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Lecture Notes in Chemistry

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Qualitative
Valence-Bond Descriptions
of Electron-Rich Molecules:
Pauling "3-Electron Bonds"
and "Increased-Valence" Theory



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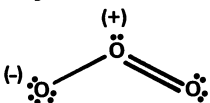
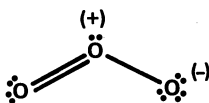
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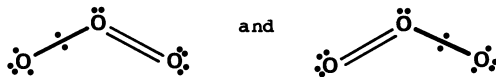
PREFACE

This book provides qualitative molecular orbital and valence-bond descriptions of the electronic structures for electron-rich molecules, with strong emphasis given to the valence-bond approach. Electron-rich molecules form an extremely large class of molecules, and the results of quantum mechanical studies from different laboratories indicate that qualitative valence-bond descriptions for many of these molecules are incomplete in so far as they usually omit "long-bond" Lewis structures from elementary descriptions of bonding. For example, the usual representation for the electronic structure of the ground-state for O_3 involves resonance between the

standard Lewis structures  and . Until recently, any contribution to resonance of the "long-bond" (or spin-paired

diradical) Lewis structure  has been largely ignored. However, it

has now been calculated to be a very important structure. For the ground-states of numerous other systems, calculations also indicate that "long-bond" structures are more important than is usually supposed, and therefore they should frequently be included in qualitative valence-bond descriptions of electronic structure. The book describes how this may be done, and some of the resulting consequences for the interpretation of the electronic structure, bond properties and reactivities of various electron-rich molecules. When appropriate, molecular orbital and valence-bond descriptions of bonding are compared, and relationships that exist between them are derived. Considerable attention is given to the use of Pauling "3-electron bonds" ($A \cdot \cdot B$) and "increased-valence" structures for providing qualitative valence-bond descriptions of electronic structure. The "increased-valence" structures for electron-rich molecules - for example



- are equivalent to resonance between standard and "long-bond" Lewis structures, and usually involve Pauling "3-electron bonds" as diatomic components. Because they include both the "long-bond" and the standard Lewis structures, the "increased-valence" structures must always provide a lower-energy representation of electronic structure than do the more familiar qualitative descriptions that utilize only the standard Lewis structures.

To provide the necessary background for readers who are familiar only with the elements of qualitative valence-bond and molecular orbital theory, extensive use is made of an elementary, even pedagogical, approach. Some relevant valence-bond and molecular orbital concepts are reviewed briefly in the first chapter. After a

discussion of the need for an "increased-valence" theory in Chapter 2, Chapters 3 to 9 are concerned primarily with qualitative descriptions of the electronic structures for numerous paramagnetic molecules that may have Pauling "3-electron bonds" as components in their valence-bond structures. The bonding and magnetic behaviour for the dimers of some of these molecules are also discussed in Chapters 7 and 8, using both Lewis valence-bond and molecular orbital theory. It is shown that if the monomer has a Pauling "3-electron bond" then the dimer may require "long-bond" as well as standard Lewis structures to contribute significantly to the ground-state resonance. An "increased-valence" description of the bonding for one of these dimers, namely N_2O_4 , is developed in Chapter 10; this provides a convenient connection between the Pauling "3-electron bond" theory for paramagnetic molecules, and the "increased-valence" theory of the remaining Chapters for (mostly) diamagnetic molecules.

The "increased-valence" theory represents a natural extension of the more familiar Lewis-Langmuir-Pauling valence-bond theory, and therefore an understanding of it may be useful for all chemists who have an interest in simple descriptions of electronic structure. For more than a decade, I have published various papers on this subject, and the present volume includes a considerable number of examples from them, together with numerous new applications.

For readers who wish to give primary consideration to the "increased-valence" theory, Sections 3-6, 3-9, 4-1 to 4-7, 6-1, 7-1 and 7-2 are the main components of the earlier chapters that are required as background for Chapters 10 to 24. A reading of Chapter 2 might also be appropriate in order to obtain a rationalization of the need for an "increased-valence" theory.

The production of this book has been helped by a number of people. The very numerous valence-bond structures and some of the diagrams were prepared primarily by Pamela Richards, with some assistance from Mr Brian Nairn (Melbourne State College), and Suzie Boxhall and Anne Pottage, (Centre for Study of Higher Education, University of Melbourne). Lesley Flanagan, Renae Alexander and Elizabeth Duff typed the draft manuscript. The final typing required considerable ingenuity; this was most capably provided by Dr William Hall, (Queen's College, University of Melbourne), using Multifont-Wordstar on a Boffin microcomputer. The Publication Sub-Committee of Melbourne University made available a generous grant to help defray production costs. I thank them, my research students, and Professor A.S. Buchanan, who gave me the opportunity to teach valence theory at Melbourne University. Special thanks are also due to Professor R.D. Brown (Monash University) who influenced and inspired me during my Ph.D. years. This book developed from the research problem that he suggested, namely why is the N-N bond of N_2O_4 long and weak.

Finally, I dedicate this book to my parents.

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CHAPTER 1

ATOMIC ORBITALS, ELECTRON SPIN, LINEAR COMBINATIONS

We shall provide here a brief survey of the relevant background quantum mechanics that is required for the chemical bonding treatment presented in this book. In general, we shall state only the main results, without any derivation of them. Much, if not all of this material should be familiar to many readers. For fuller treatments, the reader should consult some of the numerous standard texts¹ on quantum mechanics and valence.

1-1 ATOMIC ORBITALS

For any atom, there are n^2 atomic orbitals with principal quantum number n ($= 1, 2, 3, \dots$). These orbitals may be classified as ns , np , nd , nf , ... according to the value of the total orbital angular momentum quantum number l ($\equiv 0, 1, 2, \dots n - 1$) for an electron. For each value of l , there are $2l + 1$ orbitals. Thus, there are one $3s$, three $3p$ ($3p_x$, $3p_y$ and $3p_z$) and five $3d$ ($3d_{xy}$, $3d_{xz}$, $3d_{yz}$, $3d_{x^2-y^2}$ and $3d_{z^2}$) orbitals for $l = 0, 1$ and 2 ; here we have assumed that the np and nd orbitals are all real orbitals[†]. For certain purposes, the nd_{xy} , nd_{xz} and nd_{yz} are designated as t_{2g} orbitals, and the corresponding designation for the remaining pair of nd orbitals is e_g . Schematic contours for $1s$, $2p$ and $3d$ orbitals are displayed in Fig. 1-1.

When the atomic orbitals are located on the same atomic centre, it is often useful to consider the *hybridization* of some of them, i.e., to construct linear combinations of them. This may be done either by requiring that the energy of the linear combination in the molecule be a minimum, or that the bond-angles determine the nature of the hybridization^{††}. The latter is usually used for elementary discussions of (approximate) hybridization of orbitals in valence-bond structures,

[†] The hydrogenic atomic orbitals have the general form $\psi(r, \theta, \phi) = R(r)\Theta(\theta)\Phi(\phi)$, in which r , θ and ϕ are the polar coordinates for the electron. For complex atomic orbitals, $\Phi(\phi) = \exp(im_z\phi)$ with $i = \sqrt{-1}$ and $m_z = 0, \pm 1, \pm 2, \dots \pm l$. The np_{+1} , np_0 and np_{-1} orbitals have $m_z = +1, 0$ and -1 . The real np orbitals are related to the complex orbitals as follows:

$$np_x = (np_{+1} + np_{-1})/2, \quad np_y = (np_{+1} - np_{-1})/2i, \quad np_z \equiv np_0.$$

In the absence of a magnetic field, orbitals with the same n and l values are *degenerate*, i.e. they have the same energies; for given n and l values, the number of degenerate orbitals is $2l + 1$.

^{††} If λ_1 and λ_2 are the hybridization parameters for two orthogonal hybrid atomic orbitals $h_1 = s + \lambda_1 p_1$ and $h_2 = s + \lambda_2 p_2$, then the angle θ between the hybrid orbitals is given by the Coulson formula² $\cos \theta = -1/\lambda_1 \lambda_2$. If the hybrid orbitals are assumed to be oriented along the bond axes for two σ -bonds that emanate from the atomic centre, then this angle is the bond angle. The "orbital following" which is then concomitant with this approach has been recently questioned (see Ref. 3 for details), but we shall follow Symons and "continue to use this extremely useful concept"^{3b}.

and is therefore appropriate for the valence bond treatments that we shall present in this book. For our purposes, the most relevant of the hybrid orbitals are the following, in which we have indicated the explicit forms of the linear combinations for only the first two, for the special cases of equivalent hybrids.

(i) Digonal: sp ($h_1 = (s + p)/2^{1/2}$, $h_2 = (s - p)/2^{1/2}$)

(ii) Trigonal: sp^2 ($h_1 = (s + 2^{1/2}p_x)/3^{1/2}$, $h_2 = (2^{1/2}s - p_x + 3^{1/2}p_y)/6^{1/2}$,
 $h_3 = (2^{1/2}s - p_x - 3^{1/2}p_y)/6^{1/2}$)

(iii) Tetrahedral: sp^3 .

(iv) Square planar: sp^2d (ns , np_x , np_y and $nd_{x^2-y^2}$) and dsp^2 ($nd_{x^2-y^2}$, $(n+1)s$, $(n+1)p_x$ and $(n+1)p_y$) for atoms of main-group elements and transition metals.

(v) Trigonal bipyramid: sp^3d (ns , three np and $nd_{x^2-y^2}$ or nd_{z^2}) and dsp^3 ($nd_{x^2-y^2}$ or nd_{z^2} , $(n+1)s$ and three $(n+1)p$) for atoms of main-group elements and transition metals. For each of sp^3d and dsp^3 an infinite number of linear combinations of $d_{x^2-y^2}$ and d_{z^2} is possible to form the appropriate d orbital for the hybridization scheme.

(vi) Octahedral: sp^3d^2 (ns , three np , $nd_{x^2-y^2}$, nd_{z^2}) and d^2sp^3 ($nd_{x^2-y^2}$, nd_{z^2} , $(n+1)s$ and three $(n+1)p$) for atoms of main-group elements and transition metals.

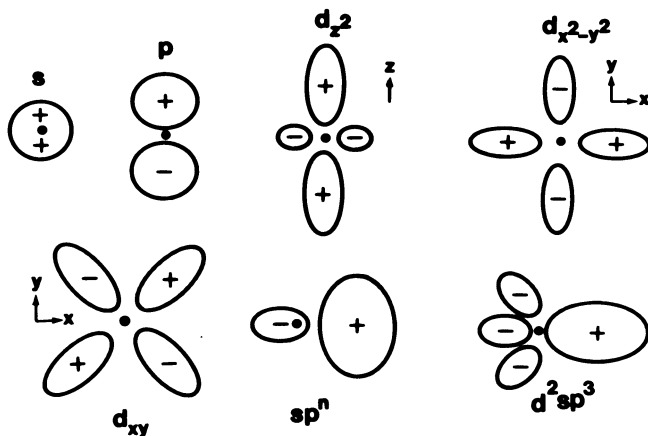


Figure 1-1 Schematic contours for $1s$, $2p$, $3d$, sp^n and d^2sp^3 atomic orbitals.

Schematic contours for some of these hybrid atomic orbitals are displayed in Fig. 1-1. In Fig. 1-2, we show the number of bonds and lone-pairs at a given atom when these hybridization schemes are appropriate for the formation of σ -bonds.

shape	σ -bond hybridization	σ -bonds	number of lone pairs	π -bonds	valence-bond structure
linear	sp	2	0	0	—A—
		2	0	1	≡A—
		2	0	2	≡A≡
trigonal planar	sp ²	3	0	0	
		3	0	1	
trigonal pyramidal	sp ²	4	0	0	
angular	sp ²	2	1	1	
tetrahedral	sp ³	4	0	0	
		4	0	2	
pyramidal	sp ³	3	1	0	
		3	1	1	
angular	sp ³	2	2	0	
square planar	dsp ²	4	4	0	
trigonal bipyramidal	sp ³ d	5	0	0	
distorted tetrahedral	sp ³ d	4	1	0	
		4	1	1	
"T-shaped"	sp ³ d	3	2	0	
octahedral	sp ³ d ²	6	0	0	
square-pyramidal	sp ³ d ²	5	1	0	
		5	1	1	
planar	sp ³ d ²	4	2	0	
pentagonal-bipyramidal	sp ³ d ³	7	0	0	

Figure 1-2 Lewis valence-bond structures for different σ -bond hybridization schemes. (Adapted from E. Carmell and G.W.A. Fowles, *Valency and Molecular Structure* (4th ed. Butterworths, 1977).

Any real orbital ψ is *normalized*[†] if $\int \psi^2 dv = 1$; if $\int \psi_i \psi_j dv = 0$ for a pair of real orbitals, then the orbitals are *orthogonal*. The square of a real orbital,

[†] For a real atomic orbital in an atom, $\int \psi^2 dv = \int_0^\infty \int_0^\pi \int_0^{2\pi} \psi^2 r^2 \sin \theta dr d\theta d\phi$. Later, $d\equiv d\tau_1 d\tau_2 d\tau_3 ds_1 ds_2 ds_3 \dots$, with s_i = "spin coordinate" for electron i .

(ψ^2) gives the charge density, or probability density for an electron when it occupies the orbital. The integral $\int \psi^2 dv = 1$ gives the total charge when one electron occupies a normalized orbital.

1-2 ELECTRON SPIN

The spin quantum number $s = 1/2$ for an electron determines the magnitude of the total spin angular momentum according to the formula $\sqrt{s(s+1)} (h/2\pi)$ (with $h = \text{Planck's constant}$). When an external magnetic field is applied, the spin angular momentum vector orients in two different directions so that the z-component of spin angular momentum (i.e. the component parallel to the direction of the magnetic field) takes values of $s_z (h/2\pi)$ with $s_z = \pm 1/2$. These orientations are displayed in Fig. 1-3.

For two electrons, the same types of spin angular momentum expressions pertain, with the two-electron spin quantum numbers S and S_z ($\equiv s_z(1) + s_z(2)$) replacing s and s_z . The allowed values for S and S_z are the following: (i) $S = 0, S_z = 0$; (ii) $S = 1, S_z = +1, 0, -1$, and the orientations of the spin angular momentum vectors for these quantum numbers

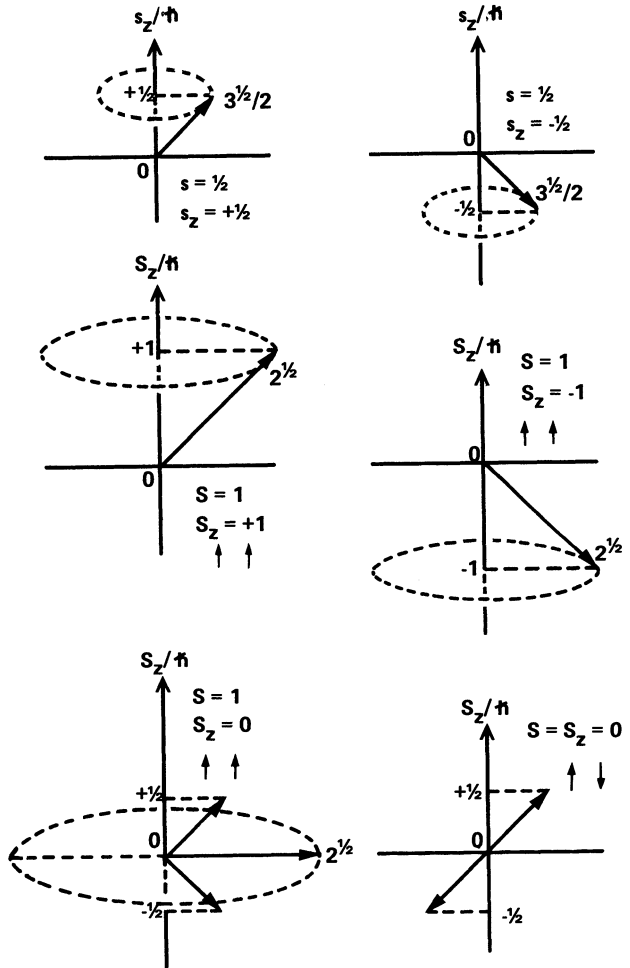


Figure 1-3 Orientations of spin angular momentum vectors for one and two electrons relative to an external magnetic field directed along the z-axis. $\hbar = h/2\pi$.

are also displayed in Fig. 1-3. The spin angular momentum vectors are parallel ($\uparrow\uparrow$) for $S = 1$, and antiparallel ($\uparrow\downarrow$) for $S = 0$.

In general, if the total spin quantum number for an atom or a molecule is S , there are $2S + 1$ values for the S_z spin quantum number, namely $S, S - 1, S - 2, \dots - S$.

If an atom or molecule has n singly-occupied orthogonal (i.e. non-overlapping) orbitals, the lowest-energy arrangement of the spins for the n electrons is that for which the spins are all parallel. This is a statement of Hund's rule of maximum spin multiplicity. The total spin quantum number is then $S = n/2$.

If an orbital is doubly-occupied, the Pauli exclusion principle does not allow the two electrons to have the same values for their s_z quantum numbers. Therefore, not more than two electrons may occupy the same orbital.[†]

Diamagnetic and paramagnetic substances develop magnetic moments that are respectively opposed to, and in the direction of an external magnetic field. The magnetic moments for the paramagnetic molecules that we shall discuss in this book arise either primarily or almost entirely from the presence of one or more unpaired-electron spins, i.e. the total spin quantum number S is non-zero for such a molecule. For a molecule with spin quantum number S , the spin angular momentum generates a magnetic moment of $\sqrt{n(n+2)}$ Bohr magneton for which $n \equiv 2S$ is the number of unpaired-electron spins.

1-3 LINEAR COMBINATIONS OF WAVE FUNCTIONS

If ψ_1 and ψ_2 are two (real) wave-functions, then linear combinations of the form $\psi = c_1\psi_1 + c_2\psi_2$ (or $\psi = \psi_1 + k\psi_2$) may be constructed, in which the coefficients c_1 and c_2 (or k) are constants. If the coefficients c_1 and c_2 are determined so that the energy of ψ (i.e. $E = \int \psi \hat{H} \psi d\tau / \int \psi^2 d\tau$ with \hat{H} = Hamiltonian operator) is a minimum, then provided that ψ_1 and ψ_2 interact (i.e. $H_{12} \equiv \int \psi_1 \hat{H} \psi_2 d\tau \neq 0$), two (orthogonal) linear combinations are generated that have respectively *lower* and *higher* energies than have either of ψ_1 and ψ_2 alone. The resulting energy-level diagrams are displayed in Fig. 1-4.

In the absence of magnetic fields, the Hamiltonian operator \hat{H} for a system of electrons in an atom or molecule involves the sum of kinetic and electrostatic potential energy operators (designated as \hat{T} and \hat{V}) for the electrons, i.e. $\hat{H} = \hat{T} + \hat{V}$. The \hat{T} operator is given by $\sum_i (-\hbar^2/8\pi^2m)\nabla_i^2$, and \hat{V} is the sum of the terms that involve the classical electrostatic attractions between the electrons and the atomic

[†] Without reference to electron spin, this result may also be deduced for atoms from Bohr circular orbit theory + Heisenberg uncertainty relationship⁴. For principal quantum number n , it may be deduced that a maximum of $2n$ electrons may occupy each of n independent circular orbits around the nucleus. There are n^2 atomic orbitals with principal quantum number n . Therefore $2n \times n/n^2 = 2$.

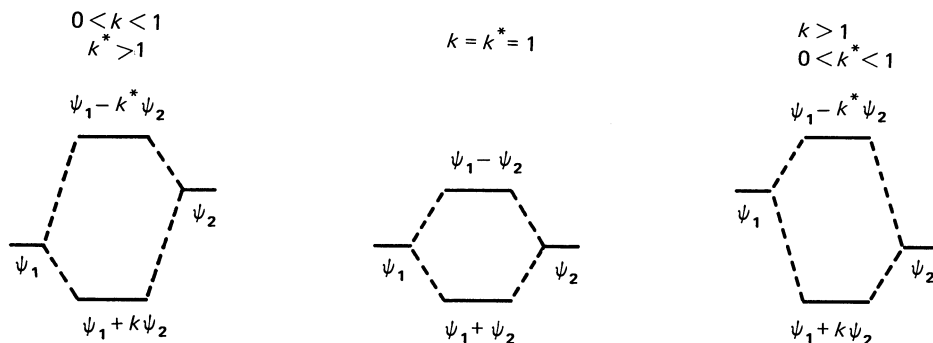


Figure 1-4 Energy level diagrams for the linear combinations of two interacting wave-functions ψ_1 and ψ_2 assuming that $\int \psi_1 \hat{H} \psi_2 d\tau < 0$. When $H_{12} = ES_{12}$ and $H_{22} \geq H_{11}$, no linear combination is stabilized relative to ψ_1 .

nuclei, and repulsions between the electrons. The requirement that $\partial E / \partial c_1 = \partial E / \partial c_2 = 0$ as a necessary condition that E is a minimum gives the secular equations

$$(H_{11} - E)c_1 + (H_{12} - ES_{12})c_2 = 0$$

$$(H_{21} - ES_{21})c_1 + (H_{22} - E)c_2 = 0$$

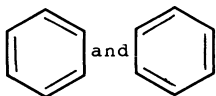
for normalized ψ_1 and ψ_2 , with $H_{ij} = \int \psi_i \hat{H} \psi_j d\tau$ and $S_{ij} = \int \psi_i \psi_j d\tau$.

In this book, the wave-functions ψ_1 and ψ_2 are of two main types:

(a) *Atomic orbitals*: If ψ_1 and ψ_2 are a pair of (real) atomic orbitals located on two atoms, the interaction integral (or resonance integral) $\int \psi_1 \hat{H} \psi_2 d\tau$ is non-zero if these atomic orbitals overlap, i.e. $\int \psi_1 \psi_2 d\tau \neq 0$. The lower and higher energy linear combinations of ψ_1 and ψ_2 are referred to as *bonding* and *antibonding* molecular orbitals respectively. If the atomic orbitals are located on the same atomic centre, then usually they are orthogonal (i.e. $\int \psi_1 \psi_2 d\tau = 0$). When this is the case, no lower-energy linear combination may be constructed. Linear combinations of atomic orbitals located on the same atomic centre are called hybrid atomic orbitals, and these have been discussed in Section 1-1.

(b) *Two-electron and many-electron configurations of electrons*: An electron configuration designates the orbital occupancies and spins for the electrons. The following two-electron or many-electron configurations need to be considered here:

(i) *Valence-bond structure functions (bond-eigenfunctions)*: These wave-functions describe the configurations of electrons that are associated with valence-bond structures. If a pair of valence-bond structures

((e.g. $\text{Li}-\text{H}$ and $\text{Li}^+ \text{:H}^-$ for LiH or  for C_6H_6) have

configuration wave-functions (or structure functions or bond-eigenfunctions) designated as ψ_1 and ψ_2 for their electrons, then the construction of linear combinations of these wave functions is equivalent to invoking resonance between the valence-bond structures. The valence-bond structures are said to be *stabilized by resonance* if one of the linear combinations has a lower energy than has either ψ_1 and ψ_2 alone. Resonance stabilization can only occur if $\int \psi_1 \hat{H} \psi_2 d\tau$ (the exchange integral) is non-zero. A necessary (but not necessarily sufficient) condition for this to occur is that the bond-eigenfunctions ψ_1 and ψ_2 must have the same sets of values for their S and S_z spin quantum numbers.

(ii) *Molecular orbital configurations*: If ψ_1 and ψ_2 are two different molecular orbital configurations with the same spatial symmetry and sets of spin quantum numbers (for example, ψ_1 and ψ_2 may represent two electrons that doubly occupy bonding and antibonding molecular orbitals, respectively), then lower-energy (and higher-energy) linear combinations of these two configurations may be constructed. This procedure is referred to as *configuration interaction*. Because the molecular orbitals are orthogonal, a lower-energy linear-combination may only be constructed if the configurations ψ_1 and ψ_2 do not differ in the orbital and spin designations of more than two electrons[†]. (This limitation does not necessarily apply to the bond-eigenfunctions of (i), because at least some of the atomic orbitals for these valence-bond configurations must overlap.)

If for any of (a) and (b), the functions ψ_1 and ψ_2 can also interact with a third wave-function ψ_3 , then the linear combination $\psi = c_1\psi_1 + c_2\psi_2 + c_3\psi_3$ (with c_1 , c_2 and c_3 chosen so that the energy of ψ is minimized) will have a lower energy than has either $\psi = c_1\psi_1 + c_2\psi_2$ or ψ_3 alone. If ψ is a molecular orbital formed from the linear combination of three overlapping atomic orbitals ψ_1 , ψ_2 and ψ_3 that are

[†] With self-consistent field molecular orbital theory, no direct interaction can occur between the lowest-energy configuration with doubly-occupied molecular orbitals and singly-excited $S = 0$ configurations with the same symmetry as that of the lowest-energy configuration, if the orbitals used to construct all configurations are the "best" orbitals for the lowest-energy configuration.

centred on three atomic nuclei, this molecular orbital is referred to as a *delocalized* or *3-centre* molecular orbital. We shall encounter such molecular orbitals on a number of occasions, and shall usually use the symbols y , a and b to designate the atomic orbitals ψ_1 , ψ_2 and ψ_3 .

Diatomic molecular orbitals which are either symmetric or antisymmetric with respect to rotation around the bond-axis are designated as σ and π . Alternatively, these orbitals have, respectively, 0 and 1 nodal planes (i.e. planes on which the orbital wave-function is zero at all points) that pass through the atomic nuclei and include the bond axis. There are two sets of degenerate π -type molecular orbitals, which we shall label here as either π_x and π_y (assuming that the z -axis is the bond axis) or π and $\bar{\pi}$. These molecular orbitals have, respectively, the xz and yz planes as nodal planes. Bonding and antibonding diatomic molecular orbitals have 0 and 1 nodal planes passing through the bond axis parallel to the xy planes. Their energies are respectively less than, and greater than the atomic orbitals from which they are constructed. The same theory is appropriate for the delocalized molecular orbitals of linear triatomic and linear polyatomic molecules. For non-linear planar molecules, the delocalized molecular orbitals may be either of σ or π or $\sigma + \bar{\pi}$ type, with π non-degenerate. The $\sigma + \bar{\pi}$ molecular orbitals have σ -symmetry with respect to at least one pair of adjacent atoms, and $\bar{\pi}$ symmetry with respect to at least another pair of adjacent atoms. In Fig. 1-5, atomic orbitals that may be used to construct $\sigma + \bar{\pi}$ molecular orbitals for N_2O_2 and FNO are displayed.

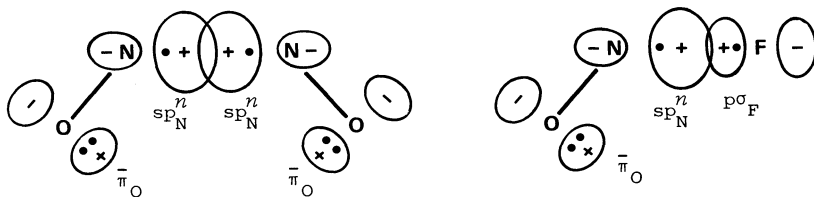


Figure 1-5 Atomic orbitals for $\sigma + \bar{\pi}$ molecular orbitals of N_2O_2 and FNO.

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1. See for example (a) R.W. McWeeny "Coulson's Valence" (Oxford, 1979); (b) J.N. Murrell, S.F.A. Kettle and J.M. Tedder "The Chemical Bond" (John Wiley, 1978).
2. Ref. 1(a), p. 196.
3. M.C.R. Symons, Chem. Soc. Specialist Reports: E.S.R. (a) **5**, 146 (1979); (b) **6**, 108 (1981).
4. R.D. Harcourt, (a) Naturwiss., **64**, 485 (1977); (b) Specul. Sci. Techn. **1**, 338 (1978). (For applications of Bohr circular orbit theory to descriptions of bonding, see also Spec. Sci. Techn., **2**, 527 (1979); **3**, 77, 628 (1980); **4**, 367 (1981)).

CHAPTER 2

PAULING "3-ELECTRON BONDS", 4-ELECTRON 3-CENTRE BONDING, AND THE NEED FOR AN "INCREASED VALENCE" THEORY

2-1 INTRODUCTION

In elementary chemical bonding theory, a rather neglected concept is a type of chemical bond that Pauling¹ has designated as the "3-electron bond". This type of bond is usually represented as $A \cdot \cdot B$ and it involves three electrons distributed amongst two overlapping atomic orbitals centred on the atoms A and B. Alternative designations² are either "3-electron 2-centre" bond or "3-electron 2-orbital" bond.

In 1931, Pauling¹ introduced the "3-electron bond", to help describe the electronic structures for a number of molecules and ions, such as NO , He_2^+ , O_2 , NO_2 and ClO_2 , whose ground-states are paramagnetic at room temperature. Pauling's valence bond structures for these systems are displayed in Fig. 2-1. Until recently, it has always been considered that the occurrence of the "3-electron bond" was restricted to paramagnetic molecules of this type. If we exclude transition metal compounds, there are only a small number of molecular systems whose ground-states are paramagnetic and stable. Therefore, the Pauling "3-electron bond" usually does not feature prominently in discussions on valence theory.

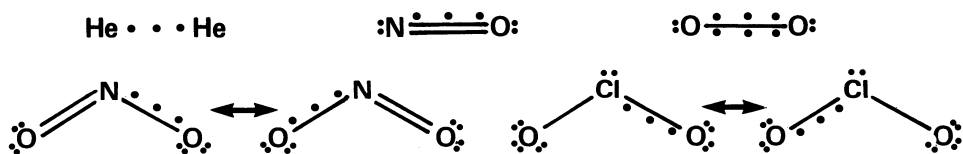


Figure 2-1. Pauling "3-electron bond" valence-bond structures for He_2^+ , NO , O_2 , NO_2 , and ClO_2 .

In this book, we shall demonstrate that, in contrast to what is usually thought the Pauling "3-electron bond" is an extremely useful construct, and that its occurrence is not restricted to paramagnetic molecules. However, to make effective use of the Pauling "3-electron bond" for descriptions of the bonding for diamagnetic molecules, it is necessary to introduce a modification to its representation, namely that proposed by Green and Linnett³ in 1960. For reasons that we shall discuss more fully in Chapter 3, these workers have shown that the $A \cdot \cdot B$ valence-bond structure for the "3-electron bond" is better written as $\overset{\cdot}{A} \cdot \overset{\cdot}{B}$, with one bonding electron and

two electrons (with parallel spins) located in atomic orbitals centred on the A and B nuclei. This modification enables emphasis to be put on Pauling's earlier conclusion that the strength of a "3-electron bond" is approximately equal to that of a 1-electron bond, and that some unpaired-electron charge is associated with each of the two atoms. This unpaired-electron charge is available for (fractional or partial) sharing with unpaired electron charges on other atoms, and it provides the basis for the development of an "increased-valence" theory.

In Chapters 3 - 9, we shall examine the electronic structures of numerous paramagnetic molecules, for which Pauling's "3-electron bonds" may be utilized in their valence-bond structures. Lewis valence-bond descriptions for the dimers of some of these molecules will also be considered. In Chapters 10 - 24, the incorporation of Pauling's "3-electron bonds" into the valence-bond structures for diamagnetic molecules will be described. The resulting valence-bond structures for diamagnetic systems are called "increased-valence" structures to stress the point that they involve more electrons in bonding than do Lewis structures which have electron-pair bonds and lone-pairs of electrons.

The remainder of this chapter provides a discussion of the need for an "increased-valence" theory. A reading of it is not required in order to follow the Pauling "3-electron bond" and Lewis theory of Chapters 3 - 9.

2-2 ELECTRON DEFICIENT AND ELECTRON EXCESS BONDING UNITS

Almost all molecules that involve atoms of main-group elements and an even number of electrons have diamagnetic ground-states. (One important exception to this statement is O_2 , to which we have referred already in Section 2-1.) For these molecules, the familiar Lewis valence-bond structures, with electron-pair bonds and lone-pairs of electrons, are used very often to provide qualitative valence-bond descriptions of their electronic structures. Sometimes, as is the case for H_2 , N_2 , H_2O , C_2H_6 , C_2H_4 and butadiene of Fig. 2-2, one Lewis structure alone can give a fairly adequate description of the bonding. If necessary, bond polarity may be indicated in these structures, either by arrowheads or by fractional net charges δ^+ and δ^- as is shown for H_2O . The bond line represents a pair of shared electrons with opposite spins, the sharing (in orbital theory) arising from atomic orbital overlap. Each lone-pair of electrons also involves two electrons with opposite spins, as is shown for N_2 and H_2O . (The crosses and circles [\times and \circ] represent electrons with s_z spin quantum numbers of $+\frac{1}{2}$ and $-\frac{1}{2}$ respectively). For each of the molecules of Fig. 2-2, the Lewis structure has the maximum number of electron-pair bonds linking pairs of adjacent atoms. Any other Lewis structure for these molecules, such as the "long-bond" and ionic or polar structures displayed for H_2O and butadiene, have fewer covalent bonds between adjacent atoms, but of course they can participate in resonance with the primary valence-bond structure.

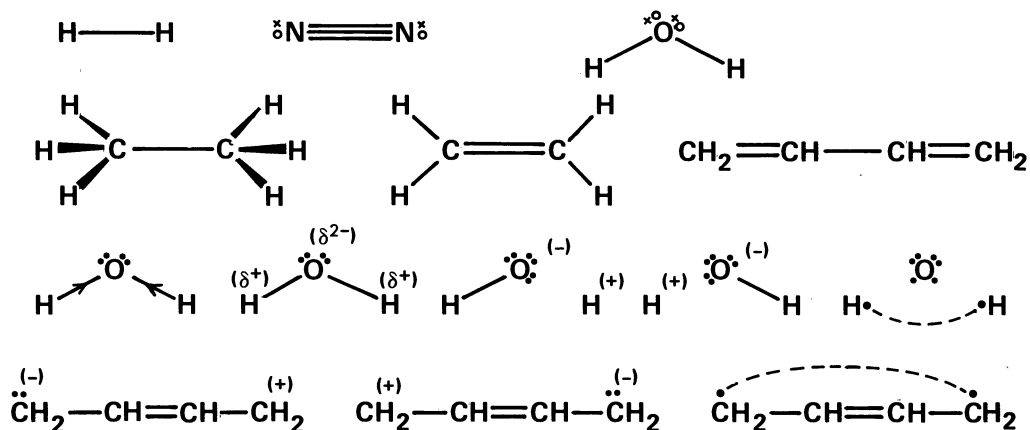


Figure 2-2. Lewis valence-bond structures for H_2 , N_2 , H_2O , C_2H_6 , C_2H_4 and C_4H_6 . "Long-bonds" between pairs of non-adjacent atoms are indicated by pecked bond lines.

Very frequently throughout this book, we shall use the expression "standard valence-bond structure" or "standard Lewis structure", which we define to be a Lewis structure that

- has the maximum number of electron-pair bonds permitted by the rules of valence for a given atomic orbital basis set (e.g. the Lewis-Langmuir octet rule for atoms of first-row elements), and
- locates electron-pair bonds between pairs of adjacent atoms only.

Thus, for butadiene, $\text{CH}_2=\text{CH}-\text{CH}=\text{CH}_2$ is a standard valence-bond structure, whereas the polar and "long-bond" structures $\overset{(+)}{\text{C}}\text{H}_2-\text{CH}=\text{CH}-\overset{(-)}{\text{C}}\text{H}_2$ and

$\overset{(-)}{\text{C}}\text{H}_2-\text{CH}=\text{CH}-\overset{(-)}{\text{C}}\text{H}_2$ are not. Similarly, each of $\text{F}-\overset{(-)}{\text{N}}=\overset{(+)}{\text{O}}$ and $\overset{(-)}{\text{F}}-\overset{(+)}{\text{N}}=\overset{(-)}{\text{O}}$ are standard Lewis structures for FNO, whereas $\overset{(-)}{\text{F}}-\overset{(-)}{\text{N}}=\overset{(+)}{\text{O}}$ and $\overset{(+)}{\text{F}}-\overset{(+)}{\text{N}}=\overset{(-)}{\text{O}}$ are not.

For a large number of molecules, it is possible to write down two or more Lewis structures that have the same number of electron-pair bonds between adjacent atoms. Familiar examples of these molecules (or ions) are C_6H_6 , H_3^+ , B_2H_6 , HF_2^- , O_3 , N_2O , FNO and the Cr-CO linkages of $\text{Cr}(\text{CO})_6$, whose standard Lewis structures (together with those for $\text{Te}(\text{ROCS}_2)_2$)⁴ are displayed in Fig. 2-3. To describe simply the electronic structures of these molecules and ions, it is common practice to invoke resonance between these structures if they are either degenerate (symmetrically equivalent structures such as those displayed for C_6H_6 then contribute equally to the resonance) or considered to have fairly similar energies.

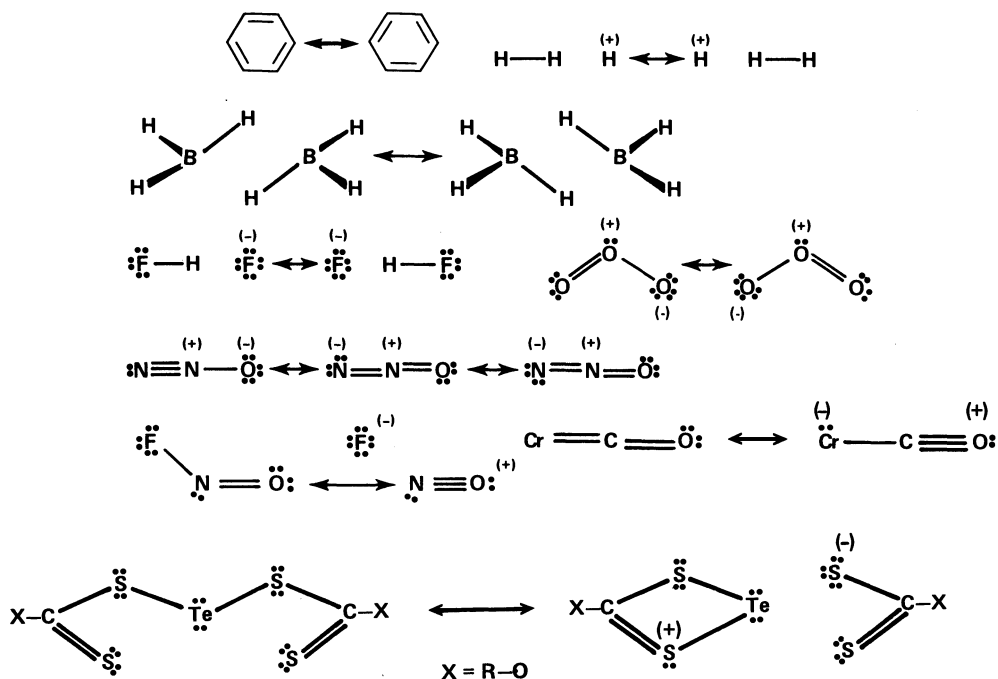
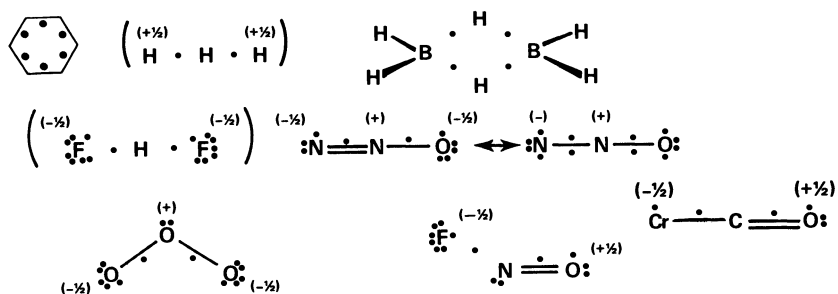


Figure 2-3. Standard Lewis structures for C_6H_6 , and some electron-deficient and electron-excess systems.

It may be noted that instead of invoking resonance between the standard Lewis structures of Fig. 2-3, it is also possible to use the Linnett non-paired spatial structures^{3b,c}, namely



Although the wave-functions for the two types of valence-bond structures are different, these structures provide the same type of qualitative information concerning bond-properties (in particular, bond-lengths). By contrast, the "increased-valence" structures that are the subject of Chapters 10-24 can provide different information than what can be obtained from inspection of the standard Lewis structures.

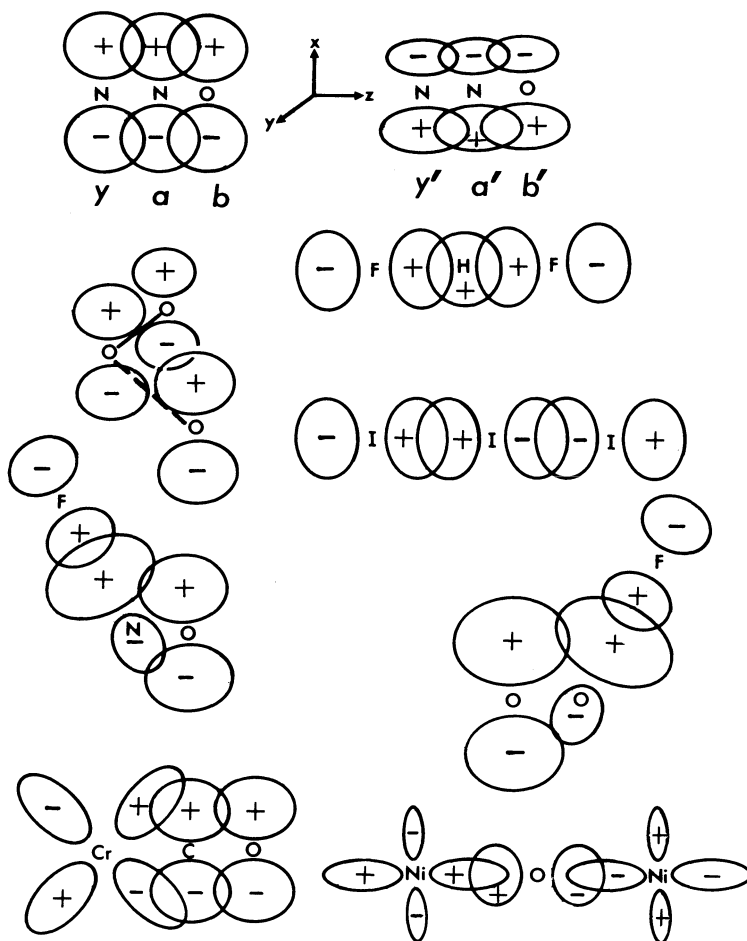
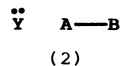
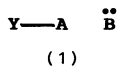


Figure 2-4 Sets of atomic orbitals used for 4-electron 3-centre bonding units for N_2O , O_3 , HF_2^- , I_3^- , FNO , F_2O_2 , Cr-CO linkage for $\text{Cr}(\text{CO})_6$ and Ni-O-Ni linkage for solid NiO.

Molecules and ions such as B_2H_6 and H_3^+ are examples of electron deficient systems, because the number of valence-shell electrons is $< 2(N - 1)$, with N = number of atoms. However, it is with molecules and ions such as N_2O , O_3 , FNO , and HF_2^- that we shall be concerned in Chapters 10 - 24. Each of these latter systems has one or more sets of four electrons distributed amongst three atoms with three overlapping atomic orbitals. The orbitals are shown in Fig. 2-4. In Fig. 2-3, the standard valence-bond arrangements for sets of four electrons that participate in resonance are of the general types (1) and (2), in which **Y**, **A**, and **B** are three atoms with overlapping atomic orbitals *y*, *a*, and *b*. Each of (1) and (2) has an electron

pair-bond and a lone-pair of electrons, and because they have more electrons than overlapping (valence-shell) orbitals, (1) and (2) are examples of standard valence-bond or standard Lewis structures for electron-rich bonding units.



Valence-bond structures of type (1) or (2) can occur as components of Lewis-type structures for a very large number of intra- and inter-molecular systems, i.e. for any system in which a Lewis structure has an atom with a lone-pair of electrons occupying an atomic orbital that overlaps with the orbitals for the electron-pair bond between two adjacent atoms. Resonance between (1) and (2) is then possible; the relative weights for these structures depend on the nature of the particular system. Some intermolecular examples, namely $(\text{H}_2\text{O})_2$, $\text{Me}_3\text{N}\cdots\text{I}_2$, the transition state for the $\text{S}_{\text{N}}2$ reaction $\text{OH}^- + \text{CH}_3\text{Br}$, and an O-Ni-O linkage for solid $\text{Ni}^{2+}\text{O}^{2-}$ are shown in Fig. 2-5. In Chapters 11-14, we shall show that any electron-excess bonding unit of types (1) or (2) can be modified and stabilized by developing a Pauling "3-electron bond" structure as a component of it. The consequences of doing this for elementary valence-bond theory and chemical insight seem to be very considerable.

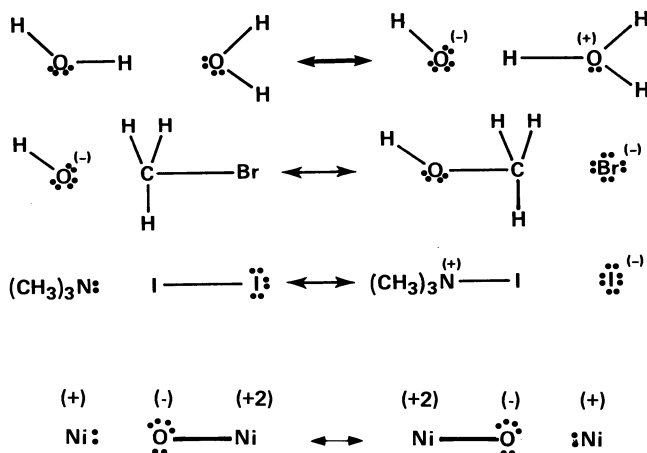
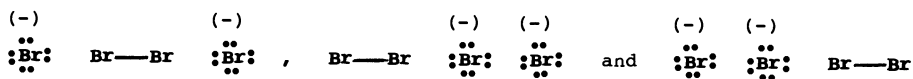
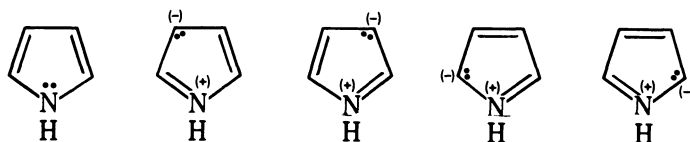


Figure 2-5. Standard Lewis structures for $(\text{H}_2\text{O})_2$, the transition state for the $\text{S}_{\text{N}}2$ reaction of $\text{OH}^- + \text{CH}_3\text{Br}$, the complex $\text{Me}_3\text{N}\cdots\text{I}_2$, and an Ni-O-Ni linkage of solid $\text{Ni}^{2+}\text{O}^{2-}$.

Other types of electron-excess bonding units are also possible. For example, Br_4^{2-} with standard Lewis structures



has a 6-electron 4-centre bonding unit for a set of six electrons distributed amongst the four overlapping $4p_z$ atomic orbitals of Fig. 2-6. A cyclic 6-electron 5-centre bonding unit obtains for the π -electrons of pyrrole (Fig. 2-6), for which the standard Lewis structures are



These longer N -centre bonding units of the general types $\ddot{\text{A}} \text{—} \text{B—C} \ddot{\text{D}}$ and $\text{Y—A} \ddot{\text{B}} \text{—C—D}$ represent elaborations of the 4-electron 3-centre bonding unit that we have described above. They will be introduced again later when it is appropriate to do so.

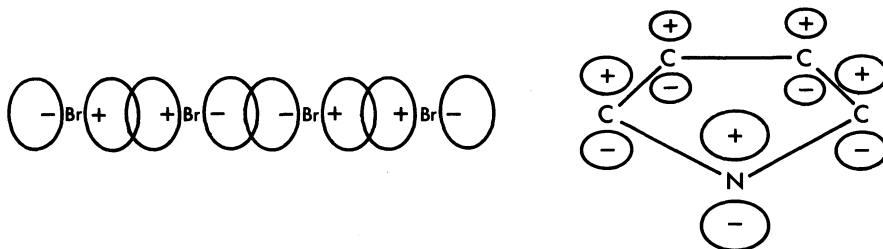
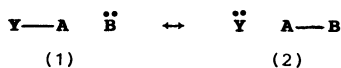


Figure 2-6. Atomic orbitals for two 6-electron 4-centre and 6-electron 5-centre bonding units. (In Fig. 1-5, a 6-electron 4-centre bonding unit of the $\sigma + \pi$ -type is displayed.)

2-3 DELOCALIZED MOLECULAR ORBITAL THEORY FOR 4-ELECTRON 3-CENTRE BONDING UNITS

In Section 2-2, we have indicated that the standard Lewis representation for a 4-electron 3-centre bonding unit involves resonance between valence-bond structures of the general types (1) and (2), i.e.



A delocalized molecular orbital description of 4-electron 3-centre bonding is also very widely used^{5,6}, and we shall describe three examples of the molecular orbital theory here.

y, a, b, y', a', and b' are displayed in Fig. 2-4 and the 3-centre molecular orbitals are the following:

$$\psi_i = c_{i1}y + c_{i2}a + c_{i3}b \quad \text{and} \quad \psi'_i = c_{i1}y' + c_{i2}a' + c_{i3}b' \quad \text{for } i = 1, 2, 3$$

The lowest-energy molecular orbital configuration is $(\psi_1)^2(\psi_2)^2(\psi'_1)^2(\psi'_2)^2$. Because the terminal nitrogen and oxygen atoms are not symmetrically-equivalent, molecular orbitals ψ_2 and ψ'_2 are not necessarily non-bonding orbitals with respect to each pair of adjacent atoms. The molecular orbital valence structure for N_2O now corresponds to that of (4). Sometimes, it is represented as (5), for which each broken line represents a set of four delocalized π -electrons.

Another example of a molecule for which non-symmetrical 4-electron 3-centre bonding units occur is F_2O_2 . This molecule has two important sets of 4-electron 3-centre bonding units, which involve the atomic orbitals of the type displayed in Fig. 2-4 for one FO component. The 3-centre molecular orbitals are also given by Eqn. (2), and the resulting molecular orbital configuration of lowest energy is of the same form as that for N_2O , namely $(\psi_1)^2(\psi_2)^2(\psi'_1)^2(\psi'_2)^2$. The valence structure that corresponds to this configuration is either (6) or (7); these structures are similar to those of (4) and (5) for N_2O . With respect to the O-O bonds, the 3-centre molecular orbitals have respectively $\bar{\pi}$ - and π -character.



The molecular orbital description of 4-electron 3-centre bonding is easy to construct, and the molecular orbital procedure is probably the most suitable to use to calculate the electron distributions in a polyatomic molecule. But, it has the disadvantage that one cannot see *by inspection* what the properties of the individual bonds for many electron-excess molecules should be when they are compared with those for molecules that have essentially localized 2-centre bonds. For example, the N-N and N-O bond-lengths[†] of 1.129 Å and 1.188 Å for N_2O are similar to the triple and double bond^{7,8} lengths of 1.098 Å and 1.214 Å for $:N \equiv N:$ and $CH_3N=O$. But inspection of the molecular orbital valence structures (4) and (5) for N_2O does not make this similarity obvious. For F_2O_2 , the O-O bond-length of 1.217 Å is almost identical⁹ to the double-bond length of 1.207 Å for free O_2 , but neither of the molecular orbital valence structures (6) or (7) gives any hint as to why this is so. The inability to provide much bond-length information *without calculation* is true of all

[†] Unless otherwise stated, all bond-lengths have been taken from reference 7. Differences in operational definitions of bond-lengths (i.e. r_s , r_o , r_g , r_e), and uncertainties in bond-lengths have been ignored.

delocalized molecular orbital descriptions of the bonding for 4-electron 3-centre bonding units.

For qualitative molecular orbital descriptions of the bonding for a large number of triatomic and polyatomic molecules, we refer the reader to Gimarc's recently published text¹⁰.

In order to compare by inspection the bond-properties of related molecules, it is necessary to use valence-bond structures that have *localized* or *two-centre* bonds, i.e. bonds that link together *pairs* of atoms only. In Section 2-4, we shall examine how this is normally done for electron-excess molecules, using N_2O and F_2O as examples again.

2-4 STANDARD VALENCE-BOND THEORY FOR N_2O AND F_2O_2

4(a) The octet rule and the electroneutrality principle The basis of the modern electronic theory of valence was established by Lewis¹¹ in 1916, who suggested that the chemical bond between two similar atoms in a covalent molecule consists of one or more pairs of shared electrons. In 1919, Langmuir¹² elaborated the Lewis theory, and gave the name of *covalent bond* to any bond that arises from electron sharing by two atoms. The concept of an energy stabilization through resonance between two or more Lewis structures was developed by Pauling and Slater in the early 1930's. For references to this period, the reader is referred to Ref. 1(b), p.184.

Lewis also suggested that when carbon, nitrogen, oxygen and fluorine atoms are bonded to other atoms in a molecule, they tend to acquire the electron configuration of the inert gas neon. With a $1s^2 2s^2 2p^6$ ground-state configuration, the neon atom has eight electrons in its valence shell. When they form covalent bonds, atoms of the other elements above acquire this neon configuration, by sharing their unpaired electrons with the unpaired electrons of other atoms. According to Lewis, stable (or low energy) valence-bond structures have eight valence-shell electrons disposed around the atomic kernels (atomic nuclei + inner-shell electrons) for any of these first-row elements. Lewis and Langmuir respectively gave the names of "rule of eight" and "octet rule" to this requirement. One quantum mechanical justification for this rule is provided by the existence of four $n = 2$ atomic orbitals (namely $2s$, $2p_x$, $2p_y$, and $2p_z$), and a maximum occupancy of two electrons per orbital is permitted by the Pauli exclusion principle.

We shall now use the covalent molecule N_2O to consider how the octet rule is usually applied. For this molecule, there are nine Lewis structures (namely (1)-(9) of Fig. 2-8) that have different π -electron distributions, and which satisfy the octet rule. Each of them will contribute to the ground state resonance description of the electronic structure[†]. To provide a simple qualitative discussion of the

[†] Altogether, there are 27 other valence-bond structures that differ in the distributions of the four

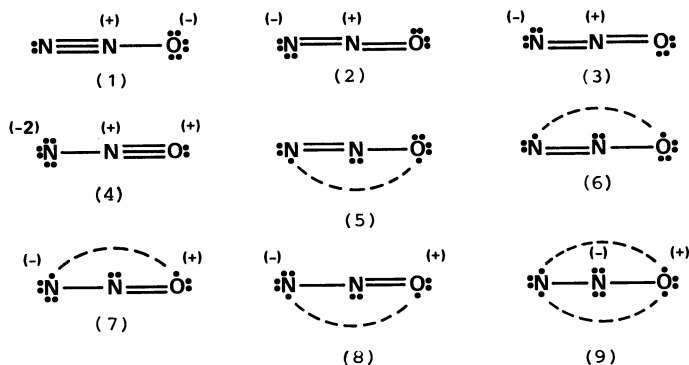


Figure 2-8 Lewis-Langmuir octet structures for N_2O . "Long-bonds" between pairs of non-adjacent atoms are indicated by pecked bond lines.

bonding, it is usual to select out those valence-bond structures that are considered to be the most important, and to make deductions about molecular properties by consideration of them. For N_2O , none of the nine Lewis structures of Fig. 2-8 alone can account for the similarity of the N-N and N-O bond-lengths (1.13 and 1.19 Å) to those of triple and double bonds (1.10 and 1.20 Å - see Section 2-3(b)). It is therefore hoped that resonance between the most stable of these structures (i.e. those of lowest energy) will account for the observation. Two simple rules are usually invoked to help decide which structures these should be. They are:

- For a covalent molecule, the low-energy Lewis structures should be those that have the maximum number of covalent bonds between pairs of adjacent atoms in the molecule.
- The low-energy structures are those whose atomic formal charges are compatible with those that are required by the *electroneutrality principle* for the molecule. This principle states¹⁴ that for a neutral covalent molecule, the atomic formal charges should be essentially zero, and not greater than $+\frac{1}{2}$ or $-\frac{1}{2}$.

The order in which these rules is usually applied is (a) before (b). Thus for N_2O , rule (a) suggests that (1)-(4) should be the most important structures. Each of them has four covalent bonds between pairs of adjacent atoms. Having selected these four structures, rule (b) is then invoked. For structure (4), the atomic

(cont. from previous page) π - and four $\bar{\pi}$ -electrons, and which participate in resonance with the octet structures of Fig. 2-8. These structures have fewer covalent bonds than have the octet structures. Here, we are restricting our attention to a consideration of the octet structures because these are usually the most useful for qualitative discussions of bonding. In Chapter 23, we shall describe how to take account of the non-octet structures when constructing wave-functions. See also Refs. 13a-d.

formal charges (-2, +1, +1) are much larger than they are for any of (1)-(3), namely (0, +1, -1) and (-1, +1, 0). Therefore, (4) should be a rather higher energy structure and its contribution to the ground-state resonance should be much smaller than are those of (1)-(3). The bond properties of N_2O are then discussed in terms of resonance between the standard Lewis structures (1)-(3), and the observed bond-lengths are assumed to be those expected as a consequence of this resonance¹⁵. Thus, if it is assumed that each of these structures has an approximately equal weight, then we would deduce that the N-N and N-O bonds (with bond-numbers[†] of 2.67 and 1.67) have lengths that are longer than triple and double bonds respectively. With respect to the N-N bond, this deduction is valid, but as we have seen, the N-O bond is slightly shorter than the double bond for $CH_3N \equiv O$. No matter how we vary the contributions of (1), (2) and (3) to the resonance, it is not possible to account for both bond-length observations simultaneously. However, very often a "resonance shortening correction" is invoked, which may increase the theoretical N-N and N-O bond-numbers to values closer to 3 and 2 respectively. We do not wish to deny that such corrections may have a valid basis in theory (see for example Ref. 13a), but we would contend that better valence-bond structures may be constructed, which can also rationalize the observations quite satisfactorily. We shall postpone consideration of this matter until Section 2-5(b).

2-4(b) Standard Valence-Bond Theory and F_2O_2 We shall use F_2O_2 to provide a second example that illustrates some unsatisfactory features of the standard Lewis descriptions for many electron-excess systems. In Section 2-3(b) we have indicated that the O-O bond-length⁹ of 1.217 Å for F_2O_2 is similar to the double-bond length of 1.207 Å for the O_2 ground state. The O-F bond-lengths of 1.575 Å are appreciably longer than the 1.42 Å for the O-F single-bonds of F_2O . A set of nine valence-bond structures that conform to the Lewis-Langmuir octet rule is displayed in Fig. 2-9. If rule (a) of Section 2-4(a) is invoked, we would select the standard Lewis structures (1)-(4) to be the important valence-bond structures for the F_2O_2 ground-state. If we then invoke rule (b) (the electroneutrality principle), we would deduce the order of importance for these standard Lewis structures to be (1) > (2) = (3) > (4). If we assume that (1) alone represents the electronic structure of F_2O_2 , then we are unable to account for the observed bond-lengths of this molecule. (By contrast it may be noted that for hydrogen peroxide H_2O_2 , the valence-bond structure which is the same as (1), with H replacing F, is in accord with the observations that O-O and O-H bond-lengths of 1.464 Å and 0.965 Å are essentially those of O-O

[†] Two different bonding indices will be used in this book, namely bond-number and bond-order. The bond number is a valence-bond concept, and it refers to the number of pairs of electrons that form a bond. It may be calculated from the weights of the valence-bond structures that are used to describe the electronic structure of the molecule, as is demonstrated above for N_2O . The bond-order is the molecular orbital index of bonding. For the purpose of qualitative discussion of diatomic bonding, we shall define the bond-order to be

$$\{(\text{No. of bonding electrons}) - (\text{No. of antibonding electrons})\}.$$

More elaborate definitions will be introduced later when necessary.

and O-H single bonds¹⁶.) For F_2O_2 , it is necessary to assume that structures (2) and (3) at least make very appreciable contributions to the ground-state resonance. A justification for this assumption is also provided by electronegativity considerations, which certainly allow fluorine atoms to acquire formal negative charges (as they do in (2) and (3)). If as is sometimes done, we assume that resonance between (2) and (3) alone may be used to describe the electronic structure of F_2O_2 , then we are able to account for the similarity of the O-O bond-length to that of an O-O double-bond, and also for the lengthening of the O-F bonds relative to those of O-F single-bonds. However, such a description ignores the contribution of Lewis structure (1) to the resonance. The absence of formal charges for this structure would suggest that it is also important. If we include (1), together with (2) and (3), then the O-O bond-length would be predicted to be rather longer than a double bond. To restore agreement between theory and experiment, it is then necessary to assume that valence-bond structure (4) (with an O-O triple bond) also contributes to the resonance, and that its weight is equal to that of structure (1). The very different sets of formal charges (and bond-arrangements) would not permit structures (1) and (4) to have similar weights. These considerations suggest that use of the

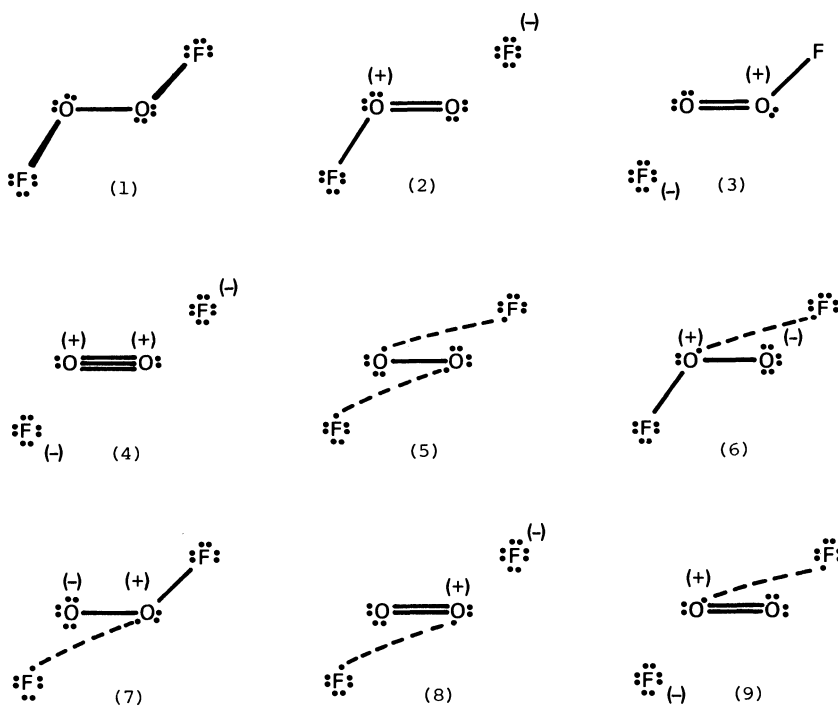


Figure 2-9 Lewis-Langmuir octet structures for F_2O_2 . "Long-bonds" between non-adjacent atoms are indicated by pecked bond lines.

standard Lewis structures (1)-(4) alone does not provide a soundly-based description of the electronic structure for F_2O_2 .

2-5 "LONG-BOND" LEWIS STRUCTURES AND A NEED FOR AN "INCREASED-VALENCE" THEORY

2-5(a) The electroneutrality Principle and "Long-Bond" Valence-Bond Structures For N_2O , let us now suppose that rule (b) of Section 2-4(a) is given precedence over rule (a). Because Lewis structures (5) and (6) of Fig. 2-8 carry zero formal charges on all atoms, we would now choose them to be the most important of the valence-bond structures displayed in the Fig. Each of (5) and (6) has a "long" π or $\bar{\pi}$ bond between the terminal nitrogen and oxygen atoms. The atomic orbitals for these "long" bonds are displayed in Fig. 2-4, namely orbitals y and b for the π -bond, and orbitals y' and b' for the $\bar{\pi}$ -bond. Because y and b are located on non-adjacent atoms, as are y' and b' , their overlap integrals ($S_{yb} \equiv \int yb dv$ etc.), are much smaller than are those that pertain for pairs of atomic orbitals located on adjacent atomic centres. Thus, we have calculated $S_{yb} \equiv S_{y'b'} = 0.01$. For the N-N and N-O π - or $\bar{\pi}$ -bonds of structures (1)-(3), which utilize atomic orbitals on adjacent atoms, the overlap integrals are $S_{ya} \equiv S_{y'a'} = 0.26$, and $S_{ab} \equiv S_{a'b'} = 0.19$. Consequently, if we assume that the magnitude of the overlap integral provides a qualitative guide to the extent of covalent bonding, then there is less covalent bonding for valence-bond structures (5) and (6) than there is for (1)-(4).

It is conceivable that the reduction in covalent bonding that occurs in the "long-bond" structures (5) and (6) may be compensated for either partially or completely by the absence of atomic formal charges. Should this be the case, then consideration of both rules (a) and (b) together on a more equal footing would lead us to conclude that Lewis structures (1), (2) (3), (5) and (6) may all make important contributions to the ground-state resonance description of the electronic structure of N_2O . For F_2O_2 , Lewis structures (1), (2), (3) and (5) of Fig. 2-9 might also be selected as important structures. If we extend these types of considerations to other molecules, then according to the electroneutrality principle, we have no right to assume that "long-bond" Lewis structures make minor contributions to the ground-state resonance description for many molecules. The results for a number of calculations of valence-bond wave-functions^{13,17} indicate that this assumption is especially not valid when the standard Lewis structures (for example, (1)-(4) of Fig. 2-8 for N_2O) carry non-zero atomic formal charges and one or more of the "long-bond" structures do not. More recently, the generalized valence-bond calculations of Goddard and his co-workers¹⁸, and the valence-bond calculations of Hiberty and Le-Forestier¹⁹, provide further support for this conclusion.

Although perhaps it is very much concealed, the bond-eigenfunctions for valence-bond structures with "long bonds" also contribute to the molecular orbital description for 4-electron 3-centre bonding^{13,17}. We shall demonstrate this here for a symmetrical 4-electron 3-centre bonding

unit, with the molecular orbitals of Eqn. (1). These molecular orbitals may be used to express the lowest-energy molecular orbital configuration $(\psi_1)^2 (\psi_2)^2$ as a linear combination of the bond-eigenfunctions for six valence-bond structures, namely^{13c}

$$\begin{aligned}
 (\psi_1)^2 (\psi_2)^2 = & 2k_1 \{ \psi_1 (\text{Y} \text{---} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}) + \psi_2 (\overset{\cdot\cdot}{\text{Y}} \text{---} \overset{\cdot\cdot}{\text{A}} \text{---} \overset{\cdot\cdot}{\text{B}}) \} + k_1^2 \psi_3 (\overset{\cdot\cdot}{\text{Y}} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}) \\
 & + 4\psi_4 (\overset{\cdot\cdot}{\text{Y}} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}) + k_1^2 \{ \psi_5 (\overset{\cdot\cdot}{\text{Y}} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}) + \psi_6 (\text{Y} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}) \}
 \end{aligned}$$

thereby showing that the bond-eigenfunction for the "long-bond" structure $\overset{\cdot\cdot}{\text{Y}} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$ contributes to the linear combination. It may be noted that because this linear combination contains only one parameter (k_1) whose value may be determined so that the total energy is a minimum, the molecular orbital configuration does not represent the "best" (i.e., lowest-energy) linear combination of the six bond-eigenfunctions. For the "best" linear combination, the coefficient for $\psi(\overset{\cdot\cdot}{\text{Y}} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}})$ differs from those for $\psi(\overset{\cdot\cdot}{\text{Y}} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}})$ and $\psi(\text{Y} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}})$ (whereas they are the same in the linear combination above). Thus for O_3 , Gould and Linnett have calculated the "best" linear combination to be^{17a}

$$\Psi(\text{best}) = 0.351(\psi_1 + \psi_2) + 0.390\psi_3 + 0.124\psi_4 + 0.028(\psi_5 + \psi_6)$$

thereby demonstrating the importance of the bond-eigenfunction for the "long-bond" structure with zero formal charges on all atoms. Similar results for O_3 obtained by other workers^{13b,d,19} are reported in Table 2-1.

We therefore suggest that satisfactory qualitative valence-bond descriptions for many molecular systems with 4-electron 3-centre bonding units often require the inclusion of certain "long-bond" structures as well as the standard Lewis structures, all of which obey the Lewis-Langmuir octet rule. Whether or not the weights of the "long-bond" Lewis structures are large, a more-stable (or lower energy) description of the molecular systems must always be obtained by including rather than excluding the "long-bond" structures (provided that the coefficients of the bond-eigenfunctions are chosen so that the total energy of the valence-bond wave-function is minimized).

In the Appendix, a further justification for the inclusion of "long-bond" structures is provided. It is based on consideration of the magnitudes of the H_{ij} matrix elements in the secular equations.

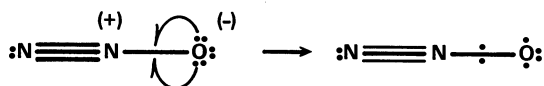
2-5(b) The Need for "Increased-Valence" Structures If a number of "long-bond" Lewis structures are included together with the standard Lewis structures in a qualitative resonance description of electronic structure, the resonance description may become rather cumbersome. We may also lose quick insight into the expected

properties of the bonds. For example, if we include the "long-bond" structures (5) and (6) together with (1), (2) and (3) to represent the ground-state electronic structure for N_2O , we might be led to deduce that the contributions from (5) and (6) would reduce the N-N and (nearest neighbour) N-O bond-numbers below the values of 2.67 and 1.67 obtained from resonance between (1), (2) and (3) (with each of these latter structures contributing equally). However, this need not be the case, because this deduction ignores the effect of resonance on bonding[†]. This suggests

that we require a technique for writing down all of the important Lewis octet structures (both standard and "long-bond") together with some indication of the effect on

bonding of resonance between these valence-bond structures. One technique that we may use to do this involves the incorporation of 1-electron bonds (via the Pauling "3-electron bonds") as well as electron-pair bonds into the valence-bond structures. In Chapters 10-14, we shall describe in some detail how this may be done. Here, we shall only display these types of structures for N_2O and F_2O_2 , and make some obvious comments about them.

In Section 13-1, we shall generate valence-bond structures (I)-(IV) of Figure 2-10 for N_2O , each of which has two 1-electron bonds as well as electron-pair bonds. (As will be demonstrated in more detail in Section 13-1, these structures may easily be generated from the standard Lewis structures (1)-(4) of Fig. 2-8 by delocalizing non-bonding π - and π^- electrons into the adjacent N-O or N-N bond regions; for example



[†] To illustrate this point, we may refer to the valence-bond structures $\overset{\cdot}{\text{H}} \overset{\cdot}{\text{H}}$ and $\overset{\cdot}{\text{H}} \overset{\cdot}{\text{H}}$ for the 1-electron molecule ion H_2^+ . Each of these structures alone does not have a bonding electron. However, resonance between them generates a 1-electron bond, i.e. $\overset{\cdot}{\text{H}} \overset{\cdot}{\text{H}} \leftrightarrow \overset{\cdot}{\text{H}} \overset{\cdot}{\text{H}}$ \equiv $(\text{H} \cdot \text{H})^+$. Orbital theory for this resonance is developed in Section 3-2.

	C_i	C_i	W_i
	0.337	0.308	0.184
	0.337	0.308	0.184
	0.859	0.793	0.593
	0.110	0.0670	0.023
	0.108	0.0674	0.008
	0.108	0.0674	0.008

Table 2-1 Bond-eigenfunction coefficients (C_i)^{13b,d} and weights ($W_i = C_i^2 S_{ii} + \frac{1}{2} \sum_{j \neq i} C_i C_j S_{ij}$)¹⁹ for the O_3 ground-state. (N.B. The C_i in the text are for non-normalized bond-eigenfunctions for Ref. 17a.)

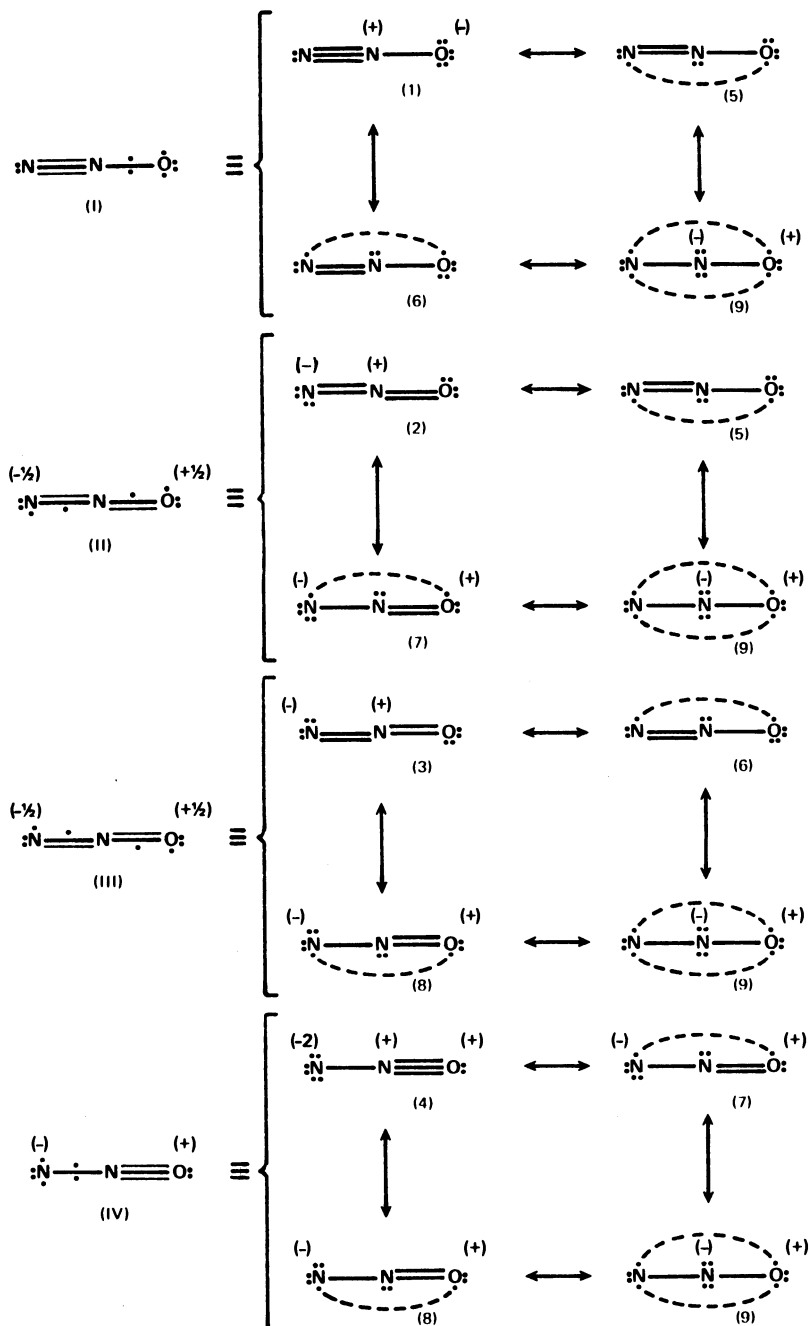


Figure 2-10 "Increased-valence" structures and equivalent Lewis octet structures.

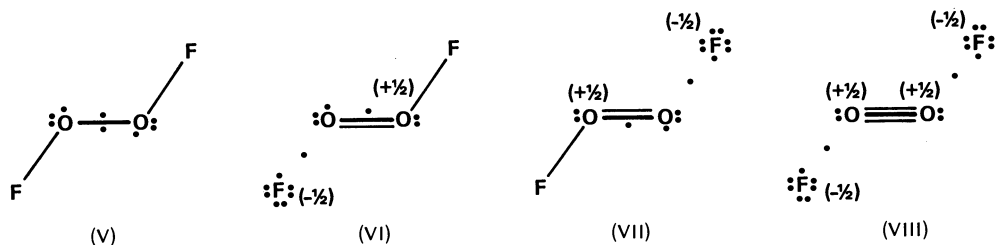
If we use the result that a 1-electron bond between a pair of atoms A and B summarizes resonance between valence-bond structures ($\overset{\bullet}{\text{A}} \text{ B}$) and ($\text{A} \overset{\bullet}{\text{B}}$) (i.e. $\text{A} \bullet \text{B} \equiv (\overset{\bullet}{\text{A}} \text{ B}) \leftrightarrow (\text{A} \overset{\bullet}{\text{B}})$), it is easy to demonstrate that each of (I)-(IV) summarizes resonance between one standard and three "long-bond" Lewis structures of Fig. 2-8. Thus, (I) \equiv (1) \leftrightarrow (5) \leftrightarrow (6) \leftrightarrow (9), (II) \equiv (2) \leftrightarrow (5) \leftrightarrow (7) \leftrightarrow (9), (III) \equiv (3) \leftrightarrow (6) \leftrightarrow (8) \leftrightarrow (9) and (IV) \equiv (4) \leftrightarrow (7) \leftrightarrow (8) \leftrightarrow (9), as is shown in Fig. 2-10. Therefore by invoking resonance between structures (I)-(IV), we are able to summarize resonance between all of the octet structures of Fig. 2-8. It may be noted also that each of (I)-(IV) seems to have two more bonding electrons than has any of the octet structures (1)-(9). Therefore (for reasons that are developed further in Section 11-1) (I)-(IV) are examples of a new class of valence-bond structures, which have been designated as "increased-valence" structures^{13,20}.

For illustrative purposes only, the formal charges for "increased-valence" structures are usually to be assigned on the assumption[†] that bonding electrons are shared equally by pairs of adjacent atoms. If we invoke the electroneutrality principle, then the absence of formal charges for (I) would suggest that this structure is more important than are any of (II), (III) and (IV). By assuming this to be the case, we may conclude that the electronic structure of N_2O more-closely resembles that of (I) than that for any of the other structures. Indeed, if we select (I) alone to represent (approximately) the electronic structures of N_2O , we may deduce that the N-O bond-length should be similar to that of a double bond, and that the N-N bond-length should be longer than that of a triple bond, but still resemble a triple bond. Both of these deductions are in accord with the observations reported in Section 2-4(a). The N-O double-bond character for (I) is implied by the presence of four bonding electrons located in the N-O bond region. Relative to the N-N triple bond of N_2 , the reduction of the N-N bond-number for (I) arises because (I) is equivalent to resonance between Lewis structures (1), (5), (6) and (9) of Fig. 2-8, and only (1) has an N-N triple bond.

In Chapter 11, we shall generate "increased-valence" structure (V) for F_2O_2 , which has two more bonding electrons than have any of the Lewis structures displayed in Fig. 2-9. This "increased-valence" structure accounts for the similarity of the O-O bond-length to that of free O_2 , and the lengthening of the O-F bonds relative to those of O-F single bonds. In (V), there are four O-O bonding electrons as is required for a double bond. It may also be deduced that (V) summarizes resonance

[†] This is the normal procedure that is used to assign formal charges to the atoms of valence-bond structures. The actual atomic formal charges for a molecule are then determined (primarily) by the weights of the different valence-bond structures that participate in resonance. However, because an "increased-valence" structure summarizes resonance between a number of Lewis structures, some of which will have different weights, the "best" set of formal charges for an "increased-valence" structure will in general not be integer or $\frac{1}{2}$ -integer in magnitude. In the absence of knowledge as to what they are, we shall use the same procedure that Linnett³ has used to assign atomic formal charges for his non-paired spatial orbital structures, namely to assume that bonding electrons are shared equally by adjacent atoms of the "increased-valence" structures.

between the standard Lewis structure (1) and the "long-bond" structures (5), (6) and (7) of Fig. 2-9. In each of (5), (6) and (7), the absence of either one or two O-F covalent bonds between a pair of adjacent oxygen and fluorine atoms reduces the O-F bond-numbers for (V) below those of unity for (1).



For F_2O_2 , "increased-valence" structures (VI)-(VIII) may also be constructed, and they may also participate in resonance with (V). The electroneutrality principle would suggest that because (V) carries zero atomic formal charges on all atoms, this structure has the largest weight, i.e. it is the most important of the four "increased-valence" structures. By assuming that this is so, we have been able to account qualitatively for the observed O-O and O-F bond-lengths without giving consideration to the contributions of (VI), (VII) and (VIII) to the resonance.

Inspection of the "increased-valence" structures (I)-(VIII) shows that each of them involves electron distributions of the following types:



We may generalize these structures to write them as $Y \text{---} A \cdot \overset{\cdot}{B}$. All "increased-valence" structures have this type of electron distribution for each set of electrons that is involved in 4-electron 3-centre bonding. As we shall demonstrate further in Chapter 11, we may generate this "increased-valence" electron distribution by bonding a Pauling "3-electron bond" structure $\overset{\cdot}{A} \cdot \overset{\cdot}{B}$ to a third atom $\overset{\cdot}{Y}$ which has an odd-electron. Thus, using the Green and Linnett representation for the Pauling "3-electron bond" (i.e. $\overset{\cdot}{A} \cdot \overset{\cdot}{B}$ rather than $A \cdot \cdot B$ - see Section 2-1), we may write



We are therefore led to conclude that all "increased-valence" structures for 4-electron 3-centre bonding units have Pauling "3-electron bonds" as components of their valence-bond structures. And because the phenomenon of 4-electron 3-centre bonding occurs extremely frequently, it follows that the relevance of Pauling "3-electron bond" and "increased-valence" theory for qualitative descriptions of

chemical bonding is very great. The need for an "increased-valence" theory has also been implied by Bent²¹ in his review on inter- and intra-molecular donor and acceptor complexes.

The discussion above shows that the general "increased-valence" structure $Y-A \cdot \dot{B}$ for 4-electron 3-centre bonding has the following properties. These will be further elaborated in Chapters 11, 12 and 14.

- (a) It summarizes resonance between the standard and "long-bond" Lewis structures $Y-A \ddot{B}$ and $Y \overset{\cdot}{A} \ddot{B}$. Therefore $Y-A \cdot \dot{B}$ is more stable than either of the component structures alone.
- (b) It can be derived either from the standard Lewis structure by delocalizing a non-bonding B electron into the adjacent A-B bond region (i.e. $Y-A \overset{\cdot}{B} + Y-A \cdot \dot{B}$) or by spin-pairing the odd electrons of the Pauling "3-electron bond" structure $\dot{A} \cdot \dot{B}$ and a \dot{Y} atom when the odd-electron orbitals overlap.
- (c) Its $Y-A$ bond is a fractional electron-pair bond, and therefore it is longer and weaker than the normal $Y-A$ electron-pair bond of $Y-A \ddot{B}$.

In Chapters 11, 12 and 14, the following additional properties will also be demonstrated.

- (d) In (b), the odd-electron of $\dot{A} \cdot \dot{B}$ that is spin-paired with that of \dot{Y} occupies an antibonding A-B orbital.
- (e) A total of three electrons may participate in fractional Y-A, Y-B and A-B bonding in $Y-A \cdot \dot{B}$. Each of $Y-A \ddot{B}$ and $Y \overset{\cdot}{A} \ddot{B}$ has two bonding electrons, and therefore the "increased-valence" designation for $Y-A \cdot \dot{B}$ is a consequence of this property.
- (f) The A atom valence for the "increased-valence" structure can exceed the value of unity that exists for the standard Lewis structure $Y-A \ddot{B}$.

For 6-electron 4-centre (and longer *N*-centre) bonding units, similar types of properties exist for most of the "increased-valence" structures. For example, by spin-pairing the odd-electrons of the Pauling "3-electron bond" structures $\dot{A} \cdot \dot{B}$ and $\dot{C} \cdot \dot{D}$, "increased-valence" structure $\dot{A} \cdot \dot{B}-C \cdot \dot{D}$ for 6-electron 4-centre bonding units is obtained. This structure summarizes resonance between $\ddot{A} \ddot{B}-C \ddot{D}$, $\overset{\cdot}{A} \overset{\cdot}{B}-C \overset{\cdot}{D}$ and $\overset{\cdot}{A} \overset{\cdot}{B} \overset{\cdot}{C} \overset{\cdot}{D}$ and may also be generated from the standard Lewis structure by delocalized non-bonding A and D electrons into the A-B and C-D bond regions (i.e. $\overset{\cdot}{A} \overset{\cdot}{B}-C \overset{\cdot}{D}$).

Some of the longer *M*-centre bonding units do not have Pauling "3-electron bonds" as components in their "increased-valence" structures. Thus, for 6-electron 5-centre bonding, no Pauling "3-electron bond" is present in the "increased-valence" structure $Y-A \cdot B \cdot C-D$ which is derived from the standard Lewis structure $Y-A \overset{\cdot\cdot}{B} C-D$ by delocalizing the two non-bonding *B* electrons into the adjacent B-A and B-C bond regions, (i.e. $Y-A \overset{\cdot\cdot}{B} C-D$). However, all "increased-valence" structures for electron-rich molecules summarize resonance between standard and "long-bond" Lewis structures, and therefore they are more stable than the standard Lewis structures from which they are derived.

Other approaches to "increased-valence" are possible for molecules that involve atoms of first-row elements. For example, the valence-bond structure $:\text{N} \equiv \text{N} = \overset{\cdot\cdot}{\text{O}}$ with an apparent valence of five for the central nitrogen atom, is sometimes used to represent the electronic structure of N_2O . In Chapter 16, we shall discuss why this type of structure is less useful for qualitative purposes than are those (such as $:\text{N} \equiv \text{N} - \overset{\cdot\cdot}{\text{O}}:$) that involve one-electron and fractional electron-pair bonds as well as normal electron-pair bonds.

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CHAPTER 3

WAVE-FUNCTIONS AND VALENCE-BOND STRUCTURES FOR 1-ELECTRON BONDS, ELECTRON-PAIR BONDS, PAULING "3-ELECTRON BONDS" AND "NO BONDS"

An elementary survey will be presented here of types of valence-bond structures and simple orbital wave-functions that may be used to describe 1-electron bonds, electron-pair bonds, Pauling "3-electron bonds" and "no-bonds" for diatomic systems.

3-1 DIATOMIC BONDING AND ANTIBONDING MOLECULAR ORBITALS

If A and B are two atoms with overlapping atomic orbitals a and b, whose overlap integral $S_{ab} \equiv \int ab d\tau$ is > 0 , we may construct the bonding and antibonding molecular orbitals $\psi_+ \equiv \psi_{ab} = a + kb$ and $\psi_- \equiv \psi_{ab}^* = k^*a - b$, for which k and k* are constants (both > 0) that are related through the requirement that the two molecular orbitals be orthogonal (i.e. $\int \psi_{ab} \psi_{ab}^* d\tau = 0$ for real orbitals). If the parameters k and k* are chosen so that the energy of ψ_{ab} is a minimum, then the bonding molecular orbital has an energy which is lower than that of the antibonding molecular orbital. For H_2^+ , H_2 , He_2^+ and He_2 , approximate contours for these orbitals, which are constructed from overlapping 1s atomic orbitals, are displayed in Fig. 3-1; the symmetry for

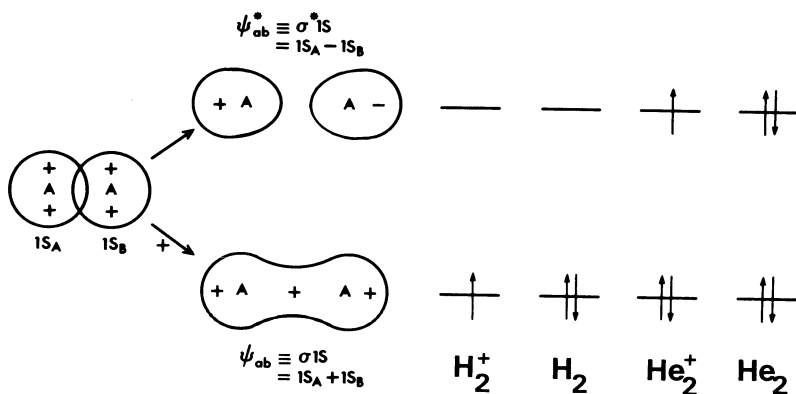


Figure 3-1 $\sigma 1s$ and $\sigma^* 1s$ bonding and antibonding molecular orbitals, and orbital occupations for the ground-state configurations of H_2^+ , H_2 , He_2^+ and He_2 .

each of these systems requires that $k = k^* = 1$. If A and B are non-equivalent atoms (or more particularly a and b are non-equivalent orbitals), then in general $k \neq k^* \neq 1$. The parameter k is then either > 1 or < 1 according to whether B is more or less electronegative than A with respect to the electron(s) that occupy the molecular orbital.

For the special case that a and b are equivalent atomic orbitals (i.e. $k = k^* = 1$), the energies for molecular orbitals ψ_{ab} and ψ_{ab}^* may be expressed according to Eqs. (1) and (2) if the atomic orbitals are normalized (i.e. $\int a^2 dv = \int b^2 dv = 1$). The α and β are the coulomb and resonance integrals defined according to Eqs. (3) and (4); \hat{H} is the Hamiltonian operator for an electron.

$$\epsilon_+ = (\alpha + \beta)/(1 + S_{ab}) \quad (1)$$

$$\epsilon_- = (\alpha - \beta)/(1 - S_{ab}) \quad (2)$$

$$\alpha \equiv \int a \hat{H} a dv \equiv \int b \hat{H} b dv \quad (3)$$

$$\beta \equiv \int a \hat{H} b dv \equiv \int b \hat{H} a dv \quad (4)$$

When $S_{ab} > 0$, it may be deduced that $\beta < 0$ and that $\epsilon_- > \epsilon_+$, i.e. that $\beta - S_{ab}\alpha < 0$.

3-2 ONE-ELECTRON BONDS

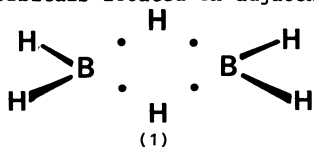
For the 1-electron bond of the valence-bond structure $\mathbf{A} \bullet \mathbf{B}$, we may use the bonding molecular orbital $\psi_{ab} = a + kb$ to accommodate the electron. This orbital wave-function shows immediately that $\mathbf{A} \bullet \mathbf{B}$ summarizes resonance between the valence-bond structures $(\overset{\bullet}{\mathbf{A}} \quad \mathbf{B})$ and $(\mathbf{A} \quad \overset{\bullet}{\mathbf{B}})$ whose wave-functions are the atomic orbitals a and b respectively, i.e. we may write



$$\psi_{ab} = a + kb \equiv \quad a \quad + \quad kb$$

The hydrogen molecule ion H_2^+ is the simplest molecular system with a 1-electron bond; its molecular orbital wave-function and corresponding valence-bond structures are $\psi_{ab} = 1s_A + 1s_B \equiv \sigma 1s$ and $(\mathbf{H} \bullet \mathbf{H})^+ \equiv (\overset{\bullet}{\mathbf{H}} \quad \mathbf{H}^+) \leftrightarrow (\mathbf{H}^+ \quad \overset{\bullet}{\mathbf{H}})$. In the Linnett valence-bond structures (1) and (2) for B_2H_6 and C_6H_6 , the bridging B-H bonds and the C-C π -bonds are 1-electron bonds¹. For each of these bonds, the a and

b atomic orbitals are a pair of boron sp^3 and hydrogen $1s$ orbitals, and a pair of $2p\pi$ -orbitals located on adjacent carbon atoms.



For H_2^+ , the bonding molecular orbital $\sigma 1s = 1s_A + 1s_B$ has the energy given by Eqn.(1). If no overlap occurs between the atomic orbitals, then β as well as S_{ab} equals zero. The energy for $\sigma 1s$ is then equal to α . The energy difference between α and $(\alpha + \beta)/(1 + S_{ab})$ namely $(\beta - S_{ab}\alpha)/(1 + S_{ab})$ is referred to as the "constructive interference energy"² and corresponds to the drop in energy that occurs for H_2^+ when the atomic orbitals overlap. (This energy is also equal to the resonance stabilization energy). An analysis of the kinetic and potential energy contributions to this energy²⁻⁵ shows that the kinetic energy is reduced appreciably and the potential energy rises slightly when the atomic orbitals overlap, i.e. the stabilization of the $\sigma 1s$ bonding molecular orbital relative to a $1s$ atomic orbital is due to a net drop in kinetic energy when overlap occurs.

3-3 ELECTRON-PAIR BONDS

For the electron-pair bond of the valence-bond structure $A \text{---} B$, two simple types of wave-functions may be used to describe the electron configuration.

- (i) *Molecular orbital*: The Pauli exclusion principle allows any orbital to have a maximum occupancy of two electrons. Consequently the two electrons of the $A \text{---} B$ bond may both occupy the bonding molecular orbital $\psi_{ab} = a + kb$. Therefore, the lowest-energy molecular orbital configuration is $\psi_{ab}(1)\psi_{ab}(2) \equiv (\psi_{ab})^2$. For H_2 , a and b are the $1s$ atomic orbitals and $k = 1$. The resulting molecular orbital configuration is $\sigma 1s(1)\sigma 1s(2) \equiv (\sigma 1s)^2$ with $\sigma 1s = 1s_A + 1s_B$.
- (ii) *Heitler-London valence-bond*: Instead of forming the 2-electron wave-function as a product of 1-electron molecular orbitals, we may also construct products of the singly-occupied overlapping atomic orbitals a and b . The resulting 2-electron wave-functions, $a(1)b(2)$ and $b(1)a(2)$ differ only in the labelling (1 or 2) of the electrons, and are equally-acceptable wave-functions. The linear combinations $a(1)b(2) \pm b(1)a(2)$ may therefore be constructed. The lower-energy

linear combination is $a(1)b(2) + b(1)a(2)$, and this is the Heitler-London (valence-bond) wave-function for the electron-pair covalent bond A—B . For H_2 , this wave-function is written as $1s_{\text{A}}(1)1s_{\text{B}}(2) + 1s_{\text{B}}(1)1s_{\text{A}}(2)$ with a normalization constant of $1/(2 + 2S_{\text{ab}}^2)^{1/2}$.

For either of the above wave functions, the Pauli exclusion principle requires that the two electrons have opposite spins (Section 3-4), i.e. the total spin quantum number (S) = 0. If we use crosses and circles (\times and \circ) to represent electrons with s_z spin quantum numbers of $+1/2$ and $-1/2$ (or α and β spin wave-functions), then we may write

$$\text{A—B} \equiv \text{A} \begin{array}{c} \times \\ \circ \end{array} \text{B} \quad \text{for } \Psi(\text{MO}) = \psi_{\text{ab}}(1)\psi_{\text{ab}}(2) \quad (5)$$

$$\text{and } \text{A—B} \equiv \begin{array}{c} \times \\ \circ \end{array} \text{A} \quad \leftrightarrow \quad \begin{array}{c} \circ \\ \times \end{array} \text{B} \quad \text{for } \Psi(\text{HLVB}) = a(1)b(2) + b(1)a(2) \quad (6)$$

For H_2 , both the molecular orbital and the Heitler-London wave-functions give appreciable electronic dissociation energies (D_e), namely 2.69 eV and 3.16 eV respectively, when hydrogen-atom 1s atomic orbitals ($\exp(-\zeta r)$ with $\zeta = 1$) are used in the energy calculations. If the orbital exponent ζ is chosen so that the total energy is minimized, these dissociation energies increase to 3.49 eV and 3.78 eV. The exact dissociation energy is $D_e = 4.75$ eV.

To improve further the molecular orbital wave-function, we may invoke "configuration interaction" (C.I.), i.e. linearly combine the bonding configuration $\psi_{\text{ab}}(1)\psi_{\text{ab}}(2)$ with the antibonding configuration $\psi_{\text{ab}}^*(1)\psi_{\text{ab}}^*(2)$. To improve the Heitler-London valence-bond function, we may invoke "covalent-ionic" resonance. This involves linearly combining the covalent wave-function $a(1)b(2) + b(1)a(2)$ with the wave-functions $a(1)a(2)$ and $b(1)b(2)$ for the ionic valence-bond structures $\text{A}^+ \text{B}^-$ and $\text{A}^- \text{B}^+$. For H_2 , the appropriate ionic wave-function is $1s_{\text{A}}(1)1s_{\text{A}}(2) + 1s_{\text{B}}(1)1s_{\text{B}}(2)$ with both ionic structures $\text{H}^+ \text{H}^-$ and $\text{H}^- \text{H}^+$ contributing equally to the resonance. Alternatively we may replace the a and b atomic orbitals of the Heitler-London wave-function with the semi-localized orbitals $a + \kappa b$ and $b + \kappa'a$ in which κ and κ' are parameters. If the parameters that arise in each of these three "improved" wave-functions are chosen so that the total energy for each wave-function is minimized, it can be shown that the three wave-functions are equivalent and will generate the same dissociation energy.

For H_2 , the three improved wave-functions of the previous paragraph are given by Eqs. (7)-(9) with $a = 1s_{\text{A}}$ and $b = 1s_{\text{B}}$. Equality is obtained when $\lambda = (1 + \kappa)/(1 - \kappa) = 2\kappa/(1 + \kappa^2)$.

$$\Psi(\text{MO,CI}) = \{a(1) + b(1)\}\{a(2) + b(2)\} + \kappa\{a(1) - b(1)\}\{a(2) - b(2)\} \quad (7)$$

$$\Psi(\text{VB,resonance}) = a(1)b(2) + b(1)a(2) + \lambda\{a(1)a(2) + b(1)b(2)\} \quad (8)$$

$$\Psi(\text{VB, semi-localized}) = \{a(1) + \kappa b(1)\}\{b(2) + \kappa a(2)\} + \{b(1) + \kappa a(1)\}\{a(2) + \kappa b(2)\} \quad (9)$$

In Table 3-1, we report the results of calculations of the dissociation energy for H_2 , which use the above types of orbital wave-functions for H_2 . Because $|\lambda|$ for Eqn. (8) is calculated to be $\ll 1$ (for example, 0.105 or 0.265), the primary component for the H_2 ground-state wave-function must be the Heitler-London wave-function.

wave-function	parameters	D_e (eV)	R_e (a_0)
$\{1s_A(1) + 1s_B(1)\}\{1s_A(2) + 1s_B(2)\}$	$\zeta = 1.0$	2.695	1.61
"	$\zeta = 1.197$	3.488	1.38
$1s_A(1)1s_B(2) + 1s_B(1)1s_A(2)$	$\zeta = 1.0$	3.156	1.64
"	$\zeta = 1.166$	3.782	1.41
$\phi_A(1)\phi_B + \phi_B(1)\phi_A(2)$ $\phi = 1s + \mu 2p_z$	$\zeta_{1s} = \zeta_{2p} = 1.19$ $\mu = 0.105$	4.04	1.416
$1s_A(1)1s_B(2) + 1s_B(1)1s_A(2)$	$\zeta = 1$	3.230	1.67
$+ \lambda\{1s_A(1)1s_A(2) + 1s_B(1)1s_B(2)\}$	$\lambda = 0.105$		
"	$\zeta = 1.194$ $\lambda = 0.265$	4.025	1.43
$\phi_A(1)\phi_B(2) + \phi_B(1)\phi_A(2)$	$\zeta = 1.190$	4.122	1.41
$+ \lambda\{1s_A(1)1s_A(2) + 1s_B(1)1s_B(2)\}$	$\lambda = 0.175$ $\mu = 0.07$		
experimental		4.74759	1.4006

Table 3-1 Simple wave-functions, dissociation energies and equilibrium internuclear distances for H_2 ground-state. (Adapted from Table 5-12 of "Atoms and Molecules", by M. Karplus and R.N. Porter, (Benjamin, N.Y., 1970).)

3-4 SPIN WAVE-FUNCTIONS FOR ONE-ELECTRON AND TWO-ELECTRON SYSTEMS

In Section 1-2, we have referred to the s and s_z spin quantum numbers for two electrons. For $s_z = +1/2$ and $s_z = -1/2$, the spin wave-functions are designated as α and β respectively. A *spin-orbital* involves the product of a spatial orbital (e.g. ψ_{ab} for the H_2^+ ground-state) with one of these spin wave-functions. Thus for the electron of the H_2^+ ground-state, we may write down two spin-orbitals, namely $\psi_{ab}(1)\alpha(1)$ and $\psi_{ab}(1)\beta(1)$. In the absence of a magnetic field, these spin-orbitals are degenerate.

The 2-electron spin wave-functions are $\alpha(1)\alpha(2)$, $\beta(1)\beta(2)$, $\{\alpha(1)\beta(2) + \beta(1)\alpha(2)\}/2^{1/2}$ and $\{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2}$. They have S_z ($\equiv s_z(1) + s_z(2)$) spin quantum numbers of +1, -1, 0 and 0 respectively. Their total spin quantum numbers may be shown to have values of $S = 1, 1, 1$ and 0. For $S = 1$, the electron spin orientations are parallel (i.e. $\uparrow\uparrow$) whereas they are antiparallel or opposed (i.e. $\uparrow\downarrow$) for $S = 0$ (see Figure 1-3). Each of the three $S = 1$ wave-functions is symmetric with respect to the interchange of the electrons, whereas the $S = 0$ wave-function is antisymmetric (i.e. changes sign) with respect to electron interchange. The Pauli exclusion principle requires that symmetric spatial wave-functions be associated with the antisymmetric spin wave-function, and vice versa. Each of the **A—B** bond wave-functions of Eqs. (5)-(9) is symmetric with respect to the interchange of electrons. Therefore they must be associated with the antisymmetric spin wave-function $\{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2}$ for which the electron spins are antiparallel. Thus we may write

$$\psi_{ab}(1)\psi_{ab}(2) \times \{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2} \quad (10)$$

and $\{a(1)b(2) + b(1)a(2)\} \times \{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2} \quad (11)$

as the total wave-functions for the molecular orbital and Heitler-London approximations to the $S = 0$ ground-state.

The symmetric $S = 1$ spin wave-functions must be associated with antisymmetric spatial wave-functions. The latter wave-functions may be written down using either the bonding and antibonding molecular orbitals or atomic orbitals, as is indicated in Eqs. (12) and (13) (together with the spin wave-functions).

$$\{\psi_{ab}(1)\psi_{ab}^*(2) - \psi_{ab}^*(1)\psi_{ab}(2)\} \times \begin{cases} \alpha(1)\alpha(2) \\ \{\alpha(1)\beta(2) + \beta(1)\alpha(2)\}/2^{1/2} \\ \beta(1)\beta(2) \end{cases} \quad (12)$$

$$\{a(1)b(2) - b(1)a(2)\} \times \begin{cases} \alpha(1)\alpha(2) \\ \{\alpha(1)\beta(2) + \beta(1)\alpha(2)\}/2^{1/2} \\ \beta(1)\beta(2) \end{cases} \quad (13)$$

For these excited-state wave-functions, the two electrons have parallel spins. An $S = 0$ excited state wave-function, with antiparallel spins for the two electrons is given by Eqn. (14).

$$\{\psi_{ab}(1)\psi_{ab}^*(2) + \psi_{ab}^*(1)\psi_{ab}(2)\} \times \{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2} \quad (14)$$

Further consideration of the electronic structures of excited states is provided in Chapter 9.

3-5 AN IMPORTANT THEOREM

We shall now deduce that, except for the presence of a multiplicative constant, the two $S = 1$ wave-functions of Eqs. (12) and (13) are entirely equivalent^{6,7}. This identity will be used often in the following sections, and indeed much of the theory of this book is based on it.

Initially we shall assume that the parameters k and k^* both equal unity in the bonding and antibonding molecular orbitals ψ_{ab} and ψ_{ab}^* of Eqn. (12). If we then substitute $\psi_{ab} = a + b$ and $\psi_{ab}^* = a - b$ into Eqn. (12) and multiply out the atomic orbital terms, we obtain Eqn. (15), thereby demonstrating the equivalence between Eqs. (12) and (13). (For convenience only, we have omitted the spin wave-functions.) In Section 3-7, this result and also those of Section 3-6 will be deduced from the properties of Slater determinantal wave-functions.

$$\psi_{ab}(1)\psi_{ab}^*(2) - \psi_{ab}^*(1)\psi_{ab}(2) = -2\{a(1)b(2) - b(1)a(2)\} \quad (15)$$

When the ψ_{ab} and ψ_{ab}^* are normalized to give $\psi_{ab} = (a + b)/(2 + 2S_{ab})^{1/2}$ and $\psi_{ab}^* = (a - b)/(2 - 2S_{ab})^{1/2}$, the multiplicative constant of -2 in Eqn. (15) is replaced by $(1 - S_{ab}^2)^{1/2}$. For the general orthogonal orbitals $\psi_{ab} = a + kb$ and $\psi_{ab}^* = k^*a - b$, we obtain the identity of Eqn. (16).

$$\psi_{ab}(1)\psi_{ab}^*(2) - \psi_{ab}^*(1)\psi_{ab}(2) = -(1 + kk^*)\{a(1)b(2) - b(1)a(2)\} \quad (16)$$

We may therefore conclude that, with respect to orbital occupancy for a diatomic system,

one antibonding electron + one bonding electron	\equiv two "non-bonding" electrons	(17)
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provided that the two electrons have parallel spins[†] and the molecular orbitals are constructed from the same set of atomic orbitals. The non-bonding property of the R.H.S. of the identity arises because the a and b electrons have parallel spins. With respect to energy, this configuration is net antibonding when the overlap integral is included in the normalization constants for the molecular orbitals; this is because ψ_{ab}^* is more antibonding than ψ_{ab} is bonding relative to the component atomic orbitals (see, for example, Eqs. (1) and (2)).

[†] If the two electrons have antiparallel spins, then the spatial wave-function of Eqn. (14) for one bonding + one antibonding electron is equivalent to $(k^* - 1)\{a(1)b(2) + b(1)a(2)\} + 2\{k^*a(1)a(2) - kb(1)b(2)\}$.

3-6 THE PAULING "3-ELECTRON BOND"

In 1931, Pauling⁸ introduced the "3-electron bond" structure $A \cdot \cdot B$ as a way to summarize resonance between the Lewis valence-bond structures $A : \cdot B$ and $A \cdot : B$, i.e., he wrote $A \cdot \cdot B \equiv A : \cdot B \leftrightarrow A \cdot : B$.

In Fig. 3-2, the 1s atomic orbital occupations for $A : \cdot B$ and $A \cdot : B$ are displayed for the helium molecule ion, He_2^+ . Because each of these valence-bond

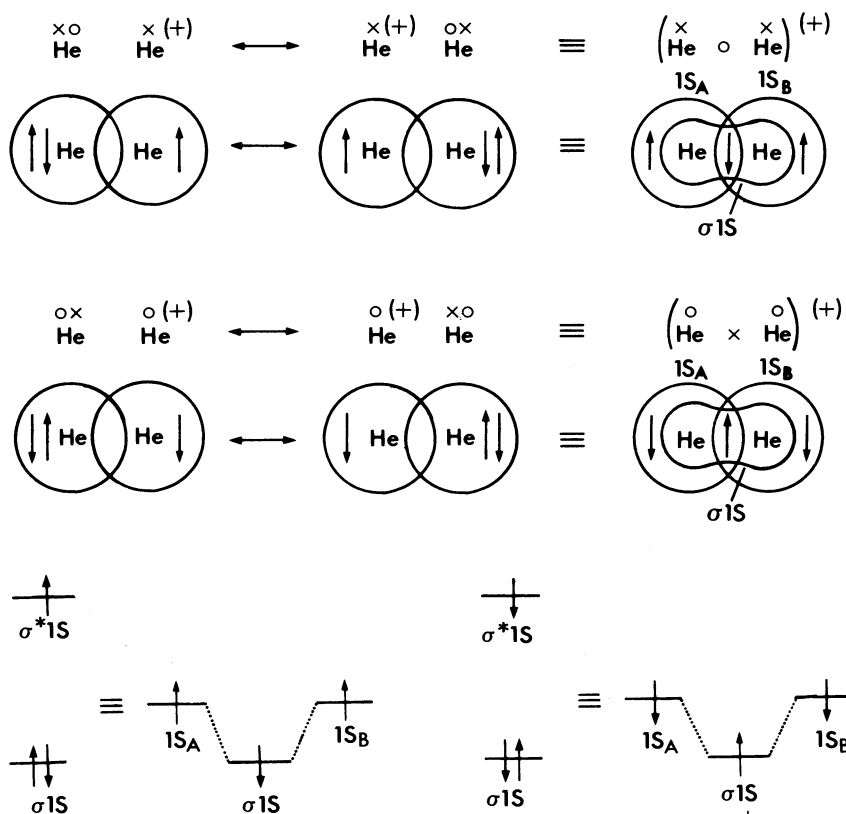
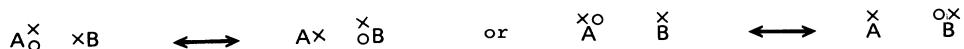


Figure 3-2 Orbital occupations and electron spins for Pauling "3-electron bonds".

structures has only one unpaired electron, Pauling deduced that the length and strength of a "3-electron bond" should be approximately equal to that of a 1-electron bond. If we indicate the spins of the electrons, as in



then it is obvious that there can only be one bonding electron, because two electrons with the same spin cannot form a bond.

For the three electrons of the Pauling "3-electron bond", a molecular orbital description may also be constructed using the bonding and antibonding molecular orbitals $\psi_{ab} = a + kb$ and $\psi_{ab}^* = ka - b$. The Pauli exclusion principle allows only a maximum of two electrons with opposite spins to occupy any orbital. Therefore for the three electrons of the valence-bond structure $\mathbf{A} \cdot \cdot \mathbf{B}$, the molecular orbital configuration involves two bonding electrons + one antibonding electron. This configuration may be written as $(\psi_{ab})^2(\psi_{ab}^*)^1$. For this configuration, the contribution to bonding by one of the two bonding electrons is cancelled by that of the antibonding electron; for two electrons with parallel spins, 1 bonding electron + 1 antibonding electron \equiv 2 non-bonding electrons according to Eqn. (17), or $(\psi_{ab})^1(\psi_{ab}^*)^1 \equiv (a)^1(b)^1$ in which a and b are the atomic orbitals from which ψ_{ab} and ψ_{ab}^* are constructed. Therefore for the molecular orbital configuration $(\psi_{ab})^2(\psi_{ab}^*)^1$, we may write[†]

$$(\psi_{ab})^2(\psi_{ab}^*)^1 \equiv (\psi_{ab})^1(a)^1(b)^1 \equiv (a + kb)^1(a)^1(b)^1 \equiv (a)^2(b)^1 + k(a)^1(b)^2 \quad (18)$$

thereby demonstrating that resonance between the valence-bond structures $\overset{\cdot\cdot}{\mathbf{A}} \overset{\cdot}{\mathbf{B}}$ and $\overset{\cdot}{\mathbf{A}} \overset{\cdot\cdot}{\mathbf{B}}$ (with atomic orbital configurations $(a)^2(b)^1$ and $(a)^1(b)^2$) is involved, just as it is for the Pauling "3-electron bond" structure $\mathbf{A} \cdot \cdot \mathbf{B}$. Because the configuration $(\psi_{ab})^1(a)^1(b)^1$ involves only one bonding electron (namely, the electron that occupies ψ_{ab}), and two non-bonding electrons, Green and Linnett⁹ in 1960 modified the "3-electron bond" valence-bond structure and wrote it as $\overset{\cdot}{\mathbf{A}} \cdot \overset{\cdot}{\mathbf{B}}$ (or $\cdot \mathbf{A} \cdot \mathbf{B} \cdot$), which indicates quite clearly that the Pauling "3-electron bond" involves only one A-B bonding electron. Further, because the a and b electrons of this structure are non-bonding electrons with parallel spins, the spin of the bonding ψ_{ab} electron must be opposite to those of the a and b electrons. (This follows because only one of the ψ_{ab} electrons of $(\psi_{ab})^2(\psi_{ab}^*)^1$ can have the same spin as that of ψ_{ab}^* .) Therefore, the electron spins of $\overset{\cdot}{\mathbf{A}} \cdot \overset{\cdot}{\mathbf{B}}$ may be those of either $\overset{\times}{\mathbf{A}} \overset{\times}{\mathbf{B}}$ or $\overset{\circ}{\mathbf{A}} \times \overset{\circ}{\mathbf{B}}$, according to whether the antibonding ψ_{ab}^* electron has a +1/2 or -1/2 (s_z) spin quantum number. In Fig. 3-2, the orbitals and electron spin assignments are displayed for these latter valence-bond structures.

The above considerations show that the Green and Linnett structure $\overset{\cdot}{\mathbf{A}} \cdot \overset{\cdot}{\mathbf{B}}$, with one bonding and two non-bonding electrons, provides a "better and clearer diagrammatic representation of the electron distribution"¹⁰ than does the Pauling structure $\mathbf{A} \cdot \cdot \mathbf{B}$, and therefore we shall use the $\overset{\cdot}{\mathbf{A}} \cdot \overset{\cdot}{\mathbf{B}}$ representation in the remainder of this book. However, (perhaps misleadingly), we shall continue to refer to this valence-bond structure as a Pauling "3-electron bond" structure.

[†] Our concern here is with orbital occupancies, and therefore this equivalence is appropriate whether or not atomic orbital overlap integrals are included in the normalization constants for the molecular orbitals. See Section 3-10 for a discussion on the inclusion of overlap integrals on the energies of Pauling "3-electron bonds".

3-7 SLATER DETERMINANTS AND THE PAULING "3-ELECTRON BOND"

Although it is not required for a reading of much of this book, it is useful here to elaborate further the discussion of the Pauli exclusion principle in order to formalize the derivation of the identity $(\psi_{ab})^2(\psi_{ab}^*)^1 \equiv (\psi_{ab})^1(a)^1(b)^1$ for the Pauling "3-electron bond". This is done by utilizing Slater determinants to represent antisymmetrized-product wave-functions. We shall do this initially for some 2-electron wave-functions for H_2 .

The Pauli exclusion principle (Section 3-4) requires that the total wave-function for an N -electron system be antisymmetric with respect to the interchange of the coordinates of any two electrons, i.e.,

$$\Psi(1,2,3,\dots,i,j,\dots) = -\Psi(1,2,3,\dots,j,i,\dots) \quad (19)$$

For a two-electron atom or molecule, the total wave-function may be written as the product of a spatial wave-function with a spin wave-function, i.e.

$$\Psi(1,2) = \Psi(1,2)^{\text{space}} \times \Psi(1,2)^{\text{spin}} \quad (20)$$

For the ground-state of H_2 , antisymmetrized product wave-functions are given by Eqs. (21) and (22) (cf. Eqs. (10) and (11), with $\psi_{ab} \equiv \sigma 1s = s_A + s_B$ and $a \equiv 1s_A \equiv s_A$ etc.)

$$\Psi(\text{MO}) = \sigma 1s(1)\sigma 1s(2)\{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2} \quad (21)$$

$$\Psi(\text{HLVB}) = \{s_A(1)s_B(2) + s_B(1)s_A(2)\}\{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2} \quad (22)$$

These wave-functions may be expressed in determinantal form. Thus $\Psi(\text{MO})$ of Eqn. (21) may be written as Eqn. (23), which is an example of the *Slater determinant* representation for an antisymmetrized product wave-function. By indicating only the two terms of the leading diagonal, this determinant may be abbreviated to Eqn. (24). Sometimes, the presence or absence of a bar over the spatial orbital indicates that the electron has a β or α spin wave-function.

$$\Psi(\text{MO}) = \frac{1}{\sqrt{2}} \begin{vmatrix} \sigma 1s(1)\alpha(1) & \sigma 1s(2)\alpha(2) \\ \sigma 1s(1)\beta(1) & \sigma 1s(2)\beta(2) \end{vmatrix} \quad (23)$$

$$\equiv |\sigma 1s(1)\alpha(1)\sigma 1s(2)\beta(2)| \equiv |\sigma 1s^\alpha \sigma 1s^\beta| \equiv |\sigma 1s\overline{\sigma 1s}| \quad (24)$$

It is easy to verify that the Heitler-London valence-bond wave-function of Eqn. (22) may be expressed as a sum of two Slater determinants according to Eqn. (25).

$$\Psi(\text{HLVB}) = |s_A^\alpha s_B^\beta| + |s_B^\alpha s_A^\beta| \quad (25)$$

One important property of a determinant is that it changes sign if two rows or columns are interchanged. Therefore

$$|\sigma_1 s^\alpha \sigma_1 s^\beta| = - |\sigma_1 s^\beta \sigma_1 s^\alpha| \quad (26)$$

and

$$|s_A^\alpha s_B^\beta| + |s_B^\alpha s_A^\beta| = |s_A^\alpha s_B^\beta| - |s_A^\beta s_B^\alpha| \quad (27)$$

The identity of Eqn. (15) that exists between the $S = 1$ configurations of Eqs. (12) and (13) may be written in terms of Slater determinants according to Eqn. (28).

$$\begin{aligned} |\psi_{ab}^\alpha \psi_{ab}^{*\alpha}| &\equiv -2 |a^\alpha b^\alpha| \\ |\psi_{ab}^\alpha \psi_{ab}^{*\beta}| - |\psi_{ab}^{*\alpha} \psi_{ab}^\beta| &\equiv -2 (|a^\alpha b^\beta| - |b^\alpha a^\beta|) \\ |\psi_{ab}^\beta \psi_{ab}^{*\beta}| &\equiv -2 |a^\beta b^\beta| \end{aligned} \quad (28)$$

Except for the possible introduction of a multiplicative constant, a determinant is unaltered by adding and subtracting multiples of rows or columns. For example

$$\begin{vmatrix} a & d \\ c & b \end{vmatrix} = -\frac{1}{25} \begin{vmatrix} a + 6d & 4a - d \\ c + 6b & 4c - b \end{vmatrix}$$

Therefore, for two electrons with parallel spins, the identity of Eqn. (29) pertains, for which the identities of Eqn. (28) are particular examples.

$$|\psi_1^\alpha \psi_2^\alpha| = - (1 + k k^*)^{-1} |(\psi_1 + k \psi_2)^\alpha (k^* \psi_1 - \psi_2)^\alpha| \quad (29)$$

Because a determinant has the value of zero if any two rows or columns have identical elements, the Slater determinant form of the antisymmetrized product wave-function indicates immediately that two electrons with parallel spins cannot occupy the same orbital. Thus $|\sigma_1 s^\alpha \sigma_1 s^\alpha| = 0$ and $|s_A^\alpha s_A^\alpha| = 0$.

For a three-electron system, it is not possible to factor out the spatial wave-function from the spin wave-function, as has been done in Eqs. (21) and (22) for a two-electron system. However, an antisymmetric total wave-function may still

be generated by constructing a Slater determinant. To demonstrate this, we shall construct such a wave-function for the $(\sigma 1s)^2(\sigma^* 1s)^1 \equiv (\sigma)^2(\sigma^*)^1$ ground-state configuration of He_2^+ (Section 3-6). If we assume that the antibonding $\sigma^* 1s$ electron has spin wave-function β , the He_2^+ wave-function may be written in Slater determinant form as:

$$|\sigma^\alpha \sigma^\beta \sigma^{*\beta}| \equiv \frac{1}{\sqrt{3!}} \begin{vmatrix} \sigma(1)\alpha(1) & \sigma(1)\beta(1) & \sigma^*(1)\beta(1) \\ \sigma(2)\alpha(2) & \sigma(2)\beta(2) & \sigma^*(2)\beta(2) \\ \sigma(3)\alpha(3) & \sigma(3)\beta(3) & \sigma^*(3)\beta(3) \end{vmatrix} \quad (30)$$

On expansion of this determinant, we obtain a linear combination of six functions, namely that of Eqn. (31). By interchanging the coordinates of any two electrons, this linear combination may be shown to be antisymmetric with respect to the interchange of two electrons, and therefore it obeys the Pauli principle.

$$\begin{aligned} |\sigma^\alpha \sigma^\beta \sigma^{*\beta}| &= [\sigma(1)\alpha(1) \{ \sigma(2)\beta(2)\sigma^*(3)\beta(3) - \sigma(3)\beta(3)\sigma^*(2)\beta(2) \} \\ &+ \sigma(2)\alpha(2) \{ \sigma(3)\beta(3)\sigma^*(1)\beta(1) - \sigma(1)\beta(1)\sigma^*(3)\beta(3) \} \\ &+ \sigma(3)\alpha(3) \{ \sigma(1)\beta(1)\sigma^*(2)\beta(2) - \sigma(2)\beta(2)\sigma^*(1)\beta(1) \}] / \sqrt{3!} \quad (31) \end{aligned}$$

$$\begin{aligned} &\equiv \{ \sigma(1)\alpha(1) |\sigma(2)\beta(2)\sigma^*(3)\beta(3)| + \sigma(2)\alpha(2) |\sigma(3)\beta(3)\sigma^*(1)\beta(1)| \\ &+ \sigma(3)\alpha(3) |\sigma(1)\beta(1)\sigma^*(2)\beta(2)| \} / \sqrt{3!} \quad (32) \end{aligned}$$

For each of the three 2×2 Slater determinants of Eqn. (32), the identity of Eqn.(28) pertains i.e. $|\sigma^\beta \sigma^{*\beta}| = -2|s_A^\beta s_B^\beta|$. Therefore, an equivalent expression for the Slater determinant of Eqn. (30) is that of Eqn. (33). If the odd-electron of He_2^+ has spin wave-function α , then the identity of Eqn. (34) is appropriate.

$$|\sigma^\alpha \sigma^\beta \sigma^{*\beta}| = -2|\sigma s_A^\beta s_B^\beta| = 2|s_A^\beta \sigma s_B^\beta| \quad (33)$$

$$|\sigma^\alpha \sigma^\beta \sigma^{*\alpha}| = -|\sigma s_A^\alpha s_B^\alpha| = 2|s_A^\alpha \sigma s_B^\alpha| = -2|s_A^\alpha \sigma^\beta s_B^\alpha| \quad (34)$$

The identities of Eqs. (33) and (34) provide a more complete statement that, except for the presence of a multiplicative constant, the wave-function for two bonding electrons + one antibonding electron is equivalent to the wave-function for two electrons occupying separate atomic orbitals with parallel spins + one bonding electron occupying a bonding molecular orbital with opposite spin. We shall make use of this result on numerous occasions.

This theory is easily extended to the general heteronuclear system AB with overlapping atomic orbitals a and b. If AB is a three-electron system, with two bonding electrons and one antibonding electron that occupy the orthogonal molecular orbitals $\psi_{ab} = a + kb$ and $\psi_{ab}^* = k^*a - b$, then by application of Eqn. (29) it may be deduced that

$$|\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{*\alpha}| = - (1 + kk^*) |a^\alpha \psi_{ab}^\beta b^\alpha| \quad \begin{matrix} \times \\ \text{A} \end{matrix} \circ \begin{matrix} \times \\ \text{B} \end{matrix} \quad (35)$$

$$|\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{*\beta}| = - (1 + kk^*) |\psi_{ab}^\alpha a^\beta b^\beta| \quad \begin{matrix} \circ \\ \text{A} \end{matrix} \times \begin{matrix} \circ \\ \text{B} \end{matrix} \quad (36)$$

thereby generating the Pauling "3-electron bond" structure $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$. The constants k and k^* may be related through the requirement that ψ_{ab} and ψ_{ab}^* be orthogonal. (If a and b are real normalized atomic orbitals, with overlap integral S_{ab} , then the orthogonality relationship is $(k^* - k) + (kk^* - 1)S_{ab} = 0$). We note that if we neglect S_{ab} , then $k^* = k$. If AB is homopolar, then $k = 1 = k^*$, as is the case for He_2^+ .

In Chapters 15 and 23, Slater determinants will be used to construct wave-functions for 4-electron 3-centre, 6-electron 4-centre and larger N -centre bonding units.

3-8 "NO BONDS"

If we add another electron to the molecular orbital configuration $(\psi_{ab})^2(\psi_{ab}^*)^1$, we obtain the four-electron configuration $(\psi_{ab})^2(\psi_{ab}^*)^2$. It is then easy to show that with respect to orbital occupations, 2 bonding electrons + 2 antibonding electrons are equivalent to 4 non-bonding electrons, i.e., $(\psi_{ab})^2(\psi_{ab}^*)^2 \equiv (a)^2(b)^2$, and therefore no bond can be formed between atoms A and B for this four-electron configuration. The valence-bond structure for the four electrons is that for two atoms, each carrying a pair of non-bonding or lone-pair electrons with their electron spins opposed, i.e., $\overset{\times}{\text{A}} \overset{\times}{\text{B}} \equiv \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$ or $\overset{\times}{\text{O}}\text{A} \overset{\times}{\text{O}}\text{B} \equiv \text{:A} \text{B:}$.

3-9 VALENCE-BOND STRUCTURES AND BOND PROPERTIES FOR H_2^+ , H_2 , He_2^+ AND He_2

The four simplest molecular system with valence-bond structures of the type $\text{A} \cdot \text{B}$, $\text{A} \text{---} \text{B}$, $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ and $\overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$ for their ground state are H_2^+ , H_2 , He_2^+ and He_2 . For each of these systems, we may use the 1s atomic orbitals to construct the bonding σ 1s and antibonding σ^* 1s molecular orbitals of Fig. 3-1. The resulting molecular orbital configurations for the ground-states are reported in Table 3-2, together with their valence-bond structures. From the molecular orbital

configurations, we may calculate the bond-orders for these four systems using the formula

$$n = (\text{No. of bonding electrons} - \text{No. of antibonding electrons})/2.$$

The bond-orders are reported in the Table, together with the dissociation energies (D_e) and bond-lengths (R_e). Inspection of the valence-bond structures shows that the number of bonding electrons in each of them reflects the trends found for the molecular properties.

			n	D_e	R_e
H_2^+	$(\sigma 1s)^1$	$(\text{H} \cdot \text{H})^+$	1/2	2.79	1.06
H_2	$(\sigma 1s)^2$	$\text{H} : \text{H}$	1	4.75	0.75
He_2^+	$(\sigma 1s)^2(\sigma^* 1s)^1$	$(\overset{\cdot}{\text{He}} \cdot \overset{\cdot}{\text{He}})^+$	1/2	2.60	1.08
He_2	$(\sigma 1s)^2(\sigma^* 1s)^2$	$\overset{\cdot\cdot}{\text{He}} \overset{\cdot\cdot}{\text{He}}$	0	0	∞

Table 3-2 Molecular orbital configurations, valence-bond structures, bond-orders, dissociation energies (eV; 1 eV = 96.4 kJ mol⁻¹) and bond-lengths (\AA , 1 \AA = 10⁻¹⁰ m) for H_2^+ , H_2 , He_2^+ and He_2 .

3-10 INCLUSION OF OVERLAP INTEGRALS IN NORMALIZATION CONSTANTS FOR MOLECULAR ORBITALS; NON-BONDED REPULSIONS

In Section 3-5, we have indicated that inclusion of the overlap integral S_{ab} in the normalization constants for the bonding and antibonding orbitals of Eqn. (37) leads to a greater destabilization for ψ_{ab}^* than stabilization for ψ_{ab} . The energies for these molecular orbitals are given by Eqs. (1) and (2), in which the coulomb and resonance integrals α and β are defined in Section 3-2 with $\beta < 0$ when $S_{ab} > 0$.

$$\psi_{ab} = (a + b)/(2 + 2S_{ab})^{1/2}, \quad \psi_{ab}^* = (a - b)/(2 - 2S_{ab})^{1/2} \quad (37)$$

When electrostatic interactions between the electrons are neglected, the total electronic energies for the Pauling "3-electron bond" and the "no-bond" configurations $(\psi_{ab})^2(\psi_{ab}^*)^1$ and $(\psi_{ab})^2(\psi_{ab}^*)^2$ are given by Eqs. (38) and (39). From them it may be deduced that, relative to the energies of 3α and 4α when $S_{ab} = 0$ at the same internuclear separation, $(\psi_{ab})^2(\psi_{ab}^*)^1$ is antibonding^{11-13†} if $S_{ab} > 1/3$ and $(\psi_{ab})^2(\psi_{ab}^*)^2$ is antibonding¹⁴ if $S_{ab} > 0$. The latter result also pertains when

† Because the Pauling "3-electron bond" structure $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ is equivalent to $\overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}} \leftrightarrow \overset{\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}} \cdot \leftrightarrow \overset{\cdot\cdot}{\text{A}} \overset{\cdot}{\text{B}}$, $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ is stabilized relative to either of the component structures when the same internuclear separation and atomic orbital overlap are appropriate for each of the three structures. Using the molecular orbitals of Eqn. (37) to construct the $(\psi_{ab})^2(\psi_{ab}^*)^1$ configuration for $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$, it may be deduced¹⁶ that the resonance stabilization energy ($E(\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}) - E(\overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}})$) is given by $(\beta - S_{ab}\alpha)/(1 + S_{ab})$. This energy is formally identical to the constructive interference energy for H_2^+ (Section 3-2).

electrostatic interactions between the electrons are explicitly included in the energy calculation¹⁵ - at least for He₂ and Ne₂.

$$2\epsilon_+ + \epsilon_- = \{(3 - S_{ab})\alpha + (1 - 3S_{ab})\beta\}/(1 - S_{ab}^2) \quad (38)$$

$$2\epsilon_+ + 2\epsilon_- = 4(\alpha - S_{ab}\beta)/(1 - S_{ab}^2) \quad (39)$$

The net antibonding character of $(\psi_{ab})^2(\psi_{ab}^*)^2 \equiv (a)^2(b)^2/(1 - S_{ab}^2)$ implies that destabilizing interactions exist when two lone-pair orbitals overlap. Thus, when two helium atoms in their ground-states approach each other, a repulsive potential is established at moderate internuclear separations¹⁵. The trans geometry of N₂H₄ and the non-planarity of H₂O₂ in their ground-states may also be partially ascribed to non-bonded repulsions between the lone-pair electrons; for a pair of non-bonding orbitals on different atomic centres, these geometries reduce the magnitude of the overlap integral S_{ab} , thereby decreasing the magnitude of the net antibonding destabilization.

Consideration of the electronic structure and geometry of the first excited (triplet-spin) state of ethylene provides an illustration of non-bonded repulsions between singly-occupied overlapping orbitals. Ethylene has two π -electrons that occupy a bonding molecular orbital in the lowest-energy configuration. If one of these electrons is excited into the antibonding π orbital, then $(\pi_{CC})^1(\pi_{CC}^*)^1$ configurations are obtained with parallel and antiparallel spins for the two electrons. Hund's rule of maximum spin multiplicity requires that the parallel spin state ($S = 1$) has lower energy. The resulting spatial wave-function is given by Eqn. (40), which is equivalent to Eqn. (41) (with a and b = carbon 2p π atomic orbitals). This $(\pi_{CC})^1(\pi_{CC}^*)^1$ configuration is net antibonding. Overlap repulsive interactions between the singly-occupied a and b orbitals of Eqn. (41) are reduced if these orbitals are rotated relative to each other around the C-C bond-axis. A non-planar $S = 1$ excited state is thus obtained.

$$\{\pi_{CC}(1)\pi_{CC}^*(2) - \pi_{CC}^*(1)\pi_{CC}(2)\}/2^{1/2} \quad (40)$$

$$\equiv \{a(1)b(2) - b(1)a(2)\}/\{2(1 - S_{ab}^2)\}^{1/2} \quad (41)$$

Examples of Pauling "3-electron bond" destabilizations are described in Refs. 11-13, 17 and 18. One of them is concerned with the structures of CH_{3-X}X radicals, with X = NH₂, OH or F. The ground-state of the CH₃ radical is nearly planar. On replacement of the H-atoms with the X-substituents, increasing pyramidalization is either predicted or observed to occur. The development of a Pauling "3-electron bond" $\overset{\cdot}{C}-\overset{\cdot}{X}$ involves two competitive overlap effects, namely a tendency for stabilization of planar CH₂-X when the overlap is small, and a tendency for stabilization of non-planar CH₂-X when the overlap is large. The magnitude of the

overlap integral becomes important in order to ascertain which of these predominates.

3-11 BOND-ORDERS

When overlap integrals are omitted from normalization constants for and orthogonality relationships between molecular orbitals, then the bonding and antibonding molecular orbitals of Eqn. (42) are normalized and orthogonal. (The atomic orbitals a and b are assumed to be normalized.) For each of the $(\psi_{ab})^1$, $(\psi_{ab})^2$, $(\psi_{ab})^2(\psi_{ab}^*)^1$ and $(\psi_{ab})^2(\psi_{ab}^*)^2$ configurations, the atomic orbital charges P_{aa} and P_{bb} , and the A-B bond-order P_{ab} are then easily calculated from Eqs. (42) and (43), in which c_{ia} and c_{ib} are the atomic orbital coefficients and n_i is the occupation number for the i^{th} molecular orbital¹⁹. The resulting charges and bond-orders are reported in Table 3-3.

$$\psi_{ab} = (a + kb)/(1 + k^2)^{1/2}, \psi_{ab}^* = (ka - b)/(1 + k^2)^{1/2} \quad (42)$$

$$P_{aa} = \sum_i n_i c_{ia}^2, P_{bb} = \sum_i n_i c_{ib}^2, P_{ab} = \sum_i n_i c_{ia} c_{ib} \quad (43)$$

	P_{aa}	P_{bb}	P_{ab}
$(\psi_{ab})^1$	$1/(1 + k^2)$	$k^2/(1 + k^2)$	$k/(1 + k^2)$
$(\psi_{ab})^2$	$2/(1 + k^2)$	$2k^2/(1 + k^2)$	$2k/(1 + k^2)$
$(\psi_{ab})^2(\psi_{ab}^*)^1$	$1 + 1/(1 + k^2)$	$1 + k^2/(1 + k^2)$	$k/(1 + k^2)$
$(\psi_{ab})^2(\psi_{ab}^*)^2$	2	2	0

Table 3-3 Atomic orbital charges and bond orders for $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$, $\overset{\cdot}{\text{A}} \text{---} \overset{\cdot}{\text{B}}$, $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ and $\overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$.

For the Pauling "3-electron bond" ($\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}} \equiv \overset{\cdot\cdot}{\text{A}} \overset{\cdot}{\text{B}} \leftrightarrow \overset{\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$), we may write $(\psi_{ab})^2(\psi_{ab}^*)^1 \equiv (a)^1(\psi_{ab})^1(b)^1 \equiv \{(a)^2(b)^1 + k(a)^1(b)^2\}/(1 + k^2)^{1/2}$, from which it may be deduced that the weights for the component structures $\overset{\cdot\cdot}{\text{A}} \overset{\cdot}{\text{B}}$ and $\overset{\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$ are $1/(1 + k^2)$ and $k^2/(1 + k^2)$. These weights correspond²⁰ to the odd-electron charges for the b and a atomic orbitals of $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$, which arise from single occupancy of the antibonding ψ_{ab}^* orbital in $(\psi_{ab})^2(\psi_{ab}^*)^1$. This result will be required in Section 14-3.

More elaborate definitions of atomic orbital charges, bond-orders and valence-bond weights are needed if atomic orbital overlap integrals are included in normalization constants and orthogonality relationships. These are not required for the considerations of this book.

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CHAPTER 4

VALENCE-BOND STRUCTURES FOR SOME DIATOMIC MOLECULES

4-1 MOLECULAR ORBITAL CONFIGURATIONS FOR HOMONUCLEAR DIATOMIC MOLECULES

We shall now generate valence-bond structures for some diatomic molecules and ions that involve atoms of first-row and second-row elements. To do this we shall use their molecular orbital configurations together with the prototype valence-bond structures of Table 3-2. Green and Linnett¹ were the first workers to adopt this approach to the construction of valence-bond structures, and they have described many of the valence-bond structures that we shall generate here. We shall restrict our attention to the molecular orbitals that are constructed from the valence-shell 2s and 2p or 3s and 3p atomic orbitals, and for simplicity in the molecular orbital notation, neglect any hybridization that may occur between s and p ($\equiv p_z$) atomic orbitals. In Figs. 4-1 and 4-2 we display schematic contours for the molecular orbitals that may be constructed from 2p atomic orbitals, and the $n = 2$ molecular orbital energy levels for homonuclear diatomic molecules. To construct the ground-state molecular orbital configuration, we feed the electrons into the lowest-energy molecular orbitals and restrict the maximum orbital occupancy to two electrons. If only two electrons are to be allocated to a pair of degenerate molecular orbitals (for example, the antibonding π_x^* and π_y^* molecular orbitals of O_2), then the lowest-energy arrangement for these electrons occurs when each orbital is singly occupied

with parallel spins for the two electrons. In Table 4-1, we have listed the valence-shell molecular orbital configurations for the ground states of a number of homonuclear diatomic

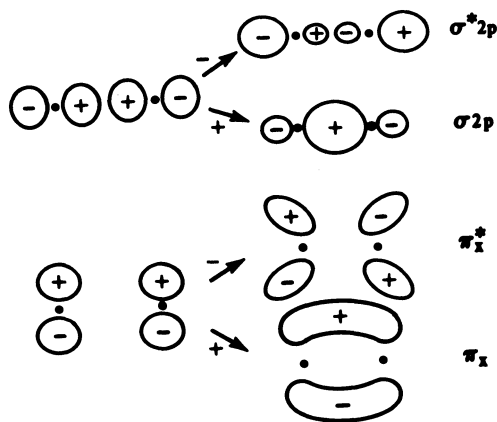


Figure 4-1 Schematic contours for σ_{2p} , σ^*_{2p} , π_x and π_x^* molecular orbitals.

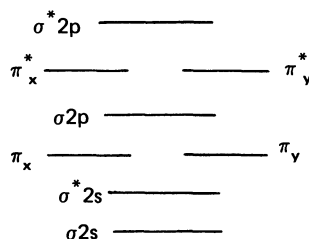


Figure 4-2 Energy levels for $n = 2$ homonuclear molecular orbitals.

systems that are formed from atoms of first-row elements, the molecular orbital bond-order (Section 3-9), and the resulting valence-bond structure.

4-2 Li_2 , Be_2 , N_2 , F_2 AND O_2^{2-}

For Li_2 and Be_2 , the molecular orbital configurations of Table 4-1 generate the valence-bond structures Li—Li and $:\text{Be} \quad \text{Be}:$, which have one and no covalent bonds, respectively. In contrast to what is the case for Li_2 , the diatomic molecule Be_2 does not exist as a stable species. For N_2 and F_2 , we obtain the Lewis octet structures (namely $:\text{N}\equiv\text{N}:$ and $:\text{F}\text{—}\text{F}:$) from the molecular orbital configurations. These structures have triple and single bonds respectively. The peroxide anion O_2^{2-} is isoelectronic with F_2 , and its valence-bond structure $:\overset{(-)}{\text{O}}\text{—}\overset{(-)}{\text{O}}:$ also involves a single bond. The bond-lengths[†] for F_2 and O_2^{2-} are 1.43 and 1.48 Å - both of which are appreciably longer than the 1.10 Å for the triple-bonded N_2 . These lengths for the single-bonds of F_2 and O_2^{2-} are also much shorter than the 2.67 Å for the single-bond of Li_2 . No doubt this reflects (at least partially) the different nature of the atomic orbitals that are used to form the bonds, namely (primarily) 2s for Li_2 and 2pσ for F_2 and O_2^{2-} .

	σ_{2s}	σ^*_{2s}	π_x	π_y	σ_{2p}	π_x^*	π_y^*	σ^*_{2p}	n	
Li_2	2								1	Li—Li
Be_2	2	2							0	$:\text{Be} \quad \text{Be}:$
B_2	2	2	1	1					1	$:\text{B} \begin{matrix} \times \\ \times \end{matrix} \text{B}:$
C_2	2	2	2	2					2	$:\text{C}\equiv\text{C}:$
N_2	2	2	2	2	2				3	$:\text{N}\equiv\text{N}:$
O_2	2	2	2	2	2	1	1		2	$:\overset{\times}{\underset{\times}{\text{O}}}\text{—}\overset{\times}{\underset{\times}{\text{O}}}: $
O_2^*	2	2	2	2	2	2			2	$:\ddot{\text{O}}\equiv\ddot{\text{O}}:$
$\text{O}_2^{2-}, \text{F}_2$	2	2	2	2	2	2	2		1	$:\overset{(-)}{\ddot{\text{O}}}\text{—}\overset{(-)}{\ddot{\text{O}}}: , :\ddot{\text{F}}\text{—}\ddot{\text{F}}:$
O_2^+	2	2	2	2	2	1			2.5	$:\overset{(+\frac{1}{2})}{\times}\overset{\circ}{\text{O}}\equiv\overset{(+\frac{1}{2})}{\times}\overset{\circ}{\text{O}}:$
O_2^-	2	2	2	2	2	2	1		1.5	$:\overset{(-\frac{1}{2})}{\times}\overset{\circ}{\text{O}}\text{—}\overset{(-\frac{1}{2})}{\times}\overset{\circ}{\text{O}}:$

Table 4-1 Molecular orbital configurations and valence-bond structures for diatomic molecule ground-states, and an O_2 excited state (O_2^*). (For O_2^* , O_2^+ and O_2^- , degenerate configurations are not reported here. See also Fig. 4-3).

[†] Bond-lengths for diatomic species are taken from Ref. 2.

4-3 O_2 , O_2^+ , O_2^- AND O_2^{2-}

Molecular oxygen has 12 valence-shell electrons. The ground-state molecular orbital configuration involves single occupancy for the degenerate π_x^* and π_y^* antibonding molecular orbitals, with parallel spins for the two electrons as is shown in Fig. 4-3. The resulting valence-bond structure of Table 4-1, (namely $\overset{\times}{\underset{\times}{\text{O}}} \div \overset{\times}{\underset{\times}{\text{O}}}$, or $\overset{\times}{\underset{\times}{\text{O}}} \overset{\times}{\underset{\times}{\text{O}}}$ if the two antibonding π -electrons have $s_z = +\frac{1}{2}$ quantum numbers), has a double bond which consists of an electron pair σ -bond + two Pauling "3-electron π -bonds". This type of valence-bond structures shows more clearly than does the Pauling structure of Figure 2-1, (namely $\text{:O} \equiv \text{O:}$), that the double bond of O_2 involves only four bonding electrons.

The O-O bond-length of 1.207 Å for the O_2 ground-state is similar to the standard N-O and C-O double-bond lengths of 1.21 Å for each of $\text{CH}_3\text{N}=\text{O}$ and $\text{H}_2\text{C}=\text{O}$, and intermediate between the single and triple bond-lengths of 1.43 Å and 1.10 Å for F_2 and N_2 .

In Table 4-1, the valence-bond structures for O_2^+ , O_2 , O_2^- and O_2^{2-} have $2\frac{1}{2}$, 2, $1\frac{1}{2}$ and 1 covalent bonds respectively, which reflect the trend observed for the bond-lengths, namely 1.12, 1.21, 1.30 and 1.49 Å. The molecular orbital configuration and valence-bond structure are also reported in Table 4-1 for an O_2 excited state in which one of the antibonding π^* molecular orbitals is doubly-occupied and the other is vacant. The valence-bond structure for this state, namely $\overset{\circ}{\text{O}} \equiv \overset{\circ}{\text{O}}$, involves a standard double bond, i.e., electron pair σ - and π -bonds. Its bond-length of 1.22 Å is slightly longer than that of the ground-state. The paramagnetism of the ground-states for O_2 , O_2^- and O_2^+ , which is a consequence of the presence of unpaired spins (i.e. $S = 1$ or $\frac{1}{2}$), is implied by the nature of the electron spins in their valence-bond structures.

In Fig. 4-3, the molecular orbital occupancies that arise from the presence of two antibonding π^* electrons are displayed, together with a more complete formulation of the wave-functions for these two electrons.

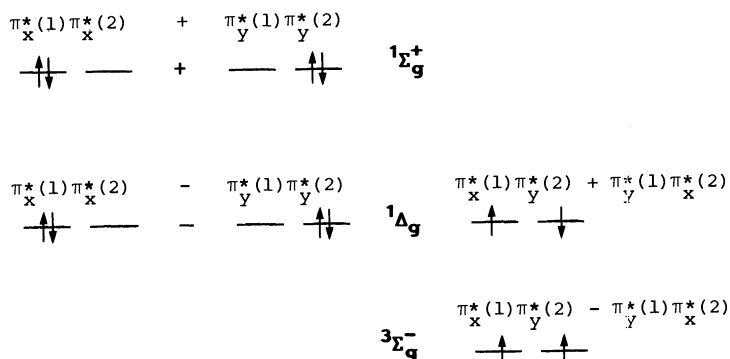


Figure 4-3 $(\pi^*)^2$ configurations.

4-4 CN⁻, CO AND NO⁺

The heteronuclear species CN⁻, CO and NO⁺ are isoelectronic with N₂, and therefore their molecular orbital configurations and valence-bond structures should be similar to those for N₂, but with some polarity for their molecular orbitals. From the molecular orbital configurations, it is easy to generate the valence-bond structures $\overset{(-)}{\text{C}}\equiv\overset{(-)}{\text{N}}:$, $\overset{(-)}{\text{C}}\equiv\overset{(+)}{\text{O}}:$ and $\overset{(+)}{\text{N}}\equiv\overset{(+)}{\text{O}}:$ if it is assumed that bonding electrons are shared equally by each pair of atoms. The bond-lengths of 1.15, 1.10 and 1.06 Å for CN⁻, N₂ and NO⁺ are respectively 0.12, 0.14 and 0.15 Å shorter than estimates of 1.27, 1.24 and 1.21 Å for C=N, N=N and N=O double bonds, and it is probably reasonable to assume that the triple-bonded structures are the primary valence-bond structures for each of these three species. However for CO, the bond-length of 1.13 Å is only 0.08 Å shorter than the length of a C=O double bond, and this suggests that valence-bond structures such as $\overset{(-)}{\text{C}}=\overset{(+)}{\text{O}}:$ and $\overset{(-)}{\text{C}}=\overset{(+)}{\text{O}}:$ as well as $\overset{(-)}{\text{C}}\equiv\overset{(+)}{\text{O}}:$ have appreciable weights. The importance of these double-bond structures for CO is that they do not carry atomic formal charges, whereas such charges are present in $\overset{(-)}{\text{C}}\equiv\overset{(+)}{\text{O}}:$. The electroneutrality principle requires that the formal charges of atoms in neutral molecules have small magnitudes, and the contributions to resonance from the double-bond structures will assist this requirement.

4-5 NO AND SN

Each of NO and SN has 11 valence-shell electrons, as has the cation O₂⁺ (Section 4-3). The lowest-energy molecular orbital configuration for NO is the same as that for O₂⁺; that for SN may be written as (σs)²(σ*s)²(σp)²(π_x)²(π_y)²(π_y^{*})¹ with the sulphur atom using its 3s and 3p orbitals to form the molecular orbitals.

The resulting valence bond structures for NO and SN are $\overset{(-\frac{1}{2})}{\text{N}}\equiv\overset{(+\frac{1}{2})}{\text{O}}:$ and $\overset{(+\frac{1}{2})}{\text{S}}\equiv\overset{(-\frac{1}{2})}{\text{N}}:$, each of which has a Pauling "3-electron bond". The NO bond-length of 1.15 Å is intermediate between the lengths of 1.06 and 1.21 Å for the N-O triple bond of NO⁺ and the double bond for CH₃N=O, and the Pauling "3-electron bond" structure for NO is in accord with this observation; there are five bonding electrons in $\overset{(-\frac{1}{2})}{\text{N}}\equiv\overset{(+\frac{1}{2})}{\text{O}}:$. The bond-length of 1.50 Å for SN is longer than the 1.44 Å for $\overset{(+)}{\text{S}}\equiv\overset{(-)}{\text{N}}:$, thereby reflecting the presence of five instead of six bonding electrons in the valence-bond structure $\overset{(+\frac{1}{2})}{\text{S}}\equiv\overset{(-\frac{1}{2})}{\text{N}}:$.

4-6 S₂, SO AND NO⁻

Each of S₂, SO and NO⁻ has 12 valence-shell electrons. As occurs with the O₂ ground-state, the degenerate antibonding π_x^{*} and π_y^{*} orbitals for these molecules are singly-occupied in the ground-state, with parallel spins for the two electrons. Therefore, the O₂, S₂, SO and NO⁻ valence-bond structures $\overset{\times}{\underset{\times}{\text{O}}}-\overset{\times}{\underset{\times}{\text{O}}}$, $\overset{\times}{\underset{\times}{\text{S}}}-\overset{\times}{\underset{\times}{\text{S}}}$, $\overset{\times}{\underset{\times}{\text{S}}}-\overset{\times}{\underset{\times}{\text{O}}}$ and $\overset{\times}{\underset{\times}{\text{N}}}-\overset{\times}{\underset{\times}{\text{O}}}$ are similar, each having two Pauling "3-electron bonds" and a bond-order of 2. The bond-lengths for SO and S₂ are 1.48 and 1.89 Å.

For NO⁻, the estimate of 1.268 Å for its bond-length is longer than the 1.21 Å for the N-O double-bond of CH₃N=O; the reason for this appreciable bond-length difference is not apparent.

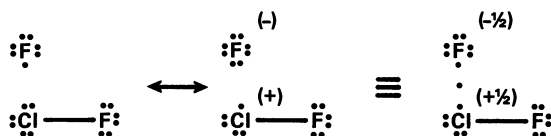
4-7 ClO AND FO

The molecular orbital configuration for the 11 valence-shell electrons of the ClO ground-state is (σs)²(σ*s)²(σp)²(π_x)²(π_y)²(π_x^{*})²(π_y^{*})¹, from which the valence-bond structure $\overset{(+\frac{1}{2})}{\underset{(-\frac{1}{2})}{\text{Cl}}}-\overset{(+\frac{1}{2})}{\underset{(-\frac{1}{2})}{\text{O}}}$ may be generated with three bonding electrons. The ClO bond-length of 1.55 Å is appreciably shorter than the Cl-O single-bond length of 1.70 Å for Cl₂O, thereby reflecting the significant development of a Pauling "3-electron bond" for one set of π-electrons for ClO. Dimers of ClO are known, one of which involves a weak bond between the oxygen atoms (Section 11-7). For FO, the valence-bond structure $\overset{(+\frac{1}{2})}{\underset{(-\frac{1}{2})}{\text{F}}}-\overset{(+\frac{1}{2})}{\underset{(-\frac{1}{2})}{\text{O}}}$ may be similarly generated from its molecular orbital configuration. However, in contrast to what occurs for Cl₂O₂, the dimer F₂O₂ has a strong O-O bond whose length of 1.217 Å is almost identical to that of the double bond for O₂ (Section 2-3(b)). Presumably, the very electronegative fluorine atom is not able to stabilize the Pauling "3-electron bond" of FO, and the valence-bond structure $\overset{\cdot\cdot}{\text{F}}-\overset{\cdot\cdot}{\text{O}}$ with the odd-electron located in an oxygen atomic orbital provides a better representation of the electronic structure. This is equivalent to saying that the electronegativity of fluorine prevents it from acquiring a formal positive charge of appreciable magnitude in a neutral molecule.

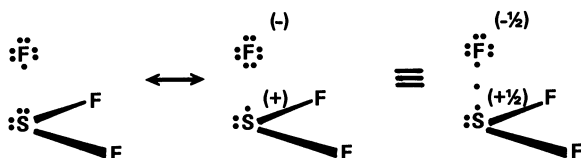
The results of recent calculations by Baird and Taylor³ show that as the difference in electronegativity between A and B in the Pauling "3-electron bond" structure $\overset{\cdot}{\text{A}}-\overset{\cdot}{\text{B}}$ increases, the stability of the bond decreases.

4-8 ClF₂ AND SF₃

For the radicals ClF₂ and SF₃, valence-bond structures may be constructed by bonding a fluorine atom to the Lewis octet structures for ClF and SF₂. This leads to the development of a Cl-F and S-F Pauling "3-electron bond", viz



and



It is assumed here that a chlorine or sulphur $3p\pi$ orbital is used for the σ -bonding in the Pauling "3-electron bond" to form 90° bond angles. Distortion of these angles away from 90° leads to sp^n hybridization for these orbitals. For ClF_2 , a bond-angle of 149° has been recently calculated⁴ using molecular orbital procedures - an experimental estimate⁵ for this angle is $136 \pm 15^\circ$. However, from e.s.r. measurements, Morton, Preston and Strach⁶ have concluded that SF_3 is a planar σ -radical with two equivalent fluorine atoms. The resulting valence-bond structure is then the planar version of that displayed above. More recently, Kiang and Zare⁷ have described Pauling "3-electron bond" theory for SF_3 and SF_5 , and assumed that SF_3 is non-planar.

4-9 N-H BOND-STRENGTHS OF NH_3 , N_2H_4 , N_2H_2 AND $\text{HN}_2 \rightarrow \text{H} + \text{N}_2$

For a number of polyatomic systems with diatomic Pauling "3-electron bonds", Baird has described some interesting applications of Pauling "3-electron bond" theory^{8,9}. We shall describe two of them here.

For the reactions $\text{NH}_3 + \text{NH}_2^\bullet + \text{H}^\bullet$, $\text{N}_2\text{H}_4 + \text{N}_2\text{H}_3^\bullet + \text{H}^\bullet$ and $\text{N}_2\text{H}_2 + \text{N}_2\text{H}^\bullet + \text{H}^\bullet$, the (calculated) N-H bond dissociation energies (D_e) are 435, 343 and 255 kJ mol^{-1} . The dissociation of NH_3 leaves the odd-electron of NH_2 located in a nitrogen atomic orbital. However, for each of $\text{N}_2\text{H}_3^\bullet$ and $\text{N}_2\text{H}^\bullet$, the odd-electron may be delocalized between two nitrogen atomic orbitals, thereby leading to the development of N-N Pauling "3-electron bonds" as follows:



The $\text{N}_2\text{H}_3^\bullet$ and $\text{N}_2\text{H}^\bullet$ radicals are thereby stabilized relative to $\text{H}_2\ddot{\text{N}}\text{---}\ddot{\text{N}}\text{H}^\bullet$ and $\text{HN}=\ddot{\text{N}}^\bullet$ as dissociation products, with the odd electron located in only one nitrogen atomic orbital. Consequently, the N-H dissociation energies for N_2H_4 and N_2H_2 are smaller than for NH_3 .

If the electronic structure for the ground-state of HN_2 is represented as $(+\frac{1}{2}) (-\frac{1}{2})$
 $\text{HN} \equiv \overset{\cdot}{\text{N}}:$, then the breaking of the N-H bond would generate an excited state of N_2 ,
 $(+\frac{1}{2}) (-\frac{1}{2})$ $(+\frac{1}{2}) (-\frac{1}{2})$
 i.e. $\text{HN} \equiv \overset{\cdot}{\text{N}}: + \text{H}^\bullet + \cdot \overset{\cdot}{\text{N}} \equiv \text{N}:$.

To obtain the N_2 ground-state ($:\text{N} \equiv \text{N}:$) as a dissociation product, it is necessary to consider another configuration for $\text{N}_2\text{H}^\bullet$, namely that obtained when the antibonding N-N π -electron of $\text{HN} \equiv \overset{\cdot}{\text{N}}:$ is transferred into the antibonding N-H σ^* -orbital which is vacant in this structure. The molecular orbital configuration for the relevant electrons of $\text{HN} \equiv \overset{\cdot}{\text{N}}:$ is $\psi_1 = (\sigma_{\text{NH}})^2 (\pi_{\text{NN}})^2 (\pi_{\text{NN}}^*)^1$. When the π_{NN}^* electron is transferred into the σ_{NH}^* orbital, the configuration $\psi_2 = (\sigma_{\text{NH}})^2 (\sigma_{\text{NH}}^*)^1 (\pi_{\text{NN}})^2$ is obtained. The latter configuration generates the valence-bond structure $\overset{(-\frac{1}{2})}{\text{H}} \cdot \overset{(+\frac{1}{2})}{\text{N}} \equiv \text{N}:$ with an N-H Pauling "3-electron bond". This structure can dissociate to generate $\text{H}^\bullet + :\text{N} \equiv \text{N}:$.

To describe the course of the reaction as the N-H bond is stretched, it is necessary to invoke configuration interaction (Section 3-3), i.e. to construct the linear combination $\Psi = C_1\psi_1 + C_2\psi_2$. When $r(\text{N-H})$ is close to the equilibrium bond-length, $|C_1| \gg |C_2|$. As the N-H bond is stretched, the N-H overlap integral is reduced in magnitude, and therefore the vacant σ_{NH}^* orbital of ψ_1 becomes less antibonding. This enables the energy separation between ψ_1 and ψ_2 to become smaller, thereby reducing the magnitude of C_1/C_2 . For large $r(\text{N-H})$, $|C_2| \gg |C_1|$, i.e. ψ_2 is the predominant configuration, which leads to the formation of $\text{H}^\bullet + :\text{N} \equiv \text{N}:$ as dissociation products when $r(\text{N-H}) = \infty$. The reaction is calculated to be exothermic, but a kinetic stability is associated with $\text{N}_2\text{H}^\bullet$ because energy is required to stretch the N-H bond of configuration ψ_1 .

Similar types of descriptions of the dissociations $\text{RCO} + \overset{(-)}{\text{R}}^\bullet + \overset{(+)}{:\text{C} \equiv \text{O}:}$ and $\text{CH}_2\text{CO} + \text{CH}_2(S = 1) + \overset{(-)}{:\text{C} \equiv \text{O}:}$ have also been described by Baird⁹.

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CHAPTER 5

PAULING "3-ELECTRON BONDS" AND HYPOLIGATED TRANSITION METAL COMPLEXES

Although it is currently not well-recognized, there exists a considerable number of transition metal complexes for which Pauling "3-electron bond" theory is of relevance. In order to illustrate this theory, consideration will be given here to descriptions of the electronic structures for a number of octahedral complexes.

5-1 HYPOLIGATED AND HYPERLIGATED TRANSITION METAL COMPLEXES

The low-energy valence-shell atomic orbitals for the transition metals are the five (inner) $(n-1)d$ orbitals and the ns and three np atomic orbitals. (For atoms of first-row transition metals Sc, \dots, Cu , these are the $3d_{x^2-y^2}$, $3d_{z^2}$, $3d_{xy}$, $3d_{xz}$, $3d_{yz}$, $4s$, $4p_x$, $4p_y$ and $4p_z$ orbitals; contours for $3d$ orbitals are displayed in Fig. 1-1.) Pauling¹ has classified transition metal complexes of the general type ML_N (M = transition-metal ion, L = ligand, N = number of ligands) as either *hyperligated* or *hypoligated* according to whether or not there are sufficient valence-shell orbitals on the metal ion to form N electron-pair $M-L$ σ -bonds. Thus the isoelectronic ions Co^{3+} and Fe^{2+} of $[Co(NH_3)_6]^{3+}$, $[CoF_6]^{3-}$ and $[Fe(H_2O)_6]^{2+}$ have $(3d)^6$ valence-shell configurations. However, magnetic susceptibility measurements for the three complexes indicate that the distributions of the six electrons amongst the $3d$ orbitals of the metal ions must differ. To account for the observed magnetic moment of zero¹ for $[Co(NH_3)_6]^{3+}$, it is necessary to assume that the three t_{2g} orbitals (d_{xy} , d_{xz} , and d_{yz}) of Co^{3+} are doubly-occupied (Fig. 5-1(a)), thereby generating a low-spin ($S = 0$) complex. The vacant e_g orbitals ($d_{x^2-y^2}$ and d_{z^2}) and the $4s$ and $4p$ orbitals may be hybridized to form six octahedral (d^2sp^3) hybrid orbitals. These orbitals are available for coordination with the six NH_3 ligands, so that six $Co-N$ electron-pair σ -bonds may be formed, as is shown in valence-bond structure (1). Because there are sufficient valence-shell orbitals of low-spin Co^{3+} to form six electron-pair $Co-N$ bonds, $[Co(NH_3)_6]^{3+}$ may be classified as a hyperligated complex.

Isoelectronic $[Fe(H_2O)_6]^{2+}$ and $[CoF_6]^{3-}$ are paramagnetic complexes with magnetic moments of 5.3 Bohr magnetons¹; the "spin-only" formula for the magnetic moment $\sqrt{n(n+2)}$ generates a magnetic moment of 4.9 Bohr magneton when the number of unpaired-electron spins (n) is four. Therefore, each of these complexes is assumed to have this number of unpaired-electrons with parallel spins. The $3d$ -orbital occupations for the Fe^{2+} and Co^{3+} ions are then those that are displayed in Fig. 5-1(b), and a high-spin ($S = 2$) complex is thereby generated. Because each of $[Fe(H_2O)_6]^{2+}$ and $[CoF_6]^{3-}$ has insufficient valence-shell orbitals to form six

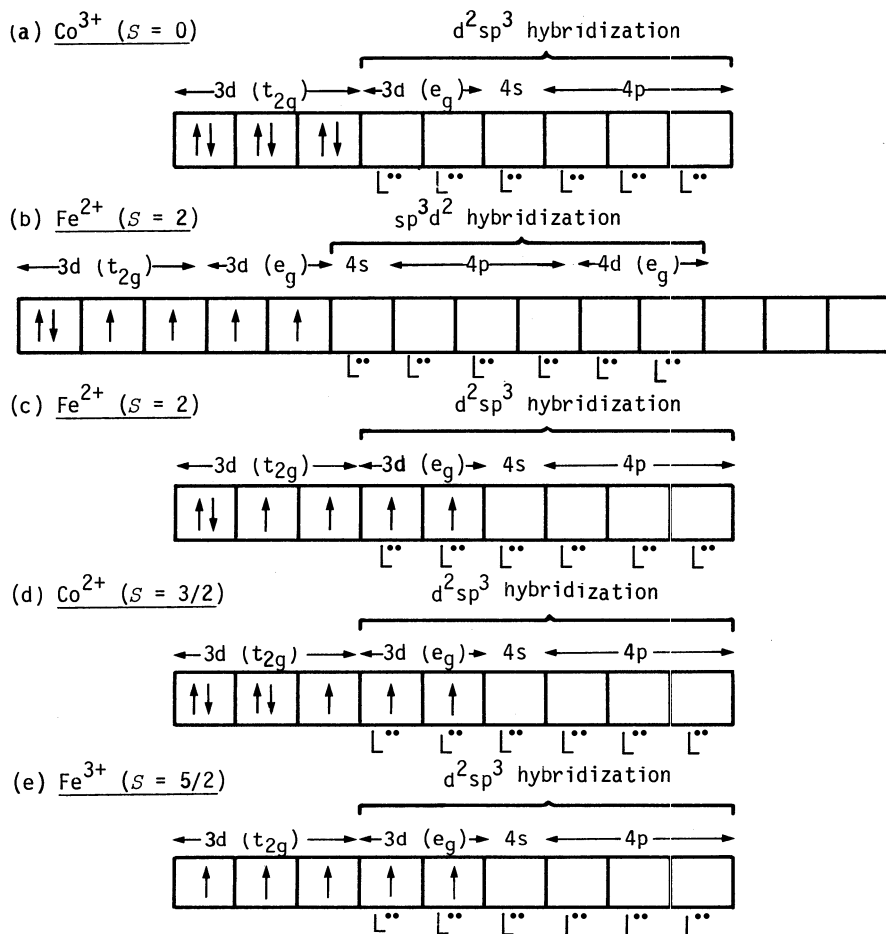


Figure 5-1 Orbital occupancies for some transition-metal ions ($L = \text{ligand}$).

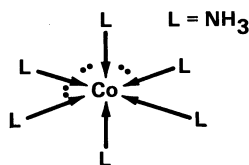
electron-pair bonds between the Fe^{2+} and Co^{3+} and the ligands, these complexes are classified as hypoligated complexes¹.

For hypoligated complexes, either of the following valence-bond procedures is sometimes used to describe the metal-ligand σ -bonding²:

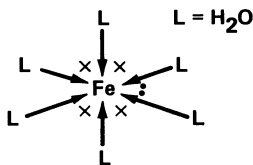
- (i) The outer $4d_{x^2-y^2}$ and $4d_{z^2}$ orbitals are hybridized with the 4s and 4p orbitals to form six octahedral (sp^3d^2) hybrid orbitals as shown in Fig. 5-1(b). These hybrid orbitals may be used for coordination with the six ligands to form six electron-pair M-L σ -bonds as in valence-bond structure (2). This approach may be criticized, because the 4d orbitals

lie too high in energy for them to be utilized in bonding to any significant extent.

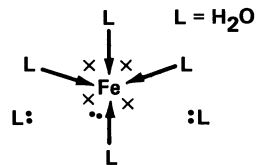
- (b) The vacant 4s and 4p orbitals, when suitably hybridized (i.e. as sp_x , p_y , and p_z , sp_y , p_z and p_x , and sp_z , p_x and p_y), may be used to form four electron-pair M-L bonds as in (3). It is then necessary to invoke resonance between a set of 15 valence-bond structures of type (3), which differ in the locations of the four M-L σ -bonds.



(1)



(2)



(3)

In contrast to what obtains for the above valence-bond descriptions of $[\text{Co}(\text{NH}_3)_6]^{3+}$, $[\text{CoF}_6]^{3-}$ and $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$, the simplest molecular orbital descriptions for both complexes use the same set of metal-ion orbitals for bonding, namely the inner $3d_{x^2-y^2}$ and $3d_{z^2}$ orbitals as well as the 4s and 4p orbitals. For $[\text{Co}(\text{NH}_3)_6]^{3+}$, the six non-bonding t_{2g} orbitals are doubly occupied and all molecular orbitals that are M-L antibonding are vacant. By contrast, two antibonding M-L molecular orbitals and two t_{2g} orbitals are singly-occupied for the $[\text{CoF}_6]^{3-}$ complex³. The atomic orbitals for these molecular orbital schemes have also been used in the above valence-bond description for $[\text{Co}(\text{NH}_3)_6]^{3+}$; they may also be used to provide a valence-bond description for $[\text{CoF}_6]^{3-}$ or $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$ if we avail ourselves of Pauling "3-electron bonds"⁴.

5-2 PAULING "3-ELECTRON BONDS" AND THE ELECTRONIC STRUCTURE OF $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$

For the purpose of bonding to the NH_3 ligands of $[\text{Co}(\text{NH}_3)_6]^{3+}$, the Co^{3+} is assumed to form six d^2sp^3 hybrid orbitals from the $3d_{x^2-y^2}$, $3d_{z^2}$, 4s and three 4p orbitals. For $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$, we allow the Fe^{2+} to form a similar set of hybrid orbitals. However, in contrast to what is the case for Co^{3+} in $[\text{Co}(\text{NH}_3)_6]^{3+}$, two of these orbitals for Fe^{2+} are singly-occupied, and four are vacant as is shown in Fig. 5-1(c). The latter four orbitals are available to form four electron-pair σ -bonds between the Fe^{2+} and four H_2O ligands. The two singly-occupied d^2sp^3 orbitals are available to form two Pauling "3-electron bonds" when these orbitals overlap with

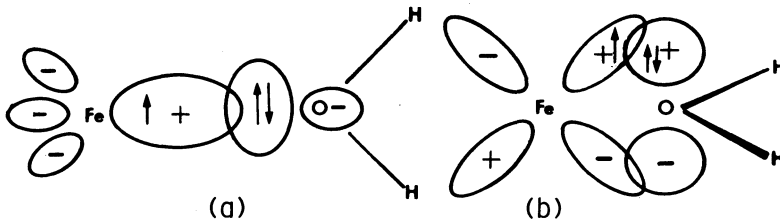


Figure 5-2 Overlap of metal-ion and ligand atomic orbitals for σ - and π -type Pauling "3-electron bonds" of $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$ and $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$.

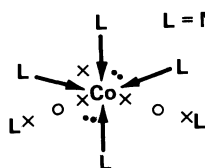
oxygen lone-pair orbitals, as is shown in Fig. 5-2(a). Two valence-bond structures are possible for each of these two FeOH_2 linkages, namely $\text{Fe} \cdot \text{:OH}_2$ and $\overset{(-)}{\text{Fe}} \cdot \overset{(+)}{\text{OH}_2}$ and resonance between them generates a Pauling "3-electron bond". Thus, we may write $\text{Fe} \cdot \text{:OH}_2 \leftrightarrow \overset{(-)}{\text{Fe}} \cdot \overset{(+)}{\text{OH}_2} \equiv \text{Fe} \cdot \cdot \text{OH}_2$ or $\overset{(-)}{\text{Fe}} \cdot \overset{(+)}{\text{OH}_2}$. The resulting valence-bond structures for the $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$ complex are of types (4) and (5), in which the singly-occupied orbitals have (s_z) spin quantum numbers of $+1/2$. Altogether, there are 15 valence-bond structures that differ in the locations of the $\text{Fe} \cdot \cdot \text{OH}_2$ and $\text{Fe} \leftarrow \text{OH}_2$ linkages, and all will contribute to the valence-bond resonance description of the complex. Similar types of valence-bond structures are also appropriate for $[\text{CoF}_6]^{3-}$.



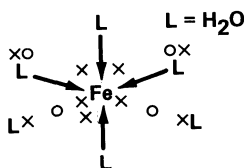
5-3 METAL-ION SPIN-STATE AND METAL-LIGAND BOND-LENGTHS

The nature of the spin-state of the metal ion may be reflected in the metal-ligand bond-lengths of the ML_N complex. This is well-exemplified for the hyperligated and hypoligated complexes $[\text{Co}(\text{NH}_3)_6]^{3+}$, and $[\text{Co}(\text{NH}_3)_6]^{2+}$, which have respectively low-spin ($3d^6$) and high-spin ($3d^7$) configurations for the Co^{3+} and Co^{2+} ions. The Co-N bond-lengths for these complexes are 1.94 Å and 2.11 Å respectively^{5,6}. In Section 5-1, we have shown that the valence-bond description for the Co(III) complex permits the formation of six electron-pair Co-N σ -bonds, as in (1).

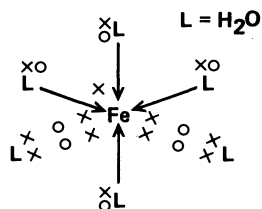
For the high-spin Co(II) complex, the orbital occupations for Co^{2+} displayed in Fig. 5-1(d) require that six NH_3 ligands form four Co-N single-bonds, and two Pauling "3-electron bonds" with bond-orders of 0.5. The resulting valence-bond structures for $[\text{Co}(\text{NH}_3)_6]^{2+}$ are of type (6), and the average Co-N σ -bond order of 5/6 is in accord with the longer Co-N bonds for this complex relative to those of low-spin $[\text{Co}(\text{NH}_3)_6]^{3+}$.



(6)



(7)



(8)

For high-spin $[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$, with valence-bond structures of types (4) and (5), the average Fe-O bond-order is also 5/6, and therefore it is not surprising that the Fe-O bond-lengths⁷ of 2.12 Å are similar to those of high-spin $[\text{Co}(\text{NH}_3)_6]^{2+}$. By contrast, the Fe-O bond-lengths⁸ of 1.99 Å for high-spin $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$ are appreciably shorter. For this Fe(III) complex, the Fe^{3+} orbital occupations are displayed in Fig. 5-1(e) and the valence-bond structures of type (7) also generate Fe-O σ -bond orders of 5/6. We may account for the shorter Fe-O bonds in this complex by noting that the Fe^{3+} ion is more electronegative than the Fe^{2+} ion. The effect of this should be to induce a significant amount of delocalization of oxygen lone-pair electrons from hybrid orbitals which overlap with the singly-occupied t_{2g} orbitals of Fe^{3+} . The orbital overlap is displayed in Figure 5-2(b). This delocalization will lead to the formation of Pauling "3-electron bond" Fe-O π -bonds, and thereby increase the Fe-O bond-orders above the value of 5/6 that pertains for the σ -bonding. In the $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$ valence-structures these π -bonds should be best developed between pairs of atoms that are linked by Pauling "3-electron bond" σ -bonds, as in (8), in order that the oxygen atoms do not acquire formal charges greater than unity. Thus, to satisfy this requirement, we have indicated only two π -bonds in (8), although on overlap considerations, three are possible. The average Fe-O bond-order for (8) is unity, but because part of the contribution arises from the π -bonding, it is not surprising that the Fe-O bond-lengths for $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$ are longer than the estimate⁹ of 1.92 Å for the length of an Fe-O σ -single bond. For the Co(II) and Co(III) complexes, the NH_3 ligands have no lone-pair electrons available for Co-N π -bonding.

5-4 INTERCONVERSION BETWEEN HYPOLIGATED AND HYPERLIGATED ELECTRONIC STATES

The Pauling "3-electron bond" theory of hypoligation has very wide applicability. All d^4 - d^9 transition-metal complexes of the type ML_N will involve one or more Pauling "3-electron bonds" in their valence-bond structures if the metal-ion has insufficient vacant inner d and valence-shell s and p orbitals available to form N electron-pair M-L σ -bonds with the N ligands. In Table 5-1, we have classified the d^4 - d^9 octahedral ML_6 complexes according to the spin-states of the transition-metal ions, and the number of electron-pair bonds and Pauling "3-electron bonds". Fairly obviously, octahedral d^4 - d^6 complexes that do not require Pauling "3-electron bonds" may be classified as hyperligated. Excited hypoligated states may be generated for such complexes by promoting one or more non-bonding t_{2g} electrons into antibonding σ_{ML}^* orbitals that are vacant in the hyperligated ground-states. In Section 3-6, we have deduced that two bonding + one antibonding electron (i.e. $(\sigma_{ML})^2(\sigma_{ML}^*)^1$ here) is the molecular orbital formulation of a Pauling "3-electron bond". Conversely, a $\sigma_{ML}^* + t_{2g}$ excitation will convert⁴ high-spin d^4 and intermediate-spin d^5 and d^6 octahedral complexes (each of which has one Pauling "3-electron bond") into hyperligated excited states.

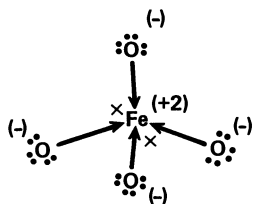
configuration	spin-state	number of bonds	
		electron-pair	"3-electron"
d^4	high ($S = 2$)	5	1
d^5, d^6, d^7, d^8	high ($S = 5/2, 2, 3/2, 1$)	4	2
d^5, d^6	intermediate ($S = 3/2, 1$)	5	1
d^7	low ($S = 1/2$)	5	1
d^9	($S = 1/2$)	4	1

Table 5-1 Metal ion configurations and M-L σ -bond types for ML_6 complexes that can involve Pauling "3-electron bonds".

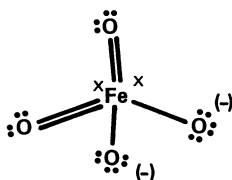
5-5 METAL-LIGAND π -BONDING AND PAULING "3-ELECTRON BONDS"

A number of paramagnetic transition metal complexes must involve Pauling "3-electron bonds" for the π -electrons only. We shall consider one example here, namely the Fe(VI) tetrahedral anion FeO_4^{2-} . This anion may be considered to involve Fe^{6+} ($3d$)² bonded to four O^{2-} ligands. In a tetrahedral environment, the lowest-energy 3d orbitals are d_{xy} and d_{yz} , which are degenerate. Consequently, the ($3d$)² configuration of lowest energy is an $S = 1$ state, with the two electrons occupying these orbitals with parallel spins. Magnetic susceptibility measurements¹⁰ support this assignment of an $S = 1$ spin-state for FeO_4^{2-} .

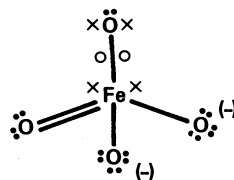
The remaining seven valence-shell orbitals of Fe^{2+} are vacant, and they are available for coordination with the O^{2-} ligands. Tetrahedral hybridization of the 4s and 4p orbitals may be used to form four Fe-O σ -bonds, as in (9). Two strong electron-pair π -bonds may also be formed by overlapping the doubly-occupied $2p\pi$ (or $2p\bar{\pi}$) orbitals of the O^- with the vacant e_g orbitals[†], to give valence-bond structures of type (10). In (10), the unpaired electrons are localized in the d_{xy} and d_{yz} orbitals and the formal charge on the Fe is zero. Zero formal charge on the Fe may also be obtained by forming one Fe-O electron-pair π -bond and two Pauling "3-electron bonds" of π - or $\bar{\pi}$ -type, as in (11). The unpaired electrons are then delocalized over all atomic centres. Both (10) and (11) involve Fe-O double-bonding, and therefore account for the observation that the Fe-O bond-lengths of 1.656 Å (as in K_2FeO_4)¹² are much shorter than the estimate⁹ of 1.92 Å for the length of an Fe-O single bond.



(9)



(10)



(11)

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[†] The $d_{x^2-y^2}$ and d_{z^2} orbitals overlap better with the oxygen π - and $\bar{\pi}$ -orbitals than do the d_{xz} , d_{yz} and d_{xy} orbitals¹¹ of tetrahedral molecules. But because the latter overlaps are non-zero, we have indicated the presence of Fe-O bonding arising from them in (11).

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CHAPTER 6

PAULING "3-ELECTRON BONDS", 5-ELECTRON 3-CENTRE BONDING AND SOME TETRA-ATOMIC RADICALS

Valence-bond structures with Pauling "3-electron bonds" between pairs of atoms may be written down for a number of triatomic radicals. Here we shall examine these types of structures for some radicals with either 17 or 19 valence-shell electrons. For these systems, it is necessary to write down two Pauling "3-electron bond" structures, which participate in resonance. The delocalized molecular orbital equivalent of this resonance involves the construction of three 3-centre molecular orbitals to accommodate five electrons; this is described in Section 6-4.

6-1 NO₂

Nitrogen dioxide with 17 valence-shell electrons is perhaps the most familiar triatomic molecule for which Pauling "3-electron bond" theory is appropriate. E.s.r. measurements indicate that the odd electron is delocalized over the three atomic centres; estimates of the nitrogen and oxygen odd-electron charges are (Table 6-1) 0.52 and 0.24, respectively. (For the purpose of qualitative discussion, we shall approximate these charges to 0.5 and 0.25). Each of the N-O bonds of NO₂ has a length¹ of 1.19 Å and the O-N-O bond angle is¹ 134°. These observations suggest that resonance between the Lewis structures (1)-(4) is needed to account for the location of the odd-electron on all three atoms and for the equality of the N-O

NO ₂	(σ)	0.52 ^(a)	NO ₂ ⁻	(π)	0.80 ^(b)
CO ₂ ⁻	(σ)	0.65 ^(b)	ClO ₂	(π)	0.59 ^(a)
BF ₂	(σ)	0.93 ^(c)	NF ₂	(π)	0.95 ^(a) , 0.77 ^(d)
O ₃ ⁻	(σ)	0.58 ^(b)	PF ₂	(π)	0.91 ^(d)
SO ₂ ⁻	(π)	0.74 ^(b)	PCl ₂	(π)	0.81 ^(d)

Table 6-1 E.s.r. estimates of A-atom odd-electron charges (ρ_A) for AY₂ radicals. (a) H.J. Bower, M.C.R. Symons and D.J.A. Tinling, in *Radical Ions* (E.T. Kaiser and L. Kevan, eds., Interscience, New York, 1968) Chapter 10; (b) M.C.R. Symons, *Chem. Soc. Specialist Reports., E.S.R.* **3**, 140 (1974); (c) W. Nelson and W. Gordy, *J. Chem. Phys.*, **51**, 4710 (1969); (d) M.S. Wei, J.H. Current and J. Gendell, *J. Chem. Phys.* **57**, 2431 (1972). For reasons that are discussed in Ref. (d) the experimental estimates of the spin densities (which we have equated to the odd-electron charges) rarely add exactly to unity. However we shall make the simplifying assumption that they do, i.e. assume that $\rho_A + 2\rho_Y = 1$ with the ρ_A given in this table.

bond-lengths. If it is assumed that each of (1)-(4) makes the same contribution to the resonance, then the nitrogen and oxygen odd-electron charges are 0.5 and 0.25, respectively. The relevant atomic orbitals that are occupied by the odd-electron are the oxygen $2p\bar{r}$ orbitals and the nitrogen hybrid orbital displayed in Fig. 6-1.

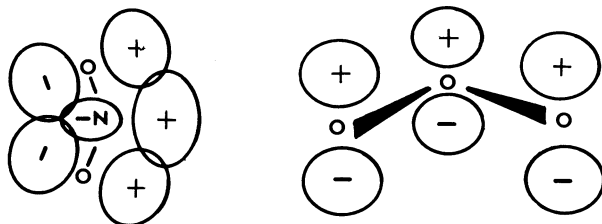
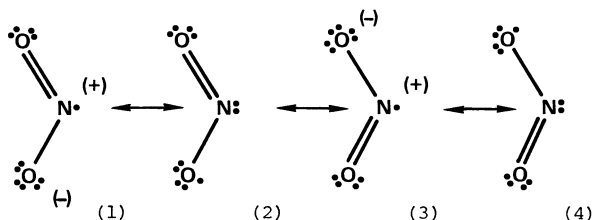
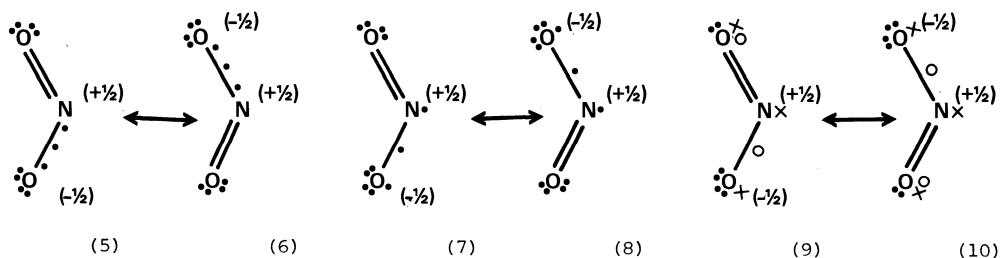


Figure 6-1 Atomic orbitals involved in the formation of Pauling "3-electron bonds" for NO_2 and O_3^- .

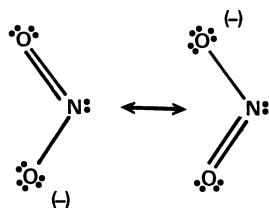
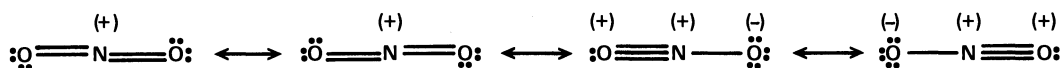
The e.s.r. measurements indicate that the nitrogen orbital has 2s as well as 2p character, and therefore this orbital is a hybrid orbital.



By utilizing Pauling "3-electron bonds", we may reduce the number of valence-bond structures that we need to write down from four to two. Thus the resonance between Lewis structures (1) and (2) generates² the Pauling "3-electron bond" structure (5). Similarly, we may summarize resonance between Lewis structures (3) and (4) by writing down the Pauling "3-electron bond" structure (6). Therefore resonance between (1)-(4) is equivalent to invoking resonance between (5) and (6). When we introduce the Green and Linnett representation³ for the Pauling "3-electron bond" (i.e. $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ instead of $\text{A} \cdot \cdot \text{B}$) we obtain valence-bond structures (7) and (8) for NO_2 . If we assume that the odd-electron has an s_z spin quantum number $+1/2$, the Green and Linnett valence-bond structures become those of (9) and (10).



As does resonance between valence-bond structures (1)-(4), these Pauling "3-electron bond" structures account qualitatively for the distribution of the odd electron of NO_2 , and for the equality of the N-O bond-lengths. They are also in accord with the observation that the N-O lengths of 1.19 Å are intermediate between those for NO_2^+ (1.15 Å)⁴ and NO_2^- (1.24 Å)⁵, as are the bond-angles (NO_2 , 134°; NO_2^+ , 180°; NO_2^- , 115°). The NO_2^+ and NO_2^- ions have, respectively, 16 and 18 valence-shell electrons, and standard Lewis structures for them are those of (11) and (12) with eight and six N-O bonding electrons, respectively. The NO_2 valence-bond structures (7) and (8) (or (9) and (10)) each have seven N-O bonding electrons. Thus, as one proceeds from NO_2^+ to NO_2^- , the number of bonding electrons in these valence-bond structures decreases and the N-O bond-lengths increase. Similarly, the O-N-O bond-angle closes as the number of nitrogen non-bonding electrons in the valence-bond structures increases from 0 for NO_2^+ to 1.5 for NO_2 , to 2 for NO_2^- .

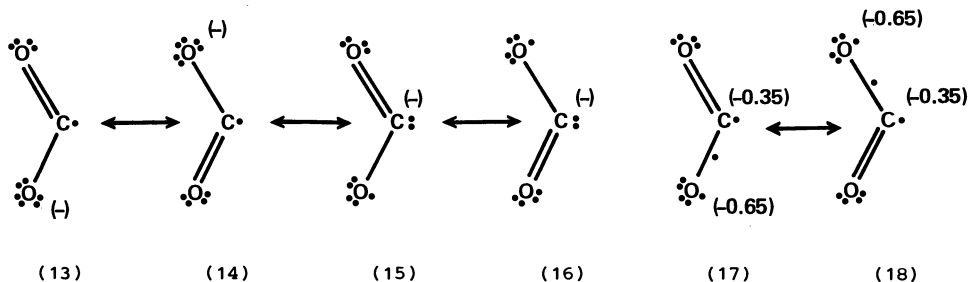


One NO_2 bond-property is not accounted for by means of the Pauling "3-electron bond" structures (7) and (8) (or (9) and (10)). The N-O bond-lengths of 1.19 Å are similar to Pauling's estimate of 1.20 Å for an N-O double bond (c.f. 1.214 Å for $\text{CH}_3\text{N}=\text{O}$)⁶. However, resonance between structures (7) and (8), each of which has seven bonding electrons, would imply that the N-O bonds for NO_2 should be longer than double bonds. To obtain an additional bonding electron in each structure, it is necessary to utilize the "increased-valence" procedures[†] described in Chapters 11 and 12.

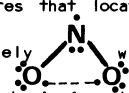
[†] In Section 6-1, we have followed convention by assuming that (1) and (3) are the (see next page)

6-2 CO_2^- AND BF_2

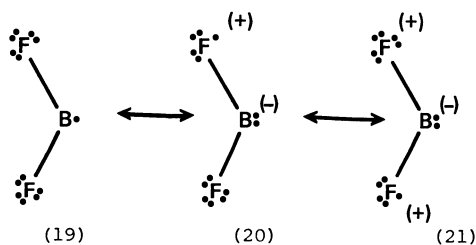
The anion CO_2^- is isoelectronic with NO_2 . E.s.r. measurements (Table 6-1) indicate that the odd-electron of CO_2^- is more located on the carbon atom than is the odd-electron of NO_2 located on the nitrogen atom. Estimates of the carbon and oxygen odd-electron charges are 0.65 and 0.175. These charges imply that valence-bond structures (13) and (14) for CO_2^- (with the odd-electron located on the carbon atom) make a larger contribution to the ground-state resonance than do (1) and (3) for NO_2 . This is in accord with what one may deduce from elementary electronegativity considerations; Lewis structures (15) and (16) with negative formal charges on the carbon atoms should be of higher energy than are (13) and (14). Therefore, the weights for (13) and (14) should be rather larger than are those for (15) and (16). Resonance between (13)-(16), with weights of 0.325, 0.325, 0.175 and 0.175 for these structures, will generate the carbon and oxygen odd-electron charges of 0.65 and 0.175. The resulting formal charges for the Pauling "3-electron bond" structures are those of (17) and (18).



The BF_2 radical is also isoelectronic with NO_2 . E.s.r. studies of BF_2 locate the odd-electron primarily in a boron hybrid atomic orbital (Table 6-1). The Lewis structure (19), with zero formal charges on all atoms and the odd-electron located on the boron atom, is in accord with this observation. Because of the unfavourable formal charge arrangements for structures (20) and (21) - each involves F^+ and B^- - the contribution of these structures to the ground-state resonance must be small, i.e. (19) is the primary structure and little development of a Pauling "3-electron bond" must occur for the BF_2 radical.

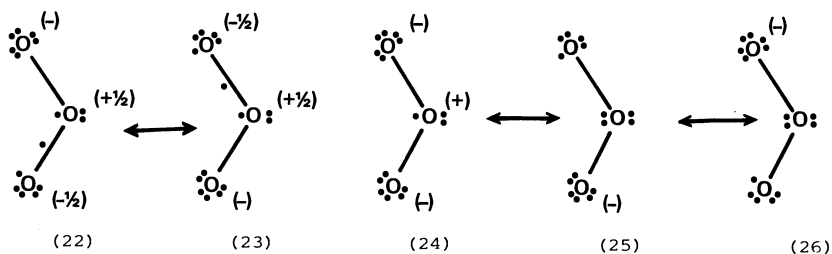
(continued from previous page) primary valence-bond structures that locate the odd electron on the nitrogen atom of NO_2 . Another valence-bond structure, namely  with a "long" O-O bond, also

locates the odd electron on the nitrogen atom. The absence of atomic formal charges for it suggests that it may also be an important valence-bond structure, and the results of quantum-mechanical valence-bond calculations⁷ lend support to this hypothesis. In Section 11-8, "increased-valence" structures are described for NO_2 ; these structures summarize resonance between seven Lewis structures, five of which are (1)-(4) and this "long-bond" structure.



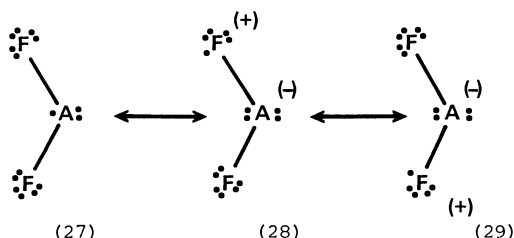
6-3 TRIATOMIC RADICALS WITH 19 VALENCE-SHELL ELECTRONS: O_3^- , SO_2^- , NF_2 AND ClO_2

Valence-bond structures with Pauling "3-electron bonds" are also appropriate for a number of radicals with 19 valence-shell electrons⁸. As our first example, we shall examine the bonding for the anion O_3^- . The Pauling "3-electron bond" structures (22) and (23) for this radical summarize resonance between Lewis structures (24) and (26), and (24) and (25), respectively. The latter three structures locate the odd-electron on one of each of the three atoms. E.s.r. measurements (Table 6-1) indicate that the odd electron is delocalized over all three atoms, and that it occupies the $2p\pi$ -type atomic orbitals of Fig. 6-1.

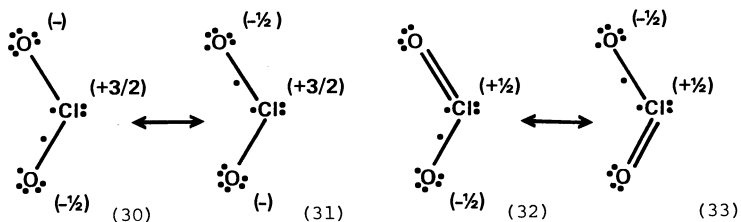


A similar valence-bond representation pertains for the anion SO_2^- , with a sulfur atom replacing the central oxygen atom. It is also appropriate for the anion NO_2^- , when $\text{N}^{(-\frac{1}{2})}$ replaces $\text{O}^{(+\frac{1}{2})}$ in (22) and (23), and N and $\text{N}^{(-)}$ replace the O^+ and (central) O atom of (24), (25) and (26). Formal charge considerations suggest that the odd-electron should be more located on the terminal oxygen atoms of O_3^- and SO_2^- , than it is for NO_2^- , and the e.s.r. estimates of the odd-electron charge on the central atom (Table 6-1) are in accord with this expectation. For NF_2 and PF_2 , the three Lewis structures that are equivalent to (24), (25) and (26) are (27)-(29) (with A = N or P), and the absence of an unfavourable formal charge distribution in (27) suggests that this structure is the most important. As is the case for BF_2 ,

little development of the Pauling "3-electron bonds" is expected for NF_2 and PF_2 , i.e. the odd-electron is located primarily (but not completely) in a nitrogen or phosphorus atomic orbital; e.s.r. estimates for the boron, nitrogen, and phosphorus odd-electron charges for these radicals are (Table 6-1) 0.93, 0.95 or 0.77, and 0.91.



For ClO_2 , the Pauling "3-electron bond" structures are (30) and (31), if only the chlorine 3s and 3p orbitals are utilized for bonding. These structures involve large formal charge separations. They may be reduced in magnitude by allowing the chlorine 3d orbitals also to participate in bonding. We thereby obtain (32) and (33) as the Pauling "3-electron bond" structures. In Section 11-8 an alternative "increased-valence" procedure is used to reduce the formal charge separations of (30) and (31). The e.s.r. measurements (Table 6-1) indicate that the odd-electron of ClO_2 is delocalized over the three atomic centres, with a chlorine odd-electron charge of 0.59, and therefore Pauling "3-electron bonds" are appropriate for any valence-bond structure for this radical.

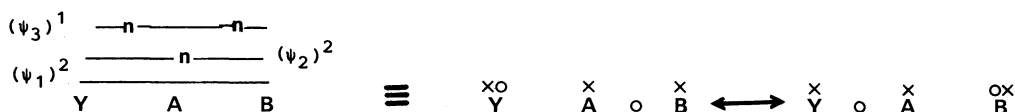


6-4 3-CENTRE MOLECULAR ORBITALS AND PAULING "3-ELECTRON BONDS"

If we designate the three atomic orbitals of Fig. 6-1 for NO_2 as y , a and b , then we may construct the delocalized molecular orbitals of Eqn (1) from them, for which k_1 and k_3 are constants, both > 0 and related through the requirement that ψ_1 and ψ_3 must be orthogonal. (These molecular orbitals are formally identical to those of Section 2-3).

$$\psi_1 = (y + b)/2^{1/2} + k_1 a, \quad \psi_2 = (y - b)/2^{1/2}, \quad \psi_3 = k_3(y + b)/2^{1/2} - a \quad (1)$$

With respect to each pair of nitrogen and oxygen atoms, molecular orbitals ψ_1 , ψ_2 and ψ_3 are respectively bonding, non-bonding and antibonding. With respect to each of the Pauling "3-electron bond" structures (7) and (8), and (17) and (18), five electrons are associated with the y, a and b atomic orbitals of Fig. 6-1. Therefore, for the delocalized molecular orbital description of these electrons, orbitals ψ_1 and ψ_2 are doubly-occupied, and ψ_3 is singly-occupied. The molecular orbital configuration for the 5-electron 3-centre bonding unit is then $(\psi_1)^2(\psi_2)^2(\psi_3)^1$. We shall now deduce⁹ that use of this configuration is equivalent to invoking resonance between the Pauling "3-electron bond" structures that have been referred to above; in general terms, we may write



when Y and B are equivalent atoms.

To provide a simple demonstration of this equivalence, it is only necessary to show that the molecular orbital configuration $(\psi_1)^2(\psi_2)^2(\psi_3)^1$ may be expressed as a linear combination of the configurations $(y)^2(a)^2(b)^1$, $(y)^2(a)^1(b)^2$ and $(y)^1(a)^2(b)^2$ for the Lewis structures $\ddot{\text{Y}} \cdot \dot{\text{A}} \cdot \ddot{\text{B}}$, $\ddot{\text{Y}} \cdot \ddot{\text{A}} \cdot \dot{\text{B}}$ and $\dot{\text{Y}} \cdot \ddot{\text{A}} \cdot \ddot{\text{B}}$. This is because resonance between the Pauling "3-electron bond" structures $\ddot{\text{Y}} \cdot \dot{\text{A}} \cdot \dot{\text{B}}$ and $\dot{\text{Y}} \cdot \dot{\text{A}} \cdot \ddot{\text{B}}$ is equivalent to resonance between $\ddot{\text{Y}} \cdot \dot{\text{A}} \cdot \ddot{\text{B}}$, $\ddot{\text{Y}} \cdot \ddot{\text{A}} \cdot \dot{\text{B}}$ and $\dot{\text{Y}} \cdot \ddot{\text{A}} \cdot \ddot{\text{B}}$. We may write $(\psi_1)^2(\psi_2)^2(\psi_3)^1$ as $\psi_1^\alpha \psi_1^\beta \psi_2^\alpha \psi_2^\beta \psi_3^\alpha$, in which α and β are the spin wave-functions for electrons with s_z spin quantum numbers of +1/2 and -1/2, and the odd-electron is assumed to have $s_z = +1/2$. By substituting the L.C.A.O. forms of the molecular orbitals of Eqn. 6-1 into this configuration, and then expanding the configuration as a linear combination of atomic orbital configurations, we obtain

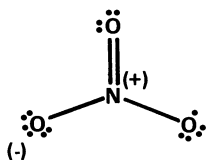
$$\psi_1^\alpha \psi_1^\beta \psi_2^\alpha \psi_2^\beta \psi_3^\alpha = \text{const} \times [-2^{1/2}(y^\alpha y^\beta b^\alpha b^\beta a^\alpha) + k_1\{(y^\alpha y^\beta a^\alpha a^\beta b^\alpha) + (y^\alpha a^\alpha a^\beta b^\alpha b^\beta)\}]$$

To obtain this expression, we have omitted all atomic orbital configurations for which two or more electrons occupy the same atomic orbital with the same s_z spin quantum numbers. Such configurations are forbidden by the Pauli exclusion principle. A derivation of the above linear combination that takes proper account of electron indistinguishability is provided in Ref. 9a,b.

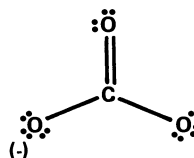
For the 19 valence-electron systems O_3^- , SO_2^- , ClO_2 and other isoelectronic species, the π -atomic orbitals that are associated with the odd electron are displayed in Figure 6-1. The molecular orbitals that may be constructed from these orbitals are also given by Eqn. (1) (with y, a and b $\equiv \pi$), and the π -electron configuration for the 5-electron 3-centre bonding is $(\psi_1)^2(\psi_2)^2(\psi_3)^1$.

6-5 SOME TETRA-ATOMIC RADICALS

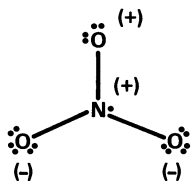
The isoelectronic radicals NO_3 and CO_3^- with 23 valence-shell electrons, are predicted to be planar¹⁰. Their standard Lewis structures are of types (34) and (35) (together with two other equivalent structures). For each of these structures, the odd-electron occupies an oxygen atomic orbital. To locate the odd-electron in a carbon or nitrogen atomic orbital, it is necessary to reduce the number of C-O and N-O covalent bonds, as occurs in structures (36)-(39), for example. These latter structures do not have a more favourable distribution of atomic formal charges than do (34) and (35). This fact, taken together with the smaller number of C-O or N-O covalent bonds, suggests that (36)-(39) should be unimportant valence-bond structures for the ground-states of these radicals. This expectation is in accord with the e.s.r. observations¹⁰ that the odd-electron for either NO_3 or CO_3^- occupies primarily atomic orbitals that are located on the oxygen atoms. Therefore, no significant development of a Pauling "3-electron bond" may occur for these systems.



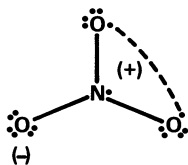
(34)



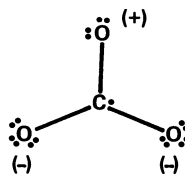
(35)



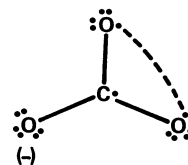
(36)



(37)

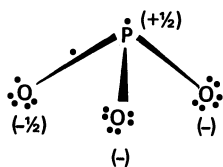


(38)

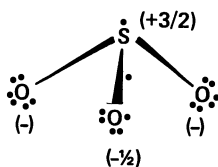


(39)

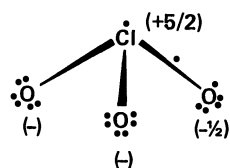
By contrast, the radicals NO_3^{2-} , PO_3^{2-} , SO_3^- and ClO_3 with 25 valence shell electrons, have been found to have their odd electron delocalized over all atomic centres¹⁰. For these radicals, Pauling "3-electron bonds" may be developed without reducing the number of A-O (with A \equiv P, S or Cl) bonding electrons. Thus we may write



(40)

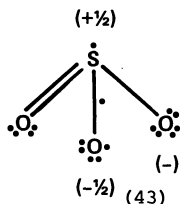


(41)

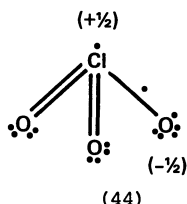


(42)

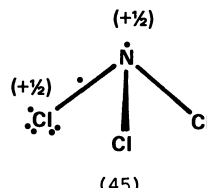
to locate the odd-electron in an A atomic orbital as well as the oxygen atomic orbitals. (For each of (40)-(42), there are two other equivalent structures that participate in resonance with these structures). The formal charges in these structures reflect the reduced importance of $\overset{\cdot}{\text{A}}-\overset{\cdot}{\text{O}}$ to the Pauling "3-electron bond" resonance $\overset{\cdot}{\text{A}}-\overset{\cdot}{\text{O}} \leftrightarrow \overset{\cdot}{\text{A}}-\overset{\cdot}{\text{O}}$ as one proceeds from PO_3^{2-} to ClO_3 . This is reflected in the values of the P, S and Cl odd-electron charges, namely (Ref. (a) of Table 6-1) 0.68, 0.58 and 0.36. For NO_3^{2-} , the nitrogen odd-electron charge is 0.81. As is the case for ClO_2 (Section 6-3), the possibility exists that sulphur and chlorine 3d orbitals may participate significantly in bonding for SO_3^- and ClO_3 . If this occurs, the resulting valence-bond structures of types (43) and (44) also have Pauling "3-electron bonds". The presence of non-bonding electrons on the A atoms of each (40)-(44) is in accord with the prediction that these 25 valence-electron radicals are non-planar¹⁰.



(43)



(44)



(45)

Group (V) trihalides are isoelectronic with PO_3^{3-} , SO_3^{2-} and ClO_3^- . Photoelectron spectrum studies permit features of the electronic structures of different states for the singly-charged cations of the trihalides to be examined¹¹. If a non-bonding electron is ionized, a Pauling "3-electron bond" can be developed in the cation, as is displayed in (45) for NCl_3^+ . These types of valence-bond structures are similar to (40)-(42) for PO_3^{2-} , SO_3^- and ClO_3 .

The influence of overlap on the stabilization or destabilization of Pauling "3-electron bonds" has been discussed in Section 3-10, together with the consequent effect on competition between planarity and pyramidalization for radicals such as CH_3 , CH_2F , CHF_2 and CF_3 . Each of CF_3 and NCl_3^+ has 25 valence-shell electrons.

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CHAPTER 7

SOME DIMERS OF TRIATOMIC RADICALS WITH 17 AND 19 VALENCE-SHELL ELECTRONS

A number of triatomic radicals can form dimers whose geometries have been well-characterized. A study of the electronic structures of these dimers can illustrate aspects of qualitative valence-bond and molecular orbital theory for electron-rich polyatomic molecules, and in particular, interconnections between these theories can be demonstrated. Dinitrogen tetroxide is a molecule *par excellence* that may be used for these purposes, and we shall give primary consideration to its electronic structure and bond properties.

7-1 THE LONG, WEAK N-N BOND OF N_2O_4 : LEWIS VALENCE-BOND THEORY

NO_2 with 17 valence-shell electrons can form several dimers¹ whose geometries are displayed in Figure 7-1. The most stable dimer is planar with a long, weak N-N bond. The N-N bond-length for this dimer is 1.78 \AA^2 , which is 0.33 \AA longer than the single bond of N_2H_4 ³. The N-N bond-dissociation energy of 57 kJ mol^{-1} for N_2O_4 is much smaller than that of 250 kJ mol^{-1} for N_2H_4 ^{4,5}. Both molecular orbital and valence-bond theory may be used to explain why the N-N bond is long and weak. The Lewis-type valence-bond explanation follows immediately from the valence-bond description of the electronic structure of NO_2 (Section 6-1).

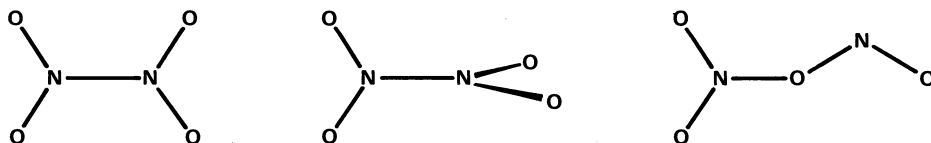
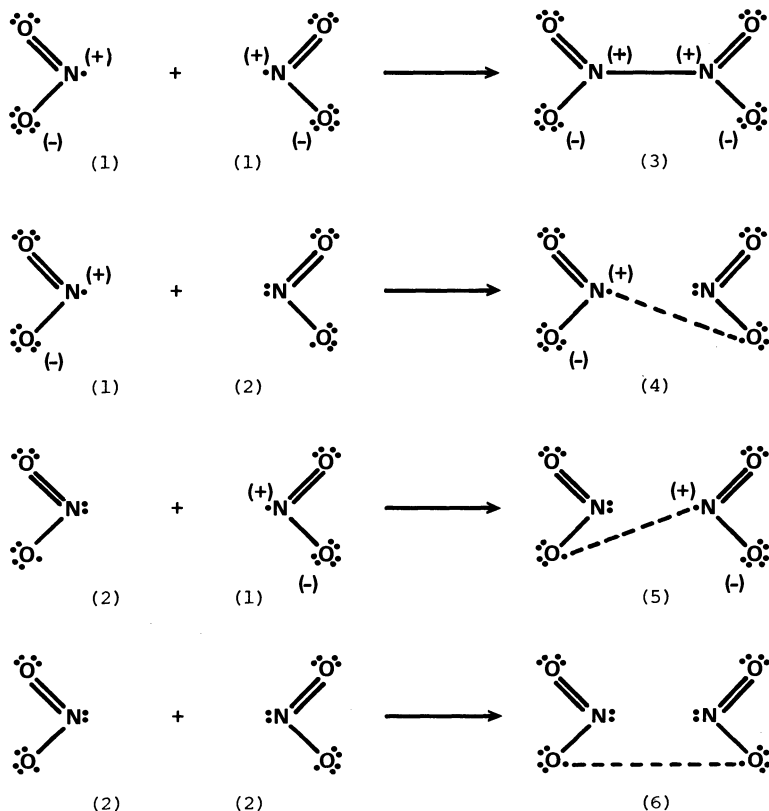


Figure 7-1 N_2O_4 isomers¹.

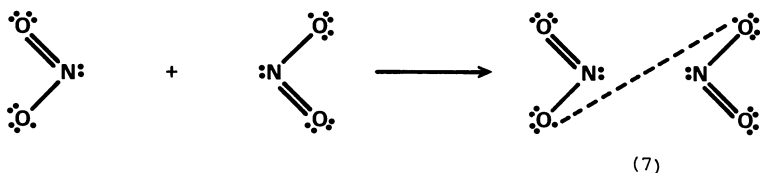
We shall assume here that the electronic structure of the ground-state for NO_2 may be described by invoking resonance between the valence-bond structures (1)-(4) of Section 6-1. (For convenience only, we shall initially restrict our attention to structures (1) and (2), but it is to be understood that these valence-bond structures participate in resonance with the symmetrically-equivalent structures (3) and (4).) When NO_2 dimerizes, the odd-electrons of the two monomers must be spin-paired to form an electron-pair bond that links the two radicals. By using valence-bond

structures of types (1) and (2) to represent each monomer, the following Lewis-structures for the dimer can be generated



In structures (4)-(6) above, we have used pecked bond-lines (----) to indicate the formation of "long-bonds" between pairs of non-adjacent atoms. Because of the small overlap that exists between atomic orbitals located on non-adjacent centres, these bonds are extremely weak (Section 2-5(b)) and have negligible strength. Sometimes these bonds are designated as "formal bonds"⁸. It follows that if resonance between structures (1) and (2) (together with their mirror-images) is used to represent the electronic structure of NO₂, then resonance between the structures (3)-(6) (together with mirror images) may be used to describe the electronic structure of N₂O₄ when charge-transfer between the NO₂ moieties is not considered. Therefore, the N-N bond number (i.e. the number of pairs of electrons that form the N-N bond) for N₂O₄ must be smaller than the bond-number of unity that pertains for the N-N single-bond of N₂H₄ (as in H₂ $\overset{+}{\text{N}}\text{---}\overset{-}{\text{N}}\text{H}_2$). A bond-number which is less than unity implies that the N-N bond is longer than a single bond. Estimates of the N-N bond-number are 0.34 from the bond-length⁹ and 0.24 from the photo-electron spectrum^{7c}.

By bonding together the NO_2 valence-bond structures of types (2) and (4) of Section 6-1, valence-bond structures of type (7) are obtained for N_2O_4 . These latter structures also participate in resonance with the structures of types (3)-(6).



In valence-bond structures (6) and (7), a lone-pair of electrons occupies each of the nitrogen hybrid atomic orbitals (h_2 and h_3 of Fig. 7-2) that pertain to the N-N σ -bond of structure (3). For this pair of orbitals, the overlap integral is 0.3, and therefore non-bonded repulsions (Section 3-10) between the nitrogen atoms will be established as a consequence of the contributions of structures (6) and (7) to the ground-state resonance. This repulsion will also lead to some lengthening of the N-N bond.

It has been suggested that the N-N bond-number for N_2O_4 is equivalent to the nitrogen odd-electron charge for the NO_2 monomer⁹. In Section 6-1, a value of approximately 0.5 was assigned to this odd-electron charge. If no reorganization of the electronic structure of NO_2 is assumed to occur when NO_2 dimerizes, then it has been argued that spin-pairing of the nitrogen odd-electron charge of 0.5 for each monomer generates an N-N σ -bond-number of 0.5 for the dimer, i.e. one half of an N-N electron-pair is formed for the N_2O_4 dimer. This argument is not valid^{7b,10}. Inspection of the valence-bond structures (3)-(5) shows that a nitrogen atom can share its odd-electron charge to form a "long" N-O bond as well as the N-N bond. Consequently, resonance between (3)-(6) must generate an N-N bond-number of 0.25 for N_2O_4 if the nitrogen odd-electron charge for NO_2 is 0.5. (To obtain a nitrogen odd-electron charge of 0.5, structures (1) and (2) for NO_2 must have equal weights. Therefore, the weights for the N_2O_4 structures (3)-(6) are each equal to 0.25.)

Each of the N_2O_4 Lewis structures (3)-(7) obeys the Lewis-Langmuir octet rule for atoms of first-row elements (Section 2-4a), and four of these structures have a "long-bond" linking a pair of non-adjacent atoms. Why should these latter structures be considered to be of importance for the ground-state resonance description of N_2O_4 ? In Section 2-4, we have referred to the electroneutrality principle, which states that if atoms of a neutral molecule have similar electronegativities, the atomic formal charges for the ground-state of the molecule will have small magnitudes. For N_2O_4 , appreciable weights for at least some of the "long-bond" structures (4)-(7) (whose formal charges are smaller than are those for the standard Lewis structure (3)) help ensure that this requirement is satisfied.

Because each NO_2 moiety of structures (3)-(7) has 17 valence-shell electrons, these structures will be referred to as "covalent" structures with the electron distributions of NO_2NO_2 . In Section 7-3, "ionic" or charge-transfer structures of the type $\text{NO}_2^+\text{NO}_2^-$ (or $\text{NO}_2^-\text{NO}_2^+$) will also be included in the description of the electronic structure. As is the case for H_2 (Section 3-3), the ionic structures are less important than are the corresponding covalent structures for the ground-state resonance^{7b,c,10}.

Molecular orbital calculations for NO_2 and N_2O_4 , with configuration interaction (C.I.) (Sections 3-3 and 10-3) included for N_2O_4 , have been parameterized so that the experimental values for the first two ionization potentials of NO_2 , the first ionization potential of N_2O_4 , and the nitrogen odd-electron charge of NO_2 (Section 6-1) are reproduced^{7b,c,13}. The NO_2 parameters have been carried over into the N_2O_4 calculations. From the MO-CI wave-function for N_2O_4 , weights of 0.24, 0.24, 0.24, 0.13 and 0.13 have been calculated for sets of covalent structures of types (3)-(7). The remaining weight of 0.02 is shared amongst various ionic structures. The covalent weights are very similar to those obtained from spin-pairing the odd-electrons of two NO_2 monomers with nitrogen odd-electron charges of 0.5, namely 0.25, 0.25, 0.25, 0.125 and 0.125, and support the hypothesis that dimerization of NO_2 involves primarily the spin-pairing of the odd-electrons of two NO_2 radicals.

The odd-electron of NO_2 is delocalized amongst a nitrogen hybrid atomic orbital and the oxygen $2p\bar{\pi}$ -orbitals that overlap with this nitrogen orbital. The three orbitals are displayed in Figure 6-1. The atomic orbitals whose occupancies differ in valence-bond structures (3)-(7) for N_2O_4 are therefore those that are displayed in Figure 7-2, namely two nitrogen hybrid and four oxygen $2p\bar{\pi}$ -orbitals, which are designated as "mobile σ -electron" orbitals^{6,7,10-13}. The "mobile σ -electron" wave-wave functions for the electron-pair bonds of (3)-(7) are assumed to be constructed using the Heitler-London procedure (Section 3-3). For example, the wave-function for the N-N bond of the standard Lewis structure (3) is $h_2(1)h_3(2) + h_3(1)h_2(2)$ in which h_2 and h_3 are the hybrid orbitals displayed in Fig. 7-2. But it is also possible to construct a molecular orbital wave-function for this bond, namely $\sigma(1)\sigma(2)$ for which $\sigma = h_2 + h_3$ is the N-N bonding molecular orbital. We shall now use this latter formulation of the N-N bond wave-function to provide a molecular orbital explanation^{11,12} for the existence of a long, weak N-N bond for N_2O_4 .

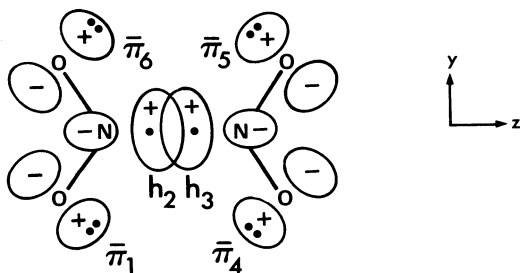


Figure 7-2 Mobile σ -electron atomic orbitals for planar N_2O_4 isomer⁷.

7-2 THE LONG WEAK N-N BOND OF N_2O_4 : MOLECULAR ORBITAL THEORY^{11,12}

For the molecular orbital description of the N-N bond of structure (3), two electrons with opposite spins occupy the N-N σ -bonding molecular orbital $\sigma = h_2 + h_3$. In this structure, the oxygen $2p\bar{\pi}$ orbitals, which overlap with the orbitals that form the N-N bond, are all doubly-occupied. However, the appreciable electronegativity of N^+ relative to O^- in structures of type (3) induces some delocalization of the oxygen $2p\bar{\pi}$ electrons into the antibonding N-N σ^* -orbital, $\sigma^* = h_2 - h_3$, which is vacant in these structures. The N-N σ -bond order[†] is then reduced below the value of unity that pertains to (3), thereby generating a long, weak N-N bond. An estimate of 0.525 for this bond-order has been obtained from molecular orbital studies of the photoelectron spectrum^{7c}.

To obtain the "long-bond" Lewis structures (4)-(6) from the standard Lewis structure (3), either one or two electrons have been delocalized from the oxygen $\bar{\pi}_1$ and $\bar{\pi}_4$ orbitals of Figure 7-2 into the singly occupied nitrogen hybrid orbitals h_2 and h_3 . We shall now use these orbitals to construct the 4-centre delocalized molecular orbitals for the mobile σ -electrons. (A fuller treatment that includes the $\bar{\pi}_5$ and $\bar{\pi}_6$ orbitals is described in Refs. 7b,c,11 and 12.)

Initially we shall form the bonding and antibonding linear combinations of each pair of nitrogen and oxygen atomic orbitals. The resulting symmetry orbitals are given in Eqs. (1) and (2), in which for simplicity only we have omitted the overlap integrals from the normalization constants. The symmetry orbitals s_1 and s_2 are the N-N σ -bonding and σ^* -antibonding molecular orbitals. The s_1 and s_3 orbitals are symmetric with respect to reflection through the xy plane of symmetry (Fig. 7-2), whereas s_2 and s_4 are antisymmetric with respect to this reflection. Because orbitals with the same symmetry can overlap, we may linearly combine s_1 with s_3 , and s_2 with s_4 , to obtain the delocalized 4-centre molecular orbitals of Eqs. (3)-(6). The parameters λ and μ are constants, both > 0 . In particular, as will become more evident below, the parameter μ provides a measure of the extent of delocalization of the oxygen $2p\bar{\pi}$ electrons into the antibonding σ^* orbital (s_2).

$$s_1 = (h_2 + h_3)/2^{1/2}, \quad s_2 = (h_2 - h_3)/2^{1/2}, \quad (1)$$

$$s_3 = (\bar{\pi}_1 + \bar{\pi}_4)/2^{1/2}, \quad s_4 = (\bar{\pi}_1 - \bar{\pi}_4)/2^{1/2}, \quad (2)$$

$$\psi_1 = (s_3 + \lambda s_1)/(1 + \lambda^2)^{1/2} \equiv (\bar{\pi}_1 + \lambda h_2 + \lambda h_3 + \bar{\pi}_4)/\{2(1 + \lambda^2)\}^{1/2} \quad (3)$$

$$\psi_2 = (s_4 + \mu s_2)/(1 + \mu^2)^{1/2} \equiv (\bar{\pi}_1 + \mu h_2 - \mu h_3 - \bar{\pi}_4)/\{2(1 + \mu^2)\}^{1/2} \quad (4)$$

$$\psi_3 = (\lambda s_3 - s_1)/(1 + \lambda^2)^{1/2} \equiv (\lambda \bar{\pi}_1 - h_2 - h_3 + \lambda \bar{\pi}_4)/\{2(1 + \lambda^2)\}^{1/2} \quad (5)$$

$$\psi_4 = (\mu s_4 - s_2)/(1 + \mu^2)^{1/2} \equiv (\mu \bar{\pi}_1 - h_2 + h_3 - \mu \bar{\pi}_4)/\{2(1 + \mu^2)\}^{1/2} \quad (6)$$

[†] These delocalizations are calculated to occur¹² at the N-N single-bond length of 1.45 Å as well as at the experimental length of 1.78 Å.

Inspection of the signs of the atomic orbital coefficients shows that molecular orbital ψ_4 is both N-N and N-O antibonding, and therefore it is the highest energy molecular orbital for the mobile σ -electrons. For the six electrons that occupy the $\bar{\pi}_1$, h_2 , h_3 and $\bar{\pi}_4$ orbitals of Fig. 7-2, the molecular orbital configuration of lowest energy is given by Eqn. (7), with orbital ψ_4 vacant.

$$\Psi_1(\text{MO}) = (\psi_1)^2(\psi_2)^2(\psi_3)^2 \quad (7)$$

It is instructive to transform the molecular orbitals of Eqn. (7) by applying the identity that we have deduced in Section 3-5 (or Section 3-7), namely

$$(a + kb)^1(k^*a - b)^1 = -(1 + kk^*)(a)^1(b)^1 \quad (8)$$

provided that the two electrons that occupy the bonding and antibonding orbitals $a + kb$ and $k^*a - b$ have parallel spins. Because the overlap integrals have been omitted from the normalization and orthogonality relationships, the molecular orbitals of Eqs. (3)-(6) are normalized and orthogonal. For these orbitals, the appropriate form of Eqn. (8) is Eqn. (9), in which a and b now correspond to a pair of symmetry orbitals from Eqs. (1) and (2), and k is either λ or μ .

$$\{(a + kb)/(1 + k^2)^{1/2}\}^1\{(ka - b)/(1 + k^2)^{1/2}\}^1 = -(a)^1(b)^1 \quad (9)$$

When this identity is applied to the ψ_1 and ψ_3 orbitals of Eqn. (7), we obtain Eqn. (10), which shows that the N-N σ -bonding orbital s_1 is doubly occupied regardless of the value of μ in molecular orbital ψ_2 .

$$\Psi_1(\text{MO}) = (\psi_1)^2(\psi_2)^2(\psi_3)^2 \equiv (s_1)^2(\psi_2)^2(s_3)^2 \quad (10)$$

If the parameter μ is set equal to zero in the ψ_2 of Eqn. (4), then $\psi_2 = s_4$, and $\Psi_1(\text{MO})$ reduces to $(s_1)^2(s_4)^2(s_3)^2 \equiv (s_1)^2(\bar{\pi}_1)^2(\bar{\pi}_4)^2$. This latter configuration corresponds to double-occupancy of the $\bar{\pi}_1$ and $\bar{\pi}_4$ orbitals of Fig. 7-2, i.e. no delocalization of electrons has occurred from these orbitals. When $\mu \neq 0$, the s_4 and s_2 symmetry orbitals mix according to Eqn. (4), i.e. $\bar{\pi}$ -electrons delocalize into the antibonding N-N σ^* orbital which is vacant in the standard Lewis structure (3). The parameter μ therefore provides a measure of the extent of this delocalization, which may be calculated from the N-N σ -bond order for $\Psi_1(\text{MO})$ of Eqn. (7). Using the bond-order formula of Eqn. (3-43), together with the molecular orbital coefficients of Eqs. (3)-(5), this bond-order may be expressed as $1/(1 + \mu^2)$. (This formula is also appropriate¹² when the $\bar{\pi}_5$ and $\bar{\pi}_6$ atomic orbitals of Fig. 7-2 are included to construct 6-centre molecular orbitals.) With $1/(1 + \mu^2) = 0.525$, $\mu = 0.951$ is obtained.

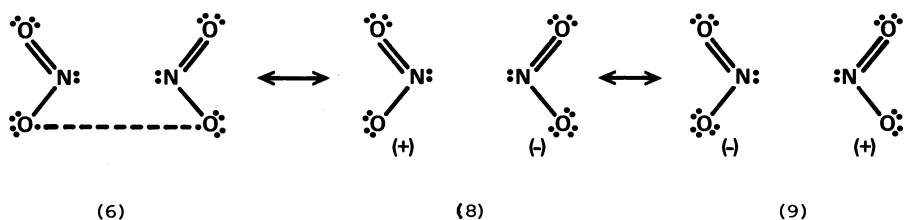
Further transformations of the orbitals for molecular orbital configuration $\Psi_1(\text{MO})$ are possible, but a discussion of them will be postponed until Chapter 10. These transformations enable a connection to be made between the molecular orbital and valence-bond descriptions of the electronic structure of N_2O_4 that we have described here.

The results of some recent molecular orbital calculations¹⁴⁻¹⁸ that treat explicitly either all of the electrons or all of the valence-shell electrons, support the molecular orbital theory^{11,12} that has been described in this Section. It may also be noted that the "through-bond" coupling¹⁹ of lone-pair orbitals over three σ -bonds is equivalent to lone-pair delocalization into the antibonding σ^* orbital between the central σ -bond.

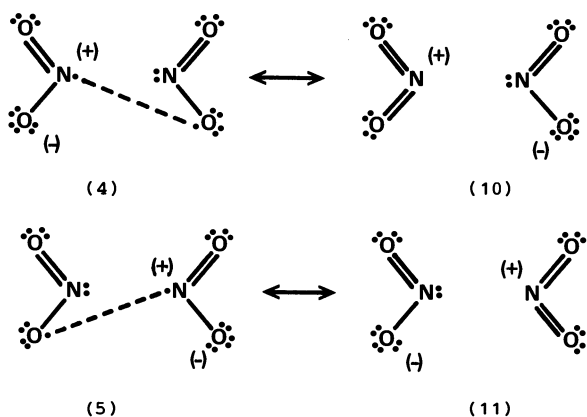
7-3 THE PLANARITY OF N_2O_4 , COVALENT-IONIC RESONANCE AND CIS O-O PAULING "3-ELECTRON BONDS"

The planarity of N_2O_4 is concomitant with a barrier to rotation^{1,20} around the N-N bond of 8-12 kJ mol^{-1} . The origin of this barrier was initially associated with weak π -bonding across the N-N bond²¹. However, the results of molecular orbital calculations^{14,15,22} now indicate that the overlap between σ -orbitals on pairs of cis oxygen atoms provides the primary contribution to this barrier. For these calculations, the oxygen orbitals were oriented parallel to the N-N bond axis. For the valence-bond structures (3)-(7), the corresponding oxygen orbitals are the $2p\bar{\pi}$ -orbitals of Fig. 7-2. The overlap integral between a pair of cis $2p\bar{\pi}$ -orbitals (e.g. $\bar{\pi}_1$ and $\bar{\pi}_4$, or $\bar{\pi}_5$ and $\bar{\pi}_6$) is 0.01^{7a}. Using valence-bond theory, we shall now give consideration to how this overlap can generate a contribution to the rotation barrier. Fuller numerical details are provided in Refs. 7a and 7c.

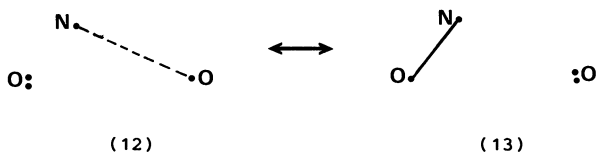
For valence-bond structure (6), there is a "long" cis O-O bond formed by the overlap of singly-occupied $2p\bar{\pi}$ -orbitals. If this structure has appreciable weight in the ground-state resonance description of the electronic structure, it might be thought that this bond could provide the valence-bond explanation of the cis O-O contribution to the barrier. However, it has been calculated^{7a} that this bond has negligible strength ($< 0.2 \text{ kJ mol}^{-1}$), and that it is not appreciably strengthened when (6) participate in resonance with the ionic ($\text{NO}_2^+\text{NO}_2^-$ and $\text{NO}_2^-\text{NO}_2^+$) structures (8) and (9) (c.f. the covalent-ionic resonance $\text{H}-\text{H} \leftrightarrow \text{H}^+ \text{:H}^- \leftrightarrow \text{H}^- \text{:H}^+$ for H_2 of Section 3-3).

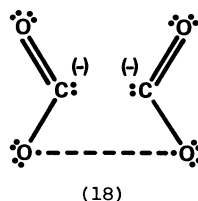
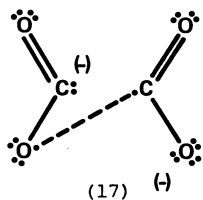
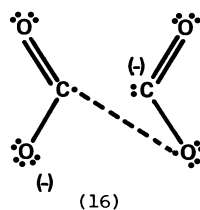
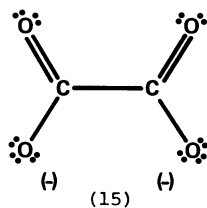


A much larger cis O-O binding energy of 20 kJ mol^{-1} is calculated when each of the covalent structures (4) and (5) participate in resonance with the ionic structures (10) and (11). It is this resonance that has been calculated to be primarily responsible for the cis O-O overlap contribution to the rotation barrier for N_2O_4 .



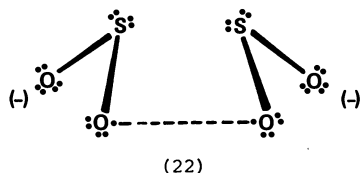
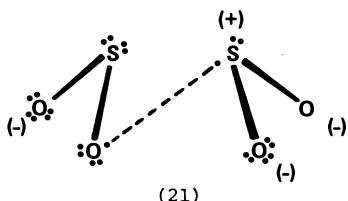
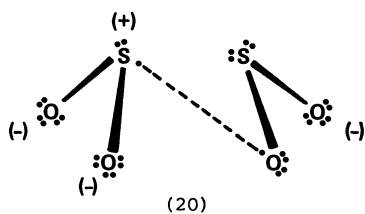
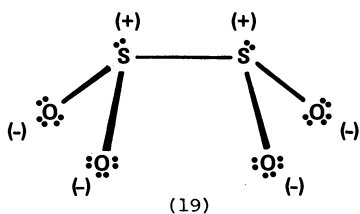
It is of interest to examine the nature of the electronic reorganization that occurs when (4) participates in resonance with (10). In structures (12) and (13), we have separated out the relevant electrons, namely those that occupy the oxygen $\bar{\pi}_1$ and $\bar{\pi}_4$ orbitals, and the nitrogen hybrid orbital h_2 . Inspection of these latter structures reveals that the (4) \leftrightarrow (10) resonance leads to the development of a Pauling "3-electron bond" ($O \bullet \bullet O \equiv \ddot{O} \bullet \ddot{O} \equiv (O \bullet \bullet O) \leftrightarrow (O \bullet \bullet O)$) between the cis oxygen atoms. We may therefore associate the cis O-O overlap contribution to the rotation barrier with the formation of this type of bond.





A Lewis-type valence-bond explanation for the difference in N-N and C-C bond-lengths may also be provided. When CO_2^- monomers with the valence-bond structures (13) and (15) of Section 6-2 dimerize, the Lewis structures of types (15)-(18) are obtained, which are equivalent to structures (3)-(6) for N_2O_4 . For $\text{C}_2\text{O}_4^{2-}$, the formal charge arrangements for (16)-(18) are no better than are those for the standard Lewis structure (15). Therefore, the "long-bond" structures (16)-(18) with no C-C bonds would be expected to make a smaller contribution to the ground-state resonance than do the corresponding structures (4)-(6) for N_2O_4 . Consequently, the standard Lewis structure (15) with a C-C σ -bond has a larger weight than has (3) (with an N-N σ -bond for N_2O_4), thereby generating a larger C-C bond-number for $\text{C}_2\text{O}_4^{2-}$.

The dithionite anion $\text{S}_2\text{O}_4^{2-}$, which is the dimer of SO_3^- (Section 6-3) is non-planar^{24,25}. The S-S bond-length of 2.39 Å for this dimer^{24,25} is 0.33 Å longer than the S-S single-bond of H_2S_2 ²⁶. The standard (octet) Lewis structure (19) has a lone-pair of electrons on each of the sulphur atoms, and these should be responsible for the non-planarity (c.f. non-planar $:\text{NH}_3$ and $:\text{SO}_3^-$, each of which has a lone-pair of electrons on the nitrogen or sulphur atom). Because of the non-planarity, the lone-pair $2p\pi$ and $2p\bar{\pi}$ orbitals on each oxygen atom can both overlap with the atomic orbitals that form the S-S σ -bond of (19). The S^+ of (19) should be strongly electronegative relative to the O^- , thereby inducing appreciable delocalization of the oxygen π and $\bar{\pi}$ electrons into the antibonding S-S σ^* orbital. An S-S σ -bond-order which is rather less than unity will then result, and so the S-S bond will be lengthened relative to the single-bond length^{12a}.



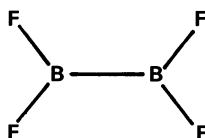
A Lewis-type valence-bond explanation²⁷ for the existence of a long S-S bond in $S_2O_4^{2-}$ is the following. On dimerization of the SO_2^- valence-bond structures (24) and (26) of Section 6-3 (with a sulphur atom replacing the central oxygen atoms of these structures) we obtain the Lewis structures (19)-(22). The nature of the formal charge distributions - particularly that of (22) - implies that the "long-bond" structures (20)-(22) with no S-S bonds should have appreciable weights. One consequence of this is that the S-S bond-number for $S_2O_4^{2-}$ must be rather less than unity, and the S-S bond is therefore longer than a single bond.

In (22), the sulphur orbitals that form the S-S σ -bond of (19) are both doubly-occupied. As is the case for N_2O_4 (Section 7-1), the resulting non-bonded repulsions must contribute to some of the lengthening of the S-S bond.

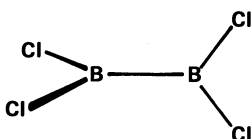
7-5 B_2Y_4 (Y = F, Cl or Br), N_2F_4 AND P_2F_4

The A-A bond-lengths for some A_2Y_4 systems, with A \equiv B, N or P, and Y \equiv halogen, are reported in Table 7-1. These lengths are a little longer than the single bonds of B_2H_4 , N_2H_4 and P_2H_4 , and may be attributed to a small amount of delocalization of halogen $p\bar{m}$ electrons into the antibonding A-A σ^* orbitals which are vacant in the Lewis structures (23)-(25). Alternatively, the odd electron for each of the AY_2 monomers (Table 6-1) is not localized entirely in a boron, nitrogen or phosphorus atomic orbital, and on dimerization an incomplete electron-pair bond is formed between pairs of these atoms. Consequently, valence-bond structures of the type (26)-(28) for B_2F_4 , for example, must also contribute slightly to the ground-state resonance description of the electronic structure. If dimerization is assumed to

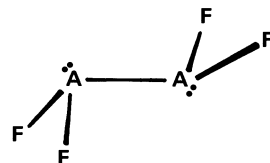
involve solely the spin-pairing of the odd-electrons of the monomers, then a boron odd-electron charge of 0.93 for BF_2 generates a weight (Section 7-1) of 0.86 for valence-bond structure (23), i.e. the B-B bond-number is 0.86. For NF_2 and PF_2 , the odd-electrons occupy π -electron molecular orbitals (c.f. Section 6-4), but spin-pair to form σ -bonds in the dimers. Therefore it may be less appropriate to obtain realistic estimates of the A-A bond-numbers for N_2F_4 and P_2F_4 from the odd-electron charges of the monomers. However, they should provide a qualitative guide to the relative importance of the different types of structures.



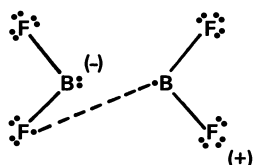
(23)



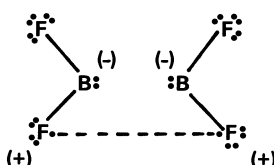
(24)



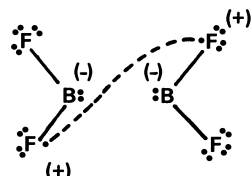
(25)



(26)



(27)



(28)

B_2H_4	1.644 ^a , 1.619 ^b	N_2H_4	1.453 ^d
B_2F_4	1.720 ^c	N_2F_4	1.489 ^e , 1.495 ^f
B_2Cl_4	1.702 ^c	P_2H_4	2.216 ^g
B_2Br_4	1.689 ^c	P_2F_4	2.281 ^h

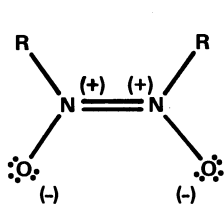
Table 7-1 A-A bond-lengths for A_2H_4 and A_2Y_4 (Y = halogen) molecules.

REFERENCES: (a) (Calc.). P. Dill, V.R. Schleyer and J.A. Pople, *J. Amer. Chem. Soc.*, 97, 3402 (1975). (b) (Calc.). I.M. Peperberg, T.A. Halgren and W.N. Lipscomb, *Inorg. Chem.* 16, 363 (1977). (c) D.D. Danielson and K. Hedberg, *J. Amer. Chem. Soc.*, 101, 3199 (1979) and references therein. (d) Ref. 3. (e) M.J. Cardillo and S.H. Bauer, *Inorg. Chem.*, 8, 2086 (1969). (f) M.M. Gilbert, G. Gundersen and K. Hedberg, *J. Chem. Phys.*, 56, 1691 (1972). (g) B. Beagley, A.R. Conrad, J.M. Freeman, J.J. Monaghan, B.G. Noron and G.C. Holywell, *J. Mol. Struct.*, 11, 371 (1972). (h) H.L. Hodges, L.S. Su and L.S. Bartell, *Inorg. Chem.*, 14, 599 (1975).

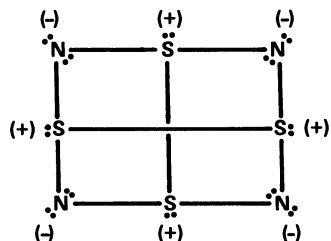
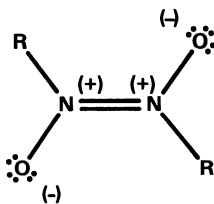
In the gas phase, B_2F_4 is planar, and B_2Cl_4 and B_2Br_4 have perpendicular conformations; experimental estimates (Ref. (c) of Table 7-1) of the rotation barriers relative to the most stable conformers are 1.8, 7.7 and 12.1 kJ mol^{-1} .

7-7 C-NITROSO DIMERS AND S_4N_4

In their standard Lewis structures (1) and (19), both N_2O_4 and $S_2O_4^{2-}$ carry positive formal charges on the adjacent nitrogen and sulphur atoms. The presence of such charges helps to induce considerable delocalization of oxygen lone-pair electrons into an antibonding σ^* -orbital between the nitrogen or sulphur atoms, with a consequent lengthening of the N-N and S-S bonds relative to single-bond lengths. A similar arrangement of positive formal charges occurs in the standard Lewis structures for a number of other molecular systems^{6,12a,28-30} and we shall discuss two examples here, namely the C-nitroso dimers $(RNO)_2$ ($R = \text{alkyl or aryl}$) and S_4N_4 . The standard Lewis structures for these molecules, (32) and (33), carry positive formal charges on the adjacent nitrogen and sulphur atoms respectively. If we assume that the rather greater electronegativity of the N^+ and S^+ relative to the O^- and N^- leads to appreciable delocalization of the O^- and N^- lone-pair electrons into the antibonding N-N σ^* and S-S σ^* orbitals that are vacant in (32) and (33), we can explain the observed lengthenings of the N-N and S-S bonds relative to double and single bond lengths. For a number of C-nitroso dimers, the N-N bond-lengths range in value between 1.30 \AA and 1.32 \AA ³¹; the length of an N-N double bond (as in $CH_3N=CH_3$) is 1.24 \AA . For S_4N_4 , the S-S bond-lengths of 2.58 \AA ³² may be compared with the S-S single-bond length of 2.06 \AA .

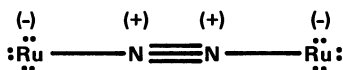


(32)

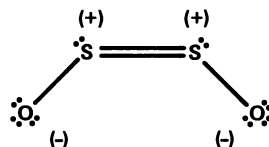


(33)

Other systems with adjacent positive charges in their standard Lewis structures include $Ru(II)-N_2-Ru(II)$ and S_2O_2 . Their standard Lewis structures are (34) and (35), and the bonding for these systems is discussed in Sections 18-2 and 11-7.



(34)



(35)

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CHAPTER 8

SOME Cu(II) BINUCLEAR TRANSITION-METAL COMPLEXES

With little modification, we may use the N_2O_4 valence-bond and molecular orbital theory of Sections 7-1 and 7-2 to examine the magnetic behaviour for some binuclear Cu(II) complexes with $(3d)^9$ configurations for the Cu^{2+} ions. As examples, we shall consider the Cu(II)-carboxylate, Cu(II)-chloro and Cu(II)-hydroxo dimers ($Cu_2(RCO_2)_4L_n$ with $n = 0$ or 2, and $Cu_2X_2^{2+}$ with $X = Cl$ or OH) with the geometries¹⁻³ displayed in Fig. 8-1. Initially we shall not include the copper 4s and 4p orbitals in the bonding schemes.

8-1 Cu(II) CARBOXYLATE DIMERS, $Cu_2(RCO_2)_4L_n$

8-1(a) Valence-Bond Structures For those Cu(II) carboxylate dimers that have the geometries displayed in Fig. 8-1, singly-occupied $3d_{x^2-y^2}$ orbitals of the Cu^{2+} ions can overlap with a lone-pair atomic orbital on each of the oxygen atoms of the carboxylate ligands, as shown in Fig. 8-2 for two ligands. The $3d_{x^2-y^2}$ orbitals also overlap with each other to form a very weak δ -bond⁴. In Fig. 8-2, each O-Cu(II)-O moiety involves five electrons and three overlapping atomic orbitals, as is also the case for NO_2 and both O-N-O linkages of N_2O_4 (see Figs. 6-1 and 7-2). The Cu^{2+} ions of Cu(II) carboxylate dimers are equivalent⁵ to the nitrogen atoms of NO_2 and N_2O_4 . Therefore, for each O-Cu(II)-O moiety, with one unpaired or magnetic electron, we may write down Lewis structures of the types (1), (2) and (3); resonance between them may be summarized by using the Pauling "3-electron bond" structures (4) and (5).

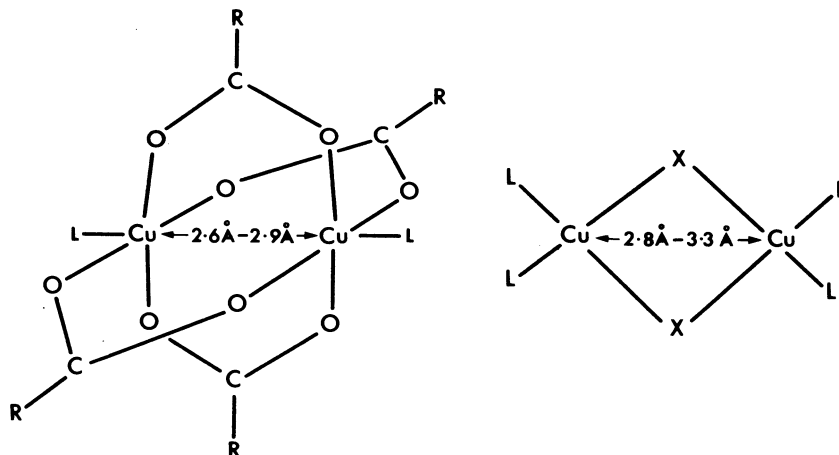
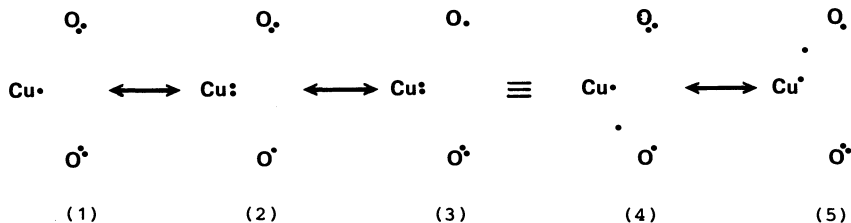


Figure 8-1 Geometrical structures for some Cu(II) carboxylate, hydroxo and chloro dimers.



The atomic orbitals for each O-Cu(II)-O moiety of Fig. 8-2 overlap weakly with those of the other moiety which involves the same RCO_2^- ligands. Therefore, the delocalized magnetic electrons of the two moieties may be spin-paired to generate the $S = 0$ valence-bond structures[†] of the types (6)-(9) (together with equivalent mirror-image structures). These structures have the same distribution for the delocalized bond (\longleftrightarrow) as have the N_2O_4 structures (3)-(7) of Section 7-1. With respect to each O-N-O or O-Cu(II)-O moiety, both sets of structures are of the "covalent" type.

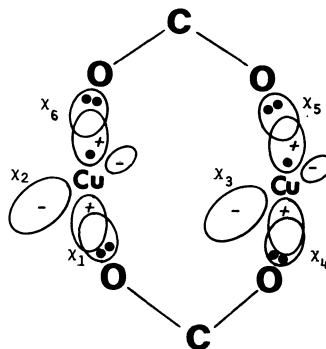
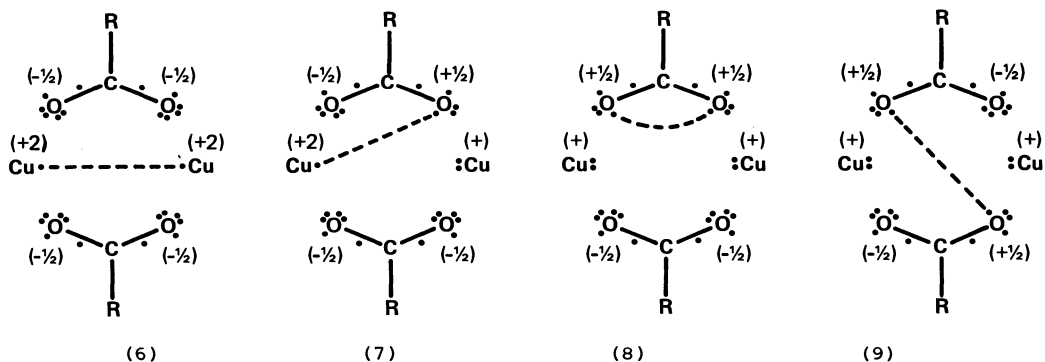


Figure 8-2 Overlap of copper $3d_{x^2-y^2}$ orbitals with oxygen lone-pair orbitals of two carboxylate ligands. The overlap between the copper orbitals generates Cu-Cu δ bonding.



[†] With respect to formal charge distribution, the Linnett structure (Section 2-2) $\text{R}-\text{C} \begin{matrix} \text{O}^{(-\frac{1}{2})} \\ \text{O}^{(-\frac{1}{2})} \end{matrix}$ that we have used for the carboxylate linkages in (6)-(9) is equivalent to that obtained from resonance between the standard Lewis structures $\text{R}-\text{C} \begin{matrix} \text{O}^{(-)} \\ \text{O}^{(-)} \end{matrix}$ and $\text{R}-\text{C} \begin{matrix} \text{O}^{(-)} \\ \text{O}^{(-)} \end{matrix}$

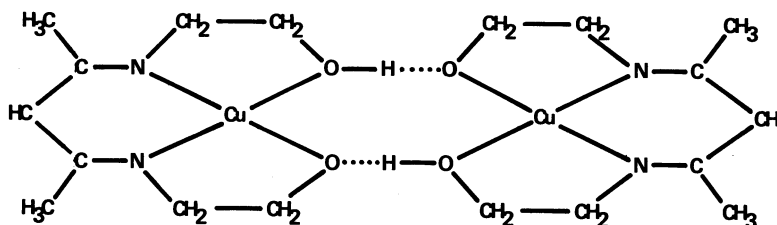
The Cu-Cu δ -bond of (6) corresponds to the N-N σ -bond of (3) in Section 7-1. However, whereas the overlap integral involving the nitrogen hybrid orbitals of Fig. 7-2 has an appreciable magnitude (≈ 0.3), the overlap integral for the copper $3d_{x^2-y^2}$ orbitals of Fig. 8-2 is very small^{4,6} (0.003-0.01). If it is assumed that the magnetic electrons of the Cu(II) carboxylate dimers are localized entirely in these copper orbitals, only a very weak Cu-Cu interaction can occur⁴⁻⁸. The results of some molecular orbital calculations⁷ indicate that the magnetic electrons can be significantly located in the oxygen as well as the copper atomic orbitals (as occurs in valence-bond structures (7)-(9)), and that the overlap between each pair of cis-oxygen atomic orbitals (overlap integral for sp^2 hybridization = 0.012) provides a stronger spin-coupling of the two magnetic electrons than does the $3d_{x^2-y^2} - 3d_{x^2-y^2}$ overlap. However, as we shall discuss in Section 8-1(c), the concomitant bonding interaction between two O-Cu(II)-O moieties arises primarily from covalent-ionic resonance of the Pauling "3-electron bond" type (c.f. Section 7-3) rather than from the spin-pairing of the unpaired-electrons in the covalent structures.

8-1(b) The Antiferromagnetism of Cu(II) Carboxylate Dimers Because the overlap between the atomic orbitals of two O-Cu(II)-O moieties is small, the spin-pairing of the two delocalized magnetic electrons to generate an $S = 0$ spin-state with antiparallel ($\uparrow\downarrow$) spins for the two electrons is weak. Little energy is required to uncouple their spins to generate an $S = 1$ excited state with parallel ($\uparrow\uparrow$) spins for these electrons. Measurements of the temperature-dependent magnetic susceptibilities for a large number of Cu(II) carboxylate dimers^{2,9} indicate that for each of these complexes an $S = 1$ excited state lies only ≈ 100 -500 cm^{-1} (1-6 kJ mol^{-1}) above the $S = 0$ ground-state[†]. In Table 8-1, we have reported these energy separations ($-2J \equiv E(S = 1) - E(S = 0)$) for a selection of these compounds. By contrast, the much larger overlap which exists between the nitrogen atomic orbitals that form the N-N σ -bond of N_2O_4 helps to generate a relatively stronger spin-coupling for the unpaired-electrons of the two NO_2 moieties. The dissociation energy of 57 kJ mol^{-1} for N_2O_4 (Section 7-1) reflects the stronger coupling relative to what occurs for the Cu(II) carboxylate dimers.

In Table 8-1, the lack of correlation that exists between the Cu-Cu bond-lengths and the energy separation between the $S = 0$ and $S = 1$ states suggests that the Cu-Cu δ bonding is not the primary antiferromagnetic interaction that occurs between the odd-electrons of the O-Cu(II)-O moieties. If it were, then a lengthening of the Cu-Cu bond would decrease the energy separation, because the overlap between the $3d_{x^2-y^2}$ orbitals would be smaller. It may also be noted that in Cu(II) complexes of amino alcohols (10), the Cu(II) ions are¹⁰ separated by 4.94 Å, and

† Because the $S = 1$ states are thermally accessible, these dimers exhibit antiferromagnetic behaviour. For some of the Cu(II)-hydroxo and chloro dimers of Section 8-2, the ground-states have $S = 1$ spin-states, and excited $S = 0$ spin-states are thermally accessible. When this occurs, the complex is ferromagnetic.

therefore for these complexes, no antiferromagnetic coupling could arise through spin pairing of the magnetic electrons if these electrons are located solely in the $d_{x^2-y^2}$ orbitals. However, $-2J$ has a value¹⁰ of $+95 \text{ cm}^{-1}$. This can only arise through cis O-O overlap, and the concomitant $S = 0$ stabilization becomes operative when oxygen lone-pair electrons delocalize into the $3d_{x^2-y^2}$ orbitals in a manner identical to that described for the Cu(II) carboxylate dimers. In general, if the primary interaction between the odd-electrons occur via some of the orbitals of the bridging ligand rather than through overlap of the metal-ion orbitals, the mechanism for the interaction is designated as a "superexchange" mechanism¹¹.



(10)

R	<u>L</u>	Cu-Cu(Å)	$-2J(\text{cm}^{-1})$	R	<u>L</u>	Cu-Cu(Å)	$-2J(\text{cm}^{-1})$
H	$\frac{1}{2}$ dioxan	2.58	+555	CH ₃	urea	2.637	----
H	NCS ⁻	2.716	+485	C ₂ H ₅	-----	2.578	+300
H	urea	2.657	----	C ₃ H ₇	-----	2.565	+322
CH ₃	H ₂ O	2.614	+284	CH ₂ Cl	α picoline	2.747	+321
CH ₃	H ₂ O	2.616	+284	CF ₃	quinoline	2.886	+310
CH ₃	pyridine	2.630	+325	Succinate	H ₂ O	2.610	+330
CH ₃	pyridine	2.645	----	o - BrC ₆ H ₄	H ₂ O	2.624	+250
CH ₃	quinoline	2.642	+320	Acetyl	-----	2.617	+340
CH ₃	NCS ⁻	2.643	+305	Salicylate			

Table 8-1 Cu-Cu bond-lengths and $-2J$ for dimeric copper (II) carboxylates, $\text{Cu}_2(\text{RCO}_2)_4 \cdot n\text{L}_n$, with $n = 0$ or 2.

8-1(c) Covalent-Ionic Resonance and the Antiferromagnetism of Cu(II) Carboxylate Dimers Because of the small overlap that exists between atomic orbitals located on non-adjacent atomic centres, the "long" Cu-O and O-O covalent bonds of structures (7)-(9) have negligible strengths. Therefore these structures are essentially degenerate with the corresponding $S = 1$ structures that have parallel spins for the two magnetic electrons. Similarly the small overlap between the $d_{x^2-y^2}$ orbitals for the Cu...Cu bond of (6) renders this structure

almost degenerate with the corresponding $S = 1$ structure. These types of near-degeneracies may be demonstrated easily by calculating $-2J$ for two hydrogen atoms separated so that the overlap between the $1s$ orbitals is 0.01 . A value of $-2J = 7 \text{ cm}^{-1}$ may be calculated¹² using tabulated values for the integrals¹³. A much larger stabilization of 240 cm^{-1} is obtained when the $S = 0$ covalent structure $\text{H}—\text{H}$ participates in resonance with the ionic structures $\text{H}^+ : \text{H}^-$ and $\text{H}^- : \text{H}^+$. For H_2 , the covalent-ionic resonance involves the two electrons that form the electron-pair bond. In Section 7-3, we have described how covalent-ionic resonance of the Pauling "3-electron bond" type ($\text{O} \cdot : \text{O} \leftrightarrow \text{O} : \cdot \text{O}$) in particular, leads to a substantial cis O-O overlap stabilization of the planar conformation for N_2O_4 . Similar types of covalent-ionic resonance are also responsible^{7,14} for the cis O-O overlap stabilization of the $S = 0$ state for the Cu(II) carboxylate dimers. This is most easily demonstrated by using molecular orbital descriptions for a pair of O-Cu(II)-O moieties, in the following manner.

For each O-Cu-O moiety, the molecular orbitals are given by Eqn. 6-1, in which y and b are oxygen atomic orbitals (e.g. χ_1 and χ_6 , or χ_4 and χ_5 of Fig. 8-2), and a is the copper orbital χ_2 or χ_3 . We shall designate these 3-centre molecular orbitals here as ϕ_i ($i = 1 - 3$) and ϕ'_i ($i = 1 - 3$), and construct the $S = 0$ and $S = 1$ configurations of Fig. 8-3 for the ten electrons. In them, the two magnetic electrons are located in the Cu-O antibonding molecular orbitals ϕ_3 and ϕ'_3 . If it is assumed that the $S = 0$ and $S = 1$ configurations ${}^1\psi_{\text{covalent}}$ and ${}^3\psi_{\text{covalent}}$ are degenerate, then the degeneracy can be removed through covalent-ionic resonance for the $S = 0$ state, i.e. by construction of the wave-function

$${}^1\psi = {}^1\psi_{\text{covalent}} + \lambda {}^1\psi_{\text{ionic}} \quad (1)$$

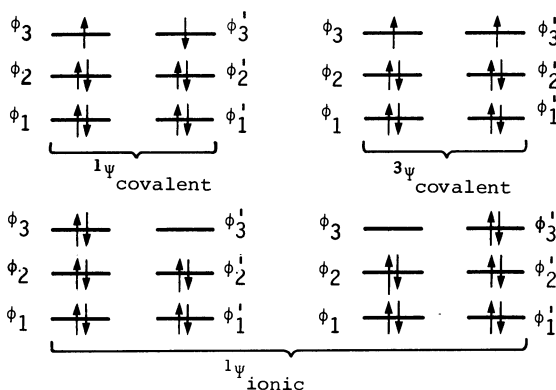


Figure 8-3 Covalent and ionic configurations for two O-Cu-O moieties.

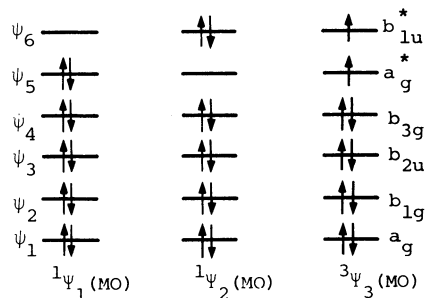
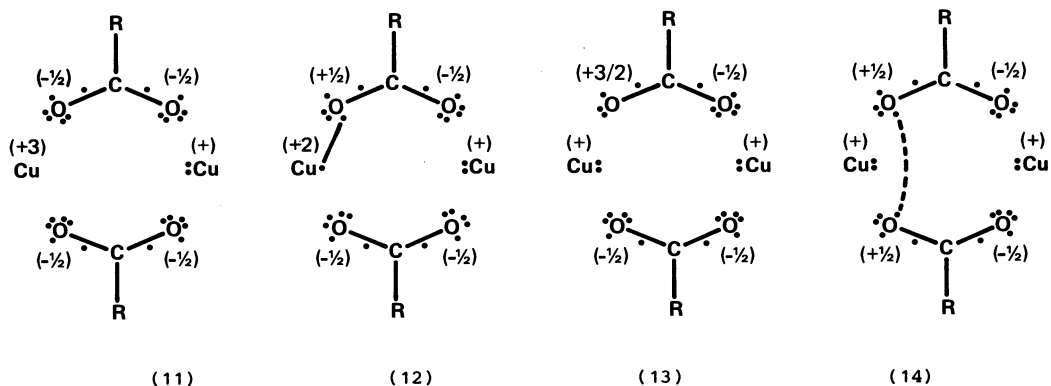


Figure 8-4 6-centre molecular orbital configurations for two O-Cu-O moieties.

At this level of approximation, the $S = 1$ state involves no ionic components. Small $S = 1$ ionic contributions do enter through consideration of excited configurations, but any additional stabilization of ${}^3\Psi_{\text{covalent}}$ through interaction with them will be of less importance than is that which arises for the $S = 0$ state through interaction of ${}^1\Psi_{\text{covalent}}$ with ${}^1\Psi_{\text{ionic}}$. The calculations of Ref. 7 provide a further illustration of this point.

We have already indicated that the valence-bond structures which contribute to ${}^1\Psi_{\text{covalent}}$ are of types (6)-(9), together with their equivalent forms. Similar structures with parallel spins for the two magnetic electrons contribute to ${}^3\Psi_{\text{covalent}}$. For ${}^1\Psi_{\text{ionic}}$, the component valence-bond structures are of types (11)-(14). The cis O-O overlap that has been calculated⁷ to be of primary importance for stabilization of the $S = 0$ state will manifest itself in covalent-ionic resonance of the types (7) \leftrightarrow (12), (8) \leftrightarrow (13) and (9) \leftrightarrow (14). The arrangements of formal charges for these structures indicate that the energy differences $E_{12} - E_7$ and $E_{14} - E_9$ will have smaller magnitudes than has $E_{13} - E_8$. Therefore the resonances of types (7) \leftrightarrow (12) and (9) \leftrightarrow (14) should be primarily responsible for the antiferromagnetism. These two resonances are of the Pauling "3-electron bond" type, i.e. they involve $\text{O}:\cdot\text{O} \leftrightarrow \text{O}\cdot:\text{O} \equiv \text{O}\cdot\cdot\text{O}$. The results of one set of calculations⁷ suggest that (9) \leftrightarrow (14) is more important than (7) \leftrightarrow (12), but further investigations are in progress¹² in order to ascertain whether or not this is a general result.



8-1(d) Covalent-Ionic Resonance and Approximate 6-Centre Molecular Orbitals

The covalent-ionic resonance described in the previous section may be related to an approximate 6-centre molecular orbital treatment for a pair of O-Cu(II)-O moieties. (The extension to form 10-centre molecular orbitals requires an elaboration of the 6-centre treatment). Because the overlap between the molecular orbitals ϕ_i and ϕ'_i of the two moieties is small, it is a good approximation to construct the canonical

molecular orbitals (ψ_i) with D_{2h} symmetry by adding and subtracting pairs of equivalent ϕ_i and ϕ_i' . Thus, ignoring overlap integrals in the normalizing constants, and assuming that the ϕ_i and ϕ_i' are normalized, we obtain

$$\begin{aligned}\psi_1 &= (\phi_1 + \phi_1')/2^{1/2} \quad , \quad \psi_2 = (\phi_1 - \phi_1')/2^{1/2} \\ \psi_3 &= (\phi_2 + \phi_2')/2^{1/2} \quad , \quad \psi_4 = (\phi_2 - \phi_2')/2^{1/2} \\ \psi_5 &= (\phi_3 + \phi_3')/2^{1/2} \quad , \quad \psi_6 = (\phi_3 - \phi_3')/2^{1/2}\end{aligned}\tag{2}$$

The $S = 0$ and $S = 1$ canonical molecular orbital configurations ${}^1\Psi_1(\text{MO})$, ${}^1\Psi_2(\text{MO})$ and ${}^3\Psi_3(\text{MO})$ of Fig. 8-4 transform with A_g , A_g and B_{1u} symmetries, respectively. By using the identity of Eqn. 3-15 for pairs of electrons with parallel spins - for example

$$\psi_1^\alpha \psi_2^\alpha \equiv -\phi_1^\alpha \phi_1'^\alpha \quad , \quad \psi_3^\alpha \psi_4^\alpha \equiv -\phi_2^\alpha \phi_2'^\alpha \quad \text{and} \quad \psi_5^\alpha \psi_6^\alpha \equiv -\phi_3^\alpha \phi_3'^\alpha$$

it is easy to deduce that

$${}^1\Psi_1(\text{MO}) = {}^1\Psi_{\text{covalent}} + {}^1\Psi_{\text{ionic}}\tag{3}$$

$${}^1\Psi_2(\text{MO}) = -{}^1\Psi_{\text{covalent}} + {}^1\Psi_{\text{ionic}}\tag{4}$$

$${}^3\Psi_3(\text{MO}) = {}^3\Psi_{\text{covalent}}\tag{5}$$

Configuration interaction (Section 3-3) is possible between the $S = 0$ configurations, to give

$${}^1\Psi(\text{CI}) = C_1 {}^1\Psi_1(\text{MO}) + C_2 {}^1\Psi_2(\text{MO})\tag{6}$$

$$\equiv (C_1 - C_2) {}^1\Psi_{\text{covalent}} + (C_1 + C_2) {}^1\Psi_{\text{ionic}}\tag{7}$$

In Section 10-3, the configuration interaction theory is described for (symmetrical) 6-electron 4-centre bonding units using non-approximate canonical molecular orbitals.

8-2 Cu(II)-X-Cu(II) LINKAGES

The 4-electron 3-centre bonding for linear triatomic M-X-M linkages has received much attention¹⁵⁻¹⁸ since it was first described by Kramers¹¹. For this type of linkage, the M are paramagnetic cations, each with a singly-occupied orbital

that overlaps with a doubly-occupied orbital of a closed-shell anion X (c.f. Figure 2-4 for $\text{Ni}^{2+}\text{O}^{2-}\text{Ni}^{2+}$). The paramagnetic cations are too widely separated for their orbitals to overlap significantly, and the phenomenon of superexchange (Section 8-1), i.e. the delocalization of electrons from the doubly occupied ligand orbital into the singly occupied cation orbitals, has been invoked to account for the observed antiferromagnetism of solids such as NiO and KNiF_3 with linear M-X-M linkages.

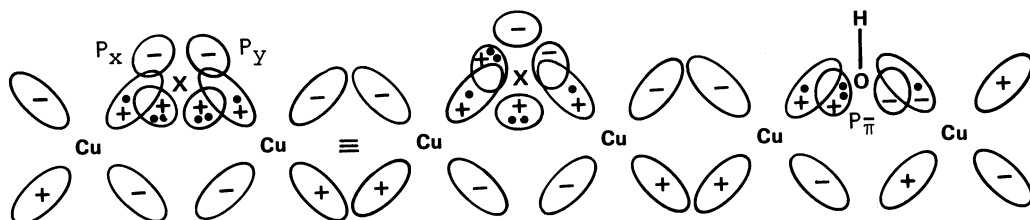


Figure 8-5 Atomic orbitals for Cu(II)-Cl-Cu(II) and Cu(II)-OH-Cu(II) linkages. The d-orbital for each Cu(II) ion may involve some hybridization with other d-orbitals; see for example Ref. 27.

In numerous binuclear transition metal complexes with M-X-M linkages, the M-X-M bond-angles deviate appreciably from 180° . For non-linear M-X-M linkages, a 6-electron 3-centre bonding unit may be established, as shown in Figure 8-5 for a Cu(II)-Cl-Cu(II) linkage of $\text{Cu}_2\text{Cl}_6^{2-}$. The singly-occupied orbital of the metal ion can overlap simultaneously with two orthogonal p orbitals on each ligand. Both ferro and antiferromagnetic complexes have been characterized. In Tables 8-2 and 8-3, we have reported experimental estimates of the values for the singlet-triplet energy separation ($-2J$) for some Cu(II)-OH-Cu(II) and Cu(II)-Cl-Cu(II) complexes. For the hydroxo-complexes, a near linear relationship has been found to exist³ between the M-OH-M bond-angle and $-2J$. (Some exceptions to this linear relationship have been more recently reported²⁰.) We shall now give consideration to the different types of theories that have been invoked to rationalize the variation in magnetic behaviour with bond-angle for M-X-M linkages.

	$-2J(\text{cm}^{-1})$	$\theta(^{\circ})$		$-2J(\text{cm}^{-1})$	$\theta(^{\circ})$
$[\text{Cu}(\text{bpy})\text{OH}]_2(\text{NO}_3)_2$	-172	95.6(1)	β - $[\text{Cu}(\text{dmaep})\text{OH}]_2(\text{ClO}_4)_2$	+200	100.4(1)
$[\text{Cu}(\text{bpy})\text{OH}]_2(\text{ClO}_4)_2$	-93	96.9(2)	$[\text{Cu}(\text{tmen})\text{OH}]_2(\text{ClO}_4)_2$	+360	102.3(4)
$[\text{Cu}(\text{bpy})\text{OH}]_2\text{SO}_4 \cdot 5\text{H}_2\text{O}$	-49	97.0(2)	$[\text{Cu}(\text{teen})\text{OH}]_2(\text{ClO}_4)_2$	+410	103.0(3)
$[\text{Cu}(\text{eaep})\text{OH}]_2(\text{ClO}_4)_2$	+130	98.8-99.5(3)	$[\text{Cu}(\text{tmen})\text{OH}]_2\text{Br}_2$	+509	104.1(2)

Table 8-2 $-2J$ and Cu-OH-Cu bond-angle for Cu(II) hydroxo-bridged dimers (bpy = 2,2'-bipyridine, eaep = 2-(2-ethylaminoethyl)pyridine, dmaep = 2-(2-dimethylaminoethyl)pyridine, tmen = N,N,N',N'-tetramethylethylenediamine, teen = N,N,N',N'-tetraethylethylenediamine).

	$-2J(\text{cm}^{-1})$	$\theta(^{\circ})$		$-2J(\text{cm}^{-1})$	$\theta(^{\circ})$
$[(\text{DMG})\text{CuCl}_2]_2^{\text{a}}$	-6.3	88	$[\text{Me}_2\text{NH}_2\text{CuCl}_3]_2$	+5	95.6
$[\text{Ph}_4\text{AsCuCl}_3]_2$	-33	93.6	$[\text{KCuCl}_3]_2$	+55	95.9
$[\text{LiCuCl}_3 \cdot 2\text{H}_2\text{O}]_2$	>0	95.1	$[(\text{Guan})\text{CuCl}_3]_2 \cdot 2\text{H}_2\text{O}$	+82.6	98
$\text{Cu}_2\text{Cl}_8^{4-}$	+14.6	95.2	$[(2\text{-Me(py)})_2\text{CuCl}_2]_2^{\text{c}}$	+7.4	101.4

Table 8-3 $-2J$ and bridging Cu-Cl-Cu bond angle for Cu(II) chloro dimers. From R.D. Willett, Chem. Comm. 607 (1973) and R.F. Drake, V.H. Crawford, N.W. Laney and W.E. Hatfield, Inorg. Chem. 13, 1246 (1974). ^aDMG = dimethylglyoximine ^bGuan = guaninium ^c2-Me(py) = 2-methylpyridine.

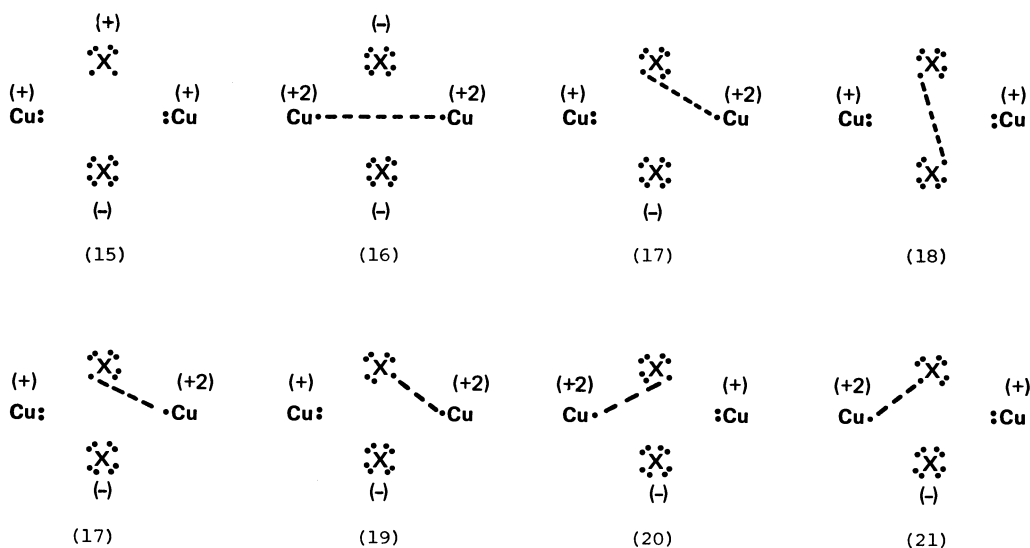
(a) van Kalkeren, Schmidt and Block¹⁶ have shown that if the M-X-M linkage is treated as a 4-electron 3-centre bonding unit for all bond-angles, the wave function for the valence-bond structure $\text{M} \cdot \overset{\cdot\cdot}{\underset{\cdot\cdot}{\text{X}}} \cdot \text{M}$ exhibits ferromagnetic coupling for the metal-ion electrons when the bridging bond-angle is around 90° , and antiferromagnetic coupling for rather smaller and larger bond-angles. In these calculations, full account is taken of the overlap that exists between the ligand and metal-ion orbitals, and no superexchange seems to be involved in the treatment. The $S = 0$ valence-bond structure $\text{M} \cdot \overset{\cdot\cdot}{\underset{\cdot\cdot}{\text{X}}} \cdot \text{M}$ is an example of a "long-bond" structure. A similar type of magnetic behaviour has been calculated by these workers using the molecular orbital procedures described in Refs. 8, 14 and 19 for the 4-electron 3-centre bonding unit.

(b) If the M-X-M linkages are treated as 6-electron 3-centre bonding units, an understanding of the magnetic behaviour must involve the following types of superexchange considerations¹⁴, for which the Goodenough-Kanamori theories²¹⁻²⁸ provide particular examples.

For the Cu(II) carboxylates, the $^1\psi_{\text{covalent}}$ and $^3\psi_{\text{covalent}}$ configurations of Figure 8-3 are essentially degenerate (Section 8-1(b)) if the very weak overlap that exists between the orbitals of two O-Cu-O moieties is neglected. However, for the Cu(II)-X dimers, $^3\psi_{\text{covalent}}$ must have significantly lower energy than $^1\psi_{\text{covalent}}$. This is primarily because although the two p-orbitals of each bridging ligand are orthogonal, the one-centre exchange integral $\iint p_x(1)p_y(2)r_{12}^{-1}p_y(1)p_x(2)d\mathbf{v}_1d\mathbf{v}_2$ has appreciable magnitude. Consequently, if the p-orbitals become singly-occupied, as in valence-bond structure (15), Hund's rule of maximum spin multiplicity (Section 1-2) requires that the electron spins be parallel in the lowest-energy state. Valence-bond structures of type (15), together with structures of types (16)-(18), are those that contribute to the $^1\psi_{\text{covalent}}$ and $^3\psi_{\text{covalent}}$ of Figure 8-3. The contribution of (15) with parallel spins to $^3\psi_{\text{covalent}}$ ensures that this latter function has a lower energy than has $^1\psi_{\text{covalent}}$ alone (with antiparallel spins for the two magnetic electrons of structures of types (15)-(18)). Therefore consideration of $^3\psi_{\text{covalent}}$ and $^1\psi_{\text{covalent}}$ leads to the prediction that Cu(II)-X

dimers have ferromagnetic ground-states, if each of (15)-(18) participates in resonance for both the $S = 0$ and $S = 1$ spin states. However, ${}^1\Psi_{\text{covalent}}$ can interact with ${}^1\Psi_{\text{ionic}}$, and some stabilization of ${}^1\Psi_{\text{covalent}}$ may then occur, the origin[†] of which is being currently investigated.

Thus, according to this 6-electron 3-centre analysis for Cu(II)-X-Cu(II) complexes, there is a competition between an tendency for ferromagnetism due to a preference for parallel spins in valence-bond structures of type (15), and a tendency for antiferromagnetism when the $S = 0$ covalent structures of types (17) and (20) participate in resonance with $S = 0$ ionic structures of types (19) and (21). Whichever has the greater tendency for a particular complex will determine the magnetic properties of the ground-state.



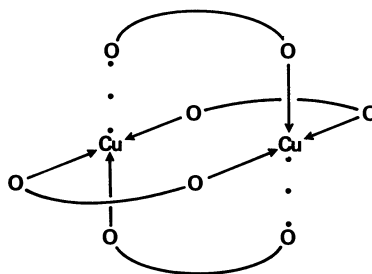
For angular Cu-X-Cu linkages, the simplest type of Goodenough-Kanamori theory involves resonance between covalent structures of types (16) and (17). Calculations of this type (together with the mirror-image for (17), namely (20)) have been reported by Barraclough and Brookes³⁰.

The 6-electron 3-centre bonding scheme for Cu(II)-X-Cu(II) linkages with X = halide or O^{2-} , is also appropriate for X = OH^- if it is assumed that two equivalent p-orbitals of OH^- accommodate the lone-pairs of electrons. The O-H σ -bond of HO^- then must utilize the oxygen 2s orbital for bonding. The oxygen (O^-) valence-state now

[†] This must include at least the overlap between the oxygen and copper atomic orbitals that are singly-occupied in structures of types (17) and (20). This overlap is non-zero when the Cu-X-Cu bond-angle is not equal to 90° . For Cu(II)-Cl-Cu(II) linkages, this overlap is the only type between the Cu(II)-Cl moieties that can be non-negligible in magnitude; the Cu-Cu distances of > 3.2 Å are too large for the copper orbitals of Figure 8-5 to overlap significantly.

involves the promoted sp^6 , V_1 configuration. If it is considered that the non-promoted s^2p^5 , V_1 is the primary valence-state configuration (as it would be in free OH^-), then the primary oxygen orbital involved in the 3-centre bonding is the $2p\bar{1}$ -orbital of Figure 8-5. The 4-electron 3-centre bonding theory then becomes relevant for the Cu(II)-OH-Cu(II) linkages.

For both types of Cu(II) complexes of this chapter, we have not given consideration to the utilization of the copper 4s and 4p orbitals for bonding to the oxygen atoms of the carboxylate, hydroxo and chloride ligands. If these orbitals are included, Pauling "3-electron bond" theory is still appropriate for the valence-bond description of the bonding. Geometrical requirements would require the utilization of (approximately) dsp^2 hybrid orbitals of Cu^{2+} . Prior to bonding to the ligands, three of these orbitals are vacant, and one is singly-occupied. Because each Cu^{2+} ion of either complex is involved in bonding to four oxygen or halide ligand atoms (see Fig. 8-1), it can participate in the formation of three electron-pair bonds and one Pauling "3-electron bond", as shown in (22), for example. The Cu(II) carboxylate and Cu(II) hydroxo or chloro dimers are, therefore, examples of hypoligated complexes (Section 5-1). In the discussion of this chapter, we have omitted the 4s and 4p orbitals, because the odd-electron charge in a copper orbital is considered to be primarily 3d in character.



(22)

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CHAPTER 9 EXCITED STATES

It is frequently considered that valence-bond theory is not easily adapted for qualitative descriptions of molecular excited states. No doubt this is often true. However, for some simple systems at least, there exists an elementary valence-bond counterpart for each molecular orbital description of the excited state. To demonstrate this point, we shall give consideration here to a few types of electronic excitations.

9-1 H₂ : $\sigma \rightarrow \sigma^*$; C₂H₄ : $\pi \rightarrow \pi^*$

For the H₂ ground-state, the covalent bond for the valence-bond structure H—H involves a pair of shared electrons with opposite spins. In Section 3-3, we have discussed the simplest wave-functions that may be associated with the electron-pair bond, namely the molecular orbital and Heitler-London wave-functions of Eqs. (1) and (2) here, in which $1s_A$ and $1s_B$ are a pair of overlapping atomic orbitals. The appropriate spin wave-function for either of these spatial wave-functions is the $S = 0$ wave-function of Eqn. (3).

$$\Psi_1(\text{MO}) = \sigma(1)\sigma(2) \quad \text{with } \sigma = 1s_A + 1s_B \quad (1)$$

$$\Psi_+(\text{HL}) = 1s_A(1)1s_B(2) + 1s_B(1)1s_A(2) \quad (2)$$

$$\Psi_{\text{spin}}(S = 0) = \{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2} \quad (3)$$

Let us now excite an electron from an orbital of each of these two wave-functions, and examine the resulting wave-functions and valence-bond structures. When an electron is excited from the bonding σ -molecular orbital of $\Psi_1(\text{MO})$ into the vacant antibonding orbital $\sigma^* = 1s_A - 1s_B$, we obtain the excited-state wave-functions of Eqs. (4) and (5), which have respectively parallel and antiparallel spins for the two electrons. (In Eqs. (4) and (5) the S and S_z spin quantum numbers have the following values: $\Psi_2(\text{MO})$: $S = 1, S_z = 1, 0, \text{ and } -1$; $\Psi_3(\text{MO})$: $S = S_z = 0$.)

$$\Psi_2(\text{MO}) = \{\sigma(1)\sigma^*(2) - \sigma^*(1)\sigma(2)\} \times \begin{cases} \alpha(1)\alpha(2) \\ \{\alpha(1)\beta(2) + \beta(1)\alpha(2)\}/2^{1/2} \\ \beta(1)\beta(2) \end{cases} \quad (4)$$

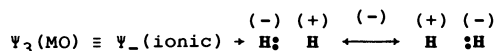
$$\Psi_3(\text{MO}) = \{\sigma(1)\sigma^*(2) + \sigma^*(1)\sigma(2)\} \times \{\alpha(1)\beta(2) - \beta(1)\alpha(2)\}/2^{1/2} \quad (5)$$

If we substitute $1s_A + 1s_B$ and $1s_A - 1s_B$ for σ and σ^* into the spatial components of these wave functions, we obtain Eqs. (6) and (7) (with the same spin wave-functions as for Eqs. (4) and (5)).

$$\Psi_2(\text{MO}) \equiv \Psi_-(\text{HL}) = -2 \{1s_A(1)1s_B(2) - 1s_B(1)1s_A(2)\} \quad (6)$$

$$\Psi_3(\text{MO}) \equiv \Psi_-(\text{ionic}) = -2\{1s_A(1)1s_A(2) - 1s_B(1)1s_B(2)\} \quad (7)$$

From each of these latter wave-functions, we may generate a valence-bond structure for an excited state. If we designate the two electrons with parallel spins for $\Psi_2(\text{MO})$ as crosses (x), we obtain the valence-bond structure $\overset{\times}{\text{H}} \overset{\times}{\text{H}}$ from $\Psi_2(\text{MO})$, because each atomic orbital is singly-occupied. For $\Psi_3(\text{MO})$, the two electrons have opposed spins, and the configurations $1s_A(1)1s_A(2)$ and $1s_B(1)1s_B(2)$ of Eq. (7) locate the two electrons in the same atomic orbital. The resulting valence-bond structures are the ionic structures $\text{H}^{\ominus} \text{H}^{\oplus}$ and $\text{H}^{\oplus} \text{H}^{\ominus}$ and these participate in resonance. The $\Psi_3(\text{MO})$ of Eq. (7) involves a minus (-) linear combination. It is also possible to write down the (+) linear combination, namely the $\Psi_+(\text{ionic})$ of Eqn. (8). Therefore, there are two types of resonance between ionic structures, which correspond to the existence of the two ionic wave-functions of Eqs. (7) and (8). To distinguish them, we shall put a + and - sign above the resonance symbol. Thus



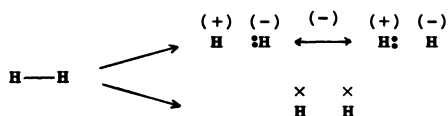
and

$$\Psi_+(\text{ionic}) = 1s_A(1)1s_A(2) + 1s_B(1)1s_B(2) \rightarrow \overset{(-)}{\text{H}} \overset{(+)}{\text{H}} \longleftrightarrow \overset{(+)}{\text{H}} \overset{(-)}{\text{H}} \quad (8)$$

Inspection of Eqn.(6) for $\Psi_2(\text{MO})$ shows that it corresponds to the Heitler-London function obtained when the + of Eqn.(2) is replaced by a - ; this is a result that we have obtained previously in Section 3-5. We may also obtain $\Psi_3(\text{MO})$ ($\equiv \Psi_-(\text{ionic})$) from $\Psi_+(\text{HL})$ by exciting an electron from one atomic orbital into the other and changing the sign of the linear combination. (The sign change is necessary in order to satisfy the spectroscopic rule that an "even" + "odd" excitation is allowed, whereas both "even" + "even" and "odd" + "odd" excitations are forbidden. The "even" and "odd" character of $\Psi_+(\text{HL})$ and $\Psi_-(\text{ionic})$ refer to the behaviour of the wave-functions with respect to inversion through the centre of symmetry of the molecule. Thus $\Psi_+(\text{HL})$ and $\Psi_+(\text{ionic})$ are symmetric (even) and $\Psi_-(\text{HL})$ and $\Psi_-(\text{ionic})$ are antisymmetric (odd).)

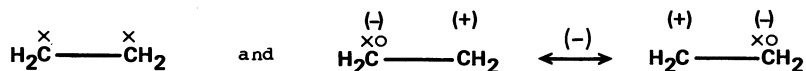
To summarize this section, we may write[†]

[†] More fully, the parallel-spin states have the valence-bond structures $\overset{\times}{\text{H}} \overset{\times}{\text{H}}$, $\overset{\times}{\text{H}} \overset{\times}{\text{H}}$, $\overset{\times}{\text{H}} \overset{\times}{\text{H}}$ \longleftrightarrow $\overset{\ominus}{\text{H}} \overset{\oplus}{\text{H}}$, $\overset{\oplus}{\text{H}} \overset{\ominus}{\text{H}}$, and $\overset{\oplus}{\text{H}} \overset{\oplus}{\text{H}}$ for each of the spin-states of Eqn. (4) with $S_z = +1, 0$ and -1 . However, we (continued next page)



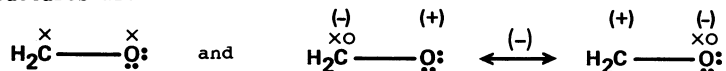
to obtain valence-bond structures for the singly-excited states of H_2 . According to Hund's rule of maximum spin multiplicity, the parallel-spin state ($\overset{\times}{\text{H}} \quad \overset{\times}{\text{H}}$) has a lower energy than has $\overset{(-)}{\text{H}} \text{:} \overset{(+)}{\text{H}} \longleftrightarrow \overset{(+)}{\text{H}} \text{:} \overset{(-)}{\text{H}}$ with antiparallel spins.

The π -electrons of ethylene may be similarly treated. When one π -electron of the ground state $\text{H}_2\text{C}=\text{CH}_2$ is excited, we obtain the valence-bond structures



for the $S = 1$ and $S = 0$ excited states of lowest energy.

For isoelectronic formaldehyde $\text{H}_2\text{C}=\overset{\cdot\cdot}{\text{O}}$ the corresponding valence-bond structures are



However, because oxygen is normally considered to be more electronegative than carbon, the weight for $\overset{(+)}{\text{H}_2\text{C}}-\overset{(-)}{\overset{\cdot\cdot}{\text{O}}}$ would be expected to be larger than that for $\overset{(-)}{\text{H}_2\text{C}}-\overset{(+)}{\overset{\cdot\cdot}{\text{O}}}$.

9-2 $n \rightarrow \pi^*$ TRANSITIONS

For H_2CO , low-lying excited states are obtained when (essentially) a non-bonding (or lone-pair) oxygen electron of the ground state is promoted into a π -electron orbital. This excitation is normally discussed in terms of a molecular orbital description for the π -electrons, and we shall initially use this type of treatment here.

The oxygen non-bonding electrons for the ground state occupy the $2s$ and $2p\bar{\pi}$ orbitals of Fig. 9-1. The C-O π -bond involves a doubly-occupied π -electron molecular orbital, namely

$$\pi_{\text{CO}} = \pi_{\text{C}} + k\pi_{\text{O}} \quad (9)$$

in which π_{C} and π_{O} are carbon and oxygen $2p\bar{\pi}$ -orbitals and $k > 1$.

The $2p\bar{\pi}$ -electrons are less firmly bound than the $2s$ electrons, and therefore, less energy is required to promote a $2p\bar{\pi}$ -electron. The $2p\bar{\pi}$ -orbital is often

(continued from previous page) shall usually use only a single valence-bond structure to represent an $S = 1$ spin-state.

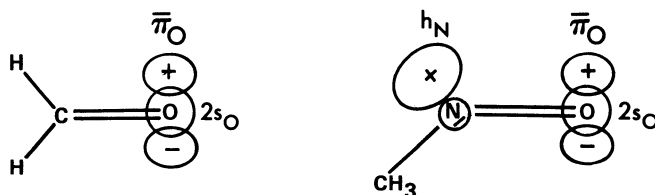


Figure 9-1 Lone-pair atomic orbitals for H_2CO and CH_3NO .

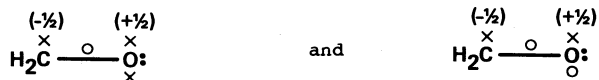
designated as n and we shall use this notation here. The vacant orbital of lowest-energy for the excited n electron is the antibonding C-O π^* -orbital of Eqn. (10), with $k^* > 1$. Two excited configurations may be constructed according to whether the two singly-occupied orbitals (n and π_{CO}^*) have parallel or antiparallel spins for the two electrons. Each excitation is designated as $n + \pi^*$, and the resulting configurations are given by Eqs. (11) and (12), together with the spatial wave-functions for the two singly-occupied orbitals.

$$\pi_{\text{CO}}^* = k^* \pi_{\text{C}} - \pi_{\text{O}} \quad (10)$$

$$(\pi_{\text{CO}})^2 (\pi_{\text{CO}}^*)^1 (n)^1, \quad S = 1; \quad \pi_{\text{CO}}^*(1)n(2) - n(1)\pi_{\text{CO}}^*(2) \quad (11)$$

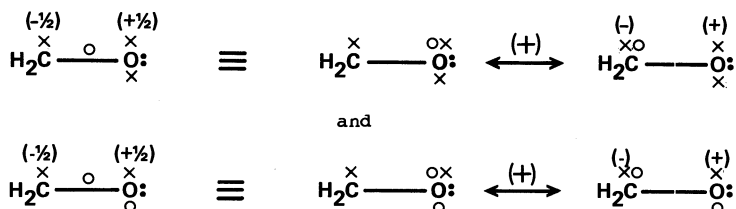
$$(\pi_{\text{CO}})^2 (\pi_{\text{CO}}^*)^1 (n)^1, \quad S = 0; \quad \pi_{\text{CO}}^*(1)n(2) + n(1)\pi_{\text{CO}}^*(2) \quad (12)$$

Each of these excited configurations has a Pauling "3-electron bond" component, namely $(\pi_{\text{CO}})^2 (\pi_{\text{CO}}^*)^1$, which is equivalent to the configuration $(\pi_{\text{C}})^1 (\pi_{\text{CO}})^1 (\pi_{\text{O}})^1$ with two non-bonding electrons and one bonding electron (c.f. Section 3-6). The non-bonding electrons, which occupy the π_{C} and π_{O} atomic orbitals, have parallel spins. If the π_{CO}^* electron is assumed to have an $s_z = +1/2$ spin quantum number, then the valence-bond structure for this π -electron configuration is $\overset{\times}{\text{C}} \circ \overset{\times}{\text{O}}$ (or $\text{C} \times \text{O} \times \text{O}$ according to the Pauling notation). In the configurations of Eqs. (11) and (12), the n electron has its spin either parallel to or opposed to that of the π_{CO}^* electron. Therefore the resulting valence-bond structures for the two excited states that are obtained from the $n + \pi^*$ excitations are



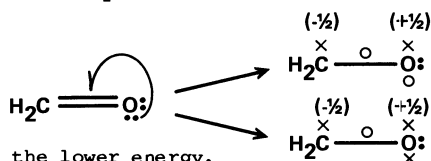
In Section 3-6 we have deduced that for any Pauling "3-electron bond", the valence-bond structure $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ is equivalent to the resonance of $\overset{\cdot\cdot}{\text{A}} \overset{\cdot}{\text{B}} \leftrightarrow \overset{\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$.

Therefore, we may write



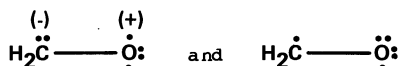
Because the n orbital is orthogonal to each of the π_{C} and π_{O} atomic orbitals, no bonding can occur due to the existence of opposed spins for the n and unpaired π electrons in each of the latter structures for the $S = 0$ state.

In summary, the valence-bond descriptions of the $n + \pi^*$ excitations may be written as



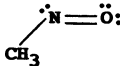
with the parallel-spin state having the lower energy.

If a Heitler-London description of the C-O π -bond is used, the ground-state configuration involves the atomic orbital occupancies of $(\pi_{\text{C}})^1(\pi_{\text{O}})^1(n)^2$, $S = 0$, with antiparallel spins for the π_{C} and π_{O} electrons. When an n electron is excited, either one of the π_{C} or π_{O} orbitals becomes doubly-occupied to generate $(\pi_{\text{C}})^2(\pi_{\text{O}})^1(n)^1$ and $(\pi_{\text{C}})^1(\pi_{\text{O}})^2(n)^1$ configurations. Ignoring spins, the resulting valence-bond structures are



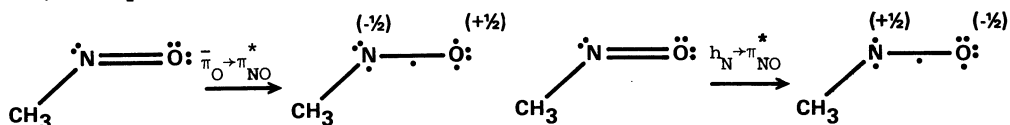
and resonance between these structures generates the Pauling "3-electron bond" structures that we have previously described.

9-3 CH₃NO and O₃ : "n → π"

The measured C-N and N-O bond-lengths for CH₃NO are 1.48 Å and 1.21 Å (Section 2-3). Pauling's estimates of 1.47 and 1.20 Å for the lengths of C-N single and N-O double bonds suggest that the standard Lewis structure  reasonably repre-

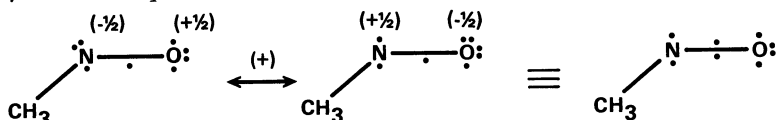
sents the ground-state electronic structure for CH₃NO. The descriptions of the electronic states that are obtained by $\pi + \pi^*$ excitations are similar to those described for both C₂H₂ and H₂CO in Section 9-1. However the descriptions for the $n + \pi^*$ excitations require some elaboration, because a lone-pair electron can be excited from either an oxygen $2p\bar{\pi}$ orbital or a nitrogen hybrid orbital.

Thus, we may write



in which the spin designations have been omitted. In each of the excited-state structures, there is a Pauling "3-electron bond" for the π electrons.

Because the h_{N} and $\bar{\pi}_{\text{O}}$ atomic orbitals overlap (Fig. 9-1), these two structures will participate in resonance, and a second Pauling "3-electron bond" will be generated, i.e. we may write



Alternatively, because the n -orbital configuration $(h_{\text{N}})^1(n_{\text{NO}})^1(\bar{\pi}_{\text{O}})^1$ for the Pauling "3-electron bond" is equivalent to $(n_{\text{NO}})^2(n_{\text{NO}}^*)^1$ in which

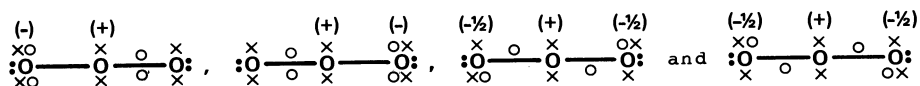
$$n_{\text{NO}} = h_{\text{N}} + k\bar{\pi}_{\text{O}} \quad \text{and} \quad n_{\text{NO}}^* = k^*h_{\text{N}} - \bar{\pi}_{\text{O}}$$

we may describe the electronic excitation as an $n_{\text{NO}}^* + \pi_{\text{NO}}^*$ excitation, i.e. as

$$(n_{\text{NO}})^2(n_{\text{NO}}^*)^2(\pi_{\text{NO}})^2 + (n_{\text{NO}})^2(n_{\text{NO}}^*)^1(\pi_{\text{NO}})^2(\pi_{\text{NO}}^*)^1$$

The $S = 1$ excited state is predicted to have an N-O bond-length which is similar to that of the ground-state, and a linear arrangement for the C, N and O atoms. The linearity will improve the overlap that exists between the h_{N} and $\bar{\pi}_{\text{O}}$ orbitals (h_{N} "grows" into $\bar{\pi}_{\text{N}}$) and thereby increases the strength of the Pauling "3-electron bond" for the three n electrons (provided that the overlap integral does not exceed 1/3 cf. Section 3-10).

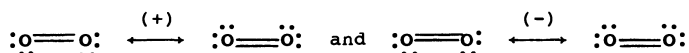
O_3 is isoelectronic with CH_3NO , and a linear $S = 1$ excited state may similarly be obtained by $n_{\text{OO}}^* + \pi_{\text{OO}}^*$ excitation. The resulting valence-bond structures are



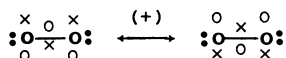
In each of these structures, there are five π - and five $\bar{\pi}$ - (or five π_{x} and five π_{y}) electrons, which form two orthogonal 5-electron 3-centre bonding units. The $S = 1$ delocalized molecular orbital configuration for the ten electrons is formally identical with that for ${}^3\Psi_{\text{covalent}}$ of Fig. 8-3, and is equivalent (Section 6-4) to resonance between the four valence-bond structures with an equal contribution from each structure.

9-4 O_2 : $\pi_x^* \rightarrow \pi_y^*$ and $\pi_x \rightarrow \pi_x^*$

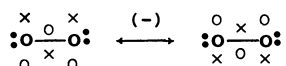
For the (${}^3\Sigma_g^-$) ground-state of O_2 , the π -electron configuration is $(\pi_x)^2(\pi_x^*)^1(\pi_y)^2(\pi_y^*)^1$ in which $\pi_x \equiv \pi_{OO} = \pi_A + \pi_B$, $\pi_y \equiv \pi_{OO} = \pi_A + \pi_B$ etc., and the antibonding π_x^* and π_y^* electrons have parallel spins (Section 4-3). If a $\pi_x^* \rightarrow \pi_y^*$ excitation occurs, with spin inversion, the $(\pi_x)^2(\pi_y)^2(\pi_y^*)^2$ configuration is obtained with valence-bond structure $:\ddot{O}=\ddot{O}:$. Similarly a $\pi_y^* \rightarrow \pi_x^*$ excitation with spin inversion generates the $(\pi_x)^2(\pi_x^*)^2(\pi_y)^2$ configuration with valence-bond structure $:\ddot{O}=\ddot{O}:$. Two linear combinations of these degenerate excited configurations may be constructed, and therefore two types of valence-bond resonance are possible, namely



In Section 4-3, it was indicated that the two electronic states that correspond to these resonances are designated as ${}^1\Sigma_g^+$ and ${}^1\Delta_g$ respectively. A second ${}^1\Delta_g$ state, which can be shown to be degenerate with that described above, is obtained from the $(\pi_x)^2(\pi_x^*)^1(\pi_y)^2(\pi_y^*)^1$ configuration, with opposed spins for the antibonding π_x^* and π_y^* electrons. The valence-bond representation for this latter state is

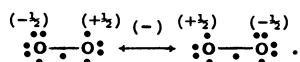


if the order of the antibonding spatial orbitals is $(\pi_x^*)^1(\pi_y^*)^1$ in each of the two configurations. (We may note here that the



resonance represents the $S_z = 0$ component of the ${}^3\Sigma_g^-$ ground state.)

If a bonding π_x electron is promoted into the singly-occupied antibonding π_x^* orbital of the ground-state, the configuration $(\pi_x)^1(\pi_x^*)^2(\pi_y)^2(\pi_y^*)^1$ is obtained (with either parallel or antiparallel spins for the two unpaired-electrons). The $(\pi_y)^2(\pi_y^*)^1$ and $(\pi_x)^1(\pi_x^*)^2$ configurations are respectively equivalent to $(\pi_A)^1(\pi_Y)^1(\pi_B)^1$ and $(\pi_A)^1(\pi_x^*)^1(\pi_B)^1$. The first of these generates the Pauling "3-electron bond" structure $\ddot{O} \cdot \ddot{O} \equiv \ddot{O} \quad \ddot{O} \xleftrightarrow{(+)} \ddot{O} \quad \ddot{O}$. However, the $(\pi_A)^1(\pi_x^*)^1(\pi_B)^1$ configuration is antibonding, and no single valence-bond structure may be written down to indicate the presence of an electron in an antibonding orbital. The only obvious representation involves the use of two structures, i.e. to write $\ddot{O} \quad \ddot{O} \xleftrightarrow{(-)} \ddot{O} \quad \ddot{O}$ with $\xleftrightarrow{(-)}$ originating from the antibonding character of $\pi_x^* = \pi_A - \pi_B$. When the electron spins are not indicated, the $(\pi_x)^1(\pi_x^*)^2(\pi_y)^2(\pi_y^*)^1$ configuration may be represented by the following resonance:



Corresponding valence-bond structures may also be constructed for the $(\pi_x)^2(\pi_x^*)^1(\pi_y)^1(\pi_y^*)^2$ configuration, and all four structures participate in resonance to generate excited ${}^1\Sigma_u^-$ and ${}^1\Delta_u$ states. We shall not elaborate on the nature of these states here; the chief purpose for introducing them is to show that $(\pi)^1(\pi^*)^2$ diatomic configurations (and their $(\sigma)^1(\sigma^*)^2$ equivalents) require two valence-bond structures to represent them, i.e. no single valence-bond structure is available to represent configurations that are overall antibonding.

REFERENCE

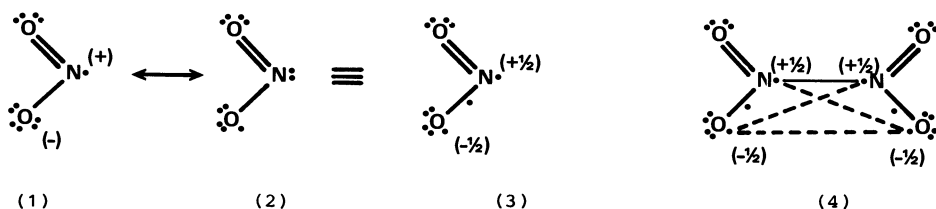
See for example (a) N.J. Turro, *Modern Molecular Photochemistry* (Benjamin-Cummings) 1978; (b) W.G. Dauben, L. Salem and N.J. Turro, *Accounts Chem. Res.* **8**, 41 (1975).

CHAPTER 10

PAULING "3-ELECTRON BONDS" AND "INCREASED VALENCE" THEORY FOR N_2O_4

10-1 PAULING "3-ELECTRON BONDS" AND "INCREASED-VALENCE" STRUCTURES FOR N_2O_4

In Section 7-1, we used the NO_2 Lewis structures of types (1) and (2) to construct Lewis structures for N_2O_4 . To do this, we have spin-paired the odd-electron of one NO_2 moiety with the odd-electron of the other moiety, to obtain the Lewis octet structures (3)-(7) of Section 7-1 for N_2O_4 . In Section 6-1, we have also indicated that resonance between the NO_2 Lewis structures (1) and (2) may be summarized by using the Pauling "3-electron bond" structure (3), which has (fractional) odd-electron charge located in both the nitrogen and oxygen atomic orbitals. Because (3) (in resonance with its mirror image) helps to provide a more economical representation of the electronic structure for NO_2 , it should be possible to use (3) to provide a more economical representation of the electronic structure for N_2O_4 . This is achieved by bonding together two NO_2 molecules, each of which is represented by valence-bond structures of type (3). The resulting valence-bond structure¹ is (4), which has both a (fractional) N-N bond, and (fractional) "long" N-O and O-O bonds. It then follows that because the Pauling "3-electron bond" structure (3) summarizes resonance between the Lewis structures (1) and (2) for NO_2 , valence-bond structure (4) for N_2O_4 must be equivalent to resonance between the Lewis (octet) structures (3)-(6) of Section 7-1. Consequently, a considerable economy in the valence-bond representation of the electronic structure of N_2O_4 is obtained by writing down valence-bond structure (4).



A comparison of the valence-bond structure (4) above, with each of the Lewis structures (3)-(6) of Section 7-1 reveals that there are two additional bonding electrons in (4). Therefore this structure has been designated as an "increased-valence" structure¹ to indicate that additional bonding electrons are present. From the discussion presented in the previous paragraph, it follows that because (4) summarizes resonance between the Lewis structures (3)-(6) of Section 7-1, this "increased-valence" structure must be more stable than any of the component Lewis

structures. N_2O_4 is an example from a large class of molecules, namely the "electron-rich" tri- and polyatomic molecules, for which "increased-valence" structures can be written down. In Chapters 11, 12 and 14 we shall describe in more detail how this may be done. Here, we have introduced the subject to demonstrate a further connection between the Pauling "3-electron bond" theory for NO_2 and the Lewis valence-bond theory for N_2O_4 . These theories may also be related to the molecular orbital theory of Section 7-2, and we shall review these latter connections in the next section.

10-2 "INCREASED-VALENCE" STRUCTURES AND MOLECULAR ORBITAL THEORY FOR N_2O_4

It is initially helpful here to re-examine the molecular orbital configuration $(\sigma 1s)^2$ for H_2 (Section 3-3), with $\sigma 1s = 1s_A + 1s_B$. This configuration may be expressed as $\Psi_{\text{covalent}} + \Psi_{\text{ionic}}$, in which the Ψ_{covalent} and Ψ_{ionic} are given by Eqs. (1) and (2).

$$\Psi_{\text{covalent}} = 1s_A(1)1s_B(2) + 1s_B(1)1s_A(2) = \Psi(\text{H}—\text{H}) \quad (1)$$

$$\Psi_{\text{ionic}} = 1s_A(1)1s_A(2) + 1s_B(1)1s_B(2) = \Psi(\text{H}^{\ominus} : \text{H}^{\oplus}) + \Psi(\text{H}^{\oplus} : \text{H}^{\ominus}) \quad (2)$$

The Ψ_{covalent} is the Heitler-London wave-function for the electron-pair bond of H_2 (Section 3-3). For the ten "mobile σ -electrons" of Figure 7-2 for N_2O_4 (with the remaining electrons localized as they are in the valence-bond structures of types (3)-(7)), the lowest-energy molecular orbital configuration may be expressed as $\Psi_{\text{covalent}} + \Psi_{\text{ionic}}$, in which $\Psi_{\text{covalent}} = \Psi(\text{O}_2\text{N}—\text{NO}_2)$ and $\Psi_{\text{ionic}} = \Psi(\text{NO}_2^+\text{NO}_2^-) + \Psi(\text{NO}_2^-\text{NO}_2^+)$. The Ψ_{covalent} is the wave-function for "increased-valence" structures of type (4), with a Heitler-London type wave-function used to describe the covalent bonding that occurs between the NO_2 moieties.

A simplified derivation of this result for N_2O_4 may be obtained from further transformations of the orbitals for the six-electron configuration of Eqn. 7-10, namely Eqn. (8) here[†]. For this configuration, the s_1 , s_3 and ψ_2 orbitals are defined in Eqs. 7-1, 7-2 and 7-4. The symmetry orbitals s_1 and s_3 of Eqn. (8) may now be linearly combined to form the new molecular orbitals ψ_1^+ and ψ_3^+ of Eqs. (3) and (4), for which the parameter μ is the same as that which occurs in the ψ_2 of Eqn. 7-4. The latter molecular orbital may also be expressed as Eqn. (5). In Eqs. (3)-(5), the ϕ_L , ϕ_R , ϕ_L^* and ϕ_R^* are the L-moiety and R-moiety N-O bonding and antibonding molecular orbitals defined in Eqs. (6) and (7). The molecular orbital configuration $\Psi_1(\text{MO})$ of Eqn. (8) may therefore be transformed to give Eqs. (9) and (10). On expansion of Eqn. (10) in terms of the NO_2 -moiety molecular orbital

[†] Although for completeness we have formulated the 6-electron wave-functions as Slater determinants (Section 3-7), this formulation is not required for the algebra of this chapter.

configurations, we obtain Eqn. (11) with the Ψ_{covalent} and Ψ_{ionic} defined in Eqs. (12) and (13).

$$\psi_1^i = (s_3 + \mu s_1)/(1 + \mu^2)^{1/2} = (\phi_L + \phi_R)/2^{1/2} \quad (3)$$

$$\psi_3^i = (\mu s_3 - s_1)/(1 + \mu^2)^{1/2} = (\phi_L^* + \phi_R^*)/2^{1/2} \quad (4)$$

$$\psi_2 = (s_4 + \mu s_2)/(1 + \mu^2)^{1/2} = (\phi_L - \phi_R)/2^{1/2} \quad (5)$$

$$\phi_L = (\bar{\pi}_1 + \mu h_2)/(1 + \mu^2)^{1/2}; \quad \phi_R = (\mu h_3 + \bar{\pi}_4)/(1 + \mu^2)^{1/2} \quad (6)$$

$$\phi_L^* = (\mu \bar{\pi}_1 - h_2)/(1 + \mu^2)^{1/2}; \quad \phi_R^* = (-h_3 + \mu \bar{\pi}_4)/(1 + \mu^2)^{1/2} \quad (7)$$

$$\Psi_1(\text{MO}) = |\psi_1^\alpha \psi_1^\beta \psi_2^\alpha \psi_2^\beta \psi_3^\alpha \psi_3^\beta| \equiv |(\psi_1)^2 (\psi_2)^2 (\psi_3)^2| \equiv |(s_1)^2 (\psi_2)^2 (s_3)^2| \quad (8)$$

$$\equiv |(\psi_1^i)^2 (\psi_2)^2 (\psi_3^i)^2| \quad (9)$$

$$\equiv \left| (\phi_L)^2 (\phi_R)^2 \left(\frac{\phi_L^* + \phi_R^*}{2^{1/2}} \right)^2 \right| \quad (10)$$

$$\equiv (\Psi_{\text{covalent}} + \Psi_{\text{ionic}})/2^{1/2} \quad (11)$$

$$\Psi_{\text{covalent}} = (|\phi_L^\alpha \phi_L^\beta \phi_R^\alpha \phi_R^\beta \phi_L^* \phi_R^*| + |\phi_L^\alpha \phi_L^\beta \phi_R^\alpha \phi_R^\beta \phi_L^* \phi_L^*|)/2^{1/2} \quad (12)$$

$$\Psi_{\text{ionic}} = (|\phi_L^\alpha \phi_L^\beta \phi_R^\alpha \phi_R^\beta \phi_L^* \phi_L^*| + |\phi_L^\alpha \phi_L^\beta \phi_R^\alpha \phi_R^\beta \phi_R^* \phi_R^*|)/2^{1/2} \quad (13)$$

Because the Pauling "3-electron bond" $\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^* \equiv -a^\alpha \psi_{ab}^\beta b^\alpha$ (Section 3-6) when ψ_{ab} and ψ_{ab}^* are normalized excluding overlapping integrals, the Ψ_{covalent} may be further transformed to give firstly Eqn. (14) and then Eqn. (15). In the latter, the $\Psi_3 - \Psi_6$ are the bond-eigenfunctions or valence-bond structure functions for the six electrons that occupy the $\bar{\pi}_1$, h_2 , h_3 and $\bar{\pi}_4$ orbitals of the Lewis structures (3) to (6) of Section 7-1.

$$\Psi_{\text{covalent}} = (|\bar{\pi}_1^\alpha \phi_L^\beta h_2^\alpha h_3^\beta \phi_R^{\alpha-\beta}| + |\bar{\pi}_1^\beta \phi_L^\alpha h_2^\beta h_3^\alpha \phi_R^{\beta-\alpha}|)/2^{1/2} \quad (14)$$

$$= \{\Psi_3 + \mu(\Psi_4 + \Psi_5) + \mu^2 \Psi_6\}/(1 + \mu^2) \quad (15)$$

10-3 "INCREASED VALENCE" THEORY AND CONFIGURATION INTERACTION FOR N_2O_4

Although it is not required for the "increased-valence" theory of the subsequent chapters, it is appropriate here to discuss aspects of configuration interaction (C.I.) theory for N_2O_4 . In particular, we shall demonstrate that the Ψ_{covalent} of Eqn. (12), which contributes equally with Ψ_{ionic} to the lowest-energy molecular orbital configuration $\Psi_1(\text{MO})$ of Eqn. (8), is the primary component of the lower-energy C.I. wave-function obtained by linearly combining $\Psi_1(\text{MO})$ with the $\Psi_2(\text{MO})$ of Eqn. (16). This result is similar to that which pertains for the ground-state of H_2 (Section 3-3).

$$\Psi_2(\text{MO}) = |\psi_1^\alpha \psi_1^\beta \psi_2^\alpha \psi_2^\beta \psi_4^\alpha \psi_4^\beta| \quad (16)$$

Because ψ_3 of Eqn. (8) is N-O antibonding (c.f. Eqn. 7-5), it is the highest-energy occupied orbital of $\Psi_1(\text{MO})$. When two electrons are excited from ψ_3 to the vacant orbital ψ_4 of Eqn. 7-6, (which is both N-O and N-N antibonding), the lowest-energy doubly-excited configuration $\Psi_2(\text{MO})$ of Eqn. (16) is obtained.

It is now helpful to express the ψ_1 of Eqn. (16) in terms of the orbitals ψ_1' and ψ_3' of Eqs. (3) and (4), in which the latter orbitals are defined in terms of the parameter μ . With ψ_1 defined in terms of λ according to Eqn. 7-3, we obtain Eqn. (17).

$$\psi_1 = \{(1 + \lambda\mu)\psi_1' + (\mu - \lambda)\psi_3'\} / \{(1 + \mu^2)(1 + \lambda)\}^{1/2} \equiv x\psi_1' + y\psi_3' \quad (17)$$

By substituting Eqn. (17) into the $\Psi_2(\text{MO})$ of Eqn. (16) and then expanding $\Psi_2(\text{MO})$ in terms of configurations that involve the ψ_1' , ψ_2' , ψ_3' and ψ_4' orbitals, we obtain Eqn. (18), in which the Ψ_2' , Ψ_2^{**} and Ψ_2^{***} are given by Eqs. (19), (21) and (23). By using techniques that are similar to those used to obtain Eqn. (11) from Eqn. (8), these three configurations may be transformed to give Eqs. (20), (22) and (24). In the latter configurations, the Ψ_{covalent} and Ψ_{ionic} are given by Eqs. (12) and (13), and the Ψ^* and Ψ^{**} configurations are obtained from the Ψ configurations by means of the excitations indicated in Eqn. (25).

$$\Psi_2(\text{MO}) = x^2\Psi_2'(\text{MO}) + 2^{1/2}xy\Psi_2^{**}(\text{MO}) + y^2\Psi_2^{***}(\text{MO}) \quad (18)$$

$$\Psi_2'(\text{MO}) = |\psi_1'^\alpha \psi_1'^\beta \psi_2'^\alpha \psi_2'^\beta \psi_4'^\alpha \psi_4'^\beta| \quad (19)$$

$$\equiv (-\Psi_{\text{covalent}} + \Psi_{\text{ionic}})/2^{1/2} \quad (20)$$

$$\Psi_2^{**}(\text{MO}) = (|\psi_1'^\alpha \psi_3'^\beta \psi_2'^\alpha \psi_4'^\beta| + |\psi_3'^\alpha \psi_1'^\beta \psi_2'^\alpha \psi_4'^\beta|)/2^{1/2} \quad (21)$$

$$\equiv (-\Psi_{\text{covalent}}^* + \Psi_{\text{ionic}}^*)/2^{1/2} \quad (22)$$

$$\Psi_2^{***} = |\psi_3^{\alpha} \psi_3^{\beta} \psi_2^{\alpha} \psi_2^{\beta} \psi_4^{\alpha} \psi_4^{\beta}| \quad (23)$$

$$\equiv (-\Psi_{\text{covalent}}^{**} + \Psi_{\text{ionic}}^{**})/2^{\frac{1}{2}} \quad (24)$$

$$\Psi_{\text{covalent}}^{*} \text{ and } \Psi_{\text{ionic}}^{*} : \phi_L + \phi_L^{*} \text{ or } \phi_R + \phi_R^{*}$$

$$\Psi_{\text{covalent}}^{**} : \phi_L + \phi_L^{*} \text{ and } \phi_R + \phi_R^{*} \quad (25)$$

$$\Psi_{\text{ionic}}^{**} : (\phi_L)^2 + (\phi_L^{*})^2 \text{ or } (\phi_R)^2 + (\phi_R^{*})^2$$

Configuration interaction is invoked by linearly combining $\Psi_1(\text{MO})$ with $\Psi_2(\text{MO})$, according to Eqn. (26). The coefficients C_1 and C_2 are chosen so that the energy of this linear combination is a minimum, a necessary condition for which is that $\partial E/\partial C_1 = \partial E/\partial C_2 = 0$, where $E = (C_1^2 H_{11} + C_2^2 H_{22} + 2C_1 C_2 H_{12}) / (C_1^2 + C_2^2)$. The integral $H_{12} = \int \Psi_1(\text{MO}) \hat{H} \Psi_2(\text{MO}) d\tau$ may be shown to be equivalent to $\iint \psi_3(1) \psi_4(2) (\epsilon^2/r_{12}) \psi_4(1) \psi_3(2) d\mathbf{v}_1 d\mathbf{v}_2$, which is > 0 . For a finite N-N internuclear separation ($r(\text{NN})$) with $H_{22} > H_{11}$, it is easy to deduce that $|C_1| > |C_2|$ and that $C_1 > 0$ when $C_2 < 0$. By substituting Eqs. (11), (20), (22) and (24) into Ψ_{CI} , we obtain Eqn. (27), which indicates that Ψ_{covalent} for "increased-valence" structure (4) is the primary contributor to the lowest-energy linear combination of $\Psi_1(\text{MO})$ with $\Psi_2(\text{MO})$.

$$\Psi(\text{CI}) = C_1 \Psi_1(\text{MO}) + C_2 \Psi_2(\text{MO}) \quad (26)$$

$$\begin{aligned} &= \{(C_1 - x^2 C_2) \Psi_{\text{covalent}} + (C_1 + x^2 C_2) \Psi_{\text{ionic}}\} / 2^{\frac{1}{2}} \\ &+ C_2 \{xy(-\Psi_{\text{covalent}}^{*} + \Psi_{\text{ionic}}^{*}) + y^2(-\Psi_{\text{covalent}}^{**} + \Psi_{\text{ionic}}^{**}) / 2^{\frac{1}{2}}\} \quad (27) \end{aligned}$$

When $r(\text{NN}) = \infty$, $\Psi_1(\text{MO})$ and $\Psi_2(\text{MO})$ are degenerate and therefore $C_1 = -C_2 = 2^{-\frac{1}{2}}$. The parameters λ and μ are also equal for this distance, and therefore $x = 1$ and $y = 0$. The $\Psi(\text{CI})$ of Eqn. (27) then reduces to Ψ_{covalent} , i.e. this C.I. wave-function for N_2O_4 generates NO_2 radicals as dissociation products. The lowest-energy molecular orbital configuration, $\Psi_1(\text{MO})$ of Eqn. (11), generates both NO_2 radicals and NO_2^{+} and NO_2^{-} ions as dissociation products, and therefore is unsatisfactory at large internuclear separations; c.f. H_2 of Section 3-3.

There are four other $S = 0$ excited configurations that may be linearly combined with $\Psi_1(\text{MO})$ and $\Psi_2(\text{MO})$, but these are of less importance for the ground-state, i.e. the primary components of the "best" (lowest-energy) linear combination of the six $S = 0$ configurations are $\Psi_1(\text{MO})$ and $\Psi_2(\text{MO})$ with $|C_1| > |C_2|$ when $r(\text{NN})$ is finite.

In Sections 11-7, 11-9, 13-2, 13-8, 18-2 and 20-6, we shall discuss aspects of the bonding for a number of other molecular systems that, like N_2O_4 , involve at least one 6-electron 4-centre bonding unit. For each of these systems, we shall use

the "increased-valence" structure whose wave-function is the Ψ_{covalent} of the C.I. wave-function of type (26) for the 6-electron 4-centre bonding unit.

CONCLUSIONS

In Sections 7-1 and 10-1, we have shown how dimerization of Pauling "3-electron bond" structures for NO_2 leads to two equivalent types of valence-bond representations for the electron distribution in the N_2O_4 dimer. One of these, namely that of Section 7-1, involves resonance between a standard Lewis structure and a number of "long-bond" Lewis structures. It has also been pointed out in Section 2-5 that "long-bond" structures are usually omitted from elementary descriptions of the electronic structure of most molecules, but according to the electroneutrality principle, such structures should often make important contributions to the ground-state resonance; this should be particularly the case when the standard structures carry atomic formal charges, and the "long-bond" structures do not. In Section 10-1, we have shown that for N_2O_4 , we may summarize resonance between these two types of Lewis structures by spin-pairing the unpaired electrons of the Pauling "3-electron bond" structures for the NO_2 moieties. The resulting valence-bond structure is an "increased-valence" structure, which has two more electrons available for bonding than do any of the component Lewis structures. Because the two types of valence-bond representations for N_2O_4 are equivalent, each of them must provide a more stable representation of the electronic structure than does the use of only the familiar standard Lewis structures. However, as has been discussed in both Section 2-5(b) and Section 10-1, the "increased-valence" structures provide a more economical representation of the electron distribution, and therefore they are more easy to use to obtain qualitative information about bond properties. In the following chapters, we shall give our attention to the construction, types and uses for "increased-valence" structures for numerous other electron-rich systems. Most of these "increased-valence" structures have Pauling "3-electron bonds" as components.

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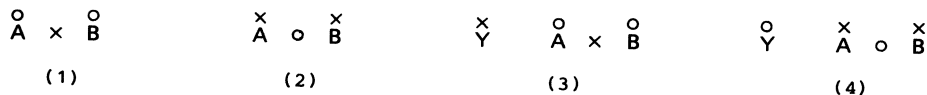
CHAPTER 11

PAULING "3-ELECTRON BONDS" AND "INCREASED-VALENCE" STRUCTURES

We are now ready to examine in detail the incorporation of the Pauling "3-electron bond" structure $\dot{A} \cdot \dot{B}$ into the valence-bond structures for electron-rich molecules that involve 4-electron 3-centre and 6-electron 4-centre bonding units. To do this, we may use any of three alternative methods. In this Chapter, we shall discuss one of them. It involves the spin-pairing of the unpaired-electron of $\dot{A} \cdot \dot{B}$ with the unpaired electron of either an atom \dot{Y} or a second Pauling "3-electron bond" structure $\dot{C} \cdot \dot{D}$.

11-1 PAULING "3-ELECTRON BONDS" AND 4-ELECTRON 3-CENTRE BONDING

To construct a valence-bond structure for a 4-electron 3-centre bonding unit, with a Pauling "3-electron bond" as a component, we commence by writing down the Pauling "3-electron bond" structure $\dot{A} \cdot \dot{B}$ with the electron spins indicated ($x = \alpha$ spin, $o = \beta$ spin) as in (1) and (2) (Section 3-6).



The next step is to introduce an atom Y with one unpaired-electron, whose spin is opposed to that of the electron located in an A-atom atomic orbital, to give the electron distributions of (3) and (4).

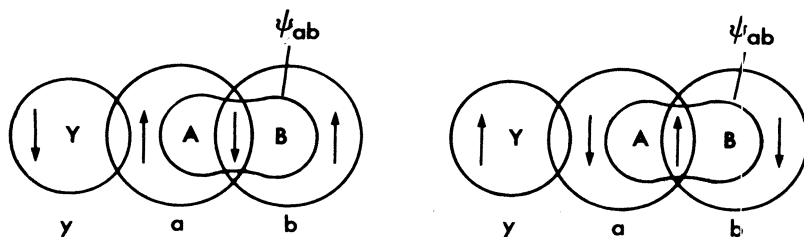
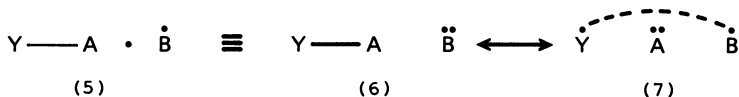


Figure 11-1 Spin-orbitals for electron distributions of structures (3) and (4).

Fig. 11-1 displays spin-orbitals for the electrons of (3) and (4), when the atomic orbitals are s orbitals. Figs. 1-5 and 2-4 display other sets of atomic orbitals that we are

frequently likely to encounter. For the A-B bonding orbital $\psi_{ab} = a + kb$, which accommodates one electron, the bond parameter k is > 0 .

If the y and a atomic orbitals of (3) and (4) overlap appreciably, we may represent as bonded together the Y and A atoms on which these atomic orbitals are centred, to give valence-bond structure (5) in which the electron spins are not specified.

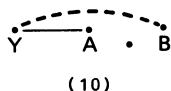


Valence-bond structure (5) summarizes resonance between structures (3) and (4). It is also equivalent to invoking resonance between the Lewis structures (6) and (7), each of which has an electron-pair bond and a lone-pair of electrons. The latter equivalence arises because the Pauling "3-electron bond" configuration $(a)^1(\psi_{ab})^1(b)^1$ with $\psi_{ab} = a + kb$ is equivalent to $(a)^2(b)^1 + k(a)^1(b)^2$, i.e. the Pauling "3-electron bond" structure $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ is equivalent to the resonance of $\overset{\cdot\cdot}{\text{A}} \text{---} \overset{\cdot}{\text{B}} \longleftrightarrow \overset{\cdot}{\text{A}} \text{---} \overset{\cdot\cdot}{\text{B}}$ (Section 3-6). If we take account of the electron spins, then it follows that (3) summarizes resonance between structures (8a) and (8b), and (4) summarizes resonance between the same structures with the electron spins reversed, i.e. (9a) and (9b). The spin distributions of (8a) and (9a) pertain to the Lewis structure (6); those of (8b) and (9b) pertain to the Lewis structure (7).



In (7), we have indicated (c.f. Sections 2-4 and 7-1) the presence of a "long bond" (or formal bond) between atoms Y and B by means of a pecked line (----). When Y and B are non-adjacent atoms, the y and b orbital overlap is very small, and therefore the Y-B bond is very weak (Section 2-4).

Since (5) summarizes resonance between (6) and (7), not all of the unpaired electron charge on Y is used to form the Y-A bond of (5); some is used to form the long weak Y-B bond. We could indicate this extra bonding in (5) by a pecked line, as is shown in (10). However, since the Y-B bond will usually be very much weaker than the Y-A bond, we shall in future not indicate the Y-B bonding in structures of type (5).



We note also that structure (7) has no Y-A bond. Therefore, the Y-A bond-number of (5) must be fractional and less than the value of unity that pertains to

the Y-A single bond of (6). This result is very important, and as we shall find when we discuss some examples, it helps to provide a qualitative understanding of the properties of many bonds. To distinguish the fractional Y-A bond of (5) from that of (6), we have used a thin bond-line in the former structure.

In each of the Lewis structures (6) and (7), there are two bonding electrons, namely those that occupy the y and a, and y and b atomic orbitals, respectively. With respect to structure (5), we shall now deduce that a maximum of three electrons can participate in bonding. To do this, it is helpful to recall (Section 3-6) that the Pauling "3-electron bond" configuration $(a)^1(\psi_{ab})^1(b)^1$ for the valence-bond structure $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ is equivalent to the molecular orbital configuration $(\psi_{ab})^2(\psi_{ab}^*)^1$ in which $\psi_{ab} = a + kb$ and $\psi_{ab}^* = k^*a - b$ are the A-B bonding and antibonding molecular orbitals. The one-electron bond of $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ ($\equiv \overset{\times}{\text{A}} \circ \overset{\times}{\text{B}}$ or $\overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}$) is associated with the bonding ψ_{ab} electron whose spin is opposed to that of the unpaired antibonding ψ_{ab}^* electron. When the ψ_{ab}^* orbital of $(\psi_{ab})^2(\psi_{ab}^*)^1$ overlaps with the singly-occupied y atomic orbital of a third atom Y, the two electrons that occupy these orbitals may be spin-paired to generate the fractional Y-A and Y-B bonding that arises in valence-bond structure (5). The orbital occupations are displayed in Figure 11-2. Therefore a total of three electrons may simultaneously participate¹ in Y-A, Y-B and A-B bonding in (5). Because of the possible presence of an additional bonding electron, we have designated this valence-bond structure as an "increased-valence" structure¹. We may conclude that an "increased-valence" structure summarizes resonance between several Lewis structures, and therefore, the "increased-valence" structure must have a lower energy than has any of the component Lewis structures.

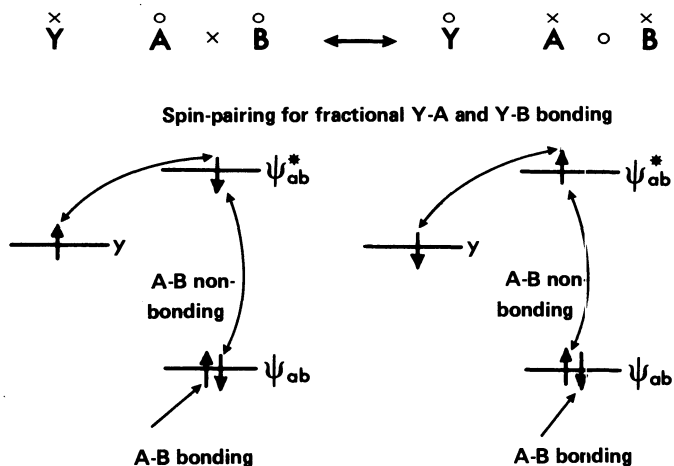
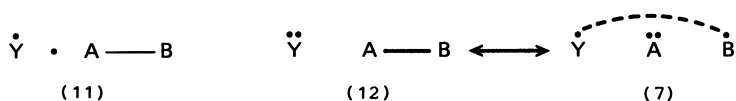


Figure 11.2 Orbital occupations and bonding properties for "increased-valence" structure $\text{Y}-\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$. The $S = 0$ wave-function for the spin-pairing is described in Section 15-1, but is not required here. Atomic orbital overlap integrals have been omitted from the normalization constants for ψ_{ab} and ψ_{ab}^* .

In most elementary accounts of valence, the Lewis "long-bond" structures are usually omitted from consideration. The results of numerous calculations^{2,3} indicate that these structures may often have significant weights. When this is the case, "long-bond" structures should be included in the elementary valence-bond description of the molecule. "Increased-valence" structures provide a very simple way of including them, together with the more familiar standard Lewis structures such as (6) (Section 2-2) with electron-pair bonds located between pairs of adjacent atoms only.

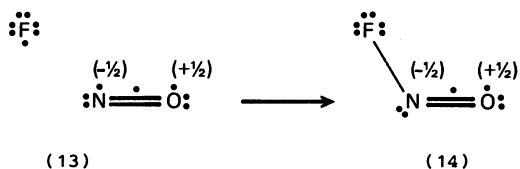
For 4-electron 3-centre bonding units, the "increased-valence" structure (11) may also be constructed by spin-pairing the unpaired electron of atom B with the antibonding Y-A electron of the Pauling "3-electron bond" structure $\dot{Y} \cdot \dot{A}$. This "increased-valence" structure is equivalent to resonance between the "long-bond" and standard Lewis structures (7) and (12), and will participate in resonance with (5). We may therefore write $(5) \leftrightarrow (11) \equiv (6) \leftrightarrow (7) \leftrightarrow (12)$, thereby including all of the Lewis electron-pair bond structures in the resonance description for the 4-electron 3-centre bonding unit. Alternatively, we may write either $(5) \leftrightarrow (12)$ or $(6) \leftrightarrow (11)$ to obtain the same result.



We shall now use "increased-valence" structures, with Pauling "3-electron bonds" as components, to discuss the electronic structures for a number of molecules that have NO, OO, SS, SO or NO₂ linkages. Bond-lengths for them are reported in Tables 11-1 to 11-4.

11-2 NITROSYL HALIDES

The length of the N-O bond of FNO is 1.136 Å, which is similar to the length of 1.150 Å for the free NO molecule. This observation suggests that we might obtain a suitable valence-bond structure for FNO by bonding a fluorine atom to the Pauling "3-electron bond" structure (13) (Section 4-5) for NO.



	r(N-O)	r(N-X)		r(N-O)	r(N-X)
NO ^{(a)†}	1.150		O ₂ NNO ₂ ^(j)	1.190	1.782
FNO ^(b)	1.136	1.512	O'NNO ₂ ^(k)	1.142 (NO')	1.864
ClNO ^(c)	1.139	1.975		1.202, 1.217 (NO)	
BrNO ^(d)	1.146	2.140	FNO ₂ ^(l)	1.180	1.467
HNO ^(e)	1.209	1.090	ClNO ₂ ^(m)	1.202	1.840
CH ₃ NO ^(f)	1.211	1.480	CF ₃ NO ₂ ⁽ⁿ⁾	1.21	1.56
CF ₃ NO ^(g)	1.197	1.546	CCl ₃ NO ₂ ^(o)	1.21	1.59
NO ₂ ^(h)	1.236		CH ₃ NO ₂ ^(p)	1.224	1.489
NO ₂ ⁽ⁱ⁾	1.193				

† REFERENCES: (a) K.P. Huber and G. Herzberg, *Molecular Spectra and Molecular Structure*, Vol. 4 (Van Nostrand Reinhold, 1979). (b) K.S. Buckton, A.C. Legon and D.J. Millen, *Trans. Faraday Soc.*, **65**, 1975 (1969). (c) D.J. Millen and J. Pannell, *J. Chem. Soc.*, 1322 (1961). (d) D.J. Millen and D. Mitra, *Trans. Faraday Soc.*, **66**, 2408 (1970). (e) J.F. Ogilvie, *J. Mol. Struct.* **31**, 407 (1976). (f) P.H. Turner and A.P. Cox, *J. Chem. Soc., Faraday II*, **74**, 533 (1978). (g) S.H. Bauer and A.L. Andreassen, *J. Phys. Chem.*, **76**, 3099 (1972). (h) G.B. Carpenter, *Acta. Cryst.*, **8**, 852 (1955). (i) G.R. Bird, J.C. Baird, A.W. Jache, J.A. Hodgeson, R.F. Curl, A.C. Kunkle, J.W. Bransford, J. Rastrup-Andersen and J. Rosenthal, *J. Chem. Phys.*, **40**, 3378 (1964). (j) B.W. McClelland, G. Gundersen and K. Hedberg, *J. Chem. Phys.* **56**, 4541 (1972). (k) A.H. Brittain, P.A. Cox and R.L. Kuczkowski, *Trans. Faraday Soc.*, **65**, 1963 (1969). (l) A.C. Legon and D.J. Millen, *J. Chem. Soc. A.*, 1736 (1968). (m) D.J. Millen and K.M. Sinnott, *J. Chem. Soc.*, 350 (1958). (n) I.L. Karle and J. Karle, *J. Chem. Phys.*, **36**, 1969 (1962). (o) W.M. Barss, *J. Chem. Phys.*, **27**, 1260 (1957). (p) A.P. Cox and S. Waring, *J. Chem. Soc. Faraday II* **68**, 1060 (1972).

Table 11-1. Bond lengths (Å) for some nitrosyl and nitro compounds.

	r(O-O)	r(O-X)		r(O-O)	r(O-X)
O ₂ ^{(a)†}	1.207		CF ₃ OOCl ^(f)	1.447	1.699 (O-Cl)
FOOF ^(b)	1.217	1.575			1.372 (O-C)
HOOH ^(c,d)	1.475	0.950	CF ₃ OOF ^(f)	1.366	1.449 (O-F)
	1.452	0.965			1.419 (O-C)
CF ₃ OOCF ₃ ^(e)	1.419	1.399	HO ₂ ^(g,h)	1.335	0.977
CF ₃ OOH ^(f)	1.447	0.974 (O-H)		1.329	0.975
		1.376 (O-C)	O ₃ ⁽ⁱ⁾	1.272	

† REFERENCES: (a) Ref. (a) of Table 11-1. (b) R.H. Jackson, *J. Chem. Soc.* 4585 (1962). (c) A.L. Redington, W.B. Olson and P.C. Cross, *J. Chem. Phys.*, **36**, 1311 (1962). (d) G. Khachkuruzov and I.W. Przheroskii, *Opt. Spectrosc.*, **36**, 172 (1974). (e) C.J. Marsden, L.S. Bartell and F.P. Diodati, *J. Mol. Struct.* **39**, 253 (1977). (f) C.J. Marsden, D.D. DesMarteau and L.S. Bartell, *Inorg. Chem.*, **16**, 2359 (1977). (g) Y. Beers and C.J. Howard, *J. Chem. Phys.*, **64**, 1541 (1976). (h) R.P. Tjackett, P.A. Freedman and W.J. Jones, *Mol. Phys.*, **37**, 403 (1979). (i) J.-C. Depannemaecker and J. Bellet, *J. Mol. Spectr.*, **66**, 106 (1977).

Table 11-2 Bond-lengths (Å) for some molecules with O-O linkages.

	r(S-S)	r(S-X)		r(S-S)	r(S-X)
S ₂ ^{(a)†}	1.889		HSSH ^(e)	2.057	1.327
FSSF ^(b)	1.888	1.635	CH ₃ SSCH ₃ ^(f,g)	2.023	1.806
ClSSCl ^(c,d)	1.931	2.057		2.029	1.816
	1.950	2.055	CF ₃ SSCF ₃ ^(h)	2.030	1.835
F ₂ SS ^(b)	1.860	1.598	SF ₄ ^(i,j)		1.545, 1.542 (eq)
					1.646, 1.643 (ax)

† REFERENCES: (a) Ref. (a) of Table 11-1. (b) R.L. Kuczkowski, J. Amer. Chem. Soc., **86**, 3617 (1964). (c) B. Beagley, G.H. Ekersley, D.P. Brown and D. Tomlinson, Trans. Faraday Soc., **65**, 2300 (1969). (d) C.J. Marsden, R.D. Brown and P.D. Godfrey, J. Chem. Soc. Chem. Comm. 399 (1979). (e) G. Winnewisser, M. Winnewisser and W. Gordy, J. Chem. Phys., **49**, 3465 (1968). (f) B. Beagley and K.T. McAloon, Trans. Farad. Soc., **67**, 3216 (1971). (g) A. Yokozeki and S.H. Bauer, J. Phys. Chem., **80**, 618 (1976). (h) C.J. Marsden and B. Beagley, submitted for publication. (i) W.M. Tolles and W.D. Gwinn, J. Chem. Phys. **36**, 1119 (1962); (j) K. Kimura and S.H. Bauer, J. Chem. Phys. **39**, 3172 (1963).

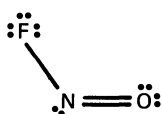
Table 11-3 Bond-lengths (Å) for some molecules with S-S linkages.

	r(S-O)	r(S-X)		r(S-O)	r(S-X)
SO ^{(a)†}	1.481		HSO ^(e)	1.494	1.389
F ₂ SO ^(b)	1.413	1.585	SO ₂ ^(f)	1.431	
FSO ^(c)	1.452	1.602	S ₂ O ^(g)	1.464	1.882
Cl ₂ SO ^(d)	1.443	2.077	OSSO ^(h)	1.458	2.025
			CH ₂ SO ⁽ⁱ⁾	1.469	1.610

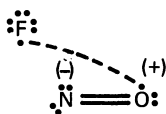
† REFERENCES: (a) Ref. (a) of Table 11-1. (b) N.J.D. Lucas and J.G. Smith, J. Molec. Spectry., **43**, 327 (1972); (c) Y. Endo, S. Saito and E. Hirota, submitted for publication. (d) I. Hargittai, Acta Chem. Acad. Sci. Hung. **59**, 351 (1969). (e) N. Ohashi, M. Kakimoto and S. Saito, J. Mol. Spectry. to be published. (f) S. Saito, J. Mol. Spectry., **30**, 1 (1969). (g) E. Tiemann, J. Hoefft, F.J. Lovas and D.R. Johnson, J. Chem. Phys., **60**, 5000 (1974). (h) F.J. Lovas, E. Tiemann and D.R. Johnson, J. Chem. Phys., **60**, 5005 (1974). (i) R.E. Penn and R.J. Olsen, J. Mol. Spectry., **61**, 21 (1976).

Table 11-4 Bond-lengths (Å) for some molecules with S-O linkages.

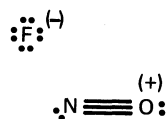
To obtain "increased-valence" structure (14), we have spin-paired the nitrogen odd-electron charge of (13) with a corresponding fraction of the fluorine unpaired electron. Because (5) \equiv (6) \leftrightarrow (7), valence-bond structure (14) is equivalent to resonance between the standard and "long-bond" Lewis structures (15) and (16). The "long-bond" structure has no N-F bond, and therefore, the N-F bond-number of (14) is less than unity.



(15)



(16)



(17)

We may construct similar types of "increased-valence" structures for ClNO and BrNO; each of these molecules has a long nitrogen-halogen bond, and an N-O bond-length similar to that of free NO. (The N-Cl and N-Br bond-lengths of 1.98 Å and 2.14 Å are longer than Pauling's estimates of 1.73 Å and 1.86 Å for the lengths of N-Cl and N-Br single bonds⁴). The orbital overlap for the "increased-valence" bonding unit of (14) is of the $\sigma + \bar{\pi}$ type displayed in Figs. 1-5 and 2-4 for FNO; a nitrogen hybrid orbital overlaps simultaneously with a halogen $p\sigma$ -orbital and an oxygen $\bar{\pi}$ -orbital.

The more familiar valence-bond explanation of the bond properties for FNO involves resonance between the standard Lewis structures (15) and (17). In Chapters 12 and 14, we shall also use these valence-bond structures to generate the "increased-valence" structure (14).

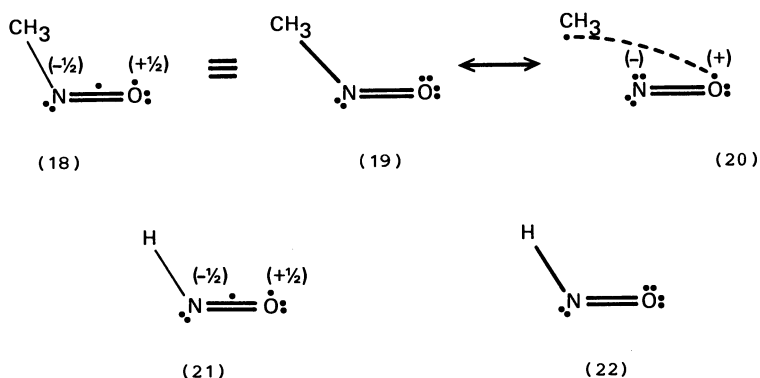
It may be noted that the N-O bond-length for each of the nitrosyl halides is slightly shorter than that of free NO, and resonance between "increased-valence" structure (14) and the standard Lewis structure (17) can account for this observation. If resonance between only the standard Lewis structures (15) and (17) is used to represent the electronic structure, the shortening of the N-O bond can only be accounted for if the weight for (17) is larger than for (15). The electroneutrality principle suggests that this should not be the case, and this is supported by the results of valence-bond calculations by Roso⁵. For the valence-bond structures (15), (16) and (17), Roso has calculated coefficients of 0.73, 0.19 and 0.13 for their bond-eigenfunctions in a valence-bond study of the 4-electron 3-centre bonding for FNO. These bond-eigenfunction coefficients suggest that (15), with zero formal charges on all atoms, must have a rather larger weight than has (17)[†].

[†] Roso's bond-eigenfunction coefficients that we report here and in other sections, were calculated using non-empirical valence-bond procedures. For the electrons that were explicitly included in the bond-eigenfunction configurations, all integrals that arise in the valence-bond calculations were evaluated using STO-5G atomic orbitals. The number of electrons that could be included in the bond-eigenfunction configurations depended on the size of the molecule. For FNO, the 1s electrons were omitted, whereas all of the electrons were included for the HNO calculation (Section 11-3). In Section 11-10, the bond eigenfunction coefficients for FNO₂ were calculated by including only some of the valence-shell electrons in the bond-eigenfunction configurations, namely those electrons whose locations vary in the valence-bond structures of Fig. 11-8. Similar types of calculations were made for the $\pi + \bar{\pi}$ -electrons of CH₂N₂ (Section 22-4). Except for HNO, we have reported here only the bond-eigenfunction coefficients for the valence-bond structures that are explicitly discussed in the text.

It should be noted that because the bond-eigenfunctions are not orthogonal in these calculations, the valence-bond weights are not equal to the squares of the bond-eigenfunction coefficients. However, the magnitudes of these coefficients should provide a reasonable qualitative guide to the relative importance of certain valence-bond structures for the ground-state resonance description of a molecule. (No doubt better valence-bond calculations may be performed by other workers in the future, but the results of Roso's studies are in accord with the expectations of the electroneutrality principle).

11-3 CH₃NO AND HNO

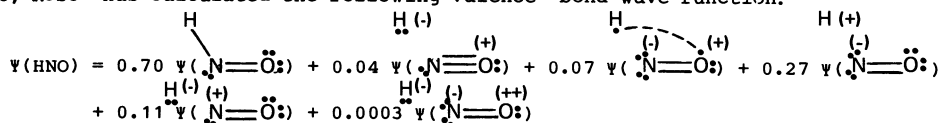
The N-O bond-length of 1.21 Å for CH₃NO is similar to Pauling's estimate of 1.20 Å for an N-O double bond, and 0.06 Å longer than that for free NO. The C-N bond-length of 1.48 Å is similar to the C-N single-bond length of 1.47 Å for CH₃NH₂. The "increased-valence" structure (18), which may be obtained by spin-pairing the odd-electron of CH₃ with that of NO, does not account for these properties. According to (18), the N-O and C-N bonds should be respectively shorter than a double bond, and longer than a single bond. Because (18) summarizes resonance between (19) and (20), the bond-lengths imply that (20) makes little contribution to resonance, and that (19) alone provides a satisfactory representation of the electronic structure for CH₃NO.



For HNO, the N-O bond-length of 1.21 Å is also similar to that of a double-bond. However, the N-H length of 1.09 Å is 0.07 Å longer than the N-H single bonds of NH₃. Neither the "increased-valence" structure (21), nor the standard Lewis structure (22) can account for the lengths of both bonds simultaneously. But the similarity of the N-O bond-lengths of both CH₃NO and HNO to those of double-bonds suggests that CH₃- and H-substituents do not bring out the "increased-valence" aspects of bonding to a significant extent, i.e. they do not lead to much development of a Pauling "3-electron bond" in a 4-electron 3-centre bonding unit for a neutral molecule[†]. This hypothesis will receive some further empirical support in

[†] This conclusion must have its origins partially in the very different magnitude of the atomic orbital overlap integral for N-F (σ) single bonds compared with those for N-H and N-CH₃ single bonds. For illustrative purposes here we shall assume that the nitrogen and carbon orbitals are respectively sp² and sp³ hybridized, and that the fluorine and hydrogen orbitals are 2pσ and 1s. The resulting Slater orbital overlap integrals are then 0.3₂, 0.5₂ and 0.6₁ for the N-F, N-H and N-CH₃ bonds. With approximate molecular orbital theory for 4-electron 3-centre bonding units (Section 14-2), the much larger N-H and N-C overlap integrals must raise the energies of the antibonding σ_{NH}^{*} and σ_{NC}^{*} orbitals relative to that of the σ_{NF}^{*} orbital, i.e. the latter orbital is more accessible for the oxygen 2pπ electrons of FNO. The greater electronegativity of F relative to CH₃ and H will also re-enforce the greater tendency for the oxygen 2pπ electrons of FNO to delocalize. Similar considerations are also appropriate for F₂O₂ vs H₂O₂ (Section 11-4), F₂S₂ vs H₂S₂ (Section 11-5) and for many related systems.

Sections 11-4 and 11-5. Another way to say this is that the contribution of the "long-bond" structure (such as (20)) to the ground-state resonance is small. For HNO, Roso⁵ has calculated the following valence-bond wave-function:



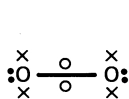
The bond-eigenfunction coefficient of 0.07 for the "long-bond" structure provides theoretical support for the unimportance of this structure, and the lengthening of

the N-H bond for HNO may arise from the contributions of the structures $\overset{\text{H}(-)}{\overset{(-)}{\underset{\cdot\cdot}{\text{N}}}}=\overset{\cdot\cdot}{\underset{\cdot\cdot}{\text{O}}}\overset{\cdot\cdot}{\underset{\cdot\cdot}{\text{O}}}$ and $\overset{\text{H}(-)}{\overset{(+)}{\underset{\cdot\cdot}{\text{N}}}}=\overset{\cdot\cdot}{\underset{\cdot\cdot}{\text{O}}}\overset{\cdot\cdot}{\underset{\cdot\cdot}{\text{O}}}$ to the ground-state resonance. Each of these latter structures retains an N-O double-bond.

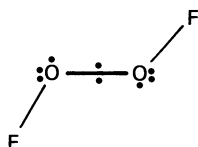
As we have found for the nitrosyl halides, if a hydrogen atom or CH₃ is replaced by the more-electronegative halogen atoms, the Pauling "3-electron bond" of NO in the nitrosyl compound can be stabilized. For CF₃NO, the electronegativity of CF₃ should be intermediate between those of CH₃ and F. Therefore, some stabilization of the Pauling "3-electron bond" for this molecule may occur. The "increased-valence" structure (18) for CF₃NO (with CF₃ replacing CH₃) implies that the C-N bond is longer than a single-bond, and that the N-O bond should be shorter than those of CH₃NO and HNO. Both of these inferences are in agreement with the observed bond-lengths of Table 11-1.

11-4 SOME DIOXYGENYL COMPOUNDS

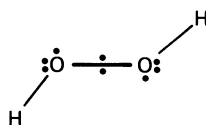
The valence-bond structure for the ground-state of molecular oxygen is (23), with two Pauling "3-electron bonds" (Section 4-3). By spin-pairing the two unpaired electrons with those of two fluorine or two hydrogen atoms, we obtain "increased-valence" structures (24) and (25) for F₂O₂ and H₂O₂. These valence-bond structures indicate O-O bond properties which are similar to that of free O₂, and long, weak O-F and O-H bonds.



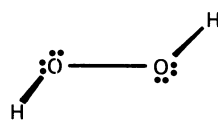
(23)



(24)



(25)

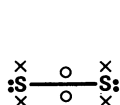


(26)

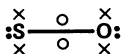
For F₂O₂, (24) is a suitable valence-bond structure; the O-O lengths of O₂ and F₂O₂ in Table 11-2 are similar, and the O-F lengths are much longer than the 1.42 Å

bonds; this they are found to be; see Table 11-3. (We have assumed that the two equatorial bonds of SF_4 , with lengths of 1.54 \AA are single-bonds; the standard

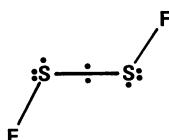
Lewis structures, namely $\begin{array}{c} \text{F} \\ | \\ \text{F} > \text{S}^{\oplus} \\ | \\ \text{F} \\ | \\ \text{F}^{\ominus} \end{array}$ and $\begin{array}{c} \text{F} \\ | \\ \text{F} > \text{S}^{\oplus} \\ | \\ \text{F} \\ | \\ \text{F}^{\ominus} \end{array}$, indicate this to be the case.) On the other hand, the reported bond-lengths for H_2S_2 and $(CH_3)_2S_2$ indicate that these molecules have S-S single bonds, with the hydrogen and methyl radicals unable to stabilize the Pauling "3-electron bonds" of S_2 .



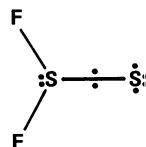
(30)



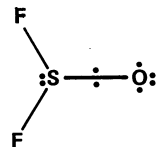
(31)



(32)

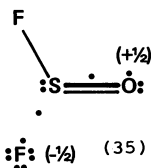


(33)

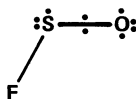


(34)

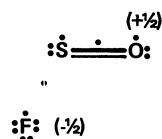
From "increased-valence" structure (34) for F_2SO , we would predict that the S-F bonds should be longer than the single-bond length of 1.54 \AA , and that the S-O length should be similar to that of free SO. Although lengthening of the S-F bonds is observed, the S-O bond-length of 1.41 \AA is shorter than the 1.48 \AA for free SO. Possibly this shortening is due to a significant contribution of "increased-valence" structure (35) to resonance with (34); in (35), the S-O bond-number + bond-order exceeds the value of 2 that occurs in (31). Similarly, for FSO, "increased-valence" structure (36) will participate in resonance with (37), from which it may be deduced that the S-F and S-O bond-lengths for this radical are respectively longer than a single bond, and shorter than that of free SO. The experimental lengths of 1.602 and 1.452 \AA are in accord with this deduction.



(35)



(36)



(37)

The above theory is also appropriate for Cl_2SO , whose S-Cl and S-O bond-lengths of 2.077 \AA and 1.443 \AA are respectively longer than the S-Cl single-bond length of 2.014 \AA for CH_3SCl , and shorter than that for free SO.

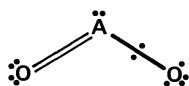
For HSO, a valence-bond structure similar to (36), with H replacing F, accounts simultaneously for the observations that the S-O length of 1.494 \AA is similar to the 1.481 \AA for free SO, and that the S-H length of 1.389 \AA is longer than the single-bond length of 1.336 \AA for H_2S . However, on the basis of the discussion in Section 11-4 for HO_2 , it would be expected that the H-S bond length for

HSO would be similar to those for HS and H₂S, and that the S-O bond-length would be appreciably longer than that of free SO.

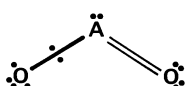
11-6 O₃, SO₂, S₂O AND NO₂⁻

In Sections 11-2 to 11-5, atomic orbitals for the "increased-valence" bonding units are of the $\sigma + \bar{\pi}$ (Fig. 1-5) type. The Y—A bonds are σ -bonds. We shall now describe some examples of "increased-valence" structures that involve Y—A π -bonds as well as σ -bonds in the "increased-valence" bonding units. For 4-electron 3-centre π -bonding, the orbital overlap is displayed in Fig. 2-4.

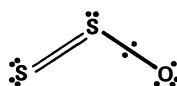
Oxygen and sulphur atoms ($:\ddot{O}\cdot$ and $:\ddot{S}\cdot$) have two unpaired electrons in their ground-states. By spin-pairing these electrons with those of the Pauling "3-electron bond" structures (23), (30) and (31) for the ground-states of O₂, SO and S₂, we may obtain the "increased-valence" structures (38)-(41) for O₃, SO₂ and S₂. In (38) and (39) the A-atom is either oxygen or sulphur. Since the two terminal oxygen atoms are symmetrically equivalent, these two valence-bond structures are of equal importance for a resonance description of O₃ and SO₂.



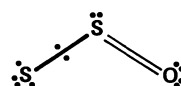
(38)



(39)

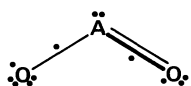


(40)

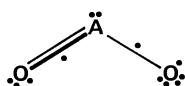


(41)

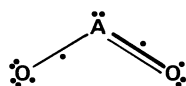
Each of (38)-(41) has two "increased-valence" bonding units, which may be rearranged to obtain "increased-valence" structures such as (42)-(45), for O₃ and SO₂. These structures participate in resonance with (38) and (39). The presence of formal charges in (42)-(45) suggests that they make a smaller contribution to the ground-state resonance than do (38)-(41). Therefore, for simplicity here and elsewhere in this book, we shall usually give consideration only to the most important of the "increased-valence" structures, i.e. those that involve the smallest formal charge separations.



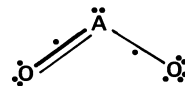
(42)



(43)



(44)



(45)

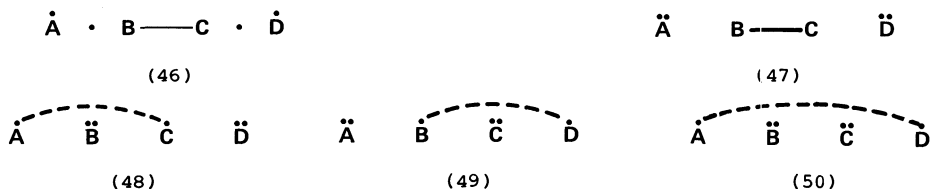
Each of the "increased-valence" structures (38) and (39) has an O-O double bond similar to (23) for O₂, and a fractional O=O bond with a bond-number less

than 2. Thus, resonance between (38) and (39) implies that, on the average, less than four electrons are involved in bonding between each pair of adjacent oxygen atoms. Consequently, it is not surprising that the bond-lengths of 1.278 Å for O₃ are longer than the 1.207 Å for the double bond of O₂. On the other hand, resonance between (38) and (39) for SO₂ (with A ≡ S) does not account for the observed shortening of its S-O lengths (1.431 Å) relative to the 1.481 Å for free SO.

The nitrite anion, NO₂⁻, is isoelectronic with O₃, and its N-O bond-lengths of 1.24 Å are about 0.04 Å longer than a "normal" N-O double bond. Resonance between the "increased-valence" structures (38) and (39), in which atom A is a nitrogen atom, reflects this observation. These structures may also be obtained by spin-pairing the two unpaired electrons that are present for the ground-states of O and NO⁻. The anion NO⁻ is isoelectronic with O₂, and therefore, its valence-bond structure $\overset{(-)}{\text{N}} \div \overset{\cdot}{\text{O}}:$ has two Pauling "3-electron bonds".

11-7 PAULING "3-ELECTRON BONDS" AND 6-ELECTRON 4-CENTRE BONDING: N₂O₂, Cl₂O₂, S₂O₂ and S₂I₄²⁺

In Fig. 11-3, the orbital occupations and electron spins are displayed for two equivalent Pauling "3-electron bond" structures $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ and $\overset{\cdot}{\text{C}} \cdot \overset{\cdot}{\text{D}}$. When the atomic orbitals of these two structures overlap, the unpaired-electrons may be spin-paired to generate the "increased-valence" structure (46), for which a total of four electrons can participate in fractional A-B, A-C, A-D, B-C, B-D and C-D bonding⁷. Only two bonding electrons are present in the standard Lewis structure (47). Because $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}} \equiv \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}} \leftrightarrow \overset{\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$ and $\overset{\cdot}{\text{C}} \cdot \overset{\cdot}{\text{D}} \equiv \overset{\cdot\cdot}{\text{C}} \overset{\cdot\cdot}{\text{D}} \leftrightarrow \overset{\cdot}{\text{C}} \overset{\cdot\cdot}{\text{D}}$, it may be deduced that "increased-valence" structure (46) is equivalent to resonance between the standard Lewis structure (47) and the "long-bond" Lewis structures (48), (49) and (50). Because no B-C bond is present in each of the latter three structures, the B-C bond-number for (46) is less than unity. Therefore, the B-C bond-length and strength for (46) will be longer and weaker than is that for a "normal" B-C electron-pair bond.



The discussion above is of course a generalization of that described previously in Section 10-1 for N₂O₄. It is appropriate for all molecules that involve extended 6-electron 4-centre bonding units, i.e. for molecules that have one or more sets of 6 electrons distributed amongst 4 overlapping atomic orbitals (a, b, c and

d). These orbitals may be either π , $\sigma + \bar{\pi}$ (Fig. 1-5), or $\sigma + \delta$ (Fig. 8-2) or σ (Fig. 2-6) in character.

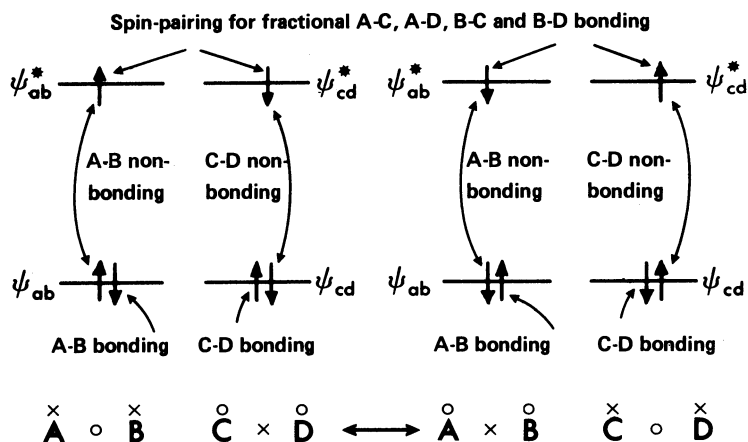
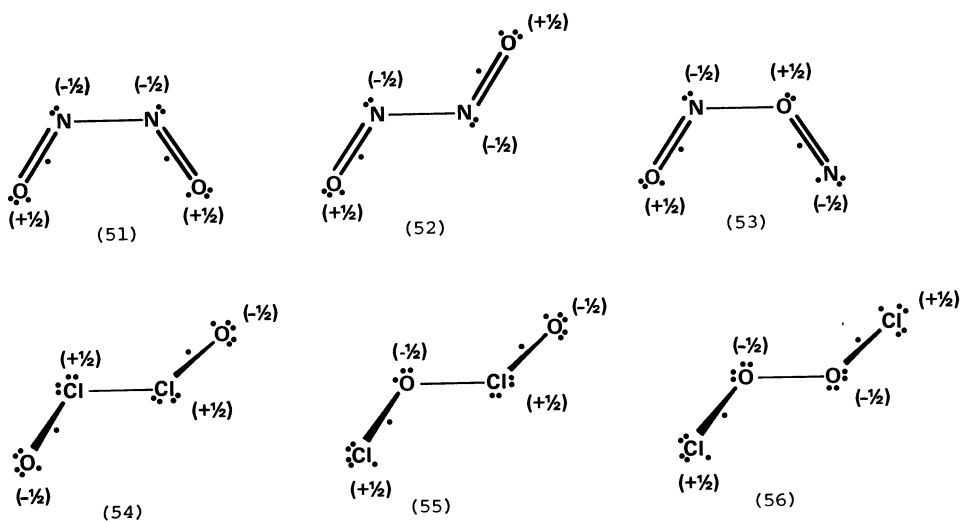
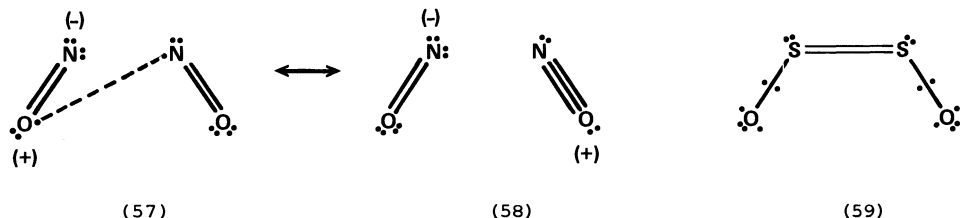


Figure 11-3 Orbital occupations and bonding properties for "increased-valence" structure $\overset{\times}{\text{A}} \cdot \overset{\circ}{\text{B}} - \overset{\circ}{\text{C}} \cdot \overset{\times}{\text{D}}$.

Each of NO and ClO has a Pauling "3-electron bond" in its ground-state valence-bond structure (Sections 4-5 and 4-7), and dimers of these radicals are known to be formed, with weak B-C type bonds. If dimerization is assumed to involve primarily the spin-pairing of the antibonding π^* -electrons of two monomers in a $\sigma + \bar{\pi}$ manner, then "increased-valence" structures such as (51)-(56) are obtained. These structures have B-C bond-numbers that are less than unity, thus accounting for the weakness of the bond between the monomers.



Both cis and trans conformers for ONNO are known⁸, with cis more stable than trans. The additional stability of the cis conformer is associated with cis O-O overlap⁹; in valence-bond theory, this occurs primarily via the oxygen $2p\bar{\pi}$ -orbitals (Fig. 1-5; c.f. N_2O_4 in Section 7-3). The stabilization energy for covalent-ionic resonance of the type (57) \leftrightarrow (58) is cis O-O overlap dependent (Section 7-3) and leads to the development of a Pauling "3-electron bond" between the oxygen atoms. The covalent structure (57) is one of the contributing forms (of type (48)) to the "increased-valence" structure (51).



Dinerman and Ewing¹⁰ have shown that the N-O stretching frequencies for gaseous NO and cis ONNO are very similar (1848 and 1860 cm^{-1}) and obtained a small dissociation energy of 11 kJ mol^{-1} (c.f. 250 kJ mol^{-1} for N_2H_4 , Section 7-1). Ab-initio molecular orbital⁹ estimates of the N-N bond-lengths for the cis and trans dimers are 1.768 \AA and 1.686 \AA . (A number of ab-initio studies have been reported more recently¹¹). The N-N and N-O bond-lengths and the ONN bond-angles for the cis isomer in the gas phase have been estimated⁸ to be approximately 1.75 \AA , 1.15 \AA and 90° . Molecular beam electron resonance spectroscopy¹² of the gaseous cis isomer give $2.33(12)\text{ \AA}$, $1.15(1)\text{ \AA}$ and $95(5)^\circ$ respectively for these lengths and angles. For the molecular crystal^{13,14}, the N-N length of 2.18 \AA is very long (c.f. 1.45 \AA for N_2H_4 , Section 7-1). The ONON isomer has been characterized recently^{8,15}, with a weak N-O bond linking the NO moieties. The bond-lengths for Cl_2O_2 have not yet been ascertained, but isomers of types (54) and (55) are considered to have been detected¹⁶⁻¹⁸. Essentially "increased-valence" descriptions of the bonding for Cl_2O_2 have been provided by Linnett¹⁹.

The geometry for a cis dimer of SO has been reported, with S-S and S-O bond-lengths of 2.025 and 1.458 \AA . The SO monomer, with two Pauling "3-electron bonds" in its valence-bond structure (31), has a bond-length of 1.481 \AA . On dimerization, "increased-valence" structure (59), with fractional S-S σ - and π -bonds, is obtained. Inspection of (31) and (59) makes clear why the SO bond-lengths for the monomer and dimer are similar, and why the S-S bond for the dimer (with an S-S bond-number < 2 in (59)) is appreciably longer than the length of 1.89 \AA for the double-bond of S_2 .

The geometry (Fig. 11-4a) for the cation $S_2I_4^{2+}$ has been reported recently²⁰. A convenient "increased-valence" structure, namely (b) of Fig. 11-4, can be constructed by spin-pairing the antibonding π_x^* and π_y^* electrons of ground-state S_2 with

the unpaired-electrons for two I_2^+ radicals. On the basis of this structure, it would be predicted that the S-S and I-I bond lengths would be similar to the 1.89 and 2.56 Å for free S_2 and I_2^+ . The observed shortening of the S-S bond and lengthening of the I-I bonds imply that other types of valence-bond structures such as (c) participate significantly in resonance with (b). In each $S_2I_2^+$ component of these structures, there is an "increased-valence" representation for a cyclic 6-electron 4-centre bonding unit. All structures account for the observation that the S-I bond-lengths are much longer than the estimate²¹ of 2.37 Å for a "normal" S-I single bond.

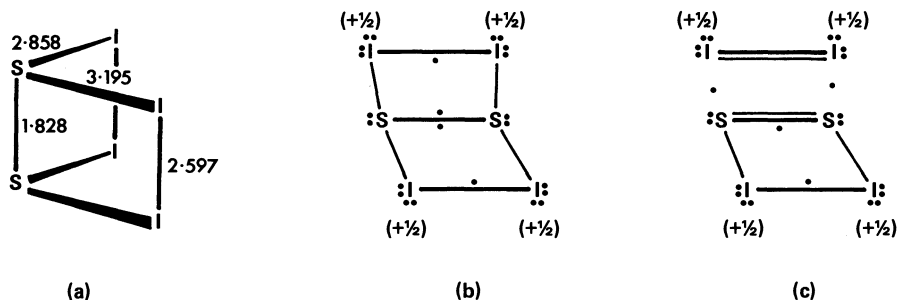
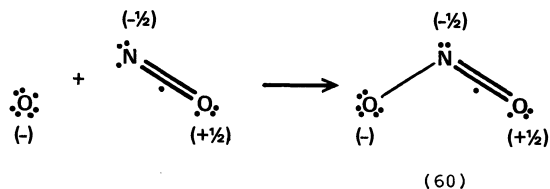


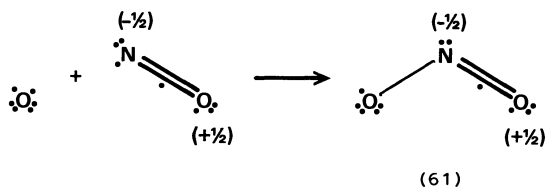
Figure 11-4 Bond-lengths and "increased-valence" structures for $S_2I_4^{2+}$.

11-8 NO_2 , NO_2^- , ClO_2 , SO_2^- AND SO_3

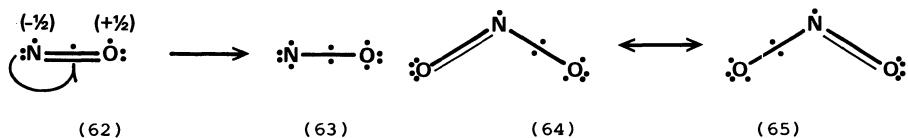
We shall now demonstrate that to obtain suitable "increased-valence" structures for some molecules, it is necessary either to use an excited state for the component diatomic system, or to re-organize the electron distribution of the "increased-valence" structure which is obtained using the diatomic ground-state.

In Section 11-6, we constructed suitable "increased-valence" structures for NO_2^- by bonding together O with NO^- . By combining O^- with NO , and O and NO , we may obtain "increased-valence" structures (60) and (61) for NO_2^- and NO_2 .





These "increased-valence" structures, together with their mirror images, indicate that the N-O properties for both systems should be very similar. However, the measured lengths of 1.24 Å (NO_2^-) and 1.19 Å (NO_2) differ significantly. E.s.r. studies²² of NO_2 indicate appreciable unpaired-electron charge (about 1/2 electron) located in a nitrogen orbital (Section 6-1). "Increased-valence" structure (61) locates the unpaired electron solely on the oxygen atom. We may conclude that (60) and (61) give unsatisfactory representations of the electronic structures of NO_2^- and NO_2 . However, if we use an excited state for NO, we can generate a more suitable type of valence-bond structure for NO_2 . The valence-bond structure for the NO ground-state, (62), can form only one bond with a second oxygen atom by using its unpaired electron. We can increase the valence of the nitrogen atom by promoting a nitrogen 2s electron into the antibonding NO π^* orbital which is vacant in (62). This $s_N \rightarrow \pi_{\text{NO}}^*$ promotion generates the valence-bond structure (63), with two Pauling "3-electron bonds".



By bonding (63) for NO to an oxygen atom ($:\ddot{O}:$) in its ground-state, "increased-valence" structures (64) and (65) are obtained for NO_2 . Resonance between these structures generates fractional odd-electron charge on each atom and, when compared with (38) \leftrightarrow (39) for NO_2^- , this resonance accounts for the observed shortening of the N-O bond-lengths of NO_2 relative to those of NO_2^- .

It may be noted here that resonance between "increased-valence" structures (64) and (65) is equivalent to resonance between the Lewis structures of Fig. 11-5. Structures (a)-(d) are the structures (1)-(4) of Section 6-1, and each of (e)-(g) has a long O-O π -bond. The absence of formal charges for (e) would suggest that it should make an important contribution to the ground-state resonance.

An alternative method that may be used to construct "increased-valence" structures (38) and (39) for NO_2^- , and (64) and (65) for NO_2 , involves the electronic reorganization displayed in Fig. 11-6 for "increased-valence" structures (60) and (61). This involves the delocalization of non-bonding electrons into bonding

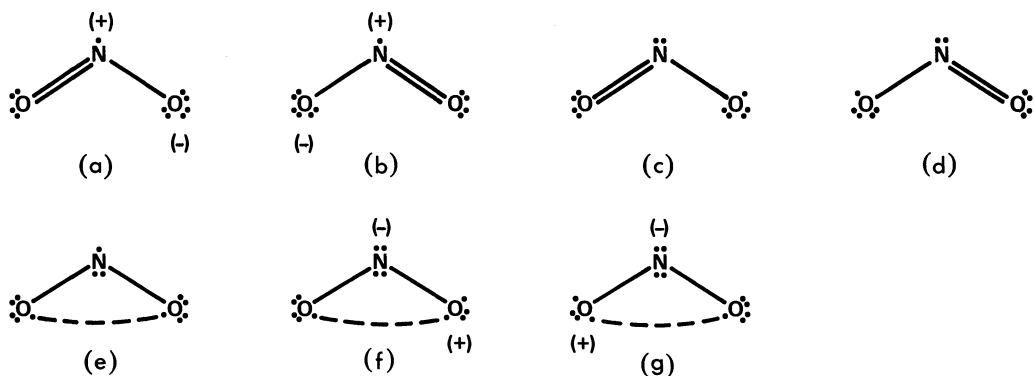


Figure 11-5 Component valence-bond structures for NO₂ "increased-valence" structures (64) and (65).

orbitals (Chapter 12), and simultaneously, the transfer of a bonding electron into an atomic orbital. Similar types of electronic reorganization are also displayed in Fig. 11-6 for ClO₂, SO₂⁻ and SO₃, when they are formed from O + ClO, O⁻ + SO and 2O + SO. For each of these latter structures, the formal charge separations are the smallest that are in accord with the presence of the maximum number of one-electron bonds and fractional electron-pair bonds.

11-9 N₂O₄, N₂O₃ AND FNO₂

In Sections 7-1 and 7-2 we have provided Lewis valence-bond and molecular orbital explanations for the existence of a long N-N bond for N₂O₄. The N-N and N-F bond-lengths for N₂O₃ and FNO₂ are also longer than single bonds (Table 11-1).

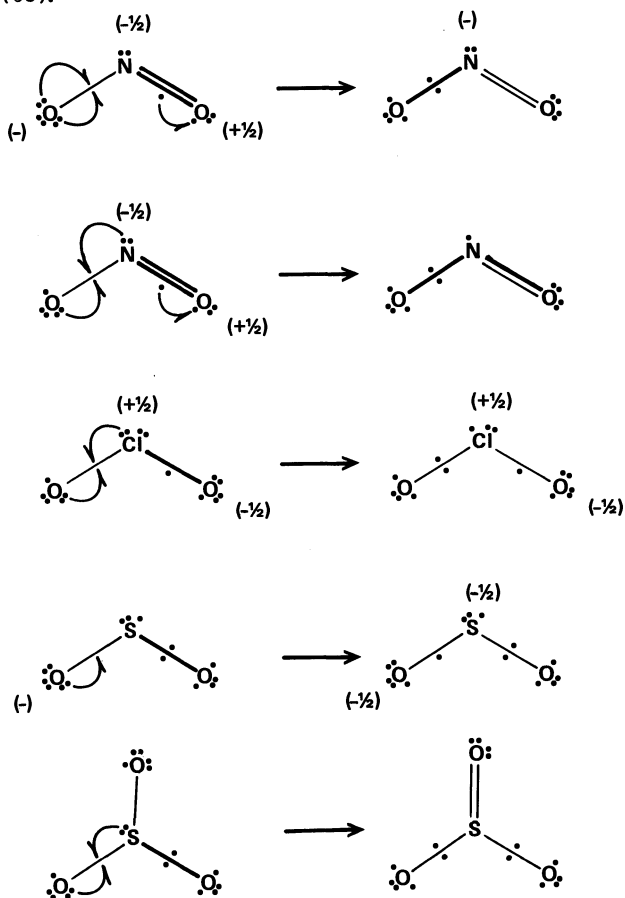
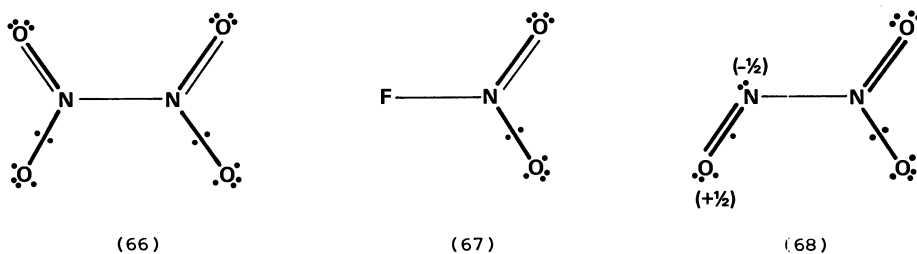


Figure 11-6 Construction of "increased-valence" structures for NO₂⁻, NO₂, ClO₂, SO₂⁻ and SO₃ from NO + O⁻, NO + O, ClO + O, SO + O⁻ and SO + O + O.

By using the NO and NO₂ valence-bond structures (62) and (64) of Section 11-8, together with the reactions NO₂ + NO₂, NO + NO₂ and F + NO₂, we may construct the "increased-valence" structures (66)-(68) for N₂O₄, N₂O₃ and FNO₂. It is easy to deduce that "increased-valence" structure (66) for N₂O₄ summarizes resonance between 16 Lewis octet structures, namely those of Fig. 11-7. Of these latter structures, eleven do not have N-N electron-pair bonds, and the absence of formal charges for some of them suggests that they make important contributions to the ground-state resonance description of the electronic structure. Consequently, the N-N bond-number for the "increased-valence" structure (66) is rather less than unity, which implies that the N-N bond for N₂O₄ is longer than a single bond. The lengthenings of the N-F and N-N bonds for FNO₂ and N₂O₃ may similarly be deduced from an examination of "increased-valence" structures (67) and (68).



"Increased-valence" structure (68) for FNO₂ summarizes resonance between the Lewis octet structures of Fig. 11-8. Two of them carry zero formal charges on all

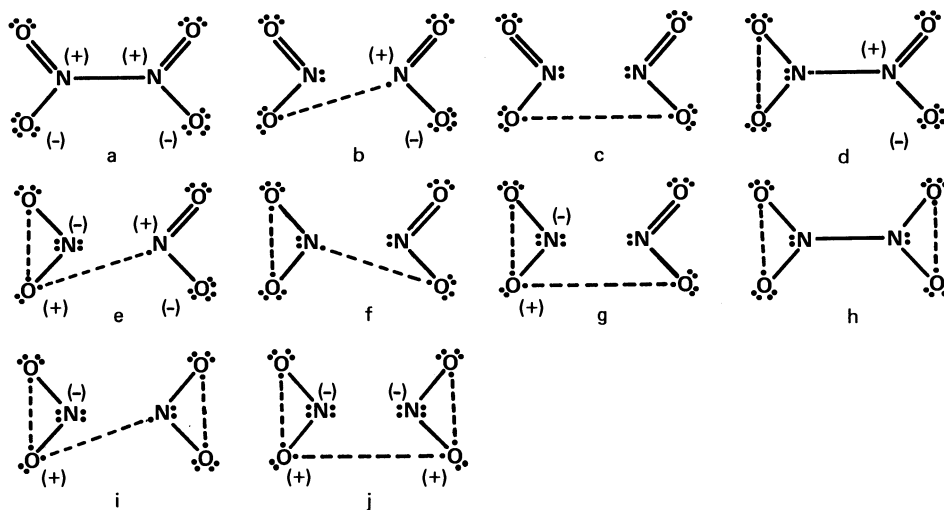


Figure 11-7 Component octet Lewis structures for N₂O₄ "increased-valence" structure (66). (Equivalent mirror-image structures are not displayed.)

atoms, and involve a "long" O-F or O-O bond. Roso's bond-eigenfunction coefficients for all structures are reported in the figure, and they imply that these "long-bond" structures may be more important than is the standard Lewis structure (a).

For each of N_2O_4 , N_2O_3 and FNO_2 , the N-O bond-lengths of Table 11-1 for the nitro-linkages are similar to the N-O double-bond length of 1.20 Å. Resonance between "increased-valence" structures of types (66)-(68) indicates why this similarity exists better than does resonance between the standard Lewis structures (e.g. types (a) for each of Figs. 11-7 and 11-8).

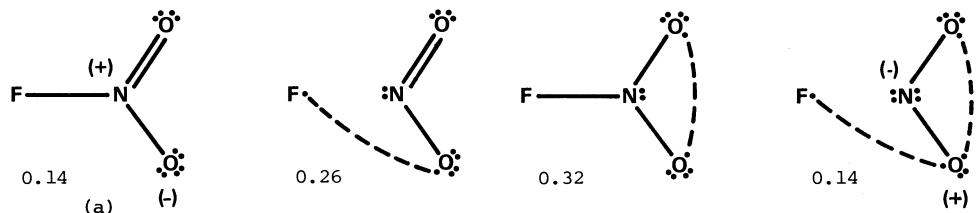
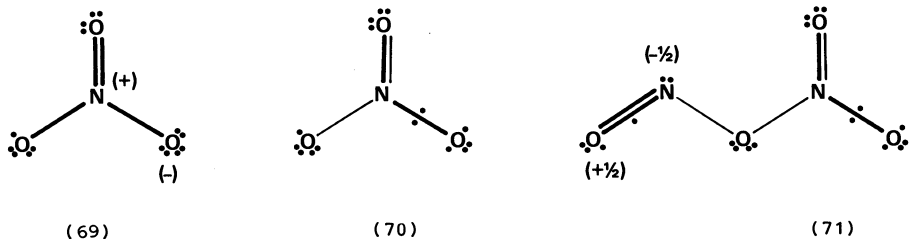


Figure 11-8 Component Lewis structures for FNO_2 "increased-valence" structure (67), together with bond-eigenfunction coefficients²⁴.

11-10 SYM NO_3 AND ASYM N_2O_4

In Section 6-5, we have given consideration to the valence-bond structures of type (69) for *sym* NO_3 . An "increased-valence" structure for this radical may be obtained by spin-pairing the odd-electron of NO_2 with an unpaired electron of an oxygen atom in its ground-state, when the NO_2 is represented by an "increased-valence" structure of type (64). The resulting "increased-valence" structure for *sym* NO_3 , namely (70), has two more bonding electrons than has (69), and therefore it is more stable. Because it does not involve formal charge separation, (70) is in accord with the requirements of the electroneutrality principle. The location of the odd-electron in an oxygen π -electron atomic orbital in these valence-bond structures is in accord with the results of e.s.r. measurements and molecular orbital considerations²⁵.



Fateley et al.²⁶ have identified an *asym* N₂O₄ isomer ONONO₂ in a nitrogen matrix, and have assigned infra-red frequencies of 1654 cm⁻¹ and 1290 cm⁻¹ to the asymmetric and symmetric stretches of the nitro (NO₂) linkage. These may be compared with 1748 cm⁻¹ and 1261 cm⁻¹ for the *sym* N₂O₄ (O₂NNO₂) isomer²⁷ in a nitrogen matrix. (The gas-phase frequencies²⁸ for the latter isomer are 1758 cm⁻¹ and 1264 cm⁻¹.) An 1829 cm⁻¹ frequency for *asym* N₂O₄ is similar to the 1876 cm⁻¹ frequency for the N-O stretch of free NO, and both are rather larger than the 1562 cm⁻¹ and 1564 cm⁻¹ stretching frequencies for the N-O double bonds²⁹ of HNO and CH₃NO. "Increased-valence" structures of type (70), which may be generated by spin-pairing the odd electrons of NO and NO₃ with the valence-bond structures of (62) and (70), are in accord with these observations.

Very recently, the peroxy O₂NO isomer of NO₃ has been identified³⁰ as one of the products of the gas phase reactions NO + O₂ and NO + O₃. "Increased-valence" structures for the *cis* and *trans* isomers may be obtained by spin-pairing the unpaired electron of (62) for NO with one of the unpaired electrons of (23) for O₂, as described in ref. 31.

11-11 CONCLUSIONS

By starting with Pauling "3-electron bond" structures for one or more diatomic systems, we have found that it is possible to construct "increased-valence" structures for polyatomic molecules. Often, use of the ground-states of the diatomic systems leads quickly to suitable polyatomic valence-bond structures. For NO₂, we needed to go through an excited state of NO in order to obtain a suitable "increased-valence" structure. This is also the case for many other molecules. However, valence-bond structures for excited states for diatomic systems are often not easily written down and it may not always be obvious how to commence to do so. Fortunately, it is possible to circumvent this problem by generating "increased-valence" structures from familiar standard Lewis structures for polyatomic molecules. In the following chapters, we shall describe how this may be done.

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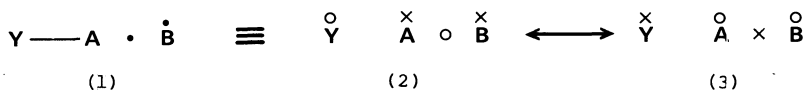
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CHAPTER 12

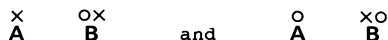
INCREASED-VALENCE STRUCTURES CONSTRUCTED FROM LEWIS STRUCTURES: DELOCALIZATION OF LONE-PAIR ELECTRONS INTO VACANT BONDING ORBITALS

For diamagnetic polyatomic molecules, it is very easy to write down standard Lewis structures that have electron-pair bonds and lone-pairs of electrons. It is then also easy to generate "increased-valence" structures from them. To do this, we must delocalize one or more lone-pair electrons into *either* two-centre bonding orbitals or two-centre antibonding orbitals, both types of orbitals being vacant in the standard Lewis structures. In this chapter, we shall describe these delocalizations into bonding orbitals in some detail.

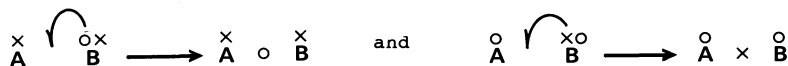
In Section 11-1, we demonstrated that "increased-valence" structure (1) involves the electron spin distributions of (2) and (3).



The wave-functions for the $\overset{\times}{\text{A}} \text{ } \overset{\times}{\text{O}} \text{ } \overset{\times}{\text{B}}$ and $\overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}$ structures of (2) and (3) utilize the orbitals a , $\psi_{ab} = a + kb$ and b , in which a and b are overlapping atomic orbitals that are centred on atoms A and B (Section 3-6). The s_z spin quantum numbers for the electrons that occupy these orbitals are $+\frac{1}{2}$, $-\frac{1}{2}$, and $+\frac{1}{2}$, and $-\frac{1}{2}$, $+\frac{1}{2}$ and $-\frac{1}{2}$. We may obtain the valence-bond structures $\overset{\times}{\text{A}} \text{ } \overset{\times}{\text{O}} \text{ } \overset{\circ}{\text{B}}$ and $\overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}$ by starting with the electron arrangements of

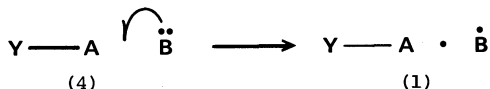


and then delocalizing an $s_z = +\frac{1}{2}(\times)$ or $s_z = -\frac{1}{2}(\circ)$ electron of B into a bonding A-B orbital. Thus, we may write



in which we have transferred one electron from the atomic orbital b into the bonding molecular orbital $\psi_{ab} = a + kb$. To indicate a one electron-transfer we have used a "curly arrow"¹, with a single barb¹⁻³, i.e. \curvearrowright .

These considerations imply that we may generate the "increased-valence" structure (1) from the standard Lewis structure (4) by delocalizing a B electron of (4) into a vacant bonding A-B orbital, i.e. by writing

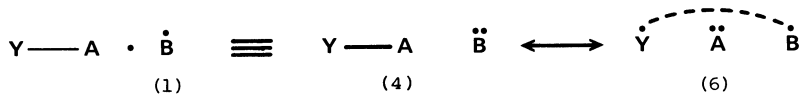


Whenever the a and b atomic orbitals overlap, the delocalization of (4) must *always* occur to some extent. It will be helped considerably if atoms A and B carry formal positive and negative charges respectively. The delocalization will then reduce the magnitudes of these formal charges. Thus, if after the delocalization, the A-B bonding electron is shared equally by the two atoms, then the A and B formal charges become $+\frac{1}{2}$ and $-\frac{1}{2}$, i.e.



In general, the electron of the A-B bond will not be shared equally by the A and B atoms, and the resulting formal charges will not be 1/2-integer in magnitude. Our example here is illustrative of formal charge reduction. However (in accord with what has been done in the previous chapters) for illustrative purposes only, formal charges are assigned on the assumption that bonding electrons are shared equally by a pair of adjacent atoms; see also Section 2-5(b).

Even if A and B carry no formal charges in (4), it is energetically advantageous to delocalize the B electron into the vacant bonding A-B orbital. By doing so, we increase the number of electrons that can participate in the overall bonding. We have already shown in Section 11-1 that (1) summarizes resonance between the standard Lewis structure (4) and the "long-bond" Lewis structure (6), and therefore any B electron delocalization into a bonding A-B orbital will stabilize (4) by means of its resonance with (6).



When describing the ground-states of neutral molecules, it is desirable that the formal charges be small in magnitude, i.e. less than unity. This requirement should be particularly appropriate when atoms A and B have fairly similar neutral atom electronegativities.

In Chapter 11, we have found that fluorine atoms could stabilize the Pauling "3-electron bond(s)" of NO, O₂, SO and S₂, and that "increased-valence" structures (8) and (10) are suitable valence-bond structures for FNO and F₂O₂. Therefore, if we write down the standard Lewis structures (7) and (9), the fluorine atom(s) must induce appreciable delocalization of oxygen lone-pair electron(s) into the bonding N-O and O-O orbitals. We have indicated these delocalizations in (7) and (9). On the other hand, hydrogen atoms do not generate appreciable stabilization of Pauling "3-electron bonds" (Sections 11-3 and 11-4) of 4-electron 3-centre bonding units in neutral molecules, and similar oxygen delocalizations for HNO and H₂O₂ must occur only to a very small extent. We have found that the standard Lewis structures (11) and (12) alone are adequate simple representations of the electronic structures of these molecules.

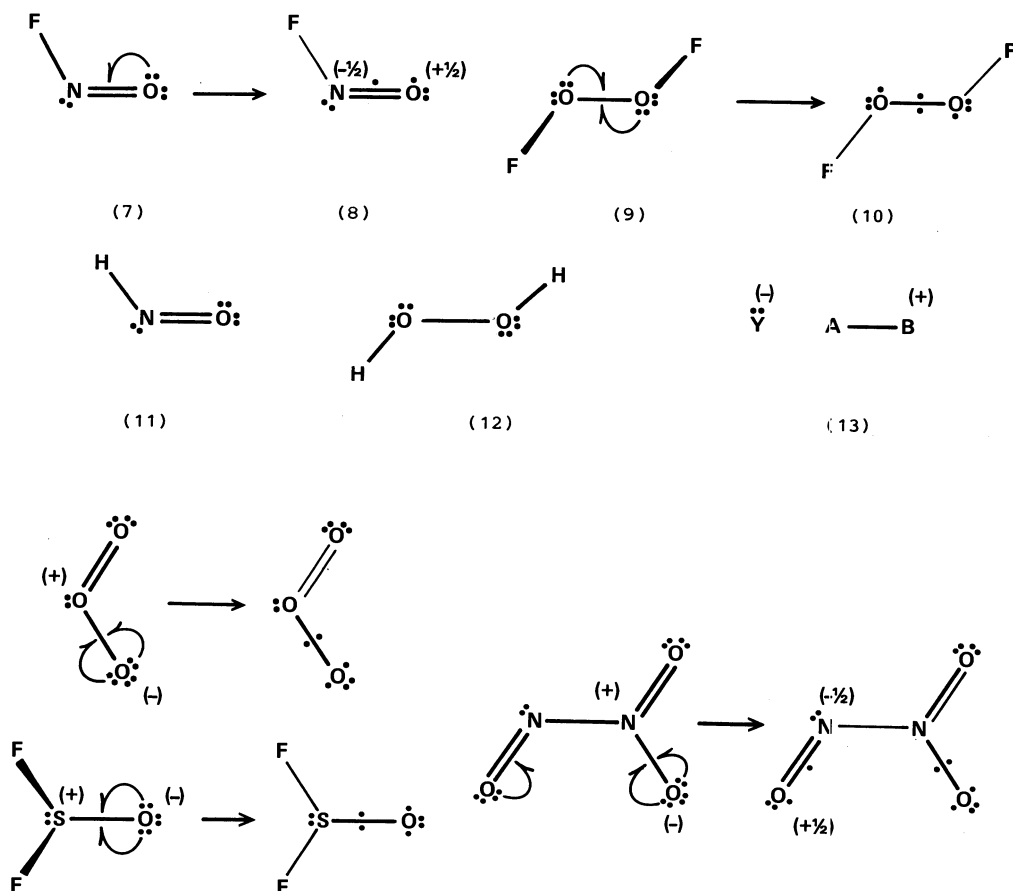


Figure 12-1 Generation of "increased-valence" structures from standard Lewis structures by delocalizing lone-pair electrons into vacant bonding orbitals.

In Fig. 12-1, we show how to use the standard Lewis structures to construct some of the "increased-valence" structures that we have considered previously in Chapter 11. For each molecule, one or more lone-pair electrons have been delocalized into vacant 2-centre bonding orbitals. This technique for generating "increased-valence" structures (and thereby stabilizing the Lewis structure) can be used whenever the arrangement of electrons shown in (4) occurs in a Lewis valence-bond structure. This must surely be the case for thousands of molecular systems!

The question may be asked, "How will such a delocalization reduce the magnitudes of the formal charges for a standard Lewis structure of type (13)?" Delocalization of a Y electron into a bonding Y-A orbital will not reduce the magnitude of

the formal charge on B. To obtain this effect, it is necessary to delocalize a π electron of (13) into an antibonding A-B orbital. This procedure will be described in Chapter 14. However, in Chapter 13, we shall use the technique described in the present chapter (namely of delocalizing non-bonding electrons into bonding orbitals) to construct "increased-valence" structures for various types of N -centre bonding units.

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- 2 R.D. Harcourt, *J. Chem. Educ.* **45**, 779 (1968); **46**, 856 (1969).
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CHAPTER 13

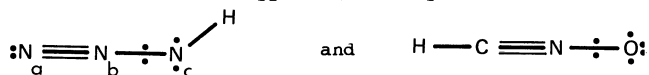
"INCREASED-VALENCE" STRUCTURES FOR n -CENTRE BONDING UNITS

The technique described in Chapter 12 for constructing "increased-valence" structures, namely that of delocalizing one or more non-bonding electrons of a standard Lewis structure into adjacent bonding orbitals, is quite general and easily applied. We shall now use this method to construct "increased-valence" structures for numerous molecular systems that involve 6-electron 5-centre, 8-electron 6-centre and longer N -centre bonding units, as well as for some molecules with 4-electron 3-centre and 6-electron 4-centre bonding units. In general, we shall find that only one or two "increased-valence" structures are required in order to make deductions concerning bond lengths that are in qualitative accord with the measured lengths, i.e. for the systems considered, "increased-valence" structures provide easily derived and economical representations of their electronic structures.

13-1 N_2O AND SOME ISOELECTRONIC MOLECULES AND IONS WITH 4-ELECTRON 3-CENTRE BONDING UNITS

In Fig. 2-10 we have displayed four "increased-valence" structures for N_2O , namely (I)-(IV) of Fig. 13-1, here. They may be generated from the standard Lewis structures (1)-(4) of Fig. 2-8 by delocalizing non-bonding π - and $\bar{\pi}$ -electrons from the terminal nitrogen and oxygen atoms into adjacent N-N and N-O π - and $\bar{\pi}$ -bonding orbitals, as is indicated in Fig. 13-1. In Section 2-5, we have used the electroneutrality principle to deduce that (I) should be the most important of the four "increased-valence" structures, and have then deduced from (I) that the N-N and N-O bond-lengths for N_2O should be respectively longer than an N-N triple bond, and similar to an N-O double bond. The bond-lengths reported in Table 13-1 are in accord with this deduction.

For HN_3 and $HCNO$, which are isoelectronic with N_2O , the standard Lewis and "increased-valence" structures are similar to those for N_2O , except for the replacement of the O and terminal N of N_2O with N-H and H-C, respectively. From the "increased-valence" structures of type (I), namely



we may deduce that the N_a - N_b and C-N bonds should be longer than triple bonds, and that the N_b - N_c and N-O bond-lengths should be similar to those of double bonds. With the possible exception of the C-N bond for $HCNO$, the bond-lengths reported in Table 13-1 are in accord with these deductions.

The symmetrical triatomic species N_3^- , NO_2^+ and CO_2 are also isoelectronic with N_2O . Their standard Lewis and "increased-valence" structures are displayed in Fig.

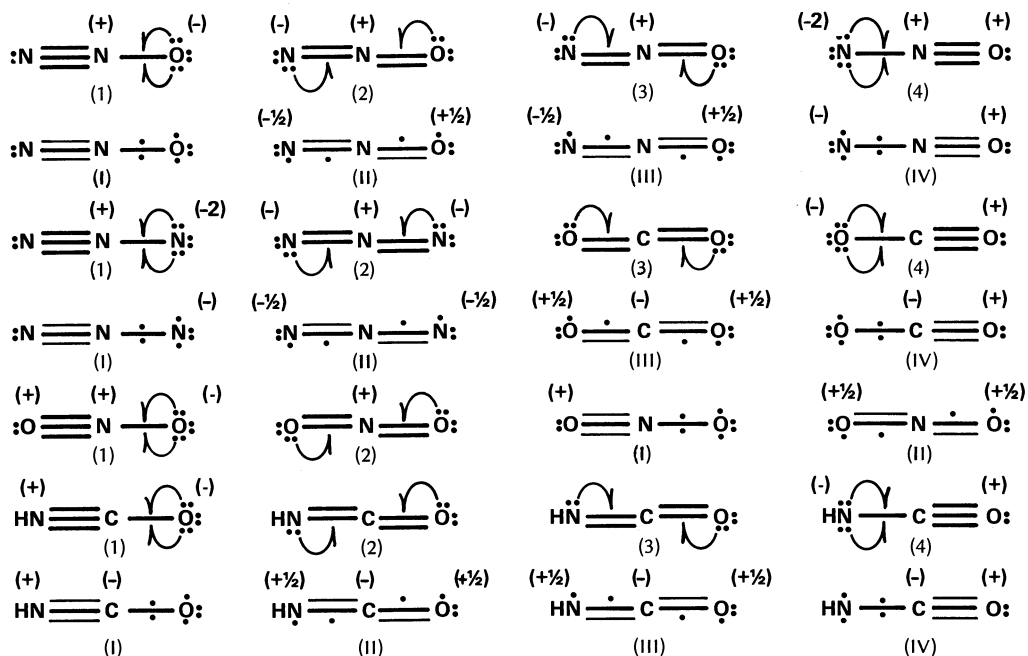


Figure 13-1 Standard Lewis and "increased-valence" structures for N_2O , N_3^- , CO_2 , NO_2^+ and $HNCO$. For N_3^- , CO_2 , and NO_2^+ , the symmetrically-equivalent structures are not displayed.

	N-N or C-N	N-O, C-O or N-NH
N_2O	1.129	1.188
HN_3	1.133	1.237
N_3^-	1.176	
$HCNO$	1.161	1.207
NO_2^+		1.153
CO_2		1.162
$HNCO$	1.207	1.171

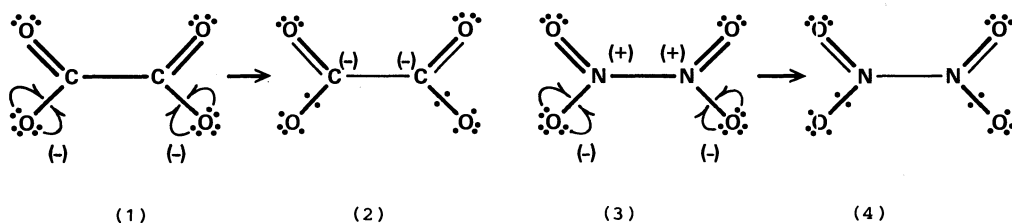
Table 13-1 Bond-lengths¹⁻⁷ (Å) for some isoelectronic systems with 16 valence-shell electrons. See also Ref. 8. Estimates of standard triple and double bond lengths are⁹: $C \equiv N$, 1.15 Å; $N \equiv N$, 1.10 Å; $C = N$, 1.27 Å; $N = N$, 1.24 Å; $C = O$, 1.21 Å; $N = O$, 1.20 Å.

13-1. For each of these systems, resonance between the four "increased-valence" structures indicates more clearly than does resonance between the standard Lewis structures that the N-N, N-O and C-O bond-lengths of 1.18 Å, 1.15 Å and 1.16 Å are shorter than those of double-bonds (see Table 13-1). The smaller formal charges

for "increased-valence" structures (II) and (III) suggest that these are the most important of the four "increased-valence" structures, and inspection of them alone makes clear why the bond-lengths are shorter than double-bonds. Similar types of "increased-valence" structures should also be the primary structures for HNCO. Inspection of them in Fig. 13-1 leads to the conclusion that the C-N and C-O bonds are both shorter than double bonds, and the bond-lengths reported in Table 13-1 support this conclusion.

13-2 N_2O_4 , $\text{C}_2\text{O}_4^{2-}$ AND $(\text{RNO})_2$, WITH 6-ELECTRON 4-CENTRE BONDING UNITS

To generate the "increased-valence" structures for NO_2^+ and CO_2 , we have delocalized oxygen non-bonding π - and $\bar{\pi}$ -electrons into the adjacent N-O and C-O bonding π - and $\bar{\pi}$ -orbitals. However, because these delocalizations lead to the formation of a negative formal charge on the carbon atom of CO_2 , they should be less extensive than are those that occur for NO_2^+ . Similarly, for $\text{C}_2\text{O}_4^{2-}$ the delocalizations of the (O^-) oxygen π - and $\bar{\pi}$ -electrons for the standard Lewis structures of type (1) should be less extensive than they are for (3) for N_2O_4 . In the resulting "increased-valence" structures (2) and (4), the carbon atoms carry formal negative charges, whereas the nitrogen atoms are uncharged. One consequence of a reduced degree of π - and $\bar{\pi}$ -delocalization for $\text{C}_2\text{O}_4^{2-}$ is that the C-O bond orders are smaller than are the N-O bond-orders for N_2O_4 . If we use this result when we compare (2) and (4), we are able to account¹⁰ for the observation that the C-O bond-lengths¹¹ of 1.26 Å for $\text{C}_2\text{O}_4^{2-}$ are longer than a C-O double bond (1.21 Å), whereas the N-O bond-lengths¹² of 1.19 Å for N_2O_4 are similar to the double-bond length of 1.20 Å. The smaller extent of $\bar{\pi}$ _O delocalization for $\text{C}_2\text{O}_4^{2-}$ also generates a C-C σ -bond number for (2) that is larger than the N-N σ -bond number for (4). This accounts for the observation that the C-C bond-length of 1.57 Å¹¹ for $\text{C}_2\text{O}_4^{2-}$ is appreciably shorter than the N-N bond-length of 1.78 Å¹² for N_2O_4 ; see also Section 7-4.



For the C-nitroso dimers $(\text{RNO})_2$ of Table 13-2, the N-N and N-O bond-lengths are both longer than double-bond lengths. The standard Lewis structures of (5) may be used to generate the "increased-valence" structures of (6) by delocalizing the oxygen π - and $\bar{\pi}$ -electrons into bonding N-O orbitals. The "increased-valence"

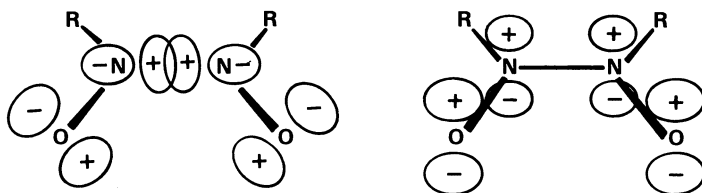


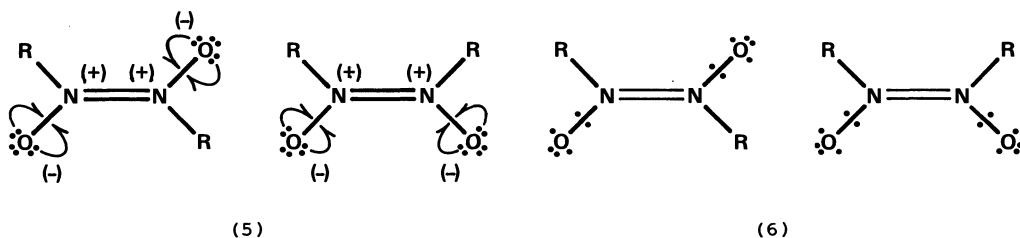
Figure 13-2 Atomic orbitals for 6-electron 4-centre bonding units of $(\text{RNO})_2$.

structures, with zero formal charges on all atoms, imply that only the N-N bond should be longer than a double bond. However, because the overlap integral for the N-N σ -bond (0.6₅) is larger than the 0.3 for the corresponding bond of N_2O_4 , the $\bar{\pi}$ -electron delocalization must occur to a much smaller extent for $(\text{RNO})_2$ than it does for N_2O_4 , and therefore the N-O $\bar{\pi}$ -bond order for $(\text{RNO})_2$ does not reach the maximum value of 0.5 that obtains for (6) when zero formal charges are present. This reduced N-O bond-order leads to the lengthening of the N-O bonds for $(\text{RNO})_2$ relative to the essentially double-bond lengths for N_2O_4 .

compound names	bond length \AA^a			geometry	ref ^e
	C-N	N-N	N-O		
<i>cis</i> -Azobenzene dioxide (Nitrosobenzene dimer)	1.454 (5)	1.321 (5)	1.268 (4)	Cis	present work
<i>trans</i> -2.2-Dicarboxyazobenzene dioxide (2-Nitrosobenzoic acid dimer)	1.460 (3)	1.308 (3)	1.267 (3)	Trans	present work
Perfluoroazobenzene dioxide (Pentafluoronitrosobenzene dimer)	1.439 (6)	1.324 (5)	1.267 (6)	Cis	41
1,8-Dinitrosonaphthalene (Internal dimer)	1.430 (6)	1.376 (5)	1.276 (6)	Cis	25
Nitrosocyclohexane	1.488 (6)	1.319 (6)	1.272 (6)	Trans	19
2-Nitronitrosoethane	1.470 (4) ^b	1.304 (6)	1.262 (4) ^c	Trans	18
Azoxyanisole	1.496 (5)	1.218 (5)	1.279 (4)	Trans	42
Azobenzene ^d	1.433 (3)	1.243 (3)		Trans	43
<i>p,p'</i> -Dichloroazobenzene	1.433 (5)	1.252 (5)		Trans	44

^a Estimated standard deviations are given in parentheses. ^b The C-N bond involving the nitroso group. ^c The N-O bond of the nitroso group. ^d Two unique molecules are present in the unit cell, one of which is disordered. The data presented are from the nondisordered molecule. The estimated standard deviations may be severely underestimated. ^e See Ref. 13 for details of these references.

Table 13-2 Bond-lengths for dimeric nitroso and structurally similar compounds¹³.

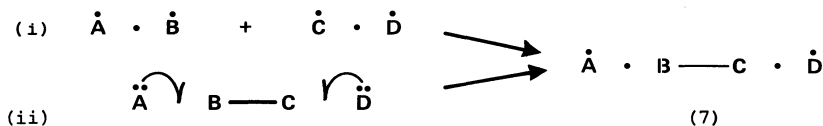


13-3 SOME COMMENTS ON 6-ELECTRON 4-CENTRE BONDING UNITS

Two "increased-valence" bonding units of general type (7) are present in the "increased-valence" structures of (6); one for the six π -electrons and one for six $\bar{\pi} + \sigma$ -electrons. The relevant atomic orbitals are displayed in Fig. 13-2 for the cis isomer. The latter type of "increased-valence" bonding unit is also present in (2) and (4) for six $\bar{\pi} + \sigma$ -electrons of $\text{C}_2\text{O}_4^{2-}$ and N_2O_4 . In this and the previous chapters, we have introduced two techniques that may be used to generate (7), namely

- (i) To bond together two Pauling "3-electron bond" structures $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ and $\overset{\cdot}{\text{C}} \cdot \overset{\cdot}{\text{D}}$ (with antiparallel spins for the two antibonding odd-electrons), and
- (ii) To delocalize non-bonding $\overset{\cdot\cdot}{\text{A}}$ and $\overset{\cdot\cdot}{\text{D}}$ electrons of the standard Lewis structure $\overset{\cdot\cdot}{\text{A}}-\text{B}=\text{C}-\overset{\cdot\cdot}{\text{D}}$ into the adjacent A-B and C-D bonding orbitals.

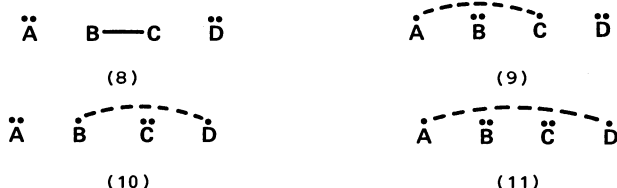
Thus, we may write



"Increased-valence" structure (7) may be generated whenever 6-electron 4-centre bonding can occur, i.e. whenever six electrons may be distributed amongst four overlapping atomic orbitals. For the special case that A and D and B and C are pairs of equivalent atoms (and therefore a and d, and b and c are pairs of equivalent atomic orbitals), the 4-centre molecular orbitals are given by Eqn. (1), in which λ and μ are parameters, both > 0 . If atomic orbital overlap integrals are omitted from the normalizing constants and the orthogonality relationships, then the molecular orbitals of Eqn. (1) are orthogonal. The mobile σ -electron molecular orbitals of Eqs. 7-3 to 7-6 for N_2O_4 are particular examples of these orbitals.

$$\begin{aligned}
 \psi_1 &= \{a + d + \lambda(b + c)\} / (2 + 2\lambda^2)^{\frac{1}{2}} \\
 \psi_2 &= \{a - d + \mu(b - c)\} / (2 + 2\mu^2)^{\frac{1}{2}} \\
 \psi_3 &= \{\lambda(a + d) - (b + c)\} / (2 + 2\lambda^2)^{\frac{1}{2}} \\
 \psi_4 &= \{\mu(a - d) - (b - c)\} / (2 + 2\mu^2)^{\frac{1}{2}}
 \end{aligned} \tag{1}$$

To construct the molecular orbitals of Eqn. (1), we have assumed that the atomic orbitals are oriented so that all overlap integrals between adjacent atomic orbitals are > 0 , as occurs for the orbitals of Fig. 13-2, for example. Therefore, ψ_4 is A-B, B-C and C-D antibonding, and so it must be the highest-energy molecular orbital. The lowest-energy molecular orbital configuration for the six electrons is then $(\psi_1)^2(\psi_2)^2(\psi_3)^2$. In Section 10-2, we have deduced that this configuration may be expressed as $\Psi_{\text{covalent}} + \Psi_{\text{ionic}}$, and that Ψ_{covalent} is the wave-function for the "increased-valence" structure (7). It is easy to demonstrate that (7) summarizes resonance between the standard and "long-bond" Lewis structures (8)-(11); this is a result that we have obtained previously from the discussion of the bonding for N_2O_4 and N_2O_2 in Sections 10-1 and 11-7.



13-4 CYCLIC 6-ELECTRON 4-CENTRE BONDING UNITS

A number of cyclic molecules and ions, for example $(\text{SN})_2$ and Se_4^{2+} , have six π -electrons distributed amongst four $p\pi$ -atomic orbitals. The standard Lewis structures for Se_4^{2+} are displayed in Fig. 13-3(a). By delocalizing non-bonding π -electrons into the adjacent Se-Se π bonding-orbitals, we may generate the "increased-valence" structures of (b), each of which has an "increased-valence" bonding unit of type (7) for the six π -electrons. However, because the atoms of (b) that correspond to the A and D atoms of (7) are adjacent, their atomic orbitals can overlap well. Therefore, we shall represent these atoms as bonded together, to form the "increased-valence" structures of (c). Either of the structures of (c) involves a cyclic "increased-valence" bonding unit of type (12) or (13), each of which summarizes

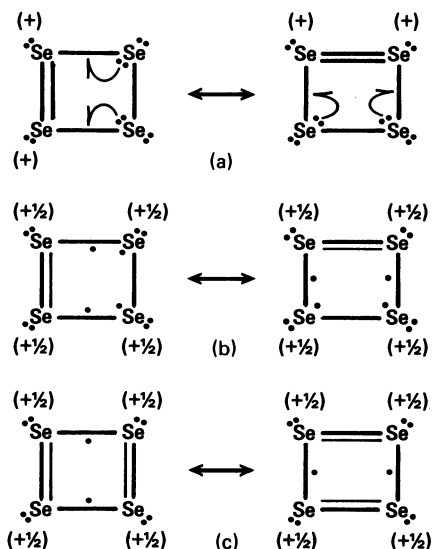


Figure 13-3 Standard Lewis and "increased-valence" structures for Se_4^{2+} . Mirror-image structures are not displayed for (a) and (b).

Resonance between these three structures is usually invoked to explain why the C-N and C-O bond-lengths¹⁸ of 1.34 Å and 1.27 Å are respectively shorter than the C-N single-bond length of 1.47 Å and longer than the C-O double-bond length of 1.21 Å. An alternative explanation may be obtained by consideration of the "increased-valence" structures of Fig. 13-4, which may be generated from the standard Lewis structures by means of the π -electron delocalizations that are indicated. The formal charges for the "increased-valence" structures suggest that (I) should be the most important of these structures, and it alone indicates that the C-O bond-number and C-N bond-orders are respectively less than two and greater than unity.

Each of the "increased-valence" structures of Fig. 13-4 involves an "increased-valence" bonding unit of type (17) for the six π -electrons. It summarizes¹⁰ resonance between the standard Lewis structure (18) and the two "long-bond" Lewis structures (19) and (20). (A fourth valence-bond structure (21), cannot be included in the resonance scheme, because it involves three electrons located in the A-atom atomic orbital)

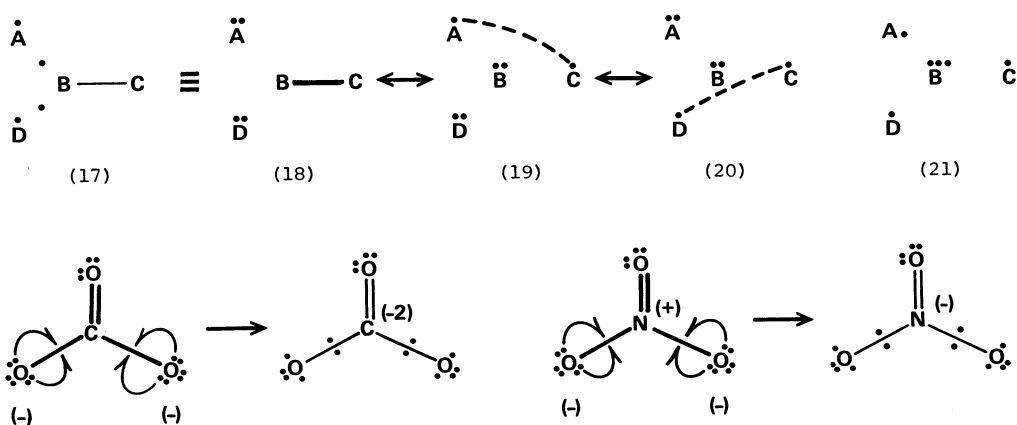


Figure 13-5 Standard Lewis and "increased-valence" structures for CO_3^{2-} and NO_3^- .

"Increased-valence" bonding units of type (17) also obtain for the NO_3^- and CO_3^{2-} anions, which are isoelectronic with $(\text{NH}_2)_2\text{CO}$. Their standard Lewis structures are displayed in Fig. 13-5. Each has standard valence-bond arrangements of type (18) for the six π -electrons and sets of four $\bar{\pi}$ + two N-O or C-O σ -electrons. The relevant atomic orbitals are displayed in Fig. 13-6. Therefore, when we generate the "increased-valence" structures of Fig. 13-5 (by delocalizing the oxygen π - and $\bar{\pi}$ -electrons into bonding N-O or C-O orbitals), two "increased-valence" bonding units of type (17) will be formed. Because the N^+ for the standard Lewis structures of NO_3^- is more electronegative than the C for CO_3^{2-} , the delocalizations of the oxygen π - and $\bar{\pi}$ -electrons for NO_3^- will be more appreciable than they are for CO_3^{2-} (c.f.

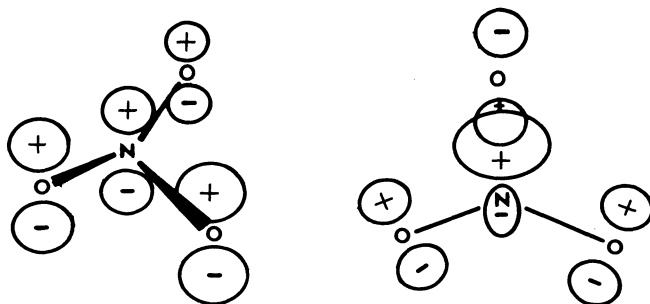


Figure 13-6 Atomic orbitals involved in the formation of 6-electron 4-centre bonding units for the valence-bond structures of Figure 13-5.

N_2O_4 and $\text{C}_2\text{O}_4^{2-}$ of Section 13-2). Therefore, the N-O bond-orders will be larger than the C-O bond-orders, and this is reflected in the bond-lengths. The N-O lengths of 1.22 Å for NO_3^- (as in NaNO_3)¹⁹ are only 0.02 Å longer than the N-O double-bond length of 1.20 Å, whereas for CO_3^{2-} , C-O lengths of 1.28 Å²⁰ are 0.07 Å longer than a double bond. Because of the symmetry of the anions, each of three "increased-valence" structures will contribute equally to the resonance, and therefore, no economy is obtained by using the "increased-valence" structures instead of the standard Lewis structures to describe the electronic structure. However, resonance between the three standard Lewis structures does not indicate why the C-O and N-O bond-orders should differ, and why the N-O bond-lengths for NO_3^- are so similar to those of double bonds.

13-6 6-ELECTRON 5-CENTRE BONDING UNITS

The phenomenon of 6-electron 5-centre bonding²¹ is conveniently introduced by consideration of the π -electron distribution for linear C_3O_2 . The standard Lewis structures (22)-(25) (together with the mirror image structures for (22)-(24)) reveal that this molecule has two sets of six π -electrons (π and $\bar{\pi}$ or π_x and π_y), each of which is distributed amongst five overlapping atomic orbitals. The orbitals are displayed in Fig. 13-7 for one set of electrons. For each set of π -electrons, the standard Lewis structures are of the general types (26)-(28), with two electron-pair bonds and a

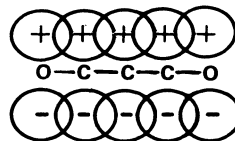
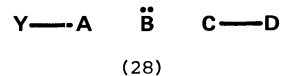
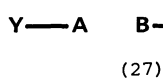
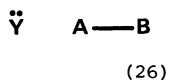
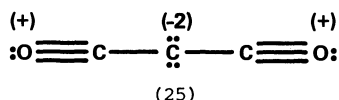
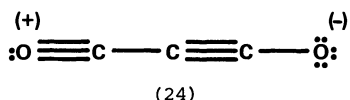
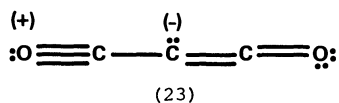
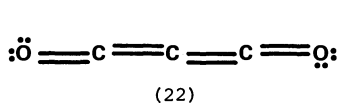
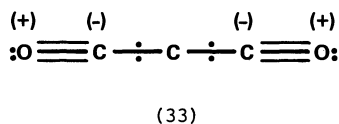
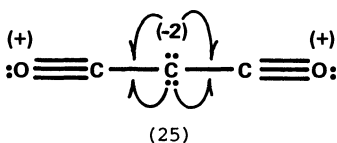
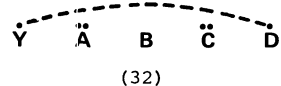
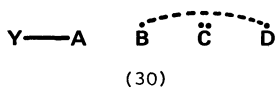
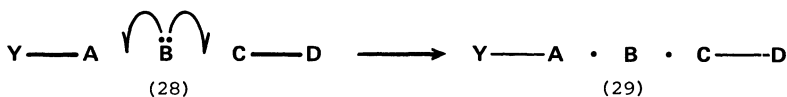


Figure 13-7 $2p\pi$ atomic orbitals for C_3O_2 .

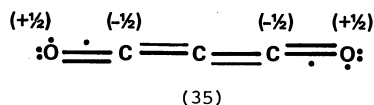
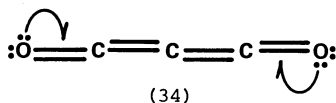
lone-pair of electrons. The C-C and C-O bond lengths²² of 1.28 Å and 1.16 Å may be compared with²³ 1.34 Å for $\text{H}_2\text{C}=\text{CH}_2$ (with sp^2 hybridized carbon atoms) and 1.13 Å for $:\text{C}\equiv\text{O}:$. Resonance between structures of types (22)-(25) is sometimes used to rationalize the bond-length variations. However, a more economical valence-bond representation of the electronic structure, which also accounts for the observed lengths, may be obtained in the following manner.



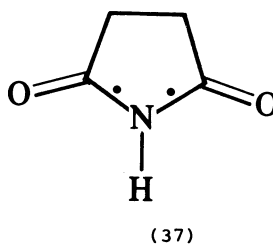
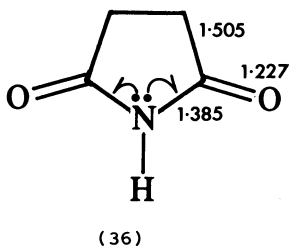
Starting with the standard Lewis structure (28), we may delocalize both of the non-bonding B electrons into the adjacent A-B and B-C bonding orbitals to form two 1-electron bonds. The resulting "increased-valence" structure (29) summarizes resonance between (28) and the "long-bond" structures (30)-(32). When this type of delocalization is applied to the C^{2-} π and $\bar{\pi}$ electrons of (25), "increased-valence" structure (33) is obtained, which summarizes resonance between (25) and 13 "long-bond" structures. Inspection of (33) indicates that the C-C bond-lengths should be similar to those of double bonds with $s-p$ hybridization²⁴ for the carbon σ -orbitals (1.30 Å), and that the C-O lengths should be longer than the 1.13 Å for free carbon monoxide ($:\text{C}\equiv\text{O}:$).



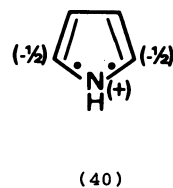
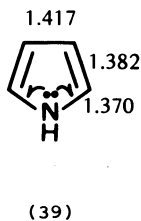
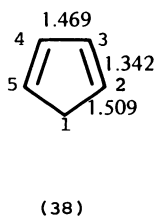
In (29) all adjacent atoms are represented as bonded together simultaneously, and two fractional electron-pair bonds are present. From each of (26) and (27), it is also possible to generate an "increased-valence" structure for a 4-electron 3-centre bonding unit by delocalizing a non-bonding Y or D electron into the adjacent Y-A or C-D bonding orbitals. When this type of delocalization is applied to the C_3O_2 structures of types (22)-(24), numerous "increased-valence" structures are obtained, all of which will participate in resonance with (33). For example, the oxygen π and $\bar{\pi}$ delocalizations displayed in (34) generate (35). These latter types of "increased-valence" structures involve fewer electrons in bonding than does (33).

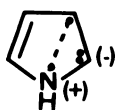


Molecules such as succinimide and pyrrole also provide a 6-electron 5-centre bonding unit for π -electrons. For succinimide with the geometry²⁶ reported in (36), the "increased-valence" structure (37) accounts immediately for the observed lengthenings and shortening of the C-O and C-N bonds relative to the standard double and single-bond lengths of 1.21 Å and 1.47 Å.

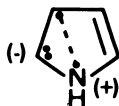


For pyrrole, it is of interest to compare the C-C bond-lengths²⁷ of (39) with the corresponding bonds for cyclopentadiene in (38)²⁸. Thus, the C_2-C_3 and C_4-C_5 bonds are longer in pyrrole, whereas the C_3-C_4 bond is shorter. The bond properties that are implied by "increased-valence" structure (40) are in accord with these observations. Although it is concealed, there is some C_3-C_4 π -bonding in (40); this bonding arises because (40) \equiv (39) \leftrightarrow (41) \leftrightarrow (42) \leftrightarrow (43), and (43) has a C_3-C_4 π -bond. "Increased-valence" structure (40) also involves some C-N π -bonding, and the C-N bonds of pyrrole are shorter than the standard single-bond length of 1.47 Å.

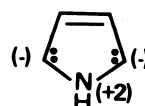




(41)

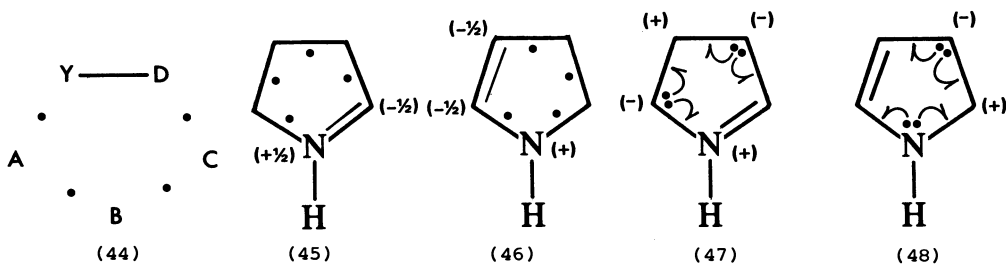


(42)



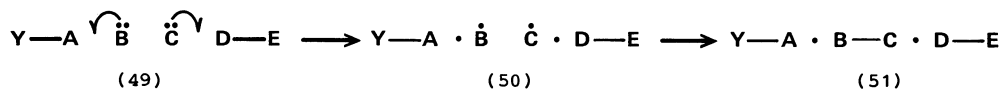
(43)

For pyrrole, the π -electrons form a cyclic 6-electron 5-centre bonding unit, in which the Y and D atoms are adjacent in the general valence-bond structures (26)-(32). The Y-D bond of (32) then becomes a normal bond, as it is in (43). Another type of cyclic "increased-valence" structure may also be constructed, namely (44) (as in (45) and (46), for example in pyrrole). "Increased-valence" structure (44) is more stable than (29), but we shall not pursue this matter here. To obtain (45) and (46) for pyrrole, it is necessary to write down the non-octet structures (47) and (48), and then to delocalize the non-bonding π -electrons into the adjacent bonding orbitals.



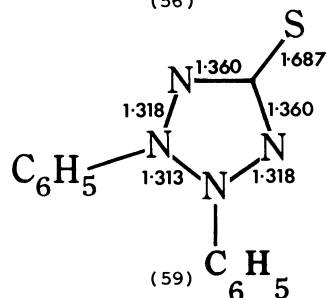
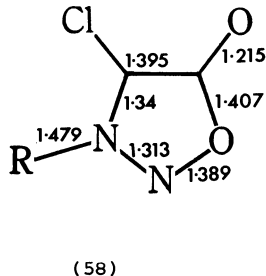
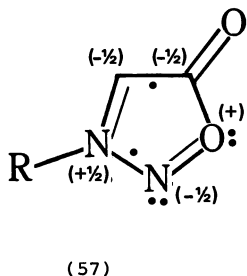
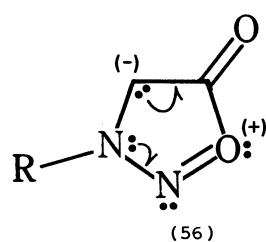
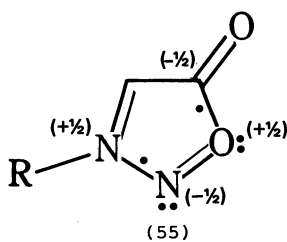
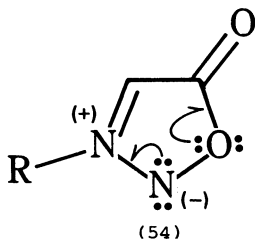
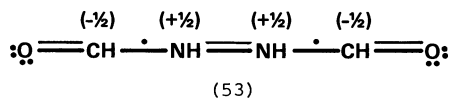
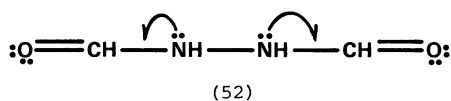
13-7 8-ELECTRON 6-CENTRE BONDING UNITS

For molecules that involve a set of eight electrons distributed amongst six overlapping atomic orbitals, three types of "increased-valence" bonding units may be relevant for descriptions of their electronic structures. One of them, namely (51), may be obtained either by bonding together the "increased-valence" structures for two 4-electron 3-centre bonding units, namely those of (50), or by writing down the standard Lewis structure (49), and then delocalizing a non-bonding electron from each of the B and C atoms into the adjacent A-B and C-D bonding orbitals. "Increased-valence" structure (50) is thereby generated by these delocalizations; it leads to the formation of (51) when the fractional odd-electron charges on the B and C atoms are spin-paired.



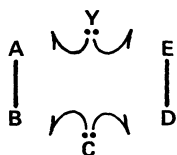
This procedure may be used to generate "increased-valence" structure (53) for diformylhydrazine from the standard Lewis structure (52). From (53), it may be deduced that each of the N-N, N-C and C-O bond-lengths should be intermediate in length between those for single and double bonds (N—N 1.45 Å; N≡N, 1.24 Å; N—C, 1.47 Å; N≡C, 1.27 Å; C—O, 1.43 Å; C≡O, 1.21 Å), and the measured bond-lengths²⁹ (N-N = 1.383 Å, N-C = 1.333 Å and C-O = 1.234 Å) show that this is the case.

Diformylhydrazine has eight π -electrons, as have the N-alkyl sydnone. For the sydnone, eight standard Lewis structures may be written down, each of which involves formal charge separation. Two of these structures, namely (54) and (56), may be used to generate "increased-valence" structures (55) and (57), each of which as an "increased-valence" representation of type (51) for the π -electrons. The experimental bond-lengths^{30,31} displayed in (58) indicate that the five bonds of the heterocyclic ring have partial double bond character if the standard N-N, C-N, N-O, C-O and C-C bond-lengths are assumed to be 1.45 Å, 1.47 Å, 1.44 Å, 1.43 Å and (for sp^2 hybridized carbon) 1.51 Å. Resonance between (55) and (57) accounts for this observation. However, the exocyclic C-O bond-length of 1.215 Å is imperceptibly longer than that of a double bond (1.21 Å), whereas both "increased-valence" structures imply that it should be a little longer.

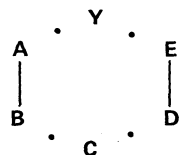


Other types of "increased-valence" structures may be constructed for 8-electron 6-centre bonding units. Two of them, namely (61) and (63) may be generated from the standard Lewis structures (60) and (62) by means of the

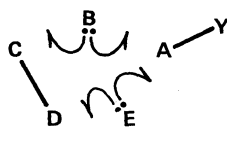
delocalizations indicated. For dehydrodithizone, the arrangement of (63) is present for the π -electrons in "increased-valence" structure (65). The bond-lengths³² are displayed in (59), and all of them are intermediate in length between those for single and double bonds. "Increased-valence" structure (65) (which has been derived from the standard Lewis structure (64)), indicates the presence of partial double bond character for all bonds. Use of "increased-valence" structure (65) provides a more economical representation of this effect; if only standard Lewis structures are used, three of them are required to provide partial double-bond character for each of the six bonds.



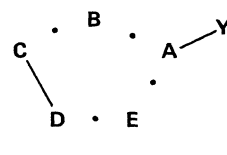
(60)



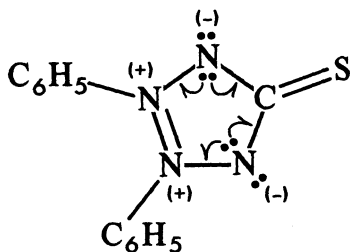
(61)



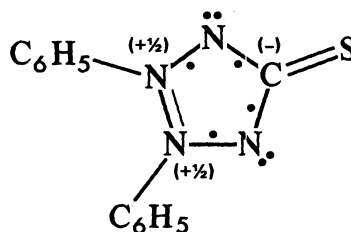
(62)



(63)



(64)



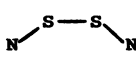
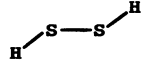
(65)

13-8 "INCREASED-VALENCE" STRUCTURES FOR LONGER *N*-CENTRE BONDING UNITS

Fairly obviously, it is possible to extend the length of an "increased-valence" bonding unit in order to describe many instances of *N*-centre bonding. To demonstrate this, we shall examine three systems with S-N bonds.

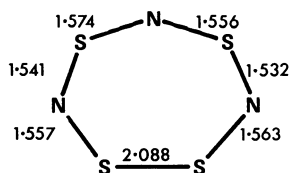
13-8(a) $S_4N_3^+$: 10-electron 7-centre bonding The $S_4N_3^+$ cation is planar and cyclic with the geometry^{33,34} of (66). It has ten π -electrons distributed amongst seven overlapping p -atomic orbitals. The S-N bond-lengths are all shorter than the estimate of 1.67 Å for the length of an S-N single-bond³⁵. From the standard Lewis structure (67), we may generate "increased-valence" structure (68), which involves a 10-electron 7-centre "increased-valence" bonding unit of type (69), and indicates the presence of partial double-bond character for all of the S-N bonds. If only the standard structures are used to represent the electronic structure of $S_4N_3^+$, it is

necessary to invoke resonance between (67) and four other valence-bond structures that differ in the positions of the two S-N π -bonds. Therefore, the main qualitative features of the electronic structure may be described more economically by using the "increased-valence" structure for $S_4N_3^+$. This "increased-valence" structure (68) associates partial double-bond character with each of the S-N bonds, thereby accounting for the observed shortening of these bonds relative to the single-bond length. Partial double-bond character is also present in (68) for the S-S bond, but the length of this bond (2.070, 2.088 Å) is longer rather than shorter than the standard single-bond length of 2.06 Å for H_2S_2 . This lengthening may be a consequence of a combination of the following factors:

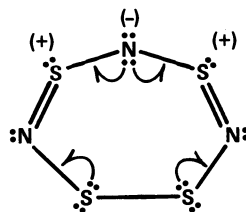
- (a) The  linkage is planar, whereas  is non-planar. Hordvik³⁶ has listed numerous examples of molecules for which the S-S bond-length varies with dihedral angle. The straining of the S-S σ -bonds is associated³⁷ with the existence of the non-bonded repulsions (Section 3-10) in standard Lewis structures such as (67) (which is a component of (68)) for $S_4N_3^+$. Therefore, if the natural conformation around the S-S bond is non-planar, the additional strain that occurs when planarity is enforced must lengthen³⁸ the S-S σ -bond.
- (b) For $S_4N_3^+NO_3^-$ and $S_4N_3^+Br^-$, lone-pair orbitals of the anions can overlap with the orbitals that form the S-S σ -bond of $S_4N_3^+$, to form 4-electron 3-centre or 6-electron 4-centre bonding units³⁹. The "increased-valence" structures $X \cdot \cdot S-S$ and $X \cdot \cdot S-S \cdot \cdot X$, which are obtained by delocalizing lone-pair X^- electrons into bonding X-S orbitals, have S-S σ -bond numbers that are less than unity.

Which of (a) and (b) is of greater relevance has yet to be ascertained, but if the S-S σ -bond of $S_4N_3^+$ is lengthened by either or both of them, then the measured S-S lengths^{33,34} of 2.088 or 2.070 Å do not preclude the presence of some S-S π -bonding.

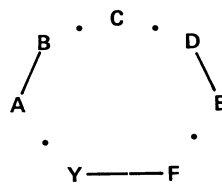
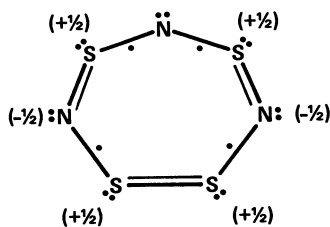
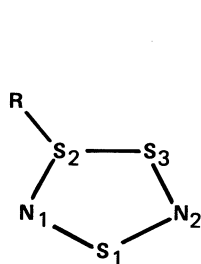
Similar considerations have also been used³⁸ to account for the lengthenings of the S-S bonds for the $S_3N_2^+$ derivatives (with planar $S_3N_2^+$ rings) listed in Table 13-3.



(66)



(67)



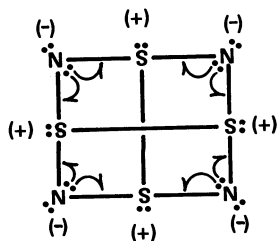
(68)

(69)

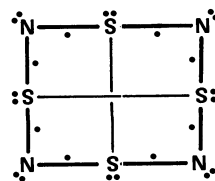
compound	S ₁ -N ₁	S ₁ -N ₂	S ₂ -N ₁	S ₃ -N ₂	S ₂ -S ₃
S ₃ N ₂ ⁺	1.575	1.555	1.617	1.602	2.141
S ₆ N ₄ ²⁺	1.569	1.569	1.605	1.605	2.154
S ₃ N ₂ C1 ⁺	1.617	1.543	1.581	1.615	2.136
S ₃ N ₂ -NSO ₂ F	1.578	1.565	1.644	1.635	2.200
S ₃ N ₂ -NCOCF ₃	1.589	1.551	1.641	1.633	2.206
S ₃ N ₂ -NP ₃ N ₃ F ₅	1.573	1.540	1.647	1.528	2.220

Table 13-3 Bond-lengths (Å) for S₃N₂ rings of S₃N₂⁺ and derivatives³⁹⁻⁴⁴.

13-8(b) S₄N₄: 12-electron 8-centre bonding In Section 7-7, a molecular orbital explanation for the existence of long S-S bonds (2.58 Å⁴⁵, c.f. 2.06 Å for an S-S single-bond) in S₄N₄ was provided. It was suggested that one set of nitrogen lone-pair electrons of the standard Lewis structure (70) could delocalize appreciably into the antibonding S-S σ*-orbital, thereby reducing the S-S bond-order well below the value of unity that pertains for (70). If these electrons are delocalized into the adjacent S-N bonding-orbitals, "increased-valence" structure (71) is obtained^{21,38} with S-S σ-bond numbers less than unity. This structure indicates that the S-S and S-N bonds should be respectively longer and shorter than single-bonds, and this they are found to be. The measured S-S and S-N bond-lengths are 2.58 Å and 1.62 Å, respectively, and the estimate of an S-N single-bond length³⁵ is 1.67 Å. A 12-electron 8-centre "increased-valence" bonding unit is present in "increased-valence" structure (71); it involves the eight nitrogen π-electrons and the four S-S σ-electrons of (70).



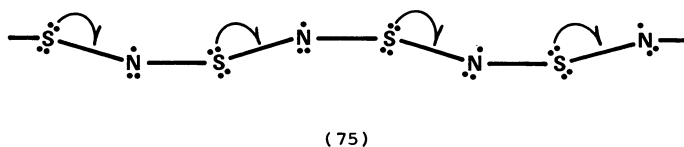
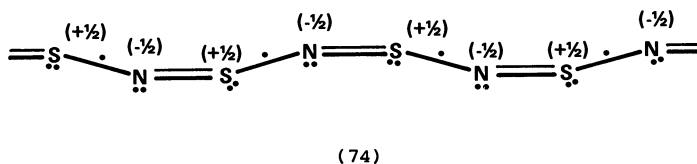
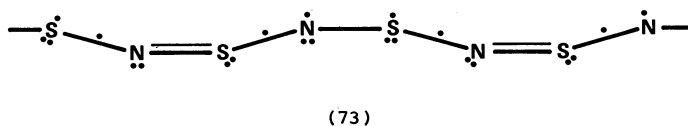
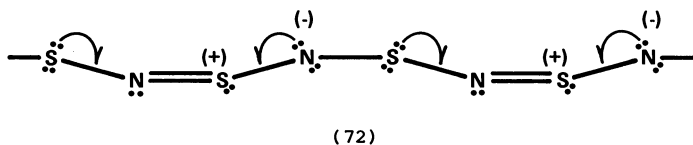
(70)

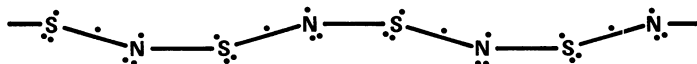


(71)

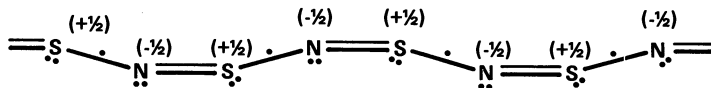
"Increased-valence" descriptions of the bonding for other cyclic S-N compounds are described in Refs. 21 and 38.

13-8(c) (SN)_x: Polymerized Pauling "3-electron bonds" and Polymerized 6-Electron 4-Centre bonding units The polymer (SN)_x consists of layers of 2-dimensional chains of alternating sulphur and nitrogen atoms. Each sulphur and nitrogen atom contributes respectively two π -electrons and one π -electron to form a 2x-centre π -electron bonding unit within a 2-dimensional chain⁴⁶. For such a chain, the standard Lewis structures are of type (72), from which the "increased-valence" structure (74)²¹ may be generated via (73) and the delocalizations indicated in (72). Alternatively, we may also obtain (74) by writing down the "long-bond" structure (75) with zero formal charges on all atoms, and then proceed to (74) via (76) by delocalizing non-bonding sulphur electrons into adjacent S-N bonding π -orbitals. Examination of (76) shows that "increased-valence" structure (74) is constructed from polymerized Pauling "3-electron bond" structures for the S-N π -electrons. Alternatively, (74) may also be considered to involve the polymerization of the 6-electron 4-centre "increased-valence" structures for the π -electrons of (73). "Increased-valence" structure (74) involves partial double-bond character for each of the S-N bonds, which is in accord with the measured bond-lengths⁴⁶ of 1.59 Å and 1.63 Å.





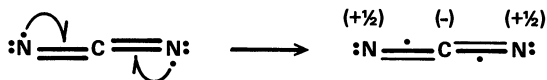
(76)



(74)

13-9 PARAMAGNETIC "INCREASED-VALENCE" STRUCTURES

All "increased-valence" structures that we have described so far are appropriate when an even number of electrons is present in the N -centre bonding unit. Therefore, they can be constructed for diamagnetic $S = 0$ spin-states. When an odd number of electrons is involved in N -centre bonding, paramagnetic "increased-valence" bonding units are also possible. The smallest of them pertain for 3-electron 3-centre, 5-electron 4-centre and 7-electron 5-centre bonding. They are exemplified in the "increased-valence" structures for (78) for CN_2 and the bimolecular HO_3 and ONO_3 complexes that pertain for the $\text{H} + \text{O}_3 \rightarrow \text{HO} + \text{O}_2$ and $\text{NO} + \text{O}_3 \rightarrow \text{NO}_2 + \text{O}_2$ reactions. "Increased-valence" mechanisms for these reactions will be described in Chapter 22. The general "increased-valence" structures for 5-electron 4-centre and 7-electron 5-centre bonding units are of types (79) and (80) respectively. They may be constructed by bonding the "increased-valence" structure $\text{Y}-\text{A} \cdot \text{B}$ to either an atom C with one unpaired electron, or to the diatomic Pauling "3-electron bond" structure $\text{C} \cdot \text{D}$, as is shown. Electron spin theory for (79) is described in Section 15-2. "Increased-valence" structure (78) for CN_2 , which may be generated from the Lewis structure (77), involves no Pauling "3-electron bond". It may be noted that 3-electron 3-centre bonding units are not electron-rich, but "increased-valence" structures can be constructed for them. A second example is provided by H_3 , with the Lewis and "increased-valence" structures of (81) and (82). It is easy to verify that "long-bond" structures are not components of "increased-valence" structures for 3-electron 3-centre bonding units.

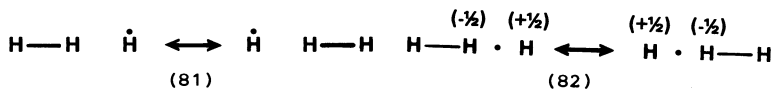
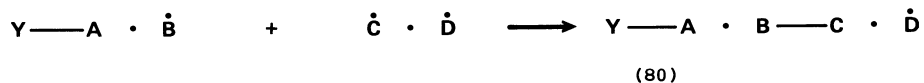


(77)

(78)



(79)



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CHAPTER 14

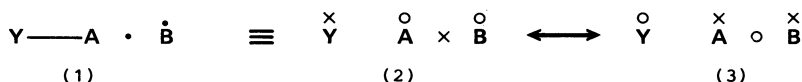
DELOCALIZATION OF LONE-PAIR ELECTRONS INTO ANTIBONDING ORBITALS: INCREASED-VALENCE STRUCTURES, MOLECULAR ORBITAL THEORY AND ATOMIC VALENCIES

Three related topics that involve diatomic antibonding orbitals will be discussed in this chapter. Firstly, "increased-valence" structures for 4-electron 3-centre bonding units will be constructed by delocalizing a lone-pair electron on one atom into an antibonding orbital between a pair of adjacent atoms. Then the approximate 3-centre molecular orbital theory that arises from delocalization of lone-pair electrons into an antibonding orbital will be presented, with emphasis given to the relationship that exists between the "increased-valence" and the molecular orbital theory. Finally, by making particular use of the charge distribution for antibonding orbitals, expressions for atomic valencies will be deduced for "increased-valence" structures.

14-1 DELOCALIZATION OF LONE-PAIR ELECTRONS INTO ANTIBONDING ORBITALS

The third method for generating "increased-valence" structures utilizes the molecular orbital description of the Pauling "3-electron bond" in terms of bonding and antibonding orbitals.

We shall commence our discussion by recalling that "increased-valence" structure (1) involves the electron spin distributions of (2) and (3).



In Section 3-6, we have demonstrated that the wave-function for a Pauling "3-electron bond" structure $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ may be expressed as either $(\psi_{ab})^2(\psi_{ab}^*)^1$ or $(a)^1(\psi_{ab})^1(b)^1$, ($\equiv a^\alpha \psi_{ab}^\beta b^\alpha$ or $a^\beta \psi_{ab}^\alpha b^\beta$), in which $\psi_{ab} = a + kb$ and $\psi_{ab}^* = k^* a - b$ are bonding and antibonding molecular orbitals, and a and b are overlapping atomic orbitals. For the Pauling "3-electron bond" structures $\overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}$ and $\overset{\times}{\text{A}} \circ \overset{\times}{\text{B}}$ of (2) and (3), the antibonding ψ_{ab}^* electron of the molecular orbital configuration $(\psi_{ab})^2(\psi_{ab}^*)^1$ must have an s_z spin quantum number of $-1/2$ and $+1/2$ respectively.

This equivalence that exists between $(\psi_{ab})^2(\psi_{ab}^*)^1$ and $(a)^1(\psi_{ab})^1(b)^1$ indicates that we may obtain the electron distributions of (2) and (3) by writing down the standard Lewis structure (4), and then delocalizing one of the non-bonding $\overset{\cdot\cdot}{\text{Y}}$

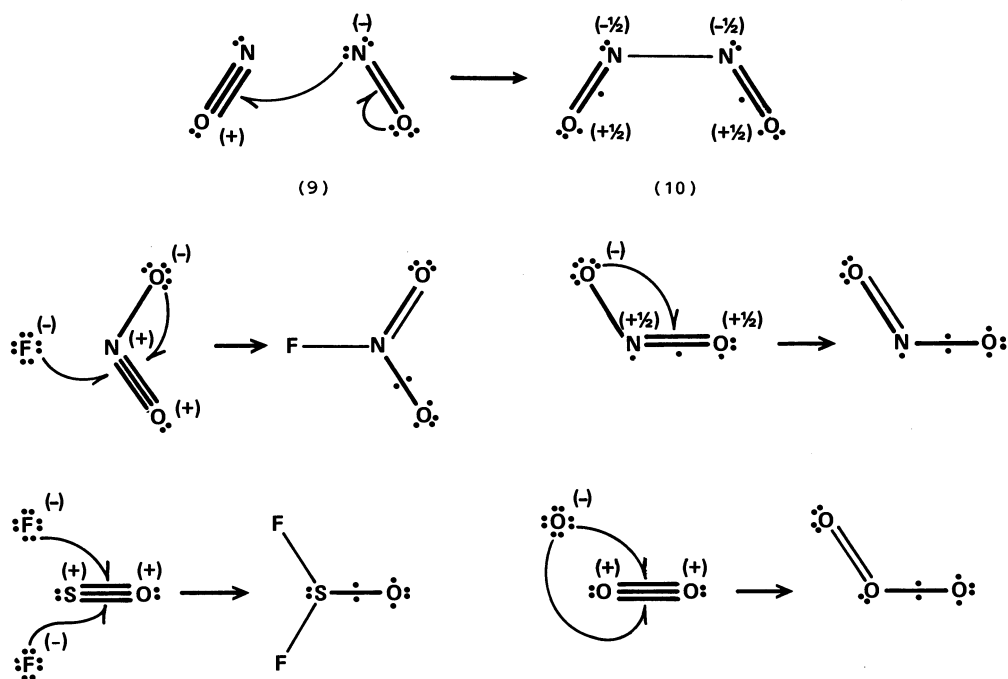
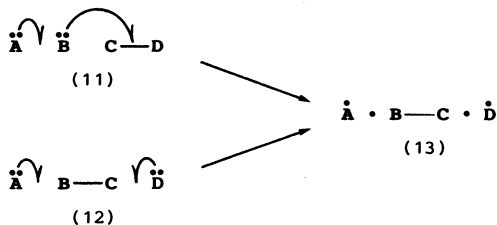


Figure 14-1 Generation of "increased-valence" structures for FNO_2 , NO_2 , F_2SO and O_3 from Lewis structures by delocalizing lone-pair electrons into vacant antibonding orbitals. For FNO_2 , F_2SO and O_3 , ionic Lewis structures have been written down.

This type of combined delocalization can be used whenever one has Lewis structures of type (11) for 6-electron 4-centre bonding units. On the other hand, the Lewis structure (12) requires delocalization of A and D electrons into bonding A-B and C-D orbitals in order to generate the "increased-valence" structure (13).

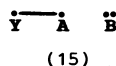


In this chapter, we have used both Heitler-London and molecular orbital descriptions of electron-pair bonds on different occasions. For example, a doubly occupied bonding molecular orbital (namely $(\psi_{ab})^2$) has been used to describe the electron-pair A-B bond of the standard Lewis structure (4), but when we delocalize a Y electron of (4) into the antibonding A-B orbital (ψ_{ab}^*), the resulting wavefunction (neglecting electron spin and indistinguishability)

$$(y)^1(\psi_{ab}^*)^1(\psi_{ab})^2 \equiv \text{constant} \times (y)^1(a)^1(\psi_{ab})^1(b)^1$$

indicates that the (fractional) Y-A bond of "increased-valence" structure (1) must have a Heitler-London type wave-function arising from the $(y)^1(a)^1$ configuration.

If one wishes to use only Heitler-London wave-functions for all electron-pair bonds, then instead of saying that we delocalize a Y electron of (4) into an antibonding A-B orbital, we may say that we delocalize a Y electron of (4) into the A and B atomic orbitals. When this is done, we obtain Lewis structures (14) and (15), with configurations $(y)^1(a)^2(b)^1$ and $(y)^1(a)^1(b)^2$ that involve Heitler-London formulations of the wave-functions for the "long" Y-B, and Y-A bonds. Resonance between (14) and (15) is equivalent to the utilization of "increased-valence" structure (1) (with a Heitler-London type wave-function for the fractional Y-A bond). However, to generate (1) from (4), it is colloquially simpler to speak of "delocalizing a Y electron into an antibonding A-B orbital", and we shall use this expression when it is appropriate to do so.



In Chapter 21, the theory of this section will be applied to Lewis acid-base reactions.

14-2 APPROXIMATE MOLECULAR ORBITAL THEORY FOR 4-ELECTRON 3-CENTRE BONDING UNITS

An approximate 3-centre molecular orbital theory has frequently been used to describe non-symmetrical 4-electron 3-centre bonding units. It involves the construction of an (approximate) 3-centre molecular orbital by linearly combining the Y lone-pair orbital with the vacant antibonding A-B orbital of the Lewis structure (4). This gives a 3-centre molecular orbital formulation for the phenomenon of lone-pair delocalization into an antibonding orbital (c.f. Sections 7-2 and 7-4 for 6-electron 4-centre bonding).

If the A-B bond of the standard Lewis structure (4) is described in terms of double occupation of the bonding molecular orbital ψ_{ab} , the wave-function[†] for this structure is given by Eqn. (1).

$$\Psi(\overset{\cdot\cdot}{Y} \quad A \text{---} B) = (y)^2(\psi_{ab})^2 \equiv |y^\alpha y^\beta \psi_{ab}^\alpha \psi_{ab}^\beta| \quad (1)$$

[†] Slater determinantal formulations for 4-electron 3-centre wave-functions are described in Section 15-1. Although they are not required for the algebra of this section, we have used them for the sake of completeness in Eqs. (1), (3), (4) and (8).

The vacant antibonding orbital ψ_{ab}^* overlaps with the doubly-occupied lone-pair orbital y . The approximate molecular orbitals of Eqn. (2) may then be constructed, which omit the overlap that also exists between y and the doubly-occupied ψ_{ab} .

$$\psi_1 = c_1 y + c_2 \psi_{ab}^*, \quad \psi_2 = c_2 y - c_1 \psi_{ab}^* \quad (2)$$

$$\Psi_1(\text{MO}) = (\psi_{ab})^2 (\psi_1)^2 \equiv |\psi_{ab}^\alpha \psi_{ab}^\beta \psi_1^\alpha \psi_1^\beta| \quad (3)$$

The lowest-energy molecular orbital configuration is then given by Eqn. (3), and this type of configuration has been frequently used or implied in qualitative molecular orbital descriptions of 4-electron 3-centre bonding units. Thus,

- (a) To account for transition metal-ligand and ligand bond-properties, back-donation of t_{2g} electrons from the metal into the antibonding π^* orbitals of CO, CN^- , NO^+ and N_2 ligands is invoked¹⁻⁵.
- (b) For some aliphatic chloro compounds that contain oxygen or fluorine atoms, Lucken⁶ has described the interaction of a p-orbital of either of these atoms with the antibonding C-Cl σ^* -orbital.
- (c) Williams⁷ has indicated that Lucken's theory might pertain to many saturated systems - for example, to account for the shortening of the C-F bonds and the lengthening of the C-H bond of CF_3H .
- (d) Spratley and Pimentel⁸ have described the relative extent of interaction of fluorine or hydrogen atomic orbitals with antibonding N-O or O-O π^* orbitals of FNO, HNO, F_2O_2 and H_2O_2 .
- (e) Pearson's⁹ molecular orbital description of $\text{S}_{\text{N}}2$ reactions involves the interaction of a lone-pair orbital of the nucleophile B with the antibonding C-Cl σ^* orbital of $\text{CH}_3\text{-Cl}$.
- (f) Drago and Corden¹⁰ have recently reviewed the spin-pairing model of the bonding of O_2 to Co(II), Cr(II), Mn(II) and Fe(II) complexes, with a ψ_1 -type molecular orbital to describe the spin-pairing. The y and ψ_{ab}^* are the metal d , and an antibonding $\pi_{\text{O}_2}^*$ orbital of ground-state O_2 .

We shall now relate this type of molecular orbital theory to the "increased-valence" theory of Section 14-1. A doubly-excited configuration $\Psi_2(\text{MO})$ of Eqn. (4) may also be constructed, in which ψ_2 instead of ψ_1 is doubly-occupied.

$$\Psi_2(\text{MO}) = (\psi_{ab})^2 (\psi_2)^2 \equiv |\psi_{ab}^\alpha \psi_{ab}^\beta \psi_2^\alpha \psi_2^\beta| \quad (4)$$

On substitution of the LCAO forms for ψ_1 and ψ_2 into Eqs. (3) and (4), we obtain

$$\psi_1(\text{MO}) = c_1^2 \psi(\ddot{\text{Y}} \text{ A} \text{---} \text{B}) + c_2^2 \psi(\text{Y} \ddot{\text{A}} \ddot{\text{B}}) + c_1 c_2 \{ \psi(\overset{\times}{\text{Y}} \overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}) + \psi(\overset{\circ}{\text{Y}} \overset{\times}{\text{A}} \overset{\times}{\text{B}}) \} \quad (5)$$

$$\psi_2(\text{MO}) = c_2^2 \psi(\ddot{\text{Y}} \text{ A} \text{---} \text{B}) + c_1^2 \psi(\text{Y} \ddot{\text{A}} \ddot{\text{B}}) - c_1 c_2 \{ \psi(\overset{\times}{\text{Y}} \overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}) + \psi(\overset{\circ}{\text{Y}} \overset{\times}{\text{A}} \overset{\times}{\text{B}}) \} \quad (6)$$

in which $\psi(\ddot{\text{Y}} \text{ A} \text{---} \text{B})$ is given by Eqn. (1),

$$\psi(\text{Y} \ddot{\text{A}} \ddot{\text{B}}) = (\psi_{ab})^2 (\psi_{ab}^*)^2 \equiv |\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{\alpha*} \psi_{ab}^{\beta*}| \quad (7)$$

and

$$\psi(\overset{\times}{\text{Y}} \overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}) + \psi(\overset{\circ}{\text{Y}} \overset{\times}{\text{A}} \overset{\times}{\text{B}}) = |\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{\alpha*} \psi_{ab}^{\beta*}| + |\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{\alpha*} \psi_{ab}^{\beta*}| \quad (8)$$

The lower-energy linear combination of $\psi_1(\text{MO})$ with $\psi_2(\text{MO})$ gives the C.I. (Section 3-3) wave-function of Eqn. (9) with $|c_1| > |c_2|$ and $c_1 > 0$ when $c_2 < 0$.

$$\psi(\text{CI}) = C_1 \psi_1(\text{MO}) + C_2 \psi_2(\text{MO}) \quad (9)$$

If c_1 and c_2 in the molecular orbitals of Eqn. (2) have similar magnitudes, i.e. if y and ψ_{ab}^* have similar energies, then the primary component of $\psi(\text{CI})$ will be given by Eqn. (8). Therefore, "increased-valence" structure (1) (which is equivalent to resonance between (2) and (3)) is the primary valence-bond structure for this approximate molecular orbital scheme when configuration interaction is invoked.

It should be noted that because ψ_{ab} as well as ψ_{ab}^* overlaps with y , the canonical 3-centre molecular orbitals¹¹ are given by Eqn. (10) rather than Eqn. (2).

$$\psi_i = c_{i1} y + c_{i2} \psi_{ab}^* + c_{i3} \psi_{ab} \quad (i = 1-3) \quad (10)$$

14-3 ATOMIC VALENCIES FOR "INCREASED-VALENCE" STRUCTURES¹²

The (co)valence of an atom in a molecule corresponds to the number of covalent bonds formed by the atom. Inspection of the standard Lewis structure (15) reveals that the valencies for the Y and A atoms are both unity. Each atom contributes one electron to form the Y-A covalent bond. For "increased-valence" structure (1), the A-atom is involved in both Y-A and A-B bonding. These two components of the A-atom valence will be designated as V_{ay} and V_{ab} , with $V_a = V_{ay} + V_{ab}$. We shall now show that V_a for "increased-valence" structure (1) can exceed unity when the molecular

orbitals of Eqn. (11) are used to construct the Pauling "3-electron bond" configuration $(\psi_{ab})^2(\psi_{ab}^*)^1$ for the A-B component of (1).

$$\psi_{ab} = (a + kb)/(1 + k^2)^{1/2}, \quad \psi_{ab}^* = (ka - b)/(1 + k^2)^{1/2} \quad (11)$$

To calculate V_{ay} , either of the following equivalent procedures may be used:

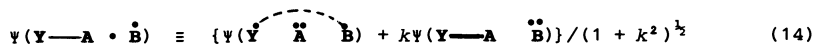
- (a) The antibonding ψ_{ab}^* electron of (1) is spin-paired with the y electron to generate fractional Y-A and Y-B bonding (Fig. 11-2). The valence V_{ay} must therefore correspond to the A-atom odd-electron charge, which is calculated from the square of the coefficient of the a orbital in ψ_{ab}^* . We thereby obtain

$$V_{ay} = k^2/(1 + k^2) \quad (12)$$

- (b) Because (1) is equivalent to resonance between (14) and (15), and (14) has no Y-A bond, V_{ay} must correspond to the weight for (15) in this resonance. In Section 3-11, we have deduced that

$$(\psi_{ab})^2(\psi_{ab}^*)^1 \equiv \{(a)^2(b)^1 + k(a)^1(b)^2\}/(1 + k^2)^{1/2} \quad (13)$$

from which it follows that



The weight for $\text{Y} \text{---} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$ is equal to the square of the coefficient of $\Psi(\text{Y} \text{---} \overset{\cdot\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}})$ in Eqn. (14). This gives the V_{ay} of Eqn. (12). It also corresponds to the bond-number of the fractional Y-A bond in (1).

For the one-electron $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ bond of (1), the valence V_{ab} must be such that for the Pauling "3-electron bond" configuration $(\psi_{ab})^2(\psi_{ab}^*)^1$, the following correlation must exist between the a-orbital charge (P_{aa}) and V_{ab} :

Structure	$\overset{\cdot\cdot}{\text{A}} \overset{\cdot}{\text{B}}$	$\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$	$\overset{\cdot}{\text{A}} \overset{\cdot\cdot}{\text{B}}$
k	0	1	∞
P_{aa}	2	1.5	1
V_{ab}	0	0.5	0

(For $k = 1$, the one-electron bond of $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ is homopolar, and therefore $V_{ab} = 0.5$). We thereby obtain Eqn. (15) ¹².

$$V_{ab} = -2(2 - P_{aa})(1 - P_{aa}) \quad (15)$$

For any value of k , the P_{aa} is given by $1 + 1/(1 + k^2)$ (Table 3-3) and therefore

$$V_{ab} = 2k^2/(1 + k^2)^2 \equiv 2P_{ab}^2 \quad (16)$$

in which P_{ab} is the bond-order for the $\dot{A} \cdot \dot{B}$ component (Table 3-3) of "increased-valence" structure (1).

By summing V_{ay} and V_{ab} of Eqs. (12) and (16) the total A-atom valence of Eqn. (17) is obtained. For $1 < k < \infty$, $V_a > 1$, i.e. the A-atom valence for "increased-valence" structure (1) exceeds the value of unity that occurs in the standard Lewis structure (15).

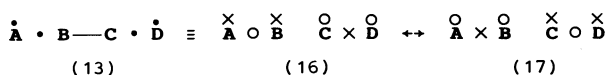
$$V_a = V_{ay} + V_{ab} = k^2/(1 + k^2) + 2k^2/(1 + k^2)^2 \quad (17)$$

Similar procedures may be used to deduce that the B-atom valence for (1) is given by Eqn. (18). Because the Y-atom valence for (1) (namely $V_Y \equiv V_{Ya} + V_{Yb}$) must always equal unity, the sum of the atomic valencies for (1) is given by Eqn. (19). It has a maximum value of 3 when $k = 1$, which is in accord with the earlier deduction (Section 11-1) that a maximum of three electrons may simultaneously participate in fractional Y-A, Y-B and A-B bonding.

$$V_b = V_{by} + V_{ba} = 1/(1 + k^2) + 2k^2/(1 + k^2)^2 \quad (18)$$

$$V_y + V_a + V_b = 2 + 4k^2/(1 + k^2)^2 \quad (19)$$

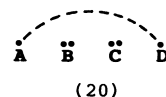
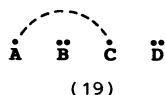
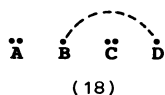
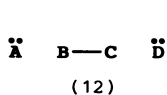
For "increased-valence" structure (13), the bonding and antibonding molecular orbitals for the Pauling "3-electron bond" components of (16) and (17) are given by Eqs. (11) and (20) when A and D, and B and C are pairs of equivalent atoms. We shall now use these orbitals to deduce that the B and C valencies of (13) can exceed unity in value.



$$\psi_{cd} = (d + kc)/(1 + k^2)^{\frac{1}{2}}, \quad \psi_{cd}^* = (kd - c)/(1 + k^2)^{\frac{1}{2}} \quad (20)$$

With $(\psi_{ab})^2(\psi_{ab}^*)^1 = (a)^2(b)^1 + k(a)^1(b)^2$ and $(\psi_{cd})^2(\psi_{cd}^*)^1 = (c)^1(d)^2 + k(c)^2(d)^1$, it is easy to deduce that the wave-function for "increased-valence" structure (13) is equivalent to that of Eqn. (21), in which Ψ_{12} , Ψ_{18} , Ψ_{19} and Ψ_{20} are the wave-functions for Lewis structures (12) and (18)-(20) (cf. Eqn. (10-15)).

$$\Psi_{13} = \{\Psi_{12} + k(\Psi_{18} + \Psi_{19}) + k^2\Psi_{20}\}/(1 + k^2) \quad (21)$$



By squaring the coefficient of Ψ_{12} in Eqn. (21), the weight (W_{12} of Eqn. (22)) for Lewis structure (12) is obtained, which corresponds to the bond-number (N_{bc}) for the B-C bond of (13), and hence to the valence V_{bc} in the latter structure. Similarly, the weights for structures (18)-(20) (Eqs. (23) and (24)) give the valencies V_{bd} , V_{ac} and V_{ad} for "increased-valence" structure (13). When V_{bc} and V_{bd} are added, the B-atom odd-electron charge (c_b^{*2} of Eqn. (25)) is obtained. The latter result shows how the fractional odd-electron charge of the B-atom is used for both B-C and B-D bonding; this has been noted previously in Section 7-1.

$$W_{12} = V_{bc} = 1/(1 + k^2)^2 \equiv N_{bc} \quad (22)$$

$$W_{18} = W_{19} = V_{bd} = V_{ac} = k^2/(1 + k^2)^2 \quad (23)$$

$$W_{20} = V_{ad} = k^4/(1 + k^2)^2 \quad (24)$$

$$V_{bc} + V_{bd} = 1/(1 + k^2) \equiv c_b^{*2} \quad (25)$$

Within the Pauling "3-electron bonds" $\overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ and $\overset{\cdot}{\text{C}} \cdot \overset{\cdot}{\text{D}}$ of (13), the B and C valencies are given by Eqn. (26) (c.f., (Eqn.(16))), in which P_{ab} and P_{cd} are the bond-orders for these bonds in (13). The total B-atom valence, namely $V_b = V_{bc} + V_{bd} + V_{ba}$, is then equal to the V_b of Eqn. (18) for "increased-valence" structure (1). Therefore, $V_b (\equiv V_c) > 1$ when $0 < k < 1$.

$$V_{ba} = V_{cd} = 2k^2/(1 + k^2)^2 \equiv 2P_{ab}^2 = 2P_{cd}^2 \quad (26)$$

In Section 13-3, the delocalized molecular orbitals are given for symmetrical 6-electron 4-centre bonding units. When these are normalized excluding atomic orbital overlap integrals, and the parameter μ is set equal k , the B-C bond-order P_{bc} for the molecular orbital configuration $\Psi_1(\text{MO}) = (\psi_1)^2(\psi_2)^2(\psi_3)^2$ is equivalent to the B-atom odd-electron charge of Eqn. (25) for "increased-valence" structure (13). The B-C bond-number for (13), namely the weight W_{12} of Eqn. (22), is equal to P_{bc}^2 for $\Psi_1(\text{MO})$ when $\mu = k$. For this value of μ , the A-B and C-D bond-orders for "increased-valence" structure (13) and $\Psi_1(\text{MO})$ are identical, with each having a value of $k/(1 + k^2)$.

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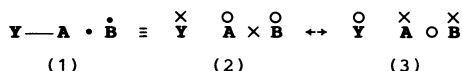
CHAPTER 15

SLATER DETERMINANTS AND WAVE-FUNCTIONS FOR "INCREASED-VALENCE" STRUCTURES

The Slater determinant theory of Section 3-7 will now be extended to construct wave-functions for "increased-valence" structures. Some of the theory for this Chapter will be used again in Chapters 20, 23 and 24.

15-1 "INCREASED-VALENCE" WAVE-FUNCTIONS FOR 4-ELECTRON 3-CENTRE AND 6-ELECTRON 4-CENTRE BONDING UNITS

In Chapters 11, 12 and 14, we have indicated that the "increased-valence" structure (1) involves the electron spin distributions of (2) and (3), in which the \times and \circ represent electrons with α and β spin wave-functions. Here, we shall construct Slater-determinantal wave-functions for (2) and (3), and hence for the "increased-valence" structure (1).



The wave-functions for the Pauling "3-electron bond" structures $\overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}$ and $\overset{\times}{\text{A}} \times \overset{\times}{\text{B}}$ of (2) and (3) are given by Eqs. (3-36) and (3-35). In (2) and (3), we have a fourth electron with spin wave-function α or β , which occupies the atomic orbital y centred on atom Y. Therefore, the wave-functions for (2) and (3) are given by the Slater determinants of Eqs. (1) and (2), for which the identities of Eqs. (3-36) and (3-35) have been used.

$$\psi(\overset{\times}{\text{Y}} \quad \overset{\circ}{\text{A}} \times \overset{\circ}{\text{B}}) = |y^\alpha \psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{*\beta}| = (1 + kk^*) |y^\alpha a^\beta \psi_{ab}^\alpha b^\beta| \quad (1)$$

$$\psi(\overset{\circ}{\text{Y}} \quad \overset{\times}{\text{A}} \times \overset{\times}{\text{B}}) = |y^\beta \psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{*\alpha}| = -(1 + kk^*) |y^\beta a^\alpha \psi_{ab}^\beta b^\alpha| \quad (2)$$

Examination of Eqs. (1) and (2) shows that each of (2) and (3) involves two singly-occupied orbitals, namely y and $\psi_{ab}^* = k^* a - b$. In order for bonding to occur between Y and AB due to overlap between y and ψ_{ab}^* , as it does in the "increased-valence" structure (1), it is necessary to spin-pair the two electrons that occupy these orbitals, thereby generating an $S = 0$ spin-state. By examination of the Heitler-London $S = 0$ wave-function of Eqn. (3-25), which also has two singly-occupied orbitals, it is seen that the appropriate wave-function for the

spin-pairing of (1) must involve the wave-function $|\dots y^\alpha \psi_{ab}^{*\beta}| + |\dots \psi_{ab}^{*\alpha} y^\beta|$ for the two singly occupied-orbitals of (1). By interchanging rows or columns of the Slater determinants of Eqs. (1) and (2), we may write

$$\Psi(\overset{\times}{\mathbf{Y}} \overset{\circ}{\mathbf{A}} \times \overset{\circ}{\mathbf{B}}) = |\psi_{ab}^\alpha \psi_{ab}^\beta y^\alpha \psi_{ab}^{*\beta}| \quad (3)$$

$$\Psi(\overset{\circ}{\mathbf{Y}} \overset{\times}{\mathbf{A}} \times \overset{\times}{\mathbf{B}}) = -|\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{*\alpha} y^\beta| \quad (4)$$

in which we have grouped together the singly-occupied orbitals. The appropriate $S = 0$ wave-function for "increased-valence" structure (1) is therefore given by Eqs. (5) and (6).

$$\begin{aligned} \Psi(\mathbf{Y} \text{---} \mathbf{A} \cdot \overset{\circ}{\mathbf{B}}) &= \Psi(\overset{\times}{\mathbf{Y}} \overset{\circ}{\mathbf{A}} \times \overset{\circ}{\mathbf{B}}) - \Psi(\overset{\circ}{\mathbf{Y}} \overset{\times}{\mathbf{A}} \times \overset{\times}{\mathbf{B}}) \\ &= |\psi_{ab}^\alpha \psi_{ab}^\beta y^\alpha \psi_{ab}^{*\beta}| + |\psi_{ab}^\alpha \psi_{ab}^\beta \psi_{ab}^{*\alpha} y^\beta| \end{aligned} \quad (5)$$

$$= (1 + kk^*)(|y^\alpha a^\beta \psi_{ab}^\alpha b^\beta| + |y^\beta a^\alpha \psi_{ab}^\beta b^\alpha|) \quad (6)$$

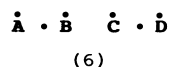
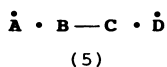
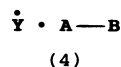
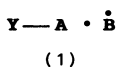
It is important to realize that $\Psi(\mathbf{Y} \text{---} \mathbf{A} \cdot \overset{\circ}{\mathbf{B}})$ may be expressed either as Eqn. (5) or as Eqn. (6). For the purpose of relating directly to the valence-bond structure (1), Eqn. (6) is appropriate, but Eqn. (5) shows clearly that the "increased-valence" structure (1) involves the spin-pairing of two electrons, one of which occupies an atomic orbital on Y, and the other occupies the antibonding A-B orbital.

Inspection of Eqn. (6) shows that a Heitler-London type wave-function has been used to construct the wave-function for the fractional Y-A bond of (1). If it is preferred to use bonding molecular orbitals to describe the wave-functions for all bonds, then we may construct the $S = 0$ wave-function of Eqn. (7) for the four electrons of (1), in which $\psi_{ya} = y + \ell a$ and $\ell > 0$. The properties of Eqs. (6) and (7) are different, and on most occasions, we shall be implying the usage of Eqn. (6). Some further considerations of Eqn. (7) will be provided in Chapters 20 and 23.

$$\Psi(\mathbf{Y} \text{---} \mathbf{A} \cdot \overset{\circ}{\mathbf{B}}) = |\psi_{ya}^\alpha \psi_{ya}^\beta \psi_{ab}^\alpha b^\beta| + |\psi_{ya}^\alpha \psi_{ya}^\beta b^\alpha \psi_{ab}^\beta| \quad (7)$$

"Increased-valence" structure (1) is the fundamental "increased-valence" structure. Together with (4), it is appropriate whenever four electrons can participate in 3-centre bonding. But, as we have discussed in Chapter 13, it is possible to construct longer "increased-valence" structures that are appropriate for different types of N -centre bonding units, with $N > 4$. Here, we shall construct a wave-function for the 6-electron 4-centre "increased-valence" structure (5) (Section 12-3), which is obtained by spin-pairing the odd-electrons of the Pauling

"3-electron bond" structures of (6). For the Pauling "3-electron bond" structures, the odd electrons occupy the antibonding ψ_{ab}^* and ψ_{cd}^* molecular orbitals, and the bonding molecular orbitals ψ_{ab} and ψ_{cd} are doubly occupied. When spin-pairing of the odd-electrons of (6) occurs, the two singly-occupied antibonding orbitals will also pertain for the wave-function for (5). Consequently, the $S = 0$ wave-function for (5) is given by Eqn. (8).

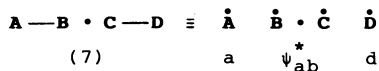


$$\psi(\dot{A} \cdot B - C \cdot \dot{D}) = |\psi_{ab}^{\alpha} \psi_{ab}^{\beta} \psi_{ab}^{*\alpha} \psi_{cd}^{*\beta} \psi_{cd}^{\alpha} \psi_{cd}^{\beta}| + |\psi_{ab}^{\alpha} \psi_{ab}^{\beta} \psi_{cd}^{*\alpha} \psi_{ab}^{*\beta} \psi_{cd}^{\alpha} \psi_{cd}^{\beta}| \quad (8)$$

Orbital-occupancy diagrams that correspond to the Slater determinants of Eqs. (5) and (8) are displayed in Figs. 11-2 and 11-3.

15-2 SPIN DEGENERACY AND WAVE-FUNCTIONS FOR "INCREASED-VALENCE" STRUCTURES

Except for 4-electron 3-centre and 6-electron 4-centre "increased-valence" structures, all other "increased-valence" structures involve the spin-pairing of three or more odd electrons, i.e. in the "increased-valence" wave-function, three or more orbitals must be singly-occupied. This may be seen by examination of the "increased-valence" structures (7) and (8) for 5-electron 4-centre and 8-electron 6-centre bonding. These structures have been expressed in terms of their atomic and Pauling "3-electron bond" components, below which we have written the singly-occupied orbitals. When three or more orbitals of an atom or molecule are singly-occupied, the phenomenon of *spin degeneracy* arises, i.e. there exist two or more wave-functions with the same set of S and S_z spin quantum numbers. For each of the "increased-valence" structures (7) and (8), the spin degeneracy is two; there are two wave-functions with $S = S_z = \frac{1}{2}$ for (7), and two wave-functions with $S = S_z = 0$ for (8). These wave-functions are given[†] by Eqs. (9)-(12), in which we have omitted all doubly-occupied orbitals from the Slater determinants.



[†] The Ψ_1 and Ψ_2 of Eqs. (9) and (10) are orthogonal, whereas the Ψ_1 and Ψ_2 of Eqs. (11) and (12) are not orthogonal. An orthogonal set may of course be constructed from the latter pair of functions, but for our present purposes, it is more useful to use Eqs. (11) and (12).

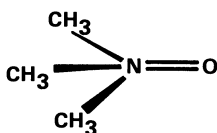
CHAPTER 16

CLASSICAL VALENCE STRUCTURES AND QUINQUEVALENT NITROGEN ATOMS

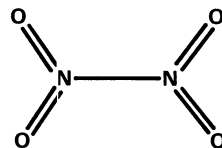
For a number of electron-excess molecules that involve atoms of first-row elements (in particular, nitrogen atoms), an older type of "increased-valence" structure is sometimes used to represent their electronic structures. Since the 1860's and up until the introduction of the Lewis-Langmuir octet theory, nitrogen atoms were very often represented with valencies of 3 or 5 in valence-bond structures. For example, valence-bond structures for N_2O , Me_3NO , and N_2O_4 were written as (1)-(3).



(1)

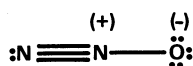


(2)

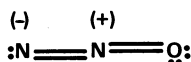


(3)

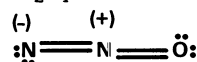
Using (1) for N_2O , with an N-N triple bond and an N-O double bond, we would be let to predict that the bond-lengths are similar to the 1.10 Å and 1.21 Å for N_2 and $CH_3N=O$. The experimental lengths of 1.13 Å and 1.19 Å confirm this expectation (Section 2-3(b)), and on this basis (1) is a suitable valence-bond structure for N_2O . But the Lewis theory, with electron-pair bonds, does not permit a valence of five for first-row atoms, provided that only the 2s and three 2p orbitals of these atoms are used for bonding. Therefore, in the Lewis theory, the quinquevalent structures are replaced³ by octet structures such as (4)-(6) for N_2O , and (7) and (8) (together with equivalent resonance forms) for Me_3NO and N_2O_4 .



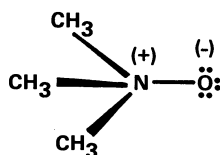
(4)



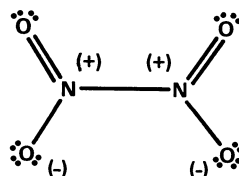
(5)



(6)



(7)



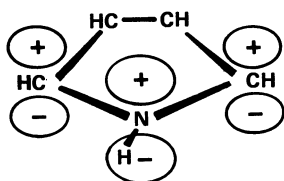
(8)

In these latter structures, the valencies of N^- , N , and N^+ are 2, 3 and 4 respectively. We may note that each of (1), (2) and (3) seems to have one more bond than have the corresponding Lewis structures, and therefore we might also call (1), (2) and (3) "increased-valence" structures. Alternatively, we may say that the quinquevalent nitrogen atom has increased its valence relative to the maximum of four which is allowed in the Lewis theory. Sometimes, the valence-bond structures such as (1), (2) and (3) are designated as "classical valence structures", and we shall refer to them as such here.

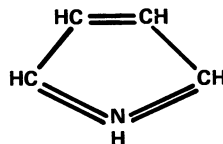
Although the use of octet structures such as (5)-(8) is extremely widespread, it is by no means universal^{4,5}. Sometimes, the classical valence structures are used to account for certain empirical information, and the quantum mechanical basis for them is not discussed, i.e. it is not suggested how the nitrogen atom forms five covalent bonds. However, there have been three major attempts to explain how a nitrogen atom (or other first-row atoms - in particular, a carbon atom) may acquire an apparent valence of five, and we shall describe them briefly here.

(a) The nitrogen ground-state configuration $2s^2 2p_x^1 2p_y^1 2p_z^1$ is promoted to either the $2s^1 2p_x^1 2p_y^1 2p_z^1 3s^1$ or the $2s^1 2p_x^1 2p_y^1 2p_z^1 3d^1$ configuration⁶⁻⁸, both of which have five unpaired electrons. This theory is usually considered to be unsatisfactory, since the $2s + 3s$ and the $2s + 3d$ promotion energies are very large.

(b) By overlapping three of its four valence orbitals with three atomic orbitals on one or more adjacent atoms, the nitrogen atom can form three normal electron-pair bonds. The fourth nitrogen valence orbital then overlaps simultaneously with two atomic orbitals on adjacent atoms and thereby forms two non-orthogonal bond orbitals. In (9) we show the latter type of overlap for the nitrogen atom of pyrrole; the classical valence structure for this molecule is (10).



(9)



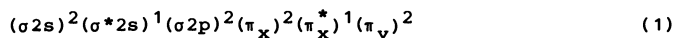
(10)

If in (9), y and b are the carbon $2p_z$ atomic orbitals, and a is the nitrogen $2p_z$ atomic orbital, then from them we may construct the two-centre bond-orbitals $\phi_L = y + ka$ and $\phi_R = b + ka$ with $k > 0$. We may put the four π -electrons of (10) into these two orbitals, to afford the bond-orbital configuration $(y + ka)^2(b + ka)^2$. It is quite satisfactory to do this, provided that it is kept in mind that the two bond-orbitals are not orthogonal, and therefore, when they are both doubly occupied,

they cannot represent two separate, independent C-N π -bonds. Therefore for this theory, the nitrogen atom does not have a true valence of five - it is only apparently quinquivalent. Bent⁹ has used this type of "increased-valence" theory to describe the bonding for numerous molecules. It may be noted also that (except for a multiplicative constant) the configuration $(y + ka)^2(b + ka)^2$ is equivalent⁹⁻¹² to the delocalized molecular orbital configuration $(y + 2ka + b)^2(y - b)^2$ for which the delocalized molecular orbitals correspond to the bonding and non-bonding molecular orbitals of Section 2-3(a). (The proof of this result is obtained by using the identity of Eqn. (3-17), namely if two electrons occupy orbitals ψ_1 and ψ_2 with the same spins, then $(\psi_1)^1(\psi_2)^1 \equiv -2(\psi_1 + \psi_2)^1(\psi_1 - \psi_2)^1$). With this equivalence, the a-orbital valence is^{13,14} $V_a = P_{ay}^2 + P_{ab}^2 = 8k^2 / (2k^2 + 1)^2$, which has a maximum value of unity when $k = 2^{-1/2}$. Consequently, the nitrogen atom of (10) remains quadrivalent¹⁴, as it is in the Lewis octet structure.

This use of two non-orthogonal π -orbitals forms the basis of Paoloni's theory⁴ of the quinquivalent nitrogen atom. Paoloni was not concerned with the construction of a wave-function for the quinquivalent nitrogen atom in a molecule, but only with indicating by means of the valence-bond structure that the two π -electrons of the pyrrolic nitrogen (tr, tr, tr, π^2) configuration (tr = sp^2) are involved in bonding to the adjacent carbon atoms.

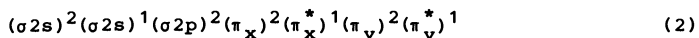
(c) The third theory of nitrogen quinquivalence has an interesting history¹⁵. By using the molecular orbital configuration



for an excited state of N_2 , Samuel¹⁶ in 1944 derived the valence-bond structure $:\text{N} \equiv \dot{\text{N}}\cdot$, which has two unpaired electrons. Samuel then paired these electrons with two unpaired electrons of an oxygen atom to form two N-O covalent bonds, i.e. he wrote



In 1945, Wheland¹⁷ defended the Lewis structures (i.e (4)-(6)), and suggested that N_2O could be formed by combination of the excited NO configuration



with a nitrogen atom. From this NO configuration, Wheland obtained the valence-bond structure $\cdot\dot{\text{N}}-\ddot{\text{O}}:$, which enabled him to retain the nitrogen quadrivalence in the Lewis structure (4). In another paper, Samuel implied that the excited NO configuration corresponded to the valence-bond structure $\cdot\dot{\text{N}}=\ddot{\text{O}}:$, which generates nitrogen quinquivalence in the reaction

$$\cdot\dot{\text{N}} + \cdot\dot{\text{N}}=\ddot{\text{O}}: \longrightarrow :\text{N} \equiv \text{N} = \ddot{\text{O}}:$$

On replying to Wheland's paper, Samuel gave some additional justification for using this NO valence-bond structure¹⁸.

It seems now that both Samuel and Wheland held the very widespread opinion that valence-bond structures for diamagnetic molecules must have only electron-pair bonds. Samuel and Wheland had attempted to transform the molecular orbital configurations for N₂ and NO so that they would obtain electron-pair bonds for N₂O. But neither worker used the correct procedure to obtain valence-bond structures from diatomic molecular orbital configurations with one or more singly-occupied antibonding molecular orbitals. The technique that should be used was developed by Linnett in 1956¹⁹, and then by Green and Linnett in 1960²⁰, and we have described it on numerous occasions in this book. When this theory is applied to the excited N₂ and NO configurations of Eqs. (1) and (2), we obtain the valence-bond structures $\ddot{\text{N}}::\ddot{\text{N}}$ and $\cdot\ddot{\text{N}}::\ddot{\text{O}}\cdot$, with two and three Pauling "3-electron bonds". When these structures are bonded to oxygen or nitrogen atoms, we obtain valence-bond structures (11) and (12) for N₂O.

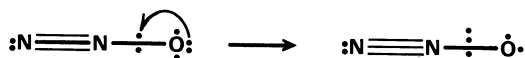


(11)



(12)

The valence-bond structure (12) is similar to the "increased-valence" structure (13) (c.f. Figures 2-10 and 13-1), and it is possible to derive (12) from (13) by delocalizing an oxygen lone-pair electron into a bonding N-O orbital. To show this we write



(13)

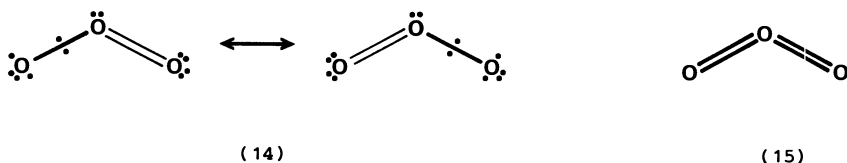
(12)

(We note that the oxygen lone-pair electron of (13) that is delocalized occupies an atomic orbital which should be predominantly 2s in character. Therefore, this electron must be quite firmly bound to the oxygen atom, and very little delocalization of it is expected to occur. Any delocalization of nitrogen or oxygen 2s lone-pair electrons has always been ignored throughout this book.)

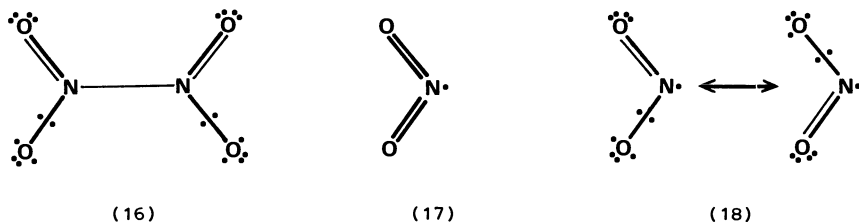
If we use valence-bond structures such as (13), which have both one-electron bonds and fractional electron-pair bonds, then we may give the following interpretation of the apparent nitrogen quinquivalence in (1). Let us assume that (1) and (13) are equivalent structures. Then it follows that one of the two N-O bond-lines of (1) represents two N-O bonding electrons occupying two different spatial orbitals, i.e. this N-O bond-line in (1) is equivalent to two one-electron bonds in (13).

Because "increased-valence" structures such as (13) make clearer the nature of the spatial distributions of the electrons than do the classical valence structures such as (1), it would seem to be preferable to use the former types of valence-bond

structures. They also have the advantage that they do not conceal the (spin-paired) diradical character, which is sometimes important for discussions of chemical reactivity. For example, O_3 reacts with univalent radicals such as hydrogen and chlorine atoms, and NO , to form $O_2 + HO$, ClO or NO_2 . In Chapter 22, we shall find that the electronic reorganization that may occur as the reactions proceed is easily followed through by using "increased-valence" structure (14) rather than the classical valence structure (15). In (14), there is (fractional) odd-electron charge occupying an atomic orbital on a terminal oxygen atom, and this may be used to form a partial bond with the univalent radical.



In Section 13-2, we have generated "increased-valence" structure (16) from the standard Lewis structure (8) for N_2O_4 . Both (3) and (16) have an *apparent* valence of 5 for each nitrogen atom^{*}, but (16) relates better to the experimental electronic structure than does (3). Thus, by inspection of (3), it is not possible to deduce that the N-N bond should be long and weak. Also, when the N-N bonds of (3) and (16) are broken, the NO_2 monomers of (17) and (18) are obtained, with their odd-electron located in a nitrogen atomic orbital of (17), but delocalized over the molecule in (18). Only the latter description is in accord with the results of e.s.r. measurements²¹.



For each of the "increased-valence" structures that we have described in this chapter, there is an apparent violation of the Lewis-Langmuir octet rule for some of the first-row atoms. However, because only the 2s and 2p orbitals are required for a minimal basis set description of the bonding, no real octet violation occurs in the molecular wave-function. Further, these structures summarize resonance between standard and "long-bond" Lewis structures, each of which obeys the octet rule. This

[†] Using the procedures described in Section 14-3, it may be deduced that the maximum nitrogen valence for (16) is 4.25, and that a total of 18 electrons participate in bonding between all pairs of atoms.

latter result has been demonstrated in Section 11-9 for "increased-valence" structure (16), whose component octet structures are displayed in Fig. 11-5. Further comments on "apparent octet violation" for atoms of first-row elements are provided in Refs. 14, 15, 22, 23.

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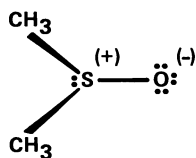
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CHAPTER 17

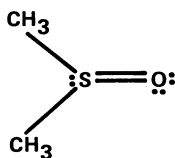
SOME TETRAHEDRAL MOLECULES AND $d_{\pi} - p_{\pi}$ BONDING FOR SOME SULPHUR COMPOUNDS

17-1 d -ORBITALS AS POLARIZATION AND HYBRIDIZATION FUNCTIONS

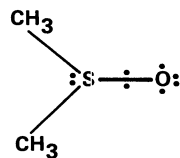
In Chapters 11 and 13, we have described some valence-bond structures for a number of molecules that involve sulphur atoms. There, we have assumed that only the valence-shell 3s and 3p orbitals need participate in bonding. Of course, atoms of the second-row of the periodic table may also utilize one or more 3d-orbitals for bonding, i.e. such atoms may expand their valence shells. Lewis-type valence-bond structures may then be written down with more electron-pair bonds than are present in the octet structures. For example, (1) and (2) are examples of Lewis octet and expanded valence-shell structures for $(\text{CH}_3)_2\text{SO}$. An "increased-valence" structure such as (3) does not necessarily involve the participation of sulphur 3d-orbitals in bonding. Structures (2) and (3) are obtained respectively by delocalizing oxygen π or $\bar{\pi}$ electrons of (1) into either a vacant sulphur 3d-orbital or into bonding S-O orbitals; the relevant (overlapping) atomic orbitals for the latter are a sulphur hybrid orbital of an adjacent S-C σ -bond and an oxygen π - or $\bar{\pi}$ -orbital. In (3), 1-electron bonds replace the additional $d_{\pi} - p_{\pi}$ bond that is formed when the sulphur atom expands its valence shell in (2). Similar types of structures for SO_4^{2-} are (4)-(6), with the sulphur atom for (5) utilizing two 3d-orbitals in the two S-O bonds.



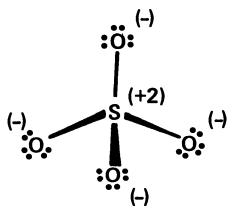
(1)



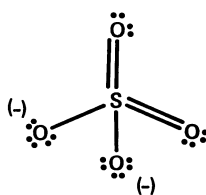
(2)



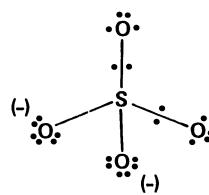
(3)



(4)



(5)



(6)

It is important to distinguish between the role of d-orbitals as hybridization functions and their role as polarization functions. For the former case, the d-orbital serves to "increase the number of distinct orbitals utilized in the wave-function"¹. Thus, the octet and expanded valence-shell structures (1) and (2) have $C_1s^2p^3, V_3 + C_2sp^4, V_3$ and $C_1s^2p^3d, V_4 + C_2sp^4d, V_4$ valence-state configurations for the trivalent and quadrivalent sulphur atoms. For structures (4) and (5) the sulphur valence-state configurations are sp^3, V_4 and sp^3d^2, V_6 . When a 3d-orbital participates as a polarization function, it "merely moderates the shape of pre-existing orthogonal hybrid atomic orbitals"¹. For example, the three sulphur orbitals that form σ -bonds in the octet structure (1) may involve some 3d as well as 3s and 3p character; i.e. each orbital may be expressed as $c_1s + c_2p + c_3d$. The resulting valence-state configuration is then $C_1s^2p^3, V_3 + C_2sp^4, V_3 + C_3s^2p^2d, V_3 + C_4sp^3d, V_3$. Therefore, the utilization of 3d orbitals as polarization functions is not precluded for either the octet structures or "increased-valence" structures such as (3) and (6). Our concern here is to distinguish between this type of "increased-valence" structure, and those that utilize 3d orbitals as hybridization functions for $d_\pi - p_\pi$ bonding. We shall restrict our attention primarily to a consideration of the bonding for some sulphur compounds.

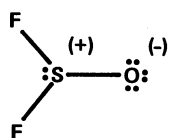
On the basis of some bond-length data, we shall suggest that expansion of the sulphur valence-shell to generate $d_\pi - p_\pi$ bonding is more likely to occur in either of the following situations:

- (a) The R substituents of R_2SO are alkyl radicals. In Sections 11-3 and 11-4 we have concluded that H and alkyl substituents seem unable to stabilize appreciable development of Pauling "3-electron bonds" in 4-electron 3-centre bonding units of neutral molecules. The delocalization of oxygen π or $\bar{\pi}$ electrons of (1) into the sulphur 3d-orbital to form (2) then helps reduce the magnitudes of the atomic formal charges.
- (b) The sulphur (or other second-row) atom is involved in the formation of four electron pair σ -bonds in a standard octet structure - for example (4) for SO_4^{2-} . This is equivalent to saying that either the oxidation state for sulphur is +6 or that the sulphur formal charge is +2 in the octet structure.

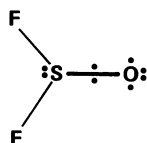
Admittedly these hypotheses are somewhat speculative, and some exceptions to them most probably exist. Therefore, the discussion for some of this chapter should be viewed more as involving orientation, rather than as definitive accounts of the bonding. The role of 3d-orbitals in bonding for second-row atoms has been discussed by numerous workers - see for example Refs. 1-6 - and the reader is referred to them for further details.

17-2 F_2SO , F_2SS AND $(CH_3)_2SO$

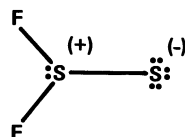
In Section 11-4, we have described the electronic structures for F_2SO and F_2SS . These molecules are isoelectronic with SO_3^{2-} . Without the participation in bonding of the sulphur 3d orbitals, we were able to account for either the shortening or the similarity of the S-O and S-S bond-lengths (1.41 Å and 1.86 Å) to those of double bonds (1.49 Å and 1.89 Å), and also for the lengthening of their S-F bonds (1.59 Å and 1.60 Å) relative to the estimate of 1.54 Å for the length of an S-F single-bond. To do this, we used primarily the "increased-valence" structures (8) and (10), which may be generated from the standard Lewis structures (7) and (9) by delocalizing oxygen π - and $\bar{\pi}$ -electrons into bonding S-O orbitals. If it is assumed that oxygen lone-pair electrons delocalize into a sulphur 3d orbital for either molecule, Lewis structures (11) and (12) are obtained. The latter structures have S-O double-bonds, but because they retain S-F single-bonds, they cannot account for the observed lengthening of the S-F bonds relative to those of single bonds.



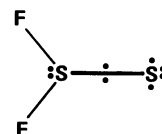
(7)



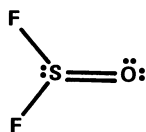
(8)



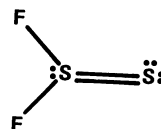
(9)



(10)



(11)



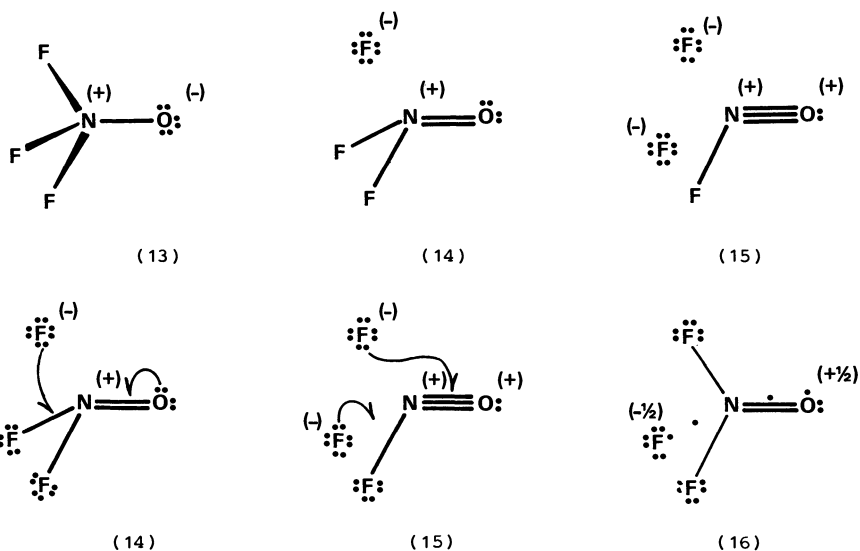
(12)

In contrast to what is the case for F_2SO , the bond-lengths for isoelectronic $(CH_3)_2SO$ (C-S = 1.80 Å, S-O = 1.48 Å)⁷ suggest that sulphur 3d orbitals do participate appreciably in S-O bonding. The S-O bond-length is shorter than a single-bond (1.70 Å), but the C-S bond-lengths are essentially those of C-S single-bonds (c.f. 1.82 Å for CH_3SH)⁸. Resonance between valence-bond structures (1) and (2), each of which has two C-S single-bonds, accounts for the observed bond-lengths. We have concluded in Section 11-3 that CH_3 groups cannot stabilize Pauling "3-electron bonds" of 4-electron 3-centre bonding units in neutral molecules, and therefore the delocalization of oxygen π and $\bar{\pi}$ electrons of (1) to generate "increased-valence" structure (3) must occur only to a small extent; otherwise the C-S bonds of $(CH_3)_2SO$ would be rather longer than single bonds.

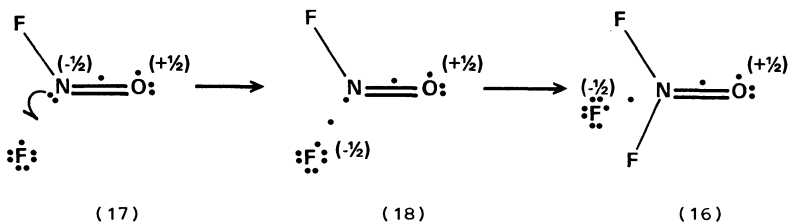
17-3 F_3NO , $(CH_3)_3NO$, F_3SN AND FSN

Each of the tetrahedral AX_3Y molecules of this Section has 32 valence-shell electrons, as have the sulphones and AO_4 anions of Sections 17-4 and 17-5. Consideration of the bonding for these AX_3Y molecules provides some support for the hypothesis that fluorine atoms can stabilize Pauling "3-electron-bonds" in 4-electron 3-centre bonding units for neutral molecules, and that Lewis structures with expanded valence-shells for sulphur atoms may be appropriate if the sulphur atoms acquire +2 formal charges in the Lewis octet structures.

For F_3NO , the standard Lewis structures are of types (13)-(15). The N-F and N-O bond-lengths⁹ of 1.432 Å and 1.159 Å for this molecule are respectively longer than the N-F bonds of NF_3 (1.37 Å) and similar to the bond-length (1.15 Å) for free NO with valence-bond structure $\overset{-\frac{1}{2}}{\text{N}} \equiv \overset{+\frac{1}{2}}{\text{O}}$ (Section 4-5). Resonance between (14) and (15) can account qualitatively for these bond properties, but the formal charges of (15) suggest that its weight should be rather less than that of (14). Alternatively, we may construct "increased-valence" structures of type (16) either from (14) or (15) by means of the delocalizations indicated below,

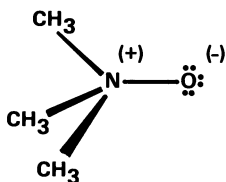


or from $3F + NO$ via FNO and F_2NO according to (17) \rightarrow (18) \rightarrow (16).

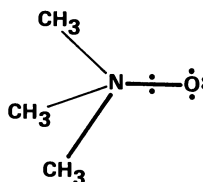


Valence-bond structures of type (16) have satisfactory arrangements of formal charges. The electronic structure of the N-O component is similar to that of free NO, and each N-F bond has a bond-number or bond-order which is less than unity. Therefore, resonance between the three equivalent structures of type (16) accounts for the nature of the observed bond-lengths.

We may contrast the bonding for F_3NO with that of $(CH_3)_3NO$. The C-N and N-O lengths¹⁰ of $(CH_3)_3NO$ are 1.495 Å and 1.404 Å, which are respectively only slightly longer and shorter than estimates of 1.47 Å and 1.44 Å for C-N and N-O single bonds. Therefore, with respect to these bond-lengths, the Lewis structure (19) gives a fairly satisfactory representation of the electronic structure of $(CH_3)_3NO$. A small amount of oxygen π and $\bar{\pi}$ electron delocalization, as is shown in (20), could be responsible for the small C-N lengthenings and N-O shortening.

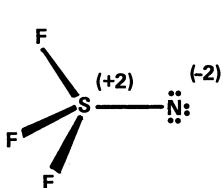


(19)

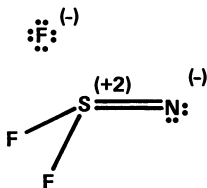


(20)

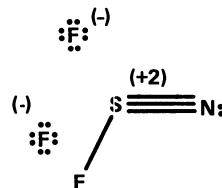
For F_3SN , we may write down the standard Lewis structures of types (21) - (23). These structures satisfy the Lewis-Langmuir octet rule, but they each carry a formal charge of +2 on the sulphur atom.



(21)



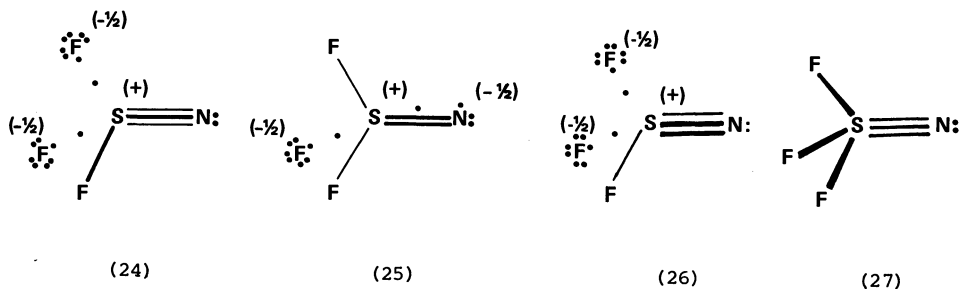
(22)



(23)

We may reduce the magnitudes of the formal charges either by

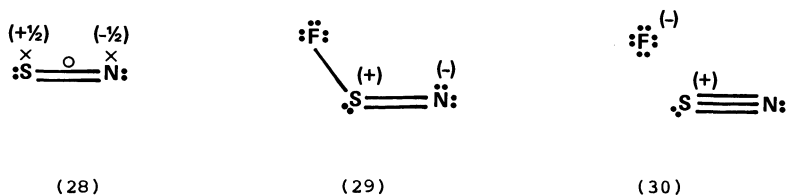
- (a) delocalizing N^{2-} or F^- electrons into bonding or anti-bonding orbitals, to obtain "increased-valence" structures such as (24)-(26)

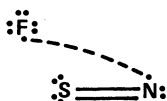


or by

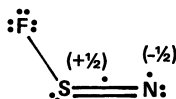
- (b) delocalizing N^{2-} , N^- or F^- electrons into vacant d-orbitals on the sulphur atom, to afford the Lewis structure (27) with an expanded valence-shell for the sulphur atom.

To help decide which set of delocalizations predominates, we shall also give consideration to the bonding for FSN. For the latter molecule, the S-N and S-F bond-lengths¹¹ of 1.45 Å and 1.65 Å are respectively shorter than 1.50 Å for free SN (with valence-bond structure (28)), and longer than the S-F single-bond length of 1.54 Å. Resonance between the standard Lewis structures (29) and (30) can account for these observations if it is assumed that the weight for (30) is larger than the weight for (29). However, the "long-bond" structure (31), with zero formal charges on all atoms should also make an important contribution to the ground-state resonance. "Increased-valence" structure (32), which may be obtained either by spin-pairing the odd-electron of SN with that of a fluorine atom, or by delocalizing a nitrogen $\bar{\pi}$ -electron of (29) into a bonding S-N orbital, is equivalent to resonance between (29) and (31). Resonance between (30) and (32), with (32) predominating, can also account for the observed bond-lengths for FSN; it also must represent a rather lower energy arrangement for the electrons than does resonance between (29) and (30).

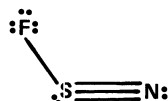




(31)



(32)

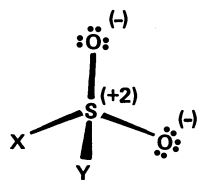


(33)

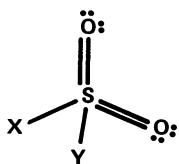
If we use the Lewis-structure (33), with an expanded valence-shell for the sulphur atom, to represent the electronic structure of FSN, we cannot account for the observed lengthening of the S-F bond relative to that of a single bond. By contrast, the S-F bond-length¹² of 1.55 Å for F₃SN is essentially that of a single bond, and the expanded valence-shell structure (27) is in accord with this observation. If we use (27) to represent the electronic structure of F₃SN, we are also able to account for the observed shortening of the S-N bond (1.42 Å)¹² relative to those of free SN (1.50 Å) and FSN (1.45 Å), whose electronic structures are to be described by (28) and resonance between (30) and (32) respectively.

17-4 SULPHONES XYSO₂

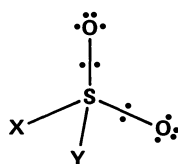
For SO₄²⁻, which is isoelectronic with F₃SN, the Lewis octet, expanded valence-shell and "increased-valence" (with no valence-shell expansion) structures are of types (4)-(6). Similar valence-bond structures for the XYSO₂ type sulphones of Table 17-1, which also have 32 valence-shell electrons, are (34)-(36). For these latter molecules, the S-X and S-Y bond-lengths are not longer than the estimates of 1.54, 2.01 and 1.82 Å (Sections 11-3, and 17-2) for standard S-F, S-Cl and S-C single bonds, and the S-O bond-lengths are shorter than the 1.48 Å for the double bond of free SO. With respect to the S-O bond-lengths, each of (35) and (36) alone predicts double-bond character. However, the bond-lengths reported in Table 17-1 suggest that the expanded valence-shell structures account better for the S-X and S-Y bond-lengths than do the "increased-valence" structures. As is the case for F₃SN, the sulphur atom carries a formal charge of +2 in the Lewis octet structure (34). Presumably, expanded valence-shell structures of type (5) should be similarly preferred to (6) for SO₄²⁻, whose S-O bond lengths of 1.48 Å¹³ are appreciably shorter than the single-bond length of 1.70 Å. It should be noted however, that for structure (5), some further "increased-valence" may be developed by delocalizing non-bonding π- or π̄-electrons from the O⁻ into bonding S-O orbitals to afford the more-stable valence-bond structures of type (37). Because the sulphur atom of (5) is already neutral, these delocalizations are not expected to be appreciable but must occur to some extent (c.f. C₂O₄²⁻ and CO₃²⁻ of Sections 13-2 and 13-5).



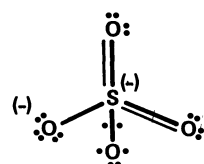
(34)










(35)



(36)



(37)

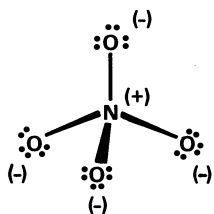
		$r(SX)$	$r(SY)$	$r(SO)$
	(a)	1.530	1.530	1.397
	(b)	1.530	1.530	1.405
	(c)	1.55	1.985	1.408 (ass.)
	(d)	2.011	2.011	1.404
	(e)	1.763	2.046	1.424
	(f)	1.759	1.561	1.410
	(g)	1.777	1.777	1.431

REFERENCES: (a) Hagen, K., Cross, V.R. and Hedberg, K., *J. Mol. Struct.*, **44**, 187 (1978). (b) Lide, D.R., Mann, D.E. and Fristrom, R.M., *J. Chem. Phys.*, **26**, 784 (1957). (c) Hargittae, I., *Lecture Notes in Chemistry 6, Sulphone Molecular Structures*, Springer Verlag, Berlin, 1978; C.W. Holt and M.C.L. Gerry, *Chem. Phys. Letts.*, **9**, 621 (1971). (d) Hargittae, I., *Acta Chim., Acad. Sci. Hung.*, **60**, 231 (1969). (e) Hargittae, M., and Hargittae, I., *J. Chem. Phys.*, **59**, 2513 (1973). (f) Hargittae, I., and Hargittae, *J. Mol. Struct.*, **15**, 399 (1973). (g) S. Saito and F. Makino, *Bull. Chem. Soc. Jap.*, **45**, 92 (1972).

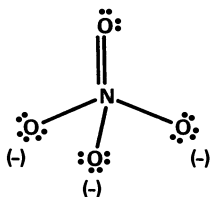
Table 17-1 Bond-lengths for some sulphones.

17-5 NO_4^{3-} , PO_4^{3-} AND F_3PO

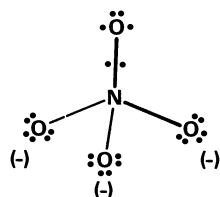
Because nitrogen 3d-orbitals do not participate in bonding as hybridization functions, "increased-valence" structure (40), rather than the expanded valence-shell structure (39) is an appropriate type of valence-bond structure for the ground-state of NO_4^{3-} . The "increased-valence" structure may be constructed either by delocalizing oxygen π - or $\bar{\pi}$ -electrons of (38) into bonding N-O orbitals, or by means of the reaction $\text{NO}^* + 3\text{O}^-$ with valence-bond structure 11-63 for NO^* . Resonance between "increased-valence" structures of type (39) accounts for the observation that the N-O bond-lengths¹⁴ of 1.39 Å for NO_4^{3-} are shorter than the estimate of 1.44 Å for an N-O single bond (cf. (20) for $(\text{CH}_3)_3\text{NO}$).



(38)

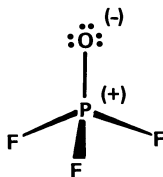


(39)

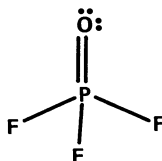


(40)

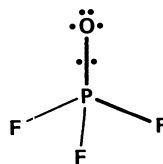
In the Lewis octet structures for PO_4^{3-} ((38) with P^+ replacing N^+), the phosphorus atom carries a formal charge of +1, and both expanded valence-shell and "increased-valence" structures that are similar to (39) and (40) may be constructed. F_3PO is isoelectronic with PO_4^{3-} , and the corresponding valence-bond structures are (41)-(43). The P-F bond-lengths¹⁵ of 1.523 Å are shorter than the 1.561 Å¹⁶ for PF_3 (with formal single-bonds), and this suggests that the expanded valence-shell structure is more appropriate than the "increased-valence" structure. If this is the case, it is probable that the expanded valence-shell structure of type (39) (with P replacing N) is of greater significance than (40) for PO_4^{3-} , whose P-O bond-lengths^{17,18} of 1.54 Å are longer than the 1.437 Å for F_3PO but much shorter than the estimate of 1.73 Å for a P-O single bond¹⁸.



(41)



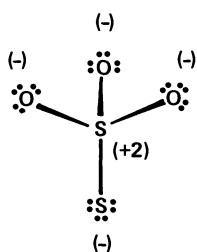
(42)



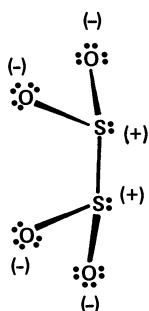
(43)

17-6 $S_2O_n^{2-}$ ($n = 3, 4, 5, 6$)

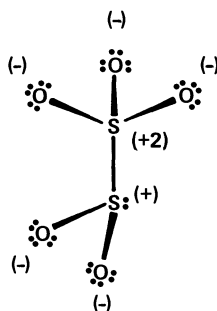
The thio anions $S_2O_n^{2-}$ ($n = 3-6$) provide an interesting set of systems to contrast the alternative delocalization theories of Sections 17-1 to 17-5, namely those of delocalization of lone-pair electrons into either vacant sulphur 3d-orbitals or vacant bonding orbitals. (Such delocalizations generate electron-pair bonds and one-electron bonds, respectively.) For these anions, the standard Lewis octet structures are (44)-(47), each of which involves considerable formal charge separation.



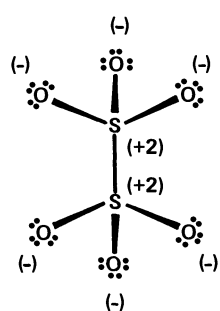
(44)



(45)

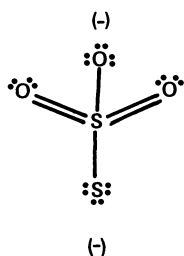


(46)

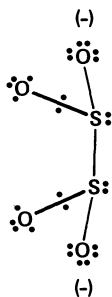


(47)

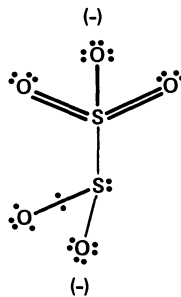
On the basis of our previous discussions, we suggest that the lone-pair delocalization into sulphur 3d-orbitals is appropriate when the sulphur atoms carry formal charges of +2 in the Lewis octet structure. But, when the sulphur atoms carry formal charges of +1, delocalization of lone-pair electrons into bonding S-O orbitals is of rather greater relevance. Using these delocalizations, we can generate valence-bond structures of types (48)-(51) from (44)-(47).



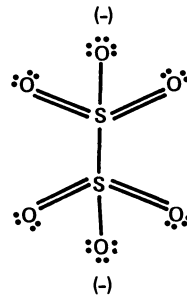
(48)



(49)



(50)



(51)

For each SO_3^- linkage of (48), (50) and (51), we have indicated delocalizations of two O^- electrons into sulphur 3d orbitals. A small amount of delocalization of O^- electrons into bonding S-O orbitals is also possible (c.f. (37) for SO_4^{2-}).

The valence-bond structures (48)-(51) suggest that the S-S lengths should increase in the order $\text{S}_2\text{O}_3^{2-} < \text{S}_2\text{O}_6^{2-} < \text{S}_2\text{O}_5^{2-} < \text{S}_2\text{O}_4^{2-}$, and the measured lengths¹⁹⁻²² of 1.97 Å, 2.08-2.16 Å, 2.17 Å and 2.39 Å show this to be the case. For $\text{S}_2\text{O}_3^{2-}$, the two $d_{\pi}-p_{\pi}$ bonds should be delocalized fairly evenly over the S-S and three S-O bonds, to give bond-numbers of $1\frac{1}{2}$ for each bond.

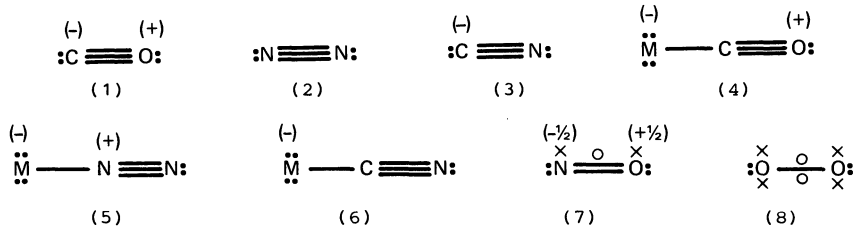
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- 11 O. Glemser, *Angewandte Chem. (Int. Ed.)*, **2**, 530 (1973).
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- 17 See for example J.R. Rea and F. Kostiner, *Acta Cryst* **B28**, 3461 (1972).
- 18 L. Pauling, *The Nature of the Chemical Bond* (Cornell 1960), p. 321.
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CHAPTER 18

TRANSITION METAL COMPLEXES WITH CO, N₂, NO AND O₂ LIGANDS

The diatomic molecules and ions, CO, N₂, CN⁻, NO and O₂, can bond to transition metals. Isoelectronic CO, N₂ and CN⁻, with ten valence-shell electrons, have triple bonds and no unpaired electrons in their Lewis octet structures (1)-(3). Each may use a lone-pair of electrons to coordinate with a transition metal, as in (4)-(6), thereby functioning initially as Lewis bases. NO and O₂, with 11 and 12 valence-shell electrons respectively, have one and two unpaired electrons. Their valence-bond structures (7) and (8) involve one or two Pauling "3-electron bonds" as well as lone-pairs of electrons. The possibility exists that these molecules may react either as Lewis bases or as free radicals. For NO, examples of both Lewis base and free radical behaviour are known, but ground-state O₂ seems to behave exclusively as a free radical. We shall now describe valence-bond structures for a few transition metal complexes that involve some of these ligands.



18-1 CARBONYL COMPLEXES

In the standard Lewis structures (4), (5) and (6), we have used a lone-pair of carbon or nitrogen electrons to form a σ -single bond with the metal M.

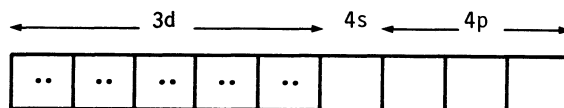
Carbonyl, dinitrogen and cyanide complexes of transition metals are generally not stable unless the metal has lone-pair electrons occupying atomic orbitals which overlap with ligand π orbitals. In structures (4)-(6), we have indicated two sets of lone-pair electrons. If we assume that these electrons occupy metal d_{xz} and d_{yz} atomic orbitals, then they can overlap with the atomic orbitals that form the π_x and π_y bonds of the ligands. For a M-CO linkage, we show the overlap of these orbitals in Fig. 2-4. These are the types of π -orbital overlaps that pertain for trigonal bipyramidal and octahedral carbonyl compounds, such as Fe(CO)₅ and Cr(CO)₆. For tetrahedral compounds such as Ni(CO)₄, the metal-carbon π overlaps are similar to those described in Section 4-5 with the d_{z^2} and $d_{x^2-y^2}$ metal orbitals forming strong π -bonds, and the d_{xy} , d_{yz} and d_{xz} orbitals forming weak π -bonds.

	ν_{CO}	n_{CO}	n_{MC}
CO	2150	3.0	
Ni(CO) ₄	2056	2.5 (2.64) ^a	1.5 (1.33) ^a
Co(CO) ₄ ⁻	1886	2.375 (2.14) ^a	1.625 (1.89) ^a
Fe(CO) ₄ ²⁻	1786	2.25 (1.85) ^a	1.75 (2.16) ^a

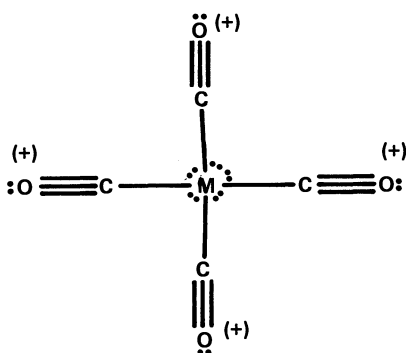
Table 18-1 Data for some carbonyl compounds. ^aExperimental estimates.

The tetracarbonyls Ni(CO)₄, Co(CO)₄⁻ and Fe(CO)₄²⁻ are isoelectronic and tetrahedral in shape. Their C-O stretching frequencies are reported in Table 18-1, and show that the strengths of the C-O bonds decrease in order of CO > Ni(CO)₄ > Co(CO)₄⁻ > Fe(CO)₄²⁻.

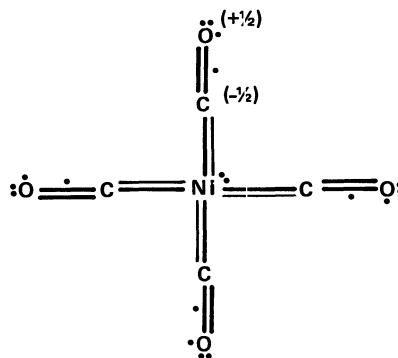
The electronic configurations of isoelectronic Ni, Co⁻ and Fe²⁻ are (3d)⁸(4s)² from which we may obtain the low-spin valence-state configuration of (9) with four vacant orbitals. These orbitals may be sp³ hybridized, and used by the four C-O ligands to form four coordinate bonds, as in (10). The metal then acquires formal negative charges of -4 for Ni, -5 for Co and -6 for Fe.



(9)



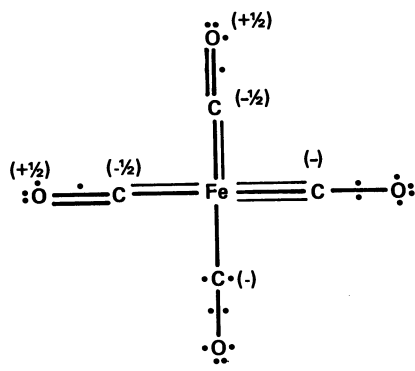
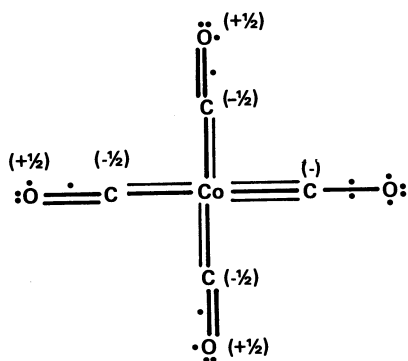
(10)



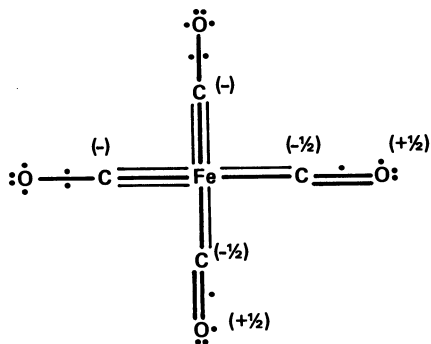
(11)

To remove formal charge from the metal, and from the oxygen atoms, we may delocalize metal electrons into antibonding C-O orbitals. For Ni⁴⁻ and Co⁵⁻, we can delocalize four and five 3d electrons, thereby generating "increased-valence"

structures (11) and (12). In each of these structures, we have obtained an uncharged metal atom, and some (fractional) double bonding for the Ni-C and Co-C bonds. To generate neutral iron in $\text{Fe}(\text{CO})_4^{2-}$, we need to delocalize six electrons into antibonding C-O orbitals. Since Fe^{6-} in (10) has only five lone-pairs of valence electrons, we must generate "increased-valence" structure (13). But this structure is unsatisfactory since it can imply paramagnetism for $\text{Fe}(\text{CO})_4^{2-}$; there are two Pauling "3-electron bonds" with uncompensated electron spins in (13). To obtain a diamagnetic structure, and a neutral iron atom, we need to assume that the iron 3p electrons can participate appreciably in M-CO bonding. If we delocalize one of these electrons, as well as five 3d electrons, we thereby generate "increased-valence" structure (14). (To the author's knowledge, no calculations have yet been made in order to ascertain whether or not the 3p electrons can participate in this manner, but it seems necessary to include them to obtain a consistent valence-bond treatment of M-CO bonding for tetra, penta and hexacarbonyls. The hypothesis invoked here is that the transition metal carries zero formal charge in the valence-bond structures.)



In Table 18-1, we have reported C-O stretching frequencies $\nu_{\text{CO}}(\text{cm}^{-1})$, and calculated and (in parentheses) experimental¹ C-O and M-C bond orders and bond-numbers n_{CO} and n_{MC} . Since the "increased-valence" bonding unit $\text{M}-\text{C} \cdot \ddot{\text{O}}$ is equivalent to the resonance of $\text{M}-\text{C} \ddot{\text{O}} \leftrightarrow \text{M} \overset{\cdot}{\text{C}} \ddot{\text{O}}$, the M-C and C-O bond indices will both equal $\frac{1}{2}$ if we assume here that the two structures contribute equally to the resonance. The calculated bond orders follow the experimental trends in bond properties. A recent empirical



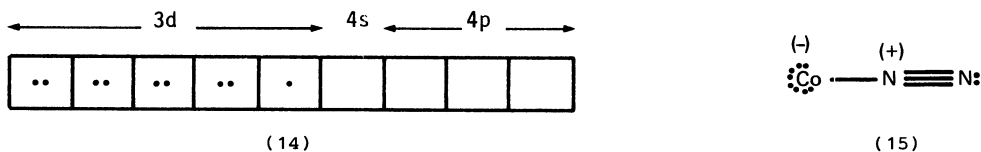
relationship that has been established² between ν_{CO} and n_{CO} , namely $\nu_{\text{CO}} = 413 n_{\text{CO}} + 904$, gives CO bond-orders of 2.79, 2.38 and 2.14 for the three tetracarbonyls of Table 18-1.

18-2 DINITROGEN COMPLEXES

Numerous complexes of N_2 with transition metals have now been prepared³, and the geometries for many of them are now known. We shall describe the metal- N_2 bonding for two of them here, namely $\text{CoH}(\text{N}_2)(\text{PPh}_3)_3$ and $[\{\text{Ru}(\text{NH}_3)_5\}_2\text{N}_2]^{4+}$.

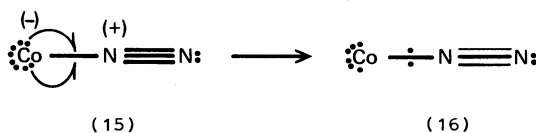
18-2(a) $\text{CoH}(\text{N}_2)(\text{PPh}_3)_3$ For $\text{CoH}(\text{N}_2)(\text{PPh}_3)_3$, the Co- N_2 linkage has been found to be linear⁴, with Co-N and N-N lengths of 1.802 Å and 1.126 Å. We may compare these lengths with the estimate of 1.96 Å for a Co-N single bond⁴, and the 1.098 Å for the triple bond of free N_2 .

From the $(3d)^7(4s)^2$ ground-state configuration of Co, we may obtain a $(3d)^9$ valence-configuration (14) with one unpaired electron. This electron may be used for σ -bonding with a hydrogen atom. The four vacant orbitals of (14) may be used for σ -bonding by N_2 and the three PPh_3 ligands. In (15), we show the σ -bonding for the Co- N_2 linkage.



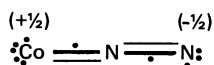
To form five σ -bonds, the cobalt may use hybrid orbitals that are constructed from its $3d_{z^2}$, $4s$ and three $4p$ orbitals. The cobalt is then dsp^3 hybridized. If we assume that the cobalt and two nitrogen atoms lie along the z -axis, then the cobalt lone-pair electrons of (15) occupy $3d_{xy}$, $3d_{yz}$, $3d_{xz}$ and $3d_{x^2-y^2}$ orbitals. The $3d_{yz}$ and $3d_{xz}$ orbitals overlap with the π_y and π_z bonds of the N_2 ligand.

In (15), the formal charge for the cobalt atom and the adjacent nitrogen atom are negative and positive respectively, relative to their values prior to coordination. We may reduce their magnitudes by delocalizing one electron from each of the d_{yz} and d_{zx} orbitals into bonding Co-N π_y and π_z orbitals, to obtain "increased-valence" structure (16).

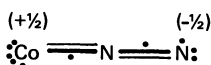


In (16), the N-N π -bonds have bond-numbers less than unity and therefore the N-N bond should be longer than that of free N_2 . The Co-N bond of (16) has double-bond character, and therefore this bond would be expected to be shorter than a single bond. The bond lengths which are reported above confirm these expectations.

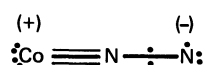
We note that the Co- N_2 bonding is similar to that which we have described for N_2O in Section 13-1. Other "increased-valence" structures such as (17), (18) and (19) may also be constructed. Elsewhere⁵, we have shown that (16) should be the most important of the four types of structures, but all will participate in resonance to some extent.



(17)

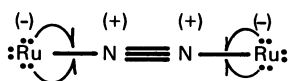


(18)

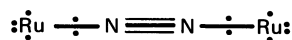


(19)

18-2(b) $[\{\text{Ru}(\text{NH}_3)_5\}_2\text{N}_2]^{4+}$ N_2 can bond simultaneously to two Ru(II) ions, and this occurs in the cation $[\{\text{Ru}(\text{NH}_3)_5\}_2\text{N}_2]^{4+}$. The Ru^{2+} configuration is $(4d)^6$, and the σ -bonding with the N_2 is shown in (20). The formal charges displayed for the ruthenium ions in this structure are those which are relative to Ru^{2+} . From (20), we may generate the "increased-valence" structure (21), by delocalizing $4d_{xz}$ and $4d_{yz}$ electrons of Ru^{2+} into vacant bonding Ru-N π -orbitals. For each set of π -electrons, there is a 6-electron 4-centre bonding unit.



(20)



(21)

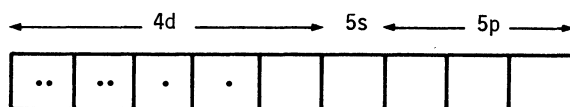
The reported Ru-N and N-N lengths⁶ are 1.928 Å and 1.124 Å. Davis and Ibers⁷ have estimated the Ru-N single bond length to be 2.125 Å and (21) indicates clearly that the Ru-N bonds of $[\{\text{Ru}(\text{NH}_3)_5\}_2\text{N}_2]^{4+}$ are shorter than single bonds. The N-N length is longer than the triple bond of free N_2 , and (21) with fractional N-N π -bonds shows why this should be so.

Numerous other binuclear dinitrogen complexes have been characterized³, with N-N bond-lengths that are also longer than the 1.098 Å for N_2 . "Increased-valence" structures that are similar to (21) are appropriate for each of these systems, and they account for the observation that the N-N and M-N bond lengths are respectively longer than triple bonds and shorter than single bonds.

18-3 TRANSITION METAL NITROSYL COMPOUNDS

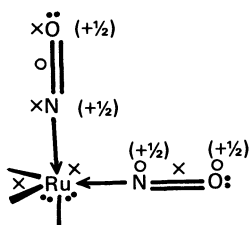
In the introduction to this chapter we have indicated that NO may react with transition metals either as a free radical, by using its unpaired electron, or as a Lewis base by using the nitrogen lone-pair of electrons. To give consideration to these two types of behaviour, we shall examine the bonding for the Ru-NO linkages of the diamagnetic complex $[\text{RuCl}(\text{PPh}_3)_2(\text{NO})_2]^+$, which we shall initially express in terms of its components as $\text{Ru}^{2+} + \text{Cl}^- + 2 \text{PPh}_3 + 2 \text{NO}$. The bond-angles for the two Ru-NO linkages are⁸ 178° and 138° , and therefore essentially linear and angular linkages are present in this complex.

The valence-shell electronic configuration of Ru^{2+} is $(4d)^6$ of (22). To form a diamagnetic complex, it is necessary for this configuration to have two unpaired electrons available for spin-pairing with the unpaired electrons of the two NO ligands. Therefore, we have represented the $(4d)^6$ configuration of (22) as an intermediate-spin configuration, with a t_{2g} orbital and an e_g orbital singly occupied. The t_{2g} orbital can overlap with an antibonding π_{NO}^* orbital of NO.

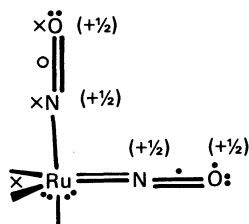


(22)

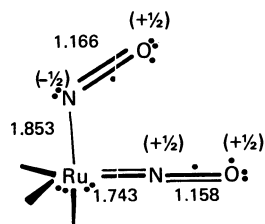
In (22), there are five vacant orbitals that may be dsp^3 hybridized, and used for σ -coordination with five ligands. If this is done, we obtain the valence-bond structure (23) with four unpaired electrons. Because the singly-occupied t_{2g} orbital and a π_{NO}^* orbital can overlap, we may spin-pair two electrons to obtain the "increased-valence" structure (24). This structure has two unpaired electrons that occupy non-overlapping e_g and π_{NO}^* orbitals, and the lowest-energy arrangement for these electrons occurs when they have parallel spins. Thus, if both Ru-NO linkages are linear, the complex would have a paramagnetic ground state.



(23)



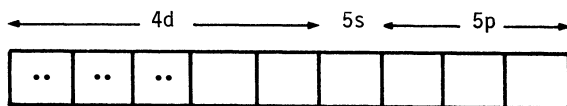
(24)



(25)

To obtain diamagnetism, it is necessary to assume that one of the NO ligands does not coordinate to the Ru^{2+} as a Lewis base, and that the π_{NO}^* unpaired electron of this ligand spin-pairs with the e_g unpaired electron of (22). This e_g orbital can hybridize with the 5s and 5p orbitals to form five dsp^3 hybrid orbitals. The spin-pairing can only provide a Ru-N bonding interaction if this linkage is angular. The resulting valence-bond structure, together with the experimental bond-lengths⁸, for the complex is (25), with one linear and one angular Ru-NO linkage. This valence-bond structure makes immediately clear why the observed N-O lengths⁸ for the complex are similar to those of free NO (1.15 Å) with valence-bond structure (7), and why the Ru-N bond of the linear Ru-NO linkage is shorter than that for the angular linkage.

It is often considered⁹ that NO^+ and NO^- , with valence-bond structures (26) and (27) are the formal ligands for linear and angular M-NO linkages. If this point of view is adopted, then the valence-bond structure (29) is obtained for the complex in which both NO^+ and NO^- have coordinated to the low-spin Ru^{2+} of (28). It is now possible to generate "increased-valence" structure (25) from (29) by delocalizing (i) a non-bonding t_{2g} electron from the ruthenium into a vacant π_{NO}^* orbital of the NO^+ , thereby reducing the magnitudes of the formal charges, and (ii) a non-bonding $\bar{\pi}_{\text{O}}$ electron of the coordinated NO^- into the adjacent NO bond-region. These delocalizations generate (30), from which (25) is obtained when the remaining t_{2g} and π_{NO}^* odd-electrons are spin-paired. However, it seems easier to generate (25) by assuming that free NO radicals rather than NO^+ and NO^- are the valence-states for the ligands.



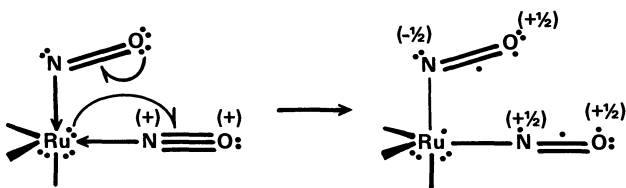
(28)



(26)



(27)



(29)

(30)

Further examples of "increased-valence" descriptions for transition-metal nitrosyls are provided in Ref. 10.

18-4 DIOXYGENYL ADDUCTS

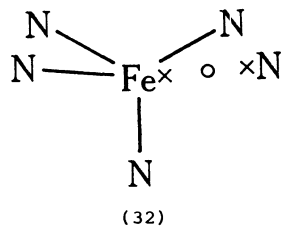
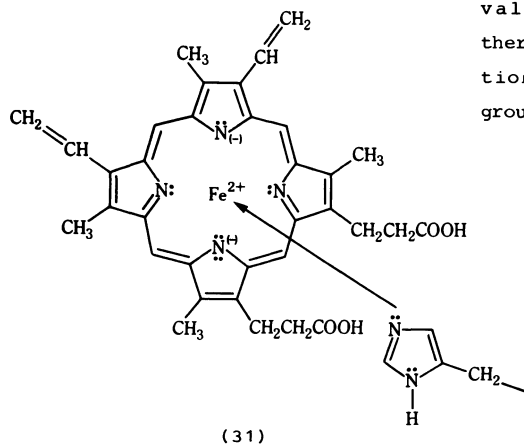
Many transition metal complexes are now known to form adducts with molecular oxygen. Those which combine reversibly with O_2 are designated as oxygen carriers; adducts in which O_2 is absorbed irreversibly are also known. Here, we shall provide "increased-valence" descriptions for some reversible Fe(II) and Co(II) dioxygenyl adducts, thereby contrasting different formulations for the oxidation state of the metal ion that have been proposed for these types of complexes.

18-4(a) Oxyhaemoglobin Haemoglobin (Hb) is probably the most familiar oxygen carrier; it transports O_2 from the lungs to the tissues of the body. The O_2 absorption is reversible; O_2 combines with the iron atoms of haemoglobin at high pressures in the lungs, and is released to the body tissues at low pressures.

Haemoglobin has a molecular weight of ≈ 64500 and contains four iron atoms which are formally in the ferrous state. Each iron atom is coordinated to four nitrogen atoms of porphyrin, and to the nitrogen atom of a histidine group. This bonding is shown in (31), and the iron has been estimated¹¹ to lie 0.83 \AA below the plane of the four porphyrin nitrogen atoms.

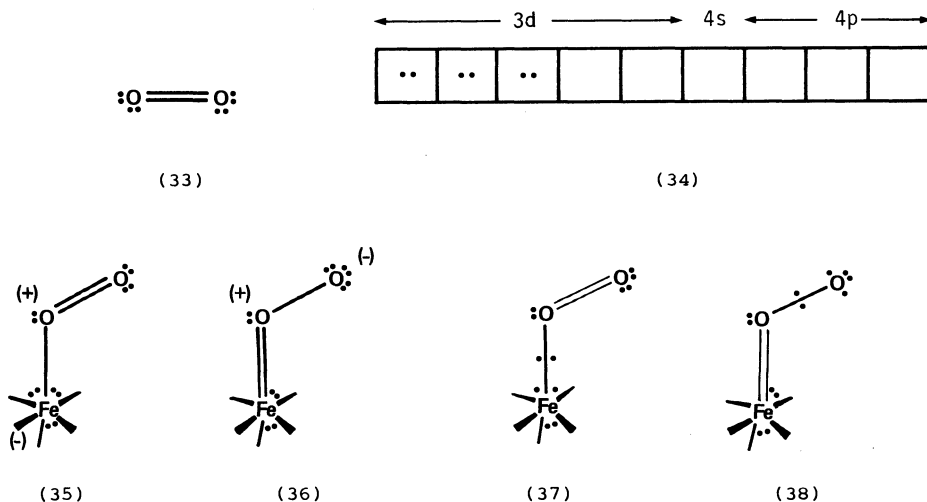
In haemoglobin, each of the four ferrous ions has four unpaired electrons with parallel spins in the ground-state, and therefore the molecule is paramagnetic¹². The six electrons of the Fe^{2+} ions have the orbital occupations displayed in Fig. 5-1 for high-spin $S = 2$ spin-states. Because five ligand nitrogen atoms of (31) can coordinate to the high-spin Fe^{2+} , and there are only four vacant orbitals (4s and 4p) for this ion, haemoglobin is an example of a hypoligated complex (Section 5-1). The bonding of the four nitrogen atoms of porphyrin to the iron may be described by utilizing three electron-pair bonds and a Pauling "3-electron bond". The remaining vacant orbital of Fe^{2+} may be used to form an Fe-N single bond between the Fe^{2+} and

the nitrogen atom of the proximal histidine of (31). Resonance between the four valence-bond structures of type (32) therefore provides a valence-bond description of the Fe-N bonding for each heme group of haemoglobin.



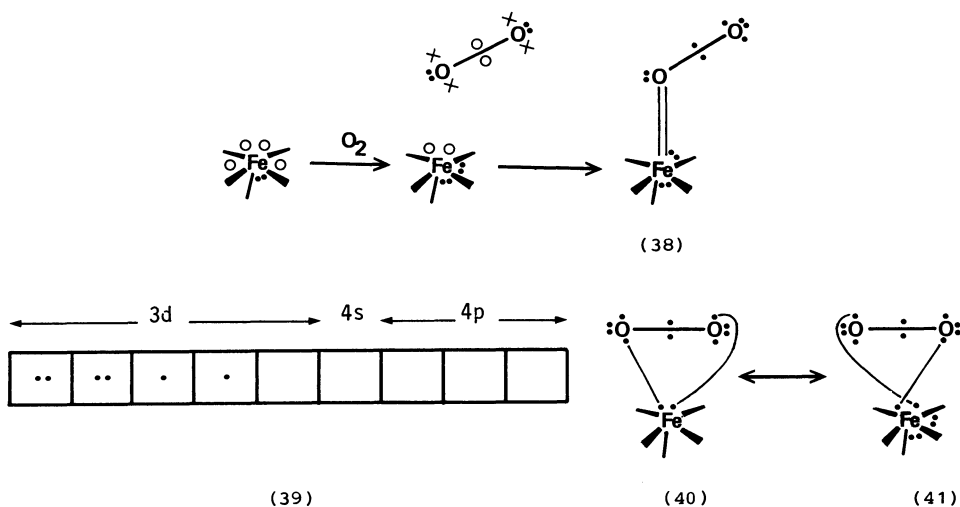
When four oxygen molecules bind to the four iron atoms of haemoglobin, oxyhaemoglobin is formed. Magnetic susceptibility measurements^{13,14} indicate that each Fe(II)O₂ linkage of oxyhaemoglobin is diamagnetic at room temperature, i.e. no unpaired electron spins are present. (It may be noted that recent magnetic susceptibility measurements¹⁵ through the temperature range of 25-250 K indicate that although the ground-state is an $S = 0$ spin state, antiferromagnetic rather than diamagnetic behaviour occurs as the temperature is raised above 50 K. However, the experimental basis for this work has been questioned¹⁴.) Here we shall describe some bonding theories for the $S = 0$ ground-state of each Fe(II)O₂ linkage. Similar theories are also appropriate for oxymyoglobin with one Fe(II)O₂ linkage, and the "picket fence" Fe(II) oxygen carriers.

To account for the diamagnetism of oxyhaemoglobin, Pauling and Coryell¹³ in 1936 suggested that an $S = 0$ excited state with valence-bond structure (33) for O₂ could coordinate with the low-spin ($S = 0$) configuration of (34) for Fe²⁺. In (34), the six vacant orbitals may be d^2sp^3 hybridized. Five of these orbitals may be used for coordination with the five nitrogen atoms of (31), and the sixth orbital is available for coordination with the O₂. For oxyhaemoglobin, the iron atoms lie in the plane of the nitrogen atoms of the porphyrin ligands¹¹. By coordinating the O₂ of (33) to the Fe²⁺ of (34), Pauling and Coryell¹³ obtained the standard Lewis structure (35) for each Fe-O₂ linkage of oxyhaemoglobin. This valence-bond structure can then participate in resonance with the standard Lewis structure (36). By comparison of these structures with (8) for O₂, Pauling and Coryell concluded that a "profound change in the electronic structure of O₂ occurs when it bonds to haemoglobin". However, if we use (35) and (36) to generate "increased-valence" structures, it is possible to show that this need not be the case.



By delocalizing lone-pair electrons from the Fe^- and O^- of (35) and (36) into vacant bonding Fe-O or O-O orbitals, we reduce the magnitude of the formal charges, and obtain "increased-valence" structures (37) and (38)¹⁶⁻²⁰.

In (37) and (38), the O_2 excited and ground-states (33) and (8) are respectively bonded to the iron. We might therefore expect (38) to be more stable than (37). If this is so, then we may give the following description of the reaction between O_2 and an iron atom of haemoglobin. As the ground-state of O_2 approaches the high-spin Fe(II), the latter is promoted to the valence-state configuration of (39), which is an intermediate-spin state ($S = 1$) with two unpaired electrons. These two electrons spin-pair with the two unpaired electrons of O_2 to generate an $S = 0$ Fe(II) O_2 linkage with the "increased-valence" structure (38). Thus, we may write.



In 1960, McClure²¹ had suggested that this promotion of Fe^{2+} to the intermediate-spin state of (39) occurs when it reacts with O_2 , and we have given here the valence-bond structure that corresponds to this description. The results of some Mössbauer measurements²² indicate that the promotion energy is rather small - $\sim 250 \text{ cm}^{-1}$.

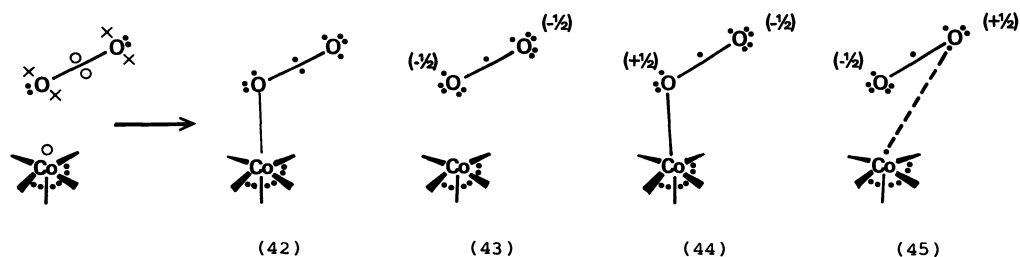
The Fe(II) ($S = 1$) + O_2 ($S = 1$) theory for the bonding of O_2 to haemoglobin has been discussed on a number of occasions^{16-21,23-26}. Generalized valence-bond²⁷ and molecular orbital calculations²⁸ provide further support for this hypothesis, although it has been recently questioned²⁹.

Although the possibility also exists that the O_2 may bond symmetrically to the Fe(II), as occurs in "increased-valence" structures (40) and (41), experimental and theoretical evidence^{30,27} now favours the non-symmetrical conformation displayed in valence-bond structures (35)-(38).

The O-O stretching frequency of 1107 cm^{-1} for oxyhaemoglobin³¹ is often cited³²⁻³⁴ as evidence that the superoxide anion O_2^- is bonded to low-spin ($S = \frac{1}{2}$) Fe^{3+} , with spin-pairing of the unpaired-electrons of these two species to form $S = 0$ Fe(III)O_2^- linkages. For O_2^- , as in KO_2 , the O-O stretching frequency is 1145 cm^{-1} , whereas that for free ground-state O_2 is 1556 cm^{-1} ³². However, when the O_2 ground-state is bonded to Fe(II) , as in (38), the electronegativity of one oxygen atom must be altered relative to that of the other, and an unequal sharing of the four O-O bonding electrons may therefore occur. The O-O bond-order for (38) can therefore be reduced below the value of 2 for free O_2 , thereby leading to a reduction of the O-O stretching frequency for oxyhaemoglobin¹⁸. Molecular orbital calculations²⁸ give an O-O bond-order of 1.6 when the O_2 ground-state is bonded to the Fe(II) .

"Increased-valence" descriptions of the bonding for the Fe-CO and Fe-NO linkages for the CO and NO derivatives of haemoglobin are described in Ref. 17.

18-4(b) Cobalt Oxygen Carriers Molecular oxygen can form both 1:1 and 2:1 adducts (Co-O_2 and $\text{Co-O}_2\text{-Co}$) with different Co(II) complexes. For the 1:1 adducts, the O-O stretching frequencies are similar to those³²⁻³⁴ of O_2^- , and an unpaired electron is located mainly on the two oxygen atoms. On the basis of these observations, the adducts have been formulated³²⁻³⁴ as Co(III)O_2^- , with the O_2^- forming a coordinate bond to low-spin Co(III) , which has a $(3d)^6$ configuration. Alternatively, we may formulate¹⁶⁻²⁰ the electronic structure as Co(II)O_2 , for which the O_2 valence-bond structure (8) has spin-paired one of its two unpaired electrons with the unpaired electron of low-spin Co(II) $(3d)^7$. Thus, we may generate the "increased-valence" structure (42) by means of this reaction.

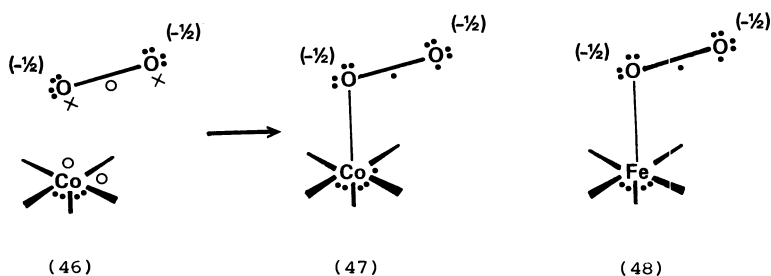


The Co(II)O_2 structure (42) accounts simply¹⁸ for the observations that we have discussed above. The O_2 retains one unpaired-electron, and because the oxygen atom bonded to the cobalt must have a different electronegativity from that of the terminal oxygen atom, the four O_2 bonding electrons will not be shared equally by the two oxygen atoms. This reduction in the extent of covalent bonding for the O_2 of (42) should be chiefly responsible for the decrease in O-O stretching frequency that is observed when O_2 bonds to Co(II) .

We shall now compare the Co(II)O_2 and the Co(III)O_2^- structures. The valence-bond structure for low-spin Co(III) and O_2^- are shown in (43). On coordinating the

O_2^- with Co(III), we obtain the Co(III) O_2^- valence-bond structure (44). We may also form the "long-bond" Co(III) O_2^- structure (45), which for non-symmetrical coordination, should be less stable than (44). We now note that the $Co-O \cdot \ddot{O}$ bonding unit summarizes resonance between $Co-O \ddot{O}$ and $\overset{\cdot}{Co}-\ddot{O}-\ddot{O}$. Therefore, the Co(II) O_2 structure (42) is equivalent to resonance between (44) and (45), and each of these Co(III) O_2^- structures is now a special form of the Co(II) O_2 structure. The Co(II) O_2 structure must be more stable than either of the Co(III) O_2^- structures.

We may construct another Co(III) O_2^- structure, namely the "increased-valence" structure (47). To do this, we spin-pair the unpaired electron of O_2^- with one of the two unpaired electrons of the Co(III) configuration of (46). Because (47) retains an unpaired electron on the cobalt, it cannot represent the ground-state for any of the adducts which have so far been studied. However, it must participate in resonance with the Co(II) O_2 structure (42), with the latter making the major contribution to the bonding. Similarly, for oxyhaemoglobin (HbO_2), the Fe(III) O_2^- structure (48) will participate in resonance with the Fe(II) O_2 structure (38), but, because the latter structure has three extra bonding electrons, it should be more stable than (48).



The $S = \frac{1}{2}$ and $S = 0$ spin wave-functions for the Co(II) O_2 and Fe(II) O_2 linkages of "increased-valence" structures (42) and (38), with three and four singly-occupied orbitals, are described in Section 15-2 and in Refs. 20 and 16.

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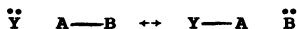
CHAPTER 19

SOME ELECTRON-EXCESS σ BONDED SYSTEMS

Most of the "increased-valence" structures that we have discussed so far may be derived from Lewis structures by delocalizing lone-pair π and/or $\bar{\pi}$ electrons into vacant bonding or antibonding orbitals. The atomic orbital overlaps which are appropriate for some of these delocalizations are shown in Figs. 1-5 and 2-4. We shall now consider a few systems whose "increased-valence" structures may be constructed by delocalizing one or more lone-pair σ electrons of a Lewis structure into bonding or antibonding σ orbitals. Some other examples will also be discussed in Chapter 20, where the theory will be presented in a slightly different form. However, the principles for both chapters are the same.

19-1 TRIHALIDE ANIONS AND SOME RELATED MOLECULES

Each of the trihalide anions I_3^- , Br_3^- , Cl_3^- and ICl_2^- , and XeF_2 , have 22 valence-shell electrons. XeF_2 is a symmetrical linear molecule¹, and a similar geometry has been reported for each of I_3^- , Br_3^- and ICl_2^- ². Non-symmetrical geometries for some of these trihalide ions are also known² but we shall not concern ourselves with them here. Excluding the possibility of d-orbital participation, we shall now describe standard Lewis, "increased-valence" and Linnett (Section 2-2) non-paired spatial orbital bonding schemes for these systems, using I_3^- and XeF_2 as representative examples. Such molecules are often referred to as "hypervalent" molecules, for which the number of ligands bonded to a central atom exceeds the covalence of the central atom in the standard Lewis octet structures. Musher³ has discussed many examples of hypervalent molecules. We point out here that hypervalence for an atom A may arise whenever valence-bond resonance of the type



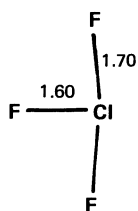
can occur for four σ -electrons. Therefore, the bonding schemes for this chapter do not differ from those of the previous chapters, except in so far as we shall be dealing only with σ -bonding. Hypervalency is an extremely widespread phenomenon, and Musher³ has also pointed this out. The delocalized molecular orbital theory for these hypervalent molecules involves 3-centre molecular orbitals, and we have given an account of it in Section 2-3(a), for the simplest hypervalent system H_3^- . This molecular orbital theory was first proposed in 1951 by Pimentel⁴, and Hach and Rundle⁵, and has been used subsequently by many workers^{2,6-9} to describe 4-electron

Probably the most convenient valence-bond structures for I_3^- and XeF_2 are the Linnett non-paired spatial orbital structures (8) and (9), which have two one-electron σ bonds.

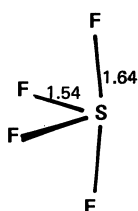
In Chapter 23, comparisons are made between the wave-functions for Lewis, "increased-valence" and Linnett structures.

For I_3^- and XeF_2 , the bond lengths of 2.93 Å and 2.01 Å are longer than the single bond lengths^{2,1,11} of 2.67 Å and 1.81 Å for I_2 and XeF_2^+ . Each of the valence-bond representations above indicates the presence of long I-I or Xe-F bonds. If we include the $5d_{z^2}$ orbital on the central atom of either system as a hybridization function (c.f. Sections 1-1 and 17-1), the valence-bond structures, such as (10) for I_3^- , have single bonds between the central and both terminal atoms, and therefore they do not make obvious why the bonds should be long.

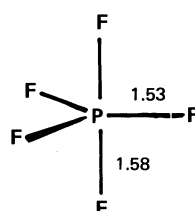
If only the 3s and 3p orbitals of the second-row atoms are assumed to participate in bonding, the axial σ -bonding for each of ClF_3 , SF_4 and PF_5 is similar to that which we have described for XeF_2 , i.e. 4-electron 3-centre bonding is involved. The geometries, standard Lewis and "increased-valence" structures are displayed in (11)-(21), (with only one equivalent structure displayed for SF_4 and PF_5). The bond-properties implied by either set of valence-bond structures are in accord with the observation¹²⁻¹⁴ that the axial bonds are longer than the equatorial bond(s) for each molecule. However, because the "increased-valence" structures are equivalent to resonance between standard and "long-bond" Lewis structures (e.g. for SF_4 , (19) \equiv (18) \leftrightarrow (22)), resonance between the "increased-valence" structures must provide a more stable representation of the electronic structure than does the more-familiar resonance between the standard Lewis structures.



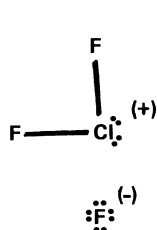
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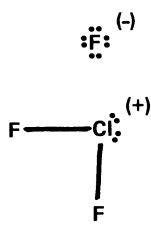
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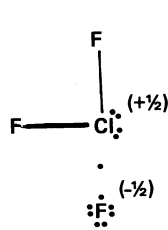
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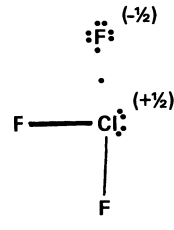
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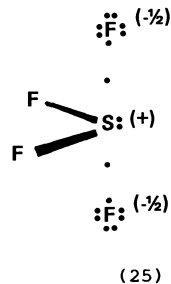
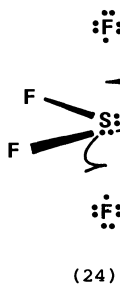
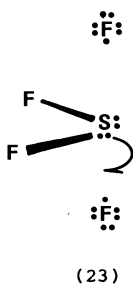
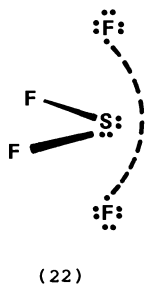
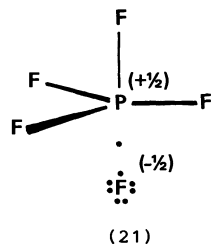
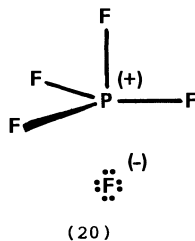
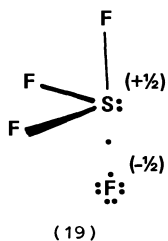
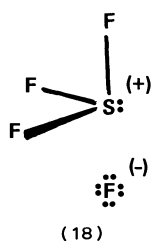
(15)



(16)



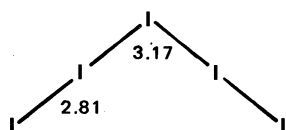
(17)



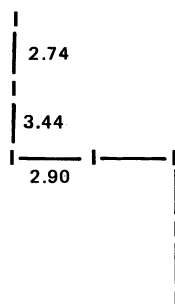
In Section 4-8, we have generated Pauling "3-electron bond" structures for ClF_2 and SF_3 from $\text{ClF} + \text{F}$ and $\text{SF}_2 + \text{F}$. A similar procedure may be used to construct the "increased-valence" structures for ClF_3 , SF_4 and PF_5 . For example, by writing down SF_4 as $\text{SF}_2 + 2\text{F}$ as in (23), then (i) delocalizing a sulphur 3p electron into an axial S-F bonding σ -orbital, and (ii) spin-pairing the unpaired-electron of SF_3 with that of a second axial fluorine atom, we obtain "increased-valence" structure (19). Alternatively by delocalizing both the sulphur 3p electrons of SF_2 into separate axial S-F bonding σ -orbitals, as in (24), we obtain the Linnett structure (25) for SF_4 .

19-2 THE POLYIODIDE ANIONS

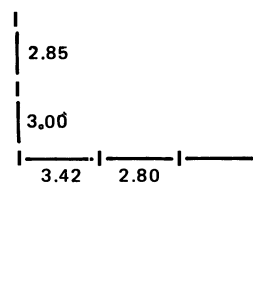
The geometries² for the polyiodide anions I_5^- , I_7^- and I_8^{2-} are given in (26), (27) and (28). Each of the I-I bond-lengths is longer than the single bond length of 2.67 Å for free I_2 . These observations may be accounted for conveniently by means of the "increased-valence" structures (30), (32) and (34), which we may derive from the Lewis or non-paired spatial orbital structures (29), (31) and (33). For the latter three structures, we have subdivided the ions into $\text{I}_2 + \text{I}^- + \text{I}_2$, $\text{I}_2 + \text{I}_3^- + \text{I}_2$, and $\text{I}_2 + \text{I}^- + \text{I}_2 + \text{I}^- + \text{I}_2$ components, and used the non-paired spatial orbital structure (8) for I_3^- . All of the bonds must be σ -bonds.



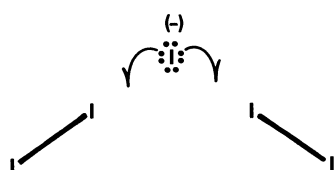
(26)



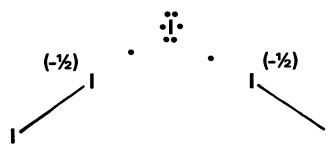
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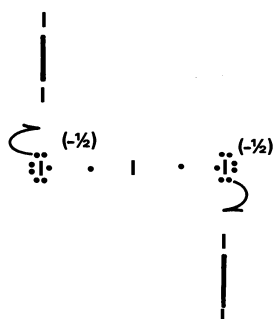
(28)



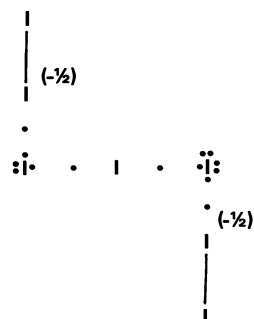
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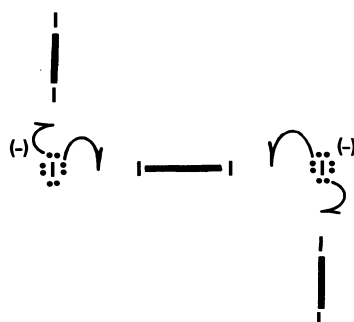
(30)



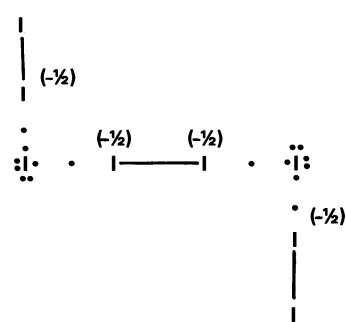
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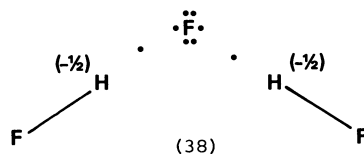
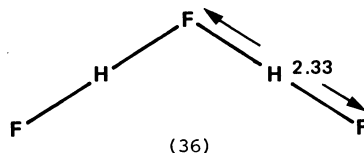
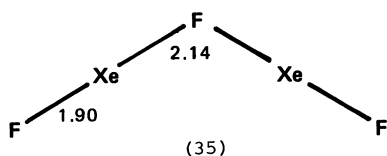
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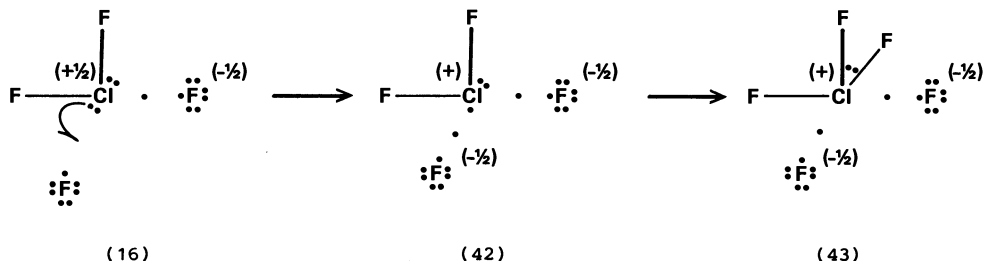
19-3 Xe_2F_3^+ AND H_2F_3^-

The penta-atomic ions Xe_2F_3^+ and H_2F_3^- have the bond-lengths^{15,16} shown in (35) and (36). We may construct the "increased-valence" structures (37) and (38) from the Lewis structures for $\text{XeF}^+ + \text{F}^- + \text{XeF}^+$ and $\text{HF} + \text{F}^- + \text{HF}$. These "increased-valence" structures are similar to (30) for I_5^- , and imply that the two terminal bonds of each ion should be shorter than the two bridging bonds, and that all bonds should be longer than the single bond lengths of 1.81 and 0.92 Å for XeF_2^+ and HF.

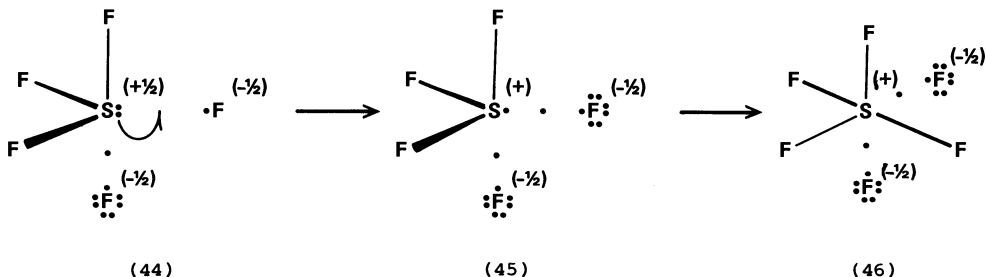


The above description is strictly valid only for 90° bridging bond-angles. When this is the case, two of the bridging fluoride 2p atomic orbitals overlap with the xenon 5p_σ- or hydrogen 1s atomic orbitals, as is shown in Fig. 19-1 for Xe_2F_3^+ . Two 4-electron 3-centre bonding units therefore pertain for the eight σ-electrons of these ions. However, both Xe_2F_3^+ and H_2F_3^- have bridging bond-angles^{15,16} which are rather larger than 90°, namely 150° and 118°. If the bridging bond-angle were 180°, then only one 2p orbital of the bridging fluorine is available for σ-bonding with the xenon or hydrogen atoms. For linear Xe_2F_3^+ , the orbital overlaps are displayed in Fig. 19-1; a 5-centre overlapping scheme is involved, which accommodates six electrons (two for F^- and two from each XeF^+ fragment); c.f. Section 13-6 for a discussion of 6-electron 5-centre bonding. An "increased-valence" structure with a 6-electron 5-centre bonding unit may be constructed by writing down the standard Lewis structure (39), and then delocalizing each of the non-bonding 2p_σ-electrons on the bridging F^- into the two adjacent Xe-F bonding orbitals¹⁷. We thereby obtain "increased-valence" structure (40), for which all Xe-F bonds should be longer than single bonds. The terminal bonds are fractional electron-pair bonds, and the central bonds each involve one bonding electron. The shorter lengths for the terminal bonds imply that their bond-numbers are larger than the bond-orders for the central bonds. It should be noted that because the bridging bond-angle is 150°, the electron distributions of both (37) and (40) are required to describe the electronic structure of Xe_2F_3^+ .

structure (43) via (16) and (42) for ClF_3 and ClF_4 . Starting with $\text{ClF}_3 + \text{F}$, a Pauling "3-electron bond" is developed in (42) for ClF_4 by delocalizing a non-bonding $3p$ electron into a bonding Cl-F orbital (c.f. $\text{ClF} + \text{F} \rightarrow \text{ClF}_2$ in Section 4-8). The resulting antibonding Cl-F σ^* electron is then spin-paired with the unpaired electron of a fifth fluorine atom to afford (43) for ClF_5 .

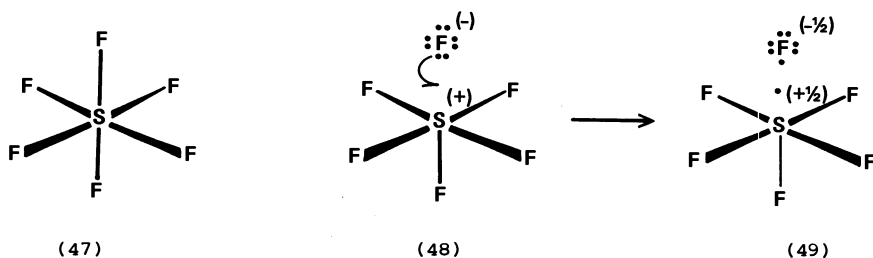


We may similarly proceed to SF_6 via SF_4 and SF_5 . When a fifth fluorine atom bonds to SF_4 , it is able to utilize the equatorial lone-pair on the sulphur atom of (19) for SF_4 , as in (44), to form "increased-valence" structure (45) for SF_5 . In (45), the newly-formed equatorial S-F bond involves a Pauling "3-electron bond". If the $F_{\text{ax}} - \text{S} - F_{\text{eq}}$ bond angles are assumed here to be 90° , then the sulphur atom is sp^2 hybridized for the equatorial σ -bonds.



To use the unpaired electron of the equatorial bond for SF_5 to bind to a sixth fluorine atom, a hybridization change must occur in order that good overlap can exist between the two odd-electron orbitals. Best overlap is obtained when the $2p\sigma_{\text{F}}$, $3p\sigma_{\text{S}}$ and $2p\sigma_{\text{F}}$ orbitals are colinear. This is achieved when the equatorial bond-angles are 90° , to give the two equatorial electron-pair bonds sp hybridization for the sulphur atom. The valence-bond structure (46) for SF_6 has "increased-valence" representations for its 4-electron 3-centre bonding units. In order that the six S-F bonds have equivalent lengths, $(1.561 \text{ \AA})^{19}$ (46) must participate in resonance with other equivalent structures that differ in the locations of the 4-electron 3-centre bonding units and the electron-pair bonds, i.e. the sulphur $3s$ orbital can participate in the axial as well as the equatorial bonding.

The S-F bond-lengths of 1.561 Å for SF₆ are only slightly longer than the estimate of 1.54 Å for an S-F single bond (Section 11-5), and if this lengthening is significant, the development of two 4-electron 3-centre bonding units does not account well for this observation. If the difference is not significant, then it is necessary to assume that the sulphur atom expands its valence-shell to form six electron-pair σ-bonds, as in the Lewis structure (47). Maclagan²⁰ has discussed the bonding for SF₆, and has concluded that ionic Lewis structures such as (48), which also involve an expansion of the sulphur valence shell, should have larger weights than has (47). It may be noted however, that each of these ionic structures may be stabilized by delocalizing a non-bonding 2p_z-electron from each of the F⁻ into a bonding S-F σ-orbital to generate "increased-valence" structure (49), which is more stable than (48). "Increased-valence" structure (49) has an expanded valence shell, and a 4-electron 3-centre bonding unit with a Pauling "3-electron bond" as a component. The bond-lengths for SF₆ suggest that resonance between structures of type (49), together with some contribution from (47), provides a more suitable representation of the electronic structure than does resonance between "increased-valence" structures of type (46). In (47) and (49), the sulphur hybridizations are sp³d² and sp³d, respectively, with the e_g-type 3d orbitals involved.

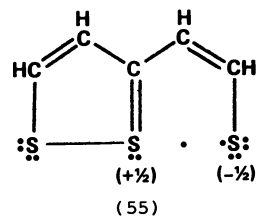
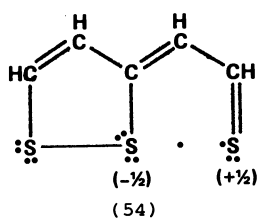
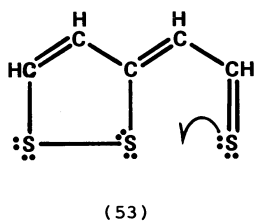
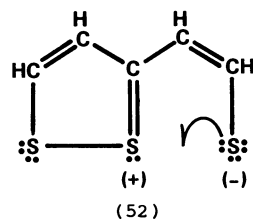
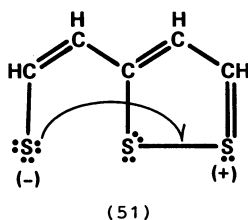
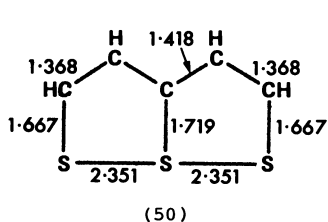


Recent studies²¹ of the geometry for SF₅Cl give S-F_{ax} = 1.571 Å, S-Cl_{ax} = 2.055 Å and S-F_{eq} = 1.570 Å, which are similar to the earlier reported lengths of 1.588, 2.047 and 1.566 Å. Resonance between valence-bond structures similar to (47) and (49) accounts for the observed bond lengthenings relative to the estimates of 1.54 and 2.01 Å for S-F and S-Cl single bonds.

19-5 THIO THIOPHTHENES

Bond lengths²² for thiothiophene are reported in (50). The S-S bonds for this molecule and many of its derivatives^{22,23} are appreciably longer than the standard single-bond length of 2.06 Å. (For the derivatives, the two S-S bond-lengths are usually unequal, due presumably to the nature of the substituent²³).

For thiothiophene, numerous standard Lewis structures such as (51) - (53) + mirror images may be written, and used to construct the (more-stable) "increased-valence" structures (54) and (55) by means of the delocalizations indicated. Resonance between either set of structures accounts for the lengthening of the S-S bonds, but additional considerations are required to rationalize the observed variations in the C-S and C-C bond lengths.



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CHAPTER 20

INTERMOLECULAR DONOR-ACCEPTOR COMPLEXES

20-1 QUANTUM MECHANICAL DESCRIPTION OF DONOR-ACCEPTOR COMPLEXES

Mulliken¹⁻³ has provided a quantum mechanical description of molecular complexes that are formed by reaction between an electron-donor (D) and an electron acceptor (A). The wave-function for the normal or ground-state of the complex may be expressed¹⁻³ approximately according to Eqn. (1).

$$\Psi_N \approx a\Psi_0(D,A) + b\Psi_1(D^+ \text{---} A^-) \quad (1)$$

Here we have retained only the first two terms of a more general expression for Ψ_N which has been described by Mulliken. The (D,A) and (D⁺---A⁻) are called "no-bond", and "dative" or "charge-transfer" structures, respectively. The designation of "no-bond" structure for (D,A) refers to the absence of covalent bonding between the donor and the acceptor.

In this Chapter, aspects of the electronic structures of complexes formed from n-type electron donors and sacrificial electron acceptors will be examined. An n-type donor donates an electron from essentially a lone-pair atomic orbital on a key atom, and a sacrificial acceptor accepts an electron into an antibonding molecular orbital¹. (Mulliken³ has also designated n-type donors as increvalent donors). Therefore, for this type of complex, D has a lone-pair of electrons and A has a vacant antibonding orbital in Eqn. (1). We shall assume here that the antibonding orbital of A extends over two adjacent atomic centres, and that the corresponding bonding molecular orbital of A is doubly occupied.

Using our discussion above, and that of Chapter 14, we may deduce that the dative structure D⁺---A⁻ of Eqn. (1) (which arises from the transfer of an electron from a lone-pair atomic orbital on D into a vacant antibonding of A) corresponds to an "increased-valence" structure. We shall now describe two examples which illustrate this type of bonding scheme. In Section 20-4, we shall examine an alternative procedure that may be used to describe such complexes.

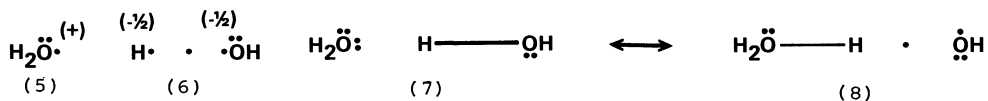
20-2 COMPLEXING OF TRIMETHYLAMINE WITH MOLECULAR IODINE

Trimethylamine (Me₃N) can form a crystalline complex with I₂. The N-I and I-I bond-lengths have been measured⁴, and they are shown in (1). The I-I length of 2.83 Å is longer than the 2.67 Å for free I₂, and the N-I length of 2.27 Å is longer than

We shall assume here that the two H₂O molecules of the water dimer form a charge-transfer complex, and describe the intermolecular bonding by means of Eqn. (1). To do this, we require one molecule to be the electron donor, and the other to be the electron acceptor. Thus, we have D = H₂O, A = H₂O, D⁺ = H₂O⁺ and A⁻ = H₂O⁻, and write the wave function for the complex as Eqn. (3).

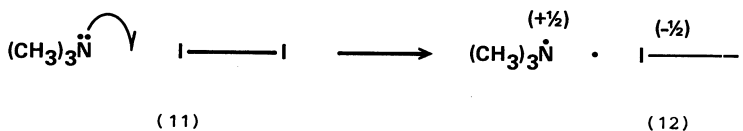
$$\psi_N \approx a\psi_0(\text{H}_2\text{O}, \text{H}_2\text{O}) + b\psi_1(\text{H}_2\text{O}^+ \text{---} \text{H}_2\text{O}^-) \quad (3)$$

To form H₂O⁻, we have transferred a non-bonding electron from the donor H₂O molecule into a vacant antibonding O-H orbital of the acceptor H₂O molecule, to generate the Pauling "3-electron bond" structure (6). By spin-pairing its unpaired electron with the unpaired electron of (5) for H₂O⁺, we obtain the "increased-valence" structure (8) for the dative structure H₂O⁺—H₂O⁻. The (H₂O)₂ complex may then be described by means of the resonance of (7) ↔ (8). It may be noted that the dipole-dipole theory of hydrogen bonding is based on dipolar attractions that may exist between the two H₂O molecules of the "no-bond" structure (7).

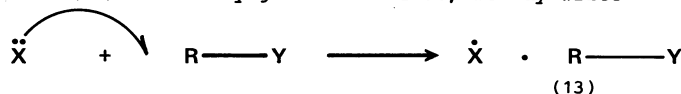


20-4 REFORMULATION OF CHARGE-TRANSFER THEORY⁸

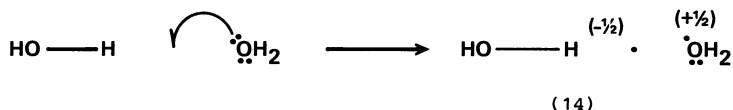
Mulliken³ has shown that the dative structure (D⁺—A⁻) = Me₃N⁺—I₂⁻ for the Me₃N...I₂ complex summarizes resonance between the standard and "long-bond" Lewis structures (9) and (10), i.e. "increased-valence" structure (3) summarizes resonance between these two structures, each of which has a Heitler-London type wave-function for the electron-pair bond. Resonance between the standard Lewis structure (2) (with a Heitler-London type wave-function for the I-I bond) and the "long-bond" structure (10) is equivalent to the use of "increased-valence" structure (12). The latter structure may be generated by delocalizing a nitrogen non-bonding electron of (2) into a bonding N-I orbital, as is shown in (11). Of the two "increased-valence" structures (3) and (12), the formal charges suggest that (12) should be the more important for the ground-state of the complex. If this is assumed, we are able to deduce the properties of the complex by examination of (12) alone. This "increased-valence" structure indicates immediately that both the N-I and I-I bonds are longer than single bonds. In order to deduce this result from the theory of Section 20-2, it was necessary to invoke resonance between the "no-bond" and dative valence-bond structures (2) and (3). A more economical representation of the electronic structure is therefore obtained by delocalizing a non-bonding electron of the donor into a bonding orbital between the donor and the acceptor, rather than into an antibonding orbital of the acceptor. By using "increased-valence" structure (12) to represent (approximately) the electronic structure of the complex, we may describe the intermolecular bond as a 1-electron bond.



If $\ddot{\text{X}}$ and R---Y are the generalized electron donor and electron acceptor, then we may represent the formation of the complex $\text{X}\cdots\text{RY}$ as follows. As X approaches RY so that the X and R atomic orbitals (x and r) overlap, one of the non-bonding electrons of X delocalizes into the two-centre bond-orbital $\psi_{\text{XR}} = x + \lambda r$ (with $\lambda > 0$) which is constructed from these atomic orbitals. The "increased-valence" structure (13) is thereby generated. Thus, we may write



For the hydrogen bonding interaction between two water molecules we may write



to obtain a 1-electron bond as the intermolecular hydrogen bond, and reducing the bond-number for the adjacent H---O bond below the value that pertains for a free H_2O molecule.

In the theory of Sections 20-1 to 20-3, the electron donor ($\ddot{\text{X}}$) and the electron acceptor (R---Y) were designated as *increvalent* and *sacrificial* donors and acceptors respectively. Here, in (12), (13) and (14), donors and acceptors are both increvalent species.

For (12) and (14), we show the relevant atomic orbital overlaps in Figure 20-1.

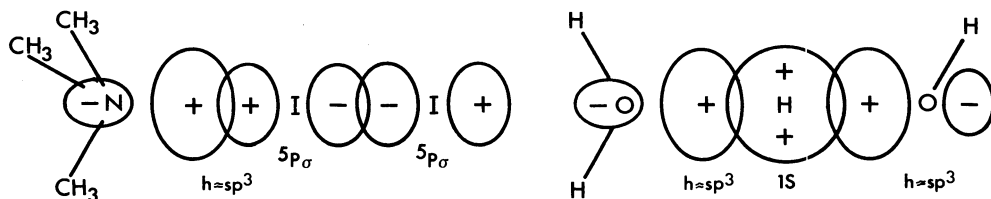


Figure 20-1 Atomic orbital overlaps of $\text{Me}_3\text{N} + \text{I}_2$ and $\text{H}_2\text{O} + \text{H}_2\text{O}$.

An interesting result is obtained if 2-centre bond-orbitals are used to accommodate all of the bonding electrons in the "increased-valence" structure (13) and the standard Lewis structure (15). We shall designate these bond orbitals as $\psi_{xr} = x + \lambda r$ and $\psi_{ry} = r + ky$, with the bond parameters λ and k both > 0 . The $S = 0$ wave-functions for (13) and (15) are then given by Eqs. (4) and (5) (c.f. Eqn. (7) of Chapter 15). The wave-function for the dative structure $\overset{+}{X} - \overset{-}{RY}$, for which one non-bonding electron of (15) has been transferred into the antibonding RY orbital $\psi_{ry}^* = k^* r - y$, is given by Eqn. (6). It is then possible to deduce^{8c} that the Mulliken wave-function for the complex, namely Eqn. (1), is equivalent to the wave-function of Eqn. (4) for the "increased-valence" structure (13). Therefore, the Mulliken wave-function of Eqn. (1) implies, but conceals an (approximate) description of the intermolecular bond as a 1-electron bond.



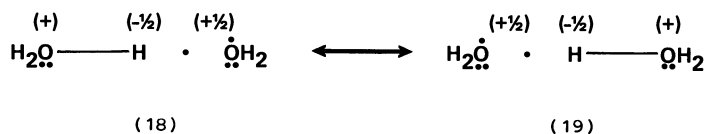
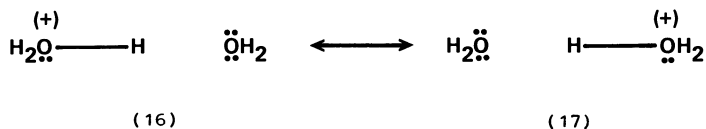
$$\psi(\overset{\cdot}{X} \cdot R \text{ --- } Y) = |x^\alpha \psi_{xr}^\beta \psi_{ry}^\alpha \psi_{ry}^\beta| + |\psi_{xr}^\alpha x^\beta \psi_{ry}^\alpha \psi_{ry}^\beta| \quad (4)$$

$$\psi(\overset{\cdot\cdot}{X} \text{ --- } R \text{ --- } Y) = |x^\alpha x^\beta \psi_{ry}^\alpha \psi_{ry}^\beta| \quad (5)$$

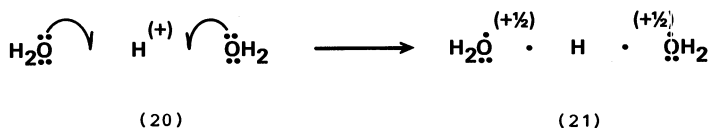
$$\psi(X \text{ --- } R \cdot \overset{\cdot}{Y}) = |x^\alpha \psi_{ry}^* \psi_{ry}^\alpha \psi_{ry}^\beta| + |\psi_{ry}^* x^\beta \psi_{ry}^\alpha \psi_{ry}^\beta| \quad (6)$$

20-5 H₅O₂⁺ AND HF₂⁻

The isoelectronic ions H₅O₂⁺ and HF₂⁻ with 16 valence-shell electrons, are examples of systems that have strong hydrogen bonds⁹. In Fig. 2-4, we have displayed the set of hydrogen 1s and fluorine 2p σ -atomic orbitals of HF₂⁻ that may be utilized for 4-electron 3-centre bonding. For H₅O₂⁺, oxygen hybrid orbitals replace the fluorine 2p σ -orbitals, and the standard Lewis structures are those of (16) and (17).

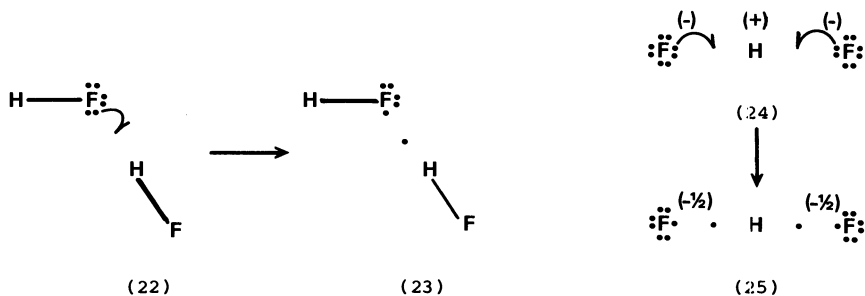


As well as using the above structures, we may also use^{8b} the Linnett non-paired spatial orbital structure (21) to represent the electronic structure of $H_5O_2^+$. By hydrogen-bonding the oxygen atoms of two H_2O molecules to a proton, we may generate (21) from (20). As each H_2O molecule approaches the proton, one oxygen lone-pair electron delocalizes into an intermolecular O-H bonding orbital. In (21), the two H_2O molecules are hydrogen bonded to the proton by means of 1-electron bonds.



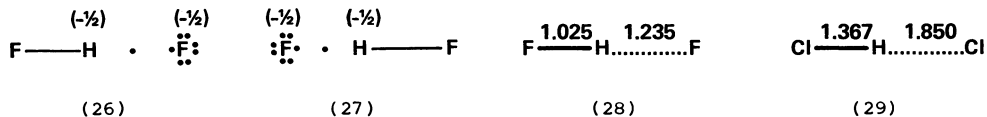
We may provide a simple explanation as to why the bridging O-H bond-lengths of 1.23 Å for $H_5O_2^+$ are appreciably shorter⁹ than the 1.808 Å for the hydrogen-bond of $(D_2O)_2$. Relative to an oxygen atom, the H^+ of (20) is more electronegative than is a hydrogen atom in (7). The extra electronegativity of H^+ should induce more delocalization of an oxygen lone-pair electron in (21), to generate an increase in the bond-order for each one-electron bond of $H_5O_2^+$.

For $(HF)_2$ and HF_2^- , the 1-electron hydrogen bonds of (23) and (25) are formed by the delocalizations of (22) and (24). Using electronegativity considerations, as we have done in the previous paragraph, we can explain why the H-F bond-lengths of 1.13 Å for HF_2^- are shorter⁹ than the length of 1.55 Å for the hydrogen-bond of $(HF)_2$.



For HF_2^- , the "increased-valence" structures are (26) and (27) (cf. (18) and (19) for $H_5O_2^+$), with both structures having equal weights and equal H-F bond-lengths when the HF_2^- is located in a symmetrical environment. Williams and Schneemeyer¹⁰ have reported the geometries of (28) and (29) for HF_2^- and HCl_2^- in non-symmetrical environments. Each of the bond-lengths is longer than the single-bond lengths of 0.92 and 1.27 Å for gaseous HF and HCl. "Increased-valence" structures of type (26)

alone (with unequal bond-lengths) are compatible with the observed bond-lengths for both anions, although of course (26) will be stabilized by resonance with (27). The latter structure will have the smaller weight.

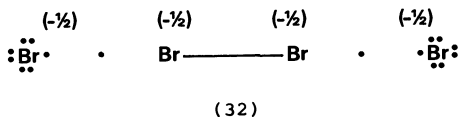
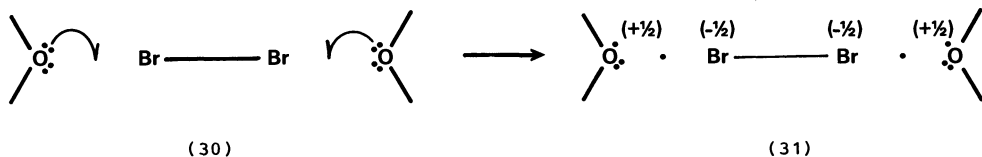


The anion HOHOH⁻ is isoelectronic with H₅O₂⁺ and HF₂⁻, and a suitable valence-bond structure for it is similar to (25), with OH replacing F, i.e. $\overset{(-\frac{1}{2})}{\text{HO}} \cdot \text{H} \cdot \overset{(-\frac{1}{2})}{\text{OH}}$. The bridging O-H bonds of H₅O₂⁺ and HOHOH⁻ have been estimated to have similar lengths and strengths¹¹.

Firestone¹² has also used Linnett structures to describe the electronic structures of symmetrical hydrogen-bond molecules.

20-6 2:1 DONOR-ACCEPTOR COMPLEXES

Two molecules of acetone or dioxan can interact with one molecule of Br₂ to form the intermolecular complexes Me₂CO...Br₂...OCMe₂ and C₅H₁₀O...Br₂...OC₅H₁₀. The reported Br-Br lengths⁴ of 2.28 and 2.31 Å are not sufficiently different from the length of 2.28 Å for free Br₂ to indicate much interaction of Br₂ with these solvents. The "increased-valence" structure (31), which we may generate from the Lewis structure (30) by delocalizing oxygen non-bonding electrons into bonding O-Br orbitals, will account for any lengthening of the Br-Br bond. A similar "increased-valence" structure, namely (32), is certainly compatible with the measured bond-lengths of Br₄²⁻. The terminal and central bond-lengths of 2.98 Å and 2.43 Å are appreciably longer than the 2.28 Å for free Br₂¹³.



For each of (31) and (32), there is an "increased-valence" representation for the 6-electron 4-centre bonding unit, and we remind the reader that its wavefunction corresponds to the covalent component of the delocalized molecular orbital configuration for the six electrons (Section 10-2). The relevant atomic orbitals for Br_4^{2-} are displayed in Fig. 2-6.

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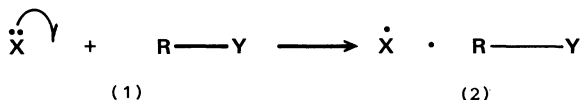
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CHAPTER 21

BASE-DISPLACEMENT REACTIONS AND ELECTRON CONDUCTION IN ALKALI METALS

21-1 INTRODUCTION

The donor-acceptor complexes of Chapter 20 were usually formed by reacting a neutral electron donor \ddot{X} with a neutral electron acceptor $R-Y$. We have suggested that it may be a good approximation to represent the formation of the complex as follows, in which we have delocalized a non-bonding electron from \ddot{X} into a vacant bonding X-R orbital.



The bonding X-R orbital becomes available when the atomic orbitals on \ddot{X} and R overlap. We shall now describe an "increased-valence" representation for the general base-displacement reaction



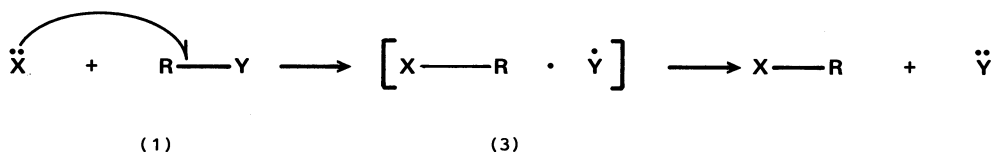
which involves the displacement of the base \ddot{Y} from a substrate RY by the base \ddot{X} . This reaction may occur when \ddot{X} is an anion and $R-Y$ is a cation, but it can also pertain when \ddot{X} is an anion and $R-Y$ is neutral, and when \ddot{X} is neutral and $R-Y$ is a cation. We shall discuss some examples of each of these three types of reactants.

The electronic reorganization that occurs in a displacement reaction is usually indicated in the following manner:



A pair of electrons is delocalized from an atomic orbital on \ddot{X} into the X-R bond region, and simultaneously the two electrons forming the $R-Y$ bond are transferred into an atomic orbital on \ddot{Y} . (This atomic orbital is the same orbital used by \ddot{Y} to form the bond of $R-Y$). The transition state is usually represented as $X \cdots R \cdots Y$, which shows the simultaneous making of the X-R bond and breaking of the R-Y bond. Since X, R and Y each contribute one atomic orbital for the bonding, the X-R and R-Y bond orbitals of this transition state cannot be orthogonal, and therefore the divalence of R is apparent, not real (cf. Chapter 16). Firestone¹ has also used the Linnett theory to formulate the transition state as $\dot{X} \cdot R \cdot \dot{Y}$.

An "increased-valence" formulation^{2,3} of the generalized base displacement reaction, which perhaps indicates more clearly how the bonds are formed and broken, involves the delocalization of one electron from \ddot{X} into the antibonding orbital of $R-Y$.



In the "increased-valence" structure (3), we have formed a fractional two-electron X-R bond and a one-electron R-Y bond. This structure is identical with the structure for Eqn. 20-6, and both have been formed in the same manner. We have pointed out in Chapter 20 that for a given (finite) X-R distance, structures (1) and (3) can participate in resonance². Therefore, for a base displacement reaction, (3) alone is not the transition state. However, (3) should often represent the main features of the transition state structure, and it does show clearly how one bond is made and how the other is simultaneously broken.

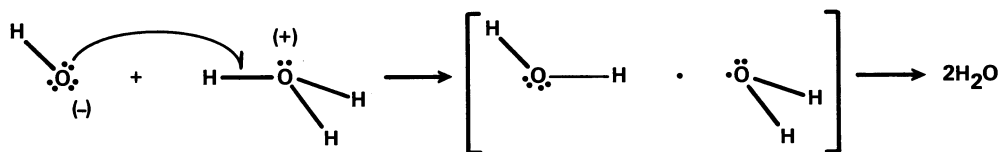
We may therefore distinguish two types of reactions between the electron donor and acceptor \ddot{X} and $R-Y$. Delocalization of an \ddot{X} electron into a bonding X-R orbital generates the complex (2), whereas delocalization of the electron into the antibonding R-Y orbital generates the complex (3) which is involved in the base displacement reaction. For nucleophilic addition of \ddot{X} to $R-Y$, the electronic structure of the product resembles² that of (3).

Very recently, Shaik⁴ has provided valence bond descriptions for a variety of organic reactions. Shaik's approach (without "increased-valence") to nucleophilic additions and substitutions in particular is essentially identical with that presented in this chapter, being based primarily on the Mulliken formulation of Eqn. (20-1) for donor-acceptor complexes. The acceptor orbital is an antibonding orbital in both treatments.

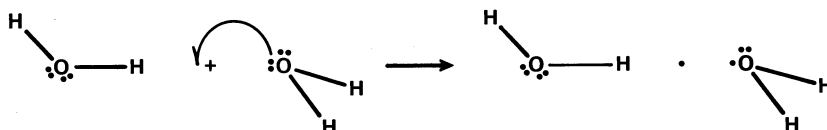
21-2 LOWRY-BRØNSTED ACID-BASE REACTIONS

In Lowry-Brønsted acid-base theory, an acid is a proton donor and a base is a proton acceptor. Since proton acceptors contribute a pair of electrons for bonding with the proton, a Lowry-Brønsted base is also a Lewis base, and therefore a Lowry-Brønsted acid is a special form of Lewis acid.

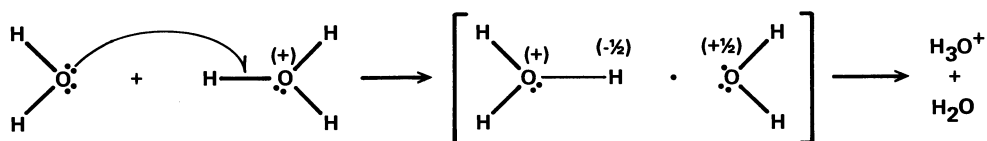
We may formulate the reaction between the Lowry-Brønsted acid and base H_3O^+ and OH^- as follows², in which a non-bonding electron of OH^- is transferred into an antibonding H-O molecular orbital of H_3O^+ .



In section 20-4, we have shown that the entity in parenthesis can represent the hydrogen-bonded complex $(\text{H}_2\text{O})_2$. There, we demonstrated that this complex may also be formed from two H_2O molecules by means of the reaction

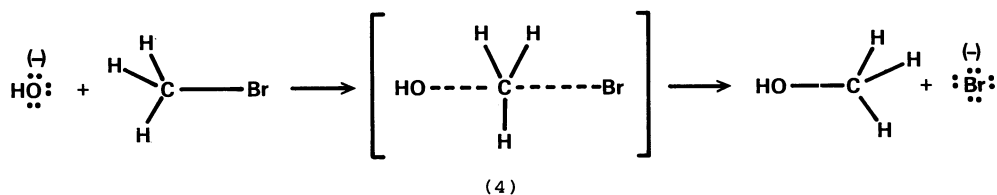


which involves the delocalization of an oxygen lone-pair electron of one molecule into a bonding O-H orbital between the two molecules. The ionization potential of H_2O is 12.6 eV, and this is large enough to make an antibonding O-H orbital of a second H_2O inaccessible at intermolecular distances which are either equal to or greater than the equilibrium value of 1.8 \AA (i.e. the energy of $\psi(\text{H}_2\text{O}, \text{H}_2\text{O}) < \psi(\text{H}_2\text{O}^+, \text{H}_2\text{O}^-)$ for this distance). On the other hand, an antibonding O-H orbital of H_3O^+ should be of lower energy, and the reaction $\text{H}_2\text{O} + \text{H}_3\text{O}^+ \rightarrow \text{H}_3\text{O}^+ + \text{H}_2\text{O}$ may proceed by transferring an electron from H_2O into an antibonding O-H orbital of H_3O^+ . We have thereby formulated the Grotthuss mechanism for proton transfer using "increased-valence" structures.



21-3 WALDEN INVERSION MECHANISM

In aqueous alkali, methyl bromide may be hydrolysed to methanol, with the OH^- displacing Br^- from its attachment to the carbon atom. The kinetics indicate that a bimolecular transition state is formed⁵, and that the methyl group undergoes inversion of configuration as the reaction proceeds. The electronic reorganization that is associated with this $\text{S}_{\text{N}}2$ reaction is usually represented in the following manner⁵:



In the transition state (4), the carbon atom is bonded to five atoms simultaneously. To account for this (apparent) quinquivalence, some workers have assumed that a carbon 3d orbital as well as the 2s and 2p orbitals can participate as a hybridization function in the bonding^{6,7}. But it is more probable that the carbon uses primarily only its 2s and 2p orbitals, and forms two bonds which are not orthogonal, as we have described for the general transition state of Section 21-1. For this latter bonding scheme, the atomic orbital overlaps are shown in Figure 21-1.

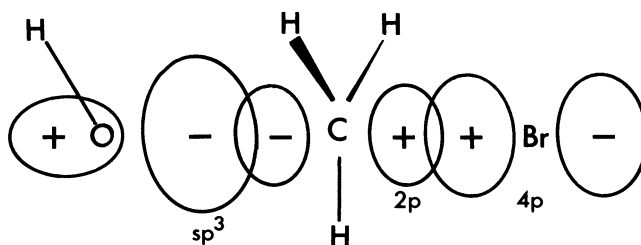
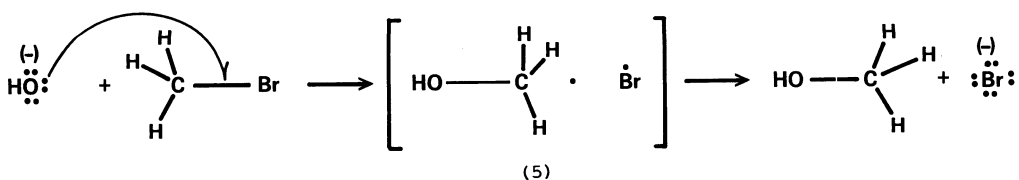


Figure 21-1 Atomic orbital overlaps for the transition state (4), omitting carbon 3d orbitals.

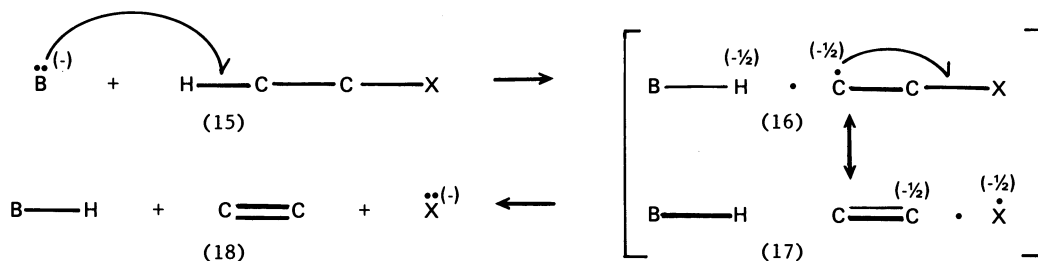
An "increased-valence" formulation² of the reaction indicates simply and clearly how the bonds are made and broken, and also provides an explanation for the inversion of configuration. The reaction can proceed by the transfer of an electron from OH^- into an antibonding O-Br orbital of CH_3Br ; this creates a fractional O-C electron-pair bond and a one-electron C-Br bond in the complex (5). As the reaction proceeds, the fractional O-C bond of (5) must become stronger than the one-electron C-Br bond. When this occurs, the O-C bond repels the three C-H bonds more strongly than does the C-Br bond, thereby leading to inversion of configuration.

For some recent molecular orbital studies of $\text{S}_{\text{N}}2$ reactions, see for example Ref. 8.



An "increased-valence" formulation of the electronic reorganization² involves the transfer of an electron from $\ddot{\text{B}}^{(-)}$ into the antibonding C-H σ^* orbital, i.e. (15) \rightarrow (16), and the transfer of an electron from a carbon atomic orbital of (16) into the antibonding C-X σ^* orbital, i.e. (16) \rightarrow (17). (For convenience of representation only, we have displayed the relevant atoms in a linear manner.) The wavefunction $\Psi = C_{15}\Psi_{15} + C_{16}\Psi_{16} + C_{17}\Psi_{17}$ may be used to describe the course of the reaction, with $C_{16} = C_{17} = 0$ initially and $C_{15} = C_{16} = 0$ at its conclusion when the structure (17) goes over to the products of (18). The electron of the C \cdot X bond occupies the bonding molecular orbital $\psi_{\text{CX}} = sp_{\text{C}}^n + kp_{\text{X}}$, with both n and $k \rightarrow \infty$ as $C_{17} \rightarrow 1$ near the conclusion of the reaction. The six mobile electrons of (16) and (17) form a 5-centre bonding unit (c.f. Section 13-6).

This approach may be contrasted with that presented very recently by Pross and Shaik¹³. Our treatment includes the "long bond" structures $\ddot{\text{B}} \cdots \ddot{\text{H}} \cdots \text{C}=\text{C}-\text{X}$ and $\text{B}-\text{H} \cdots \ddot{\text{C}}=\ddot{\text{C}} \cdots \text{X}$ that contribute to (16) and (17). For overlap reasons at least (see Appendix), we would consider them to be more important than is normally supposed.



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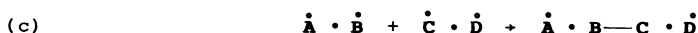
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CHAPTER 22

FREE-RADICAL AND SPIN-PAIRED DIRADICAL REACTIONS

22-1 TYPES OF FREE RADICAL REACTIONS

Free radicals, with odd numbers of electrons, must have at least one orbital (atomic or molecular) singly occupied. On occasions in the previous chapters, we have met with the following types of reactions between univalent free radicals:



For (a), the A and B are two species (atomic or molecular), each of which has an unpaired electron localized essentially in an atomic orbital. If the atomic orbitals overlap, then the unpaired electrons may be spin-paired (or antiferromagnetically coupled) to form a covalent bond if the electronegativities of A and B are not too dissimilar. Examples of this type of reaction are $H + H + H_2$, and $CH_3 + CH_3 + C_2H_6$.

Each of the \dot{Y} and $\dot{A} \cdot \dot{B}$ reactants of (b) has one unpaired electron; Y is an atomic or molecular species with its unpaired electron occupying an atomic orbital. The molecular species $\dot{A} \cdot \dot{B}$ has a Pauling "3-electron bond". In Section 3-6, we have found that the Pauling "3-electron bond" may be described either as two bonding electrons + one antibonding electron, or as two "non-bonding" electrons + one bonding electron. The bonding and antibonding electrons occupy molecular orbitals, and the non-bonding electrons occupy atomic orbitals. In the reactions of (b), the unpaired electron of Y spin-pairs with the unpaired antibonding electron of AB to generate the "increased-valence" structure $Y-A \cdot \dot{B}$. We point out again that since the Y-B bonding in this structure is very weak, we have for convenience of representation omitted it. Some examples of this type of free radical reaction, which we have discussed in Chapter 11, are $F + NO + FNO$ and $F + O_2 + FO_2$.

We have also discussed numerous examples of reactions of type (c), namely reactions in which both reactants have a Pauling "3-electron bond". Representative examples are $2NO + N_2O_2$, $NO + NO_2 + N_2O_3$, $2NO_2 + N_2O_4$ and $2ClO + Cl_2O_2$.

There exists a fourth type of free radical reaction, in which one species has an unpaired electron occupying an atomic orbital, and the other species has an electron-pair bond. Such a reaction is customarily represented as (d)

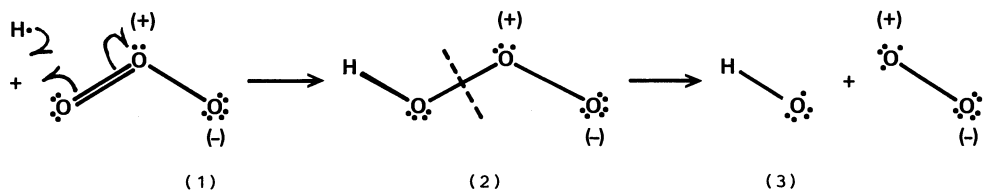


We shall now examine other aspects of the reactions (b)-(d). In particular, we shall show how the products of these reactions may themselves sometimes involve electronic rearrangements and decompositions.

22-2 R + O₃ → RO + O₂, WITH R = H, Cl, AND NO

Reactions between O₃ and univalent radicals - in particular, chlorine atoms and NO - are of ecological concern, because it has been suggested that they might lead to some destruction of the protective ozone layer in the stratosphere^{1,2}. These reactions generate univalent free radicals, for example ClO and NO₂^{1,2}. To examine how electronic reorganization might proceed for these types of reactions, we shall initially examine mechanisms for the reaction of ozone with hydrogen atoms, using both standard Lewis and "increased-valence" structures.

For O₃ the standard Lewis structures are of type (1), with no unpaired-electrons. If we use this type of valence bond structure to represent the electronic structure, it is necessary to formulate the reaction of O₃ with a hydrogen atom according to mechanism (d) of Section 22-1, as follows:



The electronic reorganization displayed in (1)-(3) does not make clear why the HO-O bond of (2) should break, and retains formal charge separation on the two oxygen atoms of (3).

An "increased-valence" mechanism for the reaction does not have these disadvantages³. The "increased-valence" structure for O₃, namely (4) (Section 11-6) may be generated (Fig. 12-1) from the standard Lewis structure (1) by delocalizing two lone-pair π - and $\bar{\pi}$ - electrons from the terminal O⁻ into two bonding O⁻-O⁺ orbitals. In the reaction steps of (4)-(8), the atomic formal charges for all of the valence-bond structures can remain unaltered at each stage. The mechanism involves the following electronic reorganization:

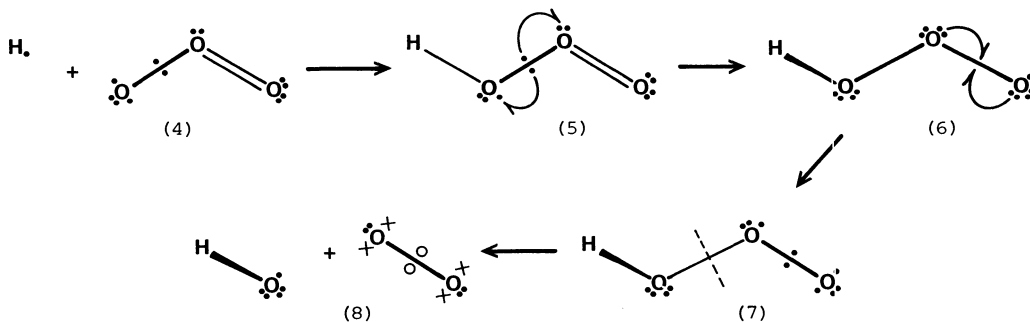
- (a) A hydrogen atom forms a weak O-H bond with O₃ by spin-pairing some of its electron charge with the corresponding "unpaired-electron" charge[†] that is

[†] (see footnote on next page)

present on a terminal oxygen atom of "increased-valence" structure (4). "Increased-valence" structure (5) is thereby generated for HO_3 .

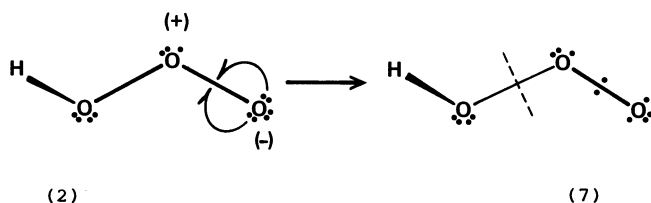
- (b) The two electrons that form the 1-electron π -bonds of (5) may be transferred from the O-O bond region into the partially occupied oxygen atomic orbitals of (5). The 1-electron transfers that are indicated in (5) generate the valence-bond structure (6) with a strengthened O-H single bond (relative to (5)) and the odd-electron located on the terminal oxygen atom. In (6), we have obtained a hydrogen-peroxide type structure for the H-O-O linkage.
- (c) "Increased-valence" may be restored by delocalizing oxygen lone-pair electrons into the vacant O-O bonding π -orbitals, as shown in (6). The resulting "increased-valence" structure (7) has a weakened O-O bond between the H-O and O-O linkages.
- (d) The weak O-O bond of (7) can now break to release the HO and O_2 products.

Although the reaction proceeds by means of a concerted mechanism, it is convenient to display a series of steps in the valence-bond representation of the electronic reorganization.



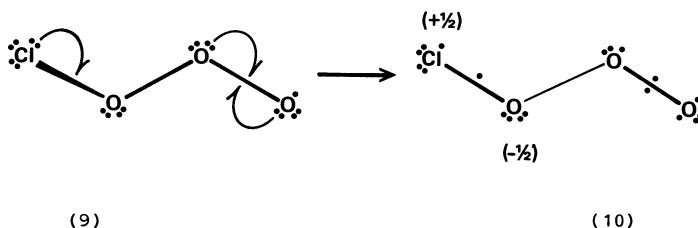
It may be noted that the HO_3 valence-bond structure (2) may also be used to generate "increased-valence" structure (7), i.e. we may write

(from previous page) In (5), an "increased-valence" 5-electron 4-centre bonding unit is present, namely $\text{H}-\text{O} \cdot \text{O}-\text{O}$. This structure summarizes resonance between the Lewis structures $\text{H}-\text{O} \overset{\cdot}{\text{O}} \overset{\cdot}{\text{O}}$, $\overset{\cdot}{\text{H}} \overset{\cdot}{\text{O}} \text{O}-\text{O}$, $\overset{\cdot}{\text{H}} \overset{\cdot}{\text{O}} \overset{\cdot}{\text{O}} \text{O}$, $\overset{\cdot}{\text{H}} \overset{\cdot}{\text{O}} \overset{\cdot}{\text{O}} \overset{\cdot}{\text{O}}$ and $\overset{\cdot}{\text{H}} \overset{\cdot}{\text{O}} \overset{\cdot}{\text{O}} \overset{\cdot}{\text{O}}$ if a valid $S = 1/2$ wave-function is constructed according to Eqn. (15-9). These structures show that much of the remainder of the hydrogen odd-electron charge is used to form "long" H-O bonds between non-adjacent atoms.

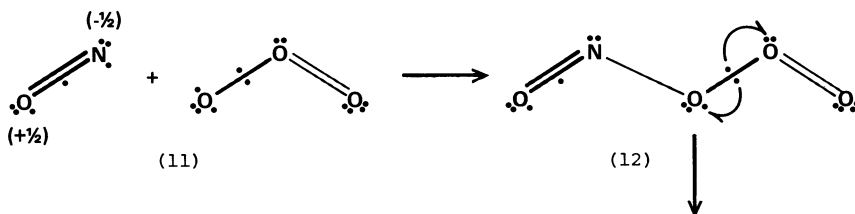


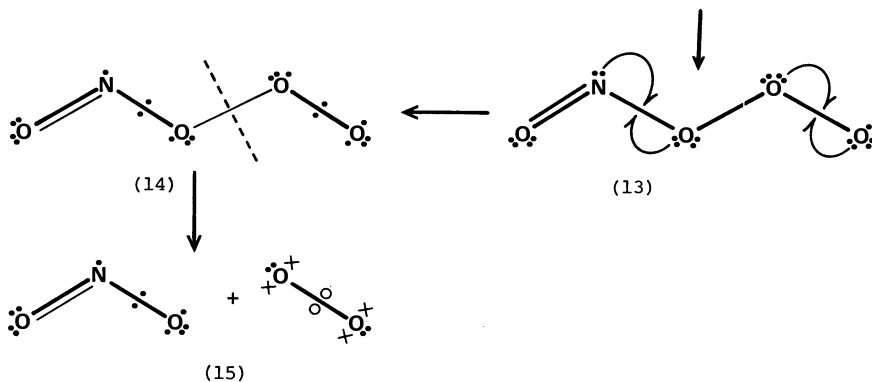
The valence-bond structure for the O_2 of (8) corresponds to that which is appropriate for the $S = 1$ ground-state. It may be deduced³ that the O_2 ground-state must be generated whenever the decomposition reaction $RO_2 \rightarrow R + O_2$ can occur. No evidence has been obtained⁴ for the formation of an O_2 excited state for the reaction $X + O_3 \rightarrow XO + O_2$ when $X = H$ or NO . It has therefore been concluded that the $^3\Sigma_g^-$ ground-state is generated⁴, in accordance with the earlier deduction³.

The reaction $Cl + O_3 \rightarrow ClO + O_2$ involves a similar type of electronic reorganization, but with the possibility for an additional electron delocalization step to occur at stage (6), namely that of (9). When the O-O bond of "increased-valence" structure (10) breaks, the ClO is generated with a Pauling "3-electron bond".



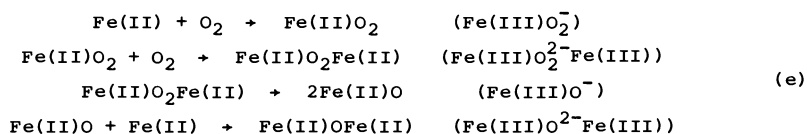
The "increased-valence" formulation of the reaction steps for $NO + O_3 \rightarrow NO_2 + O_2$ is that of (11)-(15). The delocalization of a nitrogen lone-pair electron of (13) into an N-O bonding orbital has two effects. It assists with the weakening of the O-O bond, and generates a fractional unpaired-electron charge on the nitrogen atom. E.s.r. measurements⁵ show that such a charge is present in the free NO_2 molecule. The NO_2 "increased-valence" structure of (15) has been described previously in Section 11-8†





22-3 REACTIONS OF O₂ WITH Fe(II) PORPHYRIN COMPLEXES

In Section 18-4, we have provided an "increased-valence" description of the bonding of O₂ to the Fe(II) porphyrin complex, haemoglobin. For each Fe(II)O₂ linkage of the ground-state of oxyhaemoglobin, the O₂ ground-state is bonded to the intermediate-spin Fe(II) in the "increased-valence" structure. A number of other Fe(II) porphyrin complexes are irreversibly oxidized by O₂ to form oxo-bridged dimers⁶. One reaction scheme that has been proposed⁶ is that of (e).



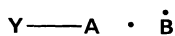
(Alternative formulations for the oxidation states of the products of each reaction step are given in parentheses.) An electronic mechanism⁷ for these reaction steps[†] is displayed in Fig. 22-1. Ground-state O₂ and intermediate-spin Fe(II) are involved as reactants at the appropriate stages of the reaction scheme. In "increased-valence" structure (a), electrons are transferred either from O-O bonding molecular orbitals into oxygen atomic orbitals, or from Fe(II) and oxygen atomic orbitals into Fe(II)-O bonding molecular orbitals. (Overlap considerations require that hybridization changes must occur at the oxygen atoms in order that the delocalization of the oxygen non-bonding electrons into the Fe(II)-O molecular orbitals may proceed.) Because the intermediate-spin Fe(II) and Fe(II)O₂ reactants of the second step have $S = 1$ and $S = 0$ spin quantum numbers respectively, the Fe(II)O₂Fe(II) species that is formed must have an $S = 1$ spin-state in order that spin be conserved. On decomposition of the Fe(II)O₂Fe(II) complex, the Fe(II)O radicals are predicted to be generated with $S = 1$ spin-states⁷. However, an $S = 0$ spin-state is appropriate for the Fe(II)OFe(II) oxo-bridged dimer, as it is for the

[†] A more recent mechanism⁸ involves additional steps that include Fe(II)O + Fe(II)O₂Fe(II) + Fe(II)OFe(II) + Fe(II)O₂, Fe(II)O₂ + Fe(II) + O₂, and Fe(II)O + Fe(II)O₂ + Fe(II)OFe(II) + O₂.

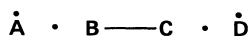
Whether or not (7) is formed directly or bypassed via (5) and (6) + (8) and (9) has yet to be ascertained. The essential point is that in the valence-bond representation for the mechanism, easily-visualized electronic reorganizations lead to the conversion of reactants into products, and these are achieved by utilizing the Pauling "3-electron bond" structure of (1) for the O_2 ground state.

From consideration of the reactions of Sections 22-2 and 22-3, it should be fairly obvious that many diamagnetic molecules that do not have a net number of unpaired electrons may react as though they were free radicals. In fact, this is theoretically possible whenever we may construct an "increased-valence" structure for a molecule, with one or more "increased-valence" bonding units of the types (16) and (17). In these structures, fractional unpaired electron charges on the B atom of (16) and the A and D atoms of (17) can be made available for weak covalent bonding with the fractional unpaired-electron charge of another entity.

In the following section, we shall discuss some radical-type reactions between a pair of molecules, neither of which is a free radical with an odd number of electrons.



(16)



(17)

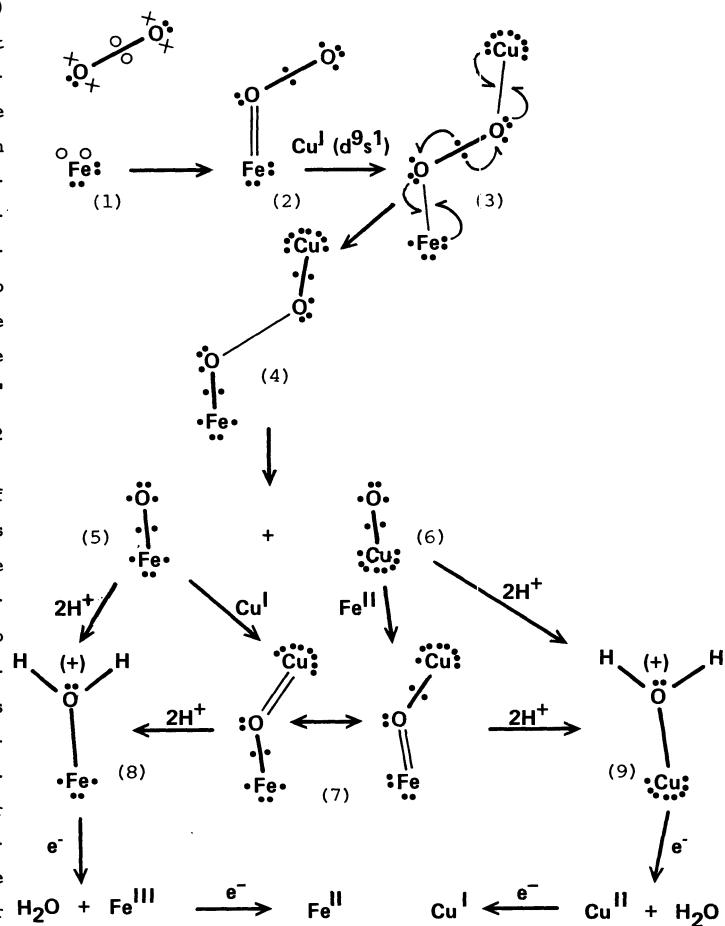
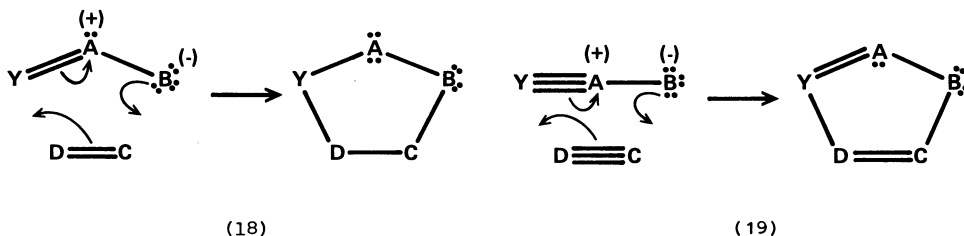


Figure 22-2 Cytochrome c oxidase catalysis of $4H^+ + 4e^- + O_2 \rightarrow 2H_2O$.

22-4 "1,3 DIPOLAR" (OR "ZWITTERIONIC DIRADICAL HYBRID") CYCLOADDITION REACTIONS

A large class of organic reactions that lead to the formation of five-membered heterocyclic molecules, have been designated as "1,3 dipolar" cycloaddition reactions¹⁰. Huisgen¹⁰ has defined the "1,3 dipole" to be 'a species which is represented by zwitterionic resonance structures (standard Lewis octet structures in this book) and which undergoes 1,3 cycloadditions to a multiple bond system, the "dipolarophile", as in (18) and (19).



In Ref. 10c, "1,3 dipoles" with C, N and O centres are classified, with their zwitterionic structures displayed. "Increased-valence" structures for many of them are displayed in Ref. 11.

The addition of diazomethane to methyl acrylate to form 1-pyrazoline is an example of a "1,3 dipolar" cycloaddition reaction¹⁰. For CH_2N_2 , the zwitterionic octet structures are (20) and (21); these, together with the sextet structures (22) and (23) are usually assumed to be the important valence-bond structures for the construction of the electronic mechanism for cycloaddition¹⁰. For the latter two structures, the terminal atoms are both nucleophilic (-) and electrophilic (+), and it is these properties of the "1,3 dipole" that are often assumed to be implicated for the electronic mechanism of the cycloaddition. As CH_2N_2 approaches the methyl acrylate, one set of π -electron atomic orbitals of CH_2N_2 overlaps with the π -orbitals of methyl acrylate (see Fig. 22-3), and the electronic reorganization is assumed to proceed according to (24)-(25). A concerted mechanism is concomitant with this valence-bond description, with the new C-C and C-N bonds being formed synchronously.

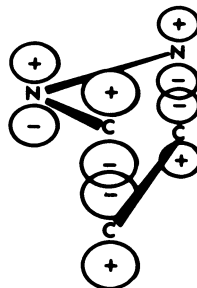
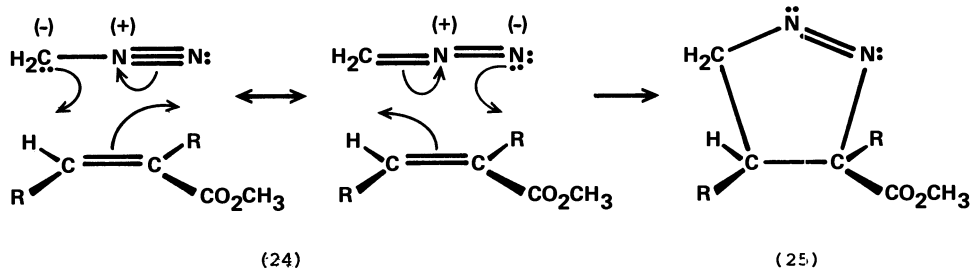
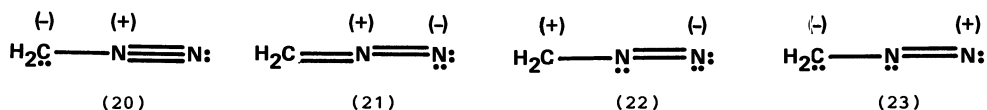
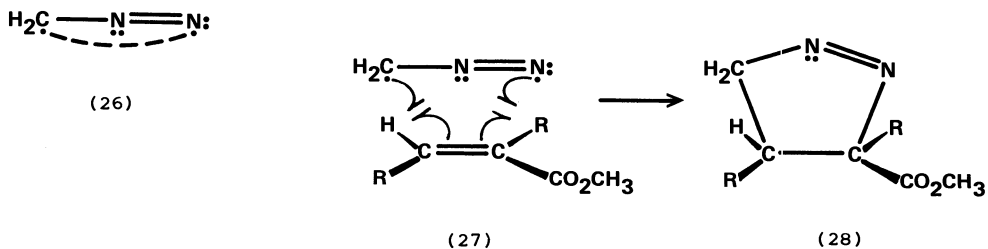


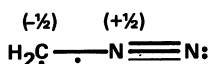
Figure 22-3 Overlapping π -electron atomic orbitals for "1,3 dipolar" cycloaddition reaction.



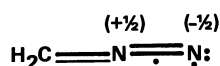
Although zwitterionic octet structures are now used^{10b,c} to represent the reaction mechanism, the assumption that the electrophilic nature of either terminal atom of the 1,3-dipole is also utilized implies that the sextet valence-bond structures must become important as the reaction proceeds. However, for the ground-state of free CH_2N_2 , the electroneutrality principle suggests that these structures should not have large weights. Each of them has one fewer covalent bonds than has either of the zwitterionic structures, and a greater spatial separation of the + and - formal charges. The absence of formal charges in the "long-bond" structure (26) would suggest that it should have a rather larger weight than has either of (22) and (23). Bond-eigenfunction coefficients of 0.31, 0.23, 0.05, 0.10 and 0.38 for the valence-bond structures (20)-(23) and (26) have been calculated by Roso¹². Hiberty and Le-Forestier¹³ have calculated weights of 0.16, 0.41, 0.01, 0.04 and 0.28 for these structures. Both sets of calculations support the expectation that (26) should be a rather more important valence-bond structure for the ground-state than are the sextet structures. If it is assumed that this is also the case as the reaction with methyl acrylate proceeds, then we may formulate the cycloaddition mechanism according to^{12,14} (27)-(28).



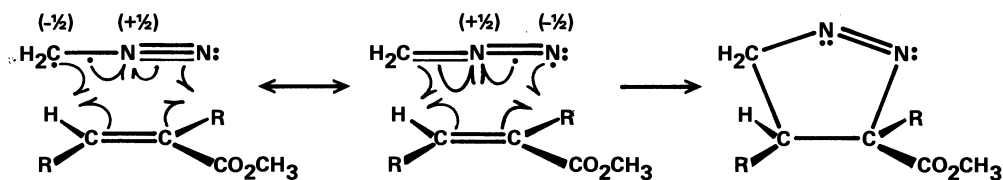
Of course, (26) is only one of the important valence-bond structures, and a better description of the electronic structure of CH_2N_2 is obtained by using ^{11,12} the "increased-valence" structures (29) and (30), which summarize resonance between the zwitterionic structures (20) and (21), and the "long-bond" structure (26) if a Heitler-London type formulation of wave-functions for electron-pair bonds is used. Thus, by using (29) and (30), we may construct the concerted mechanism of cycloaddition according to (31), and redesignate "1,3 dipolar" molecules as "zwitterionic diradical hybrids"^{11,12,14}.



(29)



(30)

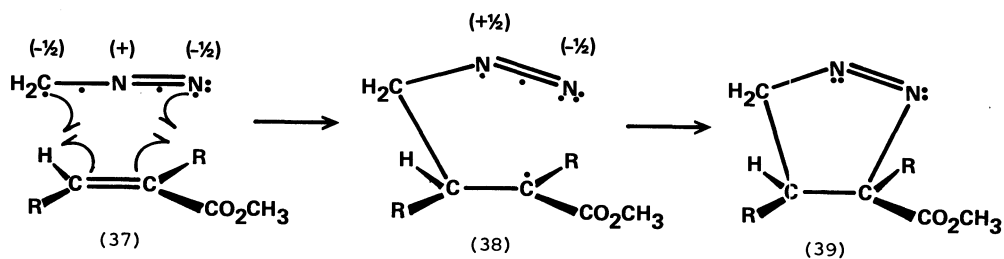
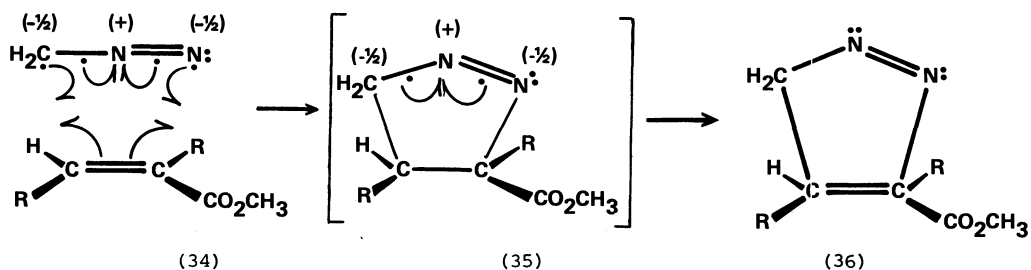
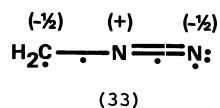
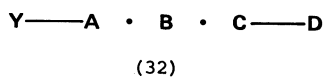


(31)

(28)

The electron-spin theory which is appropriate for the "increased-valence" mechanism of "1,3 dipolar" cycloaddition is set out in some detail in Ref. 11, where the importance of the "long-bond" structures (such as (26)) for the electronic structure and reactivity of any "1,3 dipolar" molecule has also been stressed. The latter conclusion has received support from a number of valence-bond calculations^{12,13,15}, and Goddard and Walsh¹⁶ have used (26) alone to represent the electronic structure of CH_2N_2 .

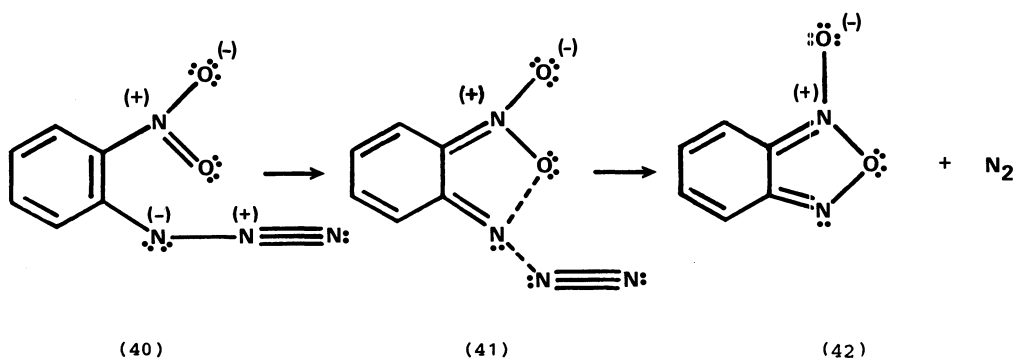
For the transition state of the "1,3 dipolar" cycloaddition, there are six electrons distributed amongst the five overlapping atomic orbitals of Fig. 22-3, for example. In Section 13-6, we have used "increased-valence" structure (32) here to represent the electron distribution for a 6-electron 5-centre bonding unit. One way to obtain this type of "increased-valence" structure in the transition state for the "1,3 dipolar cycloaddition" involves the utilization of a Linnett non-paired spatial orbital structure to represent the electronic structure of the "1,3 dipole". Thus for CH_2N_2 , the Linnett structure is (33)¹⁷, and the concerted mechanism for the cycloaddition may be formulated^{11,12,14} according to (34)-(36). In (35), there is an "increased-valence" bonding unit of type (32). Firestone has used (33) to formulate the two-step mechanism of (37)-(39), with only one O-C bond formed initially between the two reactants¹⁷.



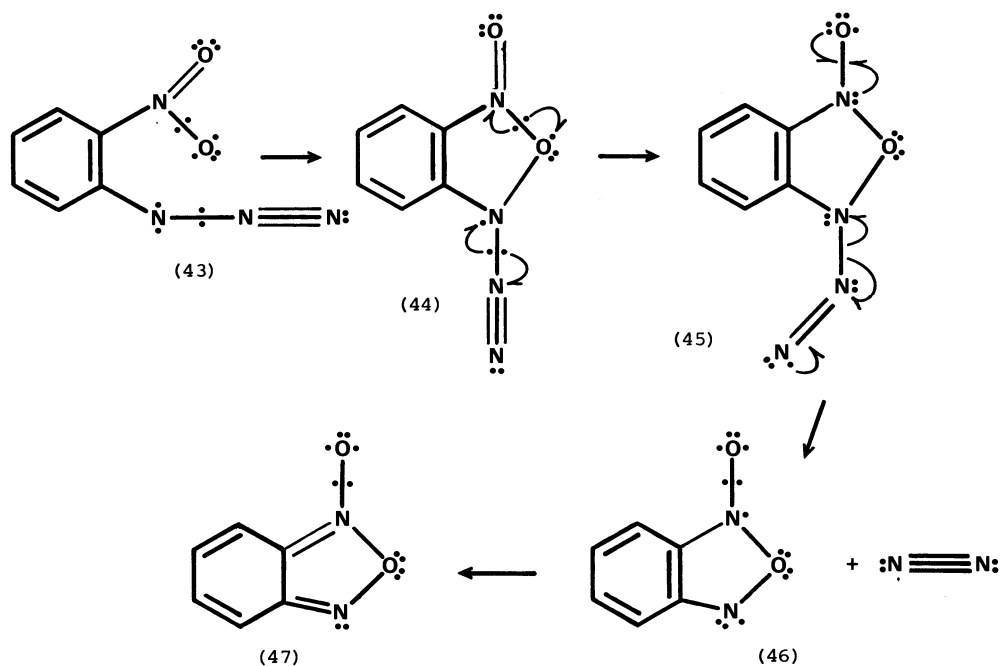
Recent molecular orbital studies of 1,3-dipolar cycloaddition reactions are discussed in Ref. 18.

22-5 THERMAL DECOMPOSITION OF *o*-NITROPHENYLHAZIDE

o-Nitrophenylazide decomposes thermally to give benzofurazan^{19,20}. Using Lewis structures, the mechanism has been formulated as follows:



From (40), we may generate the "increased-valence" structure (43), which must be more stable than (40). Using (43), we may formulate the reaction steps of (43) - (47). In (46) we have unpaired π -electron charges on each nitrogen atom, and these may spin-pair with the two electrons of the adjacent C-C π -bond to generate (47). Our justification for this is the assumption that (47) with two C-C and two (fractional) C-N π -bonds between adjacent atoms should be more stable than (46) with three C-C π -bonds between adjacent atoms.



By using "increased-valence" structures where appropriate for the reactants of this chapter, it has not been necessary to reorganize the electronic structures of the reactants in order to get the reactions started. In most of the reactions, the atomic formal charges have been able to remain constant throughout the course of the reactions. When bond-breaking has occurred, this has often been a consequence of the development of an "increased-valence" bonding unit by delocalizing a lone-pair electron into a two-centre bonding molecular orbital.

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CHAPTER 23

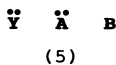
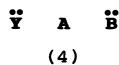
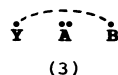
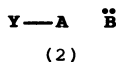
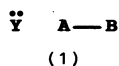
SOME COMPARISONS OF TYPES OF WAVE-FUNCTIONS FOR 4-ELECTRON 3-CENTRE BONDING UNITS

With the simplest form of "increased-valence" theory, we have been concerned with the "increased-valence" structure $Y \text{---} A \cdot \ddot{B}$, which summarizes resonance between the Lewis structures $Y \text{---} A \ddot{B}$ and $Y \overset{\cdot}{A} \text{---} \ddot{B}$, the latter structures having electron-pair bonds between adjacent and non-adjacent atoms respectively.

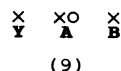
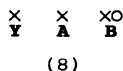
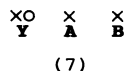
We now wish to examine in more detail some wave-functions for "increased-valence" structures, and to compare them with wave-functions that may be constructed for standard Lewis and Linnett non-paired spatial orbital structures, as well as with the delocalized molecular orbital wave-functions.

23-1 COMPLETE VALENCE-BOND RESONANCE

For a triatomic electron-excess system, with four electrons and three overlapping atomic orbitals, we may write down six Lewis structures in which all electrons are spin-paired, either through double occupation of an atomic orbital, or by electron-pair bond formation between two electrons that singly-occupy different atomic orbitals with opposite spins. These valence-bond (or canonical) structures are (1)-(6).



For $S = 0$ ground-states of electron-excess systems, these are the structures with which we need be concerned. But we note that for paramagnetic excited states, we would need to study the structures (7), (8) and (9), in which the unpaired electrons have parallel spins.



Since each of (1)-(6) represents an $S = 0$ spin-paired electron distribution, we may form linear combinations of their wave-functions, and write

$$\Psi = C_1\Psi_1 + C_2\Psi_2 + C_3\Psi_3 + C_4\Psi_4 + C_5\Psi_5 + C_6\Psi_6 \quad (1)$$

If we choose the coefficients C_1 to C_6 so that the energy of Ψ is minimized, we shall obtain six linear combinations, one of which we shall designate as $\Psi(\text{best})$. Its energy is such that no other linear combination of Ψ_1 to Ψ_6 can generate a lower energy. Alternatively, we may say that this energy is the lowest that can arise from resonance between the valence-bond structures (1)-(6). Each of these six structures is stabilized to a maximum extent by resonance with the other five structures.

In Slater determinantal form, the wave-functions Ψ_1 to Ψ_6 are given by the following:

$$\begin{aligned} \Psi_1 &= |y^\alpha y^\beta a^\alpha b^\beta| + |y^\alpha y^\beta b^\alpha a^\beta|, \quad \Psi_2 = |b^\alpha b^\beta y^\alpha a^\beta| + |b^\alpha b^\beta a^\alpha y^\beta|, \\ \Psi_3 &= |a^\alpha a^\beta y^\alpha b^\beta| + |a^\alpha a^\beta b^\alpha y^\beta|, \quad \Psi_4 = |y^\alpha y^\beta b^\alpha b^\beta|, \\ \Psi_5 &= |y^\alpha y^\beta a^\alpha a^\beta|, \quad \Psi_6 = |a^\alpha a^\beta b^\alpha b^\beta| \end{aligned} \quad (2)$$

The wave-functions for the $\mathbf{A}-\mathbf{B}$, $\mathbf{Y}-\mathbf{A}$ and $\mathbf{Y}-\mathbf{B}$ bonds of Ψ_1 , Ψ_2 and Ψ_3 are of the Heitler-London type, i.e. they involve products of two singly-occupied atomic orbitals in which the electrons have opposite spins. In Section 3-7 we have shown that the Heitler-London wave-functions for the electron-pair bond of H_2 may be expressed as $|s_A^\alpha s_B^\beta| + |s_B^\alpha s_A^\beta|$, in which s_A and s_B are the two hydrogen atom 1s atomic orbitals, and α and β are the spin wave-functions. This type of bond wave-function occurs in Ψ_1 , Ψ_2 and Ψ_3 .

For systems such as H_3^- , O_3 , NO_2^- , and HCO_2^- , the Y and B are symmetrically equivalent hydrogen and oxygen atoms. Consequently, Ψ_1 and Ψ_2 are degenerate, as are Ψ_5 and Ψ_6 . Because of this degeneracy, we may form the linear combinations $\Psi_1 + \Psi_2$, $\Psi_1 - \Psi_2$, $\Psi_5 + \Psi_6$ and $\Psi_5 - \Psi_6$. Of these, only the symmetric functions $\Psi_1 + \Psi_2$ and $\Psi_5 + \Psi_6$ can interact with Ψ_3 and Ψ_4 . We may therefore construct the linear combination

$$\Psi(\text{best}) = C_I\Psi_I + C_{II}\Psi_{II} + C_{III}\Psi_{III} + C_{IV}\Psi_{IV} \quad (3)$$

in which $\Psi_I = \Psi_1 + \Psi_2$, $\Psi_{II} = \Psi_3$, $\Psi_{III} = \Psi_4$, $\Psi_{IV} = \Psi_5 + \Psi_6$.

Linnett and his co-workers¹⁻⁶ have calculated the $\Psi(\text{best})$ for the four π -electrons of HCO_2^- , NO_2^- , O_3 and C_3H_5^- , and four σ -electrons of H_3^- . The coefficients of Ψ_I to Ψ_{IV} for each of these functions are reported in Table 23-1. To help compare the relative magnitudes of the coefficients, we have recalculated them approximately so that they pertain for normalized Ψ_I to Ψ_{IV} . To do this, we have multiplied[†] C_I by 2, C_{II} and C_{IV} by $\sqrt{2}$, and C_{III} by unity. For H_3^- , the reported coefficients refer to approximately normalized basis functions⁵. The (approximately) normalized coefficients are shown in parentheses.

[†] We have omitted π -electron overlap integrals from the normalizing constants.

In Table 23-2, the energies of Ψ_I to Ψ_{IV} , calculated relative to that of $\Psi(\text{best})$, are reported.

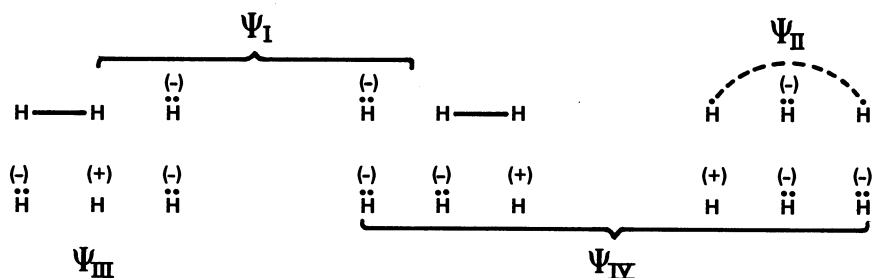


Figure 23-1 Canonical structures for H_3^- .

In Fig. 23-1, we show the canonical structures and formal charges which correspond to Ψ_I to Ψ_{IV} for H_3^- . The formal charges are also those for the corresponding valence-bond structures for NO_2^- , HCO_2^- and $C_3H_5^-$. The corresponding canonical structures for O_3 are displayed in Table 2-1.

	C_I	C_{II}	C_{III}	C_{IV}
O_3 (4π)	0.351 (0.70)	0.390 (0.55)	0.124 (0.12)	0.028 (0.04)
H_3^- (4σ)	0.812 (0.81)	0.483 (0.48)	0.314 (0.31)	0.092 (0.09)
NO_2^- (4π)	0.306 (0.61)	0.391 (0.56)	0.185 (0.19)	0.070 (0.10)
HCO_2^- (4π)	0.273 (0.55)	0.415 (0.59)	0.168 (0.17)	0.078 (0.11)
$C_3H_5^-$ (4π)	0.318 (0.64)	0.304 (0.43)	0.195 (0.20)	0.045 (0.06)

Table 23-1 Coefficients of C_I , C_{II} , C_{III} and C_{IV} for "best" valence-bond wave function. The values in parentheses are those for (approximately) normalized Ψ_I to Ψ_{IV} .

The coefficients of Table 23-1 indicate that Ψ_I and Ψ_{II} are the most important functions for each system. Their energies in Table 23-2 are much lower than those of Ψ_{III} and Ψ_{IV} . Functions Ψ_I and Ψ_{II} represent the valence-bond structures which have an extra covalent bond, smallest formal charge separations, and best electron charge correlation (i.e. best spatial separation of electrons and consequent reduction of interelectronic repulsion). Other studies for the numerous four π - or σ -electron systems⁷⁻⁹, the eight π electrons of N_2O , CO_2 , N_3^- and NO_2^+ ¹⁰ and for ten σ -electrons of N_2O_4 ¹¹ also show that their low-energy canonical structures satisfy these requirements.

	$C_3H_5^-$	NO_2^-	HCO_2^-
Ψ_I	1.94	4.93	5.16
Ψ_{II}	4.75	5.61	5.12
Ψ_{III}	8.90	16.72	16.77
Ψ_{IV}	16.04	23.21	22.56

Table 23-2 Energies (in eV) of Ψ_I to Ψ_{IV} relative to $\Psi(\text{best})$.

23-2 SIMPLE MOLECULAR ORBITAL

For a symmetrical electron-excess system, the 3-centre molecular orbitals are $\Psi_1 = y + k_1 a + b$, $\Psi_2 = y - b$ and $\Psi_3 = y - k_3 a + b$ (Section 2-3). We have assumed that the y , a and b atomic orbitals are oriented so that the overlap integrals S_{ya} and S_{ab} are both > 0 . With respect to the Y-A and A-B bonds, Ψ_1 , Ψ_2 , and Ψ_3 are respectively bonding, non-bonding and antibonding.

The molecular orbital configuration with lowest energy is $\Psi_1(\text{MO}) = |\psi_1^{\alpha} \psi_1^{\beta} \psi_2^{\alpha} \psi_2^{\beta}|$. On substituting the LCAO forms of ψ_1 and ψ_2 , we may expand $\Psi_1(\text{MO})$ and express it as a linear combination^{1-6,12} of the functions Ψ_I to Ψ_{IV} . Thus, we obtain

$$\Psi_1(\text{MO}) = 2k_1 \Psi_I + k_1^2 \Psi_{II} + 4\Psi_{III} + k_1^2 \Psi_{IV} \quad (4)$$

with one variation parameter, k_1 . Since $\Psi(\text{best})$ has three independent variation parameters, namely C_I , C_{II} and C_{III} with C_{IV} related to them through normalization, $\Psi_1(\text{MO})$ must be a more-restricted function than is $\Psi(\text{best})$. $\Psi_1(\text{MO})$ also gives considerable weight to either or both Ψ_{III} and Ψ_{IV} , neither of which is very important for the systems of Table 21-1.

In Table 23-3, some calculated energies for $\Psi_1(\text{MO})$ are reported; they are considerably higher than $\Psi(\text{best})$.

	$C_3H_5^-$	NO_2^-	HCO_2^-
VBHL (Ψ_1)	1.94	4.93	5.16
VBBO	3.01	5.92	5.82
MO	1.07	2.04	1.91
IVBO	0.99	1.91	1.82
IVHL	0.47	0.88	0.81
NPSO	0.41	0.59	0.48

Table 23-3 Energies (in eV) of VB, MO, IV and NPSO wave-functions relative to $\Psi(\text{best})$.

23-3 STANDARD VALENCE-BOND RESONANCE

The standard valence-bond resonance formulation for an electron-excess system involves resonance between the standard Lewis structures (1) and (2), which have covalent bonds only between adjacent atoms, i.e. it is usual to write



as in Ψ_I of Fig. 23-1 for H_3^- .

For the Y-A and A-B bonds, we may use two types of wave-functions, namely (i) Heitler-London (HL) functions, and (ii) two-centre bond-orbitals (BO) of the type $\phi_L = y + ka$, $\phi_R = b + ka$ with $k > 0$.

Therefore, as wave-functions for the standard valence-bond resonance, we may write^{1-5,10,12-14}

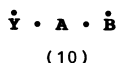
$$(i) \Psi(VBHL) = |y^\alpha y^\beta a^\alpha b^\beta| + |y^\alpha y^\beta b^\alpha a^\beta| + |y^\alpha a^\beta b^\alpha b^\beta| + |a^\alpha y^\beta b^\alpha b^\beta| \equiv \Psi_I \quad (5)$$

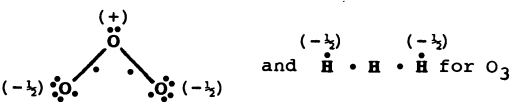
$$(ii) \Psi(VBBO) = |y^\alpha y^\beta \phi_R^\alpha \phi_R^\beta| + |\phi_L^\alpha \phi_L^\beta b^\alpha b^\beta| \equiv k\Psi_I + 2\Psi_{III} + k^2\Psi_{IV} \quad (6)$$

We note that neither of these wave-function includes the "long-bond" function Ψ_{III} , and that $\Psi(VBBO)$ overloads itself with the high-energy functions Ψ_{III} and Ψ_{IV} . In Table 23-3, neither $\Psi(VBHL)$ nor $\Psi(VBBO)$ has a low energy, and we may conclude that the standard valence-bond resonance does not give a very suitable representation for the electronic structures of these systems.

23-4 LINNETT NON-PAIRED SPATIAL ORBITAL

The general non-paired spatial orbital (NPSO) valence structure for 4-electron 3-centre bonding^{1-6,12,13} is (10)



as occurs in the valence-bond structures  and $\dot{H} \cdot H \cdot \dot{H}$ for O_3 and H_3^- . In (10), two electrons occupy y and b atomic orbitals, and two electrons occupy the two-centre bond orbitals $\phi_L = y + ka$ and $\phi_R = b + ka$ with $k > 0$.

Since the four electrons occupy different spatial orbitals, we may construct two singlet wave-functions, both with spin quantum numbers $S = S_z = 0$. The details are described in Section 15-2 and it is possible to form linear combinations of these wave-functions^{1-6,12}. For illustrative purposes here, the special linear combination that generates

$$\Psi(\text{NPSO}) = |y^{\alpha}\phi_{\text{L}}^{\beta}\phi_{\text{R}}^{\alpha}\phi_{\text{b}}^{\beta}| + |y^{\beta}\phi_{\text{L}}^{\alpha}\phi_{\text{R}}^{\beta}\phi_{\text{b}}^{\alpha}| \quad (7)$$

in which electrons occupying spatially adjacent orbitals have opposite spins, is a satisfactory wave-function and this is the NPSO wave-function that we shall examine. In terms of the functions Ψ_{I} to Ψ_{IV} , we may express it¹⁻⁶ as

$$\Psi(\text{NPSO}) = k\Psi_{\text{I}} + k^2\Psi_{\text{II}} + 2\Psi_{\text{III}} \quad (8)$$

thereby showing that it includes the "long-bond" functions Ψ_{II} and excludes the unimportant function Ψ_{IV} . The opposite pertains for the $\Psi(\text{VBBO})$ of Section 23-3, and therefore we can understand why the $\Psi(\text{NPSO})$ of Table 23-3 generate much lower energies than do the $\Psi(\text{VBBO})$.

23-5 "INCREASED-VALENCE"

The general "increased-valence" structures are (11) and (12). As we have done many times in this book, we may derive them from the standard Lewis structures (2) and (1) by delocalizing a B electron of (2) into a vacant bonding A-B orbital, and a Y electron of (1) into a vacant bonding Y-A orbital. Thus, we may write



Above the arrowheads, we have indicated the orbitals that are involved in the delocalizations.

For the standard valence-bond resonance of Section 23-3, we have used two types of wave-functions for the electron-pair bonds, namely the Heitler-London and the bond-orbital functions. We may do the same for the "increased-valence" functions of this section^{7,12-14}. If we assume that electrons which occupy spatially adjacent orbitals have opposite spins, we may write down the following Heitler-London and bond-orbital wave-functions for the resonance between the "increased-valence" structures of (11) and (12).

$$\Psi(\text{IVHL}) = |y^{\alpha}\phi_{\text{a}}^{\beta}\phi_{\text{R}}^{\alpha}\phi_{\text{b}}^{\beta}| + |y^{\beta}\phi_{\text{a}}^{\alpha}\phi_{\text{R}}^{\beta}\phi_{\text{b}}^{\alpha}| + |b^{\alpha}\phi_{\text{a}}^{\beta}\phi_{\text{R}}^{\alpha}\phi_{\text{Y}}^{\beta}| + |b^{\beta}\phi_{\text{a}}^{\alpha}\phi_{\text{R}}^{\beta}\phi_{\text{Y}}^{\alpha}| = \Psi_{\text{I}} + 2k\Psi_{\text{II}} \quad (9)$$

$$\begin{aligned}
 \Psi(\text{IVBO}) &= |\phi_{\text{L}}^{\alpha}\phi_{\text{L}}^{\beta}\phi_{\text{R}}^{\alpha}\phi_{\text{b}}^{\beta}| + |\phi_{\text{L}}^{\alpha}\phi_{\text{L}}^{\beta}\phi_{\text{R}}^{\alpha}\phi_{\text{R}}^{\beta}| + |\phi_{\text{R}}^{\alpha}\phi_{\text{R}}^{\beta}\phi_{\text{L}}^{\alpha}\phi_{\text{Y}}^{\beta}| + |\phi_{\text{R}}^{\alpha}\phi_{\text{R}}^{\beta}\phi_{\text{Y}}^{\alpha}\phi_{\text{L}}^{\beta}| \\
 &= 3k\Psi_{\text{I}} + 2k^2\Psi_{\text{II}} + 4\Psi_{\text{III}} + 2k^2\Psi_{\text{IV}} \quad (10)
 \end{aligned}$$

Both $\Psi(\text{IVHL})$ and $\Psi(\text{IVBO})$ include the standard and "long-bond" structure

functions Ψ_I and Ψ_{II} . In Table 23-3, the $\Psi(\text{IVHL})$ and the $\Psi(\text{NPSO})$ are the low-energy functions in each case, with $\Psi(\text{NPSO})$ being the slightly better function.

We may note that $\Psi(\text{MO})$ and $\Psi(\text{IVBO})$ of Eqs. (4) and (10) are similar wave-functions, and that their energies in Table 23-3 are very similar. This point has been discussed in more detail elsewhere¹².

23-6 "IMPROVED" $\Psi(\text{IVBO})$ AND $\Psi(\text{best})$

The $\Psi(\text{MO})$, $\Psi(\text{VBBO})$, $\Psi(\text{NPSO})$ and $\Psi(\text{IVBO})$ that we have described in Sections 23-5 each have one variation parameter (k_1 or k), i.e. one parameter which may be chosen so that the energy for each of these functions is minimized. Therefore, none of them can have energies as low as the $\Psi(\text{best})$ with three independent variation parameters. However, it is possible to improve these wave-functions by introducing additional variation parameters. We shall discuss how this is done here.

For the molecular orbital description of H_2 , we have shown in Section 3-3 that the bonding molecular orbital configuration $(\sigma 1s)^2$ could be improved through configuration interaction by linearly combining it with the antibonding configuration $(\sigma^* 1s)^2$. Through configuration interaction, we may also improve the $\Psi_1(\text{MO})$ of Section 23-2. By constructing the wave-function

$$\Psi(\text{CI}) = C_1\Psi_1(\text{MO}) + C_2\Psi_2(\text{MO}) + C_3\Psi_3(\text{MO}) + C_4\Psi_4(\text{MO}) \quad (11)$$

in which

$$\Psi_2(\text{MO}) = |\psi_2^\alpha \psi_2^\beta \psi_3^\alpha \psi_3^\beta|, \quad \Psi_3(\text{MO}) = |\psi_1^\alpha \psi_1^\beta \psi_3^\alpha \psi_3^\beta|, \quad \Psi_4(\text{MO}) = (|\psi_1^\alpha \psi_3^\beta \psi_2^\alpha \psi_2^\beta| + |\psi_3^\alpha \psi_1^\beta \psi_2^\alpha \psi_2^\beta|) / 2^{1/2} \quad (12)$$

and the coefficients C_1 to C_4 are chosen so that the energy of $\Psi(\text{CI})$ is a minimum, we obtain a wave-function which is equivalent to the $\Psi(\text{best})$. Without some transformation, this $\Psi(\text{CI})$ has the disadvantage that it does not correspond to one or two simple valence-bond structures.

For $\Psi(\text{VBBO})$ and $\Psi(\text{NPSO})$, we may use a different bond-parameter for each bond orbital^{6b,13}. Thus, instead of using $\phi_L = y + ka$ for both Y-A bonding electrons of the valence bond structure (2), we may use $\phi_L = y + ka$ for one electron and $\phi_L' = y + k'a$ for the other electron. Similarly, for the two A-B bonding electrons of (1), we may use the orbitals $\phi_R = b + ka$ and $\phi_R' = b + k'a$ instead of $\phi_R = b + ka$ for both electrons. The $\Psi(\text{VBBO})$ wave-function may now be expressed as

$$\Psi(\text{VBBO}) = (k + k')\Psi_I + 4\Psi_{III} + 2kk'\Psi_{IV} \quad (13)$$

which still omits the "long-bond" function Ψ_{II} .

In Table 23-4, we report the energies for some two-parameter wave functions¹³. They show that $\Psi(\text{VBBO})$ remains a high-energy function.

	XeF_2	C_3H_3^-	NO_2^-	HCO_2^-
VBBO	8.08	1.20	2.98	3.37
NPSO	0.060	0.058	0.225	0.266
IVBO	0.190	0.003	0.00001	0.005

Table 23-4 Energies (in eV) of two-parameter VBBO, NPSO and IVBO wave-functions relative to $\Psi(\text{best})$.

The $\Psi(\text{NPSO})$ may be improved by using the bond-orbitals $\phi_L = y + ka$, $\phi_R = b + k''a$, $\phi_L'' = y + k''a$, and $\phi_R = b + ka$ instead of $\phi_L = y + ka$ and $\phi_R = b + ka$. If this is done, we may express $\Psi(\text{NPSO})$ as

$$\Psi(\text{NPSO}) = (k + k'')\Psi_I + 2kk''\Psi_{II} + 4\Psi_{III} \quad (14)$$

which generates very low energies in Table 23-4. However, $\Psi(\text{NPSO})$ can never become equivalent to $\Psi(\text{best})$, because it must always omit Ψ_{IV} . With $\Psi(\text{IVBO})$, we may construct either two-parameter or three-parameter variational functions. For example, we may use $\phi_L = y + ka$ and $\phi_L' = y + k'a$ for both electrons of the two-electron Y-A bond of (11), and $\phi_R'' = b + k''a$ for the one-electron A-B bond of (11), together with the $\phi_R = b + ka$, $\phi_R' = b + k'a$ and $\phi_L'' = y + k''a$ for (12). By introducing these orbitals into $\Psi(\text{IVBO})$, we may express this wave function as

$$\Psi(\text{IVBO}) = (k + k' + k'')\Psi_I + 2kk''\Psi_{II} + 4\Psi_{III} + 2kk'\Psi_{IV} \quad (15)$$

which may be shown¹³ to be equivalent to $(4/C_3)\Psi(\text{best})$. Therefore, for symmetrical systems, resonance between the two "increased-valence" structures (11) and (12) is equivalent to unrestricted resonance between the valence-bond structures (1) to (6). So, if we are prepared to use non-orthogonal bond orbitals as wave-functions for (fractional) electron-pair bonds and one-electron bonds, we may use "increased-valence" structures and know that these can correspond to the best description of symmetrical 4-electron 3-centre bonding units.

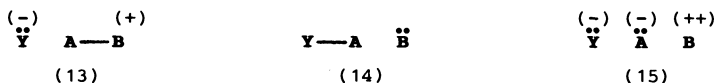
In Table 23-4, we have reported some two-parameter $\Psi(\text{IVBO})$, for which we have assumed that $k = k'$ in the bond orbitals for the two-electron bond. As is the case for the two-parameter $\Psi(\text{NPSO})$, the energies of these $\Psi(\text{IVBO})$ are very low.

If Y and B are non-equivalent atoms, the "increased-valence" structures (11) and (12) are non-equivalent structures, and they will have different energies. For neutral systems, we would expect that (11) will be the lower-energy structure if the formal charges of the standard Lewis structures (1) and (2) are those of (13) and

(14). If we use the non-orthogonal bond-orbitals ϕ_L , ϕ_L' and ϕ_R'' for the Y-A and A-B bonding electrons of (11), we obtain the three-parameter function

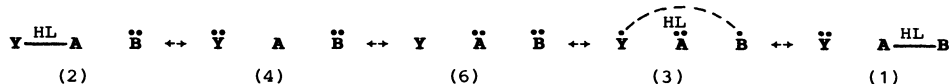
$$\Psi(\text{Y} \text{---} \overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}, \text{IVBO}) = k''\Psi_1 + 2(k + k')\Psi_2 + k'k\Psi_3 + 2\Psi_4 + 2kk'\Psi_6 \quad (16)$$

which summarizes resonance between the five canonical structures (1)-(4) and (6). The formal charges for the omitted canonical structure (15) suggest that this structure should have a small weight, and therefore this three-parameter function should approximate closely to $\Psi(\text{best})$.

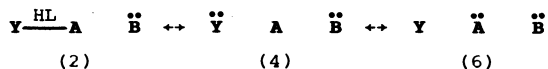


23-7 CONCLUSIONS

Throughout this book, it will be noticed how usually we have used a Heitler-London type wave-function for the (fractional) two-electron Y-A bond of the "increased-valence" structure (11). Invoking such a wave-function is the simplest way to ensure that the "increased-valence" structure summarizes resonance between the standard and "long-bond" Lewis structures (2) and (3), each of which has a Heitler-London electron-pair bond. But, as we have done in Sections 23-3 and 23-5, we may also use two-centre bond orbitals as wave functions for the two-electron Y-A bonds of (2) and (11) as well as for the one-electron A-B bond of (11). In Section 23-6, we have shown that $\text{Y} \text{---}^{\text{bo}}\text{A} \cdot \overset{\cdot}{\text{B}}$ is equivalent to the resonance of



in which we have written bo (bond-orbital) and HL (Heitler-London) above or below the bonds to indicate the type of bond wave-function. Since the valence-bond structure $\text{Y} \text{---}^{\text{bo}}\text{A} \quad \overset{\cdot\cdot}{\text{B}}$ with bond-orbitals for the Y-A bonds is equivalent to the resonance



it follows that $\text{Y} \text{---} \overset{\cdot}{\text{A}} \cdot \overset{\cdot}{\text{B}}$ summarizes the resonance of



Such an "increased-valence" description is therefore more elaborate than that which uses the Heitler London formulation for all two-electron bonds, namely

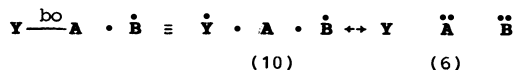


but both do include (in different ways) the standard and "long-bond" Lewis structures $Y \xrightarrow{HL} A \quad \ddot{B}$ and $Y \overset{HL}{\overset{\cdot\cdot}{A}} \dot{B}$. Our essential point is that by using $Y \xrightarrow{HL} A \cdot \dot{B}$, we do stabilize $Y \xrightarrow{HL} A \quad \ddot{B}$ through interaction with $Y \overset{HL}{\overset{\cdot\cdot}{A}} \dot{B}$, no matter what type of wave function is used for the two-electron Y-A bonds. The fundamental process of (fractional or non-fractional) electron-pair bond formation involves spin-pairing two unpaired electrons with opposite spins occupying overlapping orbitals, and the nature of the bond wave-functions need not be prescribed uniquely. Therefore, when we write



we must obtain a lower energy than when we use $Y \xrightarrow{HL} A \quad \ddot{B}$ alone.

If our wish is to use one valence-bond structure to summarize resonance between the "long-bond" structure (2) and other canonical structures, in Section 23-4 we have found that we may also use the NPSO structure (10). Because this structure summarizes resonance between the canonical structures (1), (2), (3) and (4), $\Psi(\text{NPSO})$ must always generate a lower energy than do the wave-functions for either $Y \xrightarrow{HL} A \cdot \dot{B}$ or $Y \xrightarrow{HL} A \cdot \dot{B} \leftrightarrow \dot{Y} \cdot A \xrightarrow{HL} B$. (These "increased-valence" structures are equivalent to the resonance of (2) \leftrightarrow (3), and (1) \leftrightarrow (2) \leftrightarrow (3) respectively.) However, one advantage that is obtained by using either (11), or (11) \leftrightarrow (12), is that the "increased-valence" structures are very easily generated from the standard Lewis structure (1) and (2). And if we use bond-orbitals for all three bonding electrons of $Y \xrightarrow{bo} A \cdot \dot{B}$, then this structure must be more stable than (10), since it is easy to show that $Y \xrightarrow{bo} A \cdot \dot{B}$ summarizes resonance between (10) and (6), i.e



Usually, however, the contribution of (6) should be small. Therefore, the NPSO structure is a very good alternative to the "increased-valence" structure, and perhaps has the advantage that, because it involves no (fractional) 2-electron bonds, only one type of spatial orbital wave-function may be constructed for it.

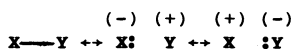
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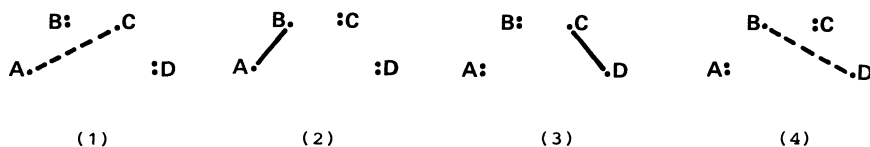
CHAPTER 24

A NOTE ON PAULING "3-ELECTRON BONDS" AND COVALENT-IONIC RESONANCE

If a pair of electrons occupy two overlapping atomic orbitals centred on two atoms X and Y, then the X-Y bond may be described in terms of resonance between a covalent structure and two ionic structures, viz

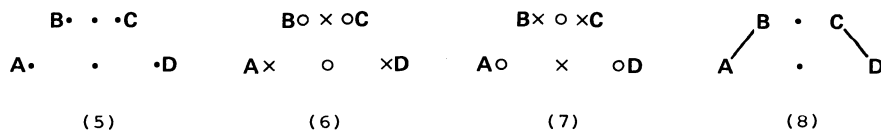


This type of covalent-ionic resonance, which involves an electron-pair bond in the covalent structure, is widely known. The discussions of Section 7-3 and 8-1(c) show that for 6-electron 4-centre bonding units, another type of covalent-ionic resonance is also possible, namely that which generates a Pauling "3-electron bond" between the diatomic moieties. If we generalize the discussion of Section 7-3, for example, we may represent this type of resonance as (1) ↔ (2), (1) ↔ (3). (Equivalent types of resonance exist for (4) with (3) and (2).)



With respect to the A-B and C-D moieties, structures (1) and (4) are covalent, whereas structures (2) and (3) are ionic. The $\text{B:} \cdot \text{C} \leftrightarrow \text{B} \cdot \text{:C}$ resonance for (1) ↔ (2), or (3) ↔ (4) and the $\text{A} \cdot \text{:D} \leftrightarrow \text{A:} \cdot \text{D}$ resonance for (1) ↔ (3) or (4) ↔ (2) generates the Pauling "3-electron bonds" $\text{B} \cdot \cdot \text{C}$ and $\text{A} \cdot \cdot \text{D}$, respectively.

Resonance between structures (1)-(4) generates two Pauling "3-electron bonds" as in (5), with the spin distributions of (6) and (7). The molecular orbital configuration for each of (5)-(7) involves two B-C and two A-D bonding electrons, and one B-C and one A-D antibonding electron. On spin-pairing the two antibonding electrons, "increased-valence" structure (8) is obtained.



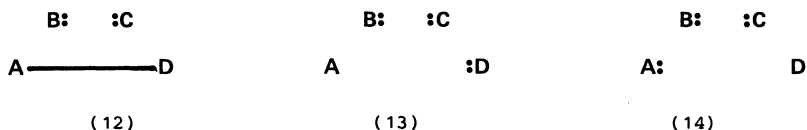
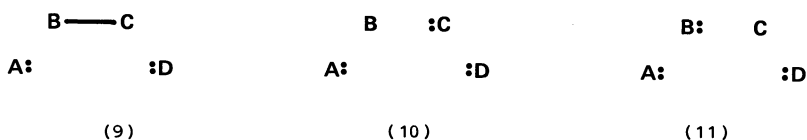
In Section 7-2, we have constructed the delocalized molecular orbitals for a symmetrical 6-electron 4-centre bonding unit. The lowest-energy configuration is given by Eqn. (1), below, for which the molecular orbitals (ψ_i) and symmetry orbitals (s_i) are defined as in Section 7-2, with overlapping orbitals χ_1 , χ_2 , χ_3 and χ_4 located on the A, B, C and D atomic centres. Algebraic expansion of Eqn. (2) generates the linear combination of the symmetry-orbital configurations given in Eqn.(3) (c.f. Ref. 1).

$$\Psi_1(\text{MO}) = |(\psi_1)^2(\psi_2)^2(\psi_3)^2| \quad (1)$$

$$\equiv \left| (s_1)^2 \left(\frac{s_4 + \mu s_2}{(1 + \mu^2)^{1/2}} \right)^2 (s_3)^2 \right| \quad (2)$$

$$= \{ |(s_1)^2(s_4)^2(s_3)^2| + \mu^2 |(s_1)^2(s_2)^2(s_3)^2| + \mu (|(s_1)^2(s_4^\alpha)^1(s_2^\beta)^1(s_3)^2| + |(s_1)^2(s_2^\alpha)^1(s_4^\beta)^1(s_3)^2|) \} / (1 + \mu^2) \quad (3)$$

The $|(s_1)^2(s_4)^2(s_3)^2|$ and $|(s_1)^2(s_2)^2(s_3)^2|$ configurations of Eqn. (3) generate the covalent and ionic structures (9)-(11), and (12)-(14), respectively, with B-C and A-D electron-pair bonds in the covalent structures (9) and (12). The remaining Slater determinants of Eqn. (3) are associated with the Pauling "3-electron bond" structures (6) and (7), in which the crosses and circles represent electrons with α and β spins. Therefore the molecular orbital configuration of Eqn. (1) for 6-electron 4-centre bonding is concomitant with covalent-ionic resonance of both the electron-pair bond and Pauling "3-electron bond" type.

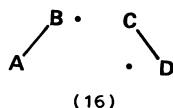
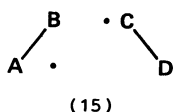


When $\Psi_1(\text{MO})$ of Eqn. (1) is linearly combined with the excited configuration $\Psi_2(\text{MO})$ of Eqn. (4), to give a lower-energy C.I. wave-function, the contributions to resonance of the ionic structures (2), (3), (10), (11), (13) and (14) are reduced

relative to those of the covalent structures (1), (4), (9) and (12). The Pauling "3-electron bond" structures (5)-(8) then acquire polarity for the 1-electron bonds. The "increased-valence" structure (8) is then replaced by resonance between (15) and (16).

$$\Psi_2(\text{MO}) = |(\psi_1)^2(\psi_2)^2(\psi_4)^2| \quad (4)$$

$$\equiv \left| \left(\frac{s_3 + \lambda s_1}{(1 + \lambda^2)^{1/2}} \right)^2 (s_2)^2 (s_4)^2 \right| \quad (5)$$



We shall conclude by noting that covalent-ionic resonance for the electron-pair bond, $\overset{(-)}{\text{X}}-\overset{(+)}{\text{Y}} \leftrightarrow \overset{(+)}{\text{X}}:\overset{(-)}{\text{Y}} \leftrightarrow \overset{(+)}{\text{X}}:\overset{(-)}{\text{Y}}$ is equivalent to resonance between the 1-electron bond structures $\overset{(-)}{\text{X}} \cdot \overset{(+)}{\text{Y}}$ and $\overset{(+)}{\text{X}} \cdot \overset{(-)}{\text{Y}}$. This is because $\overset{(-)}{\text{X}} \cdot \overset{(+)}{\text{Y}} \equiv \overset{(+)}{\text{X}}:\overset{(-)}{\text{Y}} \leftrightarrow \overset{(-)}{\text{X}}-\overset{(+)}{\text{Y}}$ and $\overset{(+)}{\text{X}} \cdot \overset{(-)}{\text{Y}} \equiv \overset{(-)}{\text{X}}-\overset{(+)}{\text{Y}} \leftrightarrow \overset{(+)}{\text{X}}:\overset{(-)}{\text{Y}}$.

With these identities, all electron-pair bonds that have both covalent and ionic character may be expressed in terms of 1-electron bond structures², i.e. for any molecule, valence-bond structures may be written down that involve only 1-electron bonds.

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APPENDIX

ATOMIC ORBITAL OVERLAP AND RESONANCE BETWEEN STANDARD AND "LONG-BOND" LEWIS STRUCTURES

As well as relative energy considerations, atomic orbital overlap via the off-diagonal matrix elements (H_{ij}) of the secular equations (Section 1-3) helps promote the importance of "long-bond" structures for N -centre electron-rich bonding units¹. We shall demonstrate this by consideration of 4-electron 3-centre bonding, for which the standard and "long-bond" Lewis structures are (1), (2) and (3) of Section 23-1. With Heitler-London type wave-functions for the electron-pair bonds, the wave-functions for these structures are the Ψ_1 , Ψ_2 and Ψ_3 of Eqn. 23-2.

The extent to which Ψ_j will linearly combine with Ψ_i , and the magnitude of the concomitant resonance stabilization energy, depends on the magnitude of the Hamiltonian matrix element H_{ij} for $i \neq j$, as well as on the energy separation $H_{jj} - H_{ii}$. The off-diagonal H_{ij} is atomic orbital overlap dependent, directly through the overlap integrals S_{ya} , S_{ab} and S_{yb} , and indirectly through the core Hamiltonian and electron repulsion integrals of the general types $H_{\mu\nu}^0$, $(\mu\nu|\lambda\lambda)$ and $(\mu\nu|\lambda\sigma)$. (The μ , ν , λ and σ are any of the atomic orbitals y , a and b , with $\mu \neq \nu$; see for example ref. 2 for integral definitions). With the Ψ_i of Eqn. 23-2, it may be deduced (see for example Ref. 3 for procedure) that the dominant terms for H_{13} and H_{23} are functions of S_{ya} and S_{ab} respectively. However because the atomic orbitals y and b are located on non-adjacent centres, the overlap integral S_{yb} has a very small magnitude, and therefore the dominant terms for H_{12} are functions of the product $S_{ya}S_{ab}$. Consequently, because all overlap integrals are less than unity in magnitude, H_{13} and H_{23} will usually have appreciably larger magnitudes than has H_{12} .

These H_{ij} considerations show that with respect to atomic orbital overlap, a pair of standard and "long-bond" structures (i.e. (1) and (3), or (2) and (3)) are better suited for resonance than are the pair of standard structures (1) and (2), i.e. the "long-bond" structure (3) helps the standard structures (1) and (2) to interact by functioning as a "bridge" between them. One may envisage the conversion of (1) into (2) to occur via (3), by transferring a Y electron of (1) into the A atomic orbital to afford (3), and then the transfer of an A electron of (3) into the B atomic orbital to obtain (2), i.e. the "long-bond" structure forms a connecting link between the standard structures.

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Addendum:

Page 37, 3 lines below Eqn. (15): replace $(1 - s_{ab}^2)^{\frac{1}{2}}$ with $-(1 - s_{ab}^2)^{-\frac{1}{2}}$.

Page 45, Eqn. (41): insert - before { .

Page 236, 2nd line of (e): replace O_2 with Fe(II).

M.F.O'Dwyer, J.E.Kent, R.D.Brown

Valency

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The science of contemporary gas kinetics owes much to the pioneering efforts of V. N. Kondratiev. In this book, he and his coauthor E. E. Nikitin describe the kinetics and mechanisms of gas reactions in terms of current knowledge of elementary processes of energy transfer, uni-, bi- and trimolecular reactions. Their consideration of formal chemical kinetics is followed by a discussion of the mechanisms of elastic collisions, and of unimolecular, combination and bimolecular reactions. In addition, they have devoted several chapters to the kinetics of the more complicated photochemical reactions, reactions in discharge and radiation-chemical reactions, the general theory of chain reactions, and processes in flames. Particular attention is paid to non-equilibrium reactions, which occur as a result of the Maxwell-Boltzmann distribution principle.

This comprehensive and critical presentation of gas phase kinetics will prove an excellent source of information for chemists and physicists in research and industry as well as for advanced students in chemistry and chemical physics (540 references).



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