# HANDBOOK OF PHILOSOPHICAL LOGIC 2ND EDITION

#### VOLUME 12

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edited by D.M. Gabbay and F. Guenthner

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#### Edited by

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and

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### PREFACE TO THE SECOND EDITION

It is with great pleasure that we are presenting to the community the second edition of this extraordinary handbook. It has been over 15 years since the publication of the first edition and there have been great changes in the landscape of philosophical logic since then.

The first edition has proved invaluable to generations of students and researchers in formal philosophy and language, as well as to consumers of logic in many applied areas. The main logic article in the Encyclopaedia Britannica 1999 has described the first edition as 'the best starting point for exploring any of the topics in logic'. We are confident that the second edition will prove to be just as good!

The first edition was the second handbook published for the logic community. It followed the North Holland one volume *Handbook of Mathematical Logic*, published in 1977, edited by the late Jon Barwise. The four volume *Handbook of Philosophical Logic*, published 1983–1989 came at a fortunate temporal junction at the evolution of logic. This was the time when logic was gaining ground in computer science and artificial intelligence circles.

These areas were under increasing commercial pressure to provide devices which help and/or replace the human in his daily activity. This pressure required the use of logic in the modelling of human activity and organisation on the one hand and to provide the theoretical basis for the computer program constructs on the other. The result was that the *Handbook of Philosophical Logic*, which covered most of the areas needed from logic for these active communities, became their bible.

The increased demand for philosophical logic from computer science and artificial intelligence and computational linguistics accelerated the development of the subject directly and indirectly. It directly pushed research forward, stimulated by the needs of applications. New logic areas became established and old areas were enriched and expanded. At the same time, it socially provided employment for generations of logicians residing in computer science, linguistics and electrical engineering departments which of course helped keep the logic community thriving. In addition to that, it so happens (perhaps not by accident) that many of the Handbook contributors became active in these application areas and took their place as time passed on, among the most famous leading figures of applied philosophical logic of our times. Today we have a handbook with a most extraordinary collection of famous people as authors!

The table below will give our readers an idea of the landscape of logic and its relation to computer science and formal language and artificial intelligence. It shows that the first edition is very close to the mark of what was needed. Two topics were not included in the first edition, even though

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they were extensively discussed by all authors in a 3-day Handbook meeting. These are:

- a chapter on non-monotonic logic
- a chapter on combinatory logic and  $\lambda$ -calculus

We felt at the time (1979) that non-monotonic logic was not ready for a chapter yet and that combinatory logic and  $\lambda$ -calculus was too far removed.<sup>1</sup> Non-monotonic logic is now a very major area of philosophical logic, alongside default logics, labelled deductive systems, fibring logics, multi-dimensional, multimodal and substructural logics. Intensive reexaminations of fragments of classical logic have produced fresh insights, including at time decision procedures and equivalence with non-classical systems.

Perhaps the most impressive achievement of philosophical logic as arising in the past decade has been the effective negotiation of research partnerships with fallacy theory, informal logic and argumentation theory, attested to by the Amsterdam Conference in Logic and Argumentation in 1995, and the two Bonn Conferences in Practical Reasoning in 1996 and 1997.

These subjects are becoming more and more useful in agent theory and intelligent and reactive databases.

Finally, fifteen years after the start of the Handbook project, I would like to take this opportunity to put forward my current views about logic in computer science, computational linguistics and artificial intelligence. In the early 1980s the perception of the role of logic in computer science was that of a specification and reasoning tool and that of a basis for possibly neat computer languages. The computer scientist was manipulating data structures and the use of logic was one of his options.

My own view at the time was that there was an opportunity for logic to play a key role in computer science and to exchange benefits with this rich and important application area and thus enhance its own evolution. The relationship between logic and computer science was perceived as very much like the relationship of applied mathematics to physics and engineering. Applied mathematics evolves through its use as an essential tool, and so we hoped for logic. Today my view has changed. As computer science and artificial intelligence deal more and more with distributed and interactive systems, processes, concurrency, agents, causes, transitions, communication and control (to name a few), the researcher in this area is having more and more in common with the traditional philosopher who has been analysing

<sup>&</sup>lt;sup>1</sup>I am really sorry, in hindsight, about the omission of the non-monotonic logic chapter. I wonder how the subject would have developed, if the AI research community had had a theoretical model, in the form of a chapter, to look at. Perhaps the area would have developed in a more streamlined way!

such questions for centuries (unrestricted by the capabilities of any hardware).

The principles governing the interaction of several processes, for example, are abstract an similar to principles governing the cooperation of two large organisation. A detailed rule based effective but rigid bureaucracy is very much similar to a complex computer program handling and manipulating data. My guess is that the principles underlying one are very much the same as those underlying the other.

I believe the day is not far away in the future when the computer scientist will wake up one morning with the realisation that he is actually a kind of formal philosopher!

The projected number of volumes for this Handbook is about 18. The subject has evolved and its areas have become interrelated to such an extent that it no longer makes sense to dedicate volumes to topics. However, the volumes do follow some natural groupings of chapters.

I would like to thank our authors and readers for their contributions and their commitment in making this Handbook a success. Thanks also to our publication administrator Mrs J. Spurr for her usual dedication and excellence and to Kluwer Academic Publishers (now Springer) for their continuing support for the Handbook.

Dov Gabbay King's College London

Logic	IT			
	Natural language processing	Program control spec- ification, verification, concurrency	Artificial in- telligence	Logic pro- gramming
Temporal logic	Expressive power of tense operators. Temporal indices. Sepa- ration of past from future	Expressive power for re- current events. Specification of tempo- ral control. Decision prob- lems. Model checking.	Planning. Time depen- dent data. Event calculus. Persistence through time— the Frame Problem. Tem- poral query language. temporal transactions.	Extension of Horn clause with time capability. Event calculus. Temporal logic programming.
Modal logic. Multi-modal logics	generalised quantifiers	Action logic	Belief revision. Inferential databases	Negation by failure and modality
Algorithmic proof	Discourse rep- resentation. Direct com- putation on linguistic input	New logics. Generic theo- rem provers	General theory of reasoning. Non-monotonic systems	Procedural approach to logic
Non- monotonic reasoning	Resolving ambigui- ties. Machine translation. Document classification. Relevance theory	Loop checking. Non-monotonic decisions about loops. Faults in systems.	Intrinsic logical discipline for AI. Evolving and com- municating databases	Negation by failure. Deduc- tive databases
Probabilistic and fuzzy logic	logical analysis of language	Real time sys- tems	Expert sys- tems. Machine learning	Semantics for logic programs
Intuitionistic logic	Quantifiers in logic	Constructive reasoning and proof theory about specifi- cation design	Intuitionistic logic is a better logical basis than classical logic	Horn clause logic is really intuitionistic. Extension of logic program- ming languages
Set theory, higher-order logic, $\lambda$ - calculus, types	Montague semantics. Situation semantics	Non-well- founded sets	Hereditary fi- nite predicates	$\lambda$ -calculus ex- tension to logic programs

Imperative vs. declar- ative lan- guages	Database theory	Complexity theory	Agent theory	Special com- ments: A look to the future
Temporal logic as a declarative programming language. The changing past in databases. The imperative future	Temporal databases and temporal transactions	Complexity questions of decision pro- cedures of the logics involved	An essential component	Temporal systems are becoming more and more so- phisticated and extensively applied
Dynamic logic	Database up- dates and action logic	Ditto	Possible ac- tions	Multimodal logics are on the rise. Quantification and context becoming very active
Types. Term rewrite sys- tems. Abstract interpretation	Abduction, rel- evance	Ditto	Agent's implementation rely on proof theory.	
	Inferential databases. Non-monotonic coding of databases	Ditto	Agent's rea- soning is non-monotonic	A major area now. Impor- tant for formal- ising practical reasoning
	Fuzzy and probabilistic data	Ditto	Connection with decision theory	Major area now
Semantics for programming languages. Martin-Löf theories	Database transactions. Inductive learning	Ditto	Agents con- structive reasoning	Still a major central alterna- tive to classical logic
Semantics for programming languages. Abstract in- terpretation. Domain recur- sion theory.		Ditto		More central than ever!

Classical logic. Classical frag- ments	Basic back- ground lan- guage	Program syn- thesis	A basic tool	
Labelled deductive systems	Extremely use- ful in modelling		A unifying framework. Context theory.	Annotated logic programs
Resource and substructural logics	Lambek calcu- lus		Truth maintenance systems	
Fibring and combining logics	Dynamic syn- tax	Modules. Combining languages	Logics of space and time	Combining fea- tures
Fallacy theory				
Logical Dynamics	Widely applied here			
Argumentation theory games		Game seman- tics gaining ground		
Object level/ metalevel			Extensively used in AI	
Mechanisms: Abduction, default relevance			ditto	
Connection with neural nets				
Time-action- revision mod- els			ditto	

	Relational databases	Logical com- plexity classes	The workhorse of logic	The study of fragments is very active and promising.
	Labelling allows for context and control.		Essential tool.	The new unify- ing framework for logics
Linear logic			Agents have limited resources	
	Linked databases. Reactive databases		Agents are built up of various fibred mechanisms	The notion of self-fibring al- lows for self- reference
				Fallacies are really valid modes of rea- soning in the right context.
			Potentially ap- plicable	A dynamic view of logic
				On the rise in all areas of applied logic. Promises a great future
			Important fea- ture of agents	Always central in all areas
			Very important for agents	Becoming part of the notion of a logic
				Of great im- portance to the future. Just starting
			A new theory of logical agent	A new kind of model