ mm}$$
$$e_{so2} = \text{second} - \text{order eccentricity}$$
$$= \frac{k_1 k_2 l_o^2 f_{yk}}{\pi^2 (103500d)}$$

Since $k_1 = \left(1 + 0.354 + \frac{f_{ck}}{200} - \frac{\lambda}{150}\right) \phi_{eff} = 0.96 \ge 1$ Hence $e_{so2} = 92.92$ mm Initial value of $k_2 = 1$ is taken prior to iteration

First iteration

 $e_{tot} = e_{total} = e_o + e_{eq} + e_{so2} = 21.756 + 16.88 + 92.92 = 131.556 \,\mathrm{mm}$

$$M_{total} = M_{tot} = N_{Ed} \cdot e_{tot} = 1650 \times 131.556 \times 10^{-3}$$

$$\frac{N_{Ed}}{bhf_{ck}} = \frac{1650 \times 10^{-3}}{450 \times 300 \times 25} = 0.489$$

$$\frac{M_{tot}}{bh^2 f_{ck}} = {}^{217 \times 10^6} / {}_{450 \times 300 \times 25} = 0.214$$

From standard design chart on EC2

$$\frac{A_s f_{yk}}{b h f_{ck}} = 0.8 \text{ looking at the chart } k_2 = 0.78$$

Second iteration

Similarly when $k_2 = 0.78$; $e_{so2} = 72.48$; $e_{tot} = 111.116$ mm

$$M_{tot} = 183 \text{ KNm}; \frac{A_s f_{yk}}{bhf_{ck}} = 0.8; \frac{M_{tot}}{bh^2 f_{ck}} = 0.158$$

 $A_s = \frac{0.6bhf_{ck}}{f_{yk}} = 4050 \text{ mm}^2 \ k_2 = 0.74$

$$N_{\text{balance}} = 0.29 f_{ck} A_c = 0.29 \times 25 \times 450 \times 300 \times 10^{-3} = 978 \text{ KN}$$
$$N_{Ed} = 0.567 f_{ck} A_c = 0.87 f_{yk} A_s = 3675 \text{ KN}$$

$$k_2 = \frac{3675 - 1650}{3675 - 978} = 0.75 \text{ is almost } k = 0.74 \text{ above}$$

PART C A NUCLEAR LABORATORY CASE STUDY BASED ON BRITISH CODES

10.8 A Nuclear Laboratory: A Case Study

10.8.1 Proposal and Preliminary Data

The provision is for an open laboratory involving only British Codes such as BS 8110, BS 5950 and BS 6399. Here a general design is given. The clear height is given to be 408 m from the nuclear concerns with a clear structural layout necessary for a number of classified testing and storage facilities. The nuclear concerns allocated an area of $50m \times 50m$. Many options regarding the structural layout can be available. Figures 10.10 and 10.11 are the structural schemes proposed for this text. A composite steel frame is chosen. The roof and cladding are of precast concrete units. It is proposed to have a concrete slab for the roof to withstand the blast load. The vertical frame is of trust type matching the roof truss supporting the concrete slab with the vertical stanchions made up of trusses. The stanchions or column are designed to withstand extreme wind loads and blast effects. Cladding play a significant part to resist such loads. Since the building is to be clayed in precast concrete units with insulation board combgated steel cover. The main door is to be top up hung when it is open to give a clear opening of $30 \text{ m} \times 40 \text{ m}$. Several doors are be located for access to personnel. They should not be more than 3.

10.8.2 Loadings

- (a) Roof = 3 KN/m^2
- (b) Point load applied 500 KN + 10% impact to roof loading at the centre



Fig. 10.10 Structural elevational details



Fig. 10.11

- (c) Internal blast pressure = 5 KN/m^2
- (d) basic design wind speed = 40 m/sec

10.8.3 Site Condition

0.0–0.31m fill 0.31–2.5m clayeysilt 0.25–18.0m solid chalk

Ground water not allowed.

The bearding capacity for the soil type is evaluated as 75 KN/m^2 Piles and pile caps can be a possibility.

10.8.4 Loading on the Roof

1. Downward loading Imposed load = 3 KN/m^2 (adverse) Dead load = snow load + finishes + dead load (adverse)= 0.75 + 1.5 +self-weight Assuming 200 mm slab Self-weight = $0.2 \times 24 = 4.8 \text{ KN/m}^2$: Deadload = $0.75 + 1.5 + 4.8 = 7.05 \text{ KN/m}^2$ Design load = $1.6 \times LL + 1.4 \times DL$ $= 1.6 \times 3 + 1.4 \times 4.8$ $= 14.67 \text{ KN/m}^2$ 2. Upward loading Imposed load = 2 KN/m^2 (benificial) Imposed load = 5 KN/m^2 blast load (adverse) Dead load = finishes + self-weight (benificial) $= 1.5 + 0.2 \times 24$ $= 6.3 \text{ KN/m}^2$ Design load = $-6.3 \times 1.4 - 3 \times 1.6 + 5 \times 1.6$ = -5.62 KN ie downward

The downward loading is chosen for this is the worse case. The negative value in the second calculation shows when blasting occurs. The load is balanced by the downward imposed load, dead load and self-weight of the roof slab.

Design load = 14.67 KN/m^2

10.8.5 Design of Roof Slab

The roof slab will be connected to the top beam flange by bolting, it is assumed that the slab is simply supported at four sides. For in reality it is actually partially fixed, reinforcement is provided at the top of the slab to overcome the fixed end moment.

In general this type of slab could deflect about both axis under load and the corner lift and curl up from supports causing torsional moments then the moment coefficient is used and the maximum moments are given by

$$M_{sx} = \alpha \ S_x \ nL^2 x$$

And

$$M_{sv} = \alpha S_v n L^2 x$$

Where M_{sx} = moment at the mid span on the strips of unit width in Lx direction;

 M_{sy} = moment at the mid span on the strips of unit width in Ly direction;

n = total ultimate load per unit area;

Lx = the length of the short side;

Ly = length of the long side;

 αS_x and $= \alpha S_y$ are the moment coefficients.

Design for bending and short span of slab



Fig. 10.12 Loading area of the roof slab. (a) Slab depth

Lx = 3.25 m

Table cover = 40 mm

$$d = 200 - 40 = 160$$

$$M_{sx} = \alpha S_x n L^2 x$$

$$= 0.118 \times 14.67 \times (3.25)^2 = 18.28 \text{ KNm}$$

$$\frac{M_{sx}}{bd^2 f_W} = \frac{18.28 \times 10^6}{1000 \times (160)^2 \times 30} = 0.023$$

(a)



Lever arm, $z = 0.94d = 0.94 \times 160 = 150 \text{ mm}$

$$A_s = \frac{M_{sx}}{0.87 f_{yz}} = \frac{18.28 \times 10^6}{0.87 \times 460 \times 150} = 305 \,\mathrm{mm} = \mathrm{per} \,\mathrm{m} \,\mathrm{width}$$

Use T12 @ 300 centre-to-centre checking for maximum span

$$\frac{M_{sx}}{bd^2} = \frac{18.28 \times 10^6}{1000 \times (160)^2} = 0.71$$

Service stress $= \frac{5}{8} \times 460 \times \frac{305}{377} = 233$

 $maximum \frac{span}{effective depth} = 20 \times 1.8 = 36m$ Reactual $\frac{span}{effective depth} = \frac{3250}{160}$ = 20.3 m < 36 m *O.K* 200 mm thick slab is adequate

10.8.6 Design for Bending and Long Span of Slab

$$M_{sy} = \alpha S_y n L^2 x$$

= 0.029 × 18.28 × (3.25)² = 5.6 KNm

As this reinforcement is at inner depth after the previous one the effective depth is reduced to

$$Z = 160 - 12 = 148 \text{ mm}$$

$$\therefore A_z = \frac{M_{sy}}{0.87 f_{yz}} = \frac{5.6 \times 10^6}{1000 \times 200} = 95 \text{ mm/m width}$$

$$\frac{100A_s}{bh} = \frac{100 \times 95}{1000 \times 200} = 0.05 < 0.13$$

Minimum transverse steel ratio = 0.13

$$\frac{100A_s}{bh} = 0.13$$
$$A_s = \frac{0.13 \times 1000 \times 200}{100} = 260 \text{ mm}^2/\text{m width}$$

Use T10 @ 300 centre to centre. (T10–300)



10.8.7 Design of Roof Frame

Calculation of forces in the chords



Fig. 10.13 Roof frame



Fig. 10.14 Top chord

From previous calculations, roof load = 14.67 KN/m^2 Requirement, point load = $14.2 \times 3.25 \times 6.5 = 310 \text{ KN}$ Self-weight of the girder, assume = $3 \text{ KN/m} \times 1.4 = 4.2 \text{ KN/m}$ BM @ centre = $2710 \times 26 - 310(22.75 + 19.5 + 16.25 + 13 + 9.75 + 6.5 + 3.25 - \frac{55}{2}(26) = 35,100 \text{ KNm}$

Force in chords $=\frac{35100}{3.25}=10,860$ KN i.e top chord10,860 compression bottom chord 10,860 tension

Design of top chord udl on top chord = $14.67 \times 6.5 + 3 \times 1.4 = 99.6$ KNm 3 KN/m = self-weight of girder Buckling about Y-Y axis

With the precast slab top flange is fully restrained

$$\Delta g = \frac{F}{P_y} \text{ take } P_y = 410 \text{ N/mm}^2$$
$$\Delta g = \frac{10800 \times 10^3}{410 \times 10^3} = 264 \text{ cm}^2$$

Try $\Delta g = 300 \,\mathrm{cm}^2$; 356 × 406 × 235 UB

$$M = \frac{wL^2}{16} = \frac{99.6 \times (3.25)^2}{16} = 65.75 \text{ KNm}$$
$$P_y \Delta g = \frac{410 \times 300 \times 10^2}{10^3} = 1923 \text{ KNm}$$



$$\frac{F}{P_v \Delta g} + \frac{M}{pbs_x} = \frac{10800}{12300} + \frac{65.75}{1923} = 0.91 < 1 \text{ O.K}$$

Design of bottom of chord Direct load = 10,800 tension



$$\Delta g = \frac{f}{P_v} = \frac{10800 \times 10^3}{410 \times 10^2} = 264 \,\mathrm{cm}^2$$

Use $356 \times 406 \times 235 UB (\Delta g = 300 \text{ cm}^2)$ Design of vertical member



$$l_{ey} = 0.85 \times 3.25 = 2763 \text{ mm}$$

 $l_{ex} = 0.85 \times 3.25 = 2763 \text{ mm}$

Taking $533 \times 210 \times 82$ UB

$$r_x = 21.3 \text{ cm } \Delta g = 104 \text{ cm}^3$$

$$r_y = 4.38 \text{ cm}$$

$$\lambda_y = \frac{2763}{4.38 \times 10} = 63.08$$

$$\lambda_x = \frac{2763}{21.3 \times 10} = 12.97$$

$$P_c = 327 \text{N/mm}^2$$



Member strength

$$= P_c \Delta_g$$

- $= 327 \times 104 \times 10^{2}$
- = 3401 KN > 2710 KN O.K

Design of diagonal member



$$T = \frac{R}{\sin 45}$$
$$= 2710\sqrt{2} = 3833KN$$



Use circular hollow section

$$\Delta g = \frac{3833 \times 10^3}{410 \times 10^2} = 93.4 \, cm^2, \text{Use } 244\emptyset 16(\Delta g 15 \, cm^2)$$

10.8.8 Design of Braced Column

Structural analysis to evaluate the moment in outer column.



Uniformly distributed liad roofing truss beam = 95.4KN



629



Fig. 10.15 Braced column using flexibilities analysis

= 16.67/EI $D_o = D_o = 1/3(3.2)(146.1)(1)/EI$ = 170.45/EI $D_{20} = D_{20} = \frac{1/3(50)(36062.2)(1)}{EI} + 17.75/EI$ $= \frac{601207}{EI}$

| 1.083 | 1.083 | 0 | ך 0 | $\begin{bmatrix} x_1 \end{bmatrix}$ | = | [170.45 ⁻ |
|-------|-------|-------|-------|-------------------------------------|---|-----------------------|
| 1.083 | 17.75 | 16.67 | 0 | <i>x</i> ₂ | | 601207 |
| 0 | 16.67 | 17.75 | 1.083 | <i>x</i> ₃ | | 601207 |
| 0 | 0 | 1.085 | 1.083 | $\lfloor x_4 \rfloor$ | | 170.45 |

$$\begin{bmatrix} x_1\\x_2\\x_3\\x_4 \end{bmatrix} \begin{bmatrix} -16.57 & 166.7 & -166.7 & 166.68\\166.6 & -166.7 & 166.7 & -166.7\\-166.7 & 16.67 & -166.7 & 166.7\\166.7 & -166.7 & 166.7 & -166.7 \end{bmatrix} = \begin{bmatrix} 170.45\\601207\\601207\\170.45 \end{bmatrix}$$
$$or = \begin{bmatrix} -17872\\18.29\\18029\\-17871\end{bmatrix}$$

 $M = M_0 + M_1 x_1 + M_2 x_2 + M_3 x_3 + M_4 x_4$ $M_1 = -17871.7KNm$ $\Delta t \operatorname{mid} 2 \operatorname{and} 3$

M = 36062.2 - 18029.1= 18233.2KNm

From the calculation it can be seen that if the outer column is totally fixed and the inner column behave as a simply supported column, the outer column will take the rotation moment and the inner column will take the maximum load.

Load supported by the inner column = 1/2(550) + 95.4(50/2) + 3.25(95.4/2)= 2815KN

Load from blasting UDL = $5 \times 6.5 = 176.8 \text{ KN}$ By assuming there is no lateral displacement at the top of column

> $R = 176.8 \times 5.5 = 972.4 \text{ KNm}$ BM at $\emptyset = 97.24 \times 20.4 - 176.8(17 + 13.6 + 10.2 + 6.8)$ = 10820 KNm

Force in chords due to blast loading = $\frac{10820}{3.25} = 3329$ KN

Inner Column C Compression.

Total axial load = 2815 + 3329 = 6144 KN $UDL = \frac{176.8}{34} = 52$ KN/m $m = \frac{52 \times 3.4^2}{16} = 37.57$ Use UC Assume $P_c = 200$ N/mm²

$$\Delta g \text{ required} = \frac{6144 \times 10^3}{200 \times 10^2} = 307.2 \text{ cm}^3$$

Try UC $356 \times 406 \times 287$

 $r_x = 16.5 r_y = 10.3 S_x = 5820$ $\lambda_x = \frac{289}{16.5} = 17.5 \lambda_y = \frac{340}{10.3} = 33$ $P_c = 242 \text{ N/mm}^2$

$$P_b = 265 \text{ N/mm}^2$$
$$P_c \Delta g = \frac{242 \times 366 \times 10^2}{10^3} = 8857.2$$
$$P_c S_x = \frac{265 \times 5820}{10^3} = 1542.3$$

Iteration



Fig. 10.15 Braced columns of a frame





$$\frac{6144}{8857.2} + \frac{37.52}{1542} = 0.718 < 1 \ O.K$$

Design of outer chord

Bending moment due to roof loading = 17,872 KNm Therefore tension in the chord = $\frac{17872}{40.8}$ = 438 KN Force in chord due toblasting = 33.92 KN Total = 3767 KN Assume $P_c = 0.9 \times 265 = 240 \text{ KN/mm}^2$ $\Delta g = \frac{3767 \times 10^3}{240 \times 10^2} = 156.9 \text{ cm}^2$ Try $UC = 356 \times 368 \times 129(165)$

Tension resistance = 265×165 = 4372.5 KN > 3767 KN is O.K

10.8.8.1 Design of Diagonal Ties



$$F_{1} = \frac{972}{\cos 46.29} = 1406.6 \text{KN}$$

$$P_{y} = 265 \text{N/mm}^{2}$$

$$\Delta g = \frac{1407 \times 10^{3}}{265 \times 10^{2}} = 53.1 \text{ cm}^{2}$$
Try 203 × 203 × 46(58.8)*UC*
Strength $\frac{265 \times 58.5 \times 10^{2}}{10^{3}} = 1588 \text{KN} > 1406 \text{KN O.K}$

972.4



Fig. 10.16 Diagonal ties



10.8.9 Design Base Plate for Inner Column

Design load = 6144 KN Chosen design strength of the concrete foundation = 7.5 N/mm² As required = $\frac{6144 \times 10^3}{7.5}$ = 819, 200 mm² = 905 × 905 mm² Use 910 square base plate Actual pressure under the plate = $\frac{6144 \times 10^3}{905 \times 905}$ = 7.42 N/mm²





Thicknes of base plate $t = \sqrt{\frac{2.5 \times 7.42}{265} [255.5^2 - 0.3 (258)^2]} = 56.3 \,\mathrm{mm}$



User 60 mm thick plate.

10.8.10 Design of Base Plate for Outer Column

Design load = $95.4 \times \frac{3.25}{2} = 155 \text{ KN}$ For concrete foundation = 7.5 N/mm^2 As required = $\frac{155 \times 10^3}{7.5} = 20,670 \text{ mm}^2 = 144 \text{ mm}^2$ 700 small for the column Chosen 500 × 500 square base plate Actual pressure under the plate = $\frac{155 \times 10^3}{500 \times 500} = 0.62 \text{ N/mm}^2$





Thickness of plate t = $\sqrt{\frac{2.5 \times 0.62[66^z - 0.3(72)^z]}{265}}$ t = 4 mm Use 25 mm thick base plate.



thickness = 25 mm

10.8.11 Design for Wind-Loading Resistance

Basic design wind speed = 40 m/s Class 3B Total weight = 40.8 + 3.25 = 44.05 $s_2 = 1.02$ $v_z = v \times s_1 \times s_2 \times s_3$ $s_1 = s_3 = 1$ $v_z = 40 \times 1 \times 1.02 \times 1 = 40.8 \text{ m/sec}$ $q = kv_z^2$ k = 0.613 $q = 0.613 \times 40.8 = 1020 \text{ N/m}^2 = 1.02 \text{ KN/m}^2 < 5 \text{ KN/m}^2$ As the loading is less than the blasting load which was the design load for the column frame in direction parallel to the main frame no bracing required in this direction.

Design of bracing in direction perpendicular to the main frame.

 $\frac{l}{w} = \frac{58.5}{52} = 1.125$ $\frac{h}{b} = \frac{44.05}{52} = 0.847 \approx 1$ cf = 0.95 $q = 0.969 < 5 \text{ KN/m}^2$





Pressure in x direction $q = 0.969 \times 1.4 = 1.3566 \, KN/mm^2$ Horizontal load on column x - x (1) = $\left(\frac{1}{3}(3.25) + \frac{1}{2}(50)1.3566\right)$ $= 26.625 \times 1.3566 = 36.12 KN/m$ Therefore horizontal load on topof column= $36.12 \times \frac{40.8 \times 3.25}{2} = 795.53 KN$ But Horizontal load on the front joint of the wind girder = $3.25 \times 1.3566 = 4.4 \text{ KN}$ $R = \frac{4.4 \times 16}{2} = 35.27 \, KN$ BM at the centre = $35.27(\frac{52}{2}) - 4.4(22.75 + 19.57 + 16.25 + 13 + 9.75 + 16.25)$ 6.5 + 3.25) = 516.66 KNmForce in chord $=\frac{216.66}{6.5}=79.49 \, KN$ $F = \frac{79.49}{\cos 63.4} = 177.52 \, KN$ Use M 24 MSFG Slip resistance = 207 KN > 177.52 KNFor the size and no. of bolt Use $200 \times 100 \times 10$ unequal angle



Fig. 10.20 Analysis for diagonal ties







10.8.12 Design of Diagonal Ties of Two Edge Column



 $\tan \theta = \frac{44.05}{6.8} \\ \theta = 61.61^{\circ} \\ F = 35.27 \\ \cos 82.59 = 241.6KN$

Use 3 M 24 HSFG



Use
$$200 \times 100 \times 10$$

 $a_e = a_1 + \left(\frac{3a_1}{3a_1 + a_2}\right)a_2$ $a_1 = (200 - 3(24)10) = 1280 \text{ mm}^2$ $a_e = 1280 + \left(\frac{3(1280)}{3(1280) + 1000}\right)1000$ 207 mm² Strength $= p_y \Delta e = \frac{2073 \times 265}{10^3} = 549.4KN > 241.6KN \therefore \text{ O.K}$



10.8.13 Foundation Design



 $M = 2 \times 1536 \times 0.295 = 906.2 \text{ KNm}$ $\frac{M}{bd^2 f_{cu}} = \frac{906 \times 10^6}{30 \times 2300 \times 715} = 0.03$ Lever armz = 0.94d

$$A_s = \frac{906 \times 10^6}{0.87 \times 460 \times 0.94 \times 715} = 3368 \, mm^2$$

Use 8v 25 (3930 mm²)

(b) Shear checkingPunching around the base plate

$$v = \frac{v}{u_c d} = \frac{6144 \times 10^3}{4 \times 910 \times 715} = 2.36 \text{ N/mm}^2$$

<0.8\sqrt{f_{cu}} Shear O.K
1.5d = 1.5 \times 715 = 997.5
>950

Distance from column centre to outer diameter of pile. No checking for shear perimeter is required. Enhanced Shear

Thickness of cap = 800 mmPilediameter = 500 mm



Fig. 10.21 Foundation design

(a) Reinforced design Enhanced shear

| Beneficial | | | |
|--|--|--|--|
| $N = \frac{6144}{2(1.5)} = 20.48$ $\frac{M}{d} = \frac{37.57}{1.5} = 25.05$ $Total P = 2073$ | | | |
| | | | |

 $v = 15.48 \,\mathrm{KN}$

$$v = \frac{2 \times 1548 \times 10^3}{2300 \times 715} = 1.88 \,\mathrm{N/mm^2}$$
$\frac{100A_s}{bd} = \frac{100 \times 3900}{2300 \times 715} = 0.239$ $v_c = 0.42 \text{ N/mm}^2$ $v'_c = v_c \times \frac{2d}{a_c}$ $= 0.42 \times 2 \times \frac{715}{295}$ $= 2.04 \text{ N/mm}^2$ $> 0.42 N/mm^2 v'_c O.K$

No link required.

10.8.14 Wall Design





Wall loading

$$w = 11.8 \text{ KN}/m$$

Bending moment $M = \frac{wL^2}{8} = \frac{11.8 \times 10.8^{\circ}}{8}$
$$= 172.0 \text{ KNm}$$
$$k = \frac{M}{bd^2 f_{cu}} = \frac{172 \times 10^6}{1000 \times 200^2 \times 30} = 0.14$$
Lever armz = 0.8*d*
$$A_s = \frac{172 \times 10^6}{0.87 \times 30 \times 0.8 \times 200}$$
$$= 2686.16 \text{ mm}^2$$

Use 725–175 (28100 mm²)

10.8.15 Beam Design

Assume each beam is of 6.5 m span and simply supported Area of slab precast unit = $50 \times 10.8 = 540 \text{ m}^2$

Self-weight of the precast unit = $0.2 \times 24 = 4.8 \text{ KN/m}^2$ Design loading = $1.4 \times 4.8 \times 10.8 = 72.58 \text{ KN/m}$ Bending moment M = $\frac{72.58 \times 6.5^2}{8} = 383.4 \text{ KNm}$

Fig. 10.22 Beam design





Assume use of compact section S_x required = S = 5 M = 5 × 383.4 = 1917 cm³ Consider 533 × 210 × 92 UB Section properties

$$D = 533.1 \text{ mm}$$

$$B = 209.3 \text{ mm}$$

$$t = 10.2 \text{ mm}$$

$$T = 15.6 \text{ mm}$$

$$r = 12.7 \text{ mm}$$

$$d = 476.5 \text{ mm}$$

$$r_y = 4.51 \text{ cm}$$

$$S_x = 2370 \text{ cm}^2$$

$$x = 36.4$$

$$p_y = 265 \text{ N/mm}^2$$

Compact check

Compact check

$$b = \frac{B-t}{2} - r = \frac{209.3 - 10.2}{2} - 12.7$$
$$= 86.85 \, mm$$

:: Flange, $\frac{\beta}{T} = \frac{86.85}{15.6} = 5.57$

 $E = \left(\frac{275}{265}\right)^{\frac{1}{2}} = 1.02$ 9.5E = 9.5 × 1.02 = 9.69 $> \frac{b}{T}$ flange check O.K $\therefore Web, \frac{d}{t} = \frac{476.5}{10.2} = 46.7$ 98*E* = 98 × 1.02 $> \frac{d}{t}$ web check O.K Shear $R = \frac{72.6 \times 6.5}{2} = 234 KN$ *Shear capacity* = $0.6 \times 265 \times 10.2 \times 533.1 = 864.6 KN$ > R Shear capacity O.K Bending capacity = $265 \times 10.2 \times [20 + (15.6 + 12.7)] = 245.3$ KN > R Bending capacity O.K Buckling Slenderness ratio $\lambda = \frac{2.5 \times 476.5}{10.2} = 116.8$ $p_c = 98 \, \text{N/mm}^2$ Web buckling = $98 \times 10.2 \times (20 + \frac{533.1}{2}) = 286.4KN$ Deflection $d = \frac{5}{384} \frac{wL^4}{EI}$ $=\frac{5\times72.6\times6.5^4}{384\times205\times10^6(5.54\times10^{-4})}=0.015\,\mathrm{m}$ $\frac{L}{200} = \frac{6.5}{200}$ = 0.032 m > 0.015 m Deflection O.K.





Fig. 10.23 Column design



Height of column = 30 mWorking load = $1.4 \times 4.8 \times \frac{540}{2} = 1814.4 KN$ For grade 50 steel Design strength $p_v = 265 \text{ N/mm}^2$ Effective length $L_E = 0.7L$ $= 0.7 \times 30 = 21 m$ Design load = 1814.4 KNColumn strength = $p_c A_g$ Assume $P_{c} = 50 \, \text{N/mm}^{2}$ $A_g = \frac{1814.4 \times 10^3}{50} = 36,288 \, mm^2 = 363 \, cm^2$ try 356 × 406 × 393 UC (A_g = 505 cm²) $r_v = 10.5 \text{ cm}$ $\lambda_v = \frac{2100}{10.5} = 200$ $P_{c} = 41 \text{ N/mm}^{2}$ Strength = $\frac{41 \times 505 \times 10^2}{10^2} = 2070.5 KN$ >1814.4 KN Column strength O.K $\frac{F}{P_{a}A_{a}} + \frac{M}{M_{b}} = 1$ $\frac{1814.4}{2070.5} + \frac{44.6}{636.5} = 0.95 < 1$

10.8.16.1 Design of Base Plate

Design load = 1814 KN Given design strengthof concrete = 7.5 N/mm² Area = $\frac{1814 \times 10^3}{7.5}$ = 241866.7 mm² = 491.8 × 491.8 Use 500 square base plate Actual pressure under plate = $\frac{1814 \times 10^3}{500 \times 500}$ = 7.26 N/mm² Plate thickness

$$t - \sqrt{\frac{2.5 \times 7.26}{265}} \left[(47 \times 72) - (0.5 \times 47 \times 72) \right] = 10.77 \,\mathrm{mm}$$

$$\not < T$$



: Use 50 mm thick plate

 $P_c A_g = \frac{41 \times 505 \times 10^2}{10^3} = 2070.5KN$ $S_x = 4160 \text{ cm}^2$ x = 7.86 $\lambda_y = 200$ $P_b = 153 \text{ N/mm}^2$ $P_b S_x = 153 \times 4160$ 636.3 KNm

Hanger Design Hangers Chosen $203 \times 203 \times 46$ UC

$$P_y = 460 \text{ N/mm}^2$$

 $E = \left(\frac{275}{460}\right)^{\frac{1}{2}} = 0.59$



Fig. 10.24 Column design

$$\frac{b}{T} = \frac{101.6}{11} = 9.23$$

 $15\varepsilon = 11.72 > \frac{b}{T}$

Effective area = 53.1 cm² Minimum value of elastic modulus Z = 365 cm² Moment capacity of major axis $M_c x = 363 \times \frac{450}{10^3} = 163.35$ KNm The applied axial load $f = (2 \times 120 + 590) \times 0.0088 = 7.30$ KNm Substitute

$$\frac{F}{A_e P_y} + \frac{M_x}{M_{ex}} = \frac{830 \times 10}{53.1 \times 450} + \frac{7.3}{163.35} = 0.40$$

<1 : O.K



Fig. 10.25 Connections details



Fig. 10.25a Structural detailing for the bottom chord



Fig. 10.26 Pile cap arangement



Fig. 10.27 Detailing top chord and vertical beams



Fig. 10.28 Beam – column connectors







Fig. 10.29 Roof slab



Fig. 10.30 Columns top and bottoms with bracings



Fig. 10.31 Columns to foundations

Appendix A Prestressing Systems and Anchorage Design

General Introduction

Prestressed concrete has attained worldwide recognition in the development of industrialised construction and design. Prestressing consists of introducing imposed deformations by tensioning prestressing wires, cables or strands and tendons to a high stress which decreases with time due to various losses such as shrinkage, creep, steel relaxation, friction and wobbling effects. The word *prestress* is associated with the following:

- (a) pretensioned concrete
- (b) post-tensioned concrete

In the case of pretensioned concrete structures, the tensioning of the tendon is carried out before concreting. The prestressing force is held temporarily either by a specially constructed prestressing bed or by a mould or form. When the concrete strength reaches the specified transfer strength, detensioning and stress transfer to such structures can be performed. In practice these structures are prefabricated.

In the case of post-tensioned concrete structures, the tensioning of the tendon is carried out after casting and hardening of the concrete. This method is more effective in the design and construction of high-rise and long-span concrete structures. The design and detailing of such structures are influenced by the serviceability classification, which includes the amount of flexural tensile stresses allowed while carrying out the design/detailing of such structures. They are then classified into individual classes which are given below:

- Class 1: no flexural tensile stresses.
- Class 2: flexural tensile stresses but no visible cracking.
- Class 3: flexural tensile stresses but surface width of cracks not exceeding
 - 0.1 mm for members in very severe environments and not exceeding 0.2 mm for all other members.

The structural detailing of prestressed concrete members must take into consideration durability, fire resistance and stability. The relevant codes EC2

and BS 8110 which should strictly be followed for the correct evaluation of design ultimate loads and the characteristic strength of concrete and steel.

Generally, high-strength concrete is used for prestressed concrete work. The steel used in prestressed concrete is generally of a much higher strength than mild steel. This aspect is discussed later on in the choice and evaluation of prestressing systems.

Material data and prestressing systems are given on Plates AIA.1 to AIA.7 provided by the manufacturers. In such the prestressing tendons can be bonded and unbonded. The structural detailing is affected when the prestressed concrete structure is designed with bonded and unbonded tendons. Before the prestressing load is transmitted into various zones of concrete with bonded or unbonded tendons, it is necessary to protect the areas immediately under the anchorages against bursting effects caused by large loads generated by prestressing tendons. In such cases, the areas below anchorages must be designed by providing anticrack or burst steel.



'FREYSSI' MONOGROUP – 15/15 mm NORMAL STRAND SYSTEM

Plate AIA.1 'Fryssi' Monogroup-15/15 mm Normal Strand System

BBRV TENDON SIZES AND THEIR PROPERTIES

| Tendon reference | | B16 | B24 | B34 | C42 | C55 | L73 | L85 | L97 | L109 | L121 |
|---|---|-----|------|------|------|------|------|------|------|------|------|
| No. of wires (7 mm dia.) | | 16 | 24 | 34 | 42 | 55 | 73 | 85 | 97 | 109 | 121 |
| Characteristic strength using 1570 N/mm ² wire | | 967 | 1450 | 2054 | 2538 | 3323 | 4411 | 5136 | 5861 | 6586 | 7311 |
| Jacking force (kN) at 80% of C.S. | | 773 | 1160 | 1643 | 2030 | 2659 | 3529 | 4109 | 4689 | 5269 | 5849 |
| Jacking force (kN) at 75% of C.S. | | 725 | 1088 | 1540 | 1903 | 2492 | 3308 | 3852 | 4396 | 4939 | 5483 |
| Jacking force (kN) at 70% of C.S. | | 677 | 1015 | 1438 | 1776 | 2326 | 3087 | 3595 | 4103 | 4610 | 5118 |
| <i>Bearing plate</i> Side lenght (sq.) | A | 178 | 220 | 250 | 280 | 300 | 335 | 360 | 385 | 405 | 425 |
| Thickness | В | 15 | 20 | 25 | 35 | 35 | 45 | 50 | 50 | 60 | 60 |
| <i>Trumpet</i> Outside diameter | С | 120 | 133 | 154 | 154 | 165 | 194 | 219 | 229 | 229 | 245 |
| Anchor Head Thread diameter | D | 100 | 115 | 130 | 90 | 98 | 125 | 130 | 145 | 150 | 155 |
| Standard length | Е | 60 | 80 | 90 | 53 | 63 | 110 | 120 | 126 | 134 | 146 |
| Overall diameter | F | — | — | _ | _ | — | 160 | 165 | 185 | 190 | 200 |
| <i>Pull Sleeve</i> Diameter | G | | _ | _ | 130 | 144 | | _ | | _ | _ |
| Standard length | Н | — | — | | 118 | 138 | _ | _ | | _ | _ |
| <i>Lock Nut</i> Diameter | J | 135 | 155 | 180 | 178 | 198 | _ | _ | _ | _ | |
| Thickness | к | 30 | 40 | 50 | 45 | 53 | _ | _ | - | _ | _ |
| <i>Chocks</i> Diameter | L | _ | _ | _ | _ | _ | 228 | 250 | 262 | 270 | 288 |
| Min. thickness | М | _ | _ | _ | _ | _ | 48 | 52 | 55 | 59 | 62 |
| Max. anchorage projection (Stnd. comps.) | Ν | 67 | 87 | 97 | 118 | 138 | 205 | 219 | 228 | 240 | 255 |
| Sheathing Internal diameter | 0 | 40 | 50 | 60 | 65 | 75 | 85 | 95 | 100 | 105 | 110 |
| External diameter | | 48 | 58 | 68 | 73 | 83 | 93 | 103 | 108 | 113 | 118 |

Lenght of trumpet 'p' <u>→</u> Extension + 105 mm (B type anchors) Extension + 120 mm (C type anchors) (L type anchors)

All dimensions are in millimetres.

Plate AIA.2

Combined asance use sheat in the Heading and the states Jestine outretore bearing plate Jeanstean Handrander Anchorages Mining Colde with the strength of the stren Hameres ing equi M. Upt stream I'd single wenter and a start of the start Minimumcert Munum control ages Jeannan annae Stressingf , d¹ strof 80% reference tensile Stat Š NO. kΝ kΝ No. Туре Туре Ref. No. mm mm mm mm mm mm $f \times g$ dia. $\mathbf{c} \times \mathbf{d}$ h×g dia. е a×b в 150 × 150 138 × 138 76 150×150 J 30 1524 × 310 1344 × 310 F 32 483 387 8 120×120 SR 120×150 60×300 SL 175 × 175 171 × 171 89 в 175 × 175 J F 64 160 × 160 40 1524 × 310 1344 × 310 966 773 16 SR 150×220 SL 80×400 В $200 \times 200 \ 197 \times 197 \ 108$ J 200×200 F 220×220 100 50 1524 × 310 1344 × 310 1450 1160 24 SS 220×220 160 × 300 SR 80×560 SL 250 × 250 235 × 235 127 С Е 235 dia. SS 130 260 × 260 55 1524×340 1324×340 1872 1498 31 SR 180 × 360 120 × 560 SL 250 × 250 235 × 235 127 В 250×250 J F 260×260 55 1524 × 340 1324 × 340 2054 1643 34 138 SS 260 × 260 SR 180 × 360 SL 120×560 280 × 280 241 × 267 152 С 270 dia. Е $65 \quad 1880 \times 440 \ 1580 \times 440$ 2537 2029 42 SS 170 300 × 300 SR 200 imes 450SL 140×650 С 300 × 300 267 × 305 152 300 dia. F 340 × 340 $75 \quad 1880 \times 440 \ 1580 \times 440$ 3322 2658 55 SS 220 SR 220×500 SL 160×700 Type A300-500 Type A600-800 Туре В Type C ◍ -Type E Type J Type SS.Sr. SL Tvpe F 11ffi ≥^##

SMALL CAPACITY TENDONS UP TO 2658 kN



Plate AIA.4

TYPE 'F' FIXED ANCHORAGE

A fixed anchorage-consisting of a rectangular steel plate drilled to receive the individual button-headed wires seated directly on this plate. A thin cover plate retains the button heads during fixing.

With this anchorage, the prestressing force is transferred to the concrete through the plate.

Type 'F' anchorages are normally used in connection with movable anchorages of the Type 'B' series.if there are, several tendons in one part of a structure.it is advisable to put half the Type 'F' anchorages at one end and half at the other.

The anchorage is fastened to the formwork with a pipe which serves at the same time as a vent or as a grout connection.

This pipe passes through the plate and should be well-greased prior to fixing to facilitate removal after grouting.

| Type F anchorage | Type designation | | F32 | | F64 | - | F100 | - | F138 | |
|---|--|-----------------------------|-----|------|-----|------|------|-------|------|-------|
| Steel | wires per anchorage, number 7 mm | maximum (0.276") dia. | 8 | | 16 | | 24 | | 34 | |
| | | | mm | in | mm | in | mm | in | mm | in |
| Anchorage | side length | Sp | 120 | 4.72 | 160 | 6.30 | 220 | 8.66 | 260 | 10.24 |
| | Thickness | \dot{D}_P | 15 | 0.59 | 25 | 0.98 | 40 | 1.58 | 50 | 1.97 |
| End trumpet | outer diameter | D _T | 87 | 3.43 | 112 | 4.41 | 128 | 5.04 | 148 | 5.83 |
| | Connection, outer dia. | DI | 35 | 1.38 | 45 | 1.77 | 55 | 2.17 | 60 | 2.36 |
| | Length | L _T | 200 | 7.87 | 250 | 9.84 | 300 | 11.81 | 350 | 13.78 |
| Helix | outer diameter | Ds | 120 | 4.72 | 160 | 6.30 | 220 | 8.66 | 260 | 10.24 |
| | Length (approx.) | Ls | 250 | 9.84 | 250 | 9.84 | 250 | 9.84 | 250 | 9.84 |
| Distance of centre vent pipe to e tendon axis | | 0 | 0 | 0 | 0 | 35 | 1.38 | 45 | 1.77 | |



BBRVF 163 No/7 mm Tendon



Plate AIA. 5 Load-Elongation diagram



Plate AIA.6 C.C.L. System

| $\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$ | internal dia. mm 42 " 51 " |
|--|---|
| $\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$ | dia. mm 42 " 51 |
| 4/13 STD. 660.0 528.0 462.0 130 U1 Cabco 4/13 SUP. 736.0 588.8 515.2 " 4/13 DYF. 836.0 668.8 585.2 " 4/15 STD. 908.0 726.4 635.6 175 4/15 SUP. 1000.0 800.0 700.0 " 4/15 DYF. 1200.0 960.0 840.0 " U2 Cabco 7/13 STD. 1155.0 924.0 808.5 " | 42 " 51 |
| U1 Cabco 4/13 SUP. 736.0 588.8 515.2 " 4/13 DYF. 836.0 668.8 585.2 " 4/15 STD. 908.0 726.4 635.6 175 4/15 SUP. 1000.0 800.0 700.0 " 4/15 DYF. 1200.0 960.0 840.0 " U2 Cabco 7/13 STD. 1155.0 924.0 808.5 " | " 51 " |
| 4/13 DYF. 836.0 668.8 585.2 " 4/15 STD. 908.0 726.4 635.6 175 4/15 SUP. 1000.0 800.0 700.0 " 4/15 DYF. 1200.0 960.0 840.0 " U2 Cabco 7/13 STD. 1155.0 924.0 808.5 " | " 51 " |
| 4/15 STD. 908.0 726.4 635.6 175 4/15 SUP. 1000.0 800.0 700.0 " 4/15 DYF. 1200.0 960.0 840.0 " U2 Cabco 7/13 STD. 1155.0 924.0 808.5 " | 51 " |
| 4/15 SUP. 1000.0 800.0 700.0 " 4/15 DYF. 1200.0 960.0 840.0 " U2 Cabco 7/13 STD. 1155.0 924.0 808.5 " | " |
| 4/15 DYF. 1200.0 960.0 840.0 " U2 Cabco 7/13 STD. 1155.0 924.0 808.5 " | |
| U2 Cabco 7/13 STD. 1155.0 924.0 808.5 " | ** |
| | " |
| 7/13 SUP. 1288.0 1030.4 901.6 " | ** |
| 7/13 DYF. 1453.0 1170.4 1024.1 " | ** |
| 4/18 STD. 1480.0 1184.0 1036.0 175 | 51 |
| 4/18 DYF. 1520.0 1216.0 1064.0 " | ** |
| 7/15 STD. 1589.0 1271.2 1112.3 215 | 75 |
| 7/15 SUP. 1750.0 1400.0 1225.0 " | " |
| Cabco 7/15 DYF. 2100.0 1680.0 1470.0 " | 63 |
| U3 12/13 STD. 1980.0 1584.0 1386.0 215 | 81 |
| 12/13 SUP. 2208.0 1766.4 1545.6 215 | " |
| Multiforce 12/13 STD. 1980.0 1584.0 1386.0 215 | " |
| 12/13 SUP. 2208.0 1766.4 1545.6 215 | " |
| 7/18 STD. 2590.0 2072.0 1813.0 245 | 81 |
| 7/18 DYF. 2660.0 2128.0 1862.0 " | 75 |
| U4 Cabco 12/13 DYF. 2508.0 2006.4 1755.6 " | 75 |
| 12/15 STD. 2724.0 2179.2 1906.8 " | 81 |
| 12/15 SUP. 3000.0 2400.0 2100.0 " | 81 |
| Cabco 12/15 DYF. 3600.0 2880.0 2520.0 265 | 81 |
| 19/13 STD. 3135.0 2508.0 2194.5 " | " |
| U5 19/13 SUP. 3496.0. 2796.8 2447.2 " | " |
| Multiforce 12/15 STD. 2724.0 2179.2 1906.8 245 | " |
| 12/15 SUP. 3000.0 2400.0 2100.0 245 | " |
| 12/15 DYF. 3600.0 2880.0 2520.0 265 | " |
| 25/13 STD. 4125.0 3300.0 2887.5 300 | 90 |
| U6 Multiforce 25/13 SUP. 4600.0 3680.0 3220.0 " | " |
| 13/15 DYF. 3900.0 3120.0 2730.0 " | 84 |
| 31/13 STD. 5115.0 4092.0 3580.5 335 | 100 |
| 31/13 SUP. 5704.0 4563.2 3992.8 " | " |
| U7 Multiforce 19/15 STD. 4313.0 3450.0 3019.1 " | " |
| 19/15 SUP. 4750.0 3800.0 3325.0 " | " |
| 19/15 DYF. 5700.0 4560.0 3990.0 " | " |
| U8 Multiforce 19/18 DYF. 7220.0 5776.0 5054.0 " | " |
| $5/18$ STD. 1776.0 1480.0 1295.0 362×89 |) 114 × 25 |
| 5/18 DYF. 1824.0 1520.0 1330.0 " | " |
| Strand-force $10/18$ STD. 3530.0 2960.0 2590.0 362×1^{-2} | 71 " twin |
| 10/18 DYF. 3648.0 3040.0 2660.0 " | " twin |

CABCO PRESTRESSING TENDON MAIN DATA

*STD. Standard SUP. Super Strand DYF. Dyform Strand

Plate AIA.7

The Largest Tendon Is the BBRV Tendon and Its Description Is as Under

BBRV—Tendons

General

BBRV tendons consist of any number of parallel wires having diameters of 4–12 mm (0.16–0.47 in.), anchored in a common anchor head by means of cold-upset button-heads. For nuclear pressure, and containment vessels, tendons are used with 121, 163 or 187 wires of 7 mm (0.28 in.) diameter, corresponding to ultimate loads of 770, 1020 or 1200 tons with the quality of steel chosen. Intermediate sizes are likewise possible, as is the use of even larger tendons. Parallel-wire tendons have the following advantages and disadvantages in comparison with strands or wire ropes.

Tendons made from a number of strands

The individual strand is more flexible, but its component wires are subject to additional fiexural and torsional stresses and thus (with the exception of stabilized strands) to greater relaxation losses. A strand is composed of wire of a smaller diameter (maximum approximately 4 mm [0-16 in.]) and is for this reason, as well as on account of the additional stresses, more susceptible to corrosion and to stress corrosion. It also manifests greater losses due to friction.

A coupling is threaded over the outside threading of the anchor's bearing nut. As soon as the required elongation has been reached, the anchor is blocked by placing the two semi-circular chocks under the bearing nut. The anchor plate consists of a concrete block with an external helix that is completely closed and an internal reinforcement of the end of the duct. The surface of the concrete block is covered by a steel plate 25 mm (098 in.) thick in order to obtain a clean working surface, so that the relatively heavy-tensioning equipment can be fastened on and for the purpose of local load distribution. The principal dimensions of this anchor construction are given below, for example, with 163 wires of 7 mm (028 in.) diameter.

| Outer diameter of anchor head | 294 mm (11.57 in.) |
|-------------------------------|--|
| Height of anchor | 120 mm (4.72 in.) |
| Bearing block | $610\times 610\times 275~mm$ |
| | $(24.0 \times 24.0 \times 1083 \text{ in.})$ |

It was first demonstrated in 1964, at the Cable testing station in Germany, that this anchorage will sustain the full ultimate load of the tendon without undergoing any plastic deformation itself; since then, the proof has been repeated in at least 24 other ultimate tensile tests carried out on tendons. A supplementary test carried out by the Swiss Federal Laboratories for Testing Materials and Research (EMPA), in order to establish the actual reserve bearing capacity of the anchor head, showed that the anchor with 163.7 mm

(0–28 in.) wires had an ultimate load of 1376 t, while that of the tendon which it may anchor is 1020 tons (EMPA Report No. 40879, BORVD964).

Whenever possible, tendons are assembled in the factory. The wires are first measured off to the required length on a fully automatic cutting bench. Then the bundle of wires is passed through a template and the one anchor head, and button-heads are cold-upset onto the wires at this end. In order to make all the wires parallel, the tendon is then pulled through the template by pulling the anchor head. To keep the differences in the lengths of the wires in a curved duct to a minimum, and to preserve the parallelism of the wires even when they are wound onto reels for transport, the tendon is given three to five complete twists and then bound at intervals of approximately 3 m (approx. 10 ft). Once the tendons are reeled the factory work is finished.

On the construction site, once the wire bundle has been unrolled off the reel and pulled directly into its duct, the other anchor head is mounted. Thus the tendon is ready to be stressed from one or both ends.

Anchorage Analysis and Design

Based on research reports 9 and 13 by C & CA (Now Concrete Society London).

General Formulation

A reference is made to Fig. AIA.1 for the design analysis

- $-f_x$ general longitudinal stresses
- $-f_{v}$ general transverse 'bursting' stresses
- ε_x general longitudinal strains
- ε_x general transverse 'bursting' strains
- P load applied to anchorage
- $-2a_1$ width of bearing plate
- -2a width of end block
- t thickness of anchor bearing plate
- $f_{\rm c}$ uniform longitudinal compressive stress

$$=\frac{P}{(4a^2 - \operatorname{area of duct})}$$
(AIA.1)

- E modulus of elasticity
- $-\gamma$ Poisson's ratio
- $-\sigma_1, \sigma_2, \sigma_3$ principal stresses, $\sigma_1 > \sigma_2 > \sigma_3$ tension + ve
- $-\varepsilon_1, \varepsilon_2, \varepsilon_3$ principal strains corresponding to γ_1 , etc.
- $-\gamma_m$ mean normal stress

Fig. AIA.1 Idealised end block showing principal notation



$$=\frac{\sigma_1+\sigma_2+\sigma_3}{3}=$$
(AIA.2)

Octahedral normal stress

The C & CA experimental tests were compared with those of six researchers and the results are plotted in Fig. AIA.2 by Taylor S.G.C. The 3D finiteelement analysis given in the text has been implemented in the program ISO-PAR. The analytical results are plotted on Fig. AIA.2.



Fig. AIA.2 Theoretical and experimental transverse stresses for $a_1/a = 0.50$ expressed as a ratio of the uniform compressive stress

The plotting of conventional steel bars below the anchorages to take an extra tensile stresses beyond the concrete tensile stresses can be plotted with in the hatched area in Fig. AIA.3. In other words, the tensile forces at a distance from loaded face can be easily plotted with hatched area at suitable spacings. It is important to replace the circular area by an equivalent square area.

The force to be taken by the reinforcement is suggested as

$$T_{\lambda} = T \left[1 - \left(\frac{f_t \text{ permissble}}{f_y \text{ maximum}} \right)^2 \right]$$
(AIA.3)

where T is the total tensile force.

Example Based on Freyssinet Anchorage System

Freyssinet system has been widely used in the reactor containment vessels Data:

Cable 12 N 0.5 mm wires Concrete prism 150×150 mm section Female cone diameter = 100 mm Total prestressing force = 222.4 KN a_1 = equivalent square area = 88.9 mm

Solution

$$\frac{a_1}{a} = \frac{88.9}{150} = 0.59$$



Fig. AIA.3 Tensile force corresponding to the calculated reinforcement

$$p = \text{uniform compressive stress} = \frac{222.4 \times 10^3}{150 \times 150} = 9.88 \text{ N/mm}^2$$

 $T = \text{maximum tensile force} = 0.22 \times 222.4 = 48.928 \text{ KN}$ $f_y = f_{t_{\text{max}}} = \text{maximum tensile stress} = 0.48 \times p = 4.74 \text{ N/mm}^2$ $f_I = f_t \text{ (permissible)} = 0.129 \text{ p} = 1.273 \text{ N/mm}^2$

Total tensile force (hatched area as a fraction of total traingular area)

$$= T_{\lambda} = T \left[1 - \left(\frac{f_1 \text{ permissible}}{f_y \max} \right)^2 \right]$$

= 0.928T

The force taken by the reinforcement = $0.928 \times 48.928 = 45.4$ KN Mild steel: Area = $\frac{45.4 \times 10^3}{250} = 181.6$ mm²

Select bars and place at 0.2a first bar, the next bars at 0.5a and pass through 125 mm with cover to 150 mm.

The 3D Finite-Element Analysis

A 3D finite element analysis has been carried out using, respectively, isoparametric element for solid concrete and bar (noded) element for reinforcement. Figure AIA.4 shows a finite element meshscheme for adjacent anchorages. Dimension loading and other parameters are kept the same of example under Section A.2.2.1. the 3D displacements are shown in Fig. AIA.5 from the output opf ratio of stress f_y/f_c are plotted in Fig. AIA.2 against the depths of the immediate blocks. The results are also compared experimental and other theories prominently shown in Fig. AIA.2.

Explanatory Notes

The mode of failure for BBRV tendons has been described earlier in the text. The following summarizes the behaviour for the tendons used in the example A.2.2.1

The mode of failure for an end block utilizing the tendon V anchorage unit as used in the model test example of

- First Uniform tensile load applied to the anchorage zone reduces the load carrying capacity of the anchorage unit and causes a reduction in the maximum tensile strain at cracking.
- Second Uniform compressive stress applied to the anchorage zone increases the load carrying capacity of the anchorage unit, the maximum tensile strain at cracking being increased.
- Third For biaxial compression–tension applied to the anchorage zone and a constant anchorage force, there is a marked reduction in the tensile stress



Fig. AIA.4 Analytical Results. (a) F.E mash system. (b) Displacement. (c) Hoopstress on external and internal faces

that can be applied to the anchorage zone as compressive stress is increased. An increase in the maximum tensile stress at cracking was noticed.

- Fourth There does not appear to be a limiting tensile stress, or strain criteria of failure for concrete under the influence of combined states of loads
- Fifth The failure envelopes for imposed loads on the anchorage zone are of a similar nature to that of plain concrete.
- Sixth It would appear that an analogy can be drawn between the behaviour of the anchorage zone and that of plain concrete.
- Seventh The distribution of transverse strains in the anchorage zone appears to be uniformly affected by imposed states of stress except for the case of applied biaxial compression-tension, where a movement of the maximum tension towards the loaded face was noticed.
- Eighth The results of the research described in this section show that a fairly simple empirical design method can be US stated under Section A.2.2.1 used for the detailing of end blocks which have uniform stresses imposed on the anchorage zone. This is based on the relation between the maximum tensile strain at cracking and the mean normal stress (octahedral normal stress). Throughout, the uniform stress due to the anchorage load has been used in calculating. However, in order to take into account variations of a_1/a , it may be better to use the stress under the bearing plate in assessing octahedral stress.
- Tenth It must be borne in mind that the complete results are based on fully saturated concrete and were short-term station.

Typical Prestressing Tendons Layout

Plates AIA.5, AIA.6 and AIA.7 give the typical layouts of the prestressing tendon layouts of the pressure and containment vessels.

Wire Winding of the Vessels

The latest vessel are provided with a wire winding system in which the wires are wound under tension into steel-lined channel either formed in the vessel walls or made of precast concrete. The band comprises of layers of wires anchored at both ends. In this way the maximum circumferential pressures are exerted with in a limited area.

Plate AIA.8 shows the general layout of the channel and Plate AIA.9 gives a brief analysis of how to find maximum pressure with in the confined area of the channel subject to wire-winding. Where standards instead of wires are used, the same analysis can simply be adopted. Care must be taken to supplement the analytical results with those of the experiments. A reference is made to the following paper of the author for detailed investigations.

(Prog. Inst. Civil. Engrs, Part 2,1975,59, Mar;195–200 and discussions 7710. Main paper Prog. Inst. Civil Engrs. Part 2, 1974, 57, Sept., 437–450)



Typical layout of prestressing systems. Dungeness B vessel. (With compliments of BNES and APC Ltd.)

Fig. AIA.5 Prestressing Layouts



Fig. AIA. 6 General layout of the channel



Fig. AIA. 7 Wire/Strand Analysis

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Appendix B Analytical Formulation for the Liner and Penetration



Plate AIB.1 Gas ducts, cooling pipes, control rods and other penetractions with finite element mesh schemes





 Q_d = Characteristic strength (kips) (KN)



Plate AIB.3 Typical bilinear hysteresis loop

 F_1 = Yield force (kips) (KN) F_{max} = Maximum force (kips) (KN) K_d = Post-elastic stiffness (kip/inch) (KN/mm²) K_u = Elastic (unloading) stiffness (kip/inch) K_{eff} = Effective stiffness Δ_m = Maximum bearing displacement

General Formulation for the Liner

In any computer package involving 2- and 3D finite-element technique, Table AIB.1 giving analytical formulation can be simulated to analyse the liner between the studs, standpipes and cooling pipes. For the global analysis of the pressure and containment vessels, these local effects can form the worst case. The vessel can be analysed with and without the contribution of the liner. Under ultimate conditions the liner local areas must be thoroughly assesed prior to the final decision of the factor safety above the elastic conditions under (pressure + prestress + temperature) the combined loading:

Table AIB.1 Analytical formulation of the steel liner

$$[K_{\text{TOT}}]\{\delta\}^* + \{F_T\} - \{R_T\} = 0$$

where

$$\begin{bmatrix} K_{\text{TOT}} \end{bmatrix} = \begin{bmatrix} K_l \end{bmatrix} + \begin{bmatrix} K_a \end{bmatrix}$$
$$\{\delta\}^* = \left\{ \begin{array}{c} \delta_{un} \\ \delta_b \end{array} \right\}; \{F_T\} = \left\{ \begin{array}{c} F_{un} \\ F_b \end{array} \right\}; \{R_T\} = \left\{ \begin{array}{c} R_{un} \\ R_b \end{array} \right\}$$

 $[K_{TOT}] = Total stiffness matrix$ = liner stiffness matrix

 $[K_l]$

 $[\mathbf{K}_a]$ = A stud stiffness matrix = Total initial load vector

 $\{F_T\}$ $\{R_T\}$ = Total external load vector

= quantities corresponding to unknown displacement

b = quantities corresponding to restrained boundaries

 $[K_{lr}]\{\delta_{un}\} + \{F_{un}\} = 0$ $\{3\}$ $= [B]{\delta}$ $\{\sigma\}$ $= [D](\{\varepsilon\} - \{\varepsilon_0\})$ $\{\delta\}$ = anchor shear forces

$$= [K_a] \cdot \{\delta_{un}\}$$

$$\{F_{un}\} = \int_{v} [B]^T [D] \{\varepsilon_0\} dv = \int_{v} [B]^T [D] \{\varepsilon_0\} dt [J] d\xi d\eta d\zeta$$

The plastic bucking matrix is given by

$$(K + \lambda K_G)F_T = 0$$

where

K = elasto-plastic stiffness matrix as a function of the current state of plastic deformation K_G = initial stress geometric stiffness matrix

The determinant $|K + \lambda K_G| = 0$.

The essential equation is characteristically triangularized for the *i*th loading step as

$$(K^i + \lambda_c K^i_G) F^i_T = 0$$

$$\lambda_c = 1 + E_{ps}$$
 E_{ps} – accuracy parameter.

Note: Table AIB.1 is a part of Programs, ISOPAR, ANSYS and others.

Penetrations Analysis: Classical and Finite Element Techniques

Penetrations in Reactor and Containment Vessels – General Introduction

Several penetrations, their sizes or locations are related to the reactor systems and their functions and layouts. Some of them have already been discussed in earlier chapters of the text under reactor and containment vessels. Their solutions and results have already been established. This appendix gives some penetration areas which may be treated as added discussions. The finite-element techniques of solving them has been fully discussed. There is no need for a reader to use it again. However, a classical approach is given to evaluate penetrations. The results are fully collaborated from the classical method with these from the finite-element technique. Plates AIB.1 and AIB.2 are giving some penetrations which need detailed discussions.

Classical Method of Analysis

In this method a thin plate theory is assumed with one to several penetrations and it is documented below.

A Thin Circular Plate with a Central Hole

We will compare in our investigations a "thin" circular plate uniformly loaded and fixed at its edges with a similarly loaded plate containing a central hole. This central hole is assumed to be closed by a simply supported plug. These two plates are shown in their radial cross-sections in Fig. 4a, b, respectively.

The solution of the problem for a monolithic circular plate is given in Timoshenkots 'Strength of Material'. Part 11 on page 97.

The moments at a distance x from the centre of the plate are

radially
$$Mrm = \frac{q}{16} \left[a^2 (I + v) - x^2 (3 + v) \right]$$
 (AIB.1)

tangentially $M \text{tm} = \frac{q}{16} \left[a^2 (I + v) - x^2 (1 + 3v) \right]$ (AIB.2)



Fig. A1B.1 Moments in radial and tangential directions



Fig. AIB.2 Circular hole in the circular plate


Fig. AIB.4

Where a is the outer radius of the plate. On assuming Poisson's ratio v to be equal to zero one obtains

$$Mrm = \frac{q}{16}(a^2 - 3x^2)....$$
 (AIB.3)
$$Mtm = \frac{q}{16}(a^2 - x^2)....$$
 (AIB.4)

A plate with a central closed penetration can be considered as a monolithic plate additionally loaded by a radial bending moment M uniformly spaced along the central hole. Assuming that this plug is fully discontinuous with the plate

Appendix B

$$M = \frac{q}{16}(a^2 - 3b^2)$$
(AIB.4)

For a 'ring plate' loaded uniformly over its inner edge by a moment M' we have (from equation of Timoshenko's 'Strength of Materials')

The angular deflection

$$\phi = \frac{c_1 x}{2} + \frac{c_2}{x} \tag{AIB.6}$$

$$M'rx = D\frac{\mathrm{d}\phi}{\mathrm{d}x} = D\left[\frac{c_1}{2} + \frac{c_2}{x^2}\right]$$
(AIB.7)

$$M'tx = D\frac{\mathrm{d}\phi}{x} = D\left[\frac{c_1}{2} + \frac{c_2}{x^2}\right]$$
(AIB.8)

For the boundary conditions we have

 $\boldsymbol{\varphi}=\boldsymbol{0}$

when
$$x = 0$$

Which gives $c_2 = c_1 - \frac{a^2}{b^2}$ (a) (AIB.9)
We also have $M'rx = M'$ when $x = b$ (b)
And hence $M' = D\left(\frac{c_1}{2} + \frac{c_1}{2}\frac{a^2}{a^2}\right)$ (c)
or $c_1 = \frac{2M'}{D}\frac{b^2}{a^2+b^2}$ (d)
And $c_2 = \frac{-M'}{D}\frac{b^2a^2}{a^2+b^2}$ (e)

Substituting these values into Eqs. (AIB.7) and (AIB.8), one has

$$M'rx = M' \left[\frac{b^2}{a^2 + b^2} + \frac{a^2}{x^2} \frac{b^2}{a^2 + b^2} \right] = M' \frac{b^2}{x^2} \frac{a^2 + x^2}{a^2 + b^2}$$
(AIB.10)

$$M'tx = M'\left[\frac{b^2}{a^2+b^2} - \frac{a^2}{x^2}\frac{b^2}{a^2+b^2}\right] = -M'\frac{b^2}{x^2}\frac{a^2-x^2}{a^2+b^2}$$
(AIB.11)

Substituting the values of M' from equation one obtains

$$M'rx = \frac{a}{16}(a^2 - 3b^2)\frac{b^2}{x^2}\frac{a^2 + x^2}{a^2 + b^2}$$
(AIB.12)

$$M'tx = \frac{a}{16}(a^2 - 3b^2)\frac{b^2}{x^2}\frac{a^2 - x^2}{a^2 + b^2}$$
(AIB.13)

Adding, respectively, these Equations one obtains the formulae for the perforated plate.

$$Mrp = \frac{a}{16} \left[a^2 - 3x^2 - (a^2 - 3b^2) \frac{b^2}{x^2} \frac{a^2 + x^2}{a^2 + b^2} \right] \text{ for } x \ge b$$
(AIB.14)

Appendix B

$$Mtp = \frac{a}{16}(a^2 - x^2) \left[1 + \frac{b^2}{x^2} \frac{a^2 - 3b^2}{a^2 + b^2} \right] \text{ for } x \ge b$$
(AIB.15)

Comparing the Eqn. (AIB.1) and (AIB.2) with Eq. (AIB.30) we can calculate ratios of bending moments and hence of stresses in plates with and without a central hole under one uniform load.

The radial bending stress concentration for factor Cr is assumed to be

$$Cr = \frac{Mrp}{Mrm} = 1 - \frac{a^2 - 3b^2}{a^2 + 3x^2} \frac{b^2}{x^2} = \frac{a^2 + x^2}{a^2 + b^2}$$
(AIB.16)

If $(x^2 \neq a^2)$

The tangential bending stress concentration factor C_t was assumed to be

$$Ct = \frac{Mtp}{Mtm} = 1 - \frac{b^2}{x^2} \frac{a^2 - 3b^2}{a^2 + b^2}$$
(AIB.17)

The values of Cr are

$$Cr = 0 \text{ for } x = b$$

$$Cr = 1 + \frac{b^2}{a^2} \frac{a^2 - 3b^2}{a^2 + b^2} \text{ for } x = a$$
(AIB.18)

If $a_2 = 9.68b^2$ and similarly it could be any ratio between *a* and *b* for 9 ft hole, Cr9 = 1.0646 and for 11'.0 hole central

$$a^2 = 6.48b^2$$

 $Cr11 = 1.0718$ (AIB.19)

The maximum value Ct if reached at the edge of the hole (x = b), then

$$Ct = \frac{1 + \frac{a^2}{b^2} - 3}{\frac{a^2}{b^2} + 1}$$
(AIB.20)

Then Ct9 = 1.627

$$Ct11 = 1.465$$
 (AIB.21)

Radial stress
$$Cr = \frac{\text{Bending stress with penetration}}{\text{Bending stress with no penetration}}$$
 (AIB.22)

Let us say $=\frac{624 \operatorname{psi}()}{700 \operatorname{psi}()} = 0.90$ $Ct = \frac{\text{Bending stress with penetration}}{\text{Bending stress with no penetration}} = \frac{57 \operatorname{psi}}{250 \operatorname{psi}} = 2.05$ (AIB.23)

Analysis of the Effect of the Large Penetrations

No reliable general method of analysing 3D stress problems in a body without circular symmetry was available for use in this. For this reason, the analysis of the stress distribution in a vessel with large penetrations consists of the extrapolation and combination of the results obtained by several less sophisticated methods of analysis.

The practical problems of the large penetrations can be divided into the following categories:-

- a) The effect of a non-symmetrical arrangement of penetrations on the stress distribution in the whole vessel.
- b) The local stress concentrations in the perforated vessel cap or *slab*.

For the reason given above, the latter problem was analysed separately for the biaxial and triaxial loading conditions. Stress concentration factors are derived for the biaxial loading condition. Additional stress concentration factors for the triaxial loading condition are calculated. The use of these factors is explained in many relevant text on stress concentration.

Biaxial Loading Conditions

Method of Analysis

The analysis was performed using the finite-element method. The results obtained by this technique are compared with the results for the same problem solved by a theoretical analysis based on classical method.

Description of the 3D Finite-Element of Computer Programme

Three-dimensional is a method for solving static problems. The solution is obtained using a set of stress–strain relationships and dynamic–equilibrium equations. The set of equations is solved using already given in the text the finite–element forms of the equations. As the equilibrium equations contain damping factors, the required static solution is approached. By an appropriate choice of the damping factors, the structure vibrates with a 'dead beat' form and so a sufficiently accurate static solution is quickly reached.

The Simplified Model of Vessel Cap

The bottom cap or top of the vessel is analysed as a perforated disc under biaxial, loading and triaxial. This simplification gives a good approximation to the conditions of cap prestressed by hoop cables. The effect of a uniform bending moment can also be treated as a special case of the plane stress analysis. However, the effect of a varying bending moment (caused by the curvature of the prestressing cables and internal pressure) cannot be truly estimated by means of such an analysis. Hence 3D finite–element is involved for this kind of work.

The Arrangement of the Loading

The radial stresses in the cap or slab are created either by the hoop tendons or by the interaction between the cap and the cylindrical art of the vessel. For this reason the radial forces loading the disc were assumed to be.

Results of the Finite-Element Analysis

The following types of bottom cap were analysed under different loading conditions. Cases 1–4 relate to an internal vessel diameter of 28 ft. Case 5 considers a vessel internal diameter of 29 ft.

- (1) A disc of 44'.0" dia without any penetration was analysed under the loading arrangements 'A'.
- (2) A disc of 44'.0" dia with two 11'.0" dia holes was analysed under the loading arrangements 'B' and 'D'.

The biggest stress concentration was found to be loading along the axis of these two penetrations. The resultant stresses together with the field stress are shown for loading 'B' in graph (). The reduction of these stresses under loading 'D' was rather small. The two peak values under 'B' were 2790 and 2400 psi; and the loading 'D' stresses at the same respective points were 2690 and 2100 psi.

The curve giving the ratio of the local stress in the perforated cap over the 'field stress' in the monolithic cap is given on Graph ().

Th comparison of the average radial deformation of the monolithic and perforated cap gives the ratio of 1.78 (the value could be used to simulate presence of the holes in the finite-element program ISOPAR).

(3) A disc 44'.0" dia with two 11'.0" hole and two 5'.0" holes was analysed under loading condition 'B'.

The result of this analysis is given on the graph ().

The ratio of the average radial deformation in this case was equal to 1.97
(4) The ring 44'.0" outside and 28'.0" inside diameter was loaded by the forces type 'C' identical in value to loading 'D' of disc (2) (44'.0" outside dia with two 11'.0" dia holes.)

The contours of the principal stresses on the ring are shown on graph.

Theses stresses vary from 3700 to 2240 psi on the inside face and from 2550 to 1500 psi on the outside face.

Therefore the variation over average stress is about $\pm 25\%$ on the inside face for the 'worst' (i.e. most unsymmetrical) arrangement of holes.

(5) The disc of 46'.0" dia with one 9'.0" central hole and two 5'.0" and from 4'.0" dial holes concentrically spaced around it was loaded uniformly spaced in the radial direction over a ring of thickness equal to the thickness of the vertical wall of the vessel.

The distribution of field stresses (σ_1) in unperforated disc follows the diagram shown in Fig. ()

A loading of radial forces uniformly spaced around the vessel parameter represents the loading due to action of hoop stresses.

The loading imposed on the cap by the interaction between the cap and the barrel of the vessel can be uniform only for a circularly symmetrical arrangement of holes in the disc. For the unsymmetrical arrangement of the holes (say two 11'.0" dia holes) this interaction will not be uniform around the circumference of the vessel. An uneven radial distortion of this cap will produce an uneven distribution of the 'continuity force' between the cap and the barrel. The effect of this variation will reduce the absolute values of the maximum local stresses in the cap, and increase locally, stresses in the barrel. The variation of these continuity forces can be assumed to be proportional to the deflection of the cap.

To simulate the above effects the following loading arrangements were analysed by the finite element.

(A) A disc without penetration was loaded by radial forces uniformly distributed both around its circumference and across the width equal to the vessel's wall thickness. Infact, it is a thick-walled slab.

The "stress field" obtained by this loading is used to calculate stress concentration factors in the next calculation.

- (B) A disc with penetration is loaded by the same forces as for case 'A'. The ratio of stresses obtained by this loading over the 'field stresses' from case (A) gives the values of the stress concentration factors.
- (C) A ring representing the vessel's barrel was loaded by radial forces uniformly distributed along the radial direction but not circumferentially. The total value of these factors is the same as for cases 'A' and 'B'. The magnitude of the varies circumferentially in the inverse proportion to the ratio of the actual over the average radial deformation of the disc under loading 'B'.
- (D) A perforated disc (as in case B) is then loaded in the same manner as the ring in case 'C'.

By the force type 'B', the results were compared with the unperforated disc of 44'.0'' diameter.

The error introduced by this difference is estimated to be in the order of $\pm 4.5\%$. The directions of the maximum principal stresses for perforated disc are shown in graph later on. The values of the maximum principal stresses are given as a ratio of the 'field' stress obtained from the analysis of the

unperforated plate. The ratio of the average deflection for the two cases is equal to 1.655 (also with an error of $\pm 4.5\%$).

The Comparison with the Theoretical Formulae

Some of the results of the finite-element calculations referred to above can be compared with results obtained from a simple classical analysis. Two methods of theoretical analysis were investigated.

The problem of an infinite plate with two holes loaded uniformly by a biaxial stress field is analysed in G.N. Savins book 'Stress Concentration Around Holes'. (pp. 134–139)

From the ratio

$$\lambda = \frac{7'6''}{5'6''} = \frac{15}{11}$$
(AIB.24)

One has from Savins table 25 the values of maximum stresses

$$\sigma A = \left(2.887 - \frac{0.133}{0.5} \times 0.476\right)p = 2.761p \tag{AIB.25}$$

$$\sigma B = \left(2.255 - \frac{0.133}{0.5} \times 0.097\right)p = 2.23p \tag{AIB.26}$$

The formulae given by Timoshenko (Trans. Royal. Society Series A, volume 221, p. 267, 1921) gives the maximum stress (of point B due to an internal pressure in a thick cylinder with an eccentric bore.)

The 'slice' of such a cylinder is shown in Fig. AIB.7. The formulae for the notation

$$\sigma' \max . = pi \left[\frac{2b^2(b^2 + a^2 - 2ae - e^2)}{(b^2 + a^2)(b^2 - a^2 - 2ae - e^2)} - 1 \right]$$
(AIB.27)

In our case we have

$$a = 5'6''$$

 $b = 22'0''$
 $c = 7'6''$

And hence

$$\sigma' \max . = pi \times 1.244 \tag{AIB.28}$$

In the absence of a similar formula for the effect of external pressure, compilation with some other theories is required. It seems a safe implication to assume that an external pressure instead of internal pressure would increase the above coefficient in the same proportion as for a cylinder with a central bore. Accepting this assumption we have F at the edge of the hole

Hoop stress
$$\sigma = \frac{a^2 p}{b^2 - a^2} \left(1 + \frac{b^2}{a^2} \right) = \frac{2pb^2}{b^2 - a^2}$$
 (AIB.29)

Hence

$$pi = p. \frac{2b^2}{a^2 + b^2}$$
 (AIB.30)

Therefore,

$$\sigma A \approx \sigma \max ... = p \times 1.244 \frac{2b^2}{a^2 + b^2} = 2.34p$$
 (AIB.31)

Comparing the factors and those shown on graph () derived from the finiteelement method, one has at point A.

Stress concentration factor obtained by computer analysis = 3.15 Stress concentration factor obtained by mathematical theory = 2.76 Ratio = $\frac{3.15}{2.76}$ = 1.14 Also at point B one has Stress concentration factor obtained by mathematical theory = 2.34 Ratio $\frac{2.7}{2.34}$ = 1.15

On can see from these ratios that the finite-element methods give both close and 'safe' results. The larger results obtained by the computer analysis are probably due to the fact that a more realistic boundary condition was used.

Triaxial Loading Conditions

The finite-element analysis described in this text deals adequately with radial loadings applied at the periphery of a disc but does not take into account the variation in radial load over the depth or radius of the disc. These variations arise from the effect of pressure loading, tendon curvature, continuity effects and the pressure of penetrations.

The study which follows attempts to evaluate the effects ignored in the simple biaxial analysis. Sections do examine three alternative approaches from which the most probable bending stress concentration factors are chosen.

Utilisation of the 'Yield Line Method' in the Elastic Analysis

Johansen's yield line method was developed for structures working in a plastic state stresses. For this reason, this method ignores the condition of continuity of deflection and retains only the condition of equilibrium of the internal and external forces. Nevertheless, this method can be safely applied in analysis of elastic problems as long as it is remembered that

- (a) The moments along a yield line now represent average, not constant, bending moments.
- (b) The ratio of the moments along different edges of any 'failed' panel must be in the same ratio to each other as the actual elastic average moments in an elastic stage of the structure.

This second condition creates great but not insurmountable difficulty. As long as the approximate range of these ratios can be estimated 'safe' results may be obtained by accepting in turn the 'worst' extremes of this range.

Two of the most probable yield line patterns for the basic vessel bottom cap are shown in Figs. AIB.5 and AIB.6. The simplified panels of these pattern are shown in Figs. AIB.7 and AIB.8, respectively, These figures are of an internal diameter of 29'0".

Let us consider the arrangement shown in Fig. AIB.7.



Fig. AIB.5 Vessel capat bottom



Fig. AIB.6 Vessel with penetrations



Fig. AIB.7 Sectoral cut zone



Fig. AIB.8 Sectoral cut with forces or moments

The edge force P/ft (reaction from the plug) is obtained by considering the equilibrium of the small triangle at the centre.

Hence,

$$p \times 4 = \frac{4}{2} 4q \tag{AIB.32}$$

or

$$P = 2q \tag{AIB.33}$$

Ignoring the effect (an error on the safe side) of the tangential moments 'm' between the outer ring of penetrations and the barrel position of the vessel, one has the equation of equilibrium for moments about line BC:

$$M_7 \times 14.5 + M_7 \times = \frac{7}{\sqrt{5}} = P \times .4 \times 10.5 + q \left(4 \times \frac{10.5^2}{2} + \frac{10.5}{3} \times \frac{10.5^2}{2} \right)$$
(AIB.34)

or $M_7 + 0.216 M_7 = 5.8q + 28.5q = 34.3q$ (AIB.34a)

or for the 28'0" internal diameter vessel

Appendix B

$$M_7 + 0.216M'_7 = 34.3q \times \frac{14^2}{14.5^2} = 32.0q$$
 (AIB.35)

For the arrangement shown in Fig. AIB.8, the equilibrium condition for moments about the line EF as

$$5.25M_8 + M'_8 \times = \frac{7}{\sqrt{5}} = P \times 4 \times 4.5 + q \ (4 \times \frac{4.5^2}{2} + \times \frac{4.5^2}{6} \times 5.75)$$

i.e. $M_8 + 0.596 \ M'_8 = 6.86q + 11.42q = 18.28q$ (AIB.36)

or for the 28'0" internal diameter vessel

$$M_8 + 0.596M'_8 = 18.26q \times \frac{14^2}{14.5^2} = 17.05q$$
 (AIB.36a)

For comparison we will analyse the yield line pattern for the cap without any penetrations. The failure yield line pattern of a disc is shown in Fig. AIB.9. The elementary failure panel is shown in Fig. AIB.10.







Taking moments about the outer edge we have

$$(M_0 + M'_0)Rd\phi = q\frac{Rd\phi}{2} \times \frac{R^2}{3}$$

Or $M_0 + M'_0 = q\frac{R^2}{6}$

Hence for R = 14'0" we have

$$M_{01} + M_{01}' = 32.7q \tag{AIB.37}$$

And R = 8'6"

$$M_{02} + M'_{02} = 12.03q \tag{AIB.38}$$

Comparing these values with Eqs. (AIB.35a) and (AIB.36a)

$$M_7 + 0.216M'_7 = \frac{32.0}{32.7}(M_{01} + M'_{01}) = 0.98(M_{01} + M'_{01})$$
 (AIB.39)

$$M_8 + 0.596M'_8 = \frac{17.05}{12.03}(M_{02} + M'_{02}) = 1.42(M_{02} + M'_{02})$$
(AIB.40)

The ratio of M_0/M'_0 is estimated from the Vany analysis for a vessel with no penetrations. The values given below have been taken from sketches PCPVD. The moments are assumed to be proportional the variation in stress through the depth of the cap.

| M'_{01} is approximately proprtional to 800 psi M'_{01} is approximately proprtional to 150 psi | at 14 ft radius |
|--|--------------------------|
| M_{02} is approximately proprtional to 370 psi | $a \pm 0/0//$ and $dima$ |
| M'_{02} is approximately proprtional to 200 psi | at 99 radius |

As stated previously we wish to compare the local stresses (which we have said are proportional to the local moments, M_7 , M_7 , M_8 and M_8 with the Vany results for vessels with simulated penetrations. Hence, the following moment values have been taken from sketches PCPVD.

- M_{p1} -Average radial (longitudinal) bending moment at the foot of the vertical walls. This moment is approximately proportional to 800 psi (5.52 MN/m²)
- M_{p2} -Average radial bending moment along the circle through the centres of the outer penetrations. This moment is approximately proportional to 385 psi (2.655 MN/m²)
- M'_{p1} -Average tangential (hoop) bending moment across the ring between the central penetration and the outer ring of penetrations. This moment is approximately proportional to 500 psi (3.448 MN/m²)

We can now rewrite Equations using these new moments: One has from Eq. (AIB.39)

$$M_7 = 0.216M'_7 = 0.98M_{pl}(1+0.188) = 1.165M_{pl}$$
(AIB.41)

Similarly $\frac{M_{02}}{M_{02}} = \frac{370}{200}$ we have from Eq. (AIB.40)

$$M_8 + 0.596M_8 = 1.42M_{02}(1 + 0.54) = 2.22M_{02}$$

Furthermore since,

$$\frac{M_{02}}{M_{p2}} = \frac{370}{385}$$
 and $\frac{M_{02}}{M_{p2}} = \frac{370}{500}$

We have from Eq. (AIB.40) either

$$M_8 + 0.596M'_8 = 1.42M_{p2} \tag{AIB.42}$$

or

$$M_8 + 0.596M'_8 = 1.62M_{p2} \tag{AIB.43}$$

In Eq. (AIB.42) the value of M_8 cannot be smaller than M_{p2} .

Hence one may write

$$0.596M_8' = 2.14M_{p2} - M_8 < 1.14M_{p2}$$

or

$$M'_8 < 1.92 M_{p2}$$

or since $\frac{M_{p2}}{M_{p2}} = \frac{385}{500}$

$$\frac{M'_8}{M_{p2}} < 1.48$$
 (AIB.44)

On the other hand, knowing that M'_8 cannot be smaller than M'_{p2} we have from Eq. (AIB.37)

 $M_8 = 1.64M'_{p2} - 0.596M'_8 < 1.044M'_{p2}$ and since

$$\frac{M'_{p2}}{M_{p2}} = \frac{500}{385}$$
(AIB.45)

$$\frac{M_8}{M_{p2}} < 1.36$$

Because theoretically we have $M'_7 = M'_8$ we have from Eq. (AIB.37)

$$M_7 = 1.165 \quad M_{pl} - 0.216 M'_8$$

or since M'_8 is bigger than M'_{p2}

Also $\frac{M'_{p2}}{M_{pl}} = \frac{500}{800}$ Therefore $\frac{M_7}{M_{pl}} < 1.03$

The formulae (AIB.44), (AIB.45), and (AIB.46) should give 'very safe' coefficient for the stress concentration at 'critical' zones in the bottom cap. Similar formulae could be found for other arrangements of the penetrations.

Large Penetration Under Pressure and Temperature



Notation

Giving assumed values where appropriate

R = radius a = internal radius = 14'

- b = external radius = 22'
- p = internal pressure = 705 psi
- x = external pressure = prestress
- t = temperature
- $ti = temperature crossfall 30^{\circ}C$
- α = coefficient of expansion = 13×10^{-6} (c degrees)⁻¹
- $E = \text{module of elasticity} = 5.25 \times 10^6$
- γ = poisons ratio = 0.15 or 0 (where neglected)
- σ_c = permissible working compressive stress = 2200 psi (for prestressed and internal pressure)
- σ_s = permissible working tensile stress = 500 psi
- σ_t = hoop stress due to temperature crossfall
- σ_p = hoop stress due to internal pressure
- σ_x = hoop stress due to prestress
- $\sigma_{\rm ti}$ = hoop stress on inside due to temperature
- σ_{to} = hoop stress on outside due to temperature
- $\sigma_{\rm pi}$ = hoop stress on inside due to internal pressure
- σ_{po} = hoop stress on outside due to intenal temperature
- σ_{xi} = hoop stress on inside due to pressure
- $\sigma_{\rm xo}$ = hoop stress on outside due to prestress

The vessel is assumed to consist of a long thick cylinder. For this condition the following formulae apply Internal pressure only:

$$\sigma p = \frac{a^2 p}{b^2 - a^2} \left(1 + \frac{b^2}{r^2} \right) \tag{AIB.46}$$

External pressure (prestress)

$$\sigma x = -\frac{b^2}{b^2 - a^2} \left(1 + \frac{a^2}{r^2} \right)$$
(AIB.47)



Fig. AIB.10 Sector for yield line analysis









For a general temperature distribution (symmetrical with respect to the axis and constant along the axis)

$$\sigma_t = \frac{E}{1-\gamma} \left[\frac{1}{r^2} \int_a^r \alpha \operatorname{trdr} + \frac{r^2 + a^2}{r^2(b^2 - a^2)} \int_a^b \alpha \operatorname{trr} - \alpha t \right]$$
(AIB.47a)

With a crossfall of magnitude *ti*, the equilibrium temperature distribution may be represented by the function

$$t = \frac{ti \log_e b/r}{\log_e b/a}$$
(AIB.47b)

Therefore we have the following:

$$\sigma t = \frac{E \alpha t i}{\frac{2(1-\gamma)\log_e b}{a}} \left[1 - \frac{\log_e b}{r} - \frac{\frac{a^2}{(b^2 - a^2)} \left(1 + \frac{b^2}{r^2}\right) \log_e b}{a} \right]$$
(AIB.48)

The derivation of the above formulae is given in Timoshenko, Strength of Materials, Part II, pp. 228–232.

Substituting in eq. (i), (ii), (iii) the values of *a*, *b*, *E* etc, we have the following:

$$\sigma p = 480 \left[1 - \frac{(22)^2}{r} \right] \tag{AIB.49}$$

$$\sigma_x = -1.68 \left[1 - \frac{(14)^2}{r} \right]$$
 (AIB.50)

$$\sigma_t = \left[-\frac{396}{r^2} - 2.66 \log_e \frac{(22)}{r} + 1.05 \right] \times 10^3$$
 (AIB.51)

With $\gamma = 0.15$

The values of the hoop stresses on the inside (r = 14') and outside (r = 22') are tabulated below.

| Internal press 705 psi | | Prestress X | psi | Temp. cross fall 30°C | | |
|------------------------|---------------|---------------|----------------|---|---|--|
| σ_{pi} | σ_{po} | σ_{xi} | σ_{xo} | σ_{ti} | σ_{to} | |
| + 1670 | +960 | -3.36X | -2.36 <i>X</i> | $(\gamma = 0.15)$ -1380 $(\gamma = 0)$ -1180 | $(\gamma = 0.15) + 1030 (\gamma = 0) + 875$ | |

The two limiting cases are On the inside

$$|\sigma ti + \sigma xi| \bar{<} |\sigma c| \tag{AIB.52}$$

On the outside For $\gamma = 0.5$

 $|-1380 - 3.36X| \le |-2200|$ (AIB.52a) Or $3.36X \le 820$ or $X \le 244$ psi

For $\gamma = 0$, the condition is

 $|-1180 - 3.36 X| \leq |-2200$ (AIB.52b) or $3.36X \leq 1020$ *i.e.* $X \leq 304$ psi

$$|+1030+960-2.36X| \leq |+500|$$

i.e. 1990-2.36X ≤ 500
or 2.36X ≥ 1490
i.e. X ≥ 6.32 psi (AIB.52c)

For $\gamma = 0$ the condition is

Equation (iii) gives For $\gamma = 0.15$

$$|+875+960-2.36X|| \leq |+500|$$

i.e. $1835-2.36X \leq 500$
or $2.36X \geq 1335$
i.e. $X \geq 566$ psi (AIB.52d)

The required range of prestress is therefore For $\gamma = 0.5$, $244 \ge X \ge 632$ psi

For $\gamma = 0$, $304 \ge X \ge 566$ psi

This is clearly impossible with given values of internal pressure and temperature and cross fall. For fixed internal pressure and vessel dimensions it is apparent that either the properties of the mix or the temperature cross fall must be altered. Therefore for further work the temperature cross fall was reduced to 20° C. The required range of prestress for this new cross fall is calculated below.

Since the stresses due to the temperature cross fall are proportional to the cross fall, the stresses due to the new cross fall are found by multiplying the temperature stresses Table (A) by $\frac{20}{30}$

For $\gamma = 0.15$

$$\sigma_{ti} = -1380 \times \frac{20}{30} = -920$$

$$\sigma_{to} = +1030 \times \frac{20}{30} = +687$$

For $\gamma = 0$,

$$\sigma_{ti} = -1180 \times \frac{20}{30} = -785$$

$$\sigma_{to} = +875 \times \frac{20}{30} = +583$$

Substituting in Eq. (AIB.52) we now get For $\gamma = 0.15$

> $|-920 - 3.36| \le |-2200|$ i.e. $3.30X \le 1280$ or $X \le 380$ psi

For $\gamma = 0$, the critical condition is

$$|-785 - 3.36| \le |-2200|$$

i.e. $3.36X \le 1415$
or $X \le 421$ psi

Equation (viii) now gives For $\gamma = 0.15$

$$|+687+960-3.36X| \le |+5000|$$

i.e. $1647-2.36X \le 500$
or $2.36X \ge 1147$
i.e. $X \ge 485$ psi

For $\gamma = 0$, the critical condition is

$$|+583+960-2.36X| \le |+500|$$

i.e. $|1543-2.36X| \le 500$
or $2.36X \ge 1043$
 $X \ge 442$ psi

The required range of prestress is therefore For $\gamma = 1.5 \ 380 \ge X \ge 485 \ \text{psi}$ For $\gamma = 0 \ 421 \ge X \ge 442 \ \text{psi}$

This case also gives an impossible value for the prestress. However, the difference is relatively small. As the calculation was based on a constant value of Young's Modulus and in practice Young's modulus fall of 20° C may be considered satisfactory. This is substantiated by that the formulae devised in Appendix A show that the effect of the varying *E* is to reduce the magnitudes of the stresses on the inner and outer faces of the wall. The computer analysis verifies that a cross fall of 20° C is acceptable.

Penetrations Liner Under Buckling

Again refer to Plates B.1 and B.2 finite-element technique to determine buckling and instability has been briefly formulated in the text. The European have given an improved design recommendations.

The European Prestandards ENV 1993-I-6 for the strength and stability of shell structures (eventually called 'shell eurocode') gives for the present buckling interaction case and the expansion is.

$$\left(\frac{\sigma_{xd}}{\sigma_{x\text{Rd}}}\right)^{k_x} \left(\frac{\tau_d}{\tau_{\text{Rd}}}\right)^{k_\tau} \le 1$$
(AIB.53)

With the boxed (i.e. provisionally recommended) values

$$k_x = 1.25, \ k_\tau = 200$$
 (AIB.54)

From the collected set of test and the own tests and from the numerical investigations carried out so far, the following tentative conclusions may be drawn:

- (a) The concave interaction design Eqs. (AIB.53) and (AIB.54) seems to be somewhat unconservative in the range of very thin-walled cylindrical shells that buckle purely elastically.
- (b) For medium-thick shells, the exponents according to Eq. (AIB.54) seem to be reasonable.
- (c) For thick shells of which the buckling is dominated by plasticity influences, the exponents according to Eq. (AIB.54) tend to deliver overconservative design predictions.

Based on shell theory, the load deflection curves based on 'half wave', 'whole wave' and 'half penetration sectional model' are plotted viewing load factor v.s displacement. They are shown in Fig. (a) of Plate AIB.3. In all penetrations the lower end is assumed as fixed and the upper end is stiffened by a rigid diaphragm. The basic displacement δ_{mb} is taken to be tateral as

$$\delta_{mb} = F_b L^3 E I \tag{AIB.55}$$

Where
$$F_b = (\sigma_y - \frac{R}{A}) \frac{I}{LR}$$
 (AIB.55a)

The final buckling behaviour is given in Plate AIB.3 while using three different models. The non-linear finite-element analysis results are plotted on the diagram (a) of Plate AIB.3 while keeping in mind the deformation of the welded stud, if any. Program ISOPAR is used to determine the buckling patterns indicated in Plates I, II and III. The maximum load factor indicates a 20% reduction in the buckling load due to an imperfection. The load factor over the non-linear bifraction load is 0.8 of the reduction is small, a large increase in the number of buckling waves. The buckling load in general is progressive but suddenly appears as computer outputs indicated 90° and 180°. Here multimodal initial imperfection is considered.

Boiler Penetration of Multi activity Vessels

The same analytical procedures are adopted as stated in the text and the nonlinear finite-element analysis given in the text under various loading conditions the boiler cavities are examined. Plates AIB.4 and AIB.5 summarized the results in the forms of stress-trajectories. These boiler holes or cavities have been discussed already in the text.





Stresses Across

Stresses at crossection under pressure and prestress + temperature Pressure from presstress = 4.67 MN/m^2 , Internmal pressure = 0

All values MN/m²



Plate AIB.5 Stresses across section



Plate AIB.6 Stresses around penetrations Thermoelastic stresses

- (a) Tangential stress along liner and outer forces
- (b) Case I = thermo elestic analysis

Case II = thermo-plastic analysis

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Concrete Part
v_c = \gamma_c = 0.15 to 0.2
```

 $E_c = 20 \text{ GN}/\text{m}^2$

Steel Part

 $V_s = 0.3 = \gamma_s$ $E_s = 200 \text{ GN/m}^2$ $P = \text{Internal pressure} = 4.45 \text{ MN/m}^2$

Appendix C Movements in Prestressed Concrete Reactor and Containment Vessels

General Note

A major part forming this appendix has been published by the author in 'Nuclear Engineering and Design' 50 (1978) pp. 463–473 by North Holland Publishing Company, under the same title. The same method can be applied to containment vessels for PWR where it can be proposed to place concrete using lift and bay arrangement for greater diameters and greater heights.

Reinforced and prestressed concrete reactor vessels are constructed by placing concrete using lift and bay arrangement. The vessels are built up in a number of individual bays. The size and shape of these bays and the order in which they are cast have a significant effect on the size and sense of construction movements. Lack of information about factors such as age of any bay before prestress, the time of year of casting and the time interval between adjacent vertical and horizontal bays would lead to costly design improvements and could lead to unforeseen technical problems both under operational and ultimate conditions. An attempt has been made to establish a philosophy and a rational method of assessing fairly accurately these movements. Various movements and their causes and effects are discussed in detail. A 3D finite-element, analysis discussed already in the text, is developed to predict these movements and to assess the behaviour of the vessel parameters under operational conditions. A computer programs F. BANG and ISOPAR, are developed and are tested against experimental and measured results.

Introduction

Prestressed concrete reactor vessels (PCRVs) have been recently adopted as primary containments for both the advanced and high temperature gas-cooled reactors. Among all the problems associated with this structure, the knowledge of predicted movements in certain parts of the vessel is still ambiguous. This chapter attempts to create a basis for the design of many plant components in relation to their built-in tolerances. Although symmetric and absolute relative movements are straightforward to calculate, the lack of knowledge concerning the complexity involved in evaluating the asymmetric movement can lead to costly design features which may be either cast into the vessel concrete or placed within the vessel itself. A 3D analysis using isoparametric elements is used to evaluate these movements under constructional and operational conditions. These movements, and the corresponding strains occurring in three dimensions, are built in to the ultimate load analysis. Under increasing gas pressure the vessel is analysed for pressure–displacement relationship with and without the initial built-in movements. In some cases the results have proved to be quite significant.

A computer program has been developed to determine these movements under constructional and operational conditions. A separate computer program is written to plot these movements using an plotter associated with IBM 7500. Finally, the theoretical model is tested against short-term partial experimental results obtained from Dungeness, Oldhury and Hartlepool vessels. The results for the Oldbury vessel are given in the text.

Philosophy of Movements

The object of this section is to discuss the philosophy of the causes, developments and the significance of movements and their effects on the safe operation of the vessel. In order to initiate such a discussion, it is logical to classify these movements on the basis of their presence at important stages during construction and operation.

Types of Movements

Constructional Movements

Constructional movements are defined as any movement of the pressure vessel concrete from the time of casting up to the application of prestress to the vessel. These movements are caused [1, 2, 3] by

- (1) changes in ambient temperature
- (2) shrinkage of the concrete
- (3) deformation under load
- (4) liberation and loss of heat of hydration

The constructional movements may he required in any one of the following two forms.

Absolute Construction Movements

The absolute construction movement of a point is defined as the movement of that point in the concrete relative to a fixed datum outside the vessel, from the moment of casting until prestress is applied to the vessel.

The absolute movements of any part of the vessel are given with respect to a datum on that vessel. The datum for vertical movements is taken as lie underside of the bottom cap. The vertical axis is taken as the datum for horizontal radial movements.

Relative Construction Movements

The relative construction movements of two points are the relative movements between the two points from the instant the second point is cast (the first point having already been cast) until prestress is applied to the vessel. The movements are given in the 3D coordinate systems which are discussed later in the development of the theoretical model. These movements can either be symmetrical or asymmetrical. When symmetry is considered, these movements occur within a vessel in which the concrete properties are entirely uniform and the loading of the vessel geometry are symmetrical about the vessel axis. The relative movement of two points on the vessel is the vertical movement of one point with respect to the other as datum. A similar definition holds for the relative radial movement of two points in the same vertical plane. For initial calculations it is assumed that the change in the distance between two points on the same horizontal plane is calculated from their absolute radial movements when the vessel is assumed symmetrical, it is safe to assume that no movement perpendicular to any radial line occurs.

The asymmetrical relative movements depend on variations which can be applied to some properties of concrete and to some loadings, and to the vessel geometry. The assessment of asymmetrical relative movements will be different to the one suggested for the symmetry. The vertical relative movements of two points will then be the vertical movement of one point with respect to the other as datum. The relative radial movement of two points on the same horizontal plane is the difference in the changes in their distances from the vessel axis. Similarly, the relative radial movement of two points in the same vertical plane is the difference in the changes in their distances from the vessel axis plus the difference in the changes in their distances from the vessel axis plus the difference in the changes in the distances of the vessel axis from its original position in the space at the levels of the two points under consideration. On the other hand the relative movements in the circumferential directions of the two points the algebraic sum of their movements are perpendicular to the radial lines through their original positions. In calculating these movement it is always advantageous to draw out the absolute movements of the two points.

Operational Movements

The operational movements are obtained by analysing the vessel under operational conditions. The reactor vessels [4, 13, 14–16] are analysed for several loading cases for these movements. Computer runs are also required in which the vessel properties, loading values, and summation factors are chosen so as to give the desired operation conditions. These independent computer runs are also necessary since they differ from the stress cases in that only the probable and maximum range of movements are calculated at the various stages in the vessel's life.

The probable movements are obtained by obtaining the expected elastic properties and the normal anticipated loads. It is suggested that the extreme movements should be the maximum inward and outward movements that are obtained by allowing extreme variation in elastic properties, shrinkage, cyclic expansion, prestress loss, pressure and coefficient of expansion, as well as for non-symmetrical conditions in the vessel. In addition to these maximum values, associated minimum values should also be calculated. They are obtained by considering the vessel subjected to the same loadings as with the maximum values but with the non-symmetry effects taken as being in the opposite direction to those used for the maximum values. These minimum values are used in the calculation of the relative movements.

Factors and Causes of Movements

Each of the individual movement factors may include general components as well as components special to the case being considered. Each of the many movement factors are components special to the case being considered. Each of the many movement factors is now discussed.

Effect of Creep

This is considered first since it is not only involved directly as a measure of the vessels stiffness but also indirectly because of its effect on prestress losses. Experimental work [2, 8, 10, 17] carried out to obtain specific strain curves indicates that a suitable relationship exists between the elastic modulus and creep rates and, of course, how much softening effect is there due to temperature.

The movements produced by externally applied loads are directly proportional to the specific strain values associated with the loading being considered. There is one difficulty, namely the complicated past history of loading and temperature. The calculation of specific strain values to be used are highly involved. Simplifying conservative assumptions have therefore been made in the theoretical model as regards the various ages of loading, time under loads and ruling temperatures. In the theoretical model the extreme value of the probable specific strain is considered as being that of a vessel loaded for 30 years at the normal working temperature, thus neglecting any occasions when the vessel is at a lower temperature, e.g. during shutdown periods. Will there be any significant effects, during shut down periods is extremely difficult to assess. In certain cases it is also difficult to judge which combination of affects will produce the desired results. For the maximum inward movements it is obvious that the specific strain must be as high as possible so as to obtain the greatest prestress movement. However, when maximum on toward movements are considered, pressure is involved and it is possible that a larger outward movement will occur with a low-specific strain value. These values have been incorporated in the input. Perhaps they will compensate for the muse caused by the shutdown effects.

Prestress Loads

The effect of prestress on the movement ranges are the prestress losses, variation of prestress and asymmetric effects. The prestress losses are in turn affected by specific strain values, temperature, concrete stresses, tendon stresses, successive tensioning during the prestressing operation, shrinkage and relaxation of the steel. In addition, high-specific strain values cause high losses by virtue of the larger deflections incurred. Temperature, in addition to increasing specific strains, also produces high relaxation losses in the tendons. The level of concrete stresses determines the amount of deformation likely to occur which is directly relatable to the tendon stresses and strains to determine the loss after prestress encountered by vessel deflections. During the prestressing stage, the tendons lose some force due to the stressing of the successive cables, and allowance must be made as compensation. The relaxation of the steel itself must be taken into account since it is being affected by the temperature. Table AIC.1 is examined.

Shrinkage is another factor tending to increase the losses and changes after prestress must be used in calculating its effects. Some allowance is made for any asymmetric effects in the vessel, the prestress layout and during the jacking operation these are usually allowed for by some overall factor. This aspect is considered in the ultimate load analysis.

Pressure Loadings

The pressure is a more determinable and controllable loading than prestress and the only special allowances are for the asymmetry of the vessel and a small factor to cover fluctuations, i.e. the gas incremental behaviour.

Temperature Loadings

The vessel temperatures are controlled fairly accurately so no great deviation from normal working temperatures should be considered in the theoretical model. For movements, either the *hot* or the *cold* vessel is used with sonic factor to cover variations in the expansion coefficient. The author emphasise this phenomenon to cover for the hot shutdown affects as stated earlier. By considering it, additional safety is maintained.

| Case | Combined items |
|------------------|---------------------------------|
| Prestress only | Elastic shortening |
| | Friction |
| | |
| Proof test | Steel relaxation (short term) |
| | Creep (short term) |
| | Elastic shortening |
| | Friction |
| | Internal proof pressure (1.15 X |
| | design pressure |
| | |
| Normal operation | Steel relaxation (long term) |
| | Creep (tong term) |
| | Elastic shortening |
| | Friction |
| | Thermal effects |
| | Internal design pressure (1.1 X |
| | working pressure) |
| | |
| Hot shut down | Steel relaxation (long term) |
| | Creep (long term) |
| | Elastic shortening |
| | Friction |
| | Thermal effects |

Shrinkage

Upper and lower bands of shrinkage are used in the computer program input which allow for both age and temperature effects. Programs ISOPAR and F. BANG are equipped with such shrinkages.

Cyclic Expansion

Following a number of temperature cycles of typical Wylfa limestone concrete [2, 8, 10, 17], it is essential that a permanent set should occur, and allowance should be made for this. However, for some concrete the effects could be much less.

Combination and Presentation of Movements

In the form of an output the movements required in a vessel as described above fall into two groups, namely absolute and relative movements. To obtain the range of possible concrete movements for presentation, movements due to the individual effects already mentioned are summed algebraically taking due account of the construction programme: for instance, the maximum negative strain of one point relative to another point or datum, due to a change of ambient temperature, does not necessarily coincide in time with the maximum negative strain due to shrinkage. In this case the maximum combined strain due to these two defects may not be the sum of the two individual maxima, but less than this sum, and should be calculated. The maximum range of movements which could occur is normally presented in the vertical, radial and circumferential directions.

For absolute movements Table AIC.2 gives the maximum anticipated inward and outward movements at the various sections used in the computer analysis. In the majority of cases one definite set of loading factors suffices for obtaining a set of movements but locally, due to vessel shape, prestress arrangements or method of support, a slightly different loading combination may be required, but in these cases the movements involved usually tend to be small.

For maximum outward movement at the centre of the top pressure and cyclic expansion are required to be among the factors included, but along the same axis at the bottom pressure and shrinkage are required, this difference being due to the relative positions of the points and supports. Another important point to be considered is that certain factors may be interdependent and so cannot be combined arbitrarily with their extreme ranges. For example, the minimum prestress losses occur with lowest specific strain values, but for maximum inward movement a vessel with high-specific strain is usually used. The method of presentation of the results depends to what use they are to be put. To indicate the significance of the various factors at a few selected points on the vessel, a diagrammatic representation of the movements in the form of a bar chart could be used.

The relative movements are more difficult to present and various methods are available. One way is to present the tables giving the maximum movements and their associated minimum movements together with a series of general rules

| | | CONCRETE DISPLACEMENTS FROM POSITIONS BEFORE PRESTRESS | | | ITEMS. | | | | | | |
|-------------------------|-------|---|----------------------|------|--------|---------|-------|-------|------------------|-------|---------|
| | | INWARD MOVEMENT | OUTWARD MOVEMENT | Ρ | P/S | т | 05 | S | S/S | с | CO. |
| | MIN. | P/S C | | 0 | MIN. | AMB. | - | 0 | MIN. | MAX. | AVERAGE |
| CAUSING | PROB. | S P/S | | 0 | PROB. | AMB. | - | PROB. | PROB. | PROB. | MIN. |
| DISPLACEMENT | MAX. | S | | 0 | MAX. | AMB. | - | MAX. | MAX. | MAX. | 0 |
| LOADING | MIN. | | P T S | D.P. | MAX. | WORKING | MIN. | MAX. | CHECK MIN/MAX | MIN. | MAX. |
| CONDITIONS CAUSING | PROB. | | P T C P/S S | W.P. | PROB. | WORKING | PROB. | PROB. | PROB. | PROB. | AVERAGE |
| OUTWARD DISPLACEMENT | MAX. | | P C T P/S | D.P. | MIN. | WORKING | MAX. | MIN. | CHECK MIN/MAX | MAX. | 0 |

| Ρ | = | PRESSURE P.S.I.G |
|------|-----|--------------------------|
| D.P. | = | DESIGN PRESSURE P.S.I.G |
| W.P | ! = | WORKING PRESSURE |
| P/S | = | PRESTRESS. |
| Т | = | TEMPERATURE. |
| œ | = | COFFEICIENT OF EXPANSION |

S = SHBINKAGE

S/S = SPECIFIC STRAIN.

= CYCLIC SRAIN.

= NET DISPLACEMENT.

CO = CARBONATION

PROB. = PROBABLE. AMB. = AMBIENT TEMPERATURE.

MIN. = MINIMUM. MAX. = MAXIMUM.

Table AIC.2 Chart of inward and outward displacements

for working out the relative movements. This method has its difficulties. It may be more prudent to use the second method. i.e., the relative movements arc calculated as individual problems so that, although the general rules are used, special allowances or treatments can be incorporated.

Having assessed the variation of material, prestress and temperature properties for the vessel, it is now possible to compute the symmetrical absolute movements to the accuracy of the assumed concrete properties, values of prestress losses, etc. To obtain these movements, it is necessary first to decide which combination of the variations in vessel properties will yield the maximum and minimum vessel movements.

Two combination factors are possible for maximum and minimum outward movements. It will be necessary to calculate each to establish the maximum and minimum outward movements at any one point on the vessel. It is suggested that in the light of the above arguments the combination of movements should be as indicated in Table AIC.2, which will be discussed later, is assimilating the input data on the lines suggested in Table AIC.2.

Three-dimensional Analysis of Movements

Three-Dimensional Analysis Techniques

A 3D analysis is carried out using isoparametric 20-node solid elements for concrete (Table AIC.3) with cubic displacement expansion in platform and a



Fig. AIC.1 (a),(b) Finite element idealisation of Oldbury vessel 20-node element, complete bay with spring locations

linear variation through the thickness of each lift and bay. The mutual response of concrete layers for lift and bays is represented by a linkage element (Fig. AIC.1b). The stiffness matrix for this element is given in table. It is assumed that while using these linkage elements the degrees of freedom of the isoparametric elements are retained at their boundaries so that the interconnection between concrete layers can be made at their interfaces. The stiffness assigned to the bond linkage is the slope of the bond-slip curve multiplied by the embedded item surface area A_s tributary to a "kink" to form in the embedded items such as ducts or reinforcement bars. The shear at the kink acts as a dowel force and is represented by vertical linkages.

When the vertical linkages are in tension, their stiffness is controlled for the most part by adhesion between the embedded items and the concrete and could

| | L | Li 0 | |
|---|--|---|--|
| $k_{\rm H} {\rm C}^2 + k_{\rm V} {\rm S}^2$ | $k_{\rm H} { m SC} - k_{ m v} { m SC}$ | $-k_{\rm H}C^2 - k_{\rm H}S^2$ | $-k_{\rm H} { m SC} + k_{\rm V} { m SC}$ |
| $h_{\rm H}SC - k_{\rm V}SC$ | $k_{\rm H}S^2 + k_{\rm V}C^2$ | $-k_{\rm H}SC + k_{\rm v}SC$ | $-k_{\rm H}S^2 - k_{\rm v}C^2$ |
| $-k_{\rm H}C^2 - k_{\rm v}S^2$ | $-k_{\rm H}{ m SC}$ + $k_{\rm v}{ m SC}$ | $k_{\rm H} {\rm C}^2 + k_{\rm v} {\rm S}^2$ | $k_{\rm H}SC - k_{\rm v}SC$ |
| $-k_{\rm H}SC + k_{\rm v}SC$ | $-k_{\rm H}S^2 - k_{\rm v}C^2$ | $k_{\rm H} { m SC} - k_{ m v} { m SC}$ | $k_{\rm H}S^2 + k_{\rm v}C^2$ |

Table AIC.3 Matrix $[K_L]$ for linkage elements

where $S = \sin \beta$, $C = \cos \beta$.

Sign convention + positive movement and tensile force between the connected.

| Г | $K_{11} = \frac{(1-v_{23}v_{32})}{v}E_1$ | $K_{12} = \frac{(v_{12} + v_{12}v_{32})}{v}E_2$ | ${}^{*}K_{13} = \frac{(v_{13}+v_{12}v_{23})}{v}E_{3}$ | $K_{14} = 0$ | $K_{15} = 0$ | $K_{16} = 0$ |
|---|---|---|---|-------------------|-------------------|-------------------|
| | $K_{21} = \frac{(v_{21} + v_{23}v_{31})}{\bar{v}}E_1$ | $K_{22} = \frac{(1-v_{13}v_{31})}{\bar{v}}E_2$ | ${}^{*}K_{23} = \frac{(v_{23} + v_{13}v_{21})}{\bar{v}}E_{3}$ | $K_{24} = 0$ | $K_{25} = 0$ | $K_{26} = 0$ |
| | $K_{31} = \frac{(v_{31} + v_{21}v_{32})}{\bar{v}}E_1$ | $K_{32} = \frac{(v_{32} + v_{12}v_{31})}{\bar{v}}E_2$ | $K_{33} = \frac{(1-v_{12}v_{21})}{\overline{v}}E_3$ | $K_{34} = 0$ | $K_{35} = 0$ | $K_{36} = 0$ |
| | $K_{41} = 0$ | $K_{42} = 0$ | $K_{43} = 0$ | $K_{44} = G_{12}$ | $K_{45} = 0$ | $K_{46} = 0$ |
| | $K_{51} = 0$ | $K_{52} = 0$ | $K_{53} = 0$ | $K_{54} = 0$ | $K_{55} = G_{23}$ | $K_{56} = 0$ |
| L | $K_{61} = 0$ | $K_{62} = 0$ | $K_{63} = 0$ | $K_{64} = 0$ | $K_{65} = 0$ | $K_{66} = G_{31}$ |
| | | | | | | |

Table AIC.4 Variable modulus and Poisson's ratio stiffness matrix [D]

where $\bar{v} = 1 - v_{12}v_{21} - v_{13}v_{31} - v_{23}v_{32} - v_{12}v_{23}v_{31} - v_{21}v_{13}v_{32}$

 Table AIC.5
 CABCO prestressing tendon main data

 Tendon Forces (kN)

| | | | Tendor | I Forces | (KIN) | | |
|-----------|------------|------------|--------|----------|-------------------|----------------------|-------------------------|
| Anchorage | System | Tendon* | P_k | 0.8Pk | 0.7P _k | Anchorage size mm | Sheath internal dia. mm |
| | | 4/13 STD. | 660.0 | 528.0 | 462.0 | 130 | 42 |
| U1 | Cabco | 4/13 SUP. | 736.0 | 588.8 | 515.2 | " | " |
| | | 4/13 DYF. | 836.0 | 668.8 | 585.2 | " | " |
| | | 4/15 STD. | 908.0 | 726.4 | 635.6 | 175 | 51 |
| | | 4/15 SUP. | 1000.0 | 800.0 | 700.0 | " | " |
| | | 4/15 DYF. | 1200.0 | 960.0 | 840.0 | " | " |
| U2 | Cabco | 7/13 STD. | 1155.0 | 924.0 | 808.5 | " | " |
| | | 7/13 SUP. | 1288.0 | 1030.4 | 901.6 | " | " |
| | | 7/13 DYF. | 1453.0 | 1170.4 | 1024.1 | " | " |
| | | 4/18 STD. | 1480.0 | 1184.0 | 1036.0 | 175 | 51 |
| | | 4/18 DYF. | 1520.0 | 1216.0 | 1064.0 | " | " |
| | | 7/15 STD. | 1589.0 | 1271.2 | 1112.3 | 215 | 75 |
| | | 7/15 SUP. | 1750.0 | 1400.0 | 1225.0 | " | " |
| | Cabco | 7/15 DYF. | 2100.0 | 1680.0 | 1470.0 | " | 63 |
| U3 | | 12/13 STD. | 1980.0 | 1584.0 | 1386.0 | 215 | 81 |
| | | 12/13 SUP. | 2208.0 | 1766.4 | 1545.6 | 215 | " |
| | Multiforce | 12/13 STD. | 1980.0 | 1584.0 | 1386.0 | 215 | " |
| | | 12/13 SUP. | 2208.0 | 1766.4 | 1545.6 | 215 | " |
| | | 7/18 STD. | 2590.0 | 2072.0 | 1813.0 | 245 | 81 |
| | | 7/18 DYF. | 2666.0 | 2128.0 | 1862.0 | " | 75 |
| U4 | Cabco | 12/13 DYF. | 2508.0 | 2006.4 | 1755.6 | " | 75 |
| | | 12/15 STD. | 2724.0 | 2179.2 | 1906.8 | " | 81 |
| | | 12/15 SUP. | 3000.0 | 2400.0 | 2100.0 | " | 81 |
| | Cabco | 12/15 DYF. | 3600.0 | 2880.0 | 2520.0 | 265 | 81 |
| | | 19/13 STD. | 3135.0 | 2508.0 | 2194.5 | " | " |
| U5 | | 19/13 SUP. | 3496.0 | 2796.8 | 2447.2 | " | " |
| | Multiforce | 12/15 STD. | 2724.0 | 2179.2 | 1906.8 | 245 | " |
| | | 12/15 SUP. | 3000.0 | 2400.0 | 2100.0 | 245 | " |
| | | 12/15 DYF. | 3600.0 | 2880.0 | 2520.0 | 265 | " |
| | | 25/13 STD. | 4125.0 | 3300.0 | 2887.5 | 300 | 90 |
| U6 | Multiforce | 25/13 SUP. | 4600.0 | 3680.0 | 3220.0 | " | " |
| | | 13/15 DYF. | 3900.0 | 3120.0 | 2730.0 | " | 84 |
| | | 31/13 STD. | 5115.0 | 4092.0 | 3580.0 | 335 | 100 |
| | | 31/13 SUP. | 5704.0 | 4563.2 | 3992.8 | " | " |
| U7 | Multiforce | 19/15 STD. | 4313.0 | 3450.0 | 3019.1 | " | " |
| | | 19/15 SUP. | 4750.0 | 3800.0 | 3325.0 | " | " |
| | | 19/15 DYF. | 5700.0 | 4560.0 | 3990.0 | " | " |

| Tendon Forces (kN) | | | | | | | | |
|--------------------|------------------|------------|----------------|----------|-------------------|----------------------|-------------------------|--|
| Anchorage | System | Tendon* | P _k | $0.8P_k$ | 0.7P _k | Anchorage size mm | Sheath internal dia. mm | |
| U8 | Multiforce | 19/18 DYF. | 7220.0 | 5776.0 | 5054.0 | " | " | |
| | | 5/18 STD. | 1776.0 | 1480.0 | 1295.0 | 362×89 | 114×25 | |
| | | 5/18 DYF. | 1824.0 | 1520.0 | 1330.0 | " | " | |
| | Strand- force | 10/18 STD. | 3530.0 | 2960.0 | 2590.0 | 362 × 171 | " twin | |
| | | 10/18 DYF. | 3648.0 | 3040.0 | 2660.0 | " | " twin | |

SUP. Super Strand DYF. Dyform Strand

be set equal to zero. The stiffness of these vertical linkages that are in compression will depend on such factors as the geometry, the concrete cover, and the presence or absence of the embedded items in that zone of the vessel concrete. The stiffness matrix for the solid element is derived using the orthotropic material matrix given in Table AIC.4. The procedure for the stiffness matrix is summarized in Table AIC.5. The program ISOPAR is provided with two solution procedures, namely the B LOCKING TECHNIQUE and the FRON-TAL SOLUTION.

Temperature, creep and shrinkage effects are included in the general formulation of the strain matrix. The details of this program are given in the text.

Concrete Stress–Strain Criteria

Concrete stress–strain criteria, plasticity and cracking [14, 15, 16, 17, 19, 20, 21, 22] have been assessed. In this work the hypoelastic approach is adopted for the multiaxial state of stress, the details of which are given in Ref. [23].

Summary of Results

Movement parameters for the Oldbury vessel, obtained from the theoretical model and from site measurements, are plotted in Fig. AIC.2 and AIC.3 for critical locations of this vessel.

They are in good agreement for many critical locations. However, at certain locations variations in results exist between the theoretical model and those obtained on site. Although net differences in value are insignificant in terms of the overall achievement of tolerances, a suitable explanation can be given.

Finite element data Strain = $\{\varepsilon\} = [B_i]\{\delta\}$ (AIC.1)


Fig. AIC.2 Absolute movements of Oldbury reactor vessel

where

$$[B_{i}] = \begin{bmatrix} \frac{\partial \rho i}{\partial x} & 0 & 0\\ 0 & \frac{\partial \rho i}{\partial y} & 0\\ 0 & 0 & \frac{\partial \rho i}{\partial z}\\ \frac{\partial \rho i}{\partial y} & \frac{\partial \rho i}{\partial x} & 0\\ 0 & \frac{\partial \rho i}{\partial z} & \frac{\partial \rho i}{\partial y}\\ \frac{\partial \rho i}{\partial z} & 0 & \frac{\partial \rho i}{\partial x} \end{bmatrix} = \frac{1}{\det |J|} \begin{bmatrix} B_{1}, & \cdots & B_{1,n}\\ \vdots & & \vdots\\ & & & \vdots\\ & & & & \\ B_{m,1} & \cdots & B_{m,n} \end{bmatrix}_{m \times n = 6 \times 6}$$
(AIC.2)

 $Stress = \{\sigma\} = [D](\{\varepsilon\} - \{\varepsilon_0\}) + \{\sigma_0\}$ (AIC.3)



Fig. AIC.3 Relative movements of the Oldbury reactor vessel

where \in_0 and σ_0 = initial strain resp. stress and ρ = shape function. [K] _{6 × 6} = element stiffness matrix

$$= \int_{-1}^{+1} \int_{-1}^{+1} \int_{-1}^{+1} [B]_{6\times n[D]6\times 6[B]6\times n \det[J] \, d\xi \, d\eta \, d\xi.}^{T''}$$
(AIC.4)

Forces:

$$\{F\} = \int_{V} [B]^{T''}[D]\{\varepsilon\} d\zeta \, d\mu \, d\zeta \tag{AIC.5}$$

T'' = Transpose

$$\{R_j\} = [K]^e \{\delta\} + \{F_x\}^e_b + \{F_x\}^e_f + \{F\}^e_{\sigma_o} + \{F\}^e_{\varepsilon_o} + \{F\}^e_t$$
(AIC.6)
elastic bond body initial temperature

Heat of Hydration

The effect on vessel movements of the heat of hydration of cement on settling is mainly felt during construction in the theoretical model; this was taken to have no further effect occur 100 days after any bay is cast. Although the figure of 100 days assumed is quite normal, this may not be so in the contractor's construction program.

Shrinkage

In order to establish the rate of increase or instantaneous values of shrinkage for any part of the vessel, it is necessary to know when a particular bay is poured and how long after the pour the temperature was applied. This might have even not been known to the contractors as different time interval is a time-dependent quantity and is extremely difficult to measure. In the theoretical model the shrinkage of concrete is related to time and temperature loading. For input the minimum shrinkage line starts from 0 to 100 microstrains. The initial gradient of the maximum shrinkage line is then continued until the temperature is applied and it rises linearly to a maximum of 400 microstrains.

Temperature Regions

This is a complex phenomenon. Movements are mainly caused by a uniform temperature across the section since the shrinkage rates are dependent on this uniform temperature. This may not be the case for temperature crossfall which causes large stresses and strains with negligible movements. The combined effect of these has been assumed in the analysis.

The age of the concrete at the time of different measurements may vary, which also has an effect on the value of the coefficient of thermal expansion.

Creep Rate

The creep rate is dependent on the type of aggregate, mixed proportion and temperature. The average values and rate increases are subject to a variation of $\pm 30\%$ due to the different quality of aggregate from any one pit and the daily variation of the mix. Only one specific rate is taken in the theoretical model on the basis of the available information. The vessel may have a different creep rate at different parts and they may be dependent also on the age of the concrete at loading. Although such variations have not been considered in the present input of the computer program, they can easily be handled by the theoretical model.

Boundary Restraints

The definition and provision of true partial restraints in the program at the level of skirt line is rather difficult. Owing to the limited computer storage, the restraint defined is the rollers in the horizontal direction and linkage effect in the vertical dimension. A rigid base or a base fully restrained was not considered since they would prevent movements and would unnecessarily cause stresses in the concrete. In fact, in practice the bottom of the cap is not rigidly jointed; instead it rests on the pads placed at a pitched circle diameter of the supporting ring column Structure.

Data for Reactor Vessels

In order to validate the theoretical model, data for the Oldburv reactor vessel are considered. This reactor vessel is a vertical concrete cylinder with top and bottom concrete flat caps. The prestressing tendons are arranged in the walls in a helical system at 45° with 11 layers running clockwise and 11 anticlockwise. Each layer contains 160 tendons. Some tendons are diverted and brought back to position since a systematic pattern of tendons cannot be followed at penetration through the walls. The tendons are anchored in the top and bottom stressing galleries creating even pitch around a circle for each layer. In both the top and bottom slabs the tendons are arranged in horizontal layers.

General Data

Tendons: PSC type 12 no/15 mm diameter having nominal high tensile steel strands with minimum g.u.t.s. 277 t per tendon.

Gas design pressure = 3.45 MN/m^2 .

The main dimensions are

$$2R_{\rm I} = 18.3 {\rm m}$$
 $2H_{\rm I} = 23.5 {\rm m}$
 $t = 4.6 {\rm m};$ $D_{\rm I} = D_2 = 6.7 {\rm rm}$

where R_1 = internal radius, H_1 = internal height, t = wall thickness and D_1 , D_2 = cap thickness top and bottom. The minimum cube strength of concrete at 28 days is 41.37 KN/mm².

Conventional reinforcement

Primary 40 mm diameter Secondary 12 mm diameter

Prestressing losses:

Vertical tendons: initial 3.5% commissioning 7.4%, 30 years 16.7%

Temperature: inside 59°C, outside 20°C Elastic and creep ratio for concrete: 0.18. Lift of concrete to be placed: 1.34 m. E_s = Young modulus of steel = 200 KN/mm². E_c = Young modulus of concrete = 41.4 KN/mm². v = Poisson's ratio for steel = 0.3 Coefficient of linear thermal expansion:

Concrete 8.0 $\mu M/m^{\circ}C$, Steel 10.0 $\mu M/m^{\circ}C$.

Thermal conductivity:

Steel = $41.6 \text{ W/m} \circ \text{C}$, Concrete = $1.75 \text{ W/m} \circ \text{C}$.

Liner thickness = 12 mm.

Studs = 12×16.3 mm pitch not exceeding 305 mm, 324 fuelling pipes and 81 control rods with outer diameter 190 mm.

Provision for holes and equipment for man access penetration, BCD penetrations, corrosion and monitoring sample tubes, CO_2 inlet penetration thermo couples and gas or circulator ducts. Total weight of appliances, 36 66 750 kg, suitably distributed at an assumed 35 number of lifts based on their locations.

Conclusions

At the beginning of this appendix various questions were raised regarding the accuracy of determining movements under constructional and operational conditions. As is evident from the above discussions, results from the proposed theoretical model compare quite well with those measured in the Old bury vessel. Unfortunately, at the time of completing this appendix no results were available from the Hartlepool and Dungeness vessels, which are under construction, and therefore, theoretical results could not be compared.

In the Oldbury vessel with a complicated tendon geometry, the analysis for constructional movements shows that the fuelling line in the top cap is not straight and fuelling pipes in the stand pipe zone have moved individually from 3.3 to 12.5 mm from their original marked positions measured from the datum of the vessel. These figures have been improved when the vessel is prestressed longitudinally and circumferentially and correspondingly they range from 1.7 to 6.13 mm. Obviously these figures need consideration since the fuelling machine will be relatively out of alignment with the stand pipes. The comparative results show that these have been considered.

It is suggested that this method will give a useful guide to the other important areas of equipment where movements may take up excessive tolerances and thus introduce costly design improvements. As and when more data are released, a great deal of sophistication can be achieved in these results by using the suggested theoretical model. The reader may attempt to work on the results of Hartlepool and Dungeness B measured results.

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AIC.1 Appendix: ISOPAR And F. BANG

The complete program for the computing movements and Elasto—plastic analysis is given in a separate Appendix and the flowchart is given here in.



Appendix D Safe Analysis for Cooling Pipes for Reactor And Containment Vessels

General Note

Major part forming this appendix has been published by the author in the *Nuclear Engineering and Design*, 55(1979), pp. 305–313 by North Holland Publishing Company under the same title. The same can be applied to containments for PWR where cooling pipes are needed. The parameters will be different and care is taken to simulate data for Program ISOPAR or similar computer packages. The major analysis will still be applied to any kind of vessels.

A step-by-step analysis is given for the direct computation of 2D heat flow and safe pitching of the cooling pipes. Two models of the cooling system have been selected and calculations have been carried out for an existing vessel. On the one model this analysis is compared with the 3D finite-element analysis for obtaining insulation conductance for various cooling pipes. A safety factor is established.

Introduction

The cooling system is located behind the steel liner which is keyed back to the concrete by an extensive array of lugs. The design features of a cooling system depend on the reactor vessel lay out and the method of anchoring of the liner. In this chapter a conventional type of reactor vessel, namely Dungeness B, is chosen which has common design features of other vessels [1-3] and in which the heat exchangers are contained within the main pressure envelop. The heat flow through the liner and the concrete is therefore divided into two parts:

- (a) Flow in the liner
- (b) Flow in the concrete

General equations are required for the heat flow along the liner to the cooling pipe and in the main concrete. These equations derived in this Chapter which gives the values of maximum temperature insulation thicknesses and



Fig. AID.1 Reactor liner insulation and concrete

conductances. Using these equations and knowing values of certain coefficients, the safe pitch value between any two cooling pipes is evaluated.

To produce a fully optimised design, further work is carried out on the arrangements of cooling pipes in regions where nuclear heating varies and which forms a large part of the heat loading of the system. All the temperature distributions derived have been calculated on the basis of a 3D isoperimetric finite-element analysis using frontal solutions [4]. For the vessel liner a basic mesh of 12 mm is used with an adiabatic boundary at a depth of 37 mm.

The overall width of the mesh is taken to be half the pipe pitch, extending from the centre liner of the cooling water pipe to a point midway between adjacent pipes. The geometry of the cooling system adopted in the calculations consists of two 19 mm I.D and 25 mm O.D. mild steel pipes welded to the liner as shown in Fig. AID.1. A computer program ISOPAR [7] is written to carry out various solutions to the finite-element analysis.

Analysis for Heat Flow in the Liner

Heat flow equations are derived using a model insulation system given in Fig. AID.1.

Section (I)–(I). Heat flow equation (I)

$$-Kt_s(d^2T/dx^2)dx = [T_G - \theta]C_idx + qdx.I.t_s$$
(AID.1)

or

$$T = Ae^{\lambda x} + Be^{-\lambda x} + T_G + qt_s/C_i = Ae^{\lambda x} + Be^{-\lambda x} + T_G + q_o/\mu C_i \quad (AID.2)$$

Where A, B are constants and $\lambda = \sqrt{C_i/Kt_s}$.

Appendix D

When the following boundary conditions are applied, constants A and B are computed:

x = 0; dT/dx = 0, at x = 0, A = B, at $x = \frac{1}{2}l_{sp}$; $T = T_1$

$$A = [T_l - T_G - q_o/\mu C_i] / \left[\exp\left(\frac{1}{2}\lambda l_{\rm sp}\right) + \exp\left(-\frac{1}{2}\lambda l_{\rm sp}\right) \right]$$

Substituting in Eq. (AID.1), T_{max} at x = 0 is given by

$$T_{\rm max} = \frac{-T_G + T_l - q_o/\mu C_i}{\cos h \frac{1}{2} \lambda l_{\rm sp}} + T_G + q_o/\mu C_i$$
(AID.3)

Net heat flow along (AID.2)-(AID.3) gives

$$-K\frac{1}{2}\phi \, dT/dy = -K\frac{1}{2}\phi[(T_i - T_l)/l_c] = -Kt_s \, dT/dx \qquad (AID.4)$$

But

$$dT/dx = (T_l - T_G q_o/\mu C_i)\lambda \tanh \lambda \frac{1}{2} l_{sp}$$

Therefore

$$T_{i} = \frac{\frac{1}{2}K\phi T_{i}/l_{c} + Kt_{s}\lambda \tan h(\frac{1}{2}\lambda l_{sp})(T_{G} + q_{o}/\mu C_{i})}{\frac{1}{2}K\phi/l_{c} + Kt_{s}\tan h(\frac{1}{2}\lambda l_{sp})}$$
(AID.5)

Knowing values of T_{max} , T_i and T_G using Eqs. (AID.3) and (AID.4), the values of l_{sp} is computed.

Analysis for Heat Flow in Concrete

Heat flow equations are derived in this section and reference is made to an idealised situation given in Fig. AID.2.

For 2D gas it is assumed that the heat flow is between two parallel boundaries. The nuclear heating is represented by

$$q = q_0 e^{-\mu x} \tag{AID.6}$$

Considering 3 strip of unit depth and thickness

at
$$x = 0, T = T_1$$
; at $x = t : T = T_\ell$ (AID.7)



Fig. AID.2 Temperature on concrete

Both heat flow across and that generated in the element are summed up and the total heat flow equation is represented by

$$-K(\mathrm{d}^2T/\mathrm{d}x^2)\mathrm{d}x = q_o e^{-ux}\mathrm{d}x$$

Upon integration, the value of T is computed as

$$T = -(q_o/K\mu^2)e^{-\mu x} + Cx + D$$
 (AID.8)

Applying boundary conditions given in Eq. (AID.7) values of C and D are computed and the following equation is derived:

$$D = T_1 + q_o/K\mu^2$$

$$T_l = -(q_o/K\mu^2)e^{-\mu t} + Ct + T_1 + q_o/K\mu^2$$
(AID.9)

At x = t, $T = T_l$ heat flow

$$K dT/dx = (q_o/K\mu)e^{-\mu t} + C$$
 (AID.10)

where

$$C = 1/t[(T_l - T_1) + (q_o/K\mu^2)(e^{-\mu t} - 1)]$$

$$D = T_1 + q_o/K\mu^2$$
(AID.11)

Since μt is large at x = t and $e^{-\mu t} \to 0$. $\therefore dT/dx = C$ Heat flow to ambient temperature $= h_t(T_t - T_l) = K.C.$ Appendix D

Hence

$$T_{l} \frac{h_{t}T_{t} + K_{t} \cdot T_{1} + q_{o}/t\mu^{2}}{h_{t} + K/t}$$
(AID.12)

For T_{max} , $dT/dx = 0 = (q_o/K\mu)e^{-\mu x} + C$, hence C is determined, i.e. $\mu x = t_n - q_o/CK\mu$,

$$\eta = -q_o/CK\mu \qquad (AID.13)$$
$$T_{\max} = \frac{C}{\mu} \left(1 + \frac{q_o}{C\mu} \right) + D = \frac{C}{\mu} (1 + t_n.\eta) + D$$

Analysis of Conductance and Insulation Thickness

Independent analysis of conductance: Mean temperature of the liner, using mean value theorem give

$$\theta_m = \frac{2}{l_{\rm sp}} \int_0^{1/2l_{\rm sp}} \left(T_G + A \cos h\lambda x + B \sin h\lambda x \right) dx \qquad (AID.14)$$
$$= \left(\frac{2}{l_{\rm sp}} \right) \left[\frac{1}{2} T_G l_{\rm sp} + (A/\lambda) \sin h \frac{1}{2} \lambda l_{\rm sp} \right]$$
$$= \left[T_G + \frac{2}{\lambda^2 l_{\rm sp}} \frac{1}{2} t_\omega (T_w - T_1')}{t_{\rm s}.l_{\rm c}} \right] \qquad (AID.15)$$

Where T'_1 the average temperature between the cooling pipe web and the liner.

$$T_{1}' + \left\{ \frac{l_{c}t_{s}\lambda T_{G} + \frac{1}{2}t_{\omega}.T_{W}\cot h(\frac{1}{2}\lambda l_{sp})}{l_{c}t_{s}\lambda + \frac{1}{2}t_{\omega}\cot h(\frac{1}{2}\lambda l_{sp})} \right\}$$
(AID.16)

Eliminating T'_1 between Eqs. (AID.15) and (AID.16) and rearranging the terms, the value of C_i is given by

$$C_{i} = \frac{12Kt_{s}(\theta_{m} - T_{G})}{l_{sp}(l_{sp} + 6t_{s}.l_{c}/\frac{1}{2}t_{\omega})(T_{G} - \theta_{m})}$$
(AID.17)

Insulation thickness

$$t_i = (K/C'_i)[(T - \theta_m)/(T_G - \theta_m)]$$
(AID.18)

If k varies with mean temperature, the approximate relationship is given by

$$K = 0.00267\theta'_m + 1.533 \tag{AID.19}$$

Where θ'_m is $100 < T < 700^{\circ}$ C and

$$\theta'_m = \frac{1}{2}(T + \theta_m) \tag{AID.20}$$

 C_i'' = insulation conductance giving a mean temperature 60°C

Three-Dimensional Finite Element Analysis

A more refined analysis is required for hear conduction, conductance and insulation thickness in 3D space. Assuming θ represent θ_m and T'_1 , then at any point the temperature θ satisfies an equation of heat conduction, provided initial and boundary conditions are given

$$\rho C_p \partial \theta / \partial T' = \operatorname{div} \left(\bar{K} \operatorname{grade} \theta \right) + q, \qquad (AID.21)$$

where ρ , C_P , K, q, $\partial T'$ denote density, specific heat, conductivity, heat generation rate and incremental time, respectively.

For a convective heat transfer from the surface, the heat flux, f, is related as

$$f = \bar{K} \cdot \frac{\partial \theta}{\partial \hat{n}} = h_i \ (T - \theta) \tag{AID.22}$$

where \hat{n} is the direction of the outward normal from the surface. For an insulated surface f = 0 and for steady-state condition $\partial \theta / \partial T' = 0$ but in other cases the temperature is allowed unboundedly though at a constant rate. An approximate solution is obtained by dividing the whole vessel and particularly the cooling system area into a series of isoparametric elements. In this case a 20-node isoparametric (Fig. AID.3) is chosen. One assumption is made and that is if the finite set of unknown temperatures consists of the temperature θ at the centroid of the element, then the following representation of the above equations for any element is true:

$$C'_{i}\frac{d\theta}{dT'} = \sum_{j=1}^{n} b_{ik}(\bar{\theta}_{k} - \theta_{i}) = q_{i}$$
(AID.23)

where θ_j and $\overline{\theta}_k$ the finite element and boundary temperatures, θ_j is the temperature of the ith element, C'_i is the heat capacity of an element equal to ρC_p , and *a*'s, *b*'s are constant coefficients known as 'admittances'. The *a*'s measure

Fig. AID.3 Threedimensional isoparametric 20 node hexahedron



the ease with which heat can pass between the one isoparametric element and another and the b s measure the ease with which heat can pass between any isoparametric element an a boundary. The exact form of admittances depends on the particular 3D geometrical configuration.

In the finite-element process, the left-hand side of Eq. (AID.23) is approximated by Crank–Nicholson method and is given by

$$\{\theta_m(T' = \Delta T') - \theta_m(T')\}/\Delta T'$$
 (AID.24)

and the right-hand side by means of its value at time T' and $T' + \Delta T'$. A set of equations is obtained for the centroidal temperatures $\theta_m(T' + \Delta T')$ in terms known values $\theta_m(T')$. These equations are solved by iteration. Choosing a small enough time step, the iteration converges rapidly. For a steady-state condition, the right-hand side of Eq. (AID.21) must be equal to zero. A more detailed finite element version of Eqs. (AID.23) and (AID.24) is given in the text.

During the solution of Eq. (AID.23), Eqs. (AID.17), (AID.18), (AID.19) and (AID.20) are examined for conductance and insulation thickness. Appendix E gives a general layout of the subrouti terma of Program ISOPAR written for CDC 6600/7630. A provision is made in this program for determining conductance with and without nuclear heating.

Application to Dungeness B Vessel

In order to test the above analysis, data given below for the Dungeness B vessel is used.

Data

| Cooling water (T_w) | |
|--|--|
| Maximum temperature | 35°C |
| Velocity | 4ft/s (1.22m/s) |
| K values (thermal conductivity): | |
| Steel | 26 CHU ft/ft ² $^{\circ}$ C (45 W/m $^{\circ}$ C) |
| Concrete | 0.84 CHU ft/ft ² h °C (1.445 W/m °C) |
| Insulation | 2.00 CHU ft/ft ² r °C (0.29 W/m°C) |
| Concrete heat transfer coefficient (h_i) At outer face 1.5 CHU/ft ² hr °C | (4.733 Wm ² h °C) |

| Gas temperature in vessel | 450°C to 750°C |
|---|---|
| local to wall (TG) | |
| Ambient temperature at outside wall of vessel | $25^{\circ}C$ |
| Liner thickness (t_s) or t_w | $\frac{1}{2}$ in to $\frac{3}{4}$ in (12–19 mm) |
| Volumetric heating in vessel liner | 152.0 CHU/ft ³ h |
| - | $(5663.4 \text{ CHU/m}^3 \text{ h})$ |
| Volumetric heating in vessel concrete | $34.36 e^{-1.953}$ |
| - | CHU/ft ³ h |
| | $(1280 \text{ e}^{-1.953} \text{kJ/m}^3)$ |
| Average temperature ($\theta_{\rm m}$) | 60°C |
| Cooling pipe pitch $(I)_{sp}$ | 6 in. (150 mm). × 10 in. (250 mm) |
| | 14 in. (350 mm) and 18 in. (450 mm) |
| | CHU/ft ² h °C. |
| Insulation conductance (C_i) | (W/m [°] C) |
| Thickness of concrete (<i>t</i>) | 12 ft 6 in. (3.81 m) |

Initial Specimen Calculations

For the Dungeness vessel parameters, the specimen calculations are carried out for maximum temperatures developed in the liner and in the concrete in the presence of cooling pipes at suitable pitches. Figures AID.1 and AID.2 are used. For the liner, using $t_s = 19$ mm. $T_1 = 29.4$ °C, $C_1 = 0.4$, $T_G = 750$ °C the following parameters are obtained:

$$\lambda = 0.496, q_o/\mu = 59.6, l_c = 0.875,$$
(AID.25)

$$T_{\text{max}} = 46^{\circ}C, l_{sp} = 277 \, mm \, (10.9'').$$
(AID.26)

$$I_{\text{max}} = 46^{\circ}C, \ l_{sp} = 277 mm (10.9^{\circ}).$$
 (AID.26)

For concrete, the following parameters are obtained:

$$T_t = 26.67^{\circ}C, T_1 = 82.23^{\circ}C, h_t = 1.5,$$
 (AID.27)

$$q_o = 71.6, K = 0.84, T_2 = 31.5^{\circ}C, T_{\text{max}} = 93.2^{\circ}C.$$
 (AID.28)

| Pitch | | | | | |
|--------------|---------------------------------------|------|------|------|-------|
| | Insulation conductance C_1 | 0.4 | 0.6 | 0.8 | 1.0 |
| 6 in. | Mean membrane temp. $\theta_{\rm m}$ | 54.7 | 63.2 | 71.3 | 79.1 |
| (150 mm) | Max. membrane temp. T_{max} | 55.9 | 64.9 | 73.5 | 81.8 |
| | Insulation conductance. C_i | 0.2 | 0.4 | 0.6 | 0.8 |
| 10 in. | Mean membrance temp. $\theta_{\rm m}$ | 52.0 | 65.5 | 78.1 | 89.7 |
| (250 mm) Max | Max. membrane temp. T_{max} | 53.6 | 68.2 | 82.0 | 94.7 |
| | Insulation conductance C_i | 0.3 | 0.4 | 0.5 | 0.6 |
| 14 in. | Mean membrane temp. $\theta_{\rm m}$ | 68.1 | 76.8 | 85.1 | 93.1 |
| (350 mm) | Max. membrane temp. T_{max} | 72.1 | 81.9 | 91.2 | 100.1 |
| | Insulation conductance C_i | 0.2 | 0.3 | 0.4 | |
| 18 in. | Mean membrane temp. $\theta_{\rm m}$ | 66.4 | 77.9 | 89.3 | |
| (450 mm) | Max membrane temp. T_{max} | 71.2 | 84.5 | 97.5 | |

 Table AID.1
 Vessel liner results

Values of the mean and maximum liner temperature for each combination of pipe pitch and insulation conductance are given in Table AID.1. The values of conductance are based on Eqs. (16) and (17). In the Dungeness B vessel pipe pitches greater than 150 mm are not practicable, the reason being that the space



| Insulation hot face temp. 450 | 0°C |
|-------------------------------|----------------|
| Pipe pitch - 6' (150 mm) | 0.4 |
| Insulation conductance | 0.6 |
| | → → 0.8 |
| | →→→ 1.0 |

Fig. AID.4 Isotherm pattern



Fig. AID.5 Dungeness B type vessel temperature distribution

available for the insulation is limited to about 75 mm rather than only on economic grounds. The estimate of the thickness of the insulation for a given mean temperature at a given cooling pipe pitch is given by Eqs. (AID.18) and (AID.20).

Using three-dimensional finite element analysis and considering the cooling pipe zone in the vessel where cooling tubes lie on each side of the lug attached to the liner, isotherm patterns are drawn for insulation conductance varying from 0.2 to 1.0. In this case the insulation hot face temperature is taken to be 450°C. The cooling pipe pitch is maintained as 150 mm. Nuclear heating in the liner and concrete is included in the analysis. Figures AID.4 and AID.5 show such isotherm pattern using program ISOPAR with subroutine TERMA.

Comparison of Two Methods of Calculation

To make a comparison on the basis of neglecting nuclear heating in both methods of calculation, the insulation thicknesses at 450°C hot face temperature appropriate to liner/concrete wall are converted back to conductance using the assumed conductivity of 2 CHU in./ft² h °C (0.29 W/m °C). The comparative values of C_i , the insulation conductance, are given in Table AID.2 for different cooling pipe pitches and with and without nuclear heating. The results are in good agreement among themselves and with those obtained from prototype data (1, 6).

| | Table AID.2 Compariso | on of insulation conducta | nces | | | | | |
|-----------------------|--|---------------------------|-------------------------|--|--|--|--|--|
| | Insulation conductance C_i (CHU/ft ² h °C) for $T_m = 60^\circ$ C and $T_G = 450^\circ$ C | | | | | | | |
| | Direct approach $C_{\rm f} = 0.832/p(p + 4)$ | Finite element | Finite element | | | | | |
| Cooling pipe pitch | Nuclear heating neglected | Nuclear heating included | Without nuclear heating | | | | | |
| 6 in. (150 mm) | 0.370 | 0.528 | 0.356 | | | | | |
| 10 in. (250 mm) | 0.207 | 0.310 | 0.215 | | | | | |
| 14 in. (350 mm) | 0.138 | 0.203 | 0.159 | | | | | |
| 18 in. (450 mm) | 0.101 | 0.146 | 0.115 | | | | | |

-----. ~ .

Conclusions

A simplified approach for computing temperature distribution in the steel liner and concrete of prestressed concrete reactor vessels has been presented. A provision is made in this analysis for estimating the cooling pipe pitches, insulation thicknesses and conductances. A 3D finite-element analysis has been carried out for comparison and validation of the above analysis.

Notation

- $C_{\rm i}$ = conductance of insulation
- h_t = heat transfer coefficient from outer concrete surface to ambient temperature
- k = thermal conductivity
- $l_e =$ length of cooling pipe from the liner
- $I_{\rm sp}$ = pitch between cooling pipes
- $T' = \text{time } \Delta T' = \text{time increment}$
- T = temperature; T'' transpose
- t = thickness of concrete
- t_i = thickness of insulation
- $t_s = \text{liner thickness}$
- $\theta_{\rm m}$ = mean temperature; $\theta_{\rm n}$ = temperature at nodes
- φ = equivalent diameter of cooling pipe
- $\lambda, \mu = =$ coefficients defined in the text
- x = distance measured from the liner concrete interface

P = shape function $\rho =$ density

Appendix D.1 3-D Finite Element Formulation Basic Thermal Diffusion Equation

Equations (D.21), D.22 and (D.23) are referred basic thermal diffusion equation

$$\left[\bar{C}_{p}\right]\left[\dot{\theta}\right] + \left[K\right]\left\{\theta\right\} = \left\{\bar{q}\right\} = \left\{\begin{array}{c}q_{x}\\q_{y}\\q_{z}\end{array}\right\}$$
(D.1)

Heat flow temperature virtual work

$$\{\bar{q}\} = [D][\dot{\theta}] \tag{D.2}$$

where

$$[D] = \begin{bmatrix} \bar{K}_{xx} & 0 & 0\\ 0 & \bar{K}_{yy} & 0\\ 0 & 0 & \bar{K}_{zz} \end{bmatrix}$$

$$\dot{\theta} = \text{temperature vector} = \begin{bmatrix} \frac{\partial \theta}{\partial x}(x, y, z) \\ \frac{\partial \theta}{\partial y}(x, y, z) \\ \frac{\partial \theta}{\partial z}(x, y, z) \end{bmatrix}$$

$$\delta w = \text{virtual work} = \int_{v} \{\delta \dot{\theta}\}^{T''} \{\bar{q}\} \, \text{dvol} = \{\delta \theta_n\}^{T''} \quad (D.3)$$
$$\int_{v} \{B\}^{T''} [D][B] \, \text{dvol} \{\theta_n\} \quad (D.4)$$

where

$$[B] = \text{strain displacement matrix} = \begin{bmatrix} \left[\frac{\partial p}{\partial x} \right]^{T''} \\ \left[\frac{\partial p}{\partial y} \right]^{T''} \\ \left[\frac{\partial p}{\partial z} \right]^{T''} \end{bmatrix}$$

 $\{\theta_n\}$ = nodal or centroidal temperature; $\{p\}$ shape function $\theta(x, y, z) = [P]^T \{\theta_n\}$

The virtual work associated with convective surfaces Equation (D.22) is referred to internal

Appendix D

$$\delta w_1 = \int_A \delta \Delta q \theta_n d \text{ (area)}$$

$$\Delta \theta = \theta(x, y, z) - T$$
(D.5)

 $q_{\hat{n}} =$ vector direction normal to the surface $= h_t \Delta \theta$

Hence

$$\delta w = \{\delta \theta_n\}^{T''} \ddot{q} \int_{v} [P] \,\mathrm{dvol} \tag{D.6}$$

 \ddot{q} = rate of heat generation/unit volume. The virtual work associated with a change stored energy in the light of Eq. (D.2) is written as

$$\delta w = \int_{v} \delta \theta_{(x,y,z)} \rho C_{p} \frac{\delta \theta_{(x,y,z)}}{\delta T'} dvol$$

$$= \{\delta \theta_{n}\}^{T''} \rho C_{p} \int_{v} \{P\} \{P\}^{T''} dvol [\dot{\theta}_{n}]$$
(D.7*a*)

where

$$[\dot{\theta}_n] = \delta\{\theta_n\}/\delta T'$$

Total element conductivity and specific heat material conductivity matrix

$$[K_c]_c = h_t \int_A \{Pl_\theta\} \{Pl_\theta\}^{T''} dA$$
 (D.8)

Specific heat matrix

$$[K]_{cp} = \rho C_p \int_A \{P\} \{P\}^{T''} dvol$$

The element heat flow matrix

$$\{q\}_c = h_l T \int_A \{Pl_\theta\} dA \{q\}_g = \ddot{q} \int_v \{P\} dvol dvol = det \{J\} d\xi d\eta d\zeta$$

Time integration scheme quadratic

$$\begin{bmatrix} \frac{2\Delta T'_o + \Delta T'_1}{\Delta T'_d} \frac{1}{\Delta T'_o} \{\bar{C}_p\} + [\bar{K}] \end{bmatrix} \{\theta\}$$

= $[\bar{q}](T') + \{\bar{C}_p\} \left(\frac{\Delta T'_d}{\Delta T'_o \Delta T'_1} \{\theta_{T-1}\} - \frac{\Delta T'_o}{\Delta T'_d - \Delta T'_1} \{\theta_{T-2}\} \right)$

where $T'_o =$ initial time, $T'_1 =$ previous considered time, $T'_2 =$ previous time considered, $T'_d = T'_o - T'_2$, $\{\theta_{T-1}\}$, etc. = temperature at previous time steps.

Appendix D.2 Subroutine terma



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Appendix E Programs Subroutines (For ISOPAR and F. BANG)

E.1 Introduction

This appendix gives short repetitive notes first associated with programs ISOPAR and F. BANG. These are then followed by computer listings of these programs.

E.2 Mass Matrices and Stiffness Matrices and Others

 Table AIE.1 Stiffness and mass matrices (courtesy STRUCOM, London)

 Orders of degree of freedom

The stiffness matrix in element co-ordination

Where

- A = element cross-sectional area
- E = Youngs's modulus
- L = element Length
- C_1 = value given in the below

$$[S_1] = \frac{F}{L} \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & C_2 & 0 & 0 & -C_2 & 0 \\ 0 & 0 & C_2 & 0 & 0 & -C_2 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -C_2 & 0 & 0 & C_2 & 0 \\ 0 & 0 & -C_2 & 0 & 0 & C_2 \end{bmatrix}$$

| Table AIE.1 | | | | | | | |
|--|---|--|--|--|--|--|--|
| Value of stiffness coefficient (C _i) | | | | | | | |
| Previous iteration resulted in a tensile strain | Previous iteration resulted in a compressive stress | | | | | | |
| 1.0 | 0.0 | | | | | | |
| 0.0 | 1.0 x 10 1.0 | | | | | | |
| $1.0 \ge 10^{-6}$ | 1.0 | | | | | | |



Fig. AIE.1 Threedimensional elastic beam

Stiffness and mass matrices (courtesy STRUCOM, London) Orders of degrees of freedom The stiffness matrix in element co-ordinates is:

 $[K_{1}] = \begin{bmatrix} AE/L & & & & \\ 0 & a_{z} & & & \\ 0 & 0 & a_{y} & & & \\ 0 & 0 & 0 & GJ/L & & & \\ 0 & c_{z} & 0 & 0 & e_{y} & & \\ 0 & c_{z} & 0 & 0 & 0 & e_{z} & & \\ -AE/L & 0 & 0 & 0 & 0 & AE/L & & \\ 0 & b_{z} & 0 & 0 & 0 & d_{z} & 0 & a_{z} & & \\ 0 & 0 & b_{y} & 0 & c_{y} & 0 & 0 & 0 & a_{y} & \\ 0 & 0 & 0 & -GJ/L & 0 & 0 & 0 & 0 & GJ/L & \\ 0 & 0 & d_{y} & 0 & f_{y} & 0 & 0 & 0 & c_{z} & 0 & \\ 0 & c_{z} & 0 & 0 & 0 & f_{z} & 0 & d_{y} & 0 & 0 & \end{bmatrix}$ Symmetric e_y

Where

$$A = \text{cross} - \text{sectional area} \qquad M_t = (\rho A + m)L(1 - \varepsilon^{in})^{T}$$

$$E = \text{Young's modulus} \qquad \rho = \text{density}$$

$$L = \text{element length} \qquad m = \text{added mass}$$

$$G = \text{shear modulus} \qquad \varepsilon^{\text{in}} = \text{prestrain}$$

$$r_y = \sqrt{\frac{I_{yy}}{A}} = \text{radius of gyration} \qquad A_z = A\left(r_z, \phi'_y\right)$$

$$A_y = A\left(r_y, \phi'_z\right)$$

$$r_y = \sqrt{\frac{I_{yy}}{A}} = \text{radius of gyration} \qquad B_z = B\left(r_z, \phi'_y\right)$$

$$[M_1] = M_t \qquad F_y = F\left(r_z, \phi'_y\right)$$

$$[K_{1}] = \begin{bmatrix} 1/3 & & & & F_{y} = F(r, \phi'_{z}) \\ 0 & A_{z} & & & F_{y} = F(r, \phi'_{z}) \\ 0 & 0 & A_{y} & & & \\ 0 & 0 & -C_{y} & 0 & E_{y} & & \\ 0 & C_{z} & 0 & 0 & 0 & E_{z} & & \\ 1/6 & 0 & 0 & 0 & 0 & 1/3 & & \\ 0 & B_{z} & 0 & 0 & 0 & D_{z} & 0 & A_{z} & & \\ 0 & 0 & B_{y} & 0 & -D_{y} & 0 & 0 & 0 & A_{y} & \\ 0 & 0 & 0 & -J_{x}/6A & 0 & 0 & 0 & 0 & J_{x}/3A & \\ 0 & 0 & D_{y} & 0 & F_{y} & 0 & 0 & 0 & C_{y} & 0 & E_{y} \\ 0 & D_{z} & 0 & 0 & 0 & F_{z} & 0 & -C_{z} & 0 & 0 & 0 & E_{z} \end{bmatrix}$$



Fig. AIE.2 Order of degree of freedom

and where

$$\begin{aligned} A(r,\phi') &= \frac{13/35 + 7/10\phi' + 1/3\phi'^2 + 6/5(r/L)^2}{(1+\phi')^2} \\ B(r,\phi') &= \frac{9/70 + 3/10\phi' + 1/6\phi'^2 - 6/5(r/L)^2}{(1+\phi')^2} \\ C(r,\phi') &= \frac{(11/210 + 11/120\phi'^2 + 1/24\phi'^2 + (1/10 - 1/2\phi')(r/L)^2)L}{(1+\phi')^2} \\ D(r,\phi') &= \frac{(13/420 + 3/40\phi' + 1/24\phi'^2 - (1/10 - 1/2\phi')(r/L)^2)L}{(1+\phi')^2} \\ E(r,\phi') &= \frac{(1/105 + 1/60\phi' + 1/120\phi'^2 + (2/15 + 1/6\phi' + 1/3\phi'^2)(r/L)^2)L^2}{(1+\phi')^2} \\ F(r,\phi') &= \frac{(1/140 + 1/60\phi' + 1/120\phi'^2 + (1/30 + 1/6\phi' - 1/6\phi'^2)(r/L)^2)L^2}{(1+\phi')^2} \\ J &= \text{torsional moment of inertia} = \begin{cases} J_x & \text{if } I_x = 0 \\ I_x & \text{if } I_x \neq 0 \end{cases} \end{aligned}$$

 I_x = input as I_{XX} I_x = Polar moment of inertia = $I_y + I_z$

AIE.2.2 The element mass matrix in element co-ordinates

$$\begin{split} &[M_1] = (\rho A + m)L \big(1 - \varepsilon^{\text{in}}\big) \\ \times \begin{bmatrix} 1/3 & 0 & 0 & 1/6 & 0 & 0 \\ 0 & A(r,\phi') & C(r,\phi') & 0 & B(r,\phi') & -D(r,\phi') \\ 0 & C(r,\phi') & E(r,\phi') & 0 & D(r,\phi') & -F(r,\phi') \\ 1/6 & 0 & 0 & 1/3 & 0 & 0 \\ 0 & B(r,\phi') & D(r,\phi') & 0 & A(r,\phi') & -C(r,\phi') \\ 0 & -D(r,\phi') & -F(r,\phi') & 0 & -C(r,\phi') & E(r,\phi') \end{bmatrix} \end{split}$$

where

 ρ = density m = added m ε^{in} = Prestrain Appendix E

$$\begin{split} A(r,\phi') &= \frac{13/35 + 7/10\phi' + 1/3\phi'^2 + 6/5(r/L)^2}{(1+\phi')^2} \\ B(r,\phi') &= \frac{9/70 + 3/10\phi' + 1/6\phi'^2 - 6/5(r/L)^2}{(1+\phi')^2} \\ C(r,\phi') &= \frac{(11/210 + 11/120\phi'^2 + 1/24\phi'^2 + (1/10 - 1/2\phi')(r/L)^2)L}{(1+\phi')^2} \\ D(r,\phi') &= \frac{(13/420 + 3/40\phi' + 1/24\phi'^2 - (1/10 - 1/2\phi')(r/L)^2)L}{(1+\phi')^2} \\ E(r,\phi') &= \frac{(1/105 + 1/60\phi' + 1/120\phi'^2 + (2/15 + 1/6\phi' + 1/3\phi'^2)(r/L)^2)L^2}{(1+\phi')^2} \\ F(r,\phi') &= \frac{(1/140 + 1/60\phi' + 1/120\phi'^2 + (1/30 + 1/6\phi' - 1/6\phi'^2)(r/L)^2)L^2}{(1+\phi')^2} \\ r &= \sqrt{\frac{1}{A}} = \text{radius of gyration} \end{split}$$

AIE.2.3 Element types, shape functions, derivatives, stiffness matrices

$$\begin{bmatrix} \frac{EA}{L} \\ 0 & \frac{12EI\xi}{L^{3}(1+\bar{\tau}_{\eta})} \\ 0 & 0 & \frac{12EI\xi}{L^{3}(1+\bar{\tau}_{\eta})} \\ 0 & 0 & 0 & \frac{GJ}{L} \\ 0 & 0 & \frac{-6EI_{\eta}}{L^{2}(1+\bar{\tau}_{\xi})} & 0 & \frac{(4+\bar{\tau})EI_{\eta}}{L(1+\bar{\tau}_{\eta})} \\ 0 & \frac{6EI\xi}{L^{2}(1+\bar{\tau}_{\eta})} & 0 & 0 & 0 & \frac{(4+\bar{\tau})EI_{\xi}}{L(1+\bar{\tau}_{\eta})} \\ \frac{-EA}{L} & 0 & 0 & 0 & 0 & 0 & \frac{AE}{L} \\ 0 & \frac{12EI\xi}{L^{3}(1+\bar{\tau}_{\eta})} & 0 & 0 & 0 & \frac{-6EI_{\xi}}{L^{2}(1+\bar{\tau}_{\eta})} & 0 & \frac{12EI_{\xi}}{L^{3}(1+\bar{\tau}_{\eta})} \\ 0 & 0 & \frac{-6EI_{\eta}}{L^{3}(1+\bar{\tau}_{\xi})} & 0 & \frac{6EI_{\eta}}{L^{2}(1+\bar{\tau}_{\xi})} & 0 & 0 & 0 & \frac{12EI_{\eta}}{L^{3}(1+\bar{\tau}_{\eta})} \\ 0 & 0 & 0 & \frac{-GI_{J}}{L^{3}(1+\bar{\tau}_{\xi})} & 0 & 0 & 0 & 0 & \frac{GJ_{L}}{L} \\ 0 & 0 & \frac{-6EI_{\eta}}{L^{2}(1+\bar{\tau}_{\eta})} & 0 & \frac{(2-\bar{\tau}_{\eta})EI_{\eta}}{L(1+\bar{\tau}_{\xi})} & 0 & 0 & 0 & \frac{GEI_{\eta}}{L^{2}(1+\bar{\tau}_{\xi})} \\ 0 & 0 & \frac{6EI_{\eta}}{L^{2}(1+\bar{\tau}_{\eta})} & 0 & 0 & 0 & \frac{(2-\bar{\tau}_{\eta})EI_{\xi}}{L(1+\bar{\tau}_{\eta})} & 0 & 0 & 0 & \frac{(4+\bar{\tau}_{\eta})EI_{\xi}}{L(1+\bar{\tau}_{\eta})} \\ \end{bmatrix}$$

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$$\bar{\tau}_{\eta} = \frac{12EI_{\xi}}{GA_{s\eta}L^2} = 24(1+\nu)\frac{A}{A_{sn}}\left(\frac{T_{\xi}}{L}\right)^2 \bar{\tau}_{\xi} = \frac{12EI_{\eta}}{GA_{s\xi}L^2} = 24(1+\nu)\frac{A}{A_{s\xi}}\left(\frac{T_{\eta}}{L}\right)^2$$

 A_s = shear area T = torsional moment of inertia P = density ξ , η local axes are parallel to Z and Y axes

The element pressure load vector in element coordinates IS

$$\left\{F_1^{pe}\right\} = \left\lfloor P_1 \, P_2 \, P_3 P_4 \, P_5 \, P_6 \right\rfloor^{\mathrm{T}}$$

| Table AIE.2 | | | | | | |
|---|--|--|--|--|--|--|
| Value of stress stiffness coefficient (C_2) Previous iteration resulted in a tensile stress | Previous iteration resulted in a compressive stress | | | | | |
| 1.0 1.0 0.0 $\frac{AE}{F \times 10^6}$ | $ \begin{array}{r} 0.0 \\ \frac{AE}{F \times 10^6} \\ 1.0 \\ 1.0 \end{array} $ | | | | | |

 $F = \begin{cases} \text{for the first iteration} : AE\varepsilon^{\text{in}} \\ \text{for all subsequent iterations} : the axial force} \\ \text{in the element as computed in the previous} \\ \text{stress pass of the element (output quantity)} \\ \\ FORC \\ C_2 = \text{Value given in the table above} \end{cases}$

AIE.2.4 The matrix for the tension-only or compression-only spar

Table AIE.3 Chain rule

| $ \partial Z $ | $\begin{bmatrix} \frac{\partial u}{\partial X} \\ \frac{\partial u}{\partial Y} \\ \frac{\partial u}{\partial Z} \\ \frac{\partial v}{\partial Z} \\ \frac{\partial v}{\partial X} \\ \frac{\partial v}{\partial Z} \\ \frac{\partial w}{\partial Z} \\ \frac{\partial W}{\partial Z} \\ \frac{\partial W}{\partial Z} \end{bmatrix} = \frac{1}{\det}$ | $\overline{J} \begin{bmatrix} C_{11} \\ C_{21} \\ C_{31} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$ | $\begin{array}{c} C_{12} \\ C_{22} \\ C_{32} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $ | $\begin{array}{c} C_{13} \\ C_{23} \\ C_{33} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $ | $\begin{array}{c} 0 \\ 0 \\ C_{11} \\ C_{21} \\ C_{31} \\ 0 \\ 0 \\ 0 \end{array}$ | $\begin{array}{c} 0 \\ 0 \\ 0 \\ C_{12} \\ C_{22} \\ C_{32} \\ 0 \\ 0 \\ 0 \\ 0 \\ \end{array}$ | $\begin{array}{c} 0 \\ 0 \\ C_{13} \\ C_{23} \\ C_{33} \\ 0 \\ 0 \\ 0 \\ 0 \\ \end{array}$ | $\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ C_{11} \\ C_{21} \\ C_{31} \end{array}$ | $\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ C_{12} \\ C_{22} \\ C_{32} \end{array}$ | $\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ C_{13} \\ C_{23} \\ C_{33} \end{array}$ | | $\begin{bmatrix} \frac{\partial u}{\partial \xi} \\ \frac{\partial u}{\partial \eta} \\ \frac{\partial u}{\partial z} \\ \frac{\partial v}{\partial \xi} \\ \frac{\partial v}{\partial \eta} \\ \frac{\partial u}{\partial \xi} \\ \frac{\partial w}{\partial y} \\ \frac{\partial w}{\partial w} \\ \frac{\partial w}{\partial w} \end{bmatrix}$ |
|----------------|--|---|--|--|--|---|--|--|---|--|--|---|
|----------------|--|---|--|--|--|---|--|--|---|--|--|---|

where

$$C_{11} = \frac{\partial Y}{\partial \xi} \frac{\partial Y}{\partial \xi} - \frac{\partial Z}{\partial \eta} \frac{\partial Y}{\partial \xi} \quad C_{12} = \frac{\partial Z}{\partial \xi} \frac{\partial Y}{\partial \xi} - \frac{\partial Z}{\partial \xi} \frac{\partial Y}{\partial \xi}$$

$$C_{13} = \frac{\partial Y}{\partial \xi} \frac{\partial Z}{\partial \xi} - \frac{\partial Z}{\partial \xi} \frac{\partial Y}{\partial \xi} \quad C_{21} = \frac{\partial Z}{\partial \xi} \frac{\partial X}{\partial \xi} - \frac{\partial X}{\partial \xi} \frac{\partial Z}{\partial \xi}$$

$$C_{22} = \frac{\partial X}{\partial \xi} \frac{\partial Z}{\partial \xi} - \frac{\partial Z}{\partial \xi} \frac{\partial X}{\partial \xi} \quad C_{23} = \frac{\partial Z}{\partial \xi} \frac{\partial X}{\partial \eta} - \frac{\partial X}{\partial \xi} \frac{\partial Z}{\partial \eta}$$

$$C_{31} = \frac{\partial X}{\partial \eta} \frac{\partial Y}{\partial \xi} - \frac{\partial Y}{\partial \eta} \frac{\partial X}{\partial \xi} \quad C_{32} = \frac{\partial Y}{\partial \xi} \frac{\partial X}{\partial \xi} - \frac{\partial X}{\partial \xi} \frac{\partial Y}{\partial \xi}$$

$$C_{33} = \frac{\partial X}{\partial \xi} \frac{\partial Y}{\partial \eta} - \frac{\partial Y}{\partial \xi} \frac{\partial X}{\partial \eta}$$

det [J] = the determinant of the Jacobian matrix





Direction cosincs of the two axes are given by

$$l_{1} = \cos(\xi, x) \quad m_{1} = \cos(\xi, y) \quad n_{1} = \cos(\xi, z) l_{2} = \cos(\eta, x) \quad m_{2} = \cos(\xi, y) \quad n_{2} = \cos(\xi, z) l_{3} = \cos(\varsigma, x) \quad m_{3} = \cos(\varsigma, y) \quad n_{3} = \cos(\varsigma, z)$$

The following relationships can be written for local and global strain and sterss vectors:

$$\left\{ \varepsilon_{x}^{\prime}
ight\} = \left[T_{\varepsilon} \right] \left\{ \varepsilon_{x}
ight\} \ \left\{ \sigma_{x}
ight\} = \left[T_{\varepsilon} \right]^{T^{\prime \prime}} \left\{ \sigma_{x}^{\prime}
ight\}$$

and also

$$\left\{\sigma'_{x}\right\} = [T_{\sigma}]\left\{\sigma_{x}\right\} \quad \left\{\varepsilon_{x}\right\} = [T_{\sigma}]^{T''}\left\{\varepsilon'_{x}\right\}$$

$$\begin{bmatrix} T_{\varepsilon}'' \end{bmatrix} = \begin{bmatrix} l_{1}^{2} & m_{1}^{2} & n_{1}^{2} & l_{1}m_{1} & m_{1}n_{1} & l_{1}n_{1} \\ l_{2}^{2} & m_{2}^{2} & n_{2}^{2} & l_{2}m_{2} & m_{2}n_{2} & l_{2}n_{2} \\ l_{3}^{2} & m_{3}^{2} & n_{3}^{2} & l_{3}m_{3} & m_{3}n_{3} & l_{3}m_{3} \\ 2l_{1}l_{2} & 2m_{1}m_{2} & 2n_{1}n_{2} & l_{1}m_{2} + l_{2}m_{1} & m_{1}n_{2} + m_{2}n_{1} & l_{1}n_{2} + l_{2}n_{1} \\ 2l_{2}l_{3} & 2m_{2}m_{3} & 2n_{2}n_{3} & l_{2}m_{3} + l_{3}m_{2} & m_{2}n_{3} + n_{2}m_{3} & l_{2}n_{3} + l_{3}n_{2} \\ 2l_{1}l_{3} & 2m_{3}m_{3} & 2m_{1}n_{3} & l_{1}m_{3} + m_{1}l_{3} & m_{1}n_{3} + m_{3}n_{1} & l_{1}n_{3} + n_{1}l_{3} \end{bmatrix}$$

$$\begin{bmatrix} T_{\varepsilon}'' \end{bmatrix} = \begin{bmatrix} l_{1}^{2} & m_{1}^{2} & n_{1}^{2} & 2l_{1}m_{1} & 2m_{1}n_{1} & 2l_{1}n_{1} \\ l_{2}^{2} & m_{2}^{2} & n_{2}^{2} & 2l_{2}m_{2} & 2m_{2}n_{2} & 2l_{2}n_{2} \\ l_{3}^{2} & m_{3}^{2} & n_{3}^{2} & 2l_{3}m_{3} & 2m_{3}n_{3} & 2l_{3}m_{3} \\ l_{1}l_{2} & m_{1}m_{2} & n_{1}n_{2} & l_{1}m_{2} + l_{2}m_{1} & m_{1}n_{2} + n_{1}m_{2} & l_{1}n_{2} + l_{2}n_{1} \\ l_{2}l_{3} & m_{2}m_{3} & n_{2}n_{3} & l_{2}m_{3} + l_{3}m_{2} & m_{2}n_{3} + n_{2}m_{3} & l_{2}n_{3} + l_{3}n_{2} \\ l_{1}l_{3} & m_{1}m_{3} & n_{1}n_{3} & l_{1}m_{3} + l_{3}m_{1} & m_{1}n_{3} + m_{3}n_{1} & l_{1}n_{3} + n_{1}l_{3} \end{bmatrix}$$

E.3 Criteria for Convergence and Acceleration

Convergence Criteria

To ensure convergence to the correct solution by finer sub-division of the mesh, *the* assumed displacement function must satisfy the convergence criteria given below:

- (a) Displacements must be continuous over element boundaries.
- (b) Rigid body movements should be possible without straining.
- (c) A state of constant strain should be reproducible.

Euclidean norm $\psi_1/R_1 \leq C$. The term ψ_1 represents the unbalanced forces and the norm of the residuals. With the aid of the iterative scheme described above, the unbalanced forces due to the initial stresses θ_1 become negligibly small. As a measure of their magnitude, the norm of the vector $||\psi_1||$ is used. The Euclidean norm and the absolute value of the largest component of the vector are written as

$$\|\psi\| = \left(|\psi_1|^2 + \dots + |\psi_n|^2\right)^{1/2}$$

$$\|R_i\| = \left(\left|\{R_i\}^{T''}\{R_i\}\right|\right)^{1/2}$$
(AIE.1)

where T'' = Transpose

The convergence criterion adopted is

$$\|\psi\| = \max_{i} |\psi_{i}| < C = 0.001$$
 (AIE.2)

E.4 Uniform Acceleration

Various procedures are available for accelerating the convergence of the modified Newton–Raphson iterations. Figure AIE.1 shows the technique of computing individual acceleration factors, δ_1 and δ_2 are known. Then, assuming a constant slope of the response curve, and from similar triangles, the value of δ_3 is computed:

$$\frac{\delta_1}{\delta_2} = \frac{\delta_2}{\delta_3} \ \delta_3 = \delta_2 \frac{\delta_2}{\delta_1}$$
(AIE.3)

When δ_3 is added to δ_2 , then the accelerated displacement δ'_2 is expressed as

$$\delta_2' = \delta_2 + \delta_3 = \delta_2 \left(1 + \frac{\delta_2}{\delta_1} \right) = \alpha \delta_2$$
 (AIE.4)

where the acceleration factor α is



Fig. AIE.3 Position vectors and motion of a deforming body

 $A\Psi_{i-1}$

 ΔU_{i-1}

<u>ΑΔ</u>U_{i –1} _____δ



(Ψ_{i-1})

K₀





Fig. AIE.4(d) Graphical representation



Generally the range of α is between 1 and 2. The value of $\alpha = 1$ for zero acceleration, and the value of a reaches the maximum value of 2 when the slope of the δ —*R* curve approaches zero.

The acceleration factor α is computed individually for every degree of freedom of the system. The displacement vector obtained from the linear stiffness matrix $[k_0]$ is then multiplied by the $[\alpha]$ matrix having the above constants on its diagonals. The remaining components of $[\alpha]$ are zero. The accelerated displacement vector is then expressed as follows:

$$\left\{\Delta u_i'\right\} = [a_{i-1}]\{+\Delta u_j\} \tag{AIE.6}$$

From these accelerated displacements $\{\Delta u'_i\}$ the initial stresses $\{\sigma_0\}$ are found and they are equilibrated with the forces $\{\psi_1\}$ They are then used for the next solution

$$\left\{\Delta \bar{u}_j\right\} = [K_0]^{-1} \{\psi_i\} \tag{AIE.7}$$

which results in a new set of acceleration factors. Now an estimate for the displacement increment is made in order to find the incremental stresses and total stresses.

The residual forces needed to re-establish equilibrium can now easily be evaluated

$$\{\hat{\psi}_i\} = \int \left[B\right]^T \{\sigma_{0_\tau}\} dV - \{R_i\}$$
(AIE.8)

where $\{R_i\}$ represents the total external load; dV is the volume.

A new displacement now results from

$$\{\Delta u_{i+1}\} = -[K_0]^{-1}\{\hat{\psi}_i\}$$
(AIE.9)

In order to carry out these iterative steps, numerical integration is required. First of all the evaluation of $\{\hat{\psi}_1\}$ from the initial stresses is required, and this requires integration over the elastic—plastic region only. The value of $\{\hat{\psi}_1\}$ is computed by carrying out the integration over the entire domain of the analysis. Since these kinds of accelerated steps unbalance the equilibrium, therefore it has to be re-established by finding the residual forces $\{\hat{\psi}_1\}$. Since the state of stress produced by the accelerated displacements is not in balance with the residual forces of the previous iteration, the new residual forces $\{\hat{\psi}_1\}$ of Eq. (AIE.9) must balance $\{\sigma_T\}$ and $\{R_1\}$. Here the acceleration scheme is needed to preserve equilibrium, which will eventually make the equivalent forces over the whole region unnecessary. This is achieved by applying a uniform acceleration, i.e. the same acceleration factor \bar{A} to all displacements, found by averaging the individual factors α_i

$$\bar{A} = \frac{1}{n} \sum_{i=1}^{n} \alpha_i \tag{AIE.10}$$

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The force–displacement equation is then written by multiplying both sides with the scalar quantity \overline{A} without disturbing the equilibrium.

$$\bar{A}\{\Delta u_i\} = [K_0]^{-1}\bar{A}\{\psi_i\}$$
(AIE.11)

Now to evaluate $\{\psi_{i+1}\}\$, the previous value of $\{\psi_1\}\$ must be multiplied by \overline{A} , and the previously accelerated forces from the initial stresses $\{\sigma_o\}\$ must be included such that

$$\{\psi_{i+1}\} = \int V[B]^{T''}\{\sigma_0\} dV - (A-1)\{\psi_{i-1}\}$$
(AIE.12)

Superelement and Substructuring

In general terms, such formulations are described by the following:

$$\left[\frac{K}{K_{R}^{T''}} | \frac{K_{R}}{K_{RR}}\right] \left\{\frac{U}{U_{R}}\right\} = \left\{\frac{F}{F_{R}}\right\}$$
(AIE.13)

The subscript *R* represents reaction forces. The top half of Eq. (AIE.13) is used to solve for $\{U\}$:

$$\{U\} = -[K]^{-1}[K_R]\{U_R\} + [K]^{-1}\{F\}$$
(AIE.14)

The reaction forces $\{F_R\}$ are computed from the bottom half of the equation as

$$\{F_R\} = [K_R]^{T''}\{U\} + [K_{RR}]\{U_R\}$$
(AIE.15)

Equation (AIE.14) must be in equilibrium with Eq. (AIE.15).

For large structures with complicated features, a substructure (super element) may be adopted on the lines suggested in Eq. (AIE.13). This super element may then be used as a reduced element from the collection of elements. If subscripts r and r' represent the retained and removed degrees of freedom of the equations partitioned into two groups, then the expressions in Eq. (AIE.13) can be written as

$$\left[\frac{K_{rr}}{K_{r'r}} | \frac{K_{rr'}}{K_{r'r'}}\right] \left\{\frac{U_r}{U_{r'}}\right\} = \left\{\frac{F_r}{F_{r'}}\right\}$$
(AIE.16)

Equation (AIE.16) when expanded assumes the following form:

$$\{F_r\} = [K_{rr}]\{U_r\} + [K_{rr'}]\{U_{r'}\}$$
(AIE.17)

$$\{F_{r'}\} = [K_{r'r}]\{U_r\} + [K_{r'r}]\{U_{r'}\}$$
(AIE.18)

When a dynamic analysis is carried out, the subscript r (retained) represents the dynamic degrees of freedom.

When Eq. (AIE.18) is solved, the value of $U_{r'}$ is then written, similarly to Eq. (AIE.14).

$$\{U_{r'}\} = [K_{r'r'}]^{-1}\{F_{r'}\} - [K_{r'r'}]^{-1}[K_{r'r}]\{U_r\}$$
(AIE.19)

Substituting $\{U_{r'}\}$ into Eq. (AIE.17) gives

$$\left[\left[[K_{rr}] - [K_{rr'}][K_{rr'}]^{-1}[K_{rr'}]\right]\right]\{U_r\} = \left[\{F_r\} - [K_{rr'}][K_{rr'}]^{-1}\{F_{r'}\}\right]$$
(AIE.20)

or

$$[\bar{K}]\{\bar{U}\} = \{\bar{F}\} \tag{AIE.21}$$

where

$$[\bar{K}] = [K_{rr}] - [K_{rr'}][K_{r'r'}]^{-1}[K_{r'r}]$$
(AIE.22)

$$\{\bar{F}\} = \{F_r\} - [K_{rr'}][K_{r'r'}]^{-1}\{F_{r'}\}$$
(AIE.23)

$$\{\bar{U}\} = \{U_r\} \tag{AIE.24}$$

and $[\bar{K}]$ and $\{\bar{F}\}$ are generally known as the substructure stiffness matrix and load vector, respectively.

In the above equations, the load vector for the substructure is taken as a total load vector. The same derivation may be applied to any number of independent load vectors. For example, one may wish to apply thermal, pressure, gravity and other loading conditions in varying proportions. Expanding the right-hand sides of Eqs. (AIE.15) and (AIE.16) gives:

$$\{F_r\} = \sum_{i=1}^{n} \{F_{ri}\}$$
(AIE.25)

$$\{F_{r'}\} = \sum_{i=1}^{n} \{F_{r'i}\}$$
(AIE.26)

where

 $[G_i]$ = matrix of shape function derivatives

 $[\tau_i]$ = matrix for the current Cauchy stresses i.e. true stresses σ_i

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$$\left[F_{i}^{nr}\right] = \int \left[B_{i}\right]^{T''} \{\sigma_{i}\} d(\text{Vol})$$
(AIE.27)

The increment of large strain $[\Delta \varepsilon_n]$ is then written as

$$[\Delta \varepsilon_{n}] = \left[R_{1/2} \right]^{1T''} [\Delta \overline{\varepsilon}_{n}] \left[R_{1/2} \right]$$
(AIE.28)

where

 $[R_{1/2}]$ = rotational matrix from the polar decomposition of the deformation gradient at the midpoint configuration

$$[F_{1/2}] = [R_{1/2}][U_{1/2}]$$
 (AIE.29)

where

$$[F_{1/2}] = [I] + \frac{\partial \{U_{1/2}\}}{\partial \{X\}}$$
 (AIE.30)

Large deformation and large strains are obtained where these formulations are linked to the main analyses, static dynamic and blast type of loading are encountered.

Introduction Interface or Gap Elements in Current Computer Programs

The potential of interface elements in elevators and escalators is vital. They play a very important role in bringing about cPose relations between various mechanical components in static and dynamic conditions. Examples are cited in lifts/elevators escalators and travelators where components rolling over each others or some static and others moving over the static ones. Various contact or gap elements have been explained in various finite-element packages : Some of them are cited below:

- (a) Haliquist et al. Method
- (b) DELFT Interface Traction Type Element
- (c) ANSYS contact Elements
- (d) ABACUS Gap/contact Elements
- (e) LS-DYNA Gap/contact Elements

With program ISOPAR Haliquist et al. method has been adopted as this method clearly establishes the contact elements which suite the scope of the book. The method is described below:

where n = the number of independent load vectors.

Substituting into Eq. (AIE.12)

$$\{\bar{F}\} = \sum_{i=1}^{n} \{F_{rr'}\} - [K_{rr'}][K_{r'r'}]^{-1} \sum_{i=1}^{n} \{F_{r'i}\}$$
(AIE.31)
Large Strain

When the strains in a material exceed more than a few percent, the changing geometry due to this deformation can no longer be neglected. Analyses which include this effect are called large strain, or finite strain, analyses. A large strain analysis is performed in a static and dynamic transient analysis.

The theory of large strain computations can be addressed by defining a few basic physical quantities (motion and deformation) and the corresponding mathematical relationship. The applied loads acting on a body make it move from one position to another. This motion can be defined by studying a position vector in the 'deformed' and 'undeformed' configurations. Say the position vectors in the 'deformed' and 'undeformed' state are represented by $\{x\}$ and $\{X\}$, respectively, then the motion (displacement) vector $\{u\}$ is computed by

$$\{u\} = \{x\} - \{X\}$$
(AIE.32)

The deformation gradient $[F_d]$ is defined as

$$[F_d] = \frac{\partial \{x\}}{\partial \{X\}} + [\mathbf{I}] = [R][u]$$
(AIE.33)

where [I] = identity matrix.

The volume change at a point

$$\frac{dV}{dV_0} = \det[F] \tag{AIE.34}$$

Where

 V_0 = Original volume

V =current volume

[u] = right stretch shape change matrix

Largestrain ε is written as

$$\{\epsilon\} = \ln[u] = \sum \ln(\lambda_i) \{e_i\} \{e_i\}^{T''}$$
(AIE.35)

where

 λ_i = eigenvalues of [u] e_i = eigenvalues of [u] **R** = rotation matrix ([**R**]^{T''}[**R**] = [**I**])

Element formulation using Lagrangian formulation technique

$$[K_j]\Delta u_j = [F^a] - [F_i^{nr}]$$
(AIE.36)

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where

$$[\mathbf{K}_{i}] = \text{tangent matrix} = [\mathbf{K}_{i}] + [S_{i}]$$

$$[\mathbf{K}_{i}] = \text{usual stiffness matrix}$$

$$= \int [B_{i}]^{T''} [D_{i}] [B_{i}] \mathrm{d(vol)}$$

(AIE.37)

$$[S_i] = \text{stress stiffness contribution or geometric stiffness} = \int [G_i]^T [\tau_i] [G_i] d(\text{vol})$$
(AIE.38)

Haliquist et al. method

Haliquist *et al.* developed a useful concept of master and slave nodes sliding on each other. As shown in Fig. AIE.1 slave nodes are constrained to slide on master segments after impact occurs and must remain on a master segment until a tensile interface force develops. The zone in which a slave segment exists is called a slave zone. A separation between the slave and the master line is known. as void. The following basic principles apply at the interface:

- (a) update the location of each slave node by finding its closest master node or the one on which it lies,
- (b) for each master segment, find out the first slave zone that overlaps,
- (c) show the existence of the tensile interface force.

Constraints are imposed on global equations by a transformation of the nodal displacement components of the slave nodes along the contact interface. Such a transformation of the displacement components of the slave nodes will eliminate their normal degrees of freedom and distribute their normal force components to the nearby master nodes. This is done using explicit time integration, as described in the finite-element solution procedures. Thereafter impact and release conditions are imposed. The slave and master nodes are shown in Fig. AIE.2. Hallquist et al. gave a useful demonstration of the identification of the contact point which is the point on the master segment to the slave node n_s and which finally becomes non-trivial during the execution of the analyses. When the master segment I is given the parametric representation and t is the position vector drawn to the slave node n_s , the contact point coordinate must satisfy the following equations:

$$\frac{\partial \hat{r}}{\partial \xi} (\xi_c, \eta_c) \times [\hat{l} - \hat{r}(\xi_c, \eta_c)] = 0$$

$$\frac{\partial \hat{r}}{\partial \eta} (\xi_c, \eta_c) \times [\hat{l} - \hat{r}(\xi_c, \eta_c)] = 0$$
(AIE.39)



 $k_{\rm n}$ — Interface normal stiffness m D, material stiffness matrix Values varied as 10³ to 10⁶ N/mm³

Fig. AIE.5 Hallquist contact method (modified by Bangash)

where (ξ_c, η_c) are the co-ordinates on the master surface segment S_i. Where penetration through the master segment S_i occurs, the slave node n_s (containing its contact point) can be identified using the interface vector f_s

$$f_s = -lk_i n_i \qquad \text{if } l < 0 \qquad (\text{AIE.40})$$

to the degree of freedom corresponding to n_s , and

$$f_m^i = N_i(\xi_c \eta_c) f_s \qquad \text{if } l < 0 \qquad (\text{AIE.41})$$

where

$$l = \hat{n}_{i}[\hat{t} - \hat{r}(\xi_{c}, \eta_{c})] < 0$$
 (AIE.42)

A unit normal

$$\hat{n}_i = \hat{n}_i(\xi_c, \eta_c); \ \hat{t}_i = \hat{n}_i \sum_{j=1}^n N_j (F_1)^j(t)$$
 (AIE.43)

$$k_i = f_{si} K_i A_i^2 / V_i \tag{AIE.44}$$

where

 $(F_I)^j(t) = \text{impact at the } j\text{th node}$ K = stiffness factor K_i, V_i, A_i = bulk modulus, volume and face area, respectively f_{si} = scale factor normally defaulted to 0.10 $N_i = \frac{1}{4}(1 + \xi\xi_i)(1 + \eta\eta_i)$ for a 4-node linear surface

Bangash extended this useful analysis for other shape functions, such as N_i for 8-noded and 12-noded elements. On the basis of this theory and owing to the non-availability of the original computer source, a new sub-program CON-TACT was writ-ten in association with the program ISOPAR. The subprogram CONTACT is in three dimensions

Gap element



$$\left\{ \vec{\mathbf{F}_{N}} \right\} = \left[\mathbf{K}_{\gamma\gamma} \right]_{i} \left\{ U_{\gamma} \right\}_{i} = \left[\Sigma K \right] \left\{ \Sigma \Delta_{i}, \Delta_{j} \dots \right\} = \left\{ \hat{\vec{\mathbf{F}}}_{i,j}, \dots \right\} + \left\{ \pm \mu \hat{\vec{\mathbf{F}}}_{n} \dots \pm k \Delta_{i} \right\}$$

$$\Delta_{\text{sl}} = \text{distance of sliding}$$
 (AIE.45)

{

$$= (\Delta_j - \Delta_i) - \frac{\mu |\vec{F}_N|}{[K_{\gamma\gamma}]}$$

$$\mu = \text{friction}$$
(AIE.46)

$$\hat{\vec{F}}_{SN} \leq \mu \{\hat{\vec{F}}_N\} \text{ no sliding}$$

$$\geq \mu\{\vec{F}_{N}\} \text{ sliding}$$

= 0 contact broken (AIE.47)
$$\theta = \cos^{-1}\frac{X}{r} \text{ or } \sin^{-1}\frac{Y}{r}$$

Appendix F Simplified Dynamic Analysis of Towers, Chimneys And Frames As Auxiliary Structures

AIF.1. Fundamental Frequency of Tower Structures

- AIF.2. For Cooling Tower Shell Shapes Analysis
- AIF.3. A Steel Frame Supporting a Rotating Machines

AIF.1 The Determination of the Fundamental Frequency of a Tower Structure

A schematic diagram of the tower is shown in the Figure AIF.1. It consists of a circular tapering, hollow concrete tower L_1 in height, surmounted by a steel mast L_2 high. 'Tower' will be used to refer to the concrete structure and the mass of the steel must lumped at its end.

The tower tapers according to a linear relationship between diameter *D*, and *x*, measured from the ground:

$$D = D_o - D_s x \tag{AIF.1}$$

And the moment of inertia, I, varies according to a third-order polynomial in *x*:

$$I(x) = I_o - I_1 x + I_2 x^2 - I_3 x^3$$
(AIF.2)

The mass per unit length, W(x), over the tower height varies according to a linear relationship:

$$W(x) = Wf - Zx \tag{AIF.3}$$



Table AIF.1 Characteristics of the tower

| Length (m) | Mass (weight) and mass (wt) coeffs kg (KN) |
|------------------------------|---|
| $L_1 = 275.0$ | $W_2 = 71121.0 (697.7)$ |
| $L_2 = 60.7$ | $W_3 = 46206.0 (453.3)$ |
| $L_3 = 35.1$ | $W_4 = 24915.0 \ (244.4)$ |
| $L_4 = 25.6$ | $W_f = 97986.9 \text{ m}^{-1} (961.3) \text{ m}^{-1}$ |
| | $Z = 299.237 \mathrm{m}^{-2} (2.9) \mathrm{m}^{-2}$ |
| Diameters and coeffin (m) | Second moments of area and coeffs (m ⁴) |
| $D_3 = 3.60$ | $I_{00} = 3044.86$ |
| $D_4 = 2.27$ | $I_1 = 38.7142 \text{ m}^{-1}$ |
| $D_{00} = 24.40$ | $I_2 = 0.172539 \text{ m}^{-2}$ |
| $D_s = 0.067 \text{ m}^{-1}$ | $I_s = 0.00026 \text{ m}^{-3}$ |



Fig. AIF.1(a) Base Tower parameters-I

The mass per unit length along the tower can be divided into a uniformly distributed load W'_1 and a triangular distribution of W'_2 as shown above.

Lengths of the tower are lumped into masses

$$MA = \int_{x_1}^{x_2} (WF - Zx) dx$$

= $(x_2 - x_1) \left[WF - \frac{Z}{2} (x_2 + x_1) \right]$ (AIF.4)

Where x_1 and x_2 are the cords of the start and end of the length under consideration.

The bending moments due to self-weight can be shown to be

$$M_0(x) = \frac{W_1}{2}(L-x)^2 + \frac{Z}{6}(L-x)^3 + MM(L-x)$$
 (AIF.5)

The second moment of area of the tower varies according to

$$I_0(x) = I_{00} - I_1 x + I_2 x^2 - I_3 x^3$$
 (AIF.6)

The bending moment due to a unit load at the lumped mass distance *Y* from the free end is

$$M_1(x) = (L - x - Y)$$
 (AIF.7)

In all cases x is measured from the support.



The static deflection of the contilever (tower) are computed by a combination of Simpson's Rule and the area–moment–inertia procedure.

The deflection DEL under any lumped mass

$$DEL = \frac{1}{E} \int \frac{M_0(x) \cdot M_1(x)}{I_0(x)} dx$$

$$= \frac{H}{6E} [M_0(1)M_1(1) \div I_0(1) + 4M_0(2)M_1(2) \div I_0(2) + M_0(3)M_1(3) \div I_0(3)]$$
(AIF.8)

E being the modulus of elasticity of concrete.

The fundamental frequency of the tower is computed by the Rayleigh method. Hence the dynamic deflection is assumed, not to differ appreciably from the static deflection 'DEL'

Max. strain energy of Oscillating masses = Potential energy

$$=\sum \frac{MA \times DEL}{2}$$
(AIF.9)

max. KE of masses
$$=\frac{\omega^2}{2g}\sum MA \times DEL^2$$

Equating SE and KE one gets

$$\sum MA \times DEL = \frac{\omega^2}{2g} \sum MA \times DEL^2$$

$$\omega^2 = g \frac{MA \times DEL}{MA \times DEL^2} = g \times \frac{NUM}{DEN}$$
(AIF.10)

$$\therefore \omega = \left[g \times \frac{\text{NUM}}{\text{DEN}} \right]^2 \tag{AIF.11}$$

Frequency
$$f = \frac{\omega}{2\pi}$$
 (AIF.12)

g =acceleration due to gravity.

A Typical Case Study



The Flow Chart



Output

The fundamental circular frequency of the structure (Tower 1) is $1.26828 \simeq 1.3$ rad per sec.

Comments and Conclusion

The Rayleigh method for natural frequencies was chosen for the computation of the fundamental frequency of a tower structure because of its considerable accuracy and ease. However, this method can be modified for the computation of a few of the lower modes frequencies.

Other methods have the advantage of computing the characteristic shapes of the various modes of vibration accurately, but are exceedingly cumbersome and require high computational times.

Since, one is only interested in the fundamental frequency, there is no justification for the adaptation of other methods.

The fundamental mode of vibration is that in which the tower and mast are in phase. In this exercise the mass of the mast, being very small compared with the mass of the tower, was lumped at the free end of the tower.

The value at $\omega = 1.3$ rad per sec is the same as that obtained by the use of Lagrange Equation (Ref: Vibration reduction in Tower Structures, by K.C. Johns & C.L. Kink).

Therefore, it can be concluded that the Rayleigh method is a very accurate method for the determination of the fundamental frequency. Other methods stated in the text can also be applied. They can be expensive and yet very elaborate result wise.

AIF.2 Cooling Tower and Cable net Tower shell Shapes for Nuclear Power Stations Hyperboloid of Revolution

When the rotating curve is a *hyperbola*, the generated surface is known as a *hyperboloid of revolution*. A single-sheet *hyperboloid of revolution* is so termed as it is a single-piece surface.

Two types of hyperboloid of revolution - i.e. a natural, draught cooling tower cable net tower shells - will be discussed below.

Natural draught cooling tower

For large power station blocks that are completely dependent on cooling tower natural draught coolers are the only types being built at present. The capital exjditure involved is relatively low and they require neither energy nor maintenance mechanical equipment. They have a correspondingly high level of reliability. If the ground conditions are adequate, an annular foundation is usually laid individual foundations, e.g. pile foundations, are required, the number of pain columns should be kept to a minimum. In this case, it is also advisable to prest the lower shell periphery. The column framework provides the free cross-sec necessary for air intake in the exterior wall and transmits the reaction forces of the cooler shell into the foundation. The construction and installation of the fraction work require great care in order to avoid unnecessary bending stresses in the section. The column cross-section is rectangular or circular: the shape may be influence aerodynamic requirements.

For the large cooling towers built in the last few decades, the thin reinforced crete shell, reinforced in two axes on both surfaces, has proved eminently suitatable. For structural, thermodynamic and flow optimization reasons rotationally hyperbolic shapes are desirable, and occasionally also cylinders. These shapes are at same time aesthetically pleasing because they make the gigantic dimensions of the structures seem tolerable.

The cooler shell can be very thin. The minimum wall thickness in the cer and upper portions in almost all towers is 14 cm; in other words, in relation to diameter it is thinner than an eggshell. In the lower portion, the shell becomes thickness until at the point of transition to the bottom edge element of the shell it is at 60–80 cm thick.

At the top of the shell, there is a study ring (top edge element) which counter the tendency of the shell to ovalize under high wind loads, and thus also yhe risk distortions without strain in the shell. This ring can also serve as a surrounding gas if aviation obstruction lighting is required on the cooling tower for safety reason this case, ladders or staircases must also be provided.

Cable Net Cooling Towers

They have considerable advantages with respect to safety during construction in service as compared to a concrete tower. There is almost no limit to its size is most favourable in the case of bad soil conditions and earthquakes. Shapes be obtained with different materials, such as fabrics – which have been discussed. 3', of the inclined straight line 3–3', along two circular paths with uniform angular speed (Fig. AIF 2.1(a)), such that the generating line 3–3', when produced, never cuts the line ($O_2 O_1$) passing through the centres of the circular paths.

Consider Figure AIF 2.1(b) in which the planes P_1 and P_2 may be parallel, but have smooth closed boundary curves.

In Figure AIF 2.1(b) a_1a_2 , b_1b_2 , etc., are straight lines, and the envelope due movement of these straight lines can be seen. Now,

1. If P_1 and P_2 are circular discs and parallel, and if $O_1a_1a_2O_2OO_1$ is a twisted (Hypar, Type II), i.e. the points a' on a_1a_2 and O on O_1O_2 , never coincide, the

generated surface as a *hyperboloid of revolution* due to the revolution line a_1a_2 about O_1O_2 .

- 2. If P_1 and P_2 are parallel circular discs, and if $O_1A_1A_2O_2O_1$ is a flat plan A_1A_2 forming a hyperbolic arc, we get a *hyperbolioid of revolution*.
- 3. If the angles $A_1O_1a_1$ and $A_2O_2A_2$ lie in the parallel planes P_1 and P_2 , arc parallel and are equal in magnitude, i.e. $\theta_1 = \theta_1$, then $O_1a_1a_2O_2O_1$ become plane consisting of two triangles O_1a_1O and O_2a_2O meeting at O on the O_1O_2 . We now have a pair of conical surfaces meeting at a common verte: boundary curve A_1A_2 is transferred into a broken line A_1O-OA_2 .

Membrane or cable net skin replaces the reinforced concrete shell of conven towers. A detailed analysis can be studied under fabric or net structures in thickness.

AIF.3 Hyperboloid of Revolution of One Sheet

The hyperboloid of revolution of one sheet has a very graceful appearance and profitably exploited for structural purposes such as a structure for the cooling towards great advantage emerges from the facts that the surface is generated by two factors of intersecting lines and the formwork can be achieved by straight boards with only slightly over their lengths. It is also interesting to note that the interset of grid straight lines form rhombuses of intersection. The shell surface can be built of precast rhombic elements, which can be repeated along the con circumference at a fixed height. Considerable utilization of this surface is being in the construction of cooling towers.

The surface is the locus of the equation

$$\frac{x^2}{C^2} + \frac{y^2}{A^2} - \frac{z^2}{B^2} = 1$$
 (AIF.13)

in three-dimensional Cartesian coordinates. It is quadratic because it is the of a second-degree equation and is doubly ruled; each point lies on more that straight line of the surface.

The particular case of hyperboloid of revolution with C = A in Eq. (AIF.13) discussed here for the surface and is defined by:

$$\frac{(x^2 + y^2)}{A^2} - \frac{z^2}{B^2} = 1$$
 (AIF.14)

In Figure AIF.2.1(a) all sections (in planes) perpendicular to the axis of revolution of the z axis) are circles. The surface is also the locus described by a hyperbola revolation around its conjugate axis. Furthermore, the surface is also the locus described straight generatrix revolving around a non-parallel axis (Fig. AIF.2.1(b)). The project of this line on a parallel coaxial plane is one of the asmyptotes of the hyperbolic sections contained on the plane. Consider in Figure AIF.2 an intersection by vertical plane y = A which being introduced in Eq. (AIF.14) gives:

$$\frac{x^2}{A^2} = \frac{z^2}{B^2}$$
 (AIF.15)

Therefore, the curve of intersection consists of a pair of straight lines have equations:

$$x = \pm \frac{A}{B}z \tag{AIF.16}$$

and slope, $\tan D = B/A$.

Since the hyperboloid is a surface of revolution, the tangent plane to any point of the waist circle will give a similar pair of straight lines on the hyperboloid so that there exist two families of straight lines each of which covers the completely.

Referring to Figures AIF.3 and the following equations may be establis

$$x = A(\sec T) \cos \theta \tag{AIF.17}$$

$$y = A(\sec T) \sin \theta$$
 (AIF.18)

$$z = B(\tan T) \tag{AIF.19}$$

and

$$R_1 = -\frac{D^2 3}{AB} \tag{AIF.20}$$

$$R_2 = \frac{AD}{B} \tag{AIF.21}$$

$$\sin\phi = \frac{B(\sec T)}{D}$$
 (AIF.22)

$$\frac{\mathrm{d}\phi}{\mathrm{d}T} = \frac{AB(\sec T)}{D^2 2} \tag{AIF.23}$$

where

$$D = (A^{2}(\tan T)^{2} + B^{2}(\sec T))^{2}0.5$$
 (AIF.24)

Considering the unit weight of the dead load

$$x = 0, y = \sin \phi$$
 and $z = -\cos \phi$

Substituting the auxiliary variables as:

$$G = \frac{A(\sec T)^2}{D} N_{\phi}$$
 (AIF.25)

Appendix F

and

$$H = S(\sec T)^2 \tag{AIF.26}$$

(where $S = N_{\theta\phi} = N_{\phi\theta}$).

The self-weight stresses are given by:

$$\frac{\partial G}{\partial T} = -\frac{A}{B} \frac{\sqrt{B^2 + A^2 \sin^2 T}}{\cos^3 T}$$
(AIF.27)

$$H = 0 \tag{AIF.28}$$

$$N_{\theta} = \frac{A^2}{D^2} N_{\phi} - \frac{A^2}{B} \tan(T)$$
 (AIF.29)

Boundary conditions

The planes of the top and bottom in Figure 6.48 are to be denoted by $T = T_1$ and $T = T_2$. Since the top is a free edge the stresses vanish there and therefore:

$$G = 0$$
, i.e. $N_{\phi} = 0$ and $H = 0$, i.e. $N_{\theta\phi} = 0$

for all values of 0 on $T = T_1$. (These conditions are sufficient for integration.)

By numerical integration with the boundary conditions the meridian force N_{ϕ} and hoop force N_{θ} can be obtained at all sections of the shell, as illustrated in the results of the computer program for NIZAM–4 cooling tower. Figure AIF.2 and its calculations indicate briefly the generalized stresses due to wind pressure at different heights when the cooling tower shapes are asymmetrical. Table AIF.1 gives loading systems and stresses per unit circumference of the tower shell surface.



Fig. AIF.2 Asymmetrical membrane state of stress



Fig. AIF.2b Generalized forms of rotational surface

Shell of revolution (refering to Fig. AIF.2)

$$N_{\phi} = \frac{P_{W}a \tan A}{6\rho^{2} \sin \phi} \left[\frac{\tan^{2} A - 2}{3 \tan^{2} A} (\rho^{3} - \rho_{0}^{3}) + \rho_{0} - \rho - \eta_{0}\rho_{0}(\eta - \eta_{0}) + \eta \ln \frac{\eta + \rho}{\eta_{0} + \rho_{0}} \right] \cos \theta$$
(AIF.30)



Fig. AIF 2.3 Cooling towers of equal radii

$$N_{\phi\theta} = N_{\theta\phi} = \frac{P_{Wa}}{2} \frac{\tan A}{\rho^{3}} [\eta_{0}\rho_{0} - \eta\rho - \eta\rho^{2}(\rho - \rho_{0}) - \frac{\tan^{2} A - 2}{3\tan^{2} A} \eta(\rho^{3} - \rho_{0}^{3}) - \ln\frac{\eta + \rho}{\eta_{0} + \rho_{0}}] \sin \theta \quad \text{(AIF.31)}$$

$$N_{\theta} = -N_{\phi} \frac{r_2}{r_1} - P_w r_2 \cos\theta \qquad (AIF.32)$$

where $\rho = \frac{r_0}{a}, \eta = \frac{z}{b} \ \rho_0, \eta_0$ value at upper edge $(\phi = \phi_0)$

Steel Frame Supporting a Rotating Machinery

Problem Example

A frame supporting a rotating machinery in a nuclear laboratory exerts a typical horizontal force F(t) at the girder level as shown in Fig. AIF.3. In a normal practice the value of F(t) is $F(t) = 200 \sin (5.3)t$ (*KN*) evaluation dynamic shear and bending moment an essentially demanded.

Data

 $L = 15 m, E = 200 \text{ KN/m}^2, \text{ I} = 0.02 \text{m}^4$ $\xi = \text{damping} = 0.05$ The girder is rigid

| nd shell forces | $\overline{\xi} = \frac{\overline{\xi} - \overline{\xi}_0}{\sqrt{1 - \beta^2 \overline{\xi}_0^2}}$ | $r\phi_0 = c\sqrt{1+\beta^2\xi_0^2}$ | $\chi_0 = {}^4 \sqrt{3(1-\mu^2)} \frac{r_{\phi 0}^2}{r^2}$ | Deformation | $egin{aligned} u' &= rac{1}{Et}(N_	heta - \mu N_oldsymbol{\phi})\ &ar{arpi} &= -rac{c}{Et}\sqrt{1+lpha^2 arepsilon^2}(N_oldsymbol{\phi} - \mu N_	heta) \end{aligned}$ | $\chi = \frac{\alpha^2 \xi}{Et} \left[\frac{1+\mu}{\sqrt{1+x^2 \xi^2}} (N_\theta - N_\phi) \right]$ | $-rac{d}{dec{\xi}}(N\phi-\mu N_{	heta}) ight]$ | |
|---|---|---|---|----------------------------|--|--|---|---|
| e AIF.1 Various loading systems on cooling towers a | shell dimensions $t = c\sqrt{1 + a^2\xi^2}$ | $\phi = c\sqrt{1+\beta^2\xi^2}$ | $	heta=rac{b^2}{c}\sqrt{(1-eta^2ec{arsigma}^2)^3}$ | shell forces | $N_{\theta} = \frac{p_E c \sqrt{1 + \beta^2 \xi^2}}{2 1 + \alpha^2 \xi^2} \left[\xi \sqrt{1 + \beta^2 \xi^2} - \frac{1}{2} (1 + \beta^2 \xi^2 - \alpha \cosh \beta \xi_0) \right]$ | $N\phi=N_{	heta}rac{lpha^2}{1+eta^2arkappi^2}-p_Ec\gamma^2arkappi,\ T=0$ | $N_{\theta} = -\frac{pc\alpha^{2}\sqrt{1+\beta^{2}\xi^{2}}}{2(1+\alpha^{2}\xi^{2})}[\xi^{2} - \xi^{2}_{0}] T = 0$ $N_{\phi} = N_{\theta} \frac{\alpha^{2}}{1+\beta^{2}\xi^{2}} - pc\sqrt{1+\beta^{2}\xi^{2}}$ | $\begin{split} N_{\theta} &= \gamma c^2 - \frac{\alpha^2 \sqrt{1 + \beta^2 \xi^2}}{1 + \alpha^2 \xi^2} \bigg[\frac{1}{3} \xi^3 - \frac{1}{2} \ddot{\xi}_0 \dot{\xi}^2 + \frac{1}{6} \ddot{\xi}_0^3 \bigg] \\ N_{\phi} &= N_{\theta} \frac{\alpha^2}{1 + \beta^2 \xi^2} - \gamma c^2 \sqrt{1 + \beta^2 \xi^2} (\xi - \xi_0) T = 0 \end{split}$ |
| Tab | | c threat radious b imaginary hyperbolic distance $a = \frac{b}{b}$ dimensionless parameters | $\beta = \sqrt{\frac{1}{p^2/q}}$ $\xi = \frac{\lambda}{p}$ dimensionless coordinate | /stem loading Imposed load | $ \begin{array}{c} & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & $ | $\int \int \frac{\xi}{\sqrt{1+\beta^2\xi^2}} p_z = p_E \frac{\xi}{\sqrt{1+\beta^2\xi^2}}$ | | $p_z = \gamma c (\xi - \xi_0)$ |



Solution

$$K = 3E^{(2I)}/L^{3}$$

= 948.15*KN/m*

$$Y_{st} = \frac{F_0}{K} = \frac{200}{948.15} 0.211 \,\mathrm{m}$$

w = circular frequency

$$= \sqrt{k/m}$$

= $\sqrt{\frac{948(9.81)}{150}} = 7.874$ rad/sec

Steady-state amplitude

$$r = \frac{\bar{w}}{w} = \frac{5.3}{7.874} = 0.673$$

$$Y = \frac{y_{st}}{(1 - r^2)^2 + (2r\xi)^2} = 0.38236 \,\mathrm{m}$$

The max. bending moment in the column = $V_{\text{max}} L$

$$lV_{\max(dyn)} = \frac{3EF}{L^3} \cdot Y$$

= $\frac{3 \times 200 \times 0.04}{(15)^3} (0.38263) = 2719 \text{ KN}$

$$M_{\rm dyn} = 2719 \times 15 = 40785 \,\rm KNm$$

AIF.4. Cooling Towers of Equal Radii

Stress resultants when cooling towers have top and bottom radii that are equally bounded by a smooth hyperboloid. The hyerbola is rotated by the *z* axis

$$\frac{B}{A} = \text{the slope of the asymptotes to the hyperbola}$$

$$A = R_0 \text{ at } Z = 0$$

$$R_0 = R_2 \sin \phi$$
(AIF.33)

With the surface intersection to a vertical plane parallel to the x-z plane are

$$\frac{x^2 + A^2}{A^2} - \frac{Z^2}{B^2} = 1 \text{ or } \frac{x^2}{A^2} = \frac{Z^2}{B^2}$$
(AIF.34)

which is a straight line (A being the throat radius)

$$Z = \frac{B}{Z}x$$
 (AIF.35)

A vertical plane tangent to the waist circle $(R_0 = A)$ will intersect the surf straight lines of the same slope.

Equations are now rewritten in the following form:

$$\frac{\partial N_{\theta}}{\partial \theta} + N_{\theta\phi} \frac{\partial R_0}{R_1 \partial \phi} + \frac{\partial (N_{\phi\theta} R_0)}{R_1 \partial \phi} + \omega_{\theta} R_0 = 0$$

$$\frac{\partial (N_{\theta} R_0)}{R_1 \partial \phi} - N_{\theta} \frac{\partial R_0}{R_1 \partial \phi} + \frac{\partial (N_{\theta\phi})}{\partial \theta} + \omega_{\phi} R_0 = 0 \qquad (AIF.36)$$

$$\frac{N_{\phi}}{R_1} + \frac{N_{\theta}}{R_2} + \omega_y = 0$$

When *z* is the vertical coordinate, the radii will then become:

$$\frac{1}{R_1} = \frac{-\partial^2 R_0 / \partial^2 \partial_1^2}{[1 + (\partial R_0 / \partial x)^2]^{(3/2)}}$$

$$R_2 = \frac{R_0}{\sin \phi} \text{ and } R_0 = \frac{A}{B} (B^2 + Z^2)^{(1/2)}$$

$$\frac{\partial R_0}{\partial Z} = \frac{A^2}{B^2} \frac{Z}{R_0}; \quad \frac{\partial^2 R_0}{\partial Z^2} = \frac{AB}{(B^2 + Z^2)^{\frac{3}{2}}}$$
(AIF.37)

Substituting into Eq. (AIF.37) the value of R_1 will become

$$R_1 = -A^2 B^2 \left(\frac{R_0^2}{A^4} + \frac{Z^2}{B^4}\right)^{(3/4)}$$
(AIF.38)

therefore

$$R_2 = A \left\{ 1 + \left(\frac{1}{B^2} + \frac{A^2}{B^4}\right) z^2 \right\}^{(1/2)}$$
(AIF.39)

and hence

$$R_1 = -\frac{B^2}{A^2} R_2^3$$
 (AIF.40)

Gravity loads

$$\omega_2 = -\omega \sin \phi; \, \omega_y = -\omega \cos \phi$$
 (AIF.41)

(Note the tangential axix Z_T along which ω_z is measured)

$$N_{\phi} = \frac{\omega}{2\pi R_2 \sin^2 \phi} = -\frac{1}{2\pi R_2 \sin^2 \phi} \int_0^{\phi} \omega 2\pi R_0 R_1 \, \mathrm{d}\phi$$

$$= -\frac{1}{R_2 \sin^2 \phi} \int_0^{\phi} \omega R_1 R_2 \sin \phi \, \mathrm{d}\phi$$

$$R_1 \, \mathrm{d}\phi = \mathrm{d}s = \frac{\mathrm{d}z}{\sin \phi}$$

$$\mathrm{d}z = R_1 \sin \phi \, \mathrm{d}\phi$$
 (AIF.42)

Eliminating all polar terms and saving extensive analytical work, the value of N_{ϕ} and N_{θ} will be evaluated as

$$N_{\theta} = -\omega_y R_2 + \frac{A^4}{B^2 R_2^2} N_{\phi} \qquad (\text{AIF.43})$$



Fig. AIF.4 Cooling tower

A solution for the cooling tower existing in the Trojan Nuclear Power Plant of the Portland General Electric Company (GEC) built in 1974.

Data: A = 9.1 m, B = 21.3 m; $z_{\text{top}} = 9.1 \text{ m}$; $z_{\text{bottom}} = 30.5 \text{ m}$ Intensity: Dead load 23.6kN/m². The stresses due to dead loads are desired strsses.

Notation for Figure AIF.5

$$\frac{R^2}{a^2} - \frac{z^2}{b^2} = 1$$
 (AIF.44)

In which R is the horizontal radius of the parallel circle; z is the vertical coordination along the axis of revolution; and a, b are characteristic curvature dimensions.

The principal radii of curvature are:

$$R_1 = -\frac{a\sin^2 \alpha \cos \alpha}{\left(\cos^2 \alpha - \cos^2 \theta\right)^{(3/2)}}$$
(AIF.45)

$$R_2 = \frac{R}{\sin \theta} \tag{AIF.46}$$

In which $\cot \alpha = a/b$ and $\tan \theta = (R/Z) \tan^2 \alpha$; R_1 and R_2 are the meridiona circumferential radii of curvature, respectively, and θ = the angle between the node to the surface and the axis of revolution.

Geometry of Hyperboloid of Revolution

The dependent variable can be separated using Fourier expansion. For example, displacements may be written as

$$u = \sum_{n=0}^{a} hu \cos n\phi.$$
 (AIF.47)

$$v = \sum_{n=0}^{a} hv \sin n\phi \tag{AIF.48}$$

$$w = \sum^{a} hw \cos n\phi \tag{AIF.49}$$



Fig. AIF.25 Geometry and stresses of cooling towers

Solution

Design factors

$$R_0(\text{at base}) = A \left\{ 1 + \frac{z^2}{B^2} \right\}^{(1/2)} = 15.894 \text{ m}$$
 (AIF.50)

$$\tan\phi = \frac{B}{A} \left\{ \frac{R_0}{R_0^2 - A^2} \right\}^{(1/2)} = 2.855; \ \cos\phi = \frac{A}{\left(A^2 + B^2\right)^{(1/2)}} \phi^1 \qquad (\text{AIF.51})$$

where $\phi^1 = 0.8415, f(\phi') = 8.277, R_0 = 9.95 \text{ m}; \tan \phi = 2.6245$ (AIF.52)

Appendix F

$$\cos\phi = \left\{\frac{4}{\sqrt{A^2 + B^2}}\right\} \times 0.8415 = 0.33041$$
$$N\phi = -\frac{W}{4}B^2 \left\{A^2 + B^2\right\}^{(1/2)} \frac{\left\{1 - \phi'^2\right\}^{(1/2)}}{(A^2 + B^2 - A^2 \phi'^2)} \left[f(\phi') - f(\phi'_0)\right]$$

At base = $13.58 \times 10^4 \text{ kN/m}$

$$N\phi = \frac{WA^2}{\left\{A^2 + B^2\right\}^{(1/2)}} \frac{\phi'}{\left\{1 - {\phi'}^2\right\}^{(1/2)}} + N\phi \frac{A^2}{B^2} (1 - {\phi'}^2)$$
(AIF.53)

At base = 7344 kN/m^2

$$N_{\phi(\text{Top})} = 0 \text{ since } f(\phi'_0) - f'(\phi'_0) = 0$$

$$N_{\theta(\text{Top})} = \frac{-WA^2}{\{A^2 + B^2\}^{(1/2)}} \frac{\phi'_0}{\{1 - \phi'_0{}^2\}^{(1/2)}} = 12.3 \text{ kN/m/m}$$
(AIF.54)

$$\frac{N_{\phi}}{R_1} + \frac{N_{\phi}}{R_2} = -z = w \cos\phi \qquad (AIF.55)$$

$$R_{2} \text{ (at base)} = \frac{R_{0}}{\sin \phi} = \frac{R_{0}}{\tan \phi \cos \phi} = \frac{15.894}{2.855 \times 0.3306} = 16.84$$

$$R_{1} = \frac{R_{2}^{3}}{(A^{2}/B^{2}) \times A^{2}} = \frac{(16.84)^{3}}{(9.1)^{4}} \times (21.3)^{2} = 316$$
(AIF.56)

Other values for *R* can be computed where variations exist. The same applied *ZZ* values, i.e. $w \cos \phi$ where w can be from wind, live loads and others. For de### $w \cos \phi = -23.6 \times 0.33041 = -7.8 \text{ kN/m}^2$. Similarly, stresses for any load correlation can be determined and the results are tabulated for the long-itudinal and tragetic stresses along the entire height of the tower.

AIF.5 Damage Scenario of the Cooling Tower

A crack pattern and a map of meridional stresses are shown in Figures AIF.6 and AIF.7 using ISOPAR and DIANA software with a fracture simulation technics.

The entire shell was discredited with degenerated finite shell elements. Eight noded isoperimetric layer shell elements were used. With a special preprocessor, geometric imperfection and large deformations were taken into account. Smeared cracking option is used. Two grids of embedded steel bars reinforce the tower shell. Plastic flow of the reinforcing bars is considered. Bilinear softening is also employed. The analysis is considered using the shell stiffened and unstiffened. Wind directions with different intensities and distributions due to interference were considered. The maximum wind assumed is 150 miles/h, The results presented are based on this wind integrity based on BS 6399. A reference is made to the author's text: *Prototype Building Structures – Analysis and Dedign*. Thomas Telford, 1999.

Fig. AIF.6 Finite element analysis



$$u = \frac{T_{1c}l_c}{2Eb_c d_c \sin^2 \alpha_0}$$
$$v = \frac{S_c l_c}{2Eb_c d_c \cos^2 \alpha_0}$$
$$w = \frac{\bar{Q}_{1c}l_c^3}{6EI} + \frac{M_{1c}l_c^2}{2EI \sin^2 \alpha_0}$$
$$\psi = \frac{\bar{Q}_{1c}l_c^2}{4EI \sin \alpha_0} + \frac{M_{1c}l_c}{2EI \sin^2 \alpha_0}$$

in which $I = b_c d_c^3/12$ and the subscript *c* applied to forces and moments indica summation over the frame width $(2I_c \cos \alpha_0)$.

Notation

 $\begin{array}{lll} a,b & = \mbox{characteristic curvature dimensions} \\ b_c & = \mbox{breadth of column} \\ C & = \mbox{elastic constant} \\ C_0 & = \mbox{extensional stiffnesses of the shell} \\ C_1, C_{12} & = \mbox{extensional meridional and shear stiffnesses respectively} \\ D_0 & = \mbox{flexural stiffnesses of shell} \end{array}$



Fig. AIF.7 Damage scenario of a cooling tower shell. Finite element mesh schemes. (a) Unstiffened shell. (b) Stiffened Shell. (DYNA-3D and ISOPAR-5 programs.)



Fig. AIF.8 V Supports for cooling towers

 D_I, D_{12} = flexural meridional and twisting stiffnesses respectively; d_c = depth of column E = Young's modulus

AIF.6 Quick Manual Solution Based on American Practices from the Equation of the Surface Defined

a = 70'; b = 181.6' x = 74.5; z = -65.5 when 2x = 149'h_{top} = 200' dia = 149'; $\beta = 20^{\circ}$ h = 214.3' dia = 140'; $\beta = 0$ h = 20.6' dia = 161.6'; $\beta = 30^{\circ}$ h = 0' dia = 251.8'; $\beta = 50^{\circ}$ t = thickness = 6'' w = self weight/unit area of membrane surface = 71.9 lbs/ft² At base of the tower = $\tan \beta = \frac{z}{b} = \frac{214.3}{181.6}$

| $\alpha = \sqrt{a^2 \tan^2 \beta + b^2 \sec^2 \beta} = 293.58$ | | | | | |
|--|----------------|--|--|--|--|
| Several values o | f | | | | |
| β | \overline{X} | | | | |
| -15° | -78 | | | | |
| -5° | -71 | | | | |
| 15° | -78 | | | | |
| 25° | -89 | | | | |
| 35° | -131 | | | | |
| 45° | -209 | | | | |
| Summation | -722 | | | | |

The value of $\bar{X} = -722 \times 72 \times 0.1745$ rad = -9080Stresses $N_{\phi} = \frac{\bar{X}\alpha}{a \sec^2 \beta} = \frac{9080 \times 293.58}{70 \times 2.4} = \frac{15900}{72} = 15900$ lbs/ft corresponding comp stress $N_{\theta} = \frac{a^2}{\alpha^2} N_{\phi} - \frac{a^2}{b^2} \tan \beta = 939$ lbs/ft σ (comp. stress) = 13 psi

Due to self weight Nominal steel will be required.

When other loads are applied the results from them will be algebraically added. Those loads may be wind and seismic loads.

```
Computer program: Dynamic wind pressure on cooling
tower (NAZAM-4)
C * Prepared by Liu, checked by Y. Bangash
C * THE SUBPROGRAM FINDS THE DYNAMIC WIND PRESSURE AT *
C * DIFFERENT HEIGHTS OF THE COOLING TOWER UNDER THE *
C * BASIC WIND SPEED 100 MPH (45 M/S).
                                                   *
C * THE BASIC WIND SPEED (V) IS THE 3-SECOND GUEST
                                                   *
C * SPEED ESTIMATED TO BE EXCEEDED ON THE AVERAGE
                                                   *
C * ONCE IN 100 YEARS.
                                                   *
C * TOPOGRAPHICAL FACTOR = S1
                                                   *
C * SHAPE FACTOR = S
                                                   *
C * STATISTICAL FACTOR = S2
                                                   *
C * FORCE COEFFICIENT = CF
                                                   *
C * DESIGN WIND SPEED (VS) = V*S1*S*S2
C * DYNAMIC WIND PRESSURE (PW) = CF*0.613*(VS**2)
                                                  *
С
С
   FUNCTION SUBPROGRAM
   SUBROUTINE WIND (PW, A, B, T, ZE)
   V = 45.0
   S1=1.0
   S3=1.0
   Z=B^* (TAN (T*0.01745))
   C = (ABS(Z/B)) * * 2.0
   XX = (A^* ((1.0+C)^{**}0.5))
   H = 7E - 7
   HEIGHT/BREADTH==RATIO
С
   CALL SHAPE (S,H)
   SP=S1*S*S3
   VS = (V*SP)
   O = 0.613 * ((VS) * 2.0)
   HB=H/(XX+XX)
   CALL COEF (CF, HB)
   PW = (CF * O) / 1000
   RETURN
   END'
   WRITE (6,4)
4
   FORMAT (///, 2X, 'THETA', 8X, 'BETA', 8X,
    'MERIDI NAL', 8X, *'HOOP', 13X, 'WIND')
   WRITE (6,5)
   FORMAT (27X, 'FORCES', 11X, 'FORCES', 11X, 'PRESSURE')
5
   WRITE (6,6)
```

```
782
```

```
FORMAT (/, 2X, ' (Deg.)', 7X, ' (Deg.)', 7X, ' (KN/m)',
6
    11X,'*' (KN/m)', 10X, (KN/m**2)'/2X, 6('*'), 7X,
    6('*'), 6X, 9('*'), * 8X, 10('*'), 7X, 9('*'))
    DO 100 T=-15,45,10
    CALL WIND (PW, A, B, T, ZE)
   AA = (X/Z) * (y^{*} * 2)
   O=ATAN (AA)
   H=SIN (O)
   K=COS (O)
   R1 = (Z^{*}3) / ((B^{*}2)^{*}(V^{*}2)^{*}(K^{*}3))
   R2=X/H
    P=X/A
   PO=RU/A
    ZO = -(HE - ZE)
   N=Z/B
   NO=ZO/B
    BB = (Y^* * 2) / ((P^* * 2) * H)
    YP = ((Y^{*}2.0) - 2.0)^{*} (P^{*}3.0 - PO^{*}3.0) / (3.0^{*} (Y^{*}2.0))
   PD=PO-P
   OPN=(NO*PO)*(N-NO)
   IL=N*(ALOG((N+P)/(NO+PO)))
С
   MERIDINAL FORCES DUE TO WIND LOADING = ANPP
   ANPP = ((PW*A)/6.0)*BB*(YP+PD-OPN+IL)*(COS(AN))
   HOOP FORCES DUE TO WIND LOADING = ANXX
С
   ANXX = (-1)*(ANPP)*(R2/R1) - (PW*R2*(COS(AN)))
С
   TOTAL MERIDINAL FORCES = MSUM
   MSUM=ANPP+ANP
С
   TOTAL HOOP FORCES = HSUM
   HSUM=ANXX+ANX
   WRITE (6,111) T.F.MSUM, HSUM, PW
111 FORMAT (1X, F6.2, 6X, F7.2, 6X, E10.3, 8X, E10.3,
    8X, F6.3)
101 CONTINUE
100 CONTINUE
    STOP
   END
  С
С
   * SUBROUTINE FOR FORCE COEFFICIENT
   С
    SUBROUTINE COEF (CF, HB)
    IF ((HB.GT.0.0) .AND.(HB.LE.0.5)) CF=0.70
    IF ((HB.GT.0.5) .AND.(HB.LE.1.0)) CF=0.70
    IF ((HB.GT.1.0) .AND.(HB.LE.2.0)) CF=0.80
    IF ((HB.GT.2.0).AND.(HB.LE.4.0)) CF=0.80
```

```
IF ((HB.GT.4.0) .AND.(HB.LE.6.0)) CF=0.80
    IF ((HB.GT.6.0) .AND.(HB.LE.10.)) CF=0.90
   IF ((HB.GT.10.0) .AND.(HB.LE.20.)) CF=0.90
   IF (HB.GT.20.0)
                                     CF=1.00
   RETURN
   END
SUBROUTINE SELF (AND ANY ZE, A, B, DENS ANG)
   H=1/(COS(TT))**2
С
   LET D BE ALPHA
   D=((A^{*}2)^{*}((ZE/B)^{*}2) + (B^{*}2)^{*}(H))^{*}0.5
   SUM=0.0
   DEF=-(A*(B**2+A**2*(SIN(T*0.01745))**2)**0.5)/
   * (B* (COS (T*0.01745)**3))
   SUM=SUM+DEF
   SG=SUM* ANG* DENS
   ANP= (SG^*D) / (A^*H)
   ANX = (((A^{*} 2) / (D^{*} 2))^{*} ANP - (A^{*} 2 / B)^{*} (ZE / B))
   RETURN
   END
С
   С
С
   * SUBROUTINE FOR SHAPE FACTOR
                                                    +
С
   SUBROUTINE SHAPE (S, H)
    IF ((H.EQ.0.0) .AND. (H.LE.3.0)) S=0.73
   IF ((H.GT.3.0) .AND. (H.LE.5.0)) S=0.78
   IF ((H.GT.5.0) .AND. (H.LE.10.0)) S=0.90
   IF ((H.GT.10.0) .AND. (H.LE.15.0)) S=0.94
   IF ((H.GT.15.0) .AND. (H.LE.20.0)) S=0.96
   IF ((H.GT.20.0) .AND. (H.LE.25.0)) S=0.98
   IF ((H.GT.25.0) .AND. (H.LE.30.0)) S=1.00
   IF ((H.GT.30.0) .AND. (H.LE.35.0)) 5=1.02
   IF ((H.GT.35.0) .AND. (H.LE.40.0)) S=1.03
   IF ((H.GT.40.0) .AND. (H.LE.45.0)) S=1.05
   IF ((H.GT.45.0) .AND. (H.LE.50.0)) S=1.06
   IF ((H.GT.50.0) .AND. (H.LE.60.0)) S=1.08
   IF ((H.GT.60.0) .AND. (H.LE.70.0)) S=1.10
   IF ((H.GT.70.0) .AND. (H.LE.80.0)) S=1.11
   IF ((H.GT.80.0) .AND. (H.LE.100.0)) S=1.13
   IF ((H.GT.100.0) .AND. (H.LE.120.0)) S=1.15
    IF ((H.GT.120.0) .AND. (H.LE.140.0)) S=1.17
```

IF ((H.GT.140.0) .AND. (H.LE.160.0)) S=1.19 IF ((H.GT.160.0) .AND. (H.LE.180.0)) S=1.20 IF ((H.GT.180.0) .AND. (H.LE.500.0)) S=1.21 RETURN END

- l = non-dimensional length of the meridian
- $l_c = \text{length of column}$

 M_1, M_2 = meridional and circumferential bending moment

- n = harmonic number in circumferential direction
- \bar{Q}_1 = effective meridional transverse shear force
- R = radius of parallel circle
- R_1, R_2 = meridional and circumferential radii, respectively
- S = membrane shear force

 T_1, T_2 = meridional and circumferential membrane forces, respectively

- U, V, W = nondimensional displacements, u/h, v/h, w/h, respectively
- u, v, w = meridional circumferential and normal displacements, respectively
- Z = vertical coordinate along axis of revolution

$$\alpha = \cot^{-1} \left(a/b \right)$$

- α_0 = inclination of columns of horizontal in their own plane
- β = nondimensional factor of order of 10
- θ = angle between normal to surface and vertical axis
- μ = Poisson's ratio
- ϕ = circumferential angle
- ψ = meridional angle of rotation

Subscript *c* refers to summation over circumferential length $(2l_c \cos \alpha_0)$.

Equivalence method

Considering the supporting system of columns, it can be shown that its equivalent uniform stiffnesses are

Membrane force,
$$T_1$$
; $C_1 = E \frac{b_c d_c \sin^3 \alpha_0 (1 - \mu^2)}{l_c \cos \alpha_0}$ (AIF.57)

Membrane shear,
$$S; C_{12} = E \frac{b_c d_c \sin \alpha_0 \cos \alpha_0 (1 - \mu^2)}{l_c}$$
 (AIF.58)

Bending moment,
$$M_1; D_1 = E\left[\frac{I\sin^3\alpha_0}{l_c\cos\alpha_0} + 4\frac{i}{l_c}\frac{\sin\alpha_0\cos\alpha_0}{(1+\mu)}\right]$$
 (AIF.59)

Torsion,
$$H; D_{12} = E\left[\frac{4I}{l_c}\sin\alpha_0\cos\alpha_0 + \frac{8}{(1+\mu)}\frac{i}{l_c}\right]$$
 (AIF.60)



| Table AIF.2 | | | | | | |
|--------------------|---------------|-------|-------|--|--|--|
| | Case number | | | | | |
| | 1 | 2 | 3 | | | |
| Relative stiffness | (Equivalence) | | | | | |
| (1) | (2) | (3) | (4) | | | |
| (C_1/C_0) | 1.16 | 1.19 | 0.12 | | | |
| (C_{12}/C_0) | 0.154 | 0.159 | 0.159 | | | |
| (D_1/D_0) | 43.7 | 1.60 | 16.0 | | | |
| (D_{12}/D_0) | 175.0 | 0.0 | 0.0 | | | |

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