- It is a theoretical language with operations that work on one or more relations to define another relation without changing the original relation (s).
- Relations are closed under relational algebra operations.

- Unary operations
 - Projection
 - The projection operation works on a single relation R and defines a relation that contains a vertical subset of R, extracting the values of specified attributes and eliminating duplicates.
 - Note: All the examples in these slides refer to the relations you were given on students records db unless otherwise specified.
 - $\pi_{a1,a2,a3,...an}(R)$
 - Where a1,a2,...,an are attributes and R is a relation.
 - Examples:
 - 1. Produce a list of all students showing their name, father's name, and sex.
 - 2. List the rooms by showing their type, number, campus, and capacity.

- Selection (or Restriction)
 - The selection operation works on a single relation R and defines a relation that contains only those tuples of R that satisfy the specified condition (predicate).
 - σ_{condition}(R)
 - Examples:
 - 1. List all students in the department of BAIS.
 - 2. List all female instructors whose department is BAIS, but are not living in Addis Ababa.
 - List the lecture halls at the main campus with capacity between 150 and 200 students together with all computer labs.
 - 4. List the instructors whose date of birth is not entered.
 - 5. Display the identification numbers and names of the female instructors with the rank of Full Professor.



Binary Operations

- Set Operations
 - Union
 - The Union of two relations R and S defines a relation that contains all the tuples of R, or S, or both R and S, duplicate tuples being eliminated. R and S must be union-compatible.
 - R u S
 - Examples:
 - 1. Take two relations A and B of your choice that are union compatible and perform the union.
 - 2. List the Kebeles where Students or Instructors of AAUCC live in Addis Ababa.

Intersection

- The Intersection operation defines a relation consisting of a set of all tuples that are in both R and S. R and S must be union-compatible.
- R ∩ S
- Examples:
 - 1. Take two relations A and B of your choice that are union compatible and perform the intersection.
 - 2. List the Kebeles where Students and Instructors of AAUCC live in Addis Ababa.

Set difference

- The set difference operation defines a relation consisting of the tuples that are in relation R, but not in S. R and S must be union-compatible.
- R S
- Examples:
 - 1. Take two relations A and B of your choice that are union compatible and perform A B and also B A.
 - 2. List the Kebeles where Students but not Instructors of AAUCC live in Addis Ababa.

Cartesian product

- The Cartesian product operation defines a relation that is the concatenation of every tuple of relation R with every tuple of relation S.
- R x S
- Examples:
 - 1. Perform this operation on two relations, say A and B, of your choice.
 - 2. Register each student in the department of BAIS for every course given by the department of BAIS.
 - 3. List the names and departments of all students who registered for the course BAIS 322 in the second semester of the academic year 2002.

O Join Operations

- Theta join (θ)
 - The Theta join operation defines a relation that contains tuples satisfying the predicate *F* from the Cartesian product of R and S. The predicate *F* is of the form R.a_i θ S.b_i where θ may be one of the comparison operators (<,≤,>,≥,=, ≠). If the comparison operator is the = sign, then the join operation is called Equijoin.
 - $\mathsf{R} \Join_F \mathsf{S}$
 - Note that: $\mathbb{R} \bowtie_F \mathbb{S} = \sigma_F (\mathbb{R} \times \mathbb{S})$
 - Examples:
 - Take your own example
 - Use example 3 of the previous slide.

Natural join

- The Natural join is an Equijoin of the two relations R and S over all common attributes x. One occurrence of each common attribute is eliminated from the result.
- R ⋈ S
- Examples:
 - Take your own example.
 - Use the 2nd example of the previous slide.

Outer join

- The (left) Outer join is a join in which tuples form R that do no have matching values in the common attributes of S are also included in the result relation. Missing values in the second relation are set to null.
- $\mathsf{R} \rtimes \mathsf{S}$
- Examples:
 - 1. Take your own example.
 - 2. Produce a status report on registration of students.
 - 3. Produce a status report on advisory assignment of instructors.
 - 4. Produce a status report on room schedules.
- Assignment:
 - Provide the definition for right outer join.

Semijoin

- The Semijoin operation defines a relation that contains the tuples of R that participate in the join of R with S.
- R ⊳_F S
- Examples:
 - Take your own example.
 - List complete details of all courses which are registered by students of the department of Accounting in the 1st semester of the academic year 2008/9.

Division Operation

- Division
 - Assume relation R is defined over the attribute set A and relation S is defined over the attribute set B such that B \subseteq A. Let C = A B. Then the Division operation R ÷ S is defined as a relation over the attributes C that consists the set of tuples from R that match the combination of every tuple in S.
 - R ÷ S
 - Examples:
 - Take two relations R and S for which R ÷ S can be performed and get R ÷ S.
 - 2. Produce the Identification numbers of all students who have registered for all courses given by the department of BAIS.

Exercises

- Refer to Student Records DB schema in specifying the following queries using Relational Algebra.
 - 1. List the names of courses on which student Abebe Bekele got "A" grades.
 - What is the name of the instructor who advised student Abebe Bekele in the 1st semester of the academic year 2004?
 - 3. What grade did student Abebe Bekele got on the course Database Systems I?
 - List the names of the courses for which student Abebe Bekele registered in the 2nd semester of the academic year 2008.
 - List the rooms where the course Introduction to management is scheduled in the 3rd period on Wednesdays of the current semester.
 - 6. Show the names and departments of the instructors who are not assigned to advise students in the current semester.
 - List the names, ranks, and date of employment of all instructors who are qualified to teach the courses E-Commerce or Database Systems I and II.
 - 8. Display the course name, course code, and the name of the department offering the course for each course that is prerequisite to the course BAIS 411.